

# **NSC3270 / NSC5270**

# **Computational Neuroscience**

Tu/Th 9:35-10:50am  
Featheringill Hall 129

Professor Thomas Palmeri  
Professor Sean Polyn

## **For Today**

Required Video

**But what \*is\* a Neural Network?**

In-Class Python Code:

`ActivFuncs.py` or `ActivFuncs.ipynb`

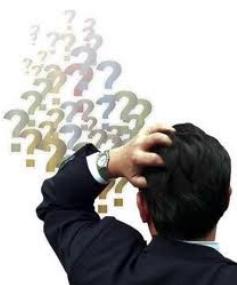
## **For Thursday**

Required Readings

Chapter 3 (selected pages) of Churchland, P.S., & Sejnowski, T.J. (2017). *The Computational Brain* (25th Anniversary Edition). MIT Press.

links on Brightspace

# At What Conceptual Levels of Analysis to Model?



## Computational Level

### NORMATIVE

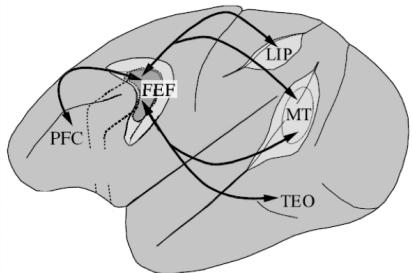
what are the goals of the organism  
what is optimal for survival

## Algorithmic/ Representational Level

### SOFTWARE

what kinds of representations and  
computations are performed

## Implementation/ Biophysical Level



### HARDWARE

how mechanisms are physically  
realized within a biological substrate  
(neurons and their connections)

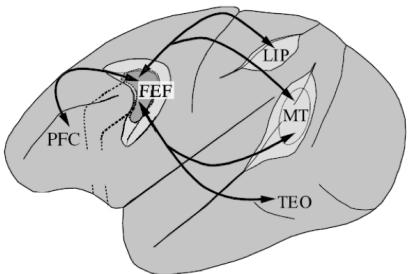
# At What Conceptual Levels of Analysis to Model?



**Computational  
Level**

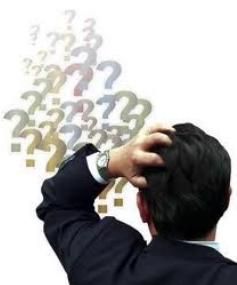
**Algorithmic/  
Representational  
Level**

**Implementation/  
Biophysical  
Level**



**BOTTOM UP APPROACH**  
how mechanisms are physically  
realized within a biological substrate  
(neurons and their connections)

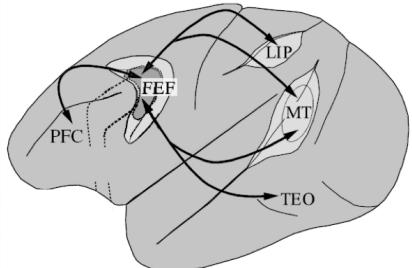
# At What Conceptual Levels of Analysis to Model?



## Computational Level

TOP DOWN APPROACH  
what are the goals of the organism  
what is optimal for survival

## Algorithmic/ Representational Level



## Implementation/ Biophysical Level



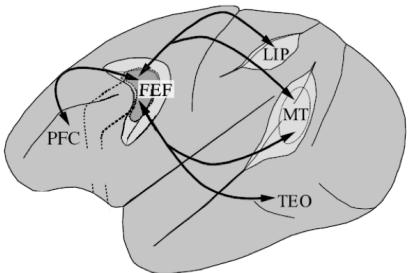
# At What Conceptual Levels of Analysis to Model?



## Computational Level

## Algorithmic/ Representational Level

## Implementation/ Biophysical Level



INSIDE OUT APPROACH  
what kinds of representations and computations are performed



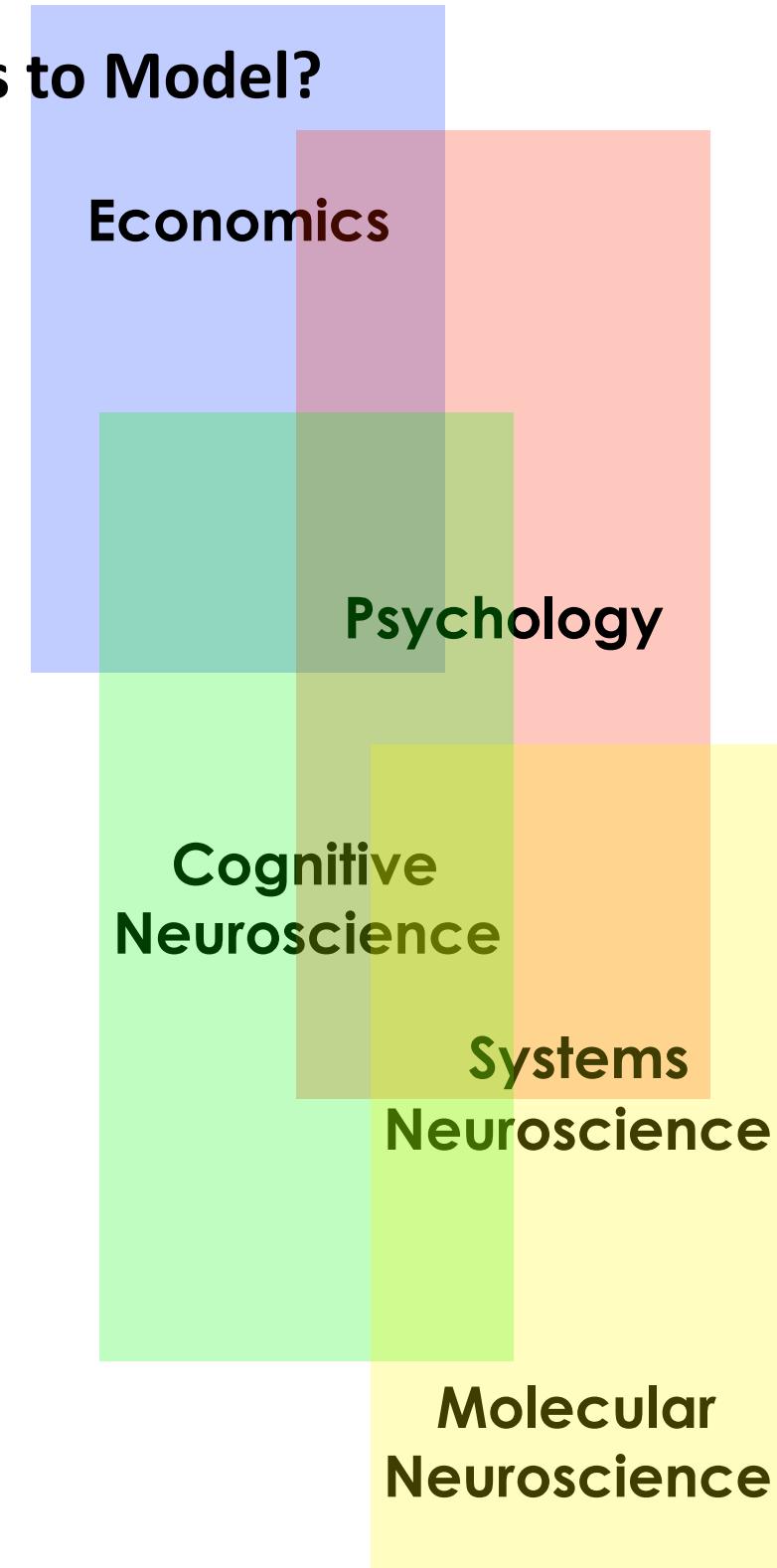
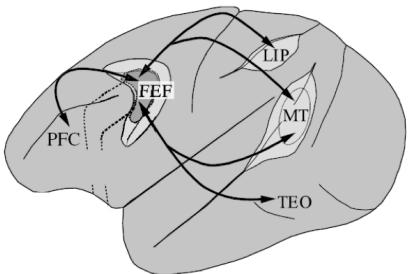
# At What Conceptual Levels of Analysis to Model?



**Computational  
Level**

**Algorithmic/  
Representational  
Level**

**Implementation/  
Biophysical  
Level**



# At What Conceptual Levels of Analysis to Model?



## Computational Level

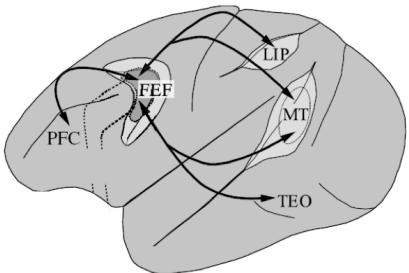
*What features is most informative in a large collection of images?*  
optimality, statistics, information theory

## Algorithmic/ Representational Level

*2nd derivative of a Gaussian smoothed image highlights edges in the image*  
image and signal processing

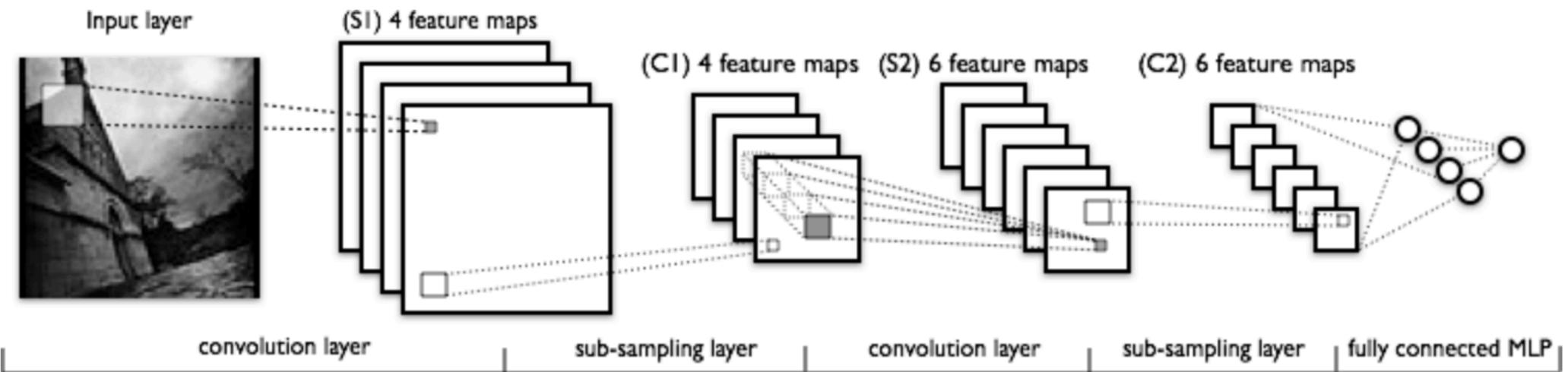
## Implementation/ Biophysical Level

*how do certain neurons in primary visual cortex (area V1) operate*  
spiking neural network models





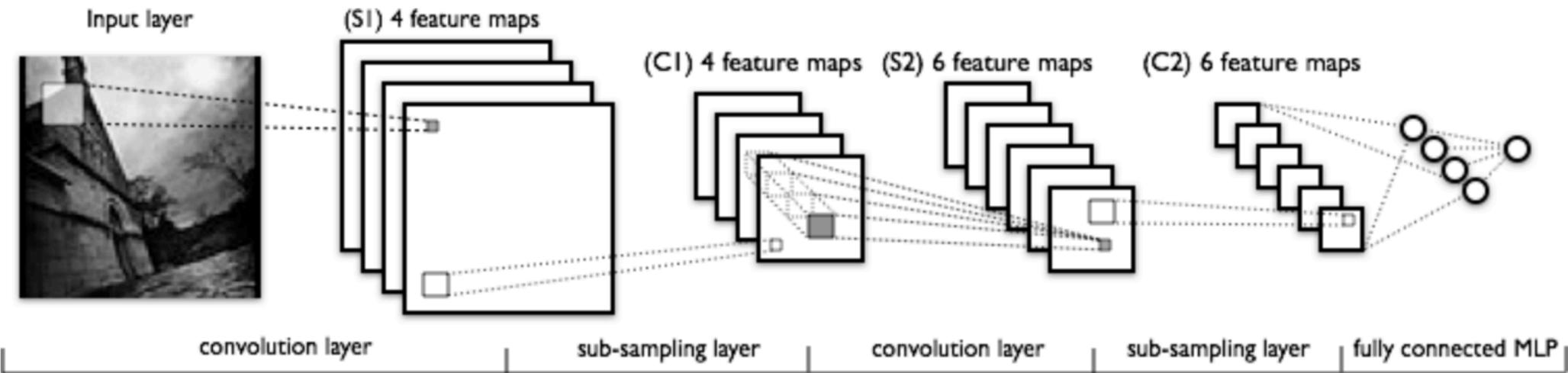
# Example Neural Network Model



LeNet-5

<http://yann.lecun.com/exdb/lenet/>

# Example Neural Network Model



## LeNet-5

<http://yann.lecun.com/exdb/lenet/>

- our focus is on using neural network models to explain behavior and the brain
- these models are now used in devices - speech recognition, image recognition, self-driving cars
- and used to analyze big, complex data

in Toronto, [Hinton] works out of Google's office downtown, which is filled with advertising employees. He's the only researcher. Occasionally, a curious employee sidles up and asks, "What do you do?"

"Do you have an Android phone?" Hinton replies.

"Yes."

"The speech recognition is pretty good, isn't it?"

"Yes."

"Well, I design the neural networks that recognize what you say."

The questioner nearly always pauses in thought.

"Wait, what do you mean?"



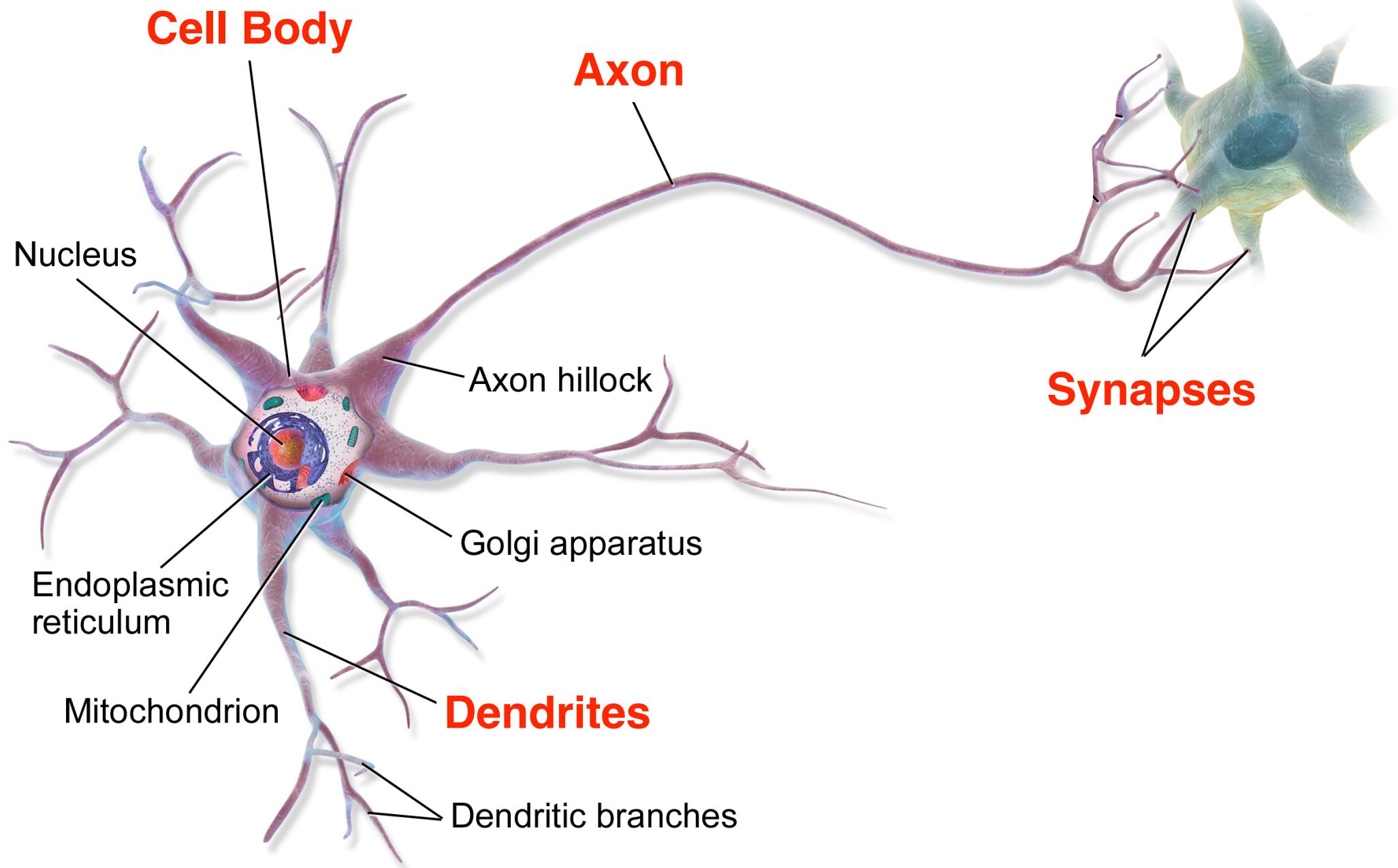
from *The Believers: The hidden story behind the code that runs our lives*  
by Paul Voosen, The Chronicle of Higher Education, Feb 23, 2015



# **Simple Models of Neurons**

# **brief overview/review of neuron structure and function**

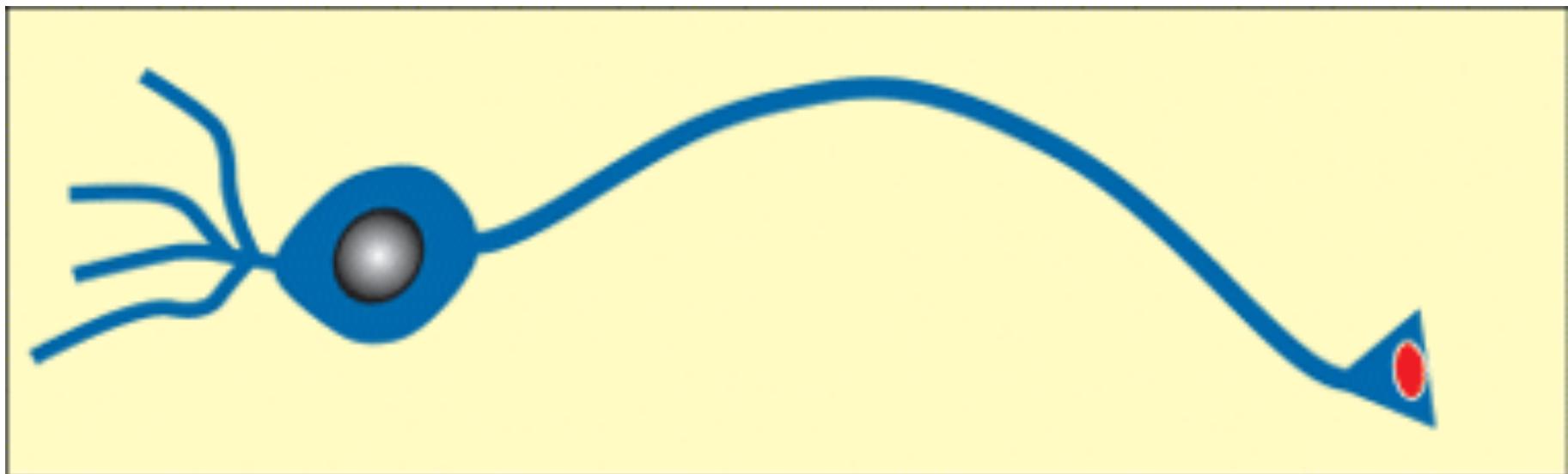
# Neuron

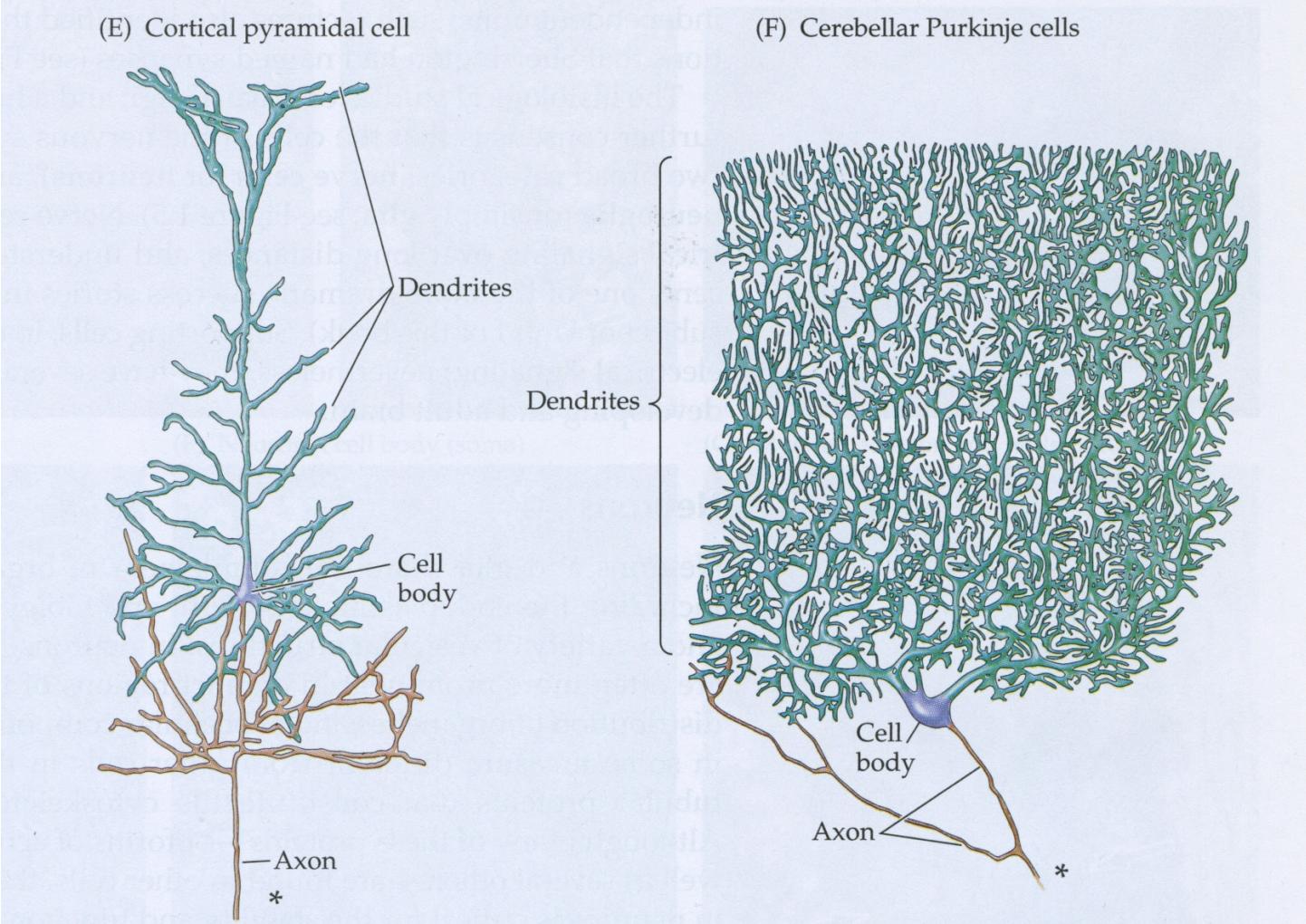
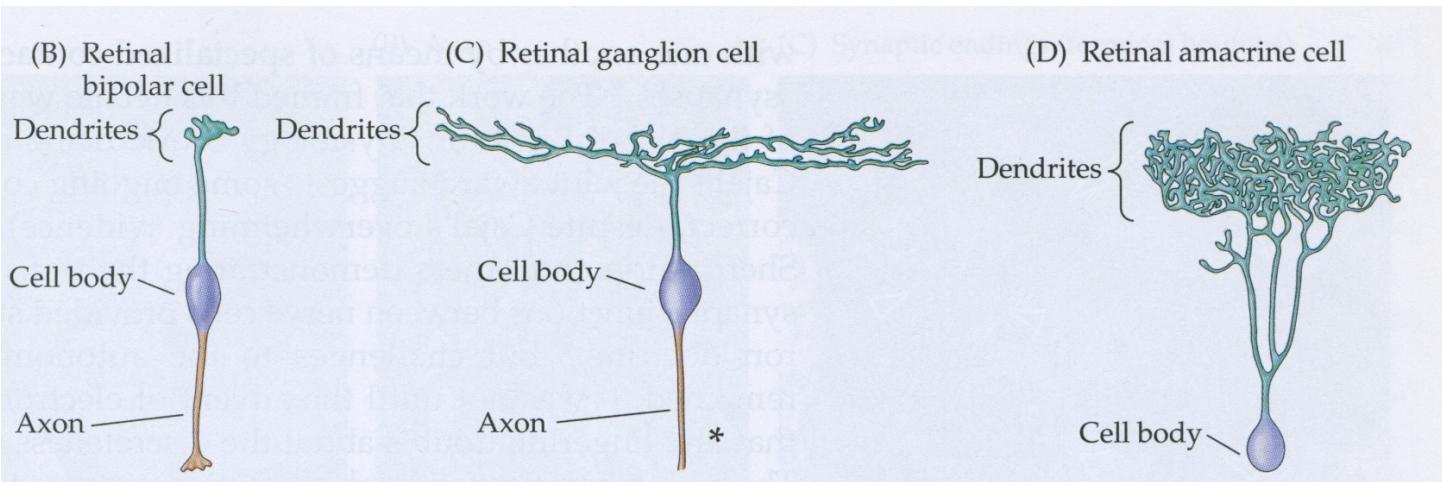


Dendrites Cell Body

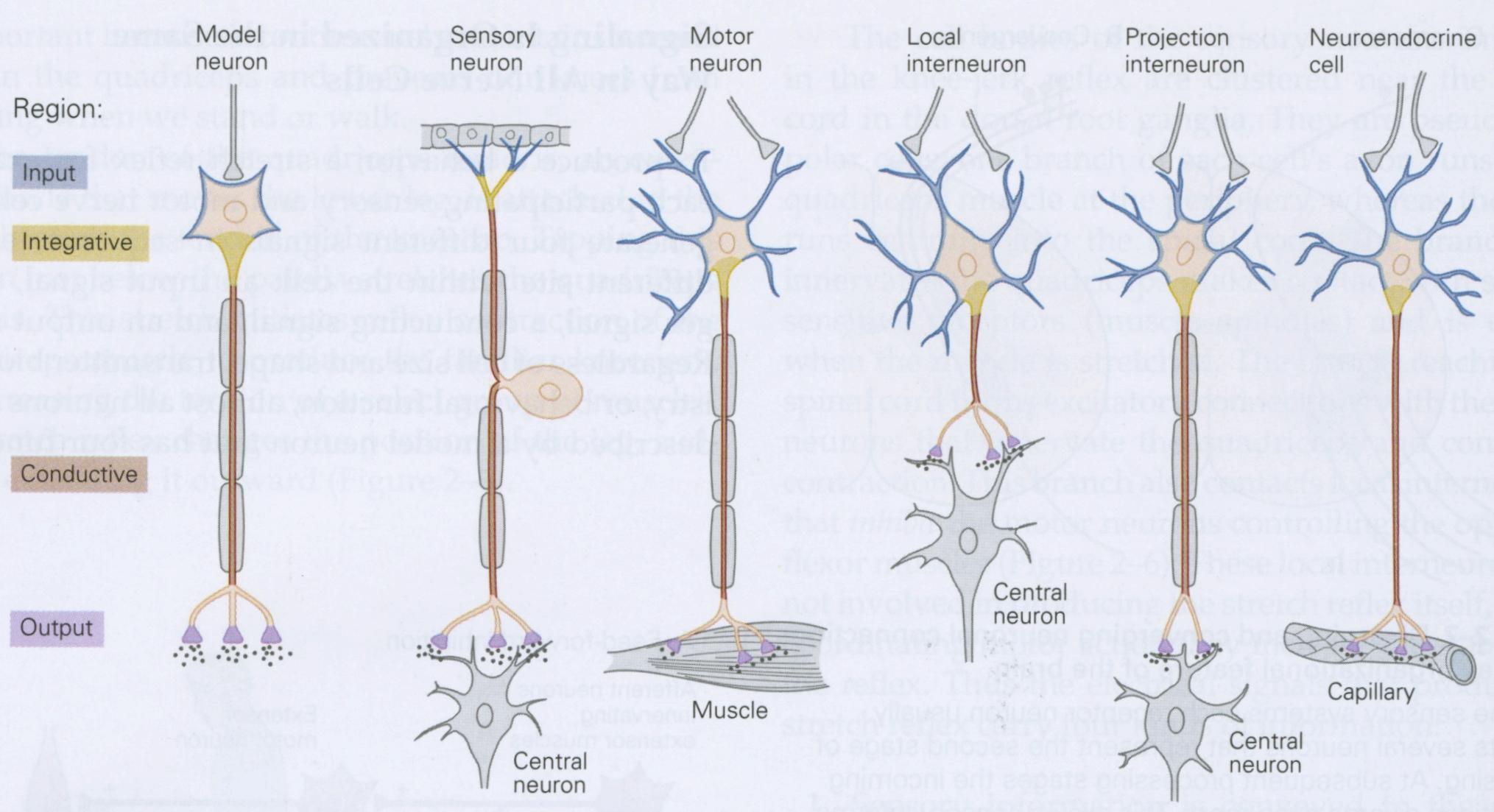
Axon

Synapses

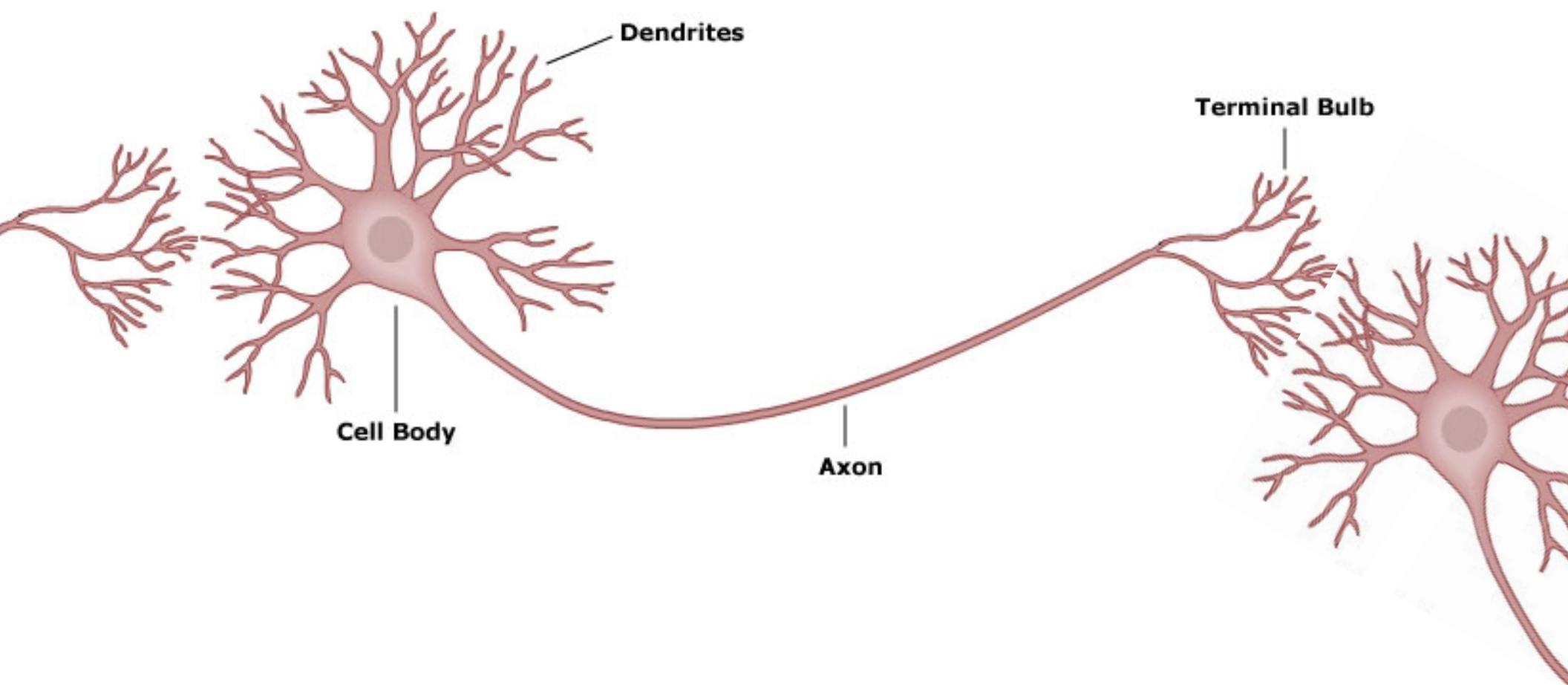


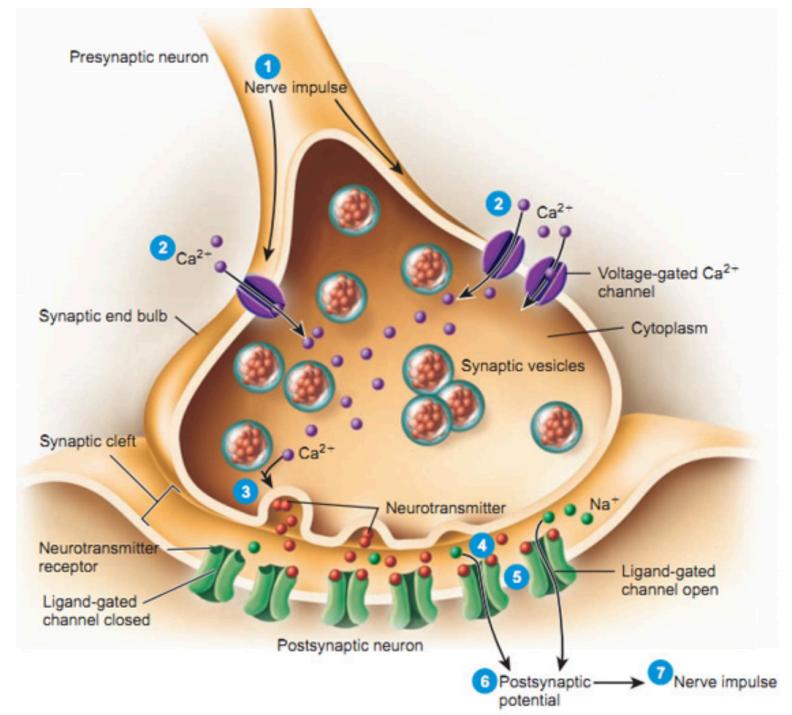
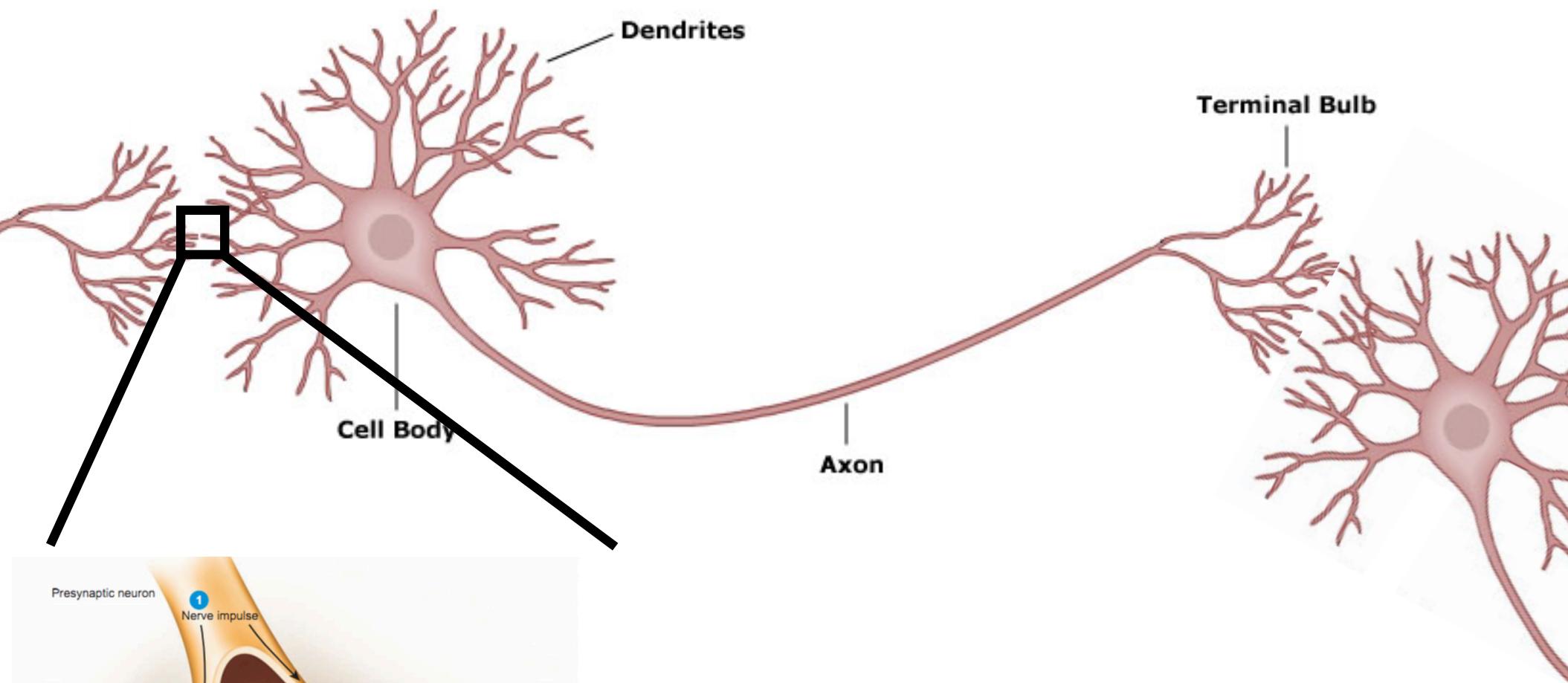


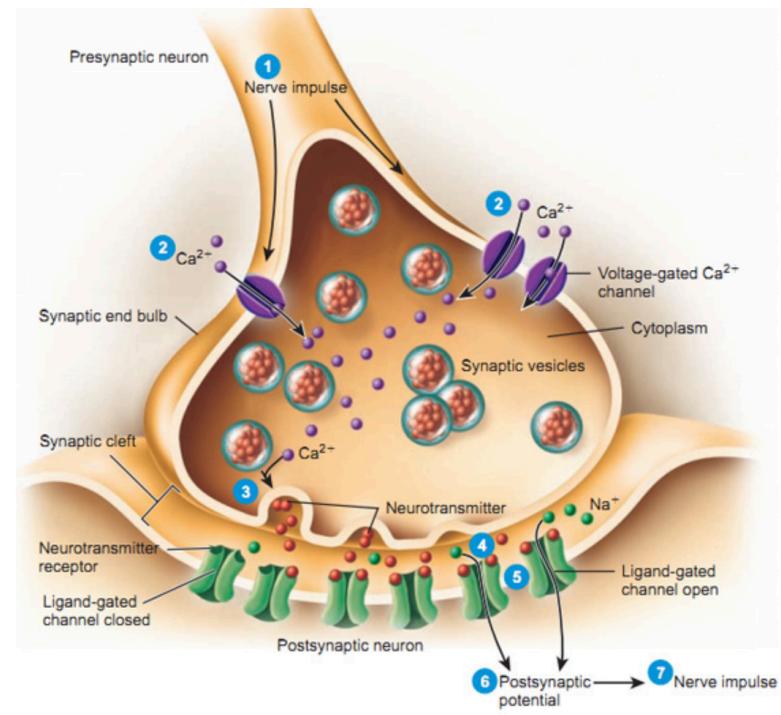
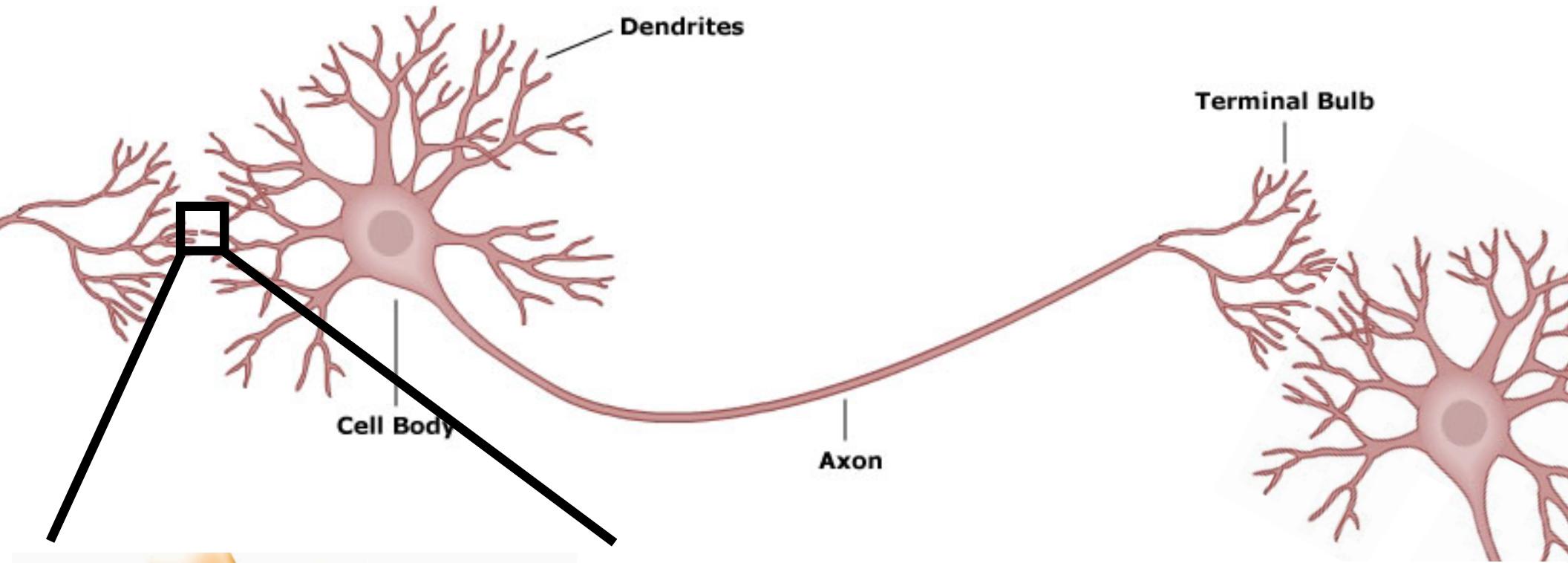
# functional similarities despite morphological differences



we will not discuss different types of neurons,  
but instead model idealized neurons

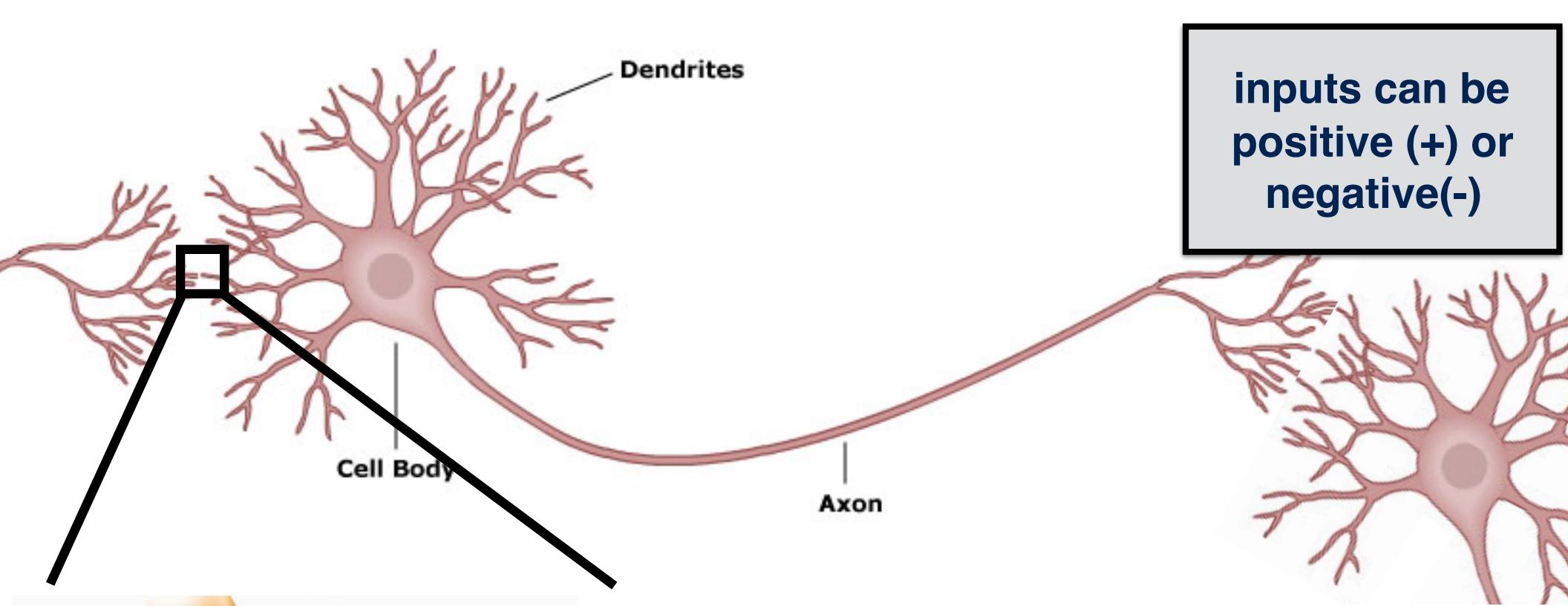




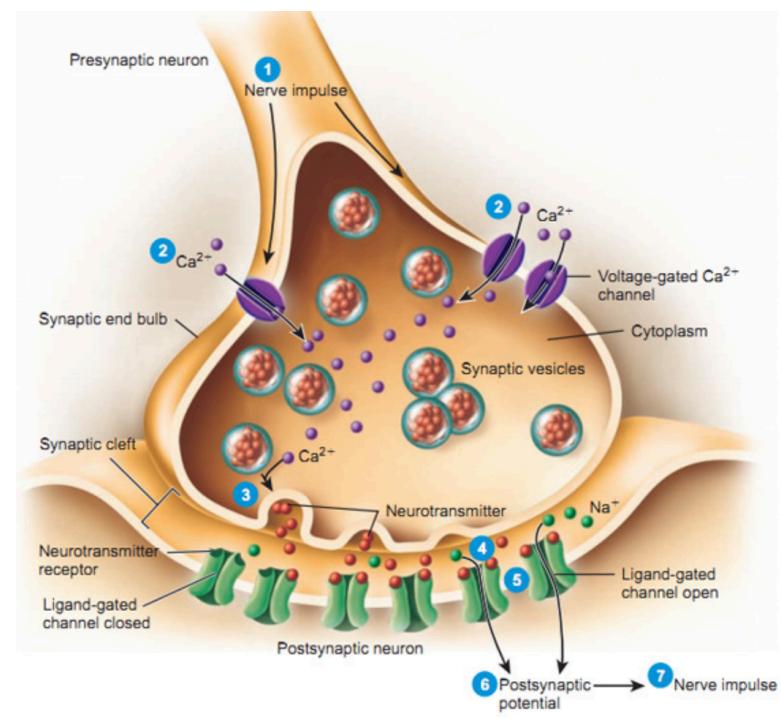


**EPSPs** (excitatory postsynaptic potentials)  
positive changes in membrane potential  
caused by excitatory pre-synaptic neurons  
(e.g., glutamate and NMDA receptors)

**IPSPs** (inhibitory postsynaptic potentials)  
negative changes in membrane potential  
caused by inhibitory pre-synaptic neurons  
(e.g., GABA and GABA receptors)

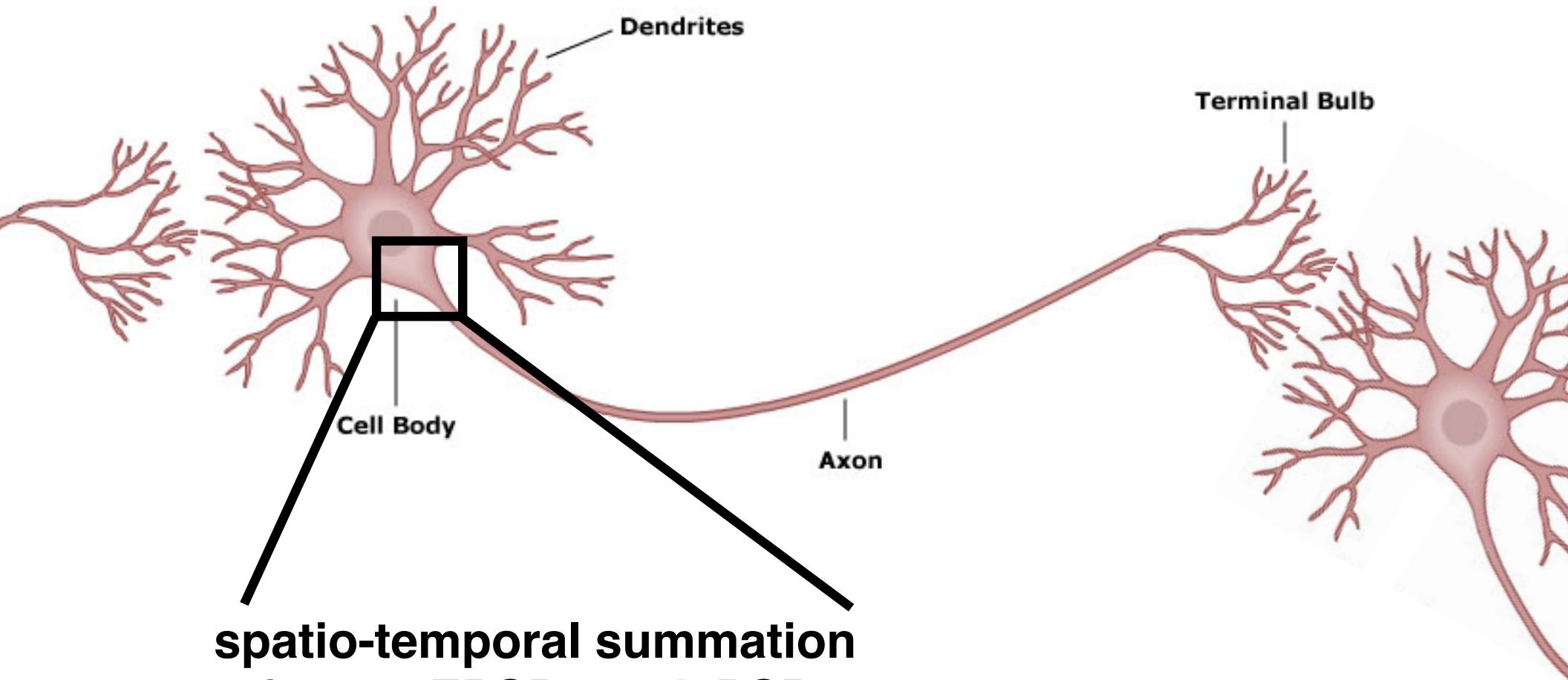


inputs can be positive (+) or negative (-)



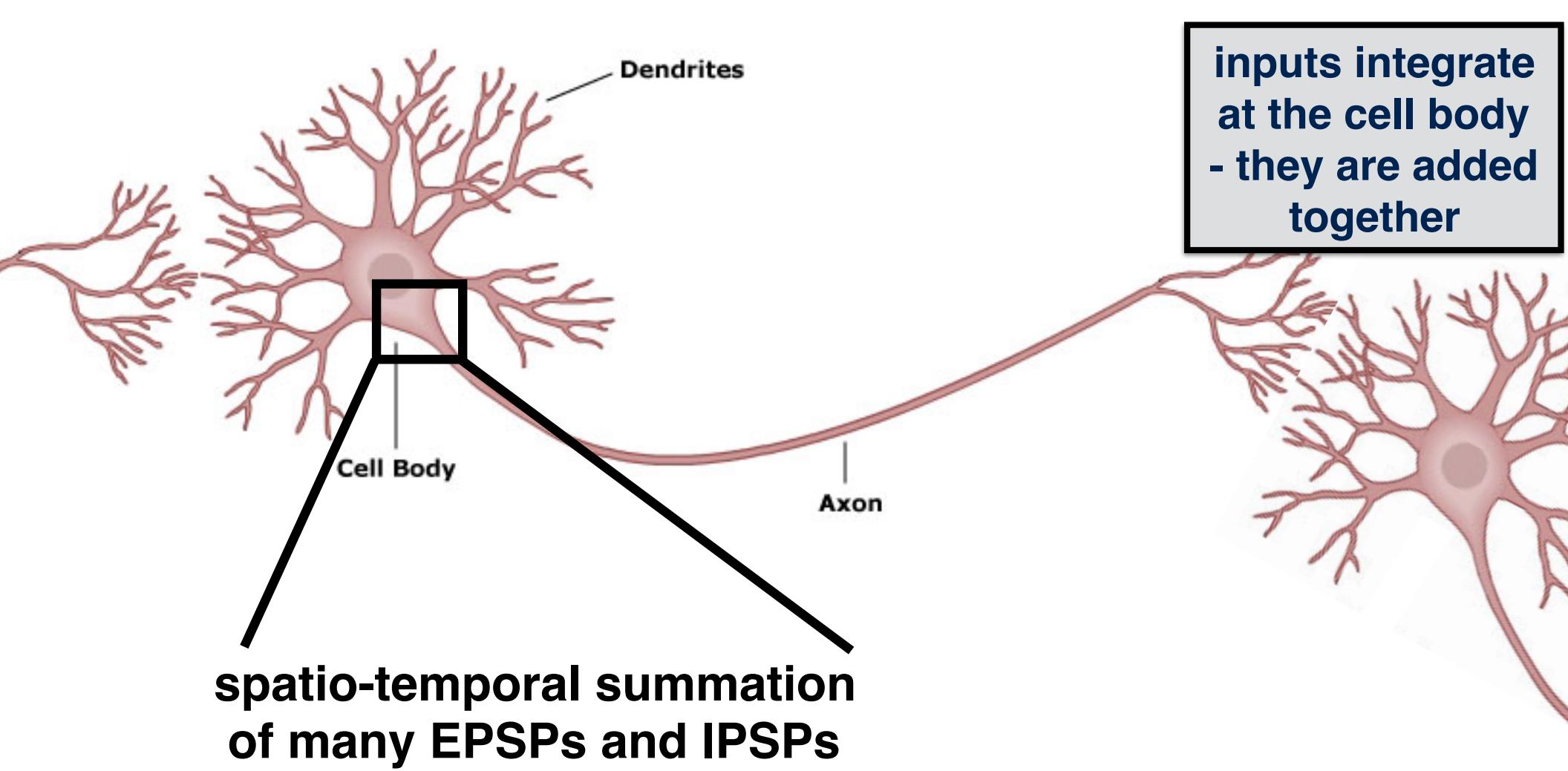
**EPSPs** (excitatory postsynaptic potentials)  
positive changes in membrane potential  
caused by excitatory pre-synaptic neurons  
(e.g., glutamate and NMDA receptors)

**IPSPs** (inhibitory postsynaptic potentials)  
negative changes in membrane potential  
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(e.g., GABA and GABA receptors)



from many of synaptic stimulations  
in close spatio-temporal proximity

potentials spread, but dissipate  
over space and time because  
neurons not good conductors

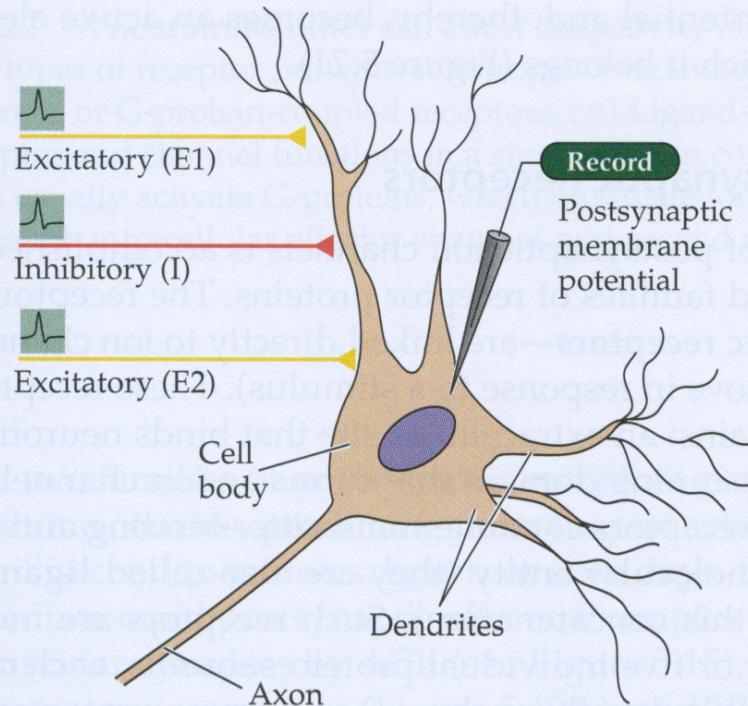


from many of synaptic stimulations  
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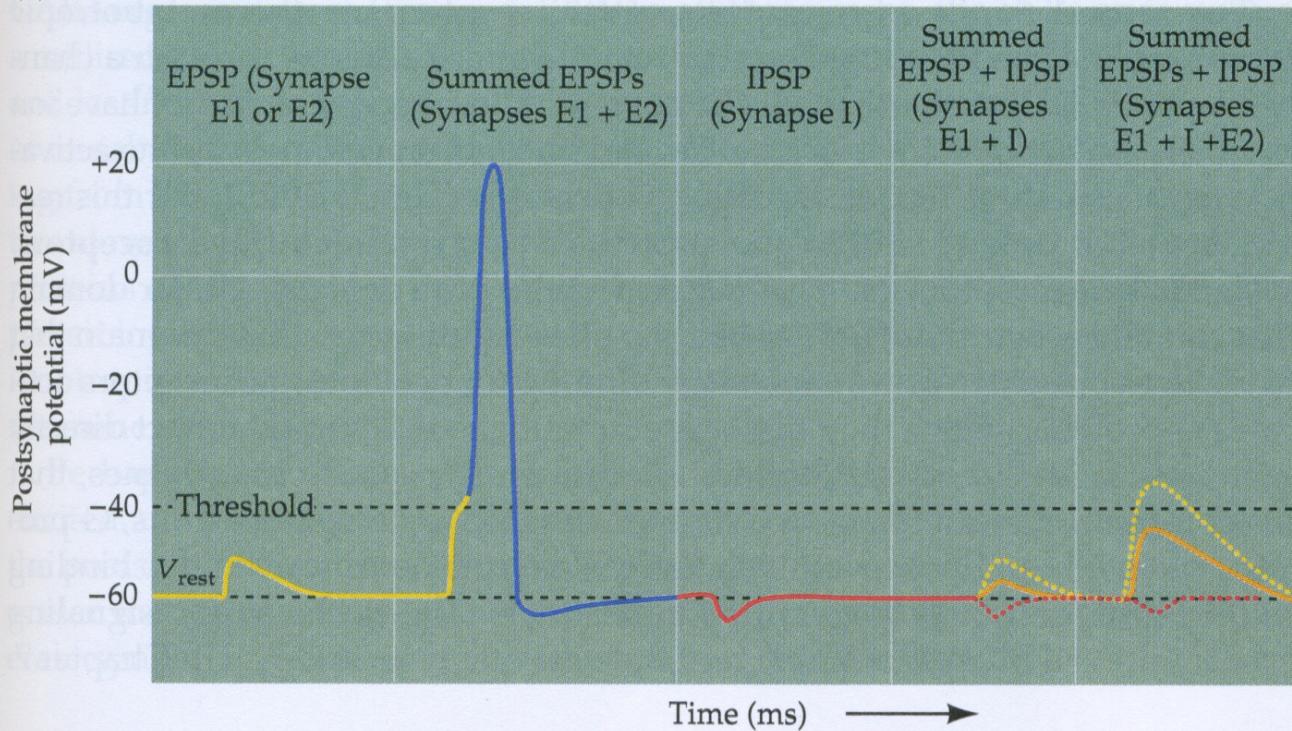
potentials spread, but dissipate  
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**inputs integrate  
at the cell body  
- they are added  
together**

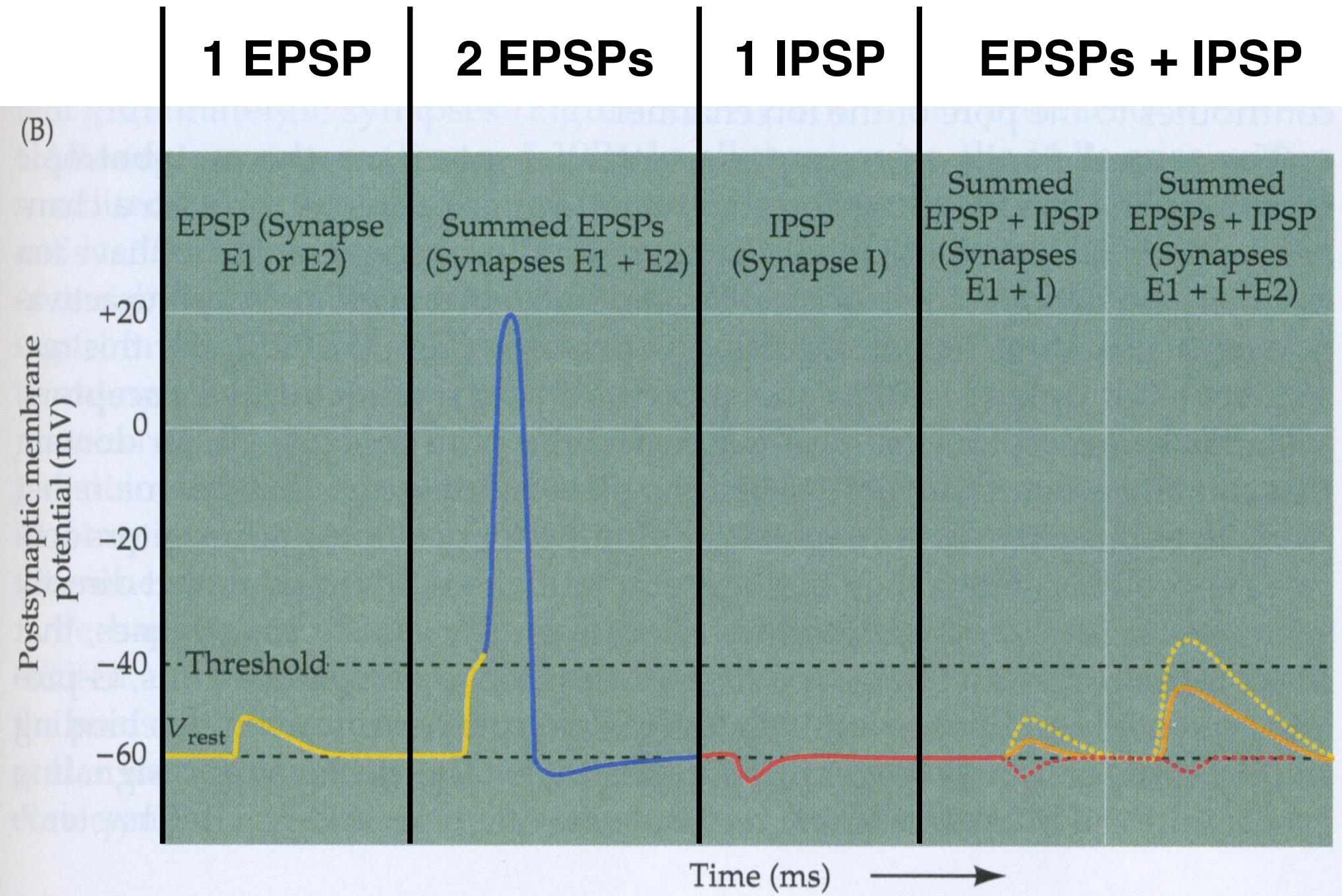
(A)

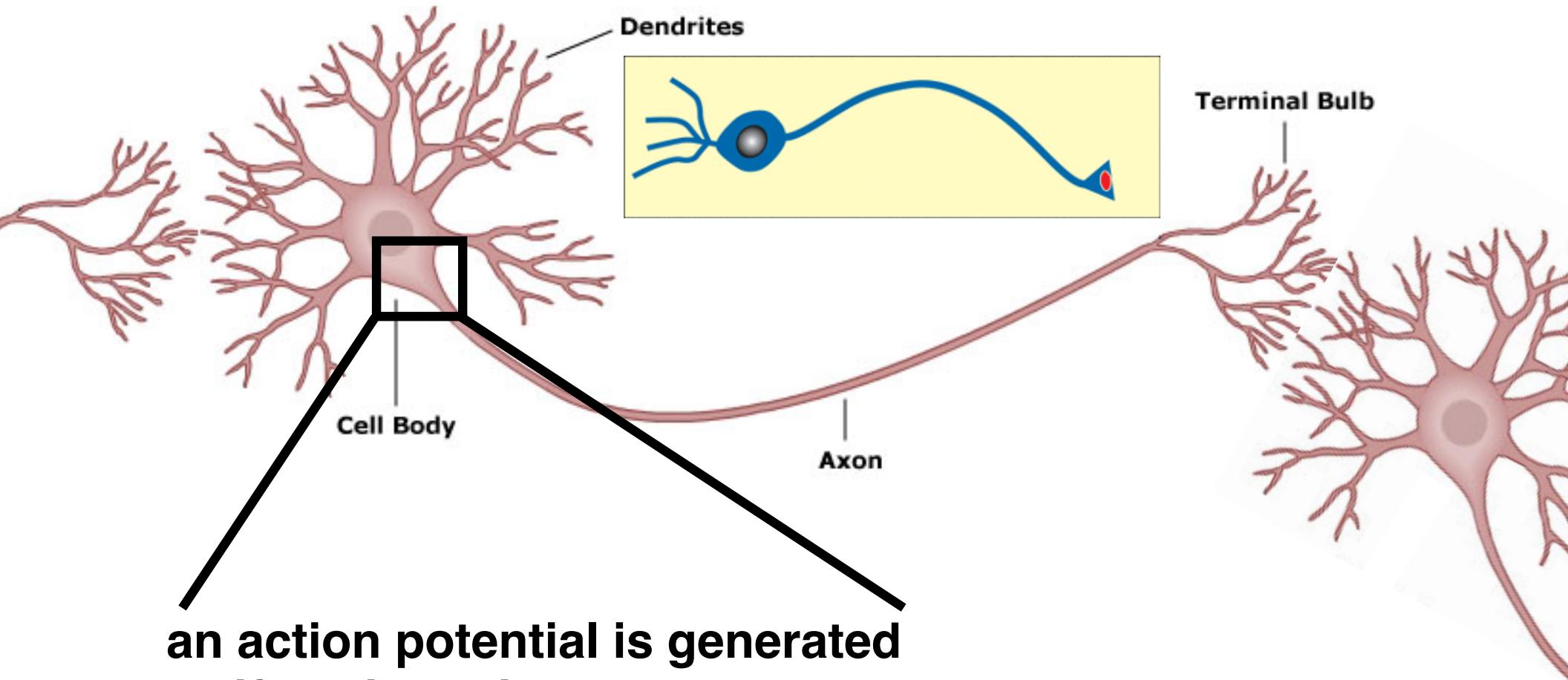


(B)

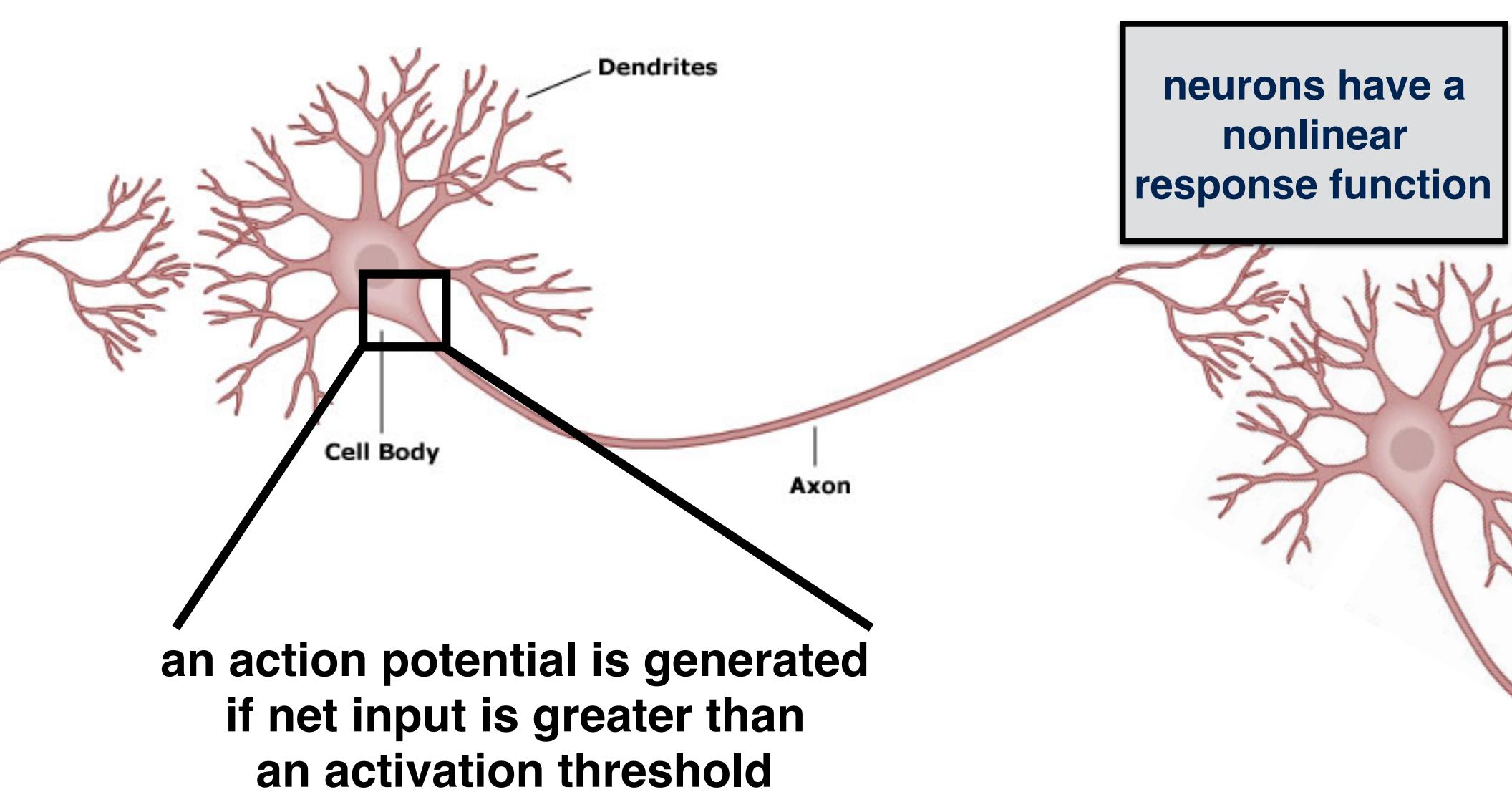


(B)



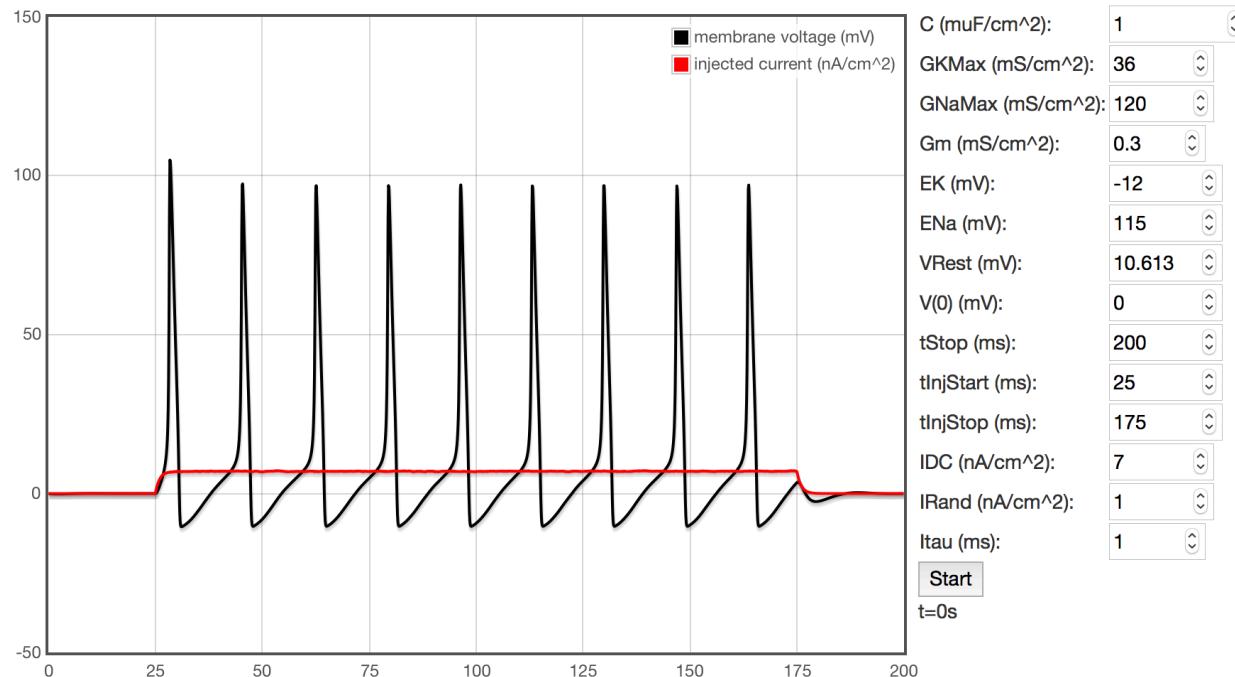


**an action potential is generated  
if net input is greater than  
an activation threshold**



# action potential simulator

## Hodgkin-Huxley Simulation with Javascript

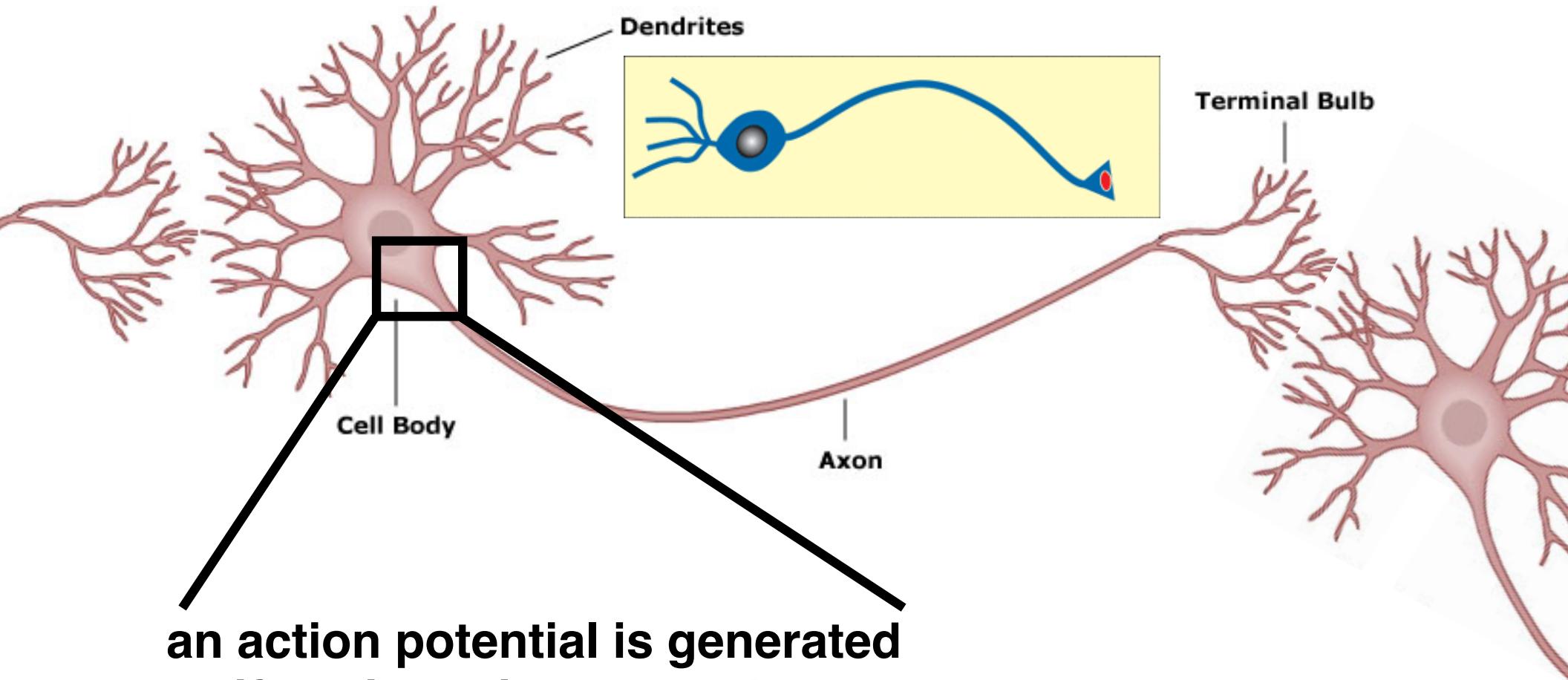


<http://myselph.de/hodgkinHuxley.html>

IDC (input/injected current)

IRand (random variability in current)

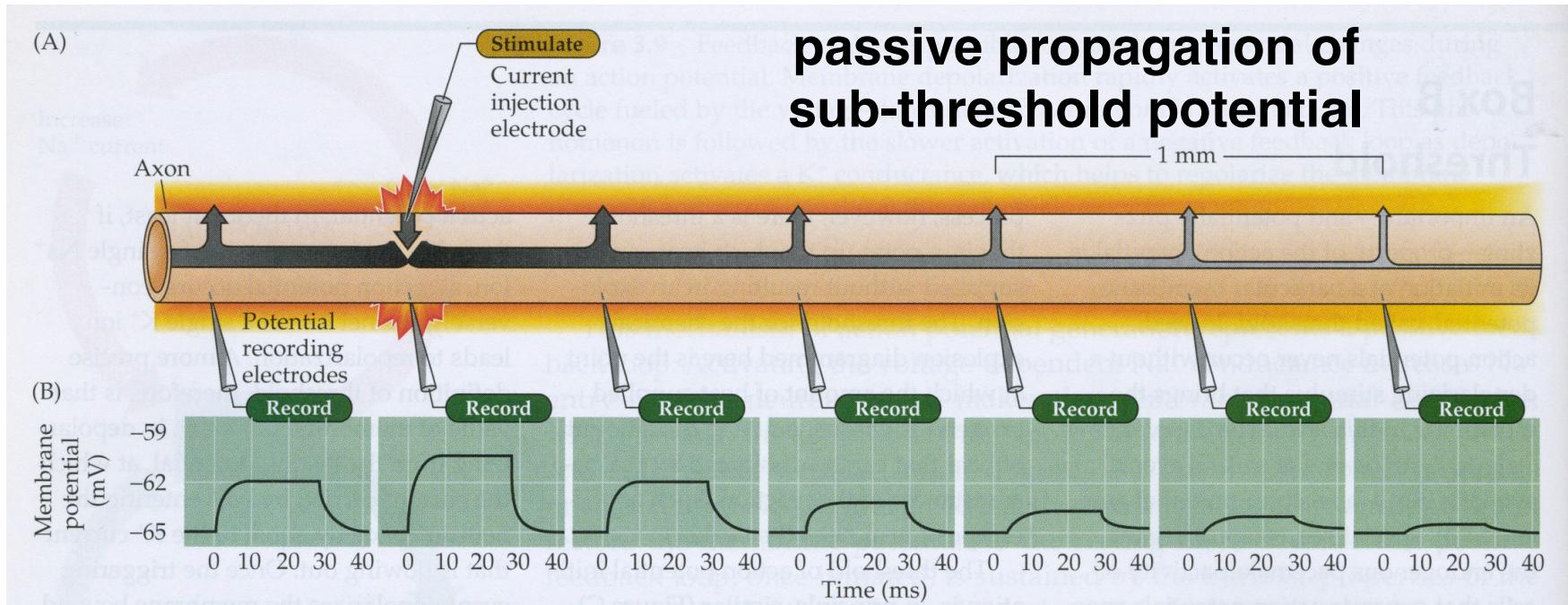
try IDC=2.355 vs. IDC=2.356 with IRand=0



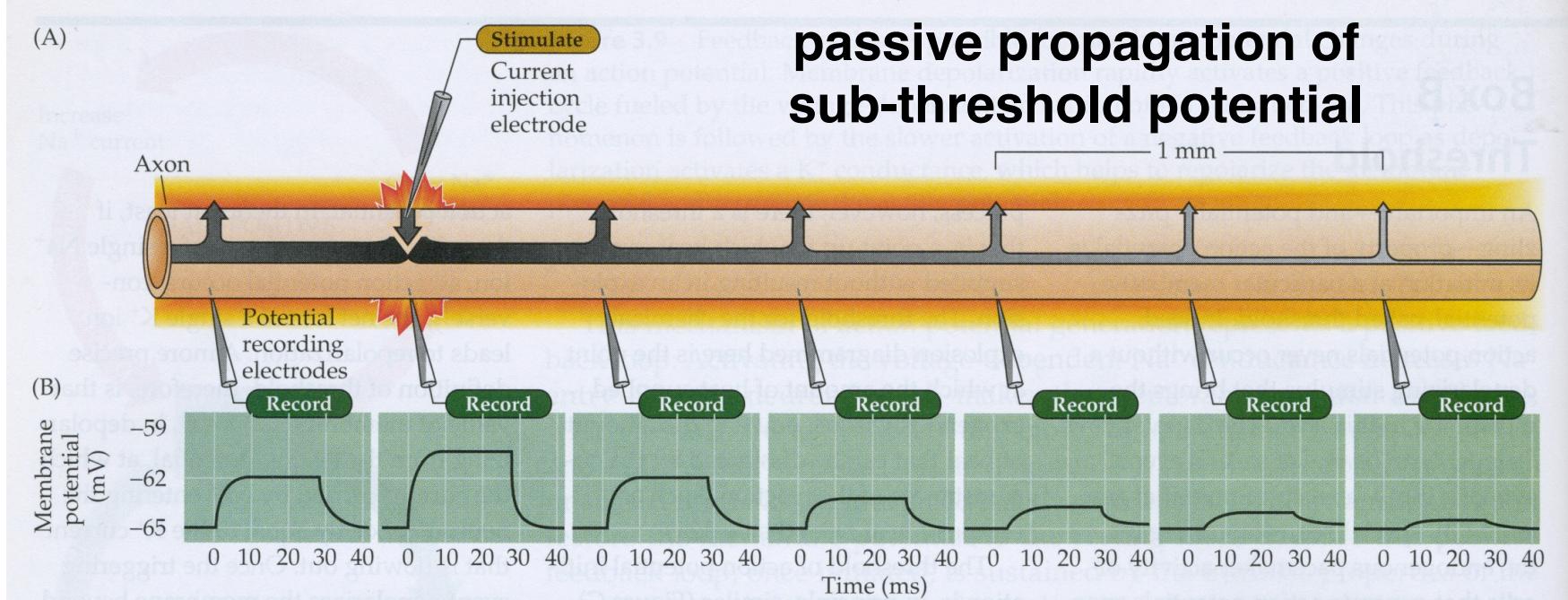
**an action potential is generated  
if net input is greater than  
an activation threshold**

action potential is nature's way of  
making the axon conductive over  
relatively long distances

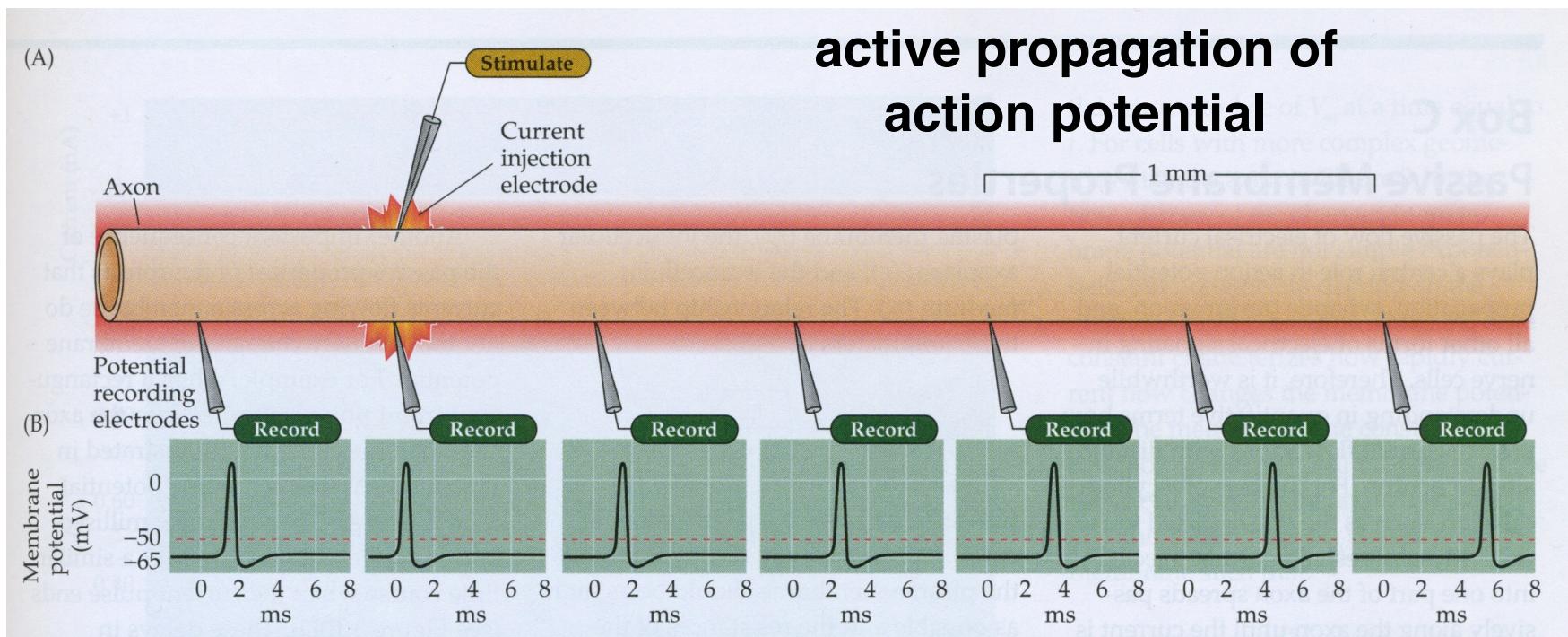
# passive propagation of sub-threshold potential

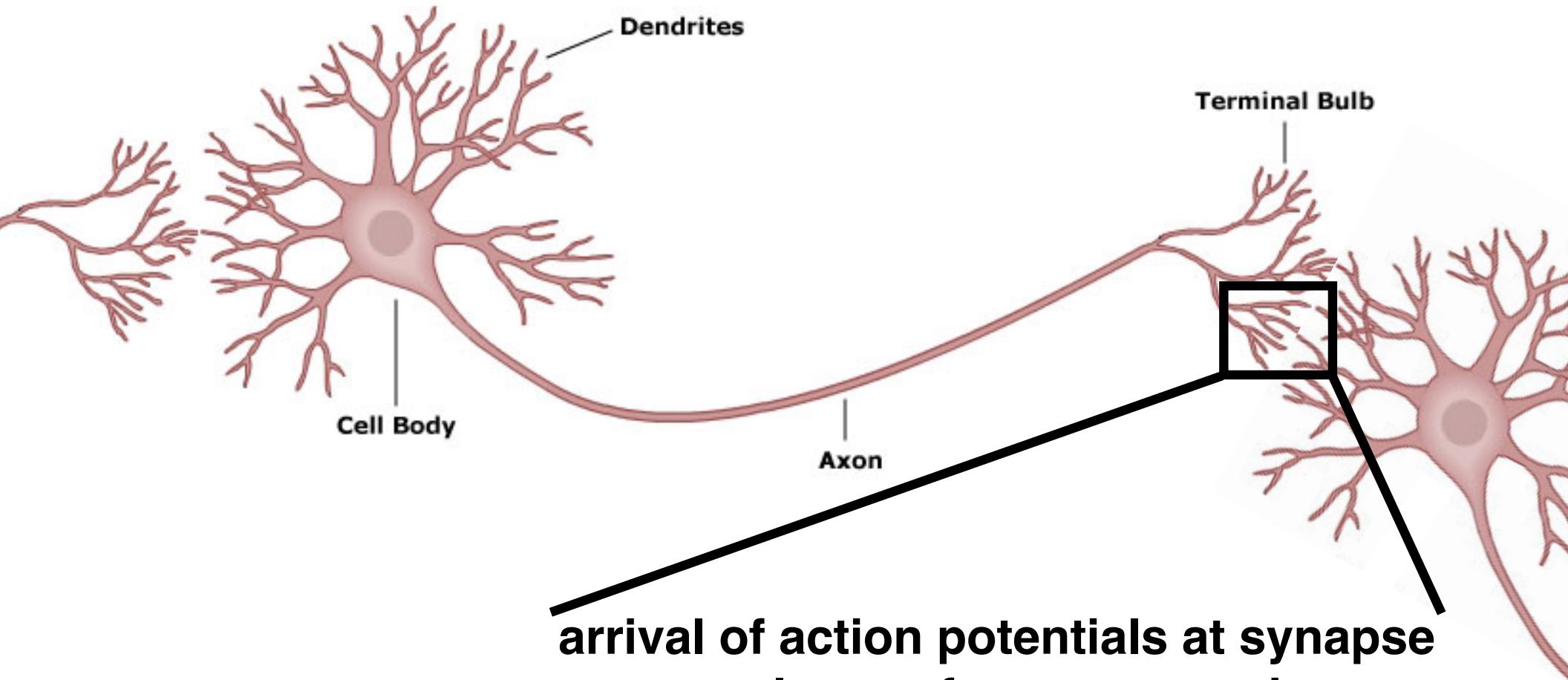


## passive propagation of sub-threshold potential



## active propagation of action potential

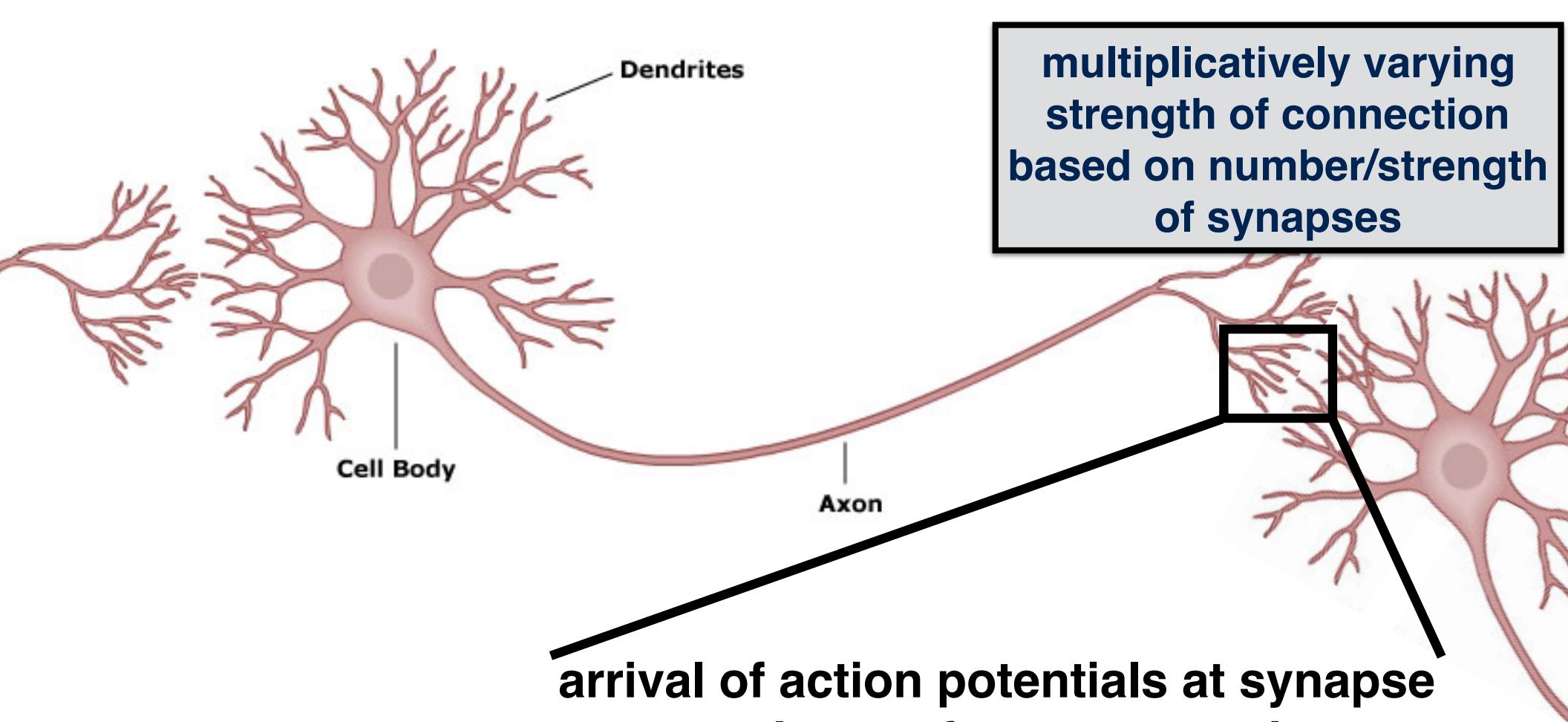




**arrival of action potentials at synapse  
causes release of neurotransmitters to  
post-synaptic neuron**

more and/or stronger synapses mean pre-synaptic neuron has more influence over post-synaptic neuron

synapses multiply effect of action potentials



**multiplicatively varying strength of connection based on number/strength of synapses**

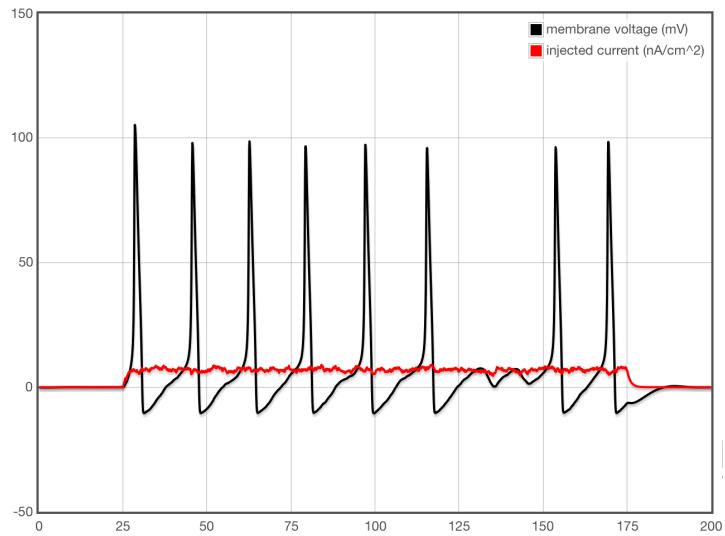
**arrival of action potentials at synapse causes release of neurotransmitters to post-synaptic neuron**

more and/or stronger synapses mean pre-synaptic neuron has more influence over post-synaptic neuron

synapses multiply effect of action potentials

# Levels of Neuron Modeling

- detailed model of action potentials (Hodgkin-Huxley model)



$$\frac{dV}{dt} = \frac{1}{C}(-I_{NA} - I_K - I_{leak} - I_{input})$$

$$\frac{dV}{dt} = \frac{1}{C}(-g_{NA}m^3h(V - E_{NA}) - g_Kn^4(V - E_K) - g_{leak}(V - E_{leak}) + I_{input})$$

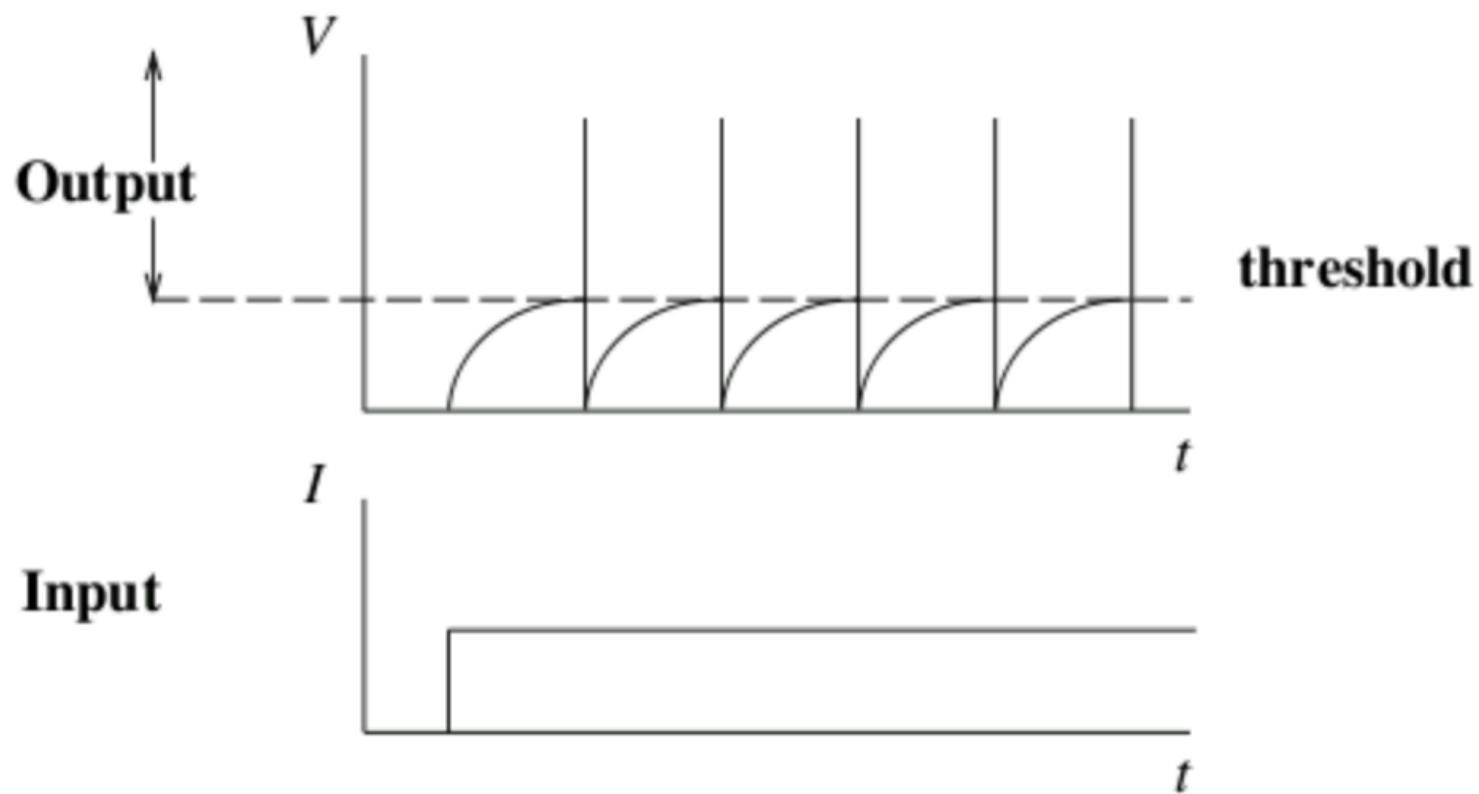
$$\frac{dm}{dt} = \frac{1}{\tau_m(V)}(-m + M(V))$$

$$\frac{dh}{dt} = \frac{1}{\tau_h(V)}(-h + H(V))$$

$$\frac{dn}{dt} = \frac{1}{\tau_n(V)}(-n + N(V))$$

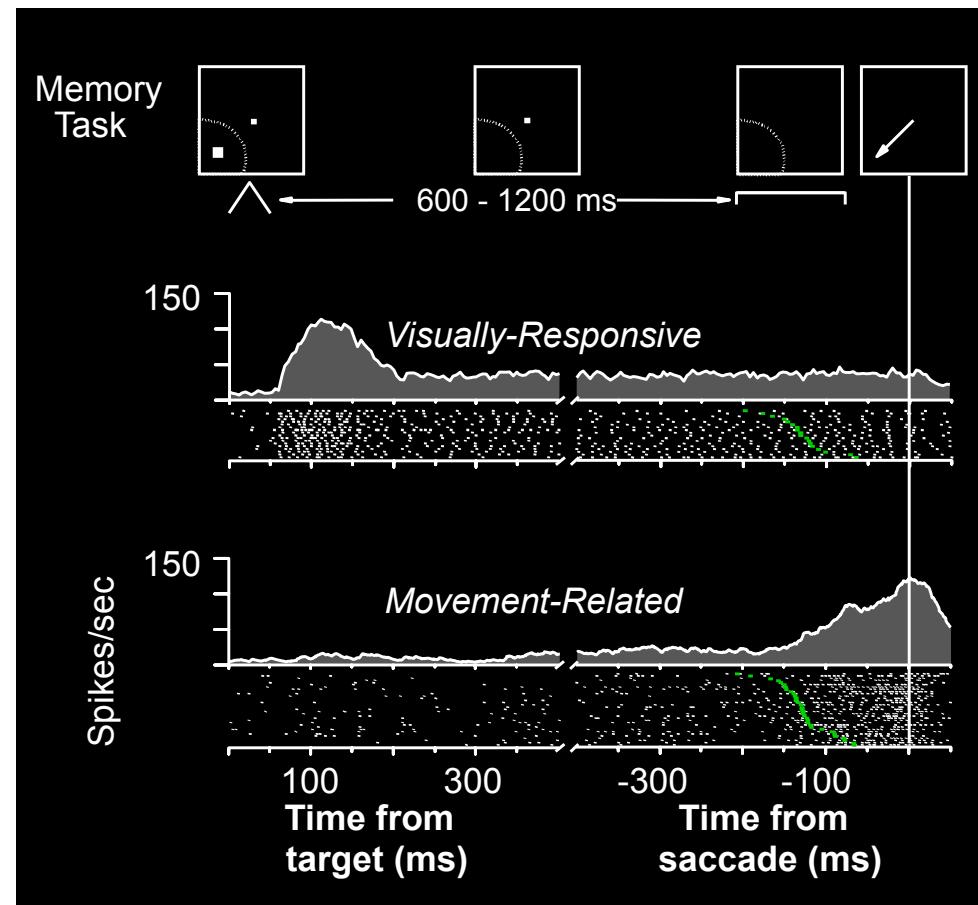
# Levels of Neuron Modeling

- detailed model of action potentials (Hodgkin-Huxley model)
- integrate-and-fire (spiking) neuron

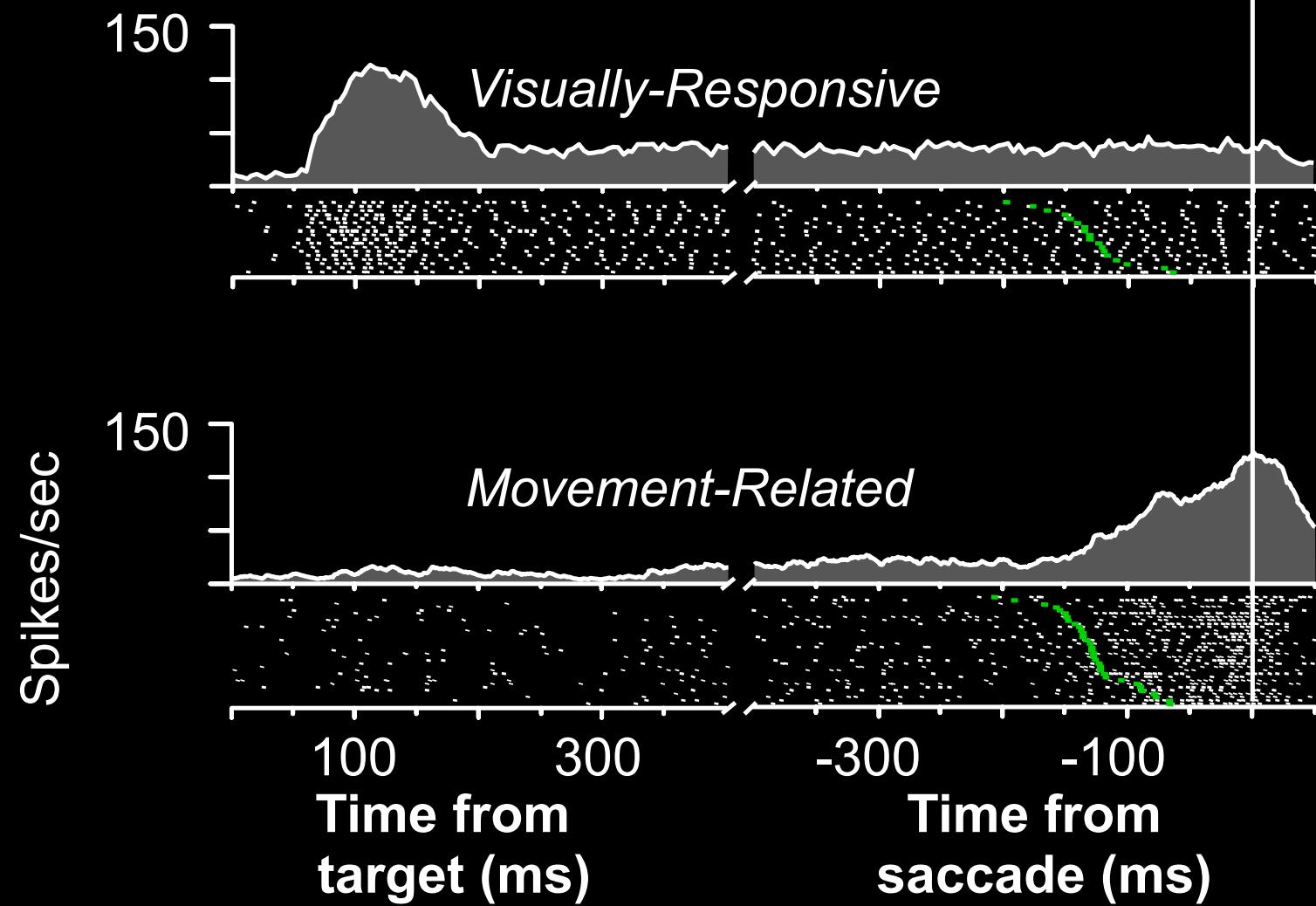
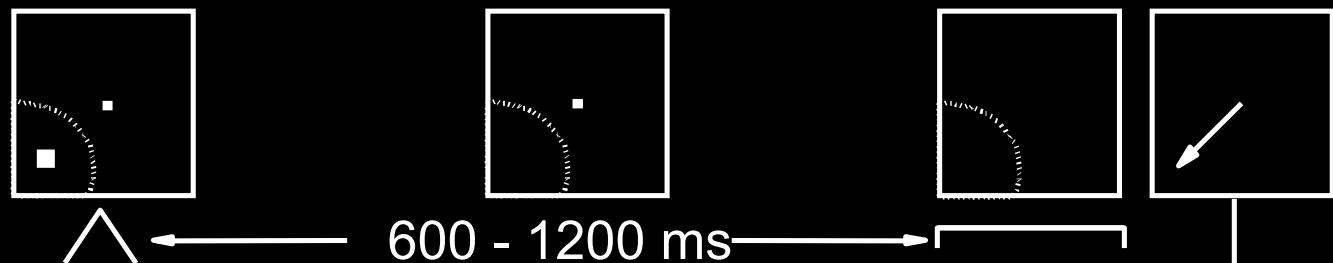


# Levels of Neuron Modeling

- detailed model of action potentials (Hodgkin-Huxley model)
- integrate-and-fire (spiking) neuron
- rate-coded neuron



Memory  
Task



# Levels of Neuron Modeling

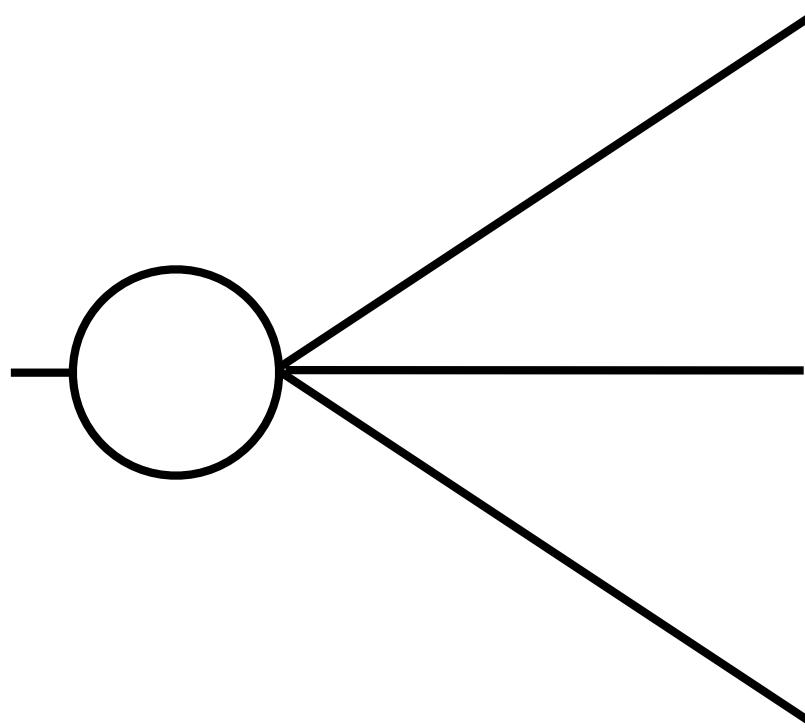
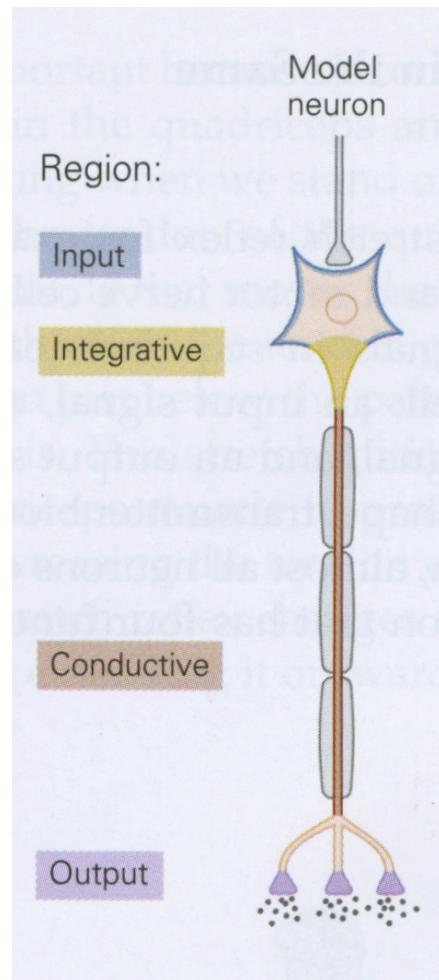
- detailed model of action potentials (Hodgkin-Huxley model)
- integrate-and-fire (spiking) neuron
- rate-coded neuron
  - we'll start by considering neural network models that not only ignore spikes, but largely ignore time altogether

then consider models that learn, networks that change over time with experience

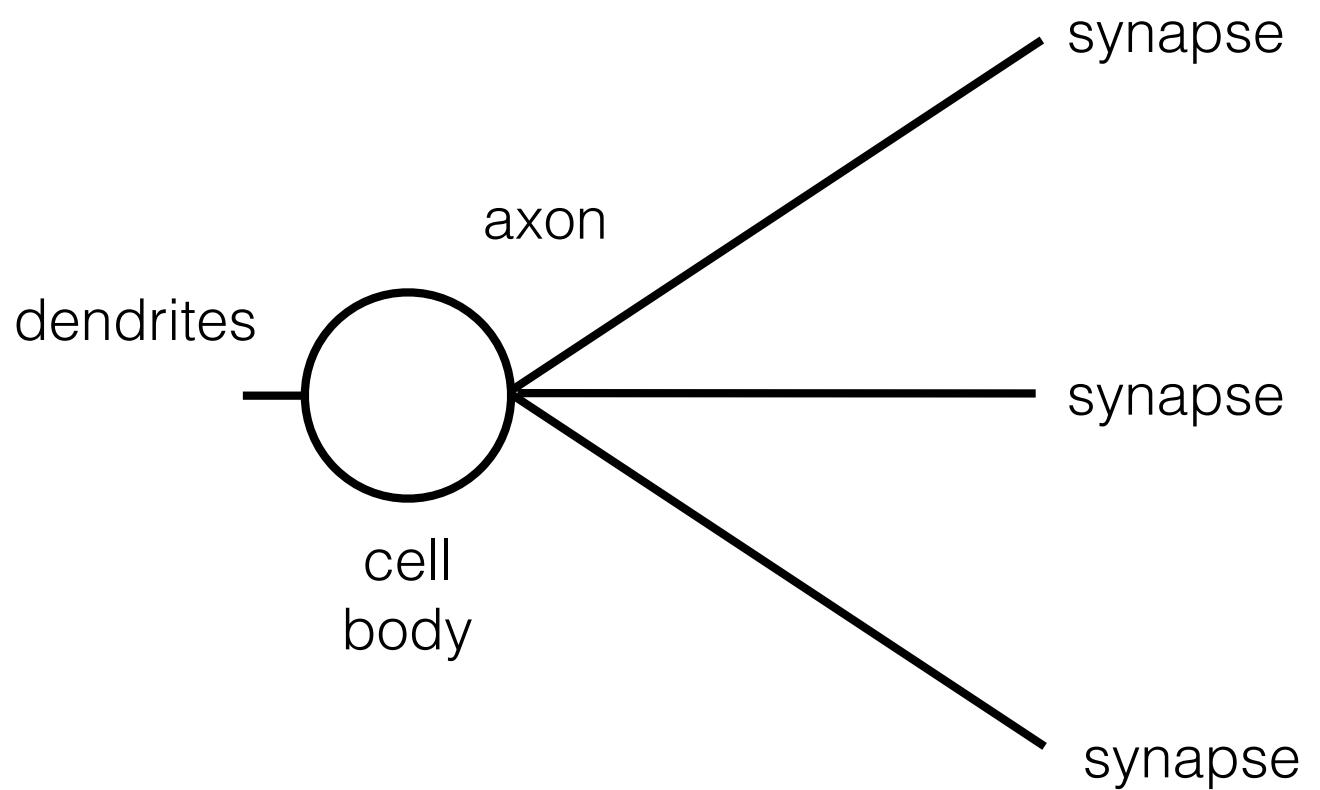
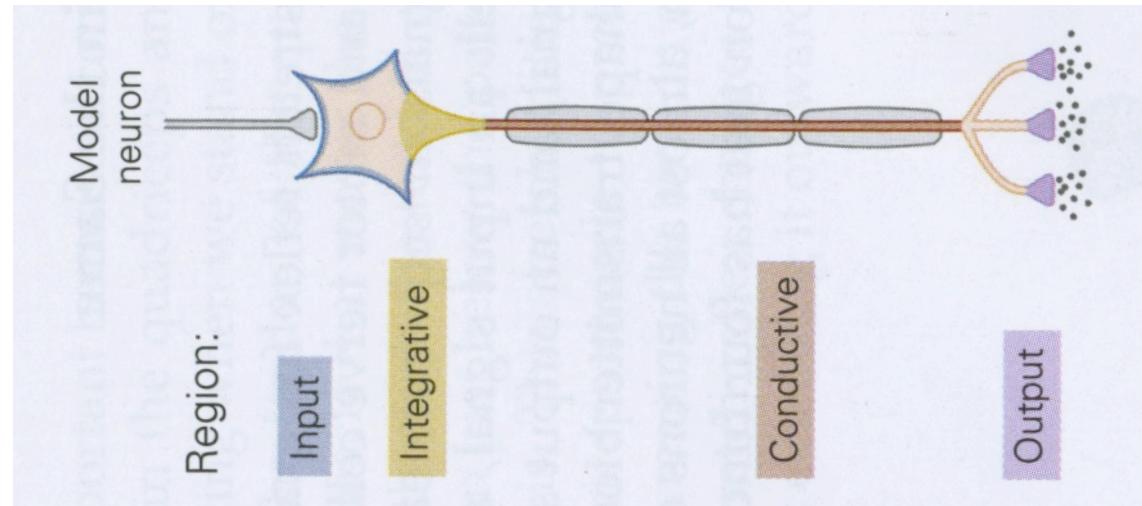
may consider models that allow for dynamics (recurrent networks, dynamical networks, spiking)



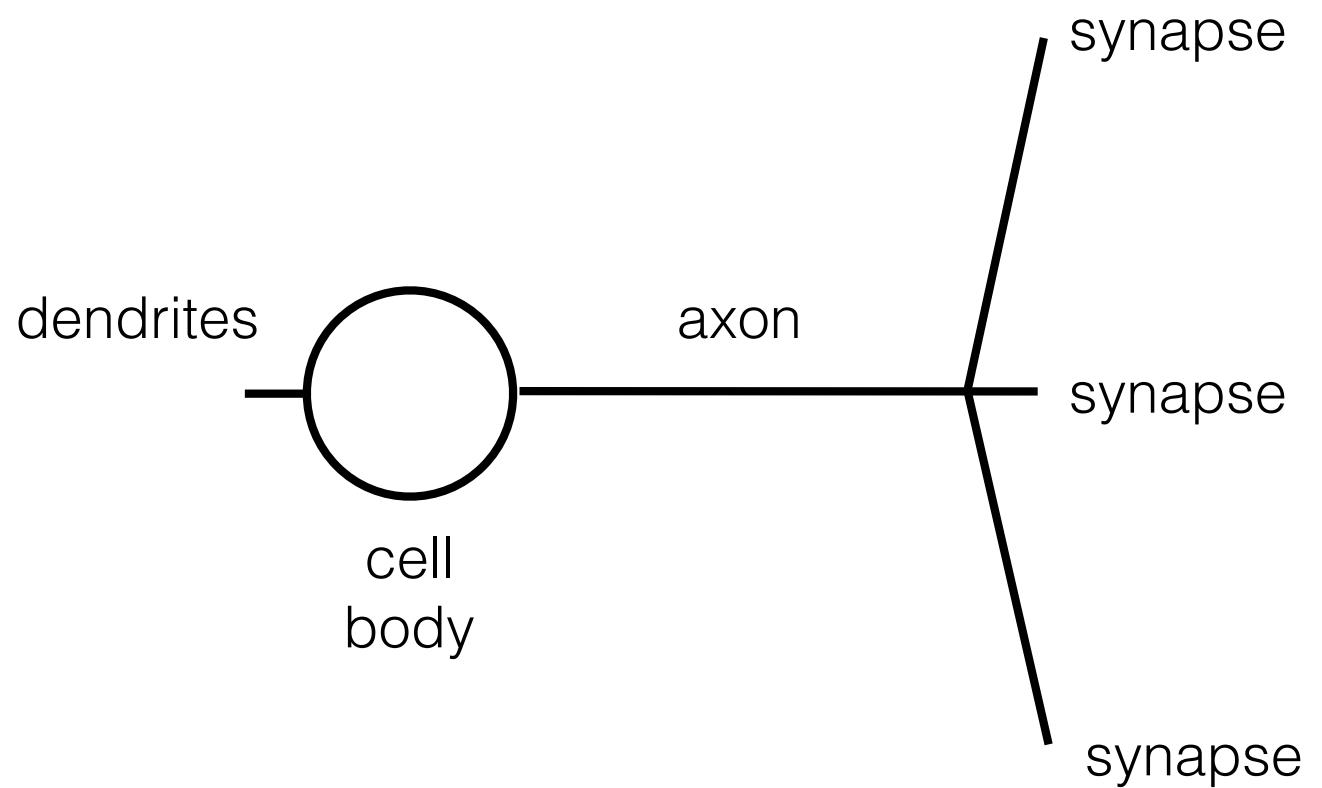
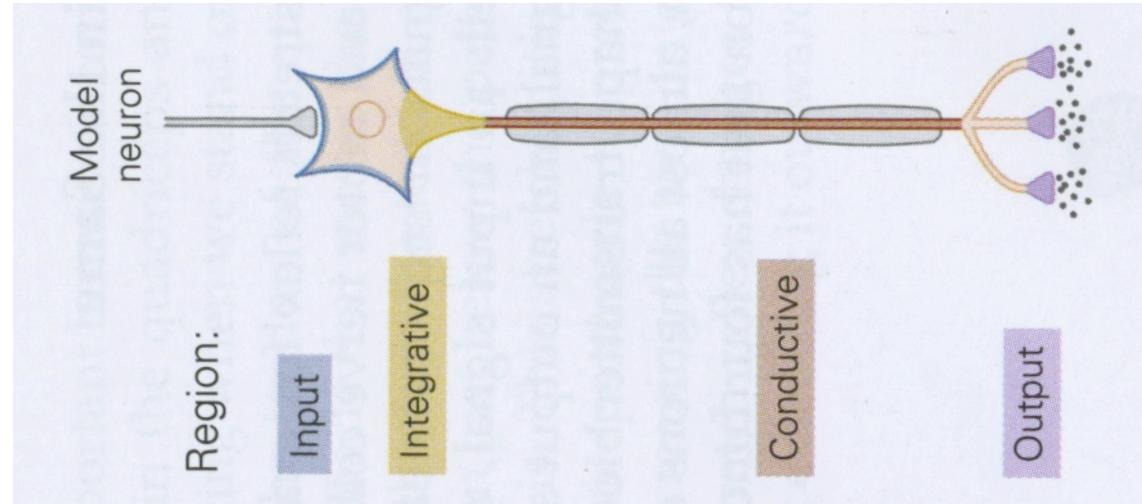
# **modeling an idealized neuron**



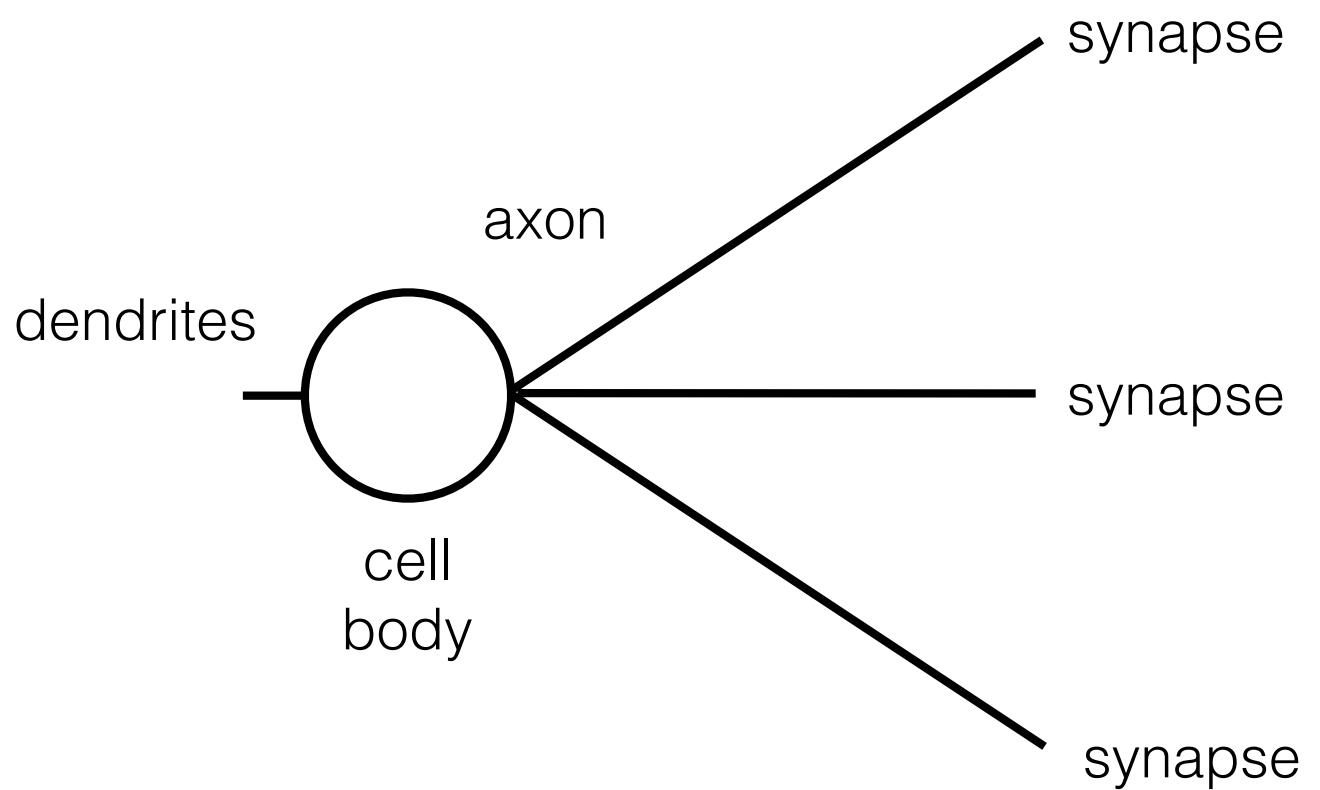
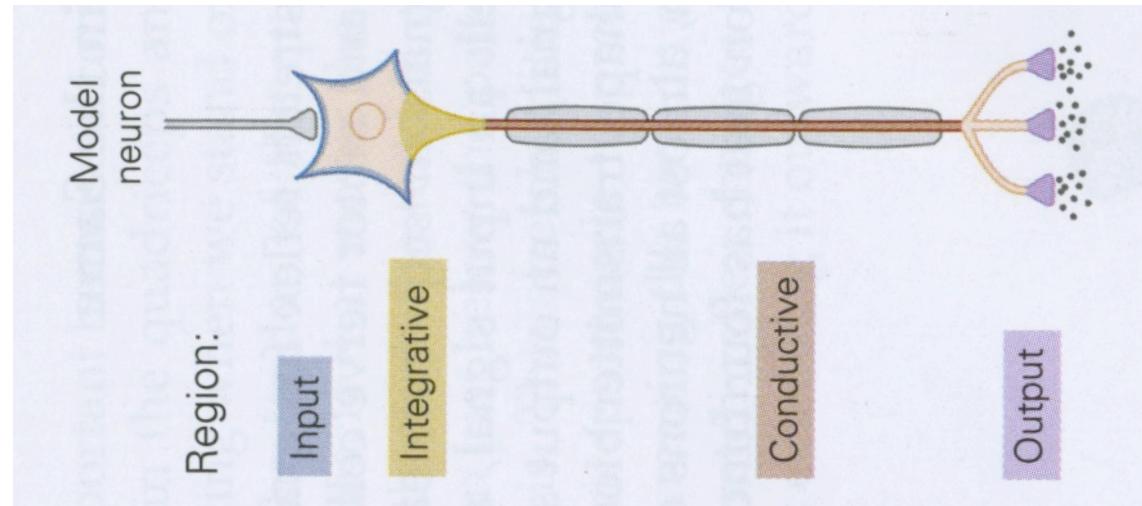
## Idealized Neuron



# Idealized Neuron



# Idealized Neuron

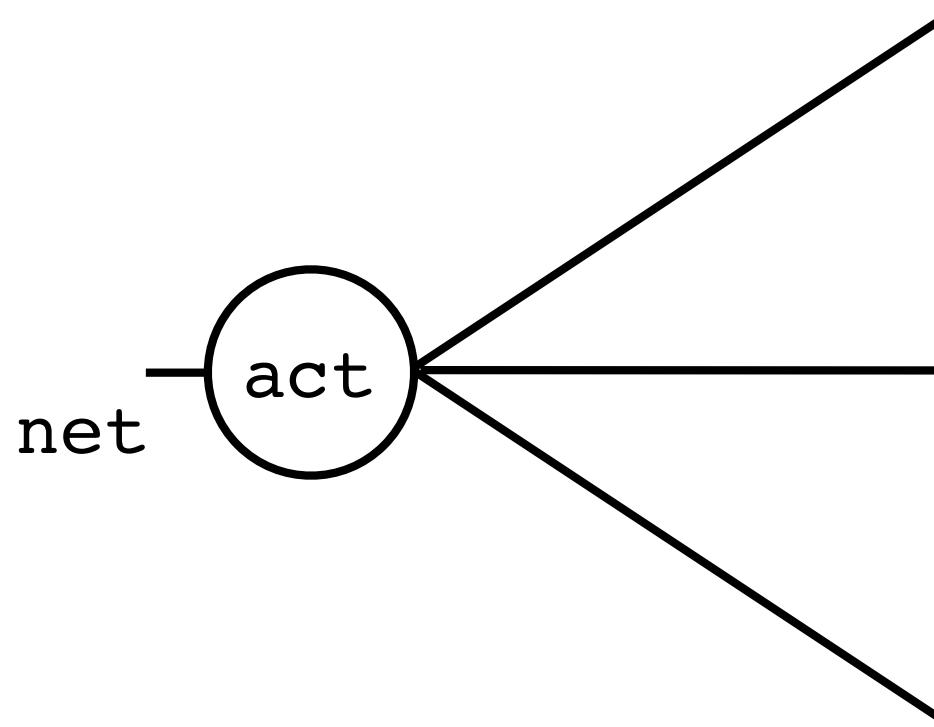


## Idealized Neuron

"unit" or "node"

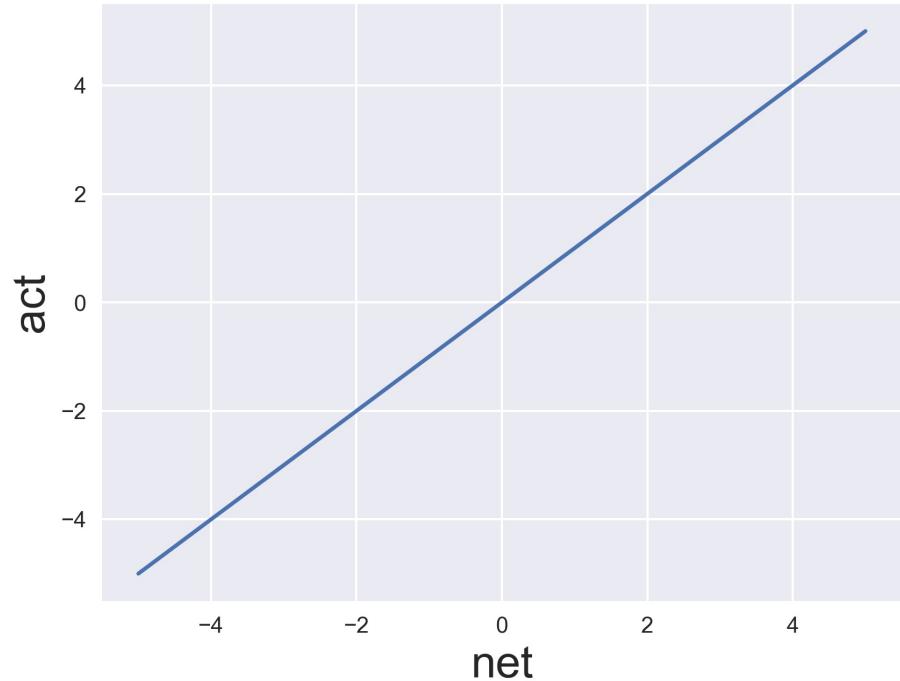
*how is the activation of a neuron  
related to its net input?*

*where "activation" is akin to spike rate*



**Idealized Neuron**

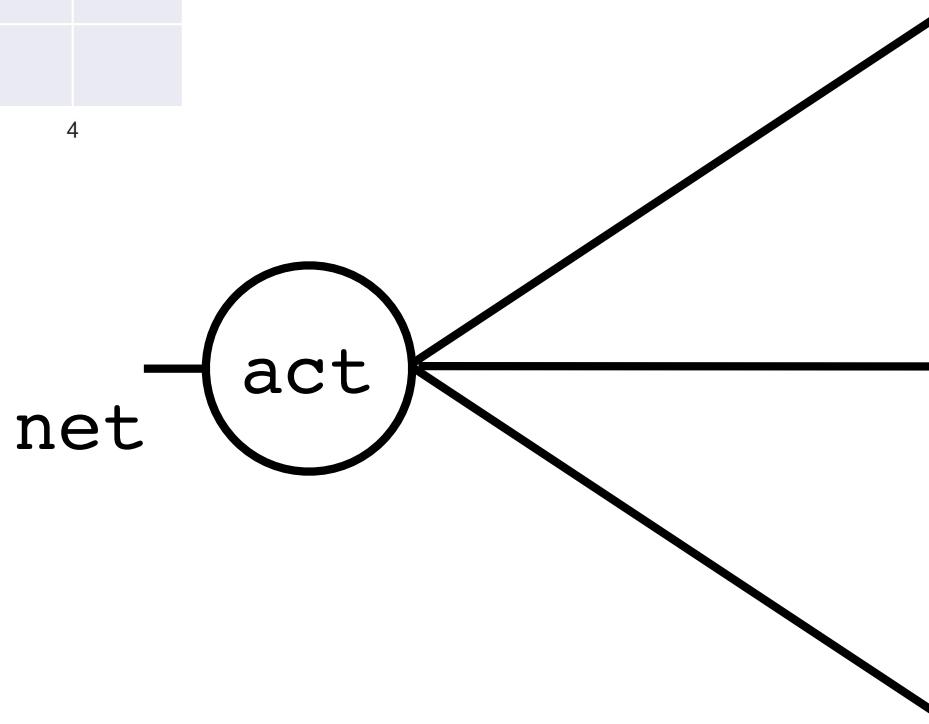
linear activation function



of course this is  
not biologically  
plausible if activation  
is equated with rate

but a unit could instead  
represent a local circuit  
or neural population

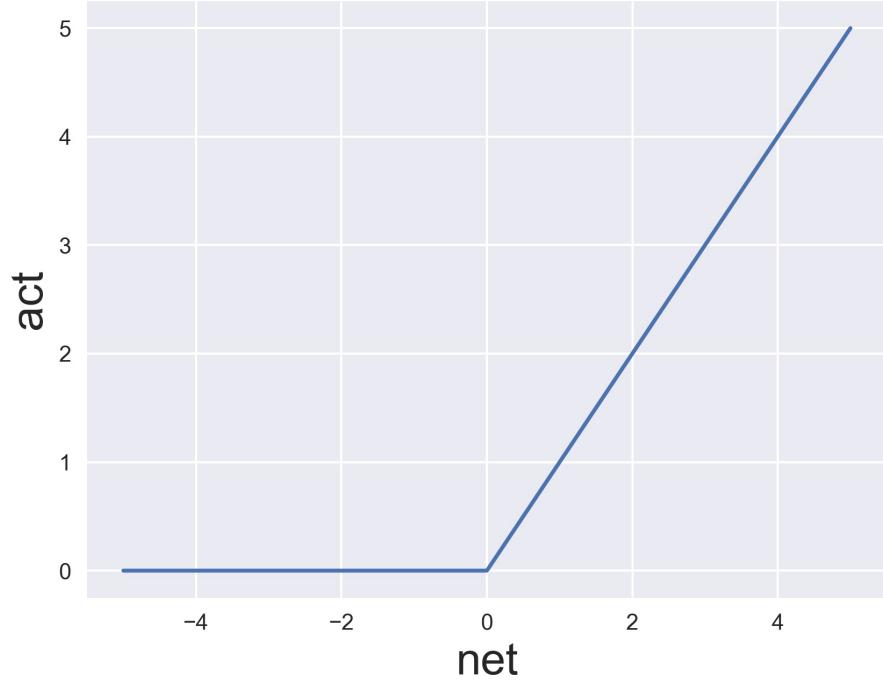
$$a_j = n_j$$



`linear()`

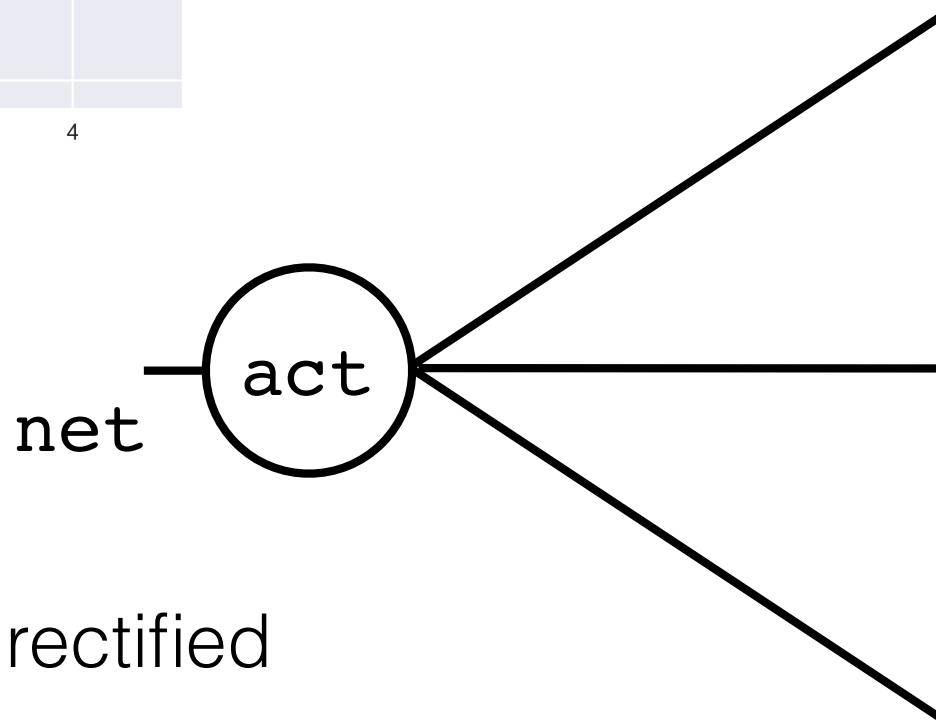
**Idealized Neuron**

rectified linear (relu)



neurons have a  
nonlinear  
response function

$$a_j = \begin{cases} 0 & \text{if } n_j \leq 0 \\ n_j & \text{otherwise} \end{cases}$$

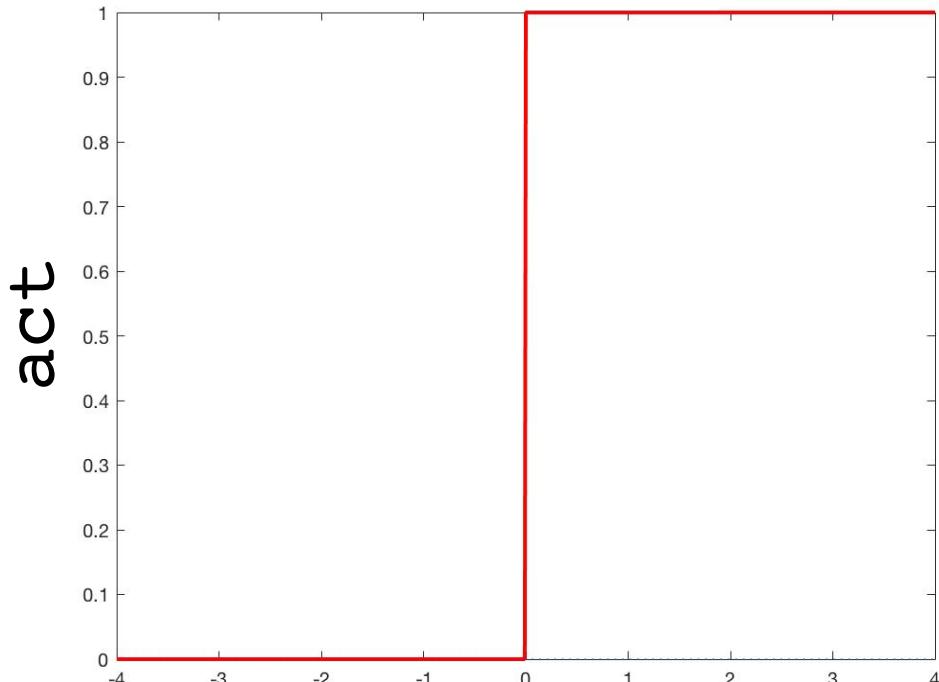


sometimes called a rectified  
linear unit (or relu)

relu()

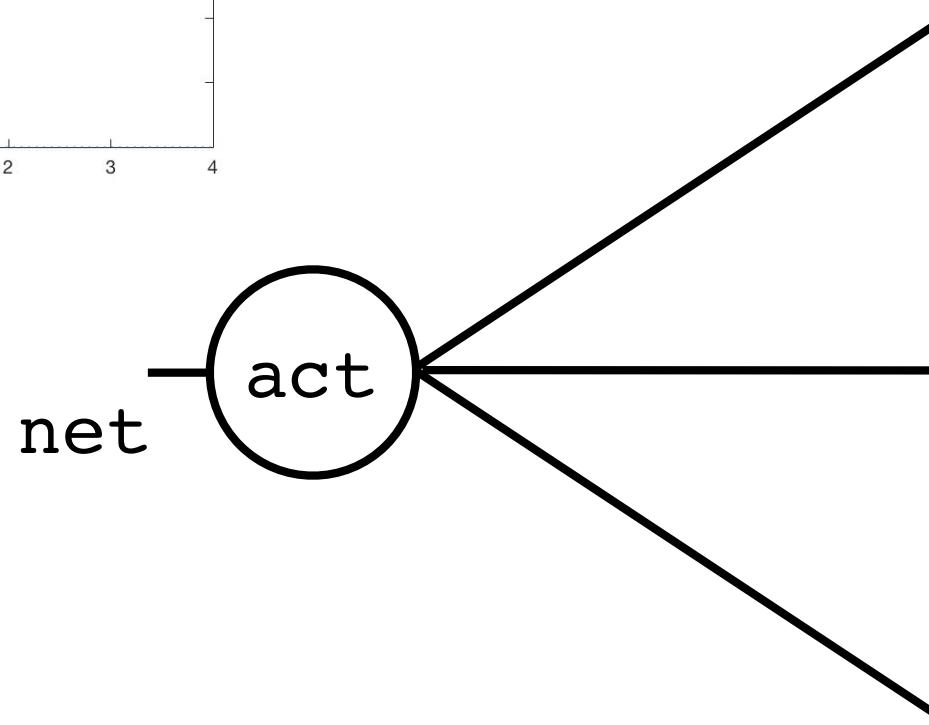
Idealized Neuron

## Step Function



neurons have a  
nonlinear  
response function

$$act = \begin{cases} 0 & \text{if } net \leq 0 \\ 1 & \text{otherwise} \end{cases}$$

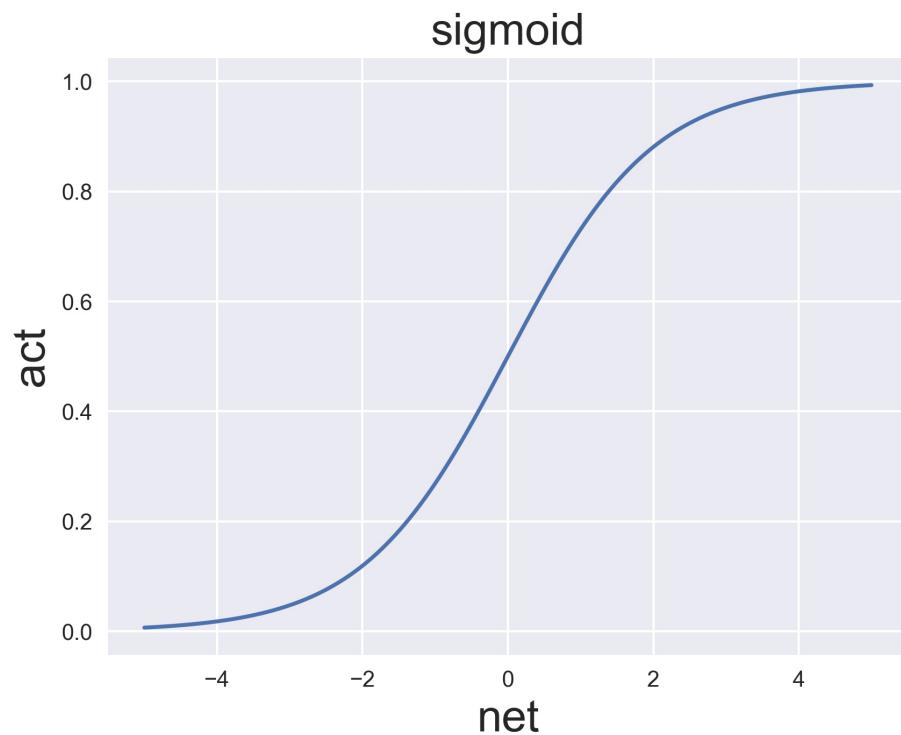


\*derivative is zero or undefined

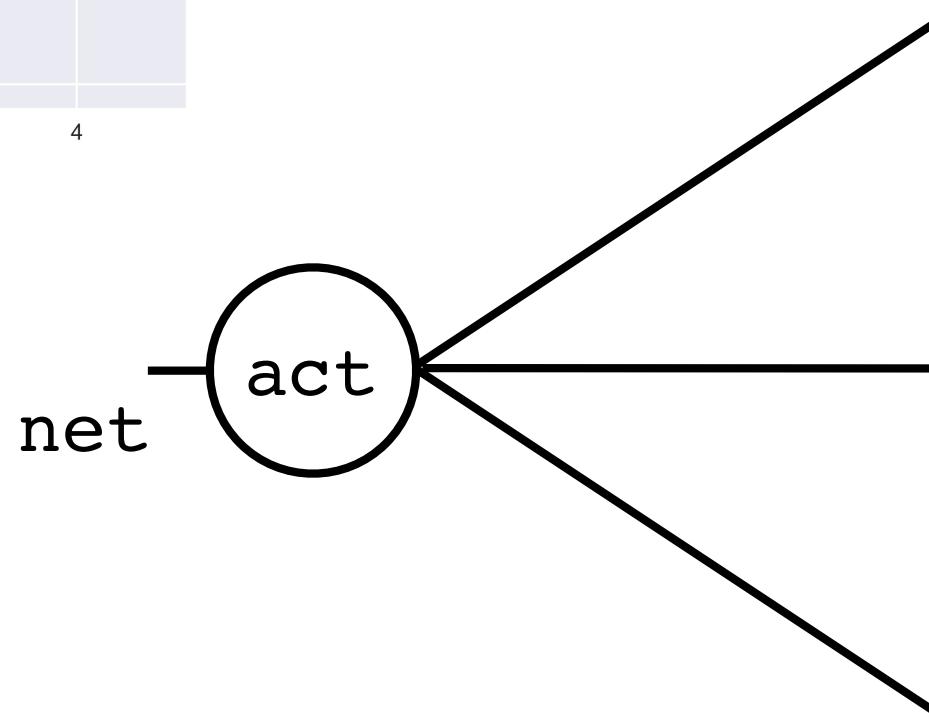
not defined\*

Idealized Neuron

**neurons have a  
nonlinear  
response function**



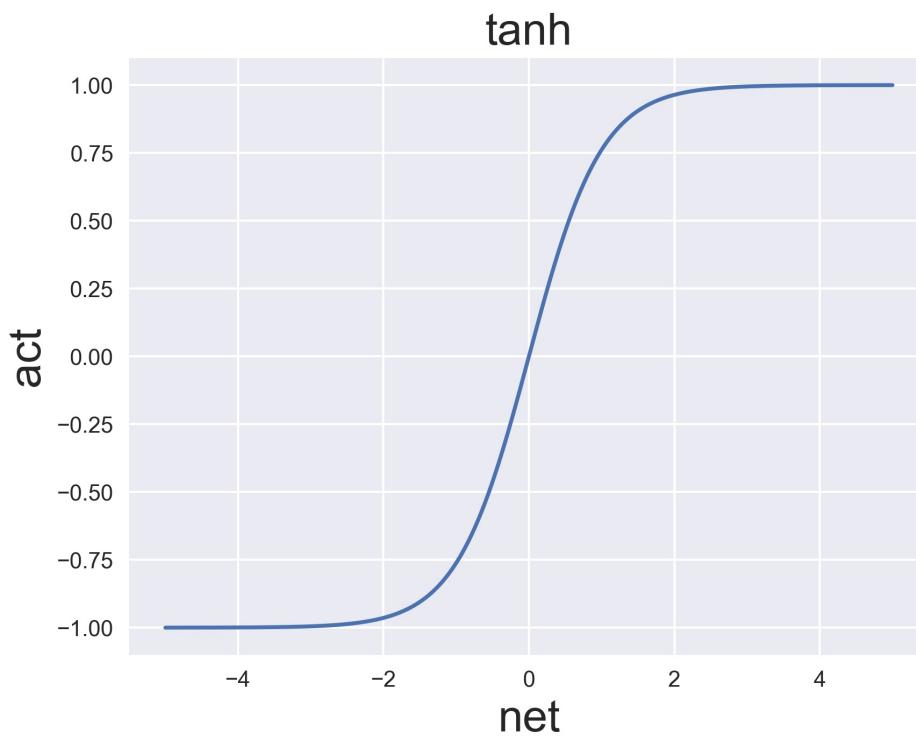
$$a_j = \frac{1}{1 + \exp(-n_j)}$$



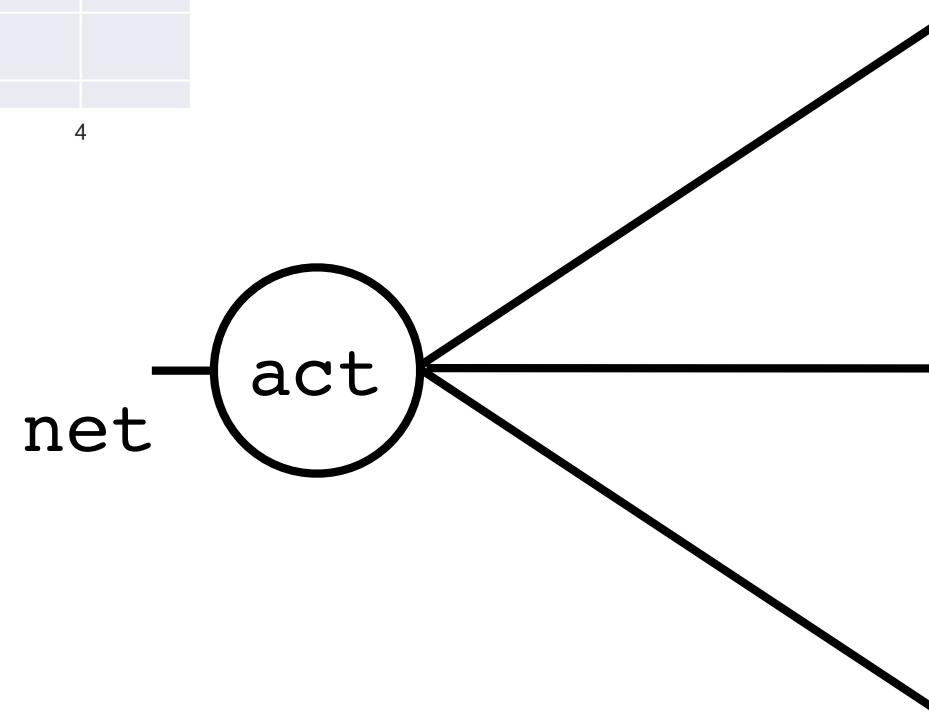
`sigmoid()`

**Idealized Neuron**

**neurons have a  
nonlinear  
response function**



$$a_j = \frac{\exp(n_j) - \exp(-n_j)}{\exp(n_j) + \exp(-n_j)}$$



tanh( )

**Idealized Neuron**

```
import numpy as np
import keras.activations as kact
import tensorflow as tf

session = tf.InteractiveSession()

netnp = np.linspace(-5.0, 5.0, 1000)
nett = tf.convert_to_tensor(netnp)

acttf = kact.sigmoid(nettf)
actnp = acttf.eval()

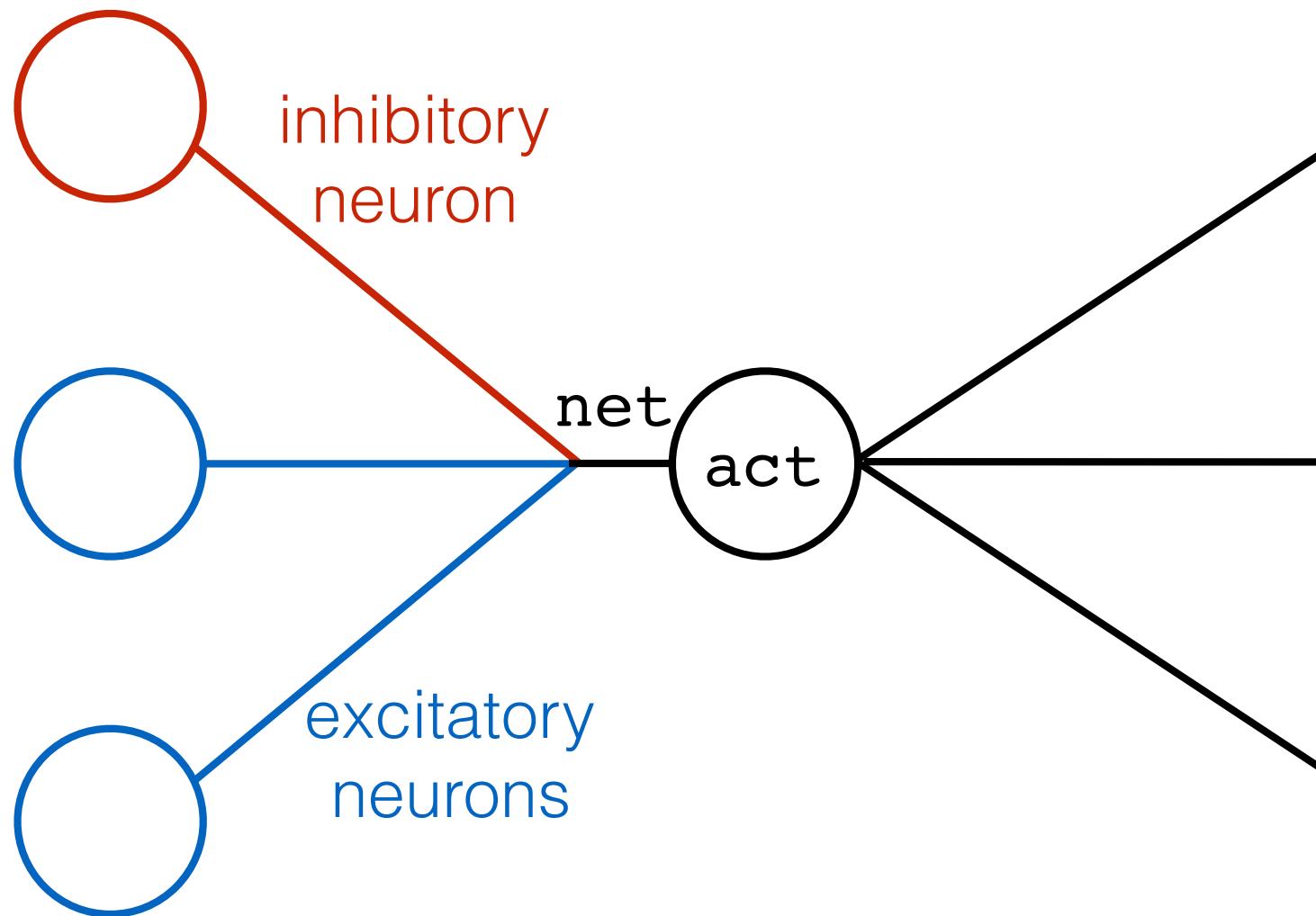
session.close()
```

## Keras / TensorFlow

see ActivFuncs.py and ActivFuncs.ipynb on Brightspace



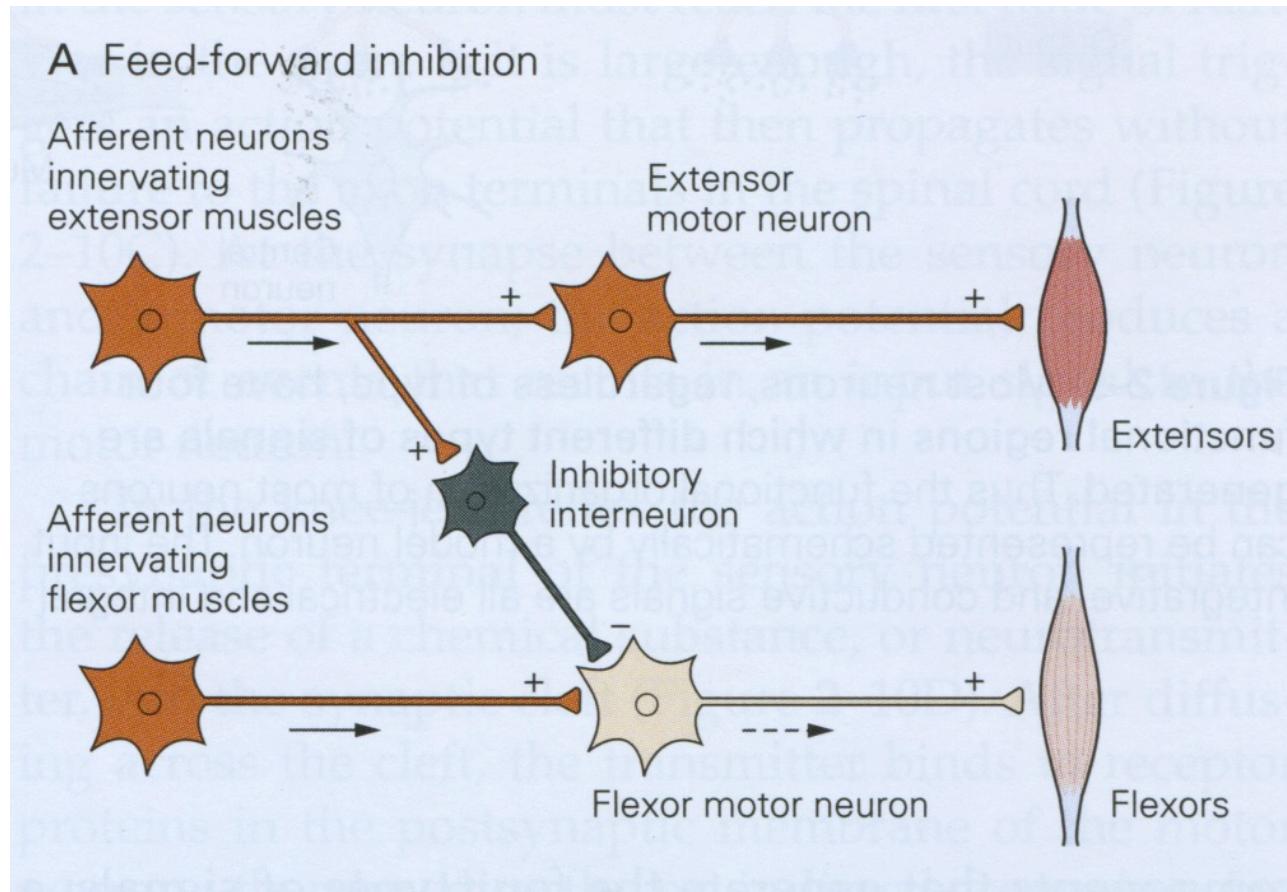
inputs can be  
positive (+) or  
negative (-)



while individual neurons are either excitatory or inhibitory, inhibitory interneurons can make an excitatory neuron inhibit indirectly

inputs can be positive (+) or negative (-)

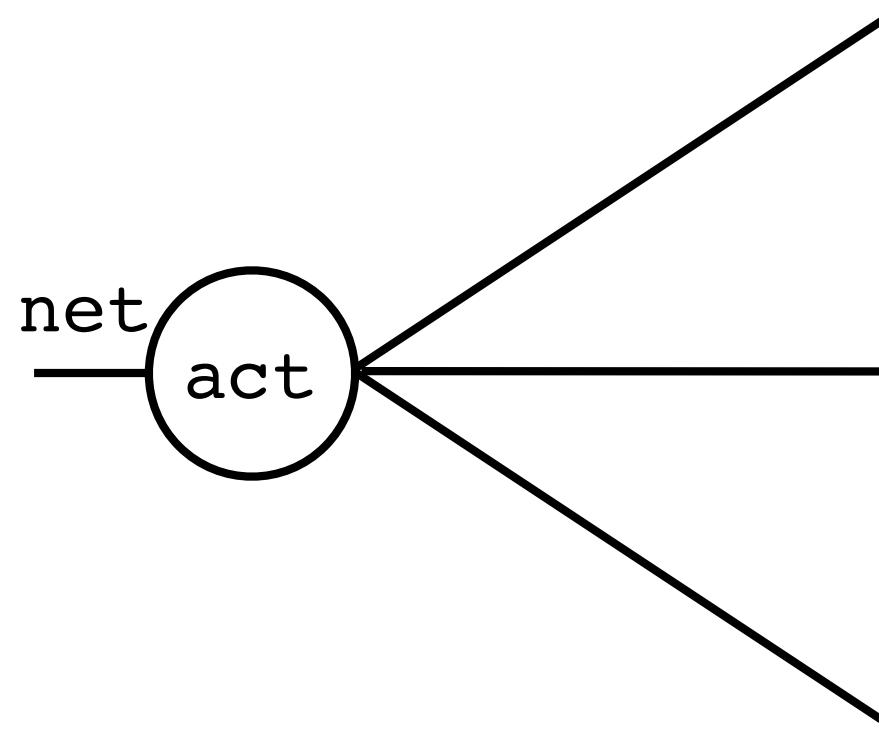
so for simplicity, we allow the same unit to be either excitatory or inhibitory



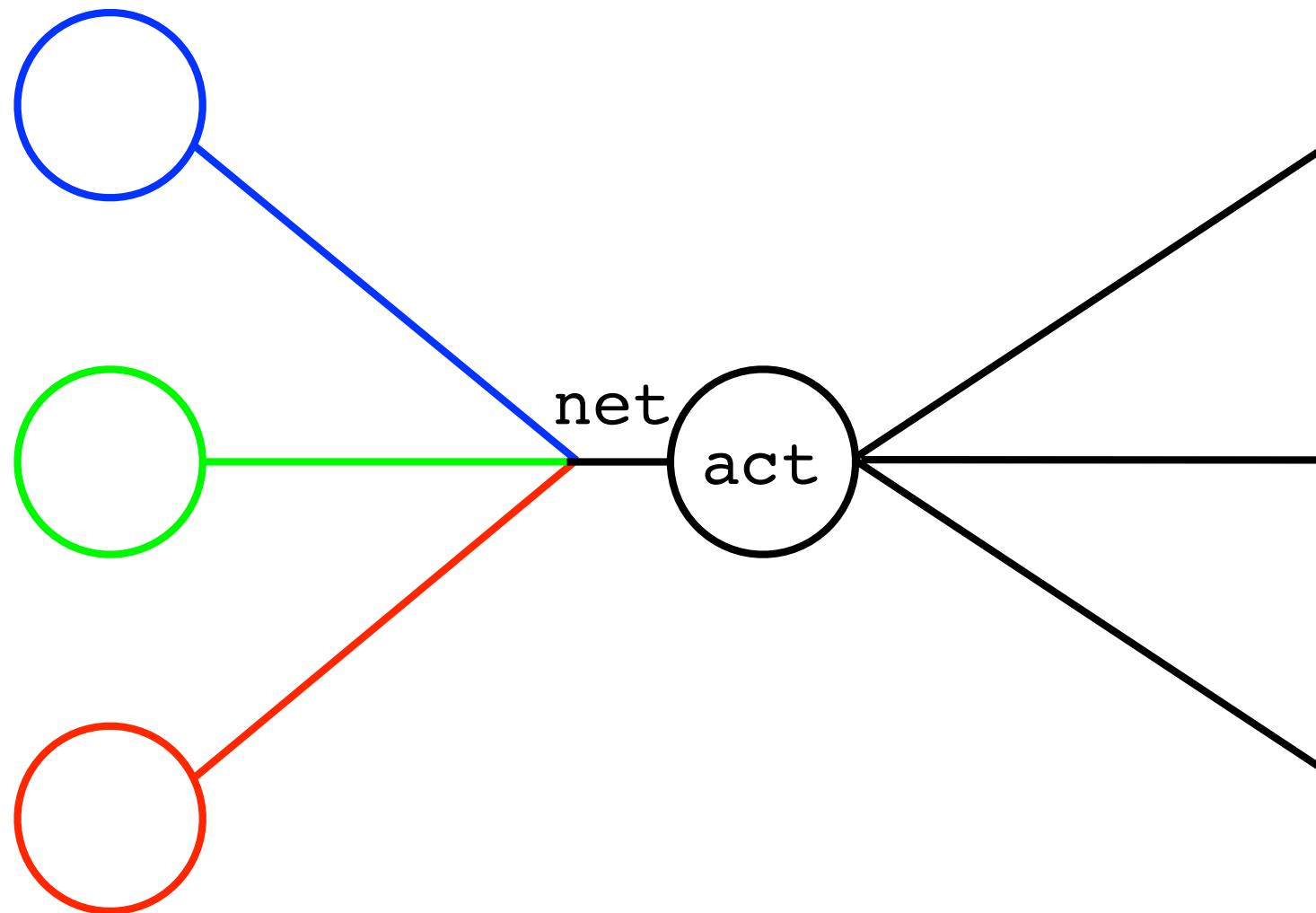
*while the implementation is different whether you allow or don't allow the same unit to be excitatory and inhibitory, the kinds of computations a network performs may well be indistinguishable*

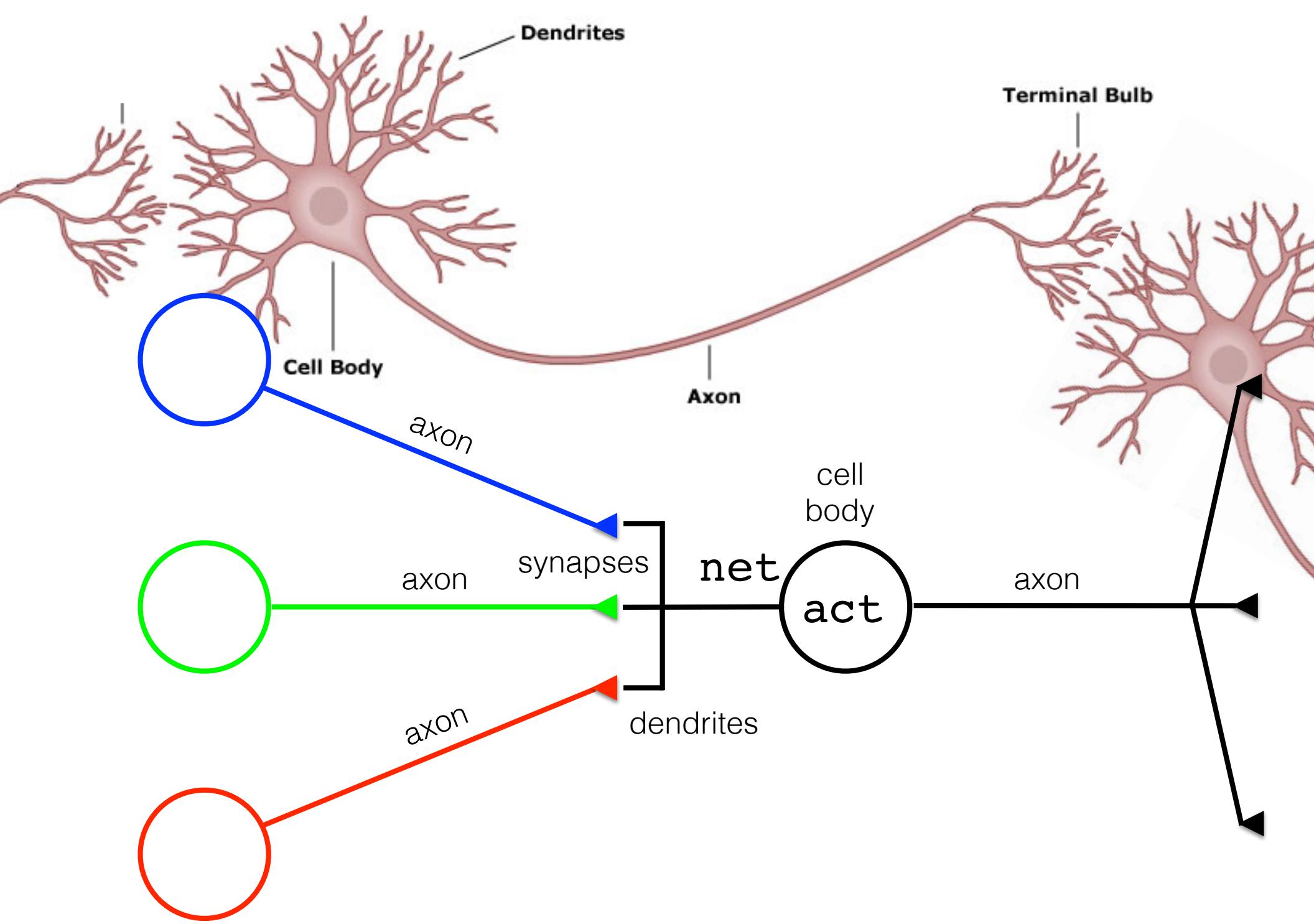


*where does the net input come from?*

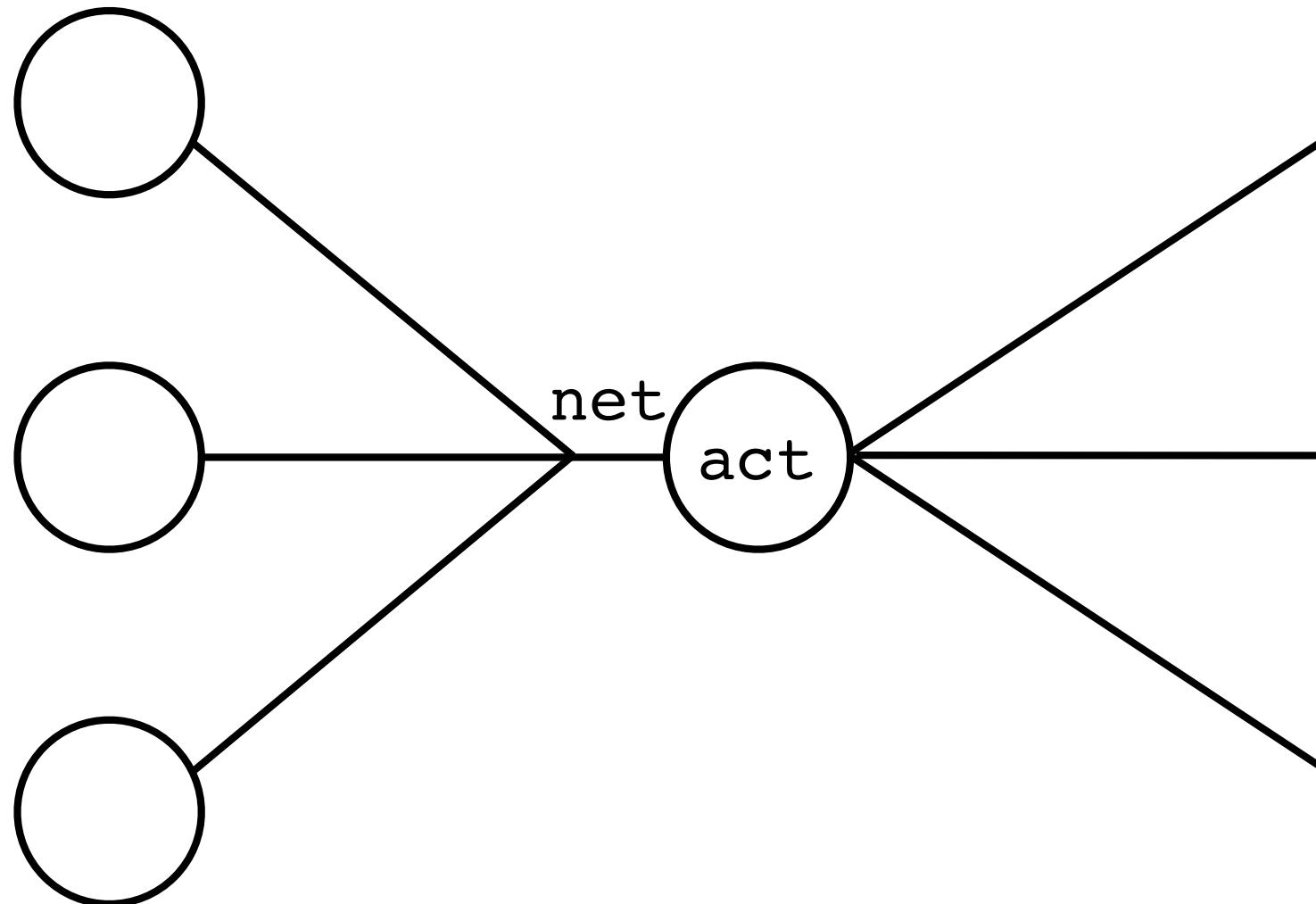


*where does the net input come from?*

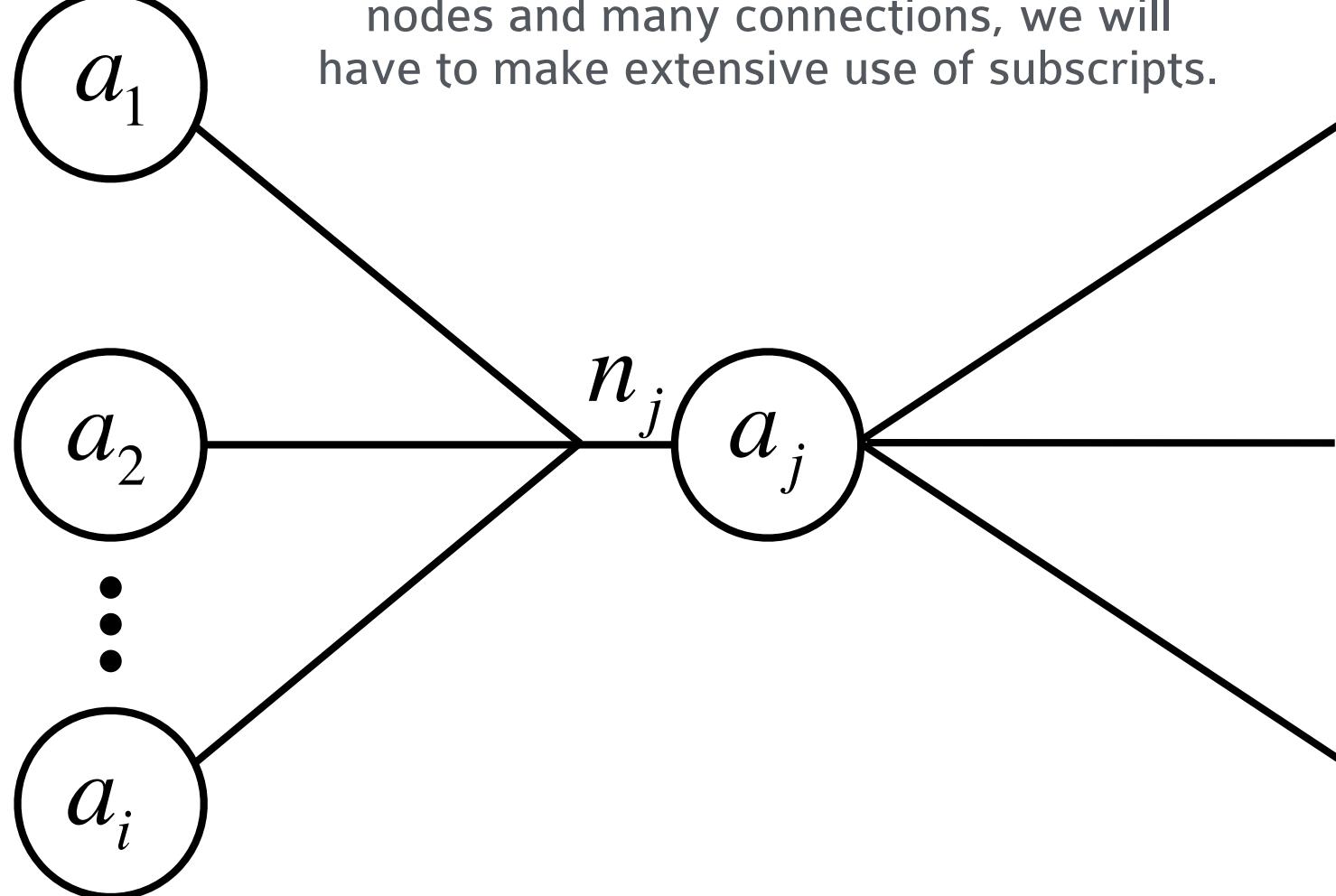




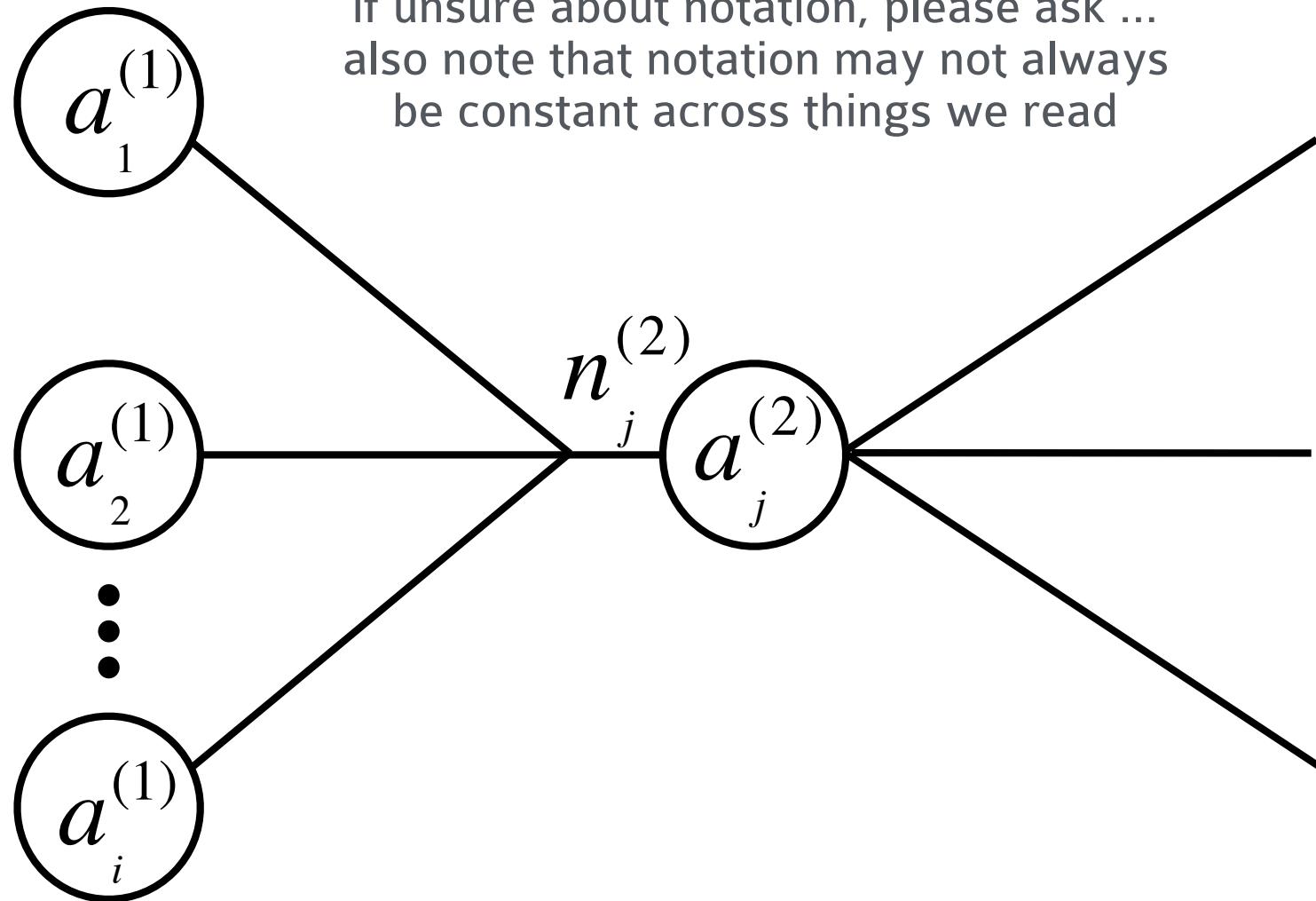
*where does the net input come from?*



# activation of pre-synaptic neurons

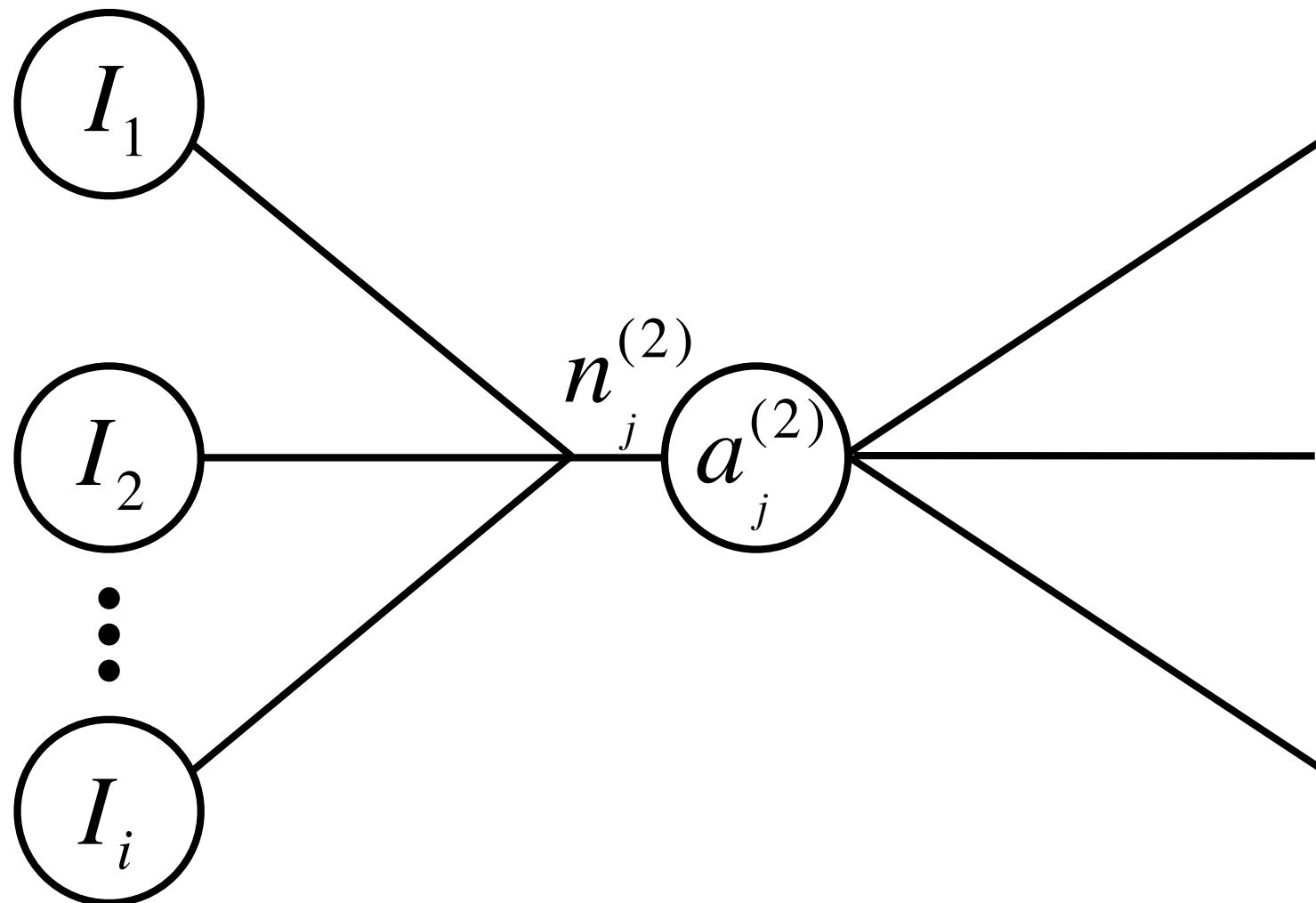


# activation of pre-synaptic neurons

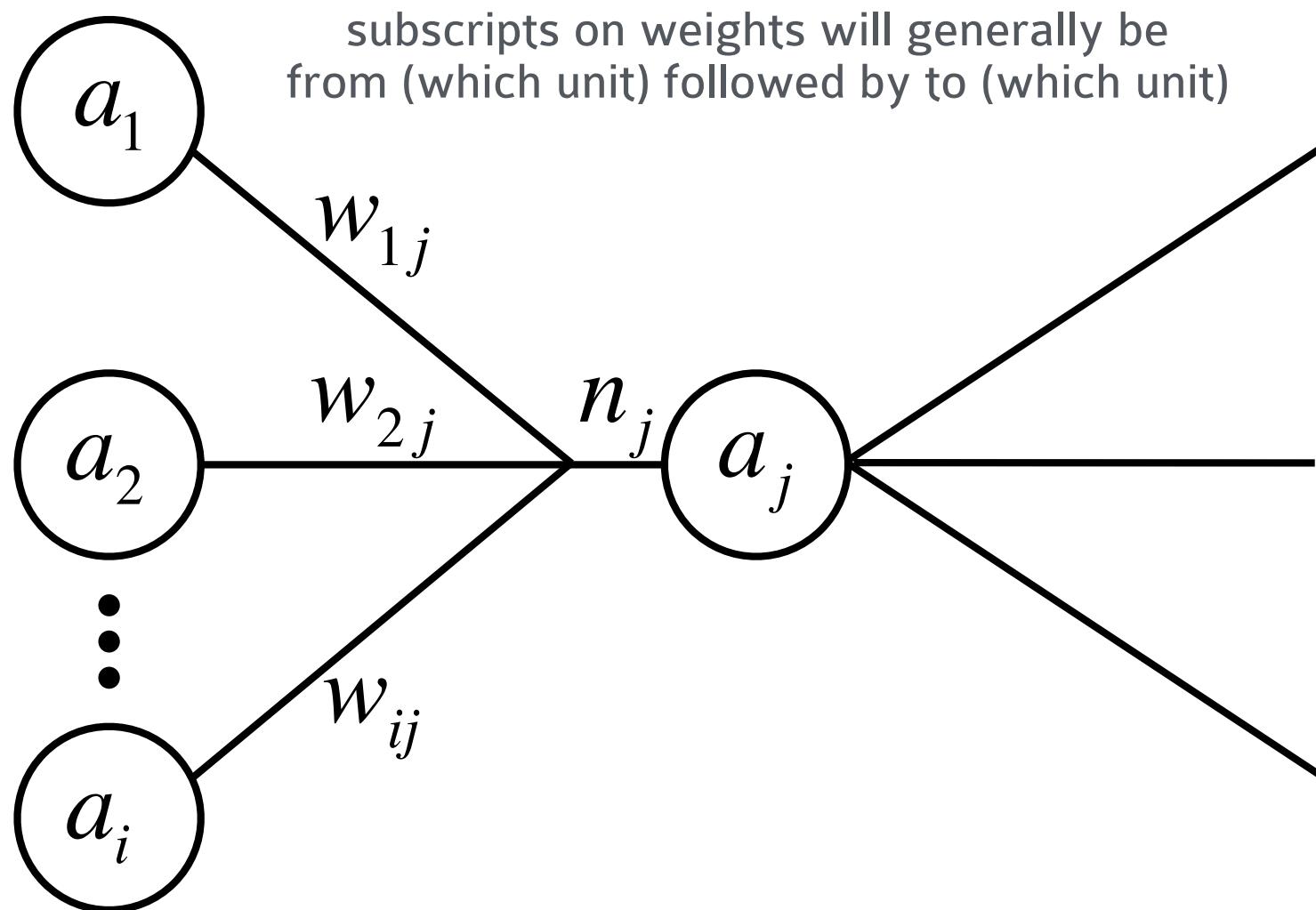


and sometimes superscripts as well ...  
if unsure about notation, please ask ...  
also note that notation may not always  
be constant across things we read

inputs clamped  
onto network



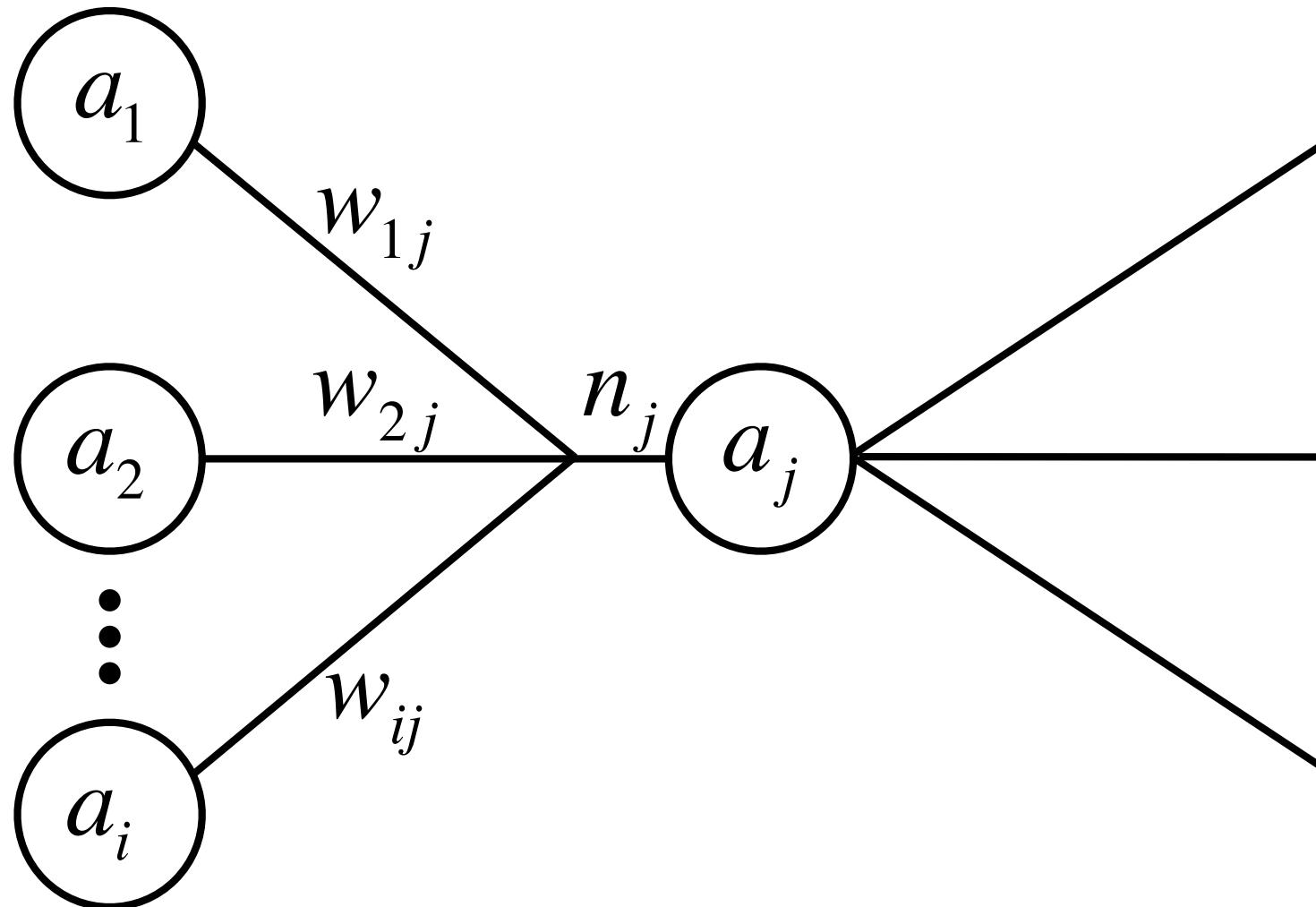
weight of  
synaptic  
connections



impact of one pre-synaptic neuron

$$a_i w_{ij}$$

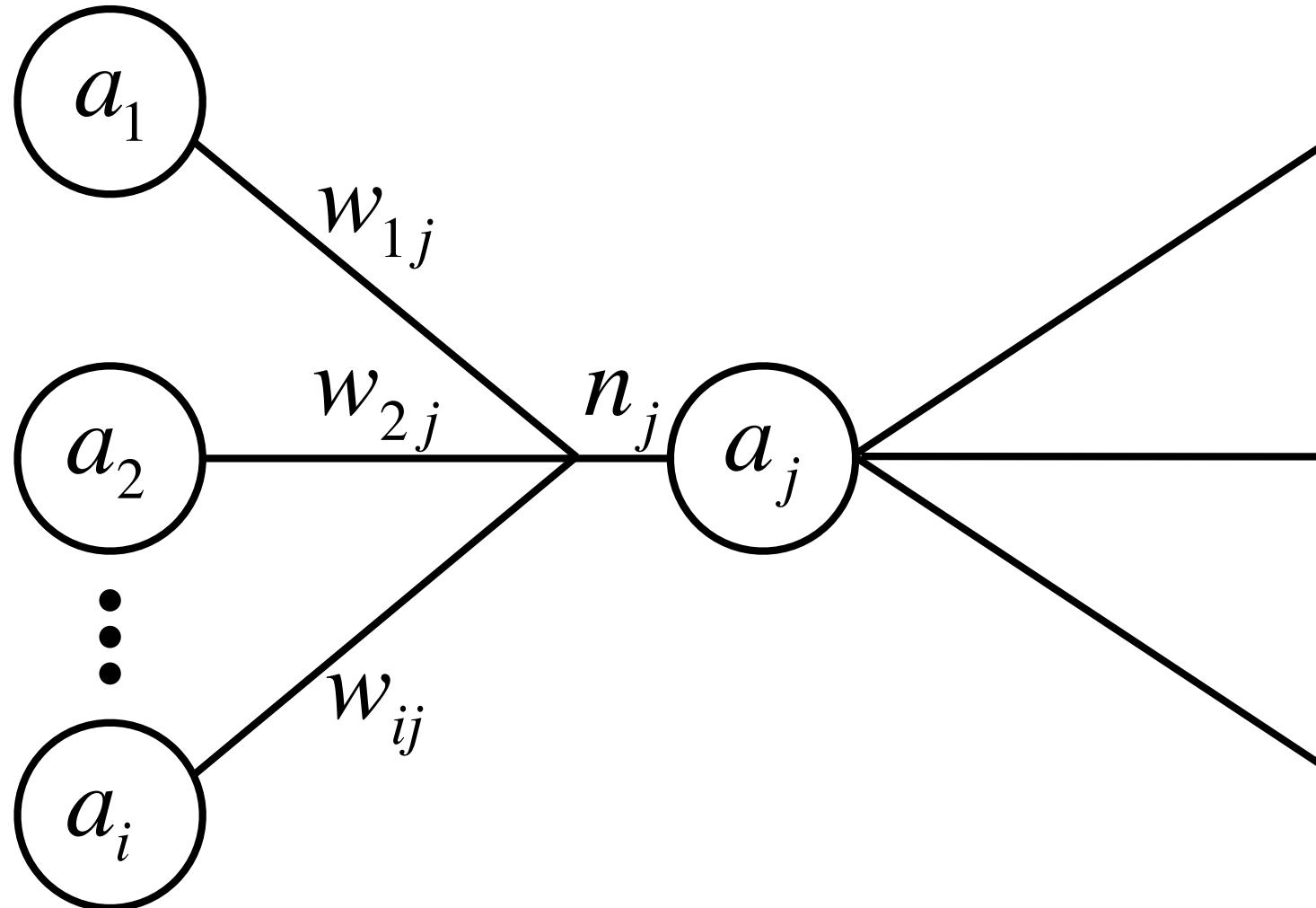
**multiplicatively varying  
strength of connection  
based on number/strength  
of synapses**



**multiplicatively varying  
strength of connection  
based on number/strength  
of synapses**

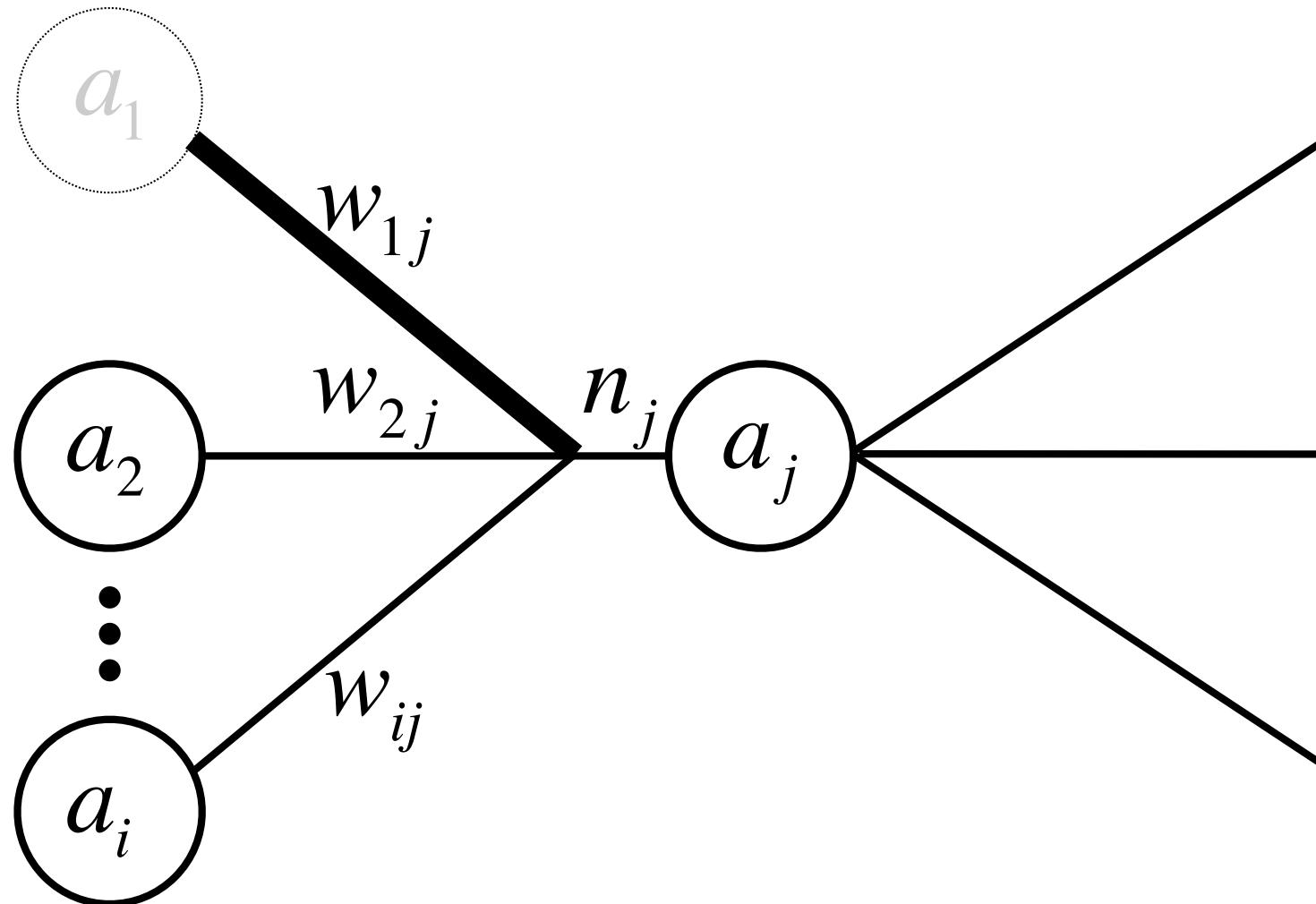
why is it multiplicative  
and not additive?

*multiplication is more  
than just repeated addition*



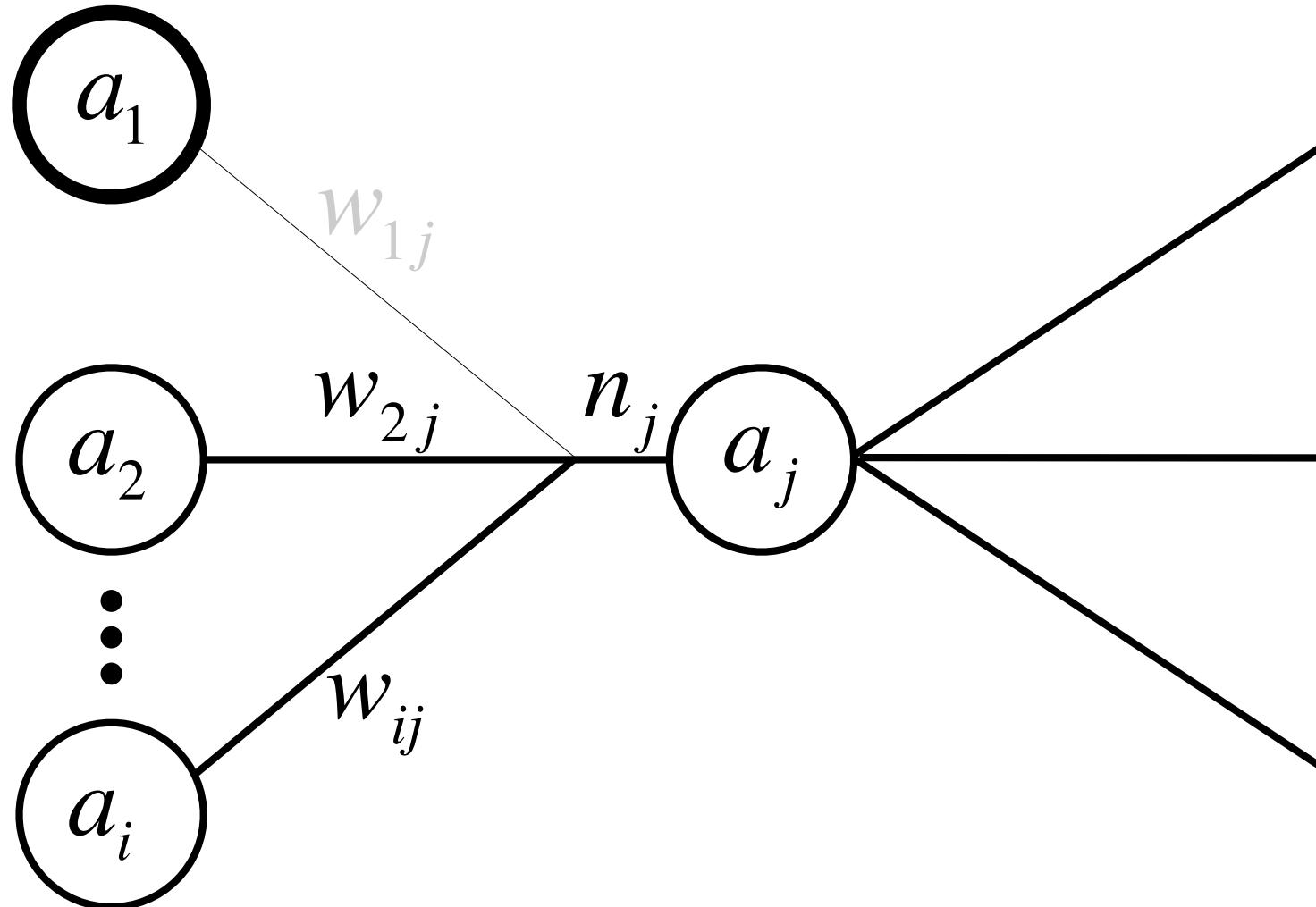
if the pre-synaptic neuron  
is inactive, it does not matter  
how strong the connection

**multiplicatively varying  
strength of connection  
based on number/strength  
of synapses**



if the connection is weak or absent entirely, it does not matter if the pre-synaptic neuron is active or not

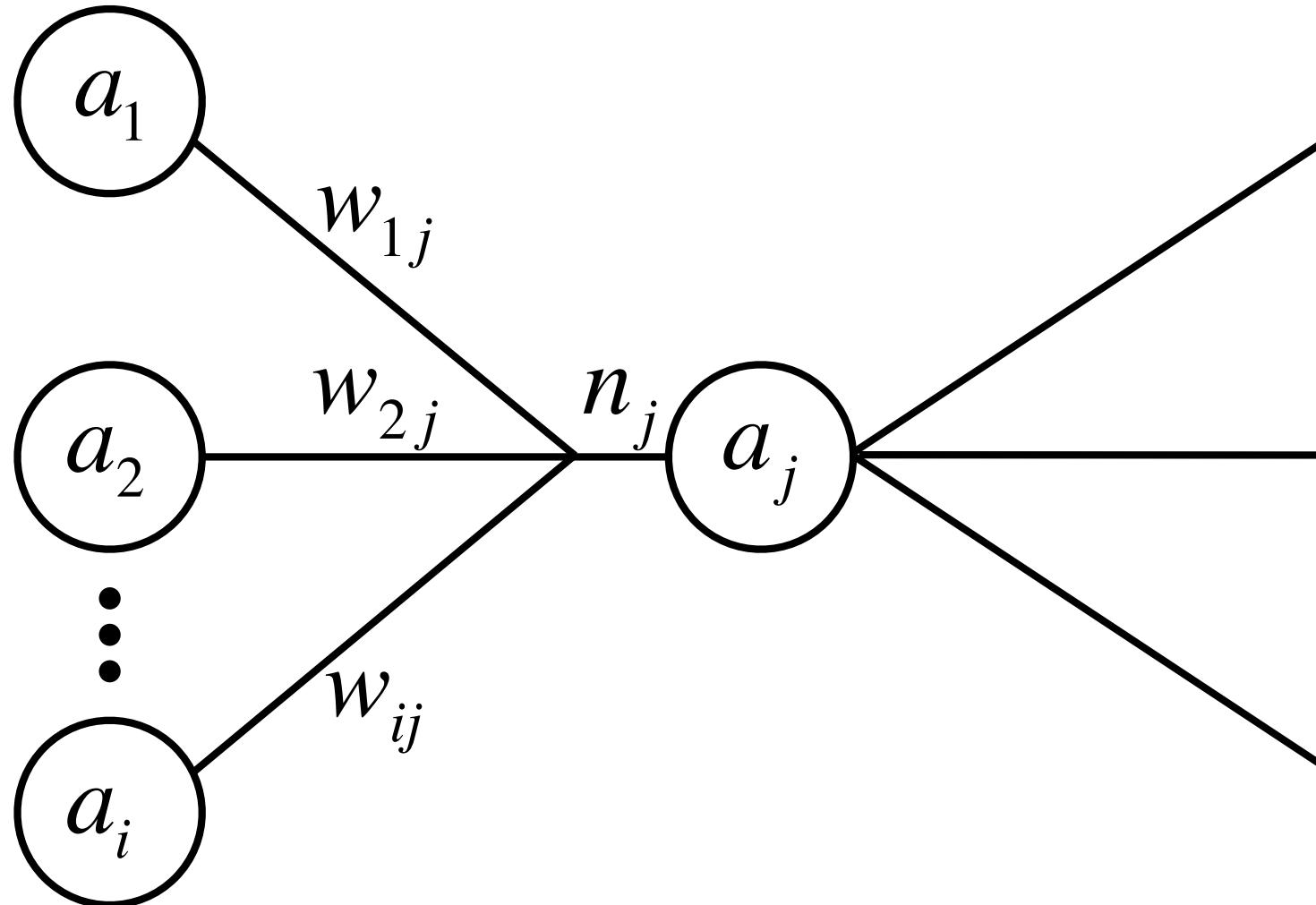
**multiplicatively varying strength of connection based on number/strength of synapses**



**inputs integrate  
at the cell body  
- they are added  
together**

net input sums the weighted inputs

$$n_j = \sum_i a_i w_{ij}$$



let's take a look at this equation

$$n_j = \sum_i a_i w_{ij}$$

let's take a look at this equation

$$n_j = \sum_i a_i w_{ij}$$

$$a = [a_1, a_2, \dots, a_m] \quad \text{activation of all the input nodes}$$

$$w_j = [w_{1j}, w_{2j}, \dots, w_{mj}] \quad \text{all weights going to 2nd layer node j}$$

let's take a look at this equation

$$n_j = \sum_i a_i w_{ij}$$

$$a = [a_1, a_2, \dots, a_m]$$

$$w_j = [w_{1j}, w_{2j}, \dots, w_{mj}]$$

```
n = 0
for i in np.arange(len(a)):
    n += a[i]*wj[i]
```

let's take a look at this equation

$$n_j = \sum_i a_i w_{ij}$$

$$a = [a_1, a_2, \dots, a_m]$$

$$w_j = [w_{1j}, w_{2j}, \dots, w_{mj}]$$

```
n = sum(a*wj)
```



element-wise multiplication of numpy arrays  
(different from Matlab, which requires .\* operator)

let's take a look at this equation

$$n_j = \sum_i a_i w_{ij}$$

$$a = [a_1, a_2, \dots, a_m]$$

$$w_j = [w_{1j}, w_{2j}, \dots, w_{mj}]$$

$$n_j = a \cdot w_j$$

```
import numpy as np  
n = np.dot(a, wj)
```

dot product