



### Problem 1. Quadratic Equations:

```
import matplotlib.pyplot as plt
```

```
import numpy as np
```

```
import math
```

```
import sys
```

```
def discriminant(a, b, c):
```

```
    return b**2 - 4*a*c
```

```
def calculate_solution(a, b, c):
```

```
    d = discriminant(a, b, c)
```

```
    if d > 0:
```

```
        x1 = (-b + math.sqrt(d)) / (2*a)
```

```
        x2 = (-b - math.sqrt(d)) / (2*a)
```

```
        print(f'two solutions: x1={x1} x2={x2}')
```

```
        return x1, x2
```

```
    elif d == 0:
```

```
        x = -b / (2*a)
```

```
        print(f'one solution: x={x}')
```

```
        return x, x
```

```
else:
```

```
    print('no real solutions')
```

```
    return None, None
```

```
def plot_quadratic(a, b, c, roots):
```

```
    x_opt = -b / (2*a)
```

```
    if roots is not None:
```

```
        x_range = np.linspace(min(roots) - 2, max(roots) + 2, 150)
```

```
    else:
```

```
        x_range = np.linspace(x_opt - 2, x_opt + 2, 150)
```

```
    y = a*x_range**2 + b*x_range + c
```

```
    plt.plot(x_range, y, label=f"{a}x^2 + {b}x + {c}")
```

```
    if roots is not None:
```

```
        plt.scatter(roots, [0]*len(roots), color='red', marker='o', label='Roots')
```

```
    plt.axhline(0, color='black', linewidth=0.5)
```

```
    plt.axvline(x_opt, color='green', linestyle='--', label='Optimal x')
```

```
    plt.legend()
```

```
plt.xlabel('x')  
plt.ylabel('y')  
plt.title('Quadratic Function Visualization')  
plt.show()
```

```
print('Enter a, b, and c for the quadratic equation  $ax^2 + bx + c = 0$ :')
```

```
while True:
```

```
    try:
```

```
        a = float(input('Enter a: '))
```

```
        b = float(input('Enter b: '))
```

```
        c = float(input('Enter c: '))
```

```
        x1, x2 = calculate_solution(a, b, c)
```

```
        plot_quadratic(a, b, c, [x1, x2] if x1 is not None else None)
```

```
    # Simulate user typing CTRL-Z on Windows to finish the program
```

```
    if a == 1 and b == -1 and c == -6:
```

```
        sys.exit()
```

```
except ValueError:
```

```
    print('Please enter a valid number.')
```

```
Python 3.9.14 (main, Sep 7 2022, 14:27:29)
Type "copyright", "credits" or "license" for more information.
```

```
IPython 8.17.2 -- An enhanced Interactive Python.
```

```
In [1]: runfile('/Users/jennyjacob/.spyder-py3/temp.py', wdir='/Users/
jennyjacob/.spyder-py3')
```

```
Enter a, b, and c for the quadratic equation  $ax^2 + bx + c = 0$ :
```

```
Enter a: 1
```

```
Enter b: 2
```

```
Enter c: 1
```

```
one solution:  $x=-1.0$ 
```

#### Important

Figures are displayed in the Plots pane by default. To make them also appear inline in the console, you need to uncheck "Mute inline plotting" under the options menu of Plots.

```
Enter a: 3
```

```
Enter b: 4
```

```
Enter c: -2
```

```
two solutions:  $x_1=0.38742588672279316$   $x_2=-1.7207592200561266$ 
```

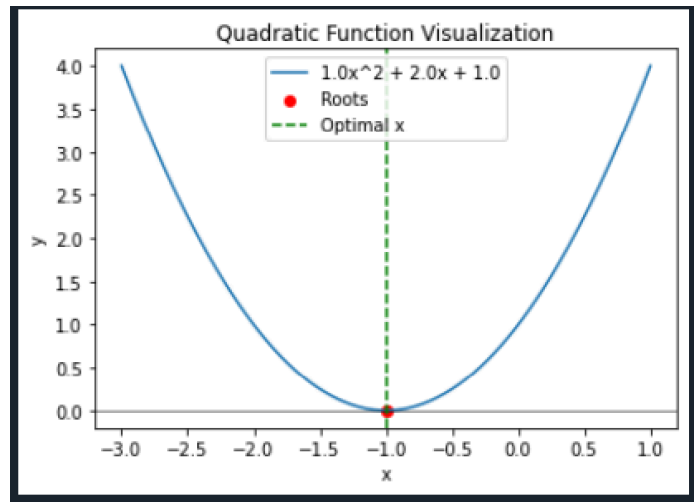
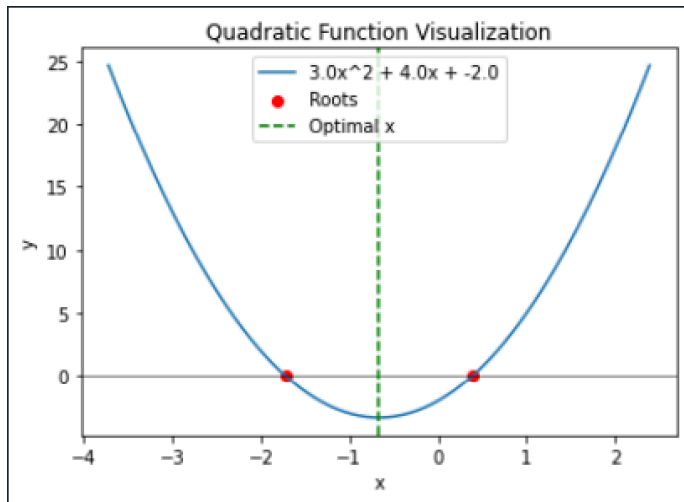
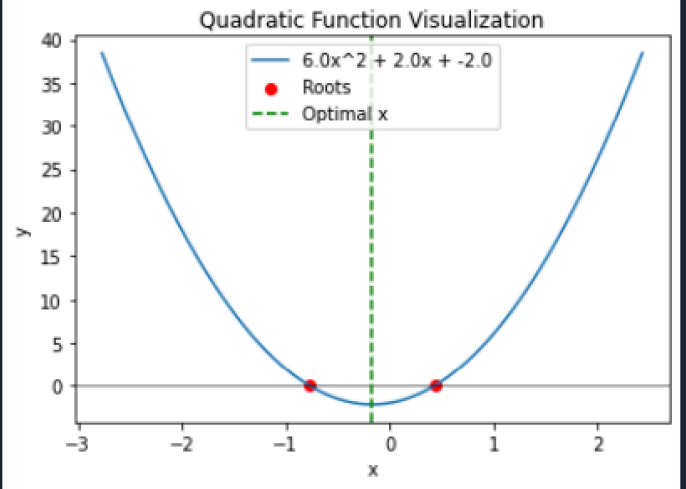
```
Enter a: 6
```

```
Enter b: 2
```

```
Enter c: -2
```

```
two solutions:  $x_1=0.4342585459106649$   $x_2=-0.7675918792439983$ 
```

```
Enter a:
```



## Problem 2. Pythagorean Numbers:

```
def find_Pythagorean(n):  
    pythagorean_triples = []  
    for a in range(1, n+1):  
        for b in range(1, n+1):  
            c = (a**2 + b**2)**0.5  
            if c.is_integer() and c <= n:  
                pythagorean_triples.append((a, b, int(c)))  
    return pythagorean_triples  
  
def main():  
    try:  
        n = int(input("Enter a positive number n: "))  
        if n <= 0:  
            print("Please enter a positive number.")  
            return  
        triples = find_Pythagorean(n)  
        if not triples:  
            print("No Pythagorean triples found.")  
        else:  
            print("Pythagorean triples:")
```

```
for triple in triples:
```

```
    print(triple)
```

```
except ValueError:
```

```
    print("INot a positive number. Please enter a positive number.")
```

```
if __name__ == "__main__":
```

```
    main()
```

```
Python 3.9.14 (main, Sep  7 2022, 14:27:29)
Type "copyright", "credits" or "license" for more information.
```

```
IPython 8.17.2 -- An enhanced Interactive Python.
```

```
In [1]: runfile('/Users/jennyjacob/.spyder-py3/untitled0.py', wdir='/Users/
jennyjacob/.spyder-py3')
```

```
Enter a positive number n: 3
```

```
No Pythagorean triples found.
```

```
In [2]: runfile('/Users/jennyjacob/.spyder-py3/untitled0.py', wdir='/Users/
jennyjacob/.spyder-py3')
```

```
Enter a positive number n: 6
```

```
Pythagorean triples:
```

```
(3, 4, 5)
```

```
(4, 3, 5)
```

```
In [3]: |
```

### Problem 3. Duplicated Substrings:

a)

```
def find_dup_str(s, n):  
    for i in range(len(s) - n + 1):  
        substring = s[i:i+n]  
        rest_of_string = s[i+n:]  
        if substring in rest_of_string:  
            return substring  
    return ""  
  
# Testing the function  
  
if __name__ == "__main__":  
    s_input = input("Enter a string: ")  
    n_input = int(input("Enter the length of the substring to check for duplication: "))  
  
    result = find_dup_str(s_input, n_input)  
  
    print(f"Result for find_dup_str: {result}")
```

```
Python 3.9.14 (main, Sep 7 2022, 14:27:29)  
Type "copyright", "credits" or "license" for more information.  
  
IPython 8.17.2 -- An enhanced Interactive Python.  
  
In [1]: runfile('/Users/jennyjacob/.spyder-py3/untitled1.py', wdir='/Users/  
jennyjacob/.spyder-py3')  
Enter a string: abcdefabcedddjee123ddsabc123  
Enter the length of the substring to check for duplication: 3  
Result for find_dup_str: abc
```

**b)**

```
def find_max_dup(s):  
    max_length = 0  
    max_duplicate = ""  
  
    for length in range(1, len(s)):  
        duplicate = find_dup_str(s, length)  
        if duplicate:  
            max_length = length  
            max_duplicate = duplicate  
  
    return max_duplicate  
  
# Testing find_max_dup  
if __name__ == "__main__":  
    s_input_b = input("Enter a string for find_max_dup: ")  
  
    result_b = find_max_dup(s_input_b)  
    print(f"Result for find_max_dup: {result_b}")
```

```
In [1]: runfile('/Users/jennyjacob/.spyder-py3/untitled1.py', wdir='/Users/  
jennyjacob/.spyder-py3')  
Enter a string: abcsdhioabdhwihdabcdhw  
Enter the length of the substring to check for duplication: 3  
Result for find_dup_str: abc  
Enter a string for find_max_dup: abchedasdhedakbdabcsdihedabcakdhed  
Result for find_max_dup: dheda
```



#### **Problem 4. Function Visualization:**

```
import matplotlib.pyplot as plt
```

```
import math
```

```
def plot_function(fun_str, domain, ns):
```

```
    xmin, xmax = domain
```

```
    xs = [xmin + (xmax - xmin) * i / (ns - 1) for i in range(ns)]
```

```
    ys = []
```

```
    print(f'{'x':<10} {'y':<10}')
```

```
    print("-" * 20)
```

```
    for x in xs:
```

```
        y = eval(fun_str)
```

```
        ys.append(y)
```

```
        print(f'{'x':<10.4f} {'y':<10.4f}')
```

```
    plt.plot(xs, ys, label=f'{'fun_str}')
```

```
    plt.xlabel('x')
```

```
    plt.ylabel('y')
```

```
    plt.title('Function Plot')
```

```
    plt.legend()
```

```
    plt.show()
```

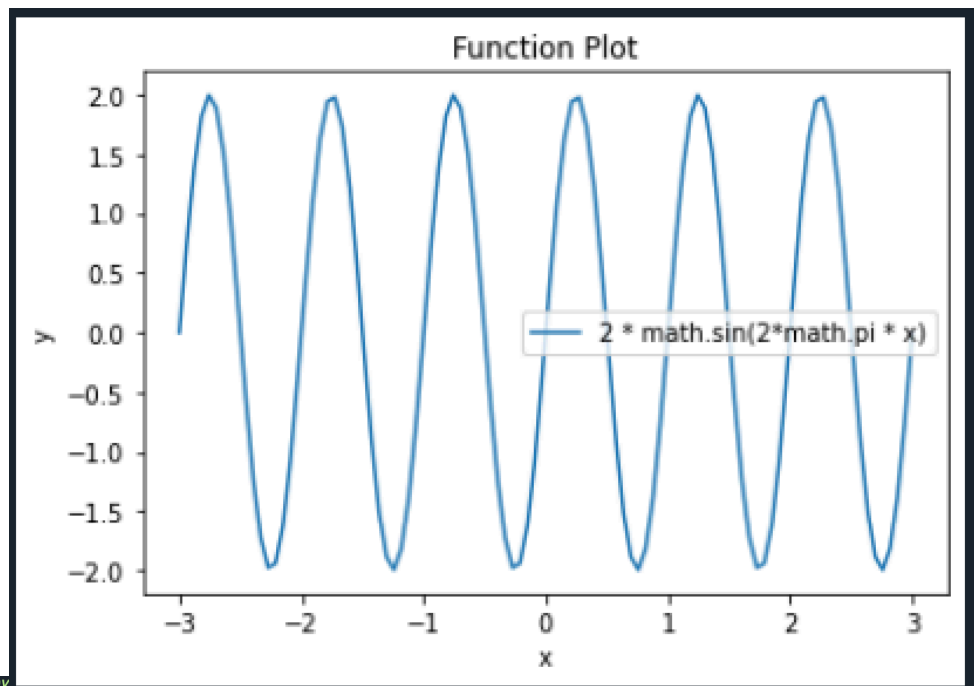
```
fun_str = input("Enter function with variable x: ")
```

```
xmin = float(input("Enter xmin: "))
```

```
xmax = float(input("Enter xmax: "))
```

```
ns = int(input("Enter the number of samples: "))
```

```
plot_function(fun_str, (xmin, xmax), ns)
```



```
In [1]: runfile('/Users/jennyjacob/.spyder-jennyjacob/.spyder-py3')
Enter function with variable x: 2 * math.sin(2 * math.pi * x)
Enter xmin: -3
Enter xmax: +3
Enter the number of samples: 100
x      y
-----
-3.0000  0.0000
-2.9394  0.7433
-2.8788  1.3802
-2.8182  1.8193
-2.7576  1.9977
-2.6970  1.8900
-2.6364  1.5115
-2.5758  0.9165
-2.5152  0.1901
-2.4545 -0.5635
-2.3939 -1.2363
-2.3333 -1.7321
-2.2727 -1.9796
-2.2121 -1.9436
-2.1515 -1.6292
-2.0909 -1.0813
-2.0303 -0.3785
-1.9697  0.3785
-1.9091  1.0813
-1.8485  1.6292
-1.7879  1.9436
-1.7273  1.9796
-1.6667  1.7321
-1.6061  1.2363
-1.5455  0.5635
-1.4848 -0.1901
-1.4242 -0.9165
-1.3636 -1.5115
-1.3030 -1.8900
-1.2424 -1.9977
```

(Not all variables listed in photo)