R Cookbook

by Paul Teetor

S Kwon, Department of Applied Statistics, Konkuk University shkwon0522@konkuk.ac.kr

Chapter 1 Getting Started and Help

This chapter sets the groundwork for the other chapters. It explains how to download, install, and run R.

1.1 Downloading and Installing R

Windows

- 1 Open http://www.r-project.org/ in your browser.
- 2 Click on CRAN? You'll see a list of mirror sites, organized by country.
- 3 Select a site near you.
- 4 Click on indows?under ownload and Install R?
- 5 Click on ase?
- 6 Click on the link for downloading the latest version of R (an .exe file).
- 7 When the download completes, double-click on the .exe file and answer the usual questions.

1.3 Entering Commands

```
• > 1+1
[1] 2
```

- > max(1,3,5)
 [1] 5
- > max(1,3,5)
 [1] 5

1.7 Getting Help on a Function

• Use **help** to display the documentation for the function:

```
> help(mean)
```

• Use args for a quick reminder of the function arguments:

```
> args(mean)
function (x, ...)
NULL
```

• Use example to see examples of using the function:

```
> example(mean)
mean> x <- c(0:10, 50)
mean> xm <- mean(x)
mean> c(xm, mean(x, trim = 0.10))
[1] 8.75 5.50
```

1.8 Searching the Supplied Documentation

- If you want to search the installed documentation for a keyword,
 - > help.search("pattern")
 - > ??pattern

1.9 Getting Help on a Package

- > help(package="tseries")
- > vignette()
 - > vignette(package="car")

1.11 Finding Relevant Functions and Packages

- Of the 2,000+ packages for R, you have no idea which ones would be useful to you.
 - Visit the list of task views at http://cran.r-project.org/web/views/.
 - Find and read the task view for your area, which will give you links to and descriptions of relevant packages.
 - Or visit http://rseek.org, search by keyword, click on the Task Views tab, and select an applicable task view.
 - Visit http://crantastic.org/ and search for packages by keyword.
 - To find relevant functions, visit http://rseek.org, search by name or keyword, and click on the Functions tab.

Some Basics

The recipes in this chapter lie somewhere between problem-solving ideas and tutorials.

2.1 Printing Something

- If you simply enter the variable name or expression at the command prompt, R will print its value.
- print function

```
> pi
[1] 3.141593
> sqrt(2)
[1] 1.414214
> print(pi)
[1] 3.141593
> print(sqrt(2))
[1] 1.414214
```

2.1 Printing Something

 Trying to print multiple items gives this mind-numbing error message:

```
> print("The zero occurs at", 2*pi, "radians.")
Error in print.default("The zero occurs at", 2 * pi,
"radians.") : unimplemented type 'character' in
'asLogical'
```

 The only way to print multiple items is to print them one at a time.

```
> print("The zero occurs at"); print(2*pi)
[1] "The zero occurs at"
[1] 6.283185
```

2.1 Printing Something

cat function

```
> fib <- c(0,1,1,2,3,5,8,13,21,34)
> cat("radians.", fib, "...\n")
radians. 0 1 1 2 3 5 8 13 21 34 ...
```

 A serious limitation, however, is that it cannot print compound data structures such as matrices and lists.

```
> cat(list("a","b","c"))
Error in cat(list(...), file, sep, fill, labels,
append) : argument 1 (type 'list') cannot be
handled by 'cat'
```

2.2 Setting Variables

 If you want to save a value in a variable, use the assignment operator < - or =.

```
> x <- 3
> y <- 4
> z <- sqrt(x^2 + y^2)
> z
[1] 5
```

2.3 Listing Variables

Is function

```
> x <- 10; y <- 50
> z <- c("three"); f <- function(a){a+1}
> ls()
[1] "f" "x" "y" "z"
```

• ls.str

```
> ls.str()
f : function (a)
x : num 10
y : num 50
z : chr "three"
```

2.4 Deleting Variables

• rm function.

```
> ls()
[1] "f" "x" "y" "z"
> rm(x)
> ls()
[1] "f" "y" "z"
> rm(list=ls())
> ls()
character(0)
```

2.5 Creating a Vector

• The c operator can construct a vector from simple elements:

```
> c(1,1,2,3,5,8,13,21)
[1] 1 1 2 3 5 8 13 21
> c(1*pi, 2*pi, 3*pi, 4*pi)
[1] 3.141593 6.283185 9.424778 12.566371
> c("Everyone", "loves", "stats.")
[1] "Everyone" "loves" "stats."
> c(TRUE,TRUE,FALSE,TRUE)
[1] TRUE TRUE FALSE TRUE
```

2.5 Creating a Vector

 If the arguments to c are themselves vectors, it flattens them and combines them into one single vector:

```
> v1 <- c(1, 2, 3); v2 <- c(4, 5, 6)
> c(v1, v2)
[1] 1 2 3 4 5 6
```

 Vectors cannot contain a mix of data types, such as numbers and strings.

```
> v1 <- c(1, 2); v3 <- c("A", "B")
> c(v1, v3)
[1] "1" "2" "A" "B"
```

2.5 Creating a Vector

 Technically speaking, two data elements can coexist in a vector only if they have the same mode.

```
> mode(3.1415)
[1] "numeric"
> mode("foo")
[1] "character"
```

 Those modes are incompatible. To make a vector from them, R converts 3.1415 to character mode so it will be compatible with "foo":

```
> c(3.1415, "foo")
[1] "3.1415" "foo"
> mode(c(3.1415, "foo"))
[1] "character"
```

2.6 Computing Basic Statistics

• Calculate basic statistics: mean, median, standard deviation, variance, correlation, or covariance.

```
> x <- c(0,1,1,2,3,5,8,13,21,34)
> mean(x)
[1] 8.8
> median(x)
[1] 4
> sd(x)
[1] 11.03328
> var(x)
[1] 121.7333
```

2.6 Computing Basic Statistics

cor and cov functions

```
> x <- c(0,1,1,2,3,5,8,13,21,34)
> y <- log(x+1)
> cor(x, y)
[1] 0.9068053
> cov(x, y)
[1] 11.49988
```

2.7 Creating Sequences

• n:m

```
> 1:5
[1] 1 2 3 4 5
> 5:1
[1] 5 4 3 2 1
```

• seq function

```
> seq(from=1, to=5, by=2)
[1] 1 3 5
```

• rep function

```
> rep(1, times=5)
[1] 1 1 1 1 1
```

2.7 Creating Sequences

 Alternatively, you can specify a length for the output sequence and then R will calculate the necessary increment:

```
> seq(from=0, to=20, length.out=5)
[1] 0 5 10 15 20
> seq(from=0, to=100, length.out=5)
[1] 0 25 50 75 100
> seq(from=1.0, to=2.0, length.out=5)
[1] 1.00 1.25 1.50 1.75 2.00
```

2.8 Comparing Vectors

R has two logical values, TRUE and FALSE.

```
> a <- 3
> pi
[1] 3.141593
> a == pi
[1] FALSE
> a == pi  # Test for equality
[1] FALSE
> a != pi  # Test for inequality
[1] TRUE
```

2.8 Comparing Vectors

More details: Read textbook!

```
> a < pi
[1] TRUE
> a > pi
[1] FALSE
> a <= pi
[1] TRUE
> a <= pi  # less or equal than
[1] TRUE
> a >= pi  # greater or eqaul than
[1] FALSE
```

2.9 Selecting Vector Elements

If you want to extract one or more elements from a vector,

```
> fib < c(0,1,1,2,3,5,8,13,21,34)
> fib
[1] 0 1 1 2 3 5 8 13 21 34
> fib[1]
Γ1<sub>1</sub> 0
> fib[4]
Γ11 2
> fib[4:9]  # Select elements 4 through 9
[1] 2 3 5 8 13 21
> fib[c(1,2,4,8)]
[1] 0 1 2 13
> fib[-1] # Ignore first element
[1] 1 1 2 3 5 8 13 21 34
```

2.9 Selecting Vector Elements

 By combining vector comparisons, logical operators, and vector indexing, you can perform powerful selections with very little R code:

```
> fib <- c(0,1,1,2,3,5,8,13,21,34)
> fib[fib>median(fib)]
[1] 5 8 13 21 34
> fib[(fib<quantile(fib,0.05))|(fib>quantile(fib,0.95))]
[1] 0 34
> fib[abs(fib-mean(fib))>2*sd(fib)]
[1] 34
```

2.10 Performing Vector Arithmetic

• If you want to operate on an entire vector at once,

```
> v \leftarrow c(11, 12, 13)
> w \leftarrow c(1, 2, 3)
> v+w
[1] 12 14 16
> v-w
[1] 10 10 10
> v*w
[1] 11 24 39
> v/w
[1] 11.000000 6.000000 4.333333
> w^v
[1] 1 4096 1594323
```

2.10 Performing Vector Arithmetic

 You can recenter an entire vector in one expression simply by subtracting the mean of its contents:

```
> w <- 1:5
> mean(w)
[1] 3
> w-mean(w)
[1] -2 -1 0 1 2
```

 Likewise, you can calculate the z-score of a vector in one expression: subtract the mean and divide by the standard deviation:

```
> w
[1] 1 2 3 4 5
> (w-mean(w))/sd(w)
[1] -1.2649111 -0.6324555 0.0000000 0.6324555
1.2649111
```

2.10 Performing Vector Arithmetic

vector-level operations

```
> sqrt(w)
[1] 1.000000 1.414214 1.732051 2.000000 2.236068
> log(w)
[1] 0.00000000 0.6931472 1.0986123 1.3862944
1.6094379
> sin(w)
[1] 0.8414710 0.9092974 0.1411200 -0.7568025
-0.9589243
```

2.12 Defining a Function

function

```
> cv <- function(x){sd(x)/mean(x)}
> cv(1:10)
[1] 0.5504819
> f.fun <- function(a,b){
+ if(b==0) return(a)
+ else return(a+1/b)
+ }
> f.fun(1,0)
[1] 1
> f.fun(1,1)
[1] 2
```

Chapter 3 Navigating the Software

There is nothing here about numerics, statistics, or graphics. This is all about dealing with R as software.

3.1 Getting and Setting the Working Directory

 Use getwd to report the working directory, and use setwd to change it:

```
> getwd()
[1] "C:/Users/User/Documents"
> setwd("Newfolder")
> getwd()
[1] "C:/Users/User/Documents/Newfolder"
```

3.2 Saving Your Workspace

• save.image function:

```
> save.image()
```

3.3 Viewing Your Command History

- up arrow or Ctrl-P or use the history function:
 - > history()
 - > history(100) # Show 100 most recent lines of history
 - > history(Inf) # Show entire saved history

3.4 Saving the Result of the Previous Command

 A special variable called .Last.value saves the value of the most recently evaluated expression.

```
> sqrt(2)
[1] 1.414214
> x <- .Last.value
> x
[1] 1.414214
```

3.5 Displaying the Search Path

search function

3.6 Accessing the Functions in a Package

• library function or the require function

 The detach function will unload a package that is currently loaded:

```
> detach(package:MASS)
> z <- lda(Sp ~ ., Iris, prior = c(1,1,1)/3)
Error: could not find function "lda"</pre>
```

3.7 Accessing Built-in Datasets

• You can use the built-in dataset called **pressure**:

 If you want to know more about pressure, use the help function to learn about it and other datasets:

```
> help(pressure)
```

3.7 Accessing Built-in Datasets

 You can see a table of contents for datasets by calling the data function with no arguments:

```
> data()
```

 MASS includes a dataset called Cars93, which you can access in this way:

```
> data(Cars93, package="MASS")
```

 After this call to data, the Cars93 dataset is available to you; then you can execute summary(Cars93), head(Cars93), and so forth.

```
> summary(Cars93)
```

> head(Cars93)

3.7 Accessing Built-in Datasets

 You can see a list of available datasets in MASS, or any other package, by using the data function with a package argument and no dataset name:

```
> data(package="MASS")
```

3.8 Viewing the List of Installed Packages

- library function
- installed.packages
 - > library()
 - > installed.packages()[,c("Package","Version")]

3.9 Installing Packages from CRAN

 Use the install.packages function, putting the name of the package in quotes:

```
> # Installing the package "ts"
> install.packages("ts")
```

3.12 Running a Script

source function

```
> source("hello.R")
[1] "Hello, World!"
```

• Setting echo=TRUE will echo the script lines before they are executed, with the R prompt shown before each line:

```
> source("hello.R", echo=TRUE)
> print("Hello, World!")
[1] "Hello, World!"
```

4.1 Entering Data from the Keyboard

Enter the data as literals using the c constructor for vectors:

```
> score <- c(61, 66, 90, 88, 100)
> score
[1] 61 66 90 88 100
```

 Alternatively, you can create an empty data frame and then invoke the built-in, spreadsheet-like editor to populate it:

```
> score <- data.frame() # Create empty data frame
> score <- edit(score) # Invoke editor, overwrite with edited data</pre>
```

4.1 Entering Data from the Keyboard

 The function data.frame works for data frames, too, by entering each variable (column) as a vector

```
> points <- data.frame(
+     label=c("Low", "Mid", "High"),
+     lbound=c(0, 0.67, 1.64),
+     ubound=c(0.674, 1.64, 2.33)
+     )
> points
label lbound ubound
1     Low     0.00     0.674
2     Mid     0.67     1.640
3     High     1.64     2.330
```

4.2 Printing Fewer Digits (or More Digits)

R normally formats floating-point output to have seven digits:

```
> pi
[1] 3.141593
> 100*pi
[1] 314.1593
```

 You can also alter the format of all output by using the options function to change the default for digits.

```
> options(digits=15)
> pi
[1] 3.14159265358979
```

4.2 Printing Fewer Digits (or More Digits)

 The print function lets you vary the number of printed digits using the digits parameter:

```
> print(pi, digits=4)
[1] 3.142
> print(100*pi, digits=4)
[1] 314.2
```

 Use the format function to format your numbers before calling cat:

```
> cat(pi, "\n")
3.141593
> cat(format(pi,digits=4), "\n")
3.142
```

4.2 Printing Fewer Digits (or More Digits)

Both print and format will format entire vectors at once:

```
> pnorm(-3:3)
[1] 0.001349898 0.022750132 0.158655254 0.500000000
[5] 0.841344746 0.977249868 0.998650102
> print(pnorm(-3:3), digits=3)
[1] 0.00135 0.02275 0.15866 0.50000 0.84134 0.97725
[7] 0.99865
```

 The print finds the number of digits necessary to format the smallest number and then formats all numbers to have the same width:

```
> q <- seq(from=0,to=3,by=0.5)
> tbl <- data.frame(Quant=q, Lower=pnorm(-q), Upper=pnorm(q))
> print(tbl) # Unformatted print
> print(tbl,digits=2) # Formatted print: fewer digits
```

4.3 Redirecting Output to a File

 You can redirect the output of the cat function by using its file argument:

```
> answer = 1e+10
> cat("The answer is", answer, "\n", file="output.txt")
> getwd()
```

 Use the sink function to begin redirecting all console output from both print and cat:

```
> sink("output.txt") # Redirect output to file
> cat(answer, file="output.txt")
> cat(answer, file="output.txt", append=TRUE)
> cat(answer, "\n", file="output.txt", append=TRUE)
> cat(answer, file="output.txt", append=TRUE)
> cat(answer, file="output.txt")
#> source("script.R") # Run the script, capturing its output
> sink() # Resume writing output to console
```

4.3 Redirecting Output to a File

 The file function opens a connection to a file and writing your output to the connection. If your are done use the close function to disconnect it:

```
> ?file
> con <- file("long_and_complex_name.txt", "w") # Open a connection
> cat(answer, file=con)
> cat(answer*100, file=con)
> cat(answer/100, file=con)
> close(con) # Close the connection
```

4.4 Listing Files

 The list.files function shows the contents of your working directory.

```
> list.files()
```

 To see all the files in your subdirectories, use recursive argument:

```
> list.files(recursive=TRUE)
```

 A possible "gotcha" of list.files is that it ignores hidden files and then try all.files argument:

```
> list.files(all.files=TRUE)
```

4.5 Dealing with "Cannot Open File"

• You can open data files by using many functions built in R but problems arise when the name contains backslashes (\):

```
> samp <- read.csv("C:\Data\sample-data.csv")
Error: '\D' is an unrecognized escape ...</pre>
```

Use forward slashes instead of backslashes:

```
> samp <- read.csv("C:/Data/sample-data.csv")
Error in file(file, "rt") : cannot open the connection
In addition: Warning message:
In file(file, "rt") :
cannot open file 'C:/Data/sample-data.csv': No such file or directory</pre>
```

An alternative solution is to double the backslashes:

```
> samp <- read.csv("C:\\Data\\sample-data.csv")
Error in file(file, "rt") : cannot open the connection
...</pre>
```

4.6 Reading Fixed-Width Records

 Suppose we want to read an entire file of fixed-width records in fixed-width.txt, shown here:

```
      Fisher
      R.A.
      1890
      1962

      Pearson
      Karl
      1857
      1936

      Cox
      Gertrude
      1900
      1978

      Yates
      Frank
      1902
      1994

      Smith
      Kirstine
      1878
      1939
```

 We need to know the column widths and use the read.fwf function:

```
> records <- read.fwf("fixed-width.txt", widths=c(10,10,5,4))
```

 The -1 in the widths argument says there is a one-character column that should be ignored:

```
> records <- read.fwf("fixed-width.txt", widths=c(6,-4,8,-2,4,-1,4))
```

4.6 Reading Fixed-Width Records

 R supplied some funky, synthetic column names. We can override that default by using a col.names argument.

 Here are records in statisticians.txt, using a space character between fields.

```
Fisher R.A. 1890 1962
Pearson Karl 1857 1936
Cox Gertrude 1900 1978
Yates Frank 1902 1994
Smith Kirstine 1878 1939
```

 The read.table function is built to read this file. By default, it assumes the data fields are separated by white space (blanks or tabs).

• If our file used colon (:) as the field separator, we would read it this way.

```
> dfrm <- read.table("statisticians-colon.txt") # not separated
> dfrm <- read.table("statisticians-colon.txt", sep=":") # separated</pre>
```

• Use the **str** function to see the class of the resulting column.

```
> str(dfrm)
'data.frame': 5 obs. of 4 variables:
$ V1: Factor w/ 5 levels "Cox", "Fisher",..: 2 3 1 5 4
$ V2: Factor w/ 5 levels "Frank", "Gertrude",..: 5 3 2 1 4
$ V3: int 1890 1857 1900 1902 1878
$ V4: int 1962 1936 1978 1994 1939
```

• Set the **stringsAsFactors** argument to FALSE:

```
> dfrm <- read.table("statisticians.txt", stringsAsFactor=FALSE)
> str(dfrm)
'data.frame': 5 obs. of 4 variables:
$ V1: chr "Fisher" "Pearson" "Cox" "Yates" ...
$ V2: chr "R.A." "Karl" "Gertrude" "Frank" ...
...
```

• Your data file might employ a different string to signal missing values, in which case use the **na.strings** argument:

 Any line that begins with a pound sign (#) is ignored, so you can put comments on those lines.

```
# This is a data file of famous statisticians.
# Last edited on 1994-06-18
lastname firstname born died
Fisher R.A. 1890 1962
Pearson Karl 1857 1936
Cox Gertrude 1900 1978
Yates Frank 1902 1994
Smith Kirstine 1878 1939
```

 Now we can tell read table that our file contains a header line, and it will use the column names when it builds the data frame.

```
> dfrm <- read.table("statisticians-header.txt", header=TRUE)
> print(dfrm)
lastname firstname born died
1 Fisher R.A. 1890 1962
2 Pearson Karl 1857 1936
3 Cox Gertrude 1900 1978
4 Yates Frank 1902 1994
5 Smith Kirstine 1878 1939
```

4.8 Reading from CSV Files

 The file table-data.csv includes a very simple comma-separated-values (CSV) where the first line is a header line that contains the column names, also separated by commas.

```
label,1bound,ubound
low,0,0.674
mid,0.674,1.64
high,1.64,2.33
```

The read.csv function can read CSV files.

```
> tbl <- read.csv("table-data.csv")
> str(tbl)
> tbl <- read.csv("table-data.csv", as.is=TRUE)
> str(tbl)
> tbl <- read.csv("table-data.csv", header=FALSE)
> str(tbl)
```

4.8 Reading from CSV Files

 The label variable in the tbl data frame just shown is actually a factor, not a character variable. You see that by inspecting the structure of tbl.

```
> str(tbl)
'data.frame': 3 obs. of 3 variables:
$ label : Factor w/ 3 levels "high","low","mid": 2 3 1
$ lbound: num 0 0.674 1.64
$ ubound: num 0.674 1.64 2.33
```

• In that case, set the as.is parameter to TRUE; this indicates that R should not interpret nonnumeric data as a factor.

```
> tbl <- read.csv("table-data.csv", as.is=TRUE)
> str(tbl)
'data.frame': 3 obs. of 3 variables:
$ label : chr "low" "mid" "high"
$ lbound: num 0 0.674 1.64
$ ubound: num 0.674 1.64 2.33
```

4.9 Writing to CSV Files

The write.csv function can write a CSV file.

```
> write.csv(x, file="filename", row.names=FALSE, col.names=TRUE)
```

4.10 Reading Tabular or CSV Data from the Web

 Use the read.csv, read.table, and scan functions, but substitute a URL for a file name.

```
> tbl <- read.csv("http://www.example.com/
+ download/data.csv")</pre>
```

 Remember that URLs work for FTP servers, not just HTTP servers. This means that R can also read data from FTP sites using URLs.

```
> tbl <- read.table("ftp://ftp.example.com/
+ download/data.txt")</pre>
```

4.11 Reading Data from HTML Tables

Use the readHTMLTable function in the XML package.

```
> library(XML)
> url <- 'http://www.example.com/data/table.html'
> tbls <- readHTMLTable(url)</pre>
```

• To read only specific tables, use the which parameter. This example reads the third table on the page.

```
> tbl <- readHTMLTable(url, which=3)
```

4.11 Reading Data from HTML Tables

 The following example, which is taken from the help page for readHTMLTable, loads all tables from the Wikipedia page entitled World population.

```
> library(XML)
> url <- 'http://en.wikipedia.org/wiki/
+ World_population'
> tbls <- readHTMLTable(url)</pre>
```

As it turns out, that page contains 17 tables.

```
> length(tbls)
[1] 17
```

• In this example we care only about the third table (which lists the largest populations by country), so we specify which=3.

```
> tbl <- readHTMLTable(url, which=3)</pre>
```

4.11 Reading Data from HTML Tables

 In that table, columns 2 and 3 contain the country name and population, respectively.

```
> tbl[,c(2,3)]
Country / Territory Population
  People's Republic of China[44] 1,338,460,000
                           India 1,182,800,000
3
                   United States
                                   309,659,000
4
                       Indonesia 231,369,500
5
                          Brazil 193,152,000
6
                        Pakistan
                                   169,928,500
7
                      Bangladesh
                                   162,221,000
8
                         Nigeria
                                   154,729,000
9
                          Russia
                                   141,927,297
10
                           Japan
                                   127,530,000
```

4.14 Saving and Transporting Objects

• Write the objects to a file using the save function.

```
> save(myData, file="myData.RData")
```

 Read them back using the load function, either on your computer or on any platform that supports R.

```
> load("myData.RData")
```

 The save function writes binary data. To save in an ASCII format, use dput or dump instead.

```
> dput(myData, file="myData.txt")
> dump("myData", file="myData.txt")
# Note quotes around variable name
```

4.14 Saving and Transporting Objects

- The first time I used load, I did this:
 - > myData <- load("myFile.RData")</pre>
 - # Achtung! Might not do what you think

4.14 Saving and Transporting Objects

 suppose we save the object in a file called z.RData. The following sequence of functions will create some confusion.

```
> load("z.RData")
# Create and populate the z variable
> plot(z)
# Does not plot what we expected: zoo pkg not loaded
```

 We should have loaded the zoo package before printing or plotting any zoo objects, like this:

```
> library(zoo) # Load the zoo package into memory
> load("z.RData")
# Create and populate the z variable
> plot(z) # Ahhh. Now plotting works correctly
```

6.1 Splitting a Vector into Groups

 Suppose x (vector) includes values that correspond groups in f (factor). You can use the split function:

```
> x = c(40,35,25,15,50,40,25,20)
> f = c("a","c","b","b","a","c","c","a")
> groups <- split(x, f)</pre>
```

Alternatively, you can use the unstack function:

```
> groups <- unstack(data.frame(x,f))</pre>
```

6.1 Splitting a Vector into Groups

 The Cars93 dataset contains a factor called textbfOrigin that has two levels, USA and non-USA. It also contains a column called MPG.city. We can split the MPG data according to origin as follows:

```
> library(MASS)
> split(Cars93$MPG.city, Cars93$Origin)
$USA

[1] 22 19 16 19 16 16 25 25 19 21 18 15 17 17 20 23 20 29 23 22 17 21 18 29 20

[26] 31 23 22 22 24 15 21 18 17 18 23 19 24 23 18 19 23 31 23 19 19 19 28

$non-USA

[1] 25 18 20 19 22 46 30 24 42 24 29 22 26 20 17 18 18 29 28 26 18 17 20 19 29

[26] 18 29 24 17 21 20 33 25 23 39 32 25 22 18 25 17 21 18 21 20
```

 Use either the lapply function or the sapply function, depending upon the desired form of the result. lapply always returns the results in list, whereas sapply returns the results in a vector if that is possible:

```
> lst <- lapply(lst, fun)
> vec <- sapply(lst, fun)</pre>
```

 Lets say I teach an introductory statistics class four times and administer comparable final exams each time. Here are the exam scores from the four semesters:

```
> scores
$S1
[1] 89 85 85 86 88 89 86 82 96 85 93 91 98 87 94 77 87 98 85 89
[21] 95 85 93 93 97 71 97 93 75 68 98 95 79 94 98 95
$S2
[1] 60 98 94 95 99 97 100 73 93 91 98 86 66 83 77
[16] 97 91 93 71 91 95 100 72 96 91 76 100 97 99 95
[31] 97 77 94 99 88 100 94 93 86
$53
[1] 95 86 90 90 75 83 96 85 83 84 81 98 77 94 84 89 93 99 91 77
[21] 95 90 91 87 85 76 99 99 97 97 97 93 96 90 87 97 88
$S4
[1] 67 93 63 83 87 97 96 92 93 96 87 90 94 90 82 91 85 93 83 90
[21] 87 99 94 88 90 72 81 93 93 94 97 89 96 95 82 97
```

• **length** function: **lapply** will return a list of lengths, and **sapply** will return a vector of lengths:

```
> lapply(scores, length)
$S1
Г1] 36
$$2
[1] 39
$S3
[1] 38
$S4
Γ11 36
> sapply(scores, length)
S1 S2 S3 S4
36 39 38 36
```

 We can see the mean and standard deviation of the scores just as easily:

 If the called function returns a vector, sapply will form the results into a matrix. The range function, for example, returns a two-element vector:

```
> sapply(scores, range)
S1    S2    S3    S4
[1,] 68    60    75    63
[2.] 98    100    99    99
```

6.3 Applying a Function to Every Row

• Use the **apply** function. Set the second argument to 1 to indicate row-by-row application of a function:

```
> results <- apply(mat, 1, fun) # mat is a matrix, fun is a function
```

- The apply function will call fun once for each row, assemble the returned values into a vector, and then return that vector.
- Suppose your matrix long is longitudinal data. Each row contains data for one subject, and the columns contain the repeated observations over time:

6.3 Applying a Function to Every Row

 You could calculate the average observation for each subject by applying the mean function to the rows. The result is a vector:

6.3 Applying a Function to Every Row

In the vector case, apply assembles the results into a matrix.
 The range function returns a vector of two elements, the minimum and the maximum, so applying it to long produces a matrix:

6.4 Applying a Function to Every Column

• For a matrix, use the apply function.

```
> results <- apply(mat, 2, fun)
```

• For a data frame, use the lapply or sapply functions.

```
> lst <- lapply(dfrm, fun)
> vec <- sapply(dfrm, fun)</pre>
```

6.4 Applying a Function to Every Column

• You can use **lapply** and **sapply** to process the columns, as described in Recipe 6.2:

```
> lst <- lapply(dfrm, fun) # Returns a list
> vec <- sapply(dfrm, fun) # Returns a vector</pre>
```

• The function **fun** should expect one argument: a column from the data frame.

6.4 Applying a Function to Every Column

 I often use this recipe to check the types of columns in data frames. The **batch** column of this data frame seems to contain numbers:

 But printing the classes of the columns reveals it to be a factor instead:

```
> sapply(batches, class)
batch clinic dosage shrinkage
"factor" "factor" "integer" "numeric"
```

 use the tapply function, which will apply a function to each group of data:

```
> tapply(x, f, fun)
```

 Suppose I have a vector with the populations of the 16 largest cities in the greater Chicago metropolitan area, taken from the data frame called **suburbs**:

```
> attach(suburbs)
> pop
[1] 2853114 90352 171782 94487 102746 106221 147779 76031 70834
[10] 72616 74239 83048 67232 75386 63348 91452
```

• We can easily compute sums and averages for all the cities:

```
> sum(pop)
[1] 4240667
> mean(pop)
[1] 265041.7
```

What if we want the sum and average broken out by county?
 We will need a factor, say county, the same length as pop

```
county
```

```
[1] Cook Kenosha Kane Kane Lake(IN) Kendall DuPage Cook
[9] Will Cook Cook Lake(IN) Cook Cook Cook Lake(IL)
Levels: Cook DuPage Kane Kendall Kenosha Lake(IL) Lake(IN) Will
```

• This example shows summing the populations by county:

```
> tapply(pop,county,sum)

Cook DuPage kane Kendall Kenosha Lake(IL) Lake(IN) Will

3281966 147779 266269 106221 90352 91452 185794 70834
```

• The next example computes average populations by county:

```
> tapply(pop,county,mean)

Cook DuPage Kane Kendall Kenosha Lake(IL) Lake(IN) Will

468852.3 147779.0 133134.5 106221.0 90352.0 91452.0 92897.0 70834.0
```

 The function given to tapply should expect a single argument: a vector containing all the members of one group.
 A good example is the length function, which takes a vector parameter and returns the vectors length. Use it to count the number of data in each group; in this case, the number of cities in each county:

```
> tapply(pop,county,length)
Cook DuPage Kane Kendall Kenosha Lake(IL) Lake(IN) Will
7     1     2     1     1     2     1
```

 The by function collects the returned values into a list and returns the list:

```
> by(dfrm, fact, fun)
```

 Here, dfrm is the data frame, fact is the grouping factor, and fun is a function. The function should expect one argument, a data frame.

 Suppose you have a data frame from clinical trials, called trials, where the dosage was randomized to study its effect:

The data includes a factor for the subjects sex, so by can split
the data according to sex and call summary for the two
groups. The result is two summaries, one for men and one for
women:

> by(trials, trials\$sex, summary) trials\$sex: F sex pre dose1 dose2 post F:7 Min. :4.156 Min. :1.000 Min. :1.000 Min. :2.886 M:0 1st Qu.:4.409 1st Qu.:1.000 1st Qu.:1.000 1st Qu.:3.075 Median: 4.895 Median: 1.000 Median: 2.000 Median: 3.163 Mean :5.020 Mean :1.429 Mean :1.571 Mean :3.174 3rd Qu.:5.668 3rd Qu.:2.000 3rd Qu.:2.000 3rd Qu.:3.314 Max. :5.932 Max. :2.000 Max. :2.000 Max. :3.389 trials\$sex: M pre dose1 dose2 post sex F:0 Min. :3.998 Min. :1.000 Min. :1.000 Min. :3.738 M:9 1st Qu.:4.773 1st Qu.:1.000 1st Qu.:1.000 1st Qu.:3.800 Median: 5.110 Median: 2.000 Median: 1.000 Median: 4.194 Mean :5.189 Mean :1.556 Mean :1.444 Mean :4.148 3rd Qu.:5.828 3rd Qu.:2.000 3rd Qu.:2.000 3rd Qu.:4.429 Max. :6.658 Max. :2.000 Max. :2.000 Max. :4.517

7.1 Getting the length of a string

- Use the nchar function, not the length function.
- The nchar function takes a string and returns the number of characters in the string:

```
> nchar("Moe")
[1] 3
> nchar("Curly")
[1] 5
```

 If you apply nchar to a vector of strings, it returns the length of each string:

```
> s <- c("Moe", "Larry", "Curly")
> nchar(s)
[1] 3 5 5
```

7.1 Getting the length of a string

When you apply the length function to a single string, R
returns the value 1 because it views that string as a singleton
vectora vector with one element:

```
> length("Moe")
[1] 1
> length(c("Moe","Larry","Curly"))
[1] 3
```

 The paste function creates a new string by joining the given strings end to end :

```
> paste("Everybody", "loves", "stats.")
[1] "Everybody loves stats."
```

• By default, paste inserts a single space between pairs of strings

```
> paste("Everybody", "loves", "stats.", sep="-")
[1] "Everybody-loves-stats."
> paste("Everybody", "loves", "stats.", sep="")
[1] "Everybodylovesstats."
```

 The function is very forgiving about nonstring arguments. It tries to convert them to strings using the as.character function:

```
> paste("The square root of twice pi is approximately", sqrt(2*pi))
[1] "The square root of twice pi is approximately 2.506628274631"
```

 If one or more arguments are vectors of strings, paste will generate all combinations of the arguments:

```
> stooges <- c("Moe", "Larry", "Curly")
> paste(stooges, "loves", "stats.")
[1] "Moe loves stats." "Larry loves stats." "Curly loves stats."
```

 The function is very forgiving about nonstring arguments. It tries to convert them to strings using the as.character function:

```
> paste("The square root of twice pi is approximately", sqrt(2*pi))
[1] "The square root of twice pi is approximately 2.506628274631"
```

 If one or more arguments are vectors of strings, paste will generate all combinations of the arguments:

```
> stooges <- c("Moe", "Larry", "Curly")
> paste(stooges, "loves", "stats.")
[1] "Moe loves stats." "Larry loves stats." "Curly loves stats."
```

 Sometimes you want to join even those combinations into one, big string. The collapse parameter lets you define a toplevel separator and instructs paste to concatenate the generated strings using that separator:

```
> paste(stooges, "loves", "stats", collapse=", and ")
[1] "Moe loves stats, and Larry loves stats, and Curly loves stats"
```

7.3 Extracting Substrings

 The substr function takes a string, a starting point, and an ending point. It returns the substring between the starting to ending points:

```
> substr("Statistics", 1, 4) # Extract first 4 characters
[1] "Stat"
> substr("Statistics", 7, 10) # Extract last 4 characters
[1] "tics"
```

7.3 Extracting Substrings

 Just like many R functions, substr lets the first argument be a vector of strings. In that case, it applies itself to every string and returns a vector of substrings:

```
> ss <- c("Moe", "Larry", "Curly")
> substr(ss, 1, 3) # Extract first 3 characters of each string
[1] "Moe" "Lar" "Cur"

> cities <- c("New York, NY", "Los Angeles, CA", "Peoria, IL")
> substr(cities, nchar(cities)-1, nchar(cities))
[1] "NY" "CA" "IL"
```

7.4 Splitting a String According to a Delimiter

 You want to split a string into substrings. The substrings are separated by a delimiter. → Use strsplit

```
> strsplit(string, delimiter)
```

7.4 Splitting a String According to a Delimiter

 It is common for a string to contain multiple substrings separated by the same delimiter. One example is a file path, whose components are separated by slashes (/):

```
> path <- "/home/mike/data/trials.csv"
```

 We can split that path into its components by using strsplit with a delimiter of /:

```
> strsplit(path, "/")
[[1]]
[1] "" "home" "mike" "data" "trials.csv"
```

7.4 Splitting a String According to a Delimiter

 Also notice that strsplit returns a list and that each element of the list is a vector of substrings.

```
> paths <- c("/home/mike/data/trials.csv",
+ "/home/mike/data/errors.csv",
+ "/home/mike/corr/reject.doc")
> strsplit(paths, "/")
[[1]]
[1] "" "home" "mike" "data" "trials.csv"
[[2]]
[1] "" "home" "mike" "data" "errors.csv"
[[3]]
[1] "" "home" "mike" "corr" "reject.doc"
```

7.5 Replacing Substrings

- Within a string, you want to replace one substring with another.
- → Use sub to replace the first instance of a substring:
- → Use gsub to replace all instances of a substring:

```
> sub(old, new, string)
> gsub(old, new, string)
```

 The sub function finds the first instance of the old substring within string and replaces it with the new substring:

```
with the new substring:
> s <- "Curly is the smart one. Curly is funny, too."
> sub("Curly", "Moe", s)
[1] "Moe is the smart one. Curly is funny, too."
```

7.5 Replacing Substrings

 gsub does the same thing, but it replaces all instances of the substring (a global replace), not just the first:

```
> gsub("Curly", "Moe", s)
[1] "Moe is the smart one. Moe is funny, too."
```

 To remove a substring altogether, simply set the new substring to be empty:

```
> sub(" and SAS", "", "For really tough problems, you need R and SAS.")
[1] "For really tough problems, you need R."
```

7.6 Seeing the Special Characters in a String

• In this example, the string seems to contain 13 characters but cat shows only a 6-character output:

```
> nchar(s)
[1] 13
> cat(s)
second
```

 The reason is that the string contains special characters, which are characters that do not display when printed. When we use print, it uses escapes (backslashes) to show the special characters:

```
> print(s)
[1] "first\rsecond\n"
```

7.7 Generating All Pairwise Combinations of Strings

 You have two sets of strings, and you want to generate all combinations from those two sets (their Cartesian product).

```
> m <- outer(strings1, strings2, paste, sep="")</pre>
```

7.7 Generating All Pairwise Combinations of Strings

 We can apply outer and paste to generate all combinations of test sites and treatments:

```
> outer(locations, treatments, paste, sep="-")
[,1] [,2] [,3]
[1,] "NY-T1" "NY-T2" "NY-T3"
[2,] "LA-T1" "LA-T2" "LA-T3"
[3,] "CHI-T1" "CHI-T2" "CHI-T3"
[4,] "HOU-T1" "HOU-T2" "HOU-T3"
```

7.7 Generating All Pairwise Combinations of Strings

 In the special case when you are combining a set with itself and order does not matter, the result will be duplicate combinations:

```
> outer(treatments, treatments, paste, sep="-")
[,1] [,2] [,3]
[1,] "T1-T1" "T1-T2" "T1-T3"
[2,] "T2-T1" "T2-T2" "T2-T3"
[3,] "T3-T1" "T3-T2" "T3-T3"
```

7.7 Generating All Pairwise Combinations of Strings

• The lower.tri function identifies that triangle, so inverting it identifies all elements outside the lower triangle:

```
> m <- outer(treatments, treatments, paste, sep="-")
> m[!lower.tri(m)]
[1] "T1-T1" "T1-T2" "T2-T2" "T1-T3" "T2-T3" "T3-T3"
```

7.8 Getting the Current Date

• You need to know todays date. \rightarrow The Sys.Date function returns the current date:

```
> Sys.Date()
[1] "2010-02-11"
> class(Sys.Date())
[1] "Date"
```

7.9 Converting a String into a Date

 This example shows the default format assumed by as.Date, which is the ISO 8601 standard format of yyyy-mm-dd:

```
> as.Date("2010-12-31")
[1] "2010-12-31"
```

 I often mistakenly try to convert the usual American date format (mm/dd/yyyy) into a Date object, with these unhappy results:

```
> as.Date("12/31/2010")
Error in charToDate(x) :
character string is not in a standard unambiguous format
```

• Here is the correct way to convert an American-style date:

```
> as.Date("12/31/2010", format="%m/%d/%Y")
[1] "2010-12-31"
```

7.10 Converting a Date into a String

 You want to convert a Date object into a character string, usually because you want to print the date. → Use either format or as.character:

```
> format(Sys.Date())
[1] "2010-04-01"
> as.character(Sys.Date())
[1] "2010-04-01"
```

 Both functions allow a format argument that controls the formatting. Use format="%m/%d/%Y" to get American-style dates, for example:

```
> format(Sys.Date(), format="%m/%d/%Y")
[1] "04/01/2010"
```

7.10 Converting a Date into a String

 Each two-letter combination of a percent sign (%) followed by another character has special meaning. Some common ones are:

```
%b; Abbreviated month name (Jan)
%B; Full month name (January)
%d; Day as a two-digit number
%m; Month as a two-digit number
%y; Year without century (0099)
%Y; Year with century
```

- You have a date represented by its year, month, and day. You want to merge these elements into a single Date object representation. → Use the ISOdate function:
- The result is a POSIXct object that you can convert into a Date object:

```
> ISOdate(year, month, day)
> as.Date(ISOdate(year, month, day))
```

 It is common for input data to contain dates encoded as three numbers: year, month, and day. The ISOdate function can combine them into a POSIXct object:

```
> ISOdate(2012,2,29)
[1] "2012-02-29 12:00:00 GMT"
```

 You can keep your date in the POSIXct format. However, when working with pure dates (not dates and times), I often convert to a Date object and truncate the unused time information:

```
> as.Date(ISOdate(2012,2,29))
[1] "2012-02-29"
```

Trying to convert an invalid date results in NA:

```
> ISOdate(2013,2,29) # Oops! 2013 is not a leap year
[1] NA
```

• ISOdate can process entire vectors of years, months, and days, which is quite handy for mass conversion of input data.

```
> years
[1] 2010 2011 2012 2013 2014
> months
[1] 1 1 1 1 1
> days
[1] 15 21 20 18 17
> ISOdate(years, months, days)
[1] "2010-01-15 12:00:00 GMT" "2011-01-21 12:00:00 GMT"
[3] "2012-01-20 12:00:00 GMT" "2013-01-18 12:00:00 GMT"
[5] "2014-01-17 12:00:00 GMT"
> as.Date(ISOdate(years, months, days))
[17] "2010-01-15" "2011-01-21" "2012-01-20" "2013-01-18" "2014-01-17"
```

 Purists will note that the vector of months is redundant and that the last expression can therefore be further simplified by invoking the Recycling Rule:

```
> as.Date(ISOdate(years, 1, days))
[1] "2010-01-15" "2011-01-21" "2012-01-20" "2013-01-18" "2014-01-17"
```

 This recipe can also be extended to handle year, month, day, hour, minute, and second data by using the ISOdatetime function (see the help page for details):

```
> ISOdatetime(year, month, day, hour, minute, second)
```

7.12 Getting the Julian Date

 Given a Date object, you want to extract the Julian datewhich is, in R, the number of days since January 1, 1970. → Either convert the Date object to an integer or use the *julian* function:

```
> d <- as.Date("2010-03-15")
> as.integer(d)
[1] 14683
> julian(d)
[1] 14683
attr(,"origin")
[1] "1970-01-01"
```

7.12 Getting the Julian Date

 A Julian date is simply the number of days since a more-or-less arbitrary starting point. In the case of R, that starting point is January 1, 1970, the same starting point as Unix systems. So the Julian date for January 1, 1970 is zero, as shown here:

7.13 Extracting the Parts of a Date

 Convert the Date object to a POSIXIt object, which is a list of date parts. Then extract the desired part from that list:

```
> d <- as.Date("2010-03-15")
> p <- as.POSIX1t(d)
> p$mday # Day of the month
[1] 15
> p$mon # Month (0 = January)
[1] 2
> p$year + 1900 # Year
[1] 2010
```

7.13 Extracting the Parts of a Date

The POSIXIt object represents a date as a list of date parts.
 Convert your Date object to POSIXIt by using the as.POSIXIt function, which will give you a list with these members:

```
sec ; Seconds (061)
min ; Minutes (059)
hour ; Hours (023)
mday ; Day of the month (131)
mon ; Month (011)
year ; Years since 1900
wday ; Day of the week (06, 0 = Sunday)
yday ; Day of the year (0365)
isdst ; Daylight savings time flag
```

7.13 Extracting the Parts of a Date

 Using these date parts, we can learn that April 1, 2010, is a Thursday (wday = 4) and the 91st day of the year (because yday = 0 on January 1):

```
> d <- as.Date("2010-04-01")
> as.POSIX1t(d)$wday
[1] 4
> as.POSIX1t(d)$yday
[1] 90
```

 A common mistake is failing to add 1900 to the year, giving the impression you are living a long, long time ago:

```
> as.POSIX1t(d)$year # Oops!
[1] 110
> as.POSIX1t(d)$year + 1900
[1] 2010
```

7.14 Creating a Sequence of Dates

 A typical use of seq specifies a starting date (from), ending date (to), and increment (by). An increment of 1 indicates daily dates:

```
> s <- as.Date("2012-01-01")
> e <- as.Date("2012-02-01")
> seq(from=s, to=e, by=1) # One month of dates

[1] "2012-01-01" "2012-01-02" "2012-01-03" "2012-01-04" "2012-01-05" "2012-01-06"

[7] "2012-01-07" "2012-01-08" "2012-01-09" "2012-01-10" "2012-01-11" "2012-01-12"

[13] "2012-01-13" "2012-01-14" "2012-01-15" "2012-01-16" "2012-01-17" "2012-01-18"

[19] "2012-01-19" "2012-01-20" "2012-01-21" "2012-01-22" "2012-01-23" "2012-01-24"

[25] "2012-01-25" "2012-01-26" "2012-01-27" "2012-01-28" "2012-01-29" "2012-01-30"

[31] "2012-01-31" "2012-02-01"
```

7.14 Creating a Sequence of Dates

 Another typical use specifies a starting date (from), increment (by), and number of dates (length.out):

```
> seq(from=s, by=1, length.out=7) # Dates, one week apart
[1] "2012-01-01" "2012-01-02" "2012-01-03" "2012-01-04" "2012-01-05" "2012-01-06"
[7] "2012-01-07"
```

• The increment (by) is flexible and can be specified in days, weeks, months, or years:

```
> seq(from=s, by="month", length.out=12) # First of the month for one year

[1] "2012-01-01" "2012-02-01" "2012-03-01" "2012-04-01" "2012-05-01" "2012-06-01"

[7] "2012-07-01" "2012-08-01" "2012-09-01" "2012-10-01" "2012-11-01" "2012-12-01"

> seq(from=s, by="3 months", length.out=4) # Quarterly dates for one year

[1] "2012-01-01" "2012-04-01" "2012-07-01" "2012-10-01"

> seq(from=s, by="year", length.out=10) # Year-start dates for one decade

[1] "2012-01-01" "2013-01-01" "2014-01-01" "2015-01-01" "2016-01-01" "2017-01-01"

[7] "2018-01-01" "2019-01-01" "2020-01-01" "2021-01-01"
```

7.14 Creating a Sequence of Dates

 Be careful with by="month" near month-end. In this example, the end of February overflows into March, which is probably not what you wanted:

```
> seq(as.Date("2010-01-29"), by="month", len=3)
[1] "2010-01-29" "2010-03-01" "2010-03-29"
```

9.1 Summarizing Your Data

summary function

9.1 Summarizing Your Data

```
> cars.list = as.list(cars)
  > summary(cars.list)
  > lapply(cars.list, summary)
  $speed
  Min. 1st Qu. Median Mean 3rd Qu.
                                   Max.
  4.0 12.0 15.0 15.4 19.0
                                     25.0
  $dist
  Min. 1st Qu. Median Mean 3rd Qu.
                                      Max.
  2.00 26.00 36.00 42.98 56.00 120.00
  $type
  Length
           Class
                      Mode
  50 character character
  $city
  Busan Daejon Seoul
  18
        13
              19
```

9.2 Calculating Relative Frequencies

 Identify the interesting observations by using a logical expression; then use the mean function to calculate the fraction of observations it identifies.

```
> x = runif(100,-1,2)
> mean(x > 0)
```

9.3 Tabulating Factors and Creating Contingency Tables

iris samples

?iris

```
data <- iris
a <- rep("y",100)
b \leftarrow rep("x",100)
ab <- rbind(a,b)
xy <- sample(ab,dim(data)[1])</pre>
data <- cbind(data,xy) # iris data with 2 factor variables</pre>
head(data)
     Sepal.Length Sepal.Width Petal.Length Petal.Width Species
                                                                      xy
           5.1
                        3.5
                                       1.4
                                                   0.2
                                                           setosa
                                                                       У
           4.9
                        3.0
                                      1.4
                                                   0.2
                                                           setosa
                                                                       x
3
           4.7
                        3.2
                                      1.3
                                                   0.2
                                                           setosa
           4.6
4
                        3.1
                                      1.5
                                                   0.2
                                                           setosa
5
           5.0
                        3.6
                                      1.4
                                                   0.2
                                                           setosa
                                                                       x
6
           5.4
                        3.9
                                      1.7
                                                   0.4
                                                           setosa
                                                                       y
```

9.3 Tabulating Factors and Creating Contingency Tables

```
table(data$xy)
y
78 72
table(data$Species, data$xy)
x y
setosa 20 30
versicolor 29 21
virginica 29 21
```

9.4 Testing Categorical Variables for Independence

 Use the table function to produce a contingency table from the two factors. Then use the summary function to perform a chi-squared test of the contingency table:

```
> summary(table(data$Species, data$xy))
Number of cases in table: 150
Number of factors: 2
Test for independence of all factors:
Chisq = 0.16, df = 2, p-value = 0.9231
```

9.5 Calculating Quantiles (and Quartiles) of a Dataset

 The quantile function can tell you which observation delimits the lower 5% of the data:

```
sam <- seq(0,1,length.out = 10^4)
vec <- sample(sam,1000)
> quantile(vec,0.05)
5%
0.04711971
> quantile(vec,c(0.05,0.95))
5% 95%
0.04711971 0.95460046
> quantile(vec)
0% 25% 50% 75% 100%
0.00110011 0.25817582 0.51705171 0.74597460 0.99849985
```

9.6 Inverting a Quantile

- Given an observation x from your data, you want to know its corresponding quantile. That is, you want to know what fraction of the data is less than x.
- Assuming your data is in a vector vec, compare the data against the observation and then use mean to compute the relative frequency of values less than x:

```
> a = mean(vec < 0.8)
> quantile(vec,a)
```

9.7 Converting Data to Z-Scores

• You want to calculate the corresponding z-scores for all data elements. (This is sometimes called normalizing the data.)

```
> cars = cars[c(1,2)]
> a = scale(cars$speed)
> b = (cars$speed-mean(cars$speed))/sd(cars$speed)
> plot(a,b)
> s.cars = scale(cars)
> a.cars = apply(cars,2,scale)
```

9.8 Testing the Mean of a Sample (t Test)

Apply the t.test function for one-sample t-test.

```
> x <- rnorm(50, mean=100, sd=15)
> t.test(x, mu=95)
One Sample t-test
data: x
t = 3.2832, df = 49, p-value = 0.001897
alternative hypothesis: true mean is not equal to 95
95 percent confidence interval:
97, 16167, 103, 98297
sample estimates:
mean of x
100.5723
> t.test(x. mu=100)
```

9.10 Forming a Confidence Interval for a Median

Wilcoxon rank sum and signed rank tests

```
> wilcox.test(x, conf.int=TRUE,mu=100)
Wilcoxon signed rank test with continuity correction
data: x
V = 559, p-value = 0.4515
alternative hypothesis: true location is not equal to 100
95 percent confidence interval:
94.56114 102.52374
sample estimates:
(pseudo)median
98.42834
```

9.11 Testing a Sample Proportion

prop.test

```
> prop.test(11, 20, 0.5, alternative="greater")
1-sample proportions test with continuity correction
data: 11 out of 20, null probability 0.5
X-squared = 0.05, df = 1, p-value = 0.4115
alternative hypothesis: true p is greater than 0.5
95 percent confidence interval:
0.3496150 1.0000000
sample estimates:
p
0.55
```

9.12 Forming a Confidence Interval for a Proportion

• Here, the number of observations is n = 9 and the number of successes is x = 6.

```
> prop.test(6, 9)
1-sample proportions test with continuity correction
data: 6 out of 9, null probability 0.5
X-squared = 0.4444, df = 1, p-value = 0.505
alternative hypothesis: true p is not equal to 0.5
95 percent confidence interval:
0.3091761 0.9095817
sample estimates:
p
0.6666667
```

9.13 Testing for Normality

shapiro.test function:

```
> shapiro.test(x)
```

Examples

```
x <- rnorm(50,0,1)
shapiro.test(x)
> shapiro.test(x)
Shapiro-Wilk normality test
data: x
W = 0.968, p-value = 0.192
```

• This example reports a p-value of 0.192 for x, which is large(normal).

9.13 Testing for Normality

Examples

```
y <- runif(50,0,1)
shapiro.test(y)
> shapiro.test(y)
Shapiro-Wilk normality test
data: y
W = 0.9498, p-value = 0.03361
```

• This example reports a p-value of 0.03361 for y, which is small(not normal).

9.14 Testing for Runs

 The tseries package contains the runs.test function, which checks a sequence for randomness.

```
> library(tseries)
> runs.test(as.factor(s))

• > library(tseries)
> s <- sample(c(0,1), 100, replace=T)
> runs.test(as.factor(s))
Runs Test
data: as.factor(s)
Standard Normal = 0.2175, p-value = 0.8279
alternative hypothesis: two.sided
```

9.15 Comparing the Means of Two Samples

• t.test function

```
> t.test(x,y)
```

> t.test(x,y,paired=TRUE)

9.15 Comparing the Means of Two Samples

Paired vs Not paired

- Paired: Randomly select one group of people. Give them the SAT test twice, once with morning coffee and once without morning coffee. For each person, we will have two SAT scores. These are paired observations.
- Not paired: Randomly select two groups of people. One group has a cup of morning coffee and takes the SAT test.
 The other group just takes the test. We have a score for each person, but the scores are not paired in any way.

9.15 Comparing the Means of Two Samples

Examples

```
x <- rnorm(50,0,1)
y <- runif(50,0,1)
> t.test(x,y)
Welch Two Sample t-test
data: x and v
t = -2.6841, df = 56.259, p-value = 0.009536
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
-0.7210333 - 0.1047653
sample estimates:
mean of x mean of y
0.0555821 0.4684814
```

9.15 Comparing the Means of Two Samples

```
> t.test(x,y,paired=TRUE)
Paired t-test
data: x and y
t = -2.7776, df = 49, p-value = 0.007739
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
-0.7116274 -0.1141713
sample estimates:
mean of the differences
-0.4128993
```

9.16 Comparing the Locations of Two Samples Nonparametrically

wilcox.test function

```
> wilcox.test(x, y, paired=TRUE)
```

• For unpaired observations, let paired default to FALSE:

```
> wilcox.test(x, y)
```

Example for x and y

```
> wilcox.test(x,y)
Wilcoxon rank sum test with continuity correction
data: x and y
W = 962, p-value = 0.04748
alternative hypothesis: true location shift is not equal to 0
```

9.17 Testing a Correlation for Significance

• coe.test function

```
> cor.test(x, y)
```

For nonnormal populations, use the Spearman method instead:

```
> cor.test(x, y, method="Spearman")
```

9.18 Testing Groups for Equal Proportions

• Use the prop.test function with two vector arguments:

```
> ns <- c(ns1, ns2, ..., nsN)
> nt <- c(nt1, nt2, ..., ntN)
> prop.test(ns, nt)
```

9.18 Testing Groups for Equal Proportions

```
> successes <- c(14,10)
> trials <- c(38,40)
> prop.test(successes, trials)
2-sample test for equality of proportions with continuity correction
data: successes out of trials
X-squared = 0.7872, df = 1, p-value = 0.3749
alternative hypothesis: two.sided
95 percent confidence interval:
-0.1110245 0.3478666
sample estimates:
prop 1 prop 2
0.3684211 0.2500000
```

9.19 Performing Pairwise Comparisons Between Group Means

 Use pairwise.t.test to perform the pairwise comparison of means:

```
> pairwise.t.test(x,f) # x contains the data, f is the grouping factor
```

Examples ; Using iris data

```
data <- iris
pairwise.t.test(data$Sepal.Length,data$Species)
> pairwise.t.test(data$Sepal.Length,data$Species)
Pairwise comparisons using t tests with pooled SD
data: data$Sepal.Length and data$Species
setosa versicolor
versicolor 1.8e-15 -
virginica < 2e-16 2.8e-09
P value adjustment method: holm
```

9.20 Testing Two Samples for the Same Distribution

ks.test function

```
> ks.test(x, y)
• x \leftarrow rnorm(50,0,1)
  y <- runif(50,0,1)
  > ks.test(x,y)
  Two-sample Kolmogorov-Smirnov test
  data: x and y
  D = 0.5, p-value = 4.808e-06
  alternative hypothesis: two-sided
```

10. Graphics

This chapter introduces the basics of "graphics".

- high-level graphics function
 plot, boxplot, hist, qqnorm, curve
- low-level graphics function
 - : points, lines, abline, segment, polygon, text

10.1 Plot

• If your data are held in two parallel vectors, x and y, then use them as arguments of plot.

```
> plot(x,y)
> plot(dfrm) # dfrm : dataframe
```

10.2 Adding a Title and Labels

- Use the main argument for a title.
- Use the xlab argument for an x-axis label.
- Use the *ylab* argument for a y-axis label.

```
> plot(x, main="The Title",
xlab="X-axis Label", ylab="Y-axis Label")
```

10.3 Adding a Grid

- Call plot with type="n" to initialize the graphics frame without displaying the data.
- Call the grid function to draw the grid.
- Call low-level graphics functions, such as points and lines, to draw the graphics overlaid on the grid.

```
> plot(x, y, type="n")
> grid()
> points(x, y)
```

10.1/2/3 Example

• 10.1/2/3 Example

```
par(mfrow=c(1,3))
plot(pressure)
plot(pressure,
main="relationship between temp and pres",
xlab="temperature(temp)",
ylab="pressure(pres)")
plot(pressure,
main="relationship between temp and pres",
xlab="temperature(temp)",
ylab="pressure(pres)",
type="n")
______
grid(); points(pressure)
```

10.4 Creating a Scatter Plot of Multiple Groups

• Use the pch argument of plot

```
> plot(x, y, pch=as.integer(f))
```

```
rm(list=ls()); dev.off()
par(mfrow=c(1,2))
iris = read.csv("C:\\Users\\pc\\Desktop\\Iris.csv",
header=TRUE, stringsAsFactor=FALSE)
with(iris, plot(Petal.Length, Petal.Width))
with(iris, plot(Petal.Length, Petal.Width, pch=1:3))
```

10.5 Adding a Legend

Legend for points

```
> legend(x, y, labels,
pch=c(pointtype1, pointtype2, ...))
```

Legend for lines according to line type

```
> legend(x, y, labels,
lty=c(linetype1, linetype2, ...))
```

Legend for lines according to line width

```
> legend(x, y, labels,
lwd=c(width1, width2, ...))
```

10.5 Adding a Legend

```
rm(list=ls()); dev.off()
f = factor(iris$Species)
with(iris, plot(Petal.Length, Petal.Width,
pch=as.integer(f)))
legend(1.5, 2.4, as.character(levels(f)),
pch=1:length(levels(f)))
```

10.6 Plotting the Regression Line of a Scatter Plot

abline function

```
> m <- lm(y ~ x)
> plot(y ~ x)
> abline(m)
```

```
##10.6 Example
rm(list=ls()); dev.off()
install.packages("faraway")
library(faraway)
data(strongx)
m = lm(crossx ~ energy, data=strongx)
plot(crossx ~ energy, data=strongx)
abline(m)
```

10.7 Plotting All Variables Against All Other Variables

Place your data in a data frame and then plot the data frame.
 R will create one scatter plot for every pair of columns.

```
> plot(dfrm)
```

```
rm(list=ls()); dev.off()
head(iris)
plot(iris[,1:4])
```

10.8 Creating One Scatter Plot for Each Factor Level

• Conditioning plot: coplot function

```
> coplot(y ~ x | f)
```

```
rm(list=ls()); dev.off()
install.packages("MASS")
data(Cars93, package="MASS")
coplot(Horsepower ~ MPG.city | Origin, data=Cars93)
```

10.9 Creating a Bar Chart

• barplot function

```
> barplot(c(height1, height2, ..., heightn))
```

```
rm(list=ls()); dev.off()
heights = tapply(airquality$Temp, airquality$Month, mean)
par(mfrow=c(1,2))
barplot(heights)
barplot(heights,
main="Mean Temp. by Month",
names.arg=c("May", "Jun", "Jul", "Aug", "Sep"),
ylab="Temp (deg. F)")
```

10.10 Adding Confidence Intervals to a Bar Chart

barplot2 function

```
> library(gplots)
> barplot2(x, plot.ci=TRUE, ci.l=lower, ci.u=upper)
```

```
rm(list=ls()); dev.off()
attach(airquality)
heights = tapply(Temp, Month, mean)
lower = tapply(Temp, Month,
function(v) t.test(v)$conf.int[1])
upper = tapply(Temp, Month,
function(v) t.test(v)$conf.int[2])
par(mfrow=c(1,2))
barplot(heights, plot.ci=TRUE, ci.l=lower, ci.u=upper)
barplot(heights, plot.ci=TRUE, ci.l=lower, ci.u=upper,
ylim=c(50,90), xpd=FALSE,
main="Mean Temp. By Month",
names.arg=c("May","Jun","Jul","Aug","Sep"),
-1-L-UT--- (J-- D)U)
```

10.11 Coloring a Bar Chart

Use the col argument of barplot

```
> barplot(heights, col=colors)
```

```
rm(list=ls()): dev.off()
attach(airquality)
heights = tapply(Temp, Month, mean)
rel.hts = rank(heights) / length(heights)
grays = gray(1 - rel.hts)
par(mfrow=c(1,2))
barplot(heights, col=grays)
rel.hts = (heights - min(heights))/
(max(heights) - min(heights))
barplot(heights, col=grays,
ylim=c(50,90), xpd=FALSE,
main="Mean Temp. By Month",
names.arg=c("May", "Jun", "Jul", "Aug", "Sep"),
vlab="Temp (deg. F)")
```

10.12 Plotting a Line from x and y Points

• Use the **plot** function with a plot type of "l".

```
> plot(x, y, type="1")
> plot(dfrm, type="1")
```

```
rm(list=ls()); dev.off()
par(mfrow=c(1,2))
plot(pressure)
plot(pressure, type="1")
```

10.13 Changing the Type, Width, or Color of a Line

- lty="solid" or lty=1 (default)
- Ity="dashed" or Ity=2
- Ity="dotted" or Ity=3
- lty="dotdash" or lty=4
- lty="longdash" or lty=5
- Ity="twodash" or Ity=6
- lty="blank" or lty=0 (inhibits drawing)

```
> plot(x, y, type="1", 1ty="")
```

10.13 Changing the Type, Width, or Color of a Line

```
rm(list=ls()); dev.off()
x = pressure$temperature
y = pressure$pressure
plot(x,y,type="l",lty=3,col="red")
```

10.14 Plotting Multiple Datasets

• Show multiple datasets in one plot

```
> xlim <- range(c(x1,x2))
> ylim <- range(c(y1,y2))
> plot(x1, y1, type="1", xlim=xlim, ylim=ylim)
> points(point.x, point.y, type="p")
```

```
rm(list=ls()); dev.off()
x = pressure$temperature
y = pressure$pressure
xlim = range(c(min(x),max(x)))
ylim = range(c(min(y),max(y)))
plot(x, y, type="l", xlim=xlim, ylim=ylim)
points(median(x), median(y),col="red",type="p")
```

10.15 Adding Vertical or Horizontal Lines

```
> abline(v=x) # Draw a vertical line at x
> abline(h=y) # Draw a horizontal line at y
```

```
rm(list=ls()); dev.off()
samp = rnorm(100)
plot(samp)
m = mean(samp)
abline(h=m)
stdevs = m + c(-2,-1,+1,+2)*sd(samp)
abline(h=stdevs, lty="dotted")
```

10.16 Creating a Box Plot

boxplot(x)

```
> boxplot(x)
```

```
rm(list=ls()); dev.off()
samp = rnorm(100)
boxplot(samp)
```

10.17 Creating One Box Plot for Each Factor Level

Use the boxplot function with a formula
 Here, x is the numeric variable and f is the factor.

```
> boxplot(x ~ f)

> plot(f, x)
```

```
rm(list=ls()); dev.off()
install.packages("MASS")
par(mfrow=c(1,2))
data(UScereal, package="MASS")
boxplot(sugars ~ shelf, data=UScereal)
data(UScereal, package="MASS")
boxplot(sugars ~ shelf, data=UScereal,
main="Sugar Content by Shelf",
xlab="Shelf", ylab="Sugar (grams per portion)")
```

10.18 Creating a Histogram

• Use **hist(x)**, where x is a vector of numeric values.

```
> hist(x)
```

```
rm(list=ls()); dev.off()
data(Cars93, package="MASS")
par(mfrow=c(1,3))
hist(Cars93$MPG.city)
hist(Cars93$MPG.city, 20)
hist(Cars93$MPG.city, 20,
main="City MPG (1993)", xlab="MPG")
```

10.19 Adding a Density Estimate to a Histogram

• Use the density function to approximate the sample density, then use lines to draw the approximation.

```
> hist(x, prob=T) # with probability scale
> lines(density(x)) # Graph the approximate density
```

```
rm(list=ls()); dev.off()
samp = rgamma(500, 2, 2)
hist(samp, 20, prob=T)
lines(density(samp))
```

10.20 Creating a Discrete Histogram

Use the table function to count occurrences.
 Then use the plot function with type="h" to graph the occurrances as a histogram.
 Here, x is a vector of discrete values.

```
> plot(table(x), type="h")
```

```
rm(list=ls()); dev.off()
par(mfrow=c(1,2))
x = sample(1:10,100,replace=T)
plot(table(x), type="h", lwd=5, ylab="Freq")
plot(table(x)/length(x), type="h", lwd=5, ylab="Freq")
```

10.21 Creating a Normal Quantile-Quantile (Q-Q) Plot

• qqnorm function, qqline

```
> qqnorm(x)
> qqline(x)
```

```
rm(list=ls()); dev.off()
par(mfrow=c(1,2))
data(Cars93, package="MASS")
qqnorm(Cars93$Price, main="Q-Q Plot: Price")
qqline(Cars93$Price)
qqnorm(log(Cars93$Price), main="Q-Q Plot: log(Price)")
qqline(log(Cars93$Price))
```

10.22 Creating Other Quantile-Quantile Plots

• Use abline to plot the diagonal line

```
> plot(qt(ppoints(y), 5), sort(y))
> abline(a=0, b=1)
```

```
rm(list=ls()); dev.off()
RATE = 1/10
N = 100
y = rexp(N, rate=RATE)
plot(qexp(ppoints(y), rate=RATE), sort(y))
abline(a=0, b=1)
plot(qexp(ppoints(y), rate=RATE), sort(y),
main="Q-Q Plot", xlab="Theoretical Quantiles",
ylab="Sample Quantiles")
abline(a=0, b=1)
```

10.23 Plotting a Variable in Multiple Colors

• Use the col argument of the plot function

```
> plot(x, col=colors)
```

```
rm(list=ls()); dev.off()
x = runif(100,-5,5)
colors = ifelse(x >= 0, "black", "gray")
plot(x, type='h', lwd=3, col=colors)
```

10.24 Graphing a Function

curve function

```
> curve(sin, -3, +3)
#Graph the sine function from -3 to +3
```

```
rm(list=ls()); dev.off()
par(mfrow=c(1,2))
curve(dnorm, -3.5, +3.5,
main="Std. Normal Density")
f = function(x) exp(-abs(x)) * sin(2*pi*x)
curve(f, -5, +5, main="Dampened Sine Wave")
```

10.25 Pausing Between Plots

```
    > par(ask=TRUE)
    > par(ask=FALSE)
    > par(mfrow=(c(N,M))
    # Divide the graphics window into N x M matrix.
```

```
rm(list=ls()); dev.off()
par(mfrow=c(2,2))
Quantile <- seq(from=0, to=1, length.out=30)
plot(Quantile, dbeta(Quantile, 2, 4),
type="l", main="First")
plot(Quantile, dbeta(Quantile, 4, 2),
type="l", main="Second")
plot(Quantile, dbeta(Quantile, 1, 1),
type="l", main="Third")
plot(Quantile, dbeta(Quantile, 0.5, 0.5),
type="l", main="Fourth")</pre>
```

10.27 Opening Additional Graphics Windows

- win.graph function
 - > win.graph()

10.28 Writing Your Plot to a File

• savePlot function

```
> savePlot(filename="filename.ext", type="type")
#type: "png","jpeg",and etc
```

10.29 Changing Graphical Parameters

 Use the par function, which lets you set values of global graphics parameters.

Parameter and type	Purpose
bg="color"	Background color
cex=number	Height of text and plotted points
col="color"	Default plotting color
lty="linetype"	Type of line: solid, dotted, dashed, etc
lwd=number	Line width: $1 = \text{normal}$, $2 = \text{thicker}$, etc.
mfcol(mfrow)=c(nr,nc)	plot matrix with nr(rows) and nc(columns)
pch=pointtype	Default point type

11. Linear Regression and ANOVA

• Simple linear regression

$$y_i = \beta_0 + \beta_1(1)x_i + \varepsilon_i$$

• Multiple linear regression

$$y_i = \beta_0 + \beta_1 u_i + \beta_2 v_i + \beta_3 w_i + \varepsilon_i$$

Linear Regression

Most of the information you need in regression is as follows.

- Is the model statistically significant?
 - : Check the F statistic at the bottom of the summary.
- Are the coefficients significant?
 - : Check the coefficient t statistics and p-values in the summary, or check their confidence intervals.
- Is the model useful?
 - : Check the R^2 near the bottom of the summary.
- Does the model fit the data well?
 - : Plot the residuals and check the regression diagnostics.
- Does the data satisfy the assumptions behind linear regression?
 - : Check whether the diagnostics confirm that a linear model is reasonable for your data.

11.1 Performing Simple Linear Regression

 The Im function performs a linear regression and reports the coefficients.

11.2 Performing Multiple Linear Regression

 Use the Im function. Specify the multiple predictors on the righthand side of the formula, separated by plus signs (+).

```
> fit2 = lm(mpg~ hp + wt , data = mtcars)
> summary(fit2)
Call:
lm(formula = mpg ~ hp + wt, data = mtcars)
Residuals:
Min 10 Median 30 Max
-3.941 -1.600 -0.182 1.050 5.854
Coefficients:
          Estimate Std. Error t value Pr(>|t|)
(Intercept) 37.22727    1.59879    23.285    < 2e-16 ***
       hp
wt
         -3.87783 0.63273 -6.129 1.12e-06 ***
Signif. codes: 0 *** 0.001 ** 0.01 * 0.05 . 0.1 1
Residual standard error: 2.593 on 29 degrees of freedom
Multiple R-squared: 0.8268, Adjusted R-squared: 0.8148
F-statistic: 69.21 on 2 and 29 DF, p-value: 9.109e-12
```

11.3 Getting Regression Statistics

- Save the regression model in a variable, say m.
 Then use functions to extract regression statistics and information below from the model.
 - anova(m) : ANOVA table
 - coefficients(m): Model coefficients
 - confint(m): Confidence intervals for the regression coefficients
 - deviance(m): Residual sum of squares
 - effects(m): Vector of orthogonal effects
 - fitted(m): Vector of fitted y values
 - residuals(m) : Model residuals
 - summary(m) : Key statistics, such as R^2 , the F statistic, and the residual standard error (σ)

11.4 Understanding the Regression Summary

Example

```
> summary(fit)
Call:
lm(formula = v.vec ~ x.vec)
Residuals:
Min 1Q Median 3Q
                             Max
-2.3651 -0.4036 0.3208 0.6613 1.1720
Coefficients:
Estimate Std. Error t value Pr(>|t|)
(Intercept) -0.7861 0.5418 -1.451 0.18485
       0.6850 0.1802 3.801 0.00523 **
x.vec
Signif. codes: 0 *** 0.001 ** 0.01 * 0.05 . 0.1 1
Residual standard error: 1.083 on 8 degrees of freedom
Multiple R-squared: 0.6436, Adjusted R-squared: 0.599
F-statistic: 14.45 on 1 and 8 DF, p-value: 0.005231
```

11.5 Performing Linear Regression Without an Intercept

You want to perform a linear regression, but you want to force the intercept to be zero.

```
• > fit = lm(y.vec^x.vec+0)
```

11.6 Performing Linear Regression with Interaction Terms

 The R syntax for regression formulas lets you specify interaction terms. The interaction of two variables, u and v, is indicated by separating their names with an asterisk (*). This corresponds to the model;

$$y_i = \beta_0 + \beta_1 u_i + \beta_2 v_i + \beta_3 u_i v_i + \varepsilon_i$$

, which includes the first-order interaction term $\beta_3 u_i v_i$.

> lm(y ~ u*v)

11.6 Performing Linear Regression with Interaction Terms

Example

```
> fit2 = lm(mpg~ hp + wt + hp*wt , data = mtcars)
> summary(fit2)
Call:
lm(formula = mpg ~ hp + wt + hp * wt, data = mtcars)
Residuals:
Min 10 Median 30 Max
-3.0632 -1.6491 -0.7362 1.4211 4.5513
Coefficients:
               Estimate Std. Error t value Pr(>|t|)
(Intercept) 49.80842 3.60516 13.816 5.01e-14 ***
hp -0.12010 0.02470 -4.863 4.04e-05 ***
wt
         -8.21662 1.26971 -6.471 5.20e-07 ***
hp:wt
         Signif. codes: 0 *** 0.001 ** 0.01 * 0.05 . 0.1 1
Residual standard error: 2.153 on 28 degrees of freedom
Multiple R-squared: 0.8848, Adjusted R-squared: 0.8724
F-statistic: 71.66 on 3 and 28 DF, p-value: 2.981e-13
```

Backward stepwise regression

```
> library(MASS)
> states = as.data.frame(state.x77[,c("Murder","Population","Illiteracy","Income","Frost")])
> full.model = lm(Murder ~ Population + Illiteracy + Income + Frost,data=states)
> reduced.model = step(full.model, direction = "backward")
```

Backward stepwise regression

```
Start: AIC=97.75
Murder ~ Population + Illiteracy + Income + Frost
Df Sum of Sq
                                                                      RSS
                                                                                                                  AIC
- Frost 1 0.021 289.19 95.753

- Income 1 0.057 289.22 95.759

<a href="mailto:roots"><a href="mailto:roots">
- Illiteracy 1 144.264 433.43 115.986
Step: AIC=95.75
Murder ~ Population + Illiteracy + Income
Df Sum of Sq RSS
                                                                                                                 AIC
- Income 1 1 <none>
                                                                                              0.057 289.25 93.763
- Illiteracy 1 236.196 525.38 123.605
Step: AIC=93.76
Murder ~ Population + Illiteracy
Df Sum of Sq RSS
                                                                                                                 AIC
<none> 289.25 93.763
- Population 1 48.517 337.76 99.516
- Illiteracy 1 299.646 588.89 127.311
```

Forward stepwise regression

```
> min.model = lm(Murder ~ 1,data=states)
> fw.model = step(min.model, direction="forward",
scope = (~ Population + Illiteracy + Income + Frost))
```

Forward stepwise regression

```
Start: AIC=131.59
Murder 1
Df Sum of Sq RSS
                           AIC
+ Illiteracy 1
                     329.98 337.76 99.516
+ Frost 1
+ Population 1
                  193.91 473.84 116.442
78.85 588.89 127.311
+ Income 1 35.35 632.40 130.875 <non> 667.75 131.594
Step: AIC=99.52
Murder ~ Illiteracy
Df Sum of Sq RSS AIC
+ Population 1 48.517 289.25 93.763
                 337.76 99.516
5.387 332.38 100.712
4.916 332.85 100.783
<none>
+ Frost
Step: AIC=93.76
Murder ~ Illiteracy + Population
Df Sum of Sq
                  RSS
                          AIC
```

11.8 Regressing on a Subset of Your Data

You want to fit a linear model to a subset of your data, not to the entire dataset.

```
> fit2 = lm(mpg~ hp + wt + hp*wt ,subset = 1:30, data = mtcars) #use only data[1:30]
  > summary(fit2)
  Call:
  lm(formula = mpg ~ hp + wt + hp * wt, data = mtcars, subset = 1:30)
  Residuals:
  Min 1Q Median 3Q Max
  -3.1320 -1.5636 -0.6691 1.4594 4.4220
  Coefficients:
  Estimate Std. Error t value Pr(>|t|)
  (Intercept) 49.380844 3.703071 13.335 3.91e-13 ***
             -0.121860 0.025383 -4.801 5.68e-05 ***
  hp
  wt -7.835597 1.356251 -5.777 4.38e-06 ***
            0.026710 0.007657 3.488 0.00175 **
  hp:wt
  Signif. codes: 0 *** 0.001 ** 0.01 * 0.05 . 0.1 1
  Residual standard error: 2.195 on 26 degrees of freedom
  Multiple R-squared: 0.8859, Adjusted R-squared: 0.8728
  F-statistic: 67.31 on 3 and 26 DF, p-value: 2.191e-12
```

11.9 Regressing on a Polynomial

 Use the poly(x,n) function in your regression formula to regress on an n-degree polynomial of x.

$$y_i = \beta_0 + \beta_0 x_i + \beta_2 (x_i)^2 + \beta_3 (x_i)^3 + \varepsilon_i$$

> lm(y.vec~poly(x.vec,3,raw=TRUE))

11.10 Regressing on Transformed Data

 You can embed the needed transformation inside the regression formula. If, for example, y must be transformed into log(y), then the regression formula becomes as follows.

```
> lm(log(y) ~x)
> Example
> x.vec = c(1.5, 2.1, 3.4, 6.4, 7.2, 16.1, 20.8, 30.7, 32.1, 42.1)
> y.vec = c(0.2,0.3,0.5,1.7,1.2,2.7,3.3,3.9,4.1,4.9)
> lm(log(y.vec)~x.vec)
Call:
lm(formula = log(v.vec) ~ x.vec)
Coefficients:
(Intercept) x.vec
-0.73993 0.06868
```

11.11 Finding the Best Power Transformation (Boxox Procedure)

boxcox

```
library(MASS)
x.vec = c(1.5,2.1,3.4,6.4,7.2,16.1,20.8,30.7,32.1,42.1)
y.vec = c(0.2,0.3,0.5,1.7,1.2,2.7,3.3,3.9,4.1,4.9)
m = lm(y.vec ~ x.vec)
boxcox(m)
```

11.12 Forming Confidence Intervals for Regression Coefficients

confint function

11.13 Plotting Regression Residuals

You want a visual display of your regression residuals.

```
m = lm(y.vec~x.vec)
plot(m,which=1)
```

11.14 Diagnosing a Linear Regression

You have performed a linear regression. Now you want to verify the model quality by running diagnostic checks.

 Start by plotting the model object, which will produce several diagnostic plots.

```
> m <- lm(y.vec ~ x.vec)
> plot(m)
```

11.15 Identifying Influential Observations

 The influence.measures function reports several useful statistics for identifying influential observations, and it flags the significant ones with an asterisk (*).
 Its main argument is the model object from your regression.

> influence.measures(m)

11.16 Testing Residuals for Autocorrelation (Durbinatson Test)

dwtest function

```
> library(lmtest)
> m <- lm(y.vec ~ x.vec) # Create a model object
> dwtest(m) # Test the model residuals
```

11.16 Testing Residuals for Autocorrelation (Durbinatson Test)

acf function

```
> acf(m) # Plot the ACF of the model residuals
```

11.17 Predicting New Values

• **predict** function

```
> m = lm(y.vec ~ x.vec)
> preds = data.frame(x.vec = 8)
> predict(m,newdata=preds)
     1
1.324312
```

11.18 Forming Prediction Intervals

• Use the predict function and specify interval="prediction"

```
> predict(m, newdata=preds, interval="prediction")
```

11.19 Logistic Regression

Model

$$y_i = \beta_0 + \beta_1 x_{1i} + \epsilon_i$$

$$i = 1, 2, \cdots, n$$

$$y_i = 1 \text{ or } 0$$

$$E(y) = \frac{\exp(\beta_0 + \beta_1 x)}{1 + \exp(\beta_0 + \beta_1 x)}$$

$$\log\left(\frac{E(y)}{1 - E(y)}\right) = \beta_0 + \beta_1 x$$

11.19 Logistic Regression

Example

```
> mydata = read.csv("https://stats.idre.ucla.edu/stat/data/binary.csv")
> mydata = mydata[,-4]
> head(mydata)
      admit gre
                  gpa
         380
              3.61
     1 660
             3.67
                                fit = glm(admit~gre+gpa.data=mvdata.familv="binomial")
    1 800 4.00
                                summary(fit)
    1 640 3.19
     0 520 2.93
         760 3.00
Coefficients:
Estimate Std. Error z value
                              Pr(>|z|)
(Intercept) -4.949378 1.075093 -4.604 4.15e-06 ***
            0.002691
                      0.001057 2.544 0.0109 *
gre
                      0.319586 2.361
                                          0.0182 *
gpa
            0.754687
hy.vec = predict(fit,mydata[,-1],type = "response")
hy.vec = ifelse(hy.vec>0.5,1,0)
t = table(mydata$admit,hy.vec)
1-sum(diag(t))/sum(t)
[1] 0.32
```