

# AI homework8

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## 1

we need to maximize the function

$$L = \prod_i^N \prod_j^N p(w_i, w'_j)^{c_{ij}(w_i, w'_j)}$$

$$\ln(L) = \ln(\sum_i \sum_j c_{ij} p(w_i, w'_j))$$

$$\ln(L) = \ln(\sum_i \sum_j c_{ij} \sum_k p(w_i, w'_j, z_k))$$

$$\ln(L) \geq \sum_i \sum_j c_{ij} \sum_k Q(z_k) \ln(p(w_i, w'_j, z_k)) - Const$$

$$\ln(L) \geq \sum_i \sum_j c_{ij} \sum_k Q(z_k) [\ln P(z_k) + \ln P(w_i|z_k) + \ln P(w'_j|z_k)] - Const$$

## 2

$$Q(z_k) = P(z_k|w_i, w'_j)$$

$$Q(z_k) = \frac{P(w_i, w'_j, z_k)}{P(w_i, w'_j)}$$

$$Q(z_k) = \frac{P(w_i, w'_j, z_k)}{\sum_k P(w_i, w'_j, z_k)}$$

$$Q(z_k) = \frac{P(z_k)P(w_i|z_k)P(w'_j|z_k)}{\sum_k P(z_k)P(w_i|z_k)P(w'_j|z_k)}$$