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## Team Note of Deobureo Minkyu Party

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## Contents

**ALL BELOW HERE ARE USELESS IF YOU READ THE STATEMENT WRONG****1 Flows, Matching****1.1 Hopcroft-Karp Bipartite Matching**

```

cpp const int MAXN = 50005, MAXM = 50005; vector<int> gph[MAXN]; int dis[MAXN],
l[MAXN], r[MAXM], vis[MAXN]; void clear() for(int i=0; i<MAXN; i++) gph[i].clear(); void
add_edge(int l, int r) gph[l].push_back(r); bool bfs(int n) queue < int > que; bool ok = 0; memset(dis, 0, sizeof(dis)); for(int i=0; i<n; i++) dis[i] = 1; void dfs(int x, int n) if(chk[x]) return; chk[x] = 1; for(auto i : gph[x]) chk[i + n] = 1; dfs(r[i], n); vector<int> int > getcover(int n, int m) // solve min. vertex cover match(n); memset(chk, 0, sizeof(chk)); for(int i=0; i<n; i++)

```

**1.2 Dinic's Algorithm**

```

cpp const int MAXN = 505; struct edge { int pos, cap, rev; }; vector<edge> gph[MAXN]; void clear() for(int i=0; i<MAXN; i++) gph[i].clear(); void
add_edge(int s, int t, int x) gph[s].push_back({t, x, (int)gph[t].size()}); gph[t].push_back({s, 0, (int)gph[s].size() - 1});

```

**1.3 Min Cost Max Flow**

```

cpp const int MAXN = 100; struct edge { int pos, cap, rev, cost; }; vector<edge> gph[MAXN]; void clear() for(int i=0; i<MAXN; i++) gph[i].clear(); void
add_edge(int s, int t, int x, int c) gph[s].push_back({t, x, (int)gph[t].size(), c}); gph[t].push_back({s, 0, (int)gph[s].size(), -c});

```

**1.4 Hell-Joseon style MCMF**

```

cpp const int MAXN = 100; struct edge { int pos, cap, rev, cost; }; vector<edge> gph[MAXN]; void clear() for(int i=0; i<MAXN; i++) gph[i].clear(); void
add_edge(int s, int t, int x, int c) gph[s].push_back({t, x, (int)gph[t].size(), c}); gph[t].push_back({s, 0, (int)gph[s].size(), -c});

```

**1.5 Circulation Problem**

```

cpp maxflow mf; lint lsum; void clear() lsum = 0; mf.clear(); void
add_edge(int s, int t, int l, int r) lsum += l; mf.add_edge(s + 2, e + 2, r - l); mf.add_edge(0, e + 2, l); mf.add_edge(s + 2, t + 2, l);

```

**1.6 Min Cost Circulation**

```

cpp // Cycle canceling (Dual of successive shortest path) // Time complexity is ridiculously high (F *
maxC * nm^2). But runs reasonably in practice (V = 70 in 1s) struct edge { int pos, cap, rev, cost; }; vector<edge> gph[MAXN]; void clear() for(int i=0; i<MAXN; i++) gph[i].clear(); void add_edge(int s, int t, int x, int c) gph[s].push_back({t, x, (int)gph[t].size(), c}); gph[t].push_back({s, 0, (int)gph[s].size(), -c});

```

**1.7 Gomory-Hu Tree**

```

cpp struct edge { int s, e, x; }; vector<edge> eds; maxflow mf; void clear() eds.clear(); void
add_edge(int s, int t, int x) eds.push_back({s, t, x}); bool vis[MAXN]; void dfs(int x) if(vis[x]) return; vis[x] = 1; for(auto i : eds[x]) pi > solve(int n) // i - j cut : i - j minimum edge cost. 0 based. vector<int> ret(n); // if i > 0, stores pair(parent, cost);

```

## 1.8 Blossom Algorithm for General Matching

```
cpp const int MAXN = 2020 + 1; // 1-based Vertex index
int vis[MAXN], par[MAXN], orig[MAXN], match[MAXN], aux[MAXN], t, N;
vector<int> conn[MAXN]; queue<int> Q; void addEdge(int u, int v) {
  conn[u].push_back(v); conn[v].push_back(u); void init(int n) { N = n; t = 0;
  for(int i = 0; i <= n; ++i) conn[i].clear(); }
```

## 1.9 Blossom Algorithm for Weighted General Matching

```

cpp // N3(but fast in practice) static const int INF = INT_MAX; static const N =
514; struct edge { int u, v, w; edge(int ui, int vi, int wi) : u(ui), v(vi), w(wi); int n, nx; edge[N]
2][N * 2]; int lab[N * 2]; int match[N * 2], slack[N * 2], st[N * 2], pa[N * 2]; int floy from[N *
2][N + 1], S[N * 2], vis[N * 2]; vector < int > flo[N * 2]; queue < int >
q; int e_delta(const edge &e) { return lab[e.u] + lab[e.v] - g[e.u][e.v].w * 2; void update_s(int, int) if (!slack[x])
long long, int > solve() { memset(match + 1, 0, sizeof(int) * n); nx = n; int m_matches = 0; long long tot_w eight

```

## 2 Graph

## 2.1 2-SAT

```
cpp strongly_connected_scc; intn; // = number of clauses void init(intn) scc.clear(); n = n; int NOT(int x) ret
bool > res) res.resize(n); scc.get_scc(2 * n); for(int i = 0; i < n; i++) if(scc.comp[i] == scc.comp[NOT(i)])
```

## 2.2 BCC

```
cpp void color(int x, int p) if(p) bcc[p].pushback(x); cmp[x].pushback(p); for(auto i :
gph[x]) if(cmp[i].size()) continue; if(low[i] >= dfn[x]) bcc[+ + c].pushback(x); cmp[x].pushback(c); color(i,
```

## 2.3 Splay Tree + Link-Cut Tree

```

cpp // Checklist 1. Is it link cut, or splay? // Checklist 2. In link cut, is son always root?
void rotate(node *x) if(!x->l)p return; push(x->l,p); // if there's lazy stuff push(x); node *p = x->l,p;
bool isleft = (p->l == x); node *b = (isleft?x->r : x->l); x->p = p->p; if(x->p->l == x)
p->p->l = p; else p->p->r = p; if(x->p->l == x) if(x->p->r == p) p->p->r = p; else if(x->p->r == p)
p->p->r = p; if(isleft)if(b)b->p = p;p->l = b;p->p = x;x->r = p;elseif(b)b->p = p;p->r = b;p->p =
p)root = x; //IFYOUARESPLAYTREEif(p->pp)//IFYOUARELINKCUTTREEx->pp = p->p->p;
x)while(x->p)node *p = x->p; node *g = p->p; if(g)if((p->l == x)(g->l == p))rotate(x); else
x)splay(x); push(x); if(x->r)x->r->pp = x; x->r->p = NULL; x->r = NULL;pull(x); while
root(node * x)access(x); while(x->l)push(x); x = x->l; access(x); return x; node * par(node *
x)access(x); if(!x->l)return NULL; push(x); x = x->l; while(x->r)push(x); x = x->r; access(x);
lca(node*s, node*t)access(s); access(t); splay(s); if(s->pp == NULL)return s; returns->pp; void link
par, node*son)access(par); access(son); son->rev = 1; //remove if needed push(son); son->l = par; par->
p)access(p); push(p); if(p->l)p->l->p = NULL; p->l = NULL; pull(p);

```

## 2.4 Offline Dynamic MST

```

    cpp int n, m, q; int st[MAXN], ed[MAXN], cost[MAXN], chk[MAXN]; pi qr[MAXN];
    bool cmp(int a, int b) return pi(cost[a], a) < pi(cost[b], b);
    void contract(int s, int e, vector<int> v, vector<int> mustst, vector<int> maybest) {
        sort(v.begin(), v.end(), cmp); vector<int> snapshot; for(int i = s; i <= e; i++) {
            int j = v[i]; if(st[j] == e) cost[qr[s].first] = qr[s].second; if(st[qr[s].first] == ed[qr[s].first]) printf("return; int minv = qr[s].second; for(auto i : v) minv = min(minv, cost[i]); printf("return; int m = (s+e)/2; vector<int> lv = v, rv = v; vector<int> mustst, maybest; for(int i = m + 1; i <= e; i++) {
                chk[qr[i].first]--; if(chk[qr[i].first] == 0) lv.push_back(qr[i].first); vector<int> pi = snapshot; contract(s, m, lv, mustst, maybest); lntlcv = cv; for(auto i : mustst) lcv += cost[i]; disj.uni(st[i], ed[i], snapshot); solve(s, m, maybest, lcv); disj.revert(snapshot); mustst.clear(); n += 1; i <= e; i++) {
                chk[qr[i].first]--; if(chk[qr[i].first] == 0) rv.push_back(qr[i].first); lntrcv

```

```

cv; contract(m + 1, e, rv, mustmst, maybemst); for(auto i : mustmst) rcv +
cost[i], disj.uni(st[i], ed[i], snapshot); solve(m + 1, e, maybemst, rcv); disj.revert(snapshot); for(int i =
s; i <= m; i++) chk[qr[i].first]++;
int main() scanf("%d", &n); vector<int> ve; for(int i=0; i<n; i++) scanf("%d", &ve[i]);
ear[i].match[i] = 0; int p = 0; add_argument(int v, int t) int pv = v, nv; do pv = par[v]; nv = match[pv].match
i++; match[qr[i].first] = par[qr[i].first]++; disj.init(n); for(int i=0; i<n; i++) if(chk[i])
ve.push_back(i); solve(0, q - 1, ve, 0);

```

## 2.5 Dominator Tree

```

cpp vector<int> E[MAXN], RE[MAXN], rdom[MAXN];
int S[MAXN], RS[MAXN], cs; int par[MAXN], val[MAXN], sdom[MAXN], rp[MAXN], dom[MAXN];
double (s[u], s[par[u], g], slack[u], x]) & slack for (int i = 0; i < slack[i]; i++) if (s[u] < s[par[u], g] + slack[i]) {
  s[u] = s[par[u], g] + slack[i]; x = x + s[u] * E[par[u], g] * slack[i]; clear(); i = 0; }
for (int i = 0; i < s[u]; i++) if (s[u] < s[par[u], g] + slack[i]) {
  s[u] = s[par[u], g] + slack[i]; x = x + s[u] * E[par[u], g] * slack[i]; clear(); i = 0; }
addEdge(int x, int y) E[x].pushBack(y); void Union(int x, int y) par[x] = y; int Find(int x, int c)
if (par[x] == x) return c - 1; x; int p = Find(par[x], 1); if (p == -1) return c * par[x] : val[x]; if (sdom[val[x]] >
up) / Calculate idoms dfs(s); for (int i = cs; i < -) for (int i = RE[i].sdom[i] = min(sdom[i], sdom[Find(e)]); if (

```

## 2.6 Global Min-Cut

```

2.6 Global Min-Cut
nx >= n? (x - n) : (x + n); void addEdge(int x, int y) // input xtodenote NOT if ((x >> 31) 1) x = (x) + n; if ((y >>
return 0; if (scanning) { if (scase(n, NOTs)) { int i; vector < int > adj; vector < int > vis; vector < int > dist(n); int mincut = 1e9; while (true) { int pos = -1, cur = -1e9; for (inti = 0; i < n; i++) if (
vector < int > adj) if (n <= 1) return 0; vector < int > vis(n); int ans = 1e9; for (inti = 0; i < n - 1; i++) { int s

```

## 2.7 Edmond's Directed MST

```
// Should be revised.cpp // starts from node 0. assumes there exists at least one dmst. // edge  
is reversed : if there is edge s -> e, INSERT IN gph[e] struct edge int to, cost, id; ; using elist =  
vector<edge>; void dmst(vector<elist>& g, vector<jint>& res) const int n = g.size(); vector<edge*> to(n);  
vector<jint> u(n, 0); for (int i = 1; i <= n; ++i) int mn = g[i][0].cost; for (int j = 0; j < g[i].size(); ++j)  
mn = min(mn, g[i][j].cost); for (int j = 0; j < g[i].size(); ++j) if (g[i][j].cost == mn) to[i] = g[i][j];  
g[i][j].cost -= mn; for (int i = 1; i <= n; ++i) if (u[i]) continue; int x = i; vector<jint> order(1, x);  
u[x] = 1; while (!to[x].to || !u[to[x].to]) {x = to[x].to; u[x] = 1; order.push_back(x);} int y =  
to[x].to; pp = to[x].to; for (int i = cycle.begin(), it = cycle.end(); it != cycle.end(); ++it) if (cycle.size() ==  
0) continue; rotate(y, to[x], void&ress(nodes)); for(int j = 0; j < cycle.size(); ++j) incycle[cycle[j]] =  
1; vector<int> nw,d(n); for(int i = 1; i <= n; ++i) nw[i] += r-j; d[i] += j; p = N;  
x[1]+incycle[j]; intnn = n - cycle.size(); vector<elid> elist; gn(nn+1+j); for(int j = 1; j <= n-1;  
++j){if(!incycle[j])for(intk = 0;k < g[j].size();++k){if(!incycle[g[j][k].to])gn[nn].push_back(nw;d[g[j][k].to,g[j][k]  
.id)}used_e(res.begin(),res.end());for(intj = 0;j < cycle.size();++j)  
>}bool found = false;for(intk = 0;k < g[cycle[j]].size();++k)found |= used_e.count(g[cycle[j]][k].id);if(found)
```

## 2.8 Vizing's Theorem

```

cpp namespace Vizing // returns edge coloring in adjacent matrix G. 1 - based int C[MAXN][MAXN],
G[MAXN][MAXN]; void clear(int N) for(int i=0; i<N; i++) for(int j=0; j<N; j++) C[i][j] = G[i][j]
= 0; void solve(vector<pi>, E, int N, int M) int X[MAXN] = , a; auto update = [](int u) for(X[u].first, G[u][X[u].first], swap(c, a)) { if((this->jump(tst, c), c) == 0) break; } else revert
= c; C[u][c] = v; C[v][c] = u; C[u][p] = C[v][p] = 0; if( p ) X[u] = X[v] = p; else update(u), up-
date(v); return p; ; auto flip = [](int u, int c1, int c2) int p = C[u][c1]; swap(C[u][c1], C[u][c2]); if(
p ) G[u][p] = G[p][u] = c2; if( !C[u][c1] ) X[u] = c1; if( !C[u][c2] ) X[u] = c2; return p; ; for(int i
= 1; i <= N; i++) X[i] = 1; for(int t = 0; t < E.size(); t++) int u = E[t].first, v0 = E[t].second,
v = v0, c0 = X[u], c = c0, d; vector<pi> L; int vst[MAXN] = ; while(!G[u][v0]) L.emplace_back(v, d =
N+u); if(L[0].first == (int)L.size()-1; a >= 0; a-->c = color(u, L[a].first, c); elseif(!C[u][d]) for(a =
(int)L.size()-1; a >= 0; a--)color(u, L[a].first, L[a].second); elseif(vst[d])break; else vst[d] = 1, v =
C[u][d]; if(!G[u][v0])for(; v = flip(v, c, d), swap(c, d)); if(C[u][c0])for(a = (int)L.size()-2; a >= 0L[a].second

```

### 3 Strings

#### 3.1 Aho-Corasick Algorithm

```
cpp const int MAXN = 100005, MAXC = 26; int trie[MAXN][MAXC], fail[MAXN], term[MAXN],
piv; void init(vector<string> &v) memset(trie, 0, sizeof(trie)); memset(fail, 0, sizeof(fail)); memset(term,
0, sizeof(term)); piv = 0; for(auto i : v) int p = 0; for(auto j : i) if(!trie[p][j]) trie[p][j] = ++piv; p
= trie[p][j]; term[p] = 1; queue<int> que; for(int i=0; i<MAXC; i++) if(trie[0][i]) que.push(trie[0][i]);
while(!que.empty()) int x = que.front(); que.pop(); for(int i=0; i<MAXC; i++) if(trie[x][i]) int p =
fail[x]; while(p !& trie[p][i]) p = fail[p]; p = trie[p][i]; fail[trie[x][i]] = p; if(term[p]) term[trie[x][i]] = 1;
que.push(trie[x][i]); bool query(string s) int p = 0; for(auto i : s) while(p !& trie[p][i]) p = fail[p]; p =
trie[p][i]; if(term[p]) return 1; return 0;
```

#### 3.2 Suffix Array

```
cpp const int MAXN = 500005; int ord[MAXN], nord[MAXN], cnt[MAXN], aux[MAXN]; void solve(int
n, char *str, int *sfx, int *rev, int *lcp) int p = 1; memset(ord, 0, sizeof(ord)); for(int i=0; i<n; i++) sfx[i] =
i; ord[i] = str[i]; int pnt = 1; while(1) memset(cnt, 0, sizeof(cnt)); for(int i=0; i<n; i++) cnt[ord[min(i+p,
n)]]++; for(int i=1; i<=n — i=255; i++) cnt[i] += cnt[i-1]; for(int i=n-1; i<=0; i-) aux[-cnt[ord[min(i+p,
n)]]] = i; memset(cnt, 0, sizeof(cnt)); for(int i=0; i<n; i++) cnt[ord[i]]++; for(int i=1; i<=n — i=255;
i++) cnt[i] += cnt[i-1]; for(int i=n-1; i<=0; i-) sfx[-cnt[ord[aux[i]]]] = aux[i]; if(pnt == n) break; pnt = 1;
nord[sfx[0]] = 1; for(int i=1; i<n; i++) if(ord[sfx[i-1]] != ord[sfx[i]] — ord[sfx[i-1] + p] != ord[sfx[i] + p])
pnt++; nord[sfx[i]] = pnt; memcpy(ord, nord, sizeof(int) * n); p *= 2; for(int i=0; i<n; i++) rev[sfx[i]] =
i; int h = 0; for(int i=0; i<n; i++) if(rev[i]) int prv = sfx[rev[i] - 1]; while(str[prv + h] == str[i + h]) h++;
lcp[rev[i]] = h; h = max(h-1, 0);
```

#### 3.3 Manacher's Algorithm

```
cpp const int MAXN = 1000005; int aux[2 * MAXN - 1]; void solve(int n, int *str, int *ret) // *ret
: number of nonobvious palindromic character pair for(int i=0; i<n; i++) aux[2*i] = str[i]; if(i != n-1)
aux[2*i+1] = -1; int p = 0, c = 0; for(int i=0; i<2*n-1; i++) int cur = 0; if(i == p) cur = min(ret[2 * c -
i], p - i); while(i - cur - 1 <= 0 i + cur + 1 < 2*n-1 aux[i-cur-1] == aux[i+cur+1]) cur++; ret[i] = cur;
if(i + ret[i] < p) p = i + ret[i]; c = i;
```

#### 3.4 Suffix Array (Linear time)

```
Should be revised.cpp class SuffixArray public: int A[7 * N / 10],
B[7 * N / 10], cnt[N + 2], SAV[N]; int mem[5 * N]; int* mempt =
mem; void clear(int n) int *ptr = mem; while(ptr != mempt) *ptr = 0; ptr++; mempt = mem; for(int i = 0; i < n; i++)
mloc(size_t sz) int *ret = mempt; mempt = mempt + sz; return ret; void rsort(int *a, int *b, int *
dat, int n, int k) for(int i = 0; i <= k; i++) cnt[i] = 0; for(int i = 0; i < n; i++) SAV[i] = dat[a[i]], cnt[SAV[i]]++;
define I(x) ((x)define I2(x) (x)num1)?(3*x+1):(3*(x-num1)+2) static int cmp(int x, int y, int str[], int
A[], int num1) if (x if (y else return str[x] < str[y] — str[x] == str[y] A[I(x+1)] < A[I(y+1)]; else
return str[x] > str[y] — str[x] == str[y] cmp(x+1, y+1, str, A, num1); void make(int* str, int* sa,
int n, int k) if (n == 0) return; int num1 = (n + 2) / 3, num2 = n / 3; int num = num1 + num2; str[n]
= str[n + 1] = str[n + 2] = 0; int *nsa = mloc(num), *nstr = mloc(num + 3);
for (int i = 0, j = 0; i < n; i++) if (i if (n rsort(A, B, str + 2, num, k); rsort(B, A, str + 1, num, k);
rsort(A, B, str, num, k);
int cnt = 1; nstr[I(B[0])] = 1; for (int i = 1; i < num; i++) int c = B[i], p = B[i - 1]; if (str[p] != str[c]
— str[p + 1] != str[c + 1] — str[p + 2] != str[c + 2]) cnt++; nstr[I(c)] = cnt; if (cnt == num) for
(int i = 0; i < num; i++) nsa[nstr[i] - 1] = i; else make(nstr, nsa, num, cnt);
for (int i = 0, j = 0; i < num; i++) if (nsa[i] < num1) A[j++] = 3 * nsa[i]; rsort(A, B, str, num1, k); for
(int i = 0; i < num; i++) A[nsa[i]] = i, nsa[i] = I2(nsa[i]); A[num] = -1; merge(B, B + num1, nsa + (n
return cmp(x, y, str, A, num1); ); return; sa;
```

#### 3.5 eertree

```
cpp int nxt[MAXN][26]; int par[MAXN], len[MAXN], slink[MAXN], ptr[MAXN], diff[MAXN], se-
ries[MAXN], piv; void clear(int n = MAXN) memset(par, 0, sizeof(int) * n); memset(len, 0, sizeof(int)
* n); memset(slink, 0, sizeof(int) * n); memset(nxt, 0, sizeof(int) * 26 * n); piv = 0; void init(int
n, char *a) par[0] = 0; par[1] = 1; a[0] = -1; len[0] = -1; piv = 1; int cur = 1; for(int i=1; i<n;
i++) while(a[i] != a[i - len[cur] - 1]) cur = slink[cur]; if(!nxt[cur][a[i]]) nxt[cur][a[i]] = ++piv; par[piv]
= cur; len[piv] = len[cur] + 2; int lnk = slink[cur]; while(a[i] != a[i - len[lnk] - 1]) lnk = slink[lnk];
if(nxt[lnk][a[i]]) lnk = nxt[lnk][a[i]]; if(len[piv] == 1 — lnk == 0) lnk = 1; slink[piv] = lnk; diff[piv]
= len[piv] - len[lnk]; if(diff[piv] == diff[lnk]) series[piv] = series[lnk]; else series[piv] = piv; cur =
nxt[cur][a[i]]; ptr[i] = cur; int query(int s, int e) int pos = ptr[e]; while(len[pos] <= e - s + 1) if(len[pos]
len[series[pos]] <= e - s + 1) return true; pos = series[pos]; pos = slink[pos]; return false; vector<pi>
minimumpartition(int n) //(oddmin, evenmin)vector < pi > dp(n+1); vector < pi > seriesans(n+10); dp[0] =
```

#### 3.6 Circular LCS

```
cpp string s1, s2; int dp[4005][2005]; int nxt[4005][2005]; int n, m; void reroot(int px) int py = 1; while(py
j = m nxt[px][py] != 2) py++; nxt[px][py] = 1; while(px < 2 * n py < m) if(nxt[px+1][py] == 3) px++;
nxt[px][py] = 1; else if(nxt[px+1][py+1] == 2) px++; py++; nxt[px][py] = 1; else py++; while(px < 2 *
n nxt[px+1][py] == 3) px++; nxt[px][py] = 1;
int track(int x, int y, int e) // use this routine to find LCS as string int ret = 0; while(y != 0 x != e)
if(nxt[x][y] == 1) y--; else if(nxt[x][y] == 2) ret += (s1[x] == s2[y]), x--, y--; else if(nxt[x][y] == 3) x--;
return ret;
int solve(string a, string b) n = a.size(), m = b.size(); s1 = "" + a + a; s1 = "" + b; for(int i=0; i<2*n;
i++) for(int j=0; j<m; j++) if(j == 0) nxt[i][j] = 3; continue; if(i == 0) nxt[i][j] = 1; continue; dp[i][j]
= -1; if(dp[i][j] < dp[i][j-1]) dp[i][j] = dp[i][j-1]; nxt[i][j] = 1; if(dp[i][j] < dp[i-1][j-1] + (s1[i] == s2[j])) dp[i][j]
= dp[i-1][j-1] + (s1[i] == s2[j]); nxt[i][j] = 2; if(dp[i][j] < dp[i-1][j]) dp[i][j] = dp[i-1][j]; nxt[i][j] = 3; int
ret = dp[n][m]; for(int i=1; i<n; i++) reroot(i), ret = max(ret, track(n+i, m, i)); return ret;
```

### 4 Geometry

#### 4.1 Smallest Enclosing Circle / Sphere

```
cpp namespace cover2doubleleaps = 1e - 9; using Point = complex < double >; struct CirclePointp; doubler; do
namespace cover3ddoubleenclosing_sphere(vector < double > x, vector < double > y, vector < double > z)intn
```

#### 4.2 3D Convex Hull

```
cpp struct vec3 ll x, y, z; vec3(): x(0), y(0), z(0) vec3(ll a, ll b, ll c): x(a), y(b), z(c) vec3 operator*(const
vec3 v) const return vec3(x*v.v.z-z*v.v.y, z*v.v.x-x*v.v.z, x*v.v.y-y*v.v.x); vec3 operator-(const vec3 v) const return
vec3(x-10x, y-7y, z-10z); vec3 operator+(const vec3 v) const return vec3(x+10x, y+7y, z+10z); vec3 operator<
x*v.v.x+y*v.v.y+z*v.v.z; ;
struct face { int a, b; void insert(int x) cnt[a]++; if (x == a) cnt[a] = 1; for (int i = 0; i < cnt[a]; i++) S
x — b == x; void erase(int x) (a == x ? a : b) = -1; int size() return (a != -1) + (b != -1);
E[MAXN][MAXN]; // i < j
struct face vec3 norm; ll disc; int I[3]; ;
face makeface(inti, intj, intk, intii, vector < vec3 > A) // pT * norm < discE[i][j].insert(k); E[i][k].insert(j); E
vector<face> gethull(vector < vec3 > A)intN = A.size(); vector < face > faces; memset(E, -1, sizeof(E)); fo
```

#### 4.3 Dynamic Convex Hull Trick

```
cpp using linet = double; constlinetisquery = -1e18;
struct Line linetm, b; mutablefunction < constLine * () > succ; booloperator <
(constLinerhs)constif(rhs.b != isquery)returnm < rhs.m; constLine * s = succ(); if(!s)return0; linetx = rhs.m
struct HullDynamic : public multiset<Line> // will maintain upper hull for maximum
bool bad(iterator y) auto z = next(y); if (y == begin()) if (z == end()) return 0; re
```

```

turn y-lm == z-lm  y-lb j= z-lb;  auto x = prev(y); if (z == end()) return y-lm == x-
lm  y-lb j= x-lb; return (x-lb - y-lb)*(z-lm - y-lm) l= (y-lb - z-lb)*(y-lm - x-lm);  void
insert(linetm, linetb) auto y = insert(m, b); y- > succ = [=]return next(y) == end()? : *next(y); if (b

```

#### 4.4 Half-plane Intersection

```

cpp const double eps = 1e-8; typedef pair<long double, long double> pi; bool z(long double x)
return fabs(x) < eps; struct line long double a, b, c; bool operator==(const line l) const bool flag1 =
pi(a, b) < pi(0, 0); bool flag2 = pi(l.a, l.b) < pi(0, 0); if(flag1 != flag2) return flag1 < flag2; long
double t = ccw(pi(0, 0), pi(a, b), pi(l.a, l.b)); return z(t) ? c * hypot(l.a, l.b) < l.c * hypot(a, b) :
t < 0; pi slope() return pi(a, b); ; pi cross(line a, line b) long double det = a.a * b.b - b.a * a.b;
return pi((a.c * b.b - a.b * b.c) / det, (a.a * b.c - a.c * b.a) / det); bool bad(line a, line b, line c)
if(ccw(pi(0, 0), a.slope(), b.slope())) == 0) return false; pi crs = cross(a, b); return crs.first * c.a +
crs.second * c.b < c.c; bool solve(vector<line> v, vector<pi> solution) // ax + by = c; sort(v.begin(),
v.end()); deque<line> dq; for(auto i = v) if(!dq.empty()) z(ccw(pi(0, 0), dq.back().slope(), i.slope()))
continue; while(dq.size() <= 2 bad(dq[dq.size()-2], dq.back(), i)) dq.pop_back(); while(dq.size() >=
2bad(i, dq[0], dq[1])dq.pop_front(); dq.push_back(i); while(dq.size() > 2bad(dq[dq.size() -
2], dq.back(), dq[0])dq.pop_back(); while(dq.size() > 2bad(dq.back(), dq[0], dq[1])dq.pop_front(); vector
pi > tmp; for(int i = 0; i < dq.size(); i++)line cur = dq[i], nst = dq[(i + 1)if(ccw(pi(0, 0), cur.slope(), nst.s
tmp; return true;

```

#### 4.5 Point-in-polygon test / Point-to-polygon tangent

```

cpp // C : counter,clockwise(C[0] == C[N]), N >= 3//return highest point in C < -P(clockwise) or -
1 if strictly in P // polygon is strongly convex, C[i]! = Pintconvex_tangent(vector < pi > C, piP, intup =
1) auto sign = [] (lintc) return c > 0? up : c == 0? 0 : -up;; auto local = [] (piP, pia, pib, pic) return sign(ccw(P,

```

## 4.6 kd-tree

```

    cpp typedef pair<int, int> pi; struct node pi pnt; int spl, sx, ex, sy, ey; tree[270000];
    pi a[100005]; int n, ok[270000];
    lint sqr(int x) return 1ll * x * x; bool cmp1(pi a, pi b) return a.j < b.j; bool cmp2(pi a, pi b) return
pi(a.second, a.first) < pi(b.second, b.first);
    // init(0, n-1, 1) : Initialize kd-tree // set dap = INF, and call solve(1, P). dap = (closest point from
P) void init(int s, int e, int p) // Initialize kd-tree int minx = 1e9, maxx = -1e9, miny = 1e9, maxy =
-1e9; int m = (s+e)/2; for(int i=s; i<=e; i++) minx = min(minx, a[i].first); miny = min(miny, a[i].second);
maxx = max(maxx, a[i].first); maxy = max(maxy, a[i].second); tree[p].spl = (maxx - minx < maxy - miny);
sort(a+s, a+e+1, [](const pi a, const pi b) return tree[p].spl ? cmp2(a, b) : cmp1(a, b); ); ok[p] = 1;
tree[p] = a[m], tree[p].spl, minx, maxx, miny, maxy; if(s <= m-1) init(s, m-1, 2*p); if(m+1 <= e) init(m+1,
e, 2*p+1);
    lint dap = 3e18;
    void solve(int p, pi x) // find closest point from point x (L^2) if(x!
= tree[p].pnt)dap = min(dap, sqr(x.first - tree[p].pnt.first) + sqr(x.second -
tree[p].pnt.second)); if(tree[p].spl)if(!cmp2(tree[p].pnt, x))if(ok[2 * p])solve(2 * p, x); if(ok[2 * p + 1])sqr(tr

```

## 5 Math

## 5.1 FFT / NTT

```

    cpp typedef complex<double> base; void fft(vector<base> &a, bool inv) { int n = a.size(), j = 0; vector<base> roots(n/2); for(int i=1; i<n; i++) int bit = (n << 1); while(j <= bit) j -= bit; <<= 1; j += bit; if(i < j) swap(a[j], a[i]); double ang = 2 * acos(-1) / n * (inv ? -1 : 1); for(int i=0; i<n/2; i++) roots[i] = base(cos(ang * i), sin(ang * i)); /* In NTT, let prr = primitive root. Then, int ang = ipow(prr, (mod - 1) / n); if(inv) ang = ipow(ang, mod - 2); for(int i=0; i<n/2; i++) roots[i] = (i ? (1ll * roots[i-1] * ang % XOR Convolution : set roots[*] = 1. OR Convolution : set roots[*] = 1, and do following: if (linv) a[j + k] = u + v; a[j + k + i/2] = u; else a[j + k] = v; a[j + k + i/2] = u - v; */ for(int i=2; i<n; i+=i) int step =

```

```

= n / i; for(int j=0; jjn; j+=i) for(int k=0; kj/2; k++) base u = a[j+k], v = a[j+k+i/2] * roots[step * k];
a[j+k] = u+v; a[j+k+i/2] = u-v; if(inv) for(int i=0; ijn; i++) a[i] /= n; // skip for OR convolution.
d(y)vector<int> ret(n); vector<int> v, w; for(int i=0; i<n; i++) v[i] = a[i], w[i] = b[i]; erase(v.begin(), v.end());
w.erase(w.begin(), w.end()); int n = 2; while(n < v.size() + w.size()) n <<= 1; fv.resize(n); fw.resize(n); fft(fv, 0); fft(fw,
0); for(int i=0; ijn; i++) fv[i] *= fw[i]; fft(fv, 1); vector<int> ret(n); for(int i=0; ijn; i++) ret[i] =
(lint)round(fv[i].real()); return ret; vector<int> multiply(vector<int> v, vector<int> w, lint mod) int n =
2; while(n < v.size() + w.size()) n <<= 1; vector<base> v1(n), v2(n), r1(n), r2(n); for(int i=0; i<v.size());
i++) v1[i] = base(v[i] % 15, v[i] % 32767); for(int i=0; i<w.size()); i++) v2[i] = base(w[i] % 15, w[i] % 32767);
fft(v1, 0); fft(v2, 0); for(int i=0; ijn; i++) int j = (i ? (n - i) : i); base ans1 = (v1[i] + conj(v1[j])) *
base(0.5, 0); base ans2 = (v1[i] - conj(v1[j])) * base(0, -0.5); base ans3 = (v2[i] + conj(v2[j])) * base(0.5,
0); base ans4 = (v2[i] - conj(v2[j])) * base(0, -0.5); r1[i] = (ans1 * ans3) + (ans1 * ans4) * base(0, 1); r2[i] =
(ans2 * ans3) + (ans2 * ans4) * base(0, 1); fft(r1, 1); fft(r2, 1); vector<int> ret(n); for(int i=0; ijn; i++)
lint av = (lint)round(r1[i].real()); lint bv = (lint)round(r1[i].imag()) + (lint)round(r2[i].real()); lint cv =
(lint)round(r2[i].imag()); av ret[i] = (av > 30) + (bv > 15) + cv; ret[i] ret[i] += mod; ret[i] return ret;

```

## 5.2 Hell-Joseon style FFT

```

cpp include jsmmintrin.h; include jmmmintrin.h; pragma GCC target("avx2")
#pragma GCC target("fma4"); #define m_256dc m_256m
#define m_256dd m_256shufflen(a,a,15);

```

### 5.3 NTT Polynomial Division

[illegible]

## 5.4 Black Box Linear Algebra + Kitamasa

```

cpp vector<int> berlekamp_massey(vector<int> x) vector<int> ls, cur; int lf, ld; for(int i = 0; i < x.size(); i++)
int > rec, vector<int> dp, lintn) int m = rec.size(); vector<int> s(m), t(m); s[0] = 1; if(m! = 1) t[1] = 1; else
int > x, lintn) if(n < x.size()) return x[n]; vector<int> v = berlekamp_massey(x); if(v.empty()) return 0; return
-v, 0 - based. noduplicateplease.. vector<int> get_min_poly(intn, vector<elem>
M)/smallestpoly P such that A^i = sum_{j< i} A^j * P_j vector<int> > rnd1, rnd2; mt19937rng(0x14004); autorand(int
elem > M) vector<int> > rnd; mt19937rng(0x14004); autorand(int = [rng](intlb, intub) return uni_form(inta, intb);

```

## 5.5 Gaussian Elimination

```

cpp int n, inv; vector<int> basis[505]; lint gysu = 1;
void insert(vector<int> v) for(int i=0; i<n; i++) if(basis[i].size()) inv
=1; //inversionnumincreasesif(v[i]basis[i].empty())basis[i] = v; return; if(v[i]lintminv = ipow(basis[i][i], mod
[2 * p + 1].sy - x.second) < dap)solve(2 * p + 1, x); else if(ok[2 * p + 1])solve(2 * p + 1, x); if(ok[2 * p]sqr(tree[2 *

```

## 5.6 Simplex Algorithm

```

cpp using T = long double; const int N = 410, M = 30010; const T eps = 1e-
7; int n, m; int Left[M], Down[N]; // time complexity: exponential. fast  $O(MN^2)$ 
in experiment. dependent on the modeling. // Ax  $_i = b$ ,  $\max C^T x$ . :  $v$ ,
sol[i].1basedTa[M][N], b[M], c[N], v, sol[N]; boole(Ta, Tb) return fabs(a - b) < eps; boolls(Ta, Tb) return a < b;
for(int i = 1; i ≤ m; i++) if(i == x — eq(a[i][y], 0)) continue; k = a[i][y]; a[i][y] = 0; b[i] -= k*b[x];
for(int j : nz) a[i][j] -= k*a[x][j]; if(eq(c[y], 0)) return; k = c[y]; c[y] = 0; v += k*b[x]; for(int i : nz) c[i]
-= k*a[x][i]; // 0: found solution, 1: no feasible solution, 2: unbounded int solve() for(int i = 1; i ≤ n;
i++) Down[i] = i; for(int i = 1; i ≤ m; i++) Left[i] = n+1; while(1) // Eliminating negative b[i] int x =
0, y = 0; for(int i = 1; i ≤ m; i++) if (ls(b[i], 0)) (x = 0 — b[i] | b[x]) x = i; if(x == 0) break; for(int
i = 1; i ≤ n; i++) if (ls(a[x][i], 0)) (y = 0 — a[x][i] | a[x][y]) y = i; if(y == 0) return 1; pivot(x, y);

```

```

while(1) int x = 0, y = 0; for(int i = 1; i != n; i++) if (ls(0, c[i]) != c[i] & c[y]) y = i; if(y == 0) break; for(int i = 1; i != m; i++) if (ls(0, a[i][y]) != b[i]/a[i][y] & b[x]/a[x][y]) x = i; if(x == 0) return 2; pivot(x, y); for(int i = 1; i != m; i++) if(Left[i] != n) sol[Left[i]] = b[i]; return 0;

```

## 5.7 Pentagonal Number Theorem for Partition Number Counting

```
cpp vector<pair<int, int>> gp; lint P[MAXN+1] = ; gp.emplace_back(0,0); for(int i = 1; gp.back().second <= MAXN; i++) gp.emplace_back(igp.emplace_back(iP[1] = 1; for(int n = 2; n <= MAXN; n++) for(auto it : gp) if(n >= it.second) P[n] += P[n - it.second] * it.first + MOD; P[n]
```

## 5.8 De Bruijn Sequence

```

cpp // Create cyclic string of length k^n that contains every length n string as substring. alphabet =
[0, k - 1] int res[10000000]; // >= k^n int aux[10000000]; // >= k *
n int de, ruijn(int k, int n) // Return size(k^n) if (k == 1) res[0] = 0; return 1; for (inti = 0; i < k * n; i++) au

```

## 5.9 Discrete Kth root

```

cpp /* * Solve x for x^P = AmodQ * (P,Q - 1) = 1- > P-1mod(Q -
1)exists * xhassolutioniffA^(Q - 1)/P = 1modQ * PP|(Q - 1)- > P <
sqrt(Q),solvexGroundsofdiscretelog * else- > findast.s(Pa - 1)- > ans = A^a */usingLL=
longlong;LLmul(LLx,LLy,LLmod)return(_int128)x*yLLadd(LLx,LLy,LLmod)return(x+y)LLpw(LLx,LLy,LL
LLdisjog(LLx)FOR(i,X)LLiaXi=iaXe[i];LLrst=mul(x,iaXi,Q);if(ht.count(rst))returni*X+h
0)return0;if(t==0)/a^P-1modphi(Q)LLx,y,gcd(P,Q-1,x,y);if(x<0)x=(xLLans=pw(A,Q,x);
residueif(pw(A,(Q-1)/P,Q)!=1)return-1;for(g=2;g<Q;g++)
g)if(pw(g,(Q-1)/P,Q)!=1)break;LLalpha=0;LLy,gcd(P,s,alpha,y);if(alpha<0)alpha=(alpha
1)LLans=pw(A,alpha,Q);returnans;LLa=pw(g,(Q-1)/P,Q);build(a);LLb=
pw(A,add(mul(PLlc=pw(g,s,Q);LLh=1;LLe=(Q-1)/s/P;//r^-1REP(i,1,t-
1)e/=P;LLd=pw(b,e,Q);LLj=0;if(d!=1)j=-disjog(d);if(j<0)j=(j+mul(b,pw(c,mul(Ph=

```

### 5.10 Miller-Rabin Test + Pollard Rho Factorization

```

cpp namespace millerrabinlintmul(lintx, lenty, lintmod) return (nt128)xxylintpow(lintx, lenty, lintp) lintret;
namespace pollardrholintf(lintx, lintn, lintc) return (c + millerrabin :: mul(x, x, n)) void rec(lintn, vector
lint > factorize(lintn) vector < lint > ret; rec(n, ret); sort(ret.begin(), ret.end()); return ret;;

```

### 5.11 Highly Composite Numbers, Large Prime

```

cpp | 10knumberdivisors23571113171923293137 - - - - -
-----
1641112601221138403231114756064331158316012833111672072024042111178648640448631111873513440768
| 10kprimeofprime < 10kprime - - - - -
-----
1741099999999672972511999999999773997168129999999998949973122913999999999971599991959214999
NTT Prime:
998244353 = 119 × 223 + 1. Primitive root: 3.
985661441 = 235 × 222 + 1. Primitive root: 3.
1012924417 = 483 × 221 + 1. Primitive root: 5.

```

## 6 Miscellaneous

## 6.1 Mathematics

- **Tutte Matrix.** For a simple undirected graph  $G$ , Let  $M$  be a matrix with entries  $A_{i,j} = 0$  if  $(i, j) \notin E$  and  $A_{i,j} = -A_{j,i} = X$  if  $(i, j) \in E$ .  $X$  could be any random value. If the determinants are non-zero, then a perfect matching exists, while other direction might not hold for very small probability.

- **Cayley's Formula.** Given a degree sequence  $d_1, d_2, \dots, d_n$  for each labeled vertices, there exists  $\frac{(n-2)!}{(d_1-1)!(d_2-1)! \dots (d_n-1)!}$  spanning trees. Summing this for every possible degree sequence gives  $n^{n-2}$ .
- **Kirchhoff's Theorem.** For a multigraph  $G$  with no loops, define Laplacian matrix as  $L = D - A$ .  $D$  is a diagonal matrix with  $D_{i,i} = \deg(i)$ , and  $A$  is an adjacency matrix. If you remove any row and column of  $L$ , the determinant gives a number of spanning trees.

- **Green's Theorem.** Let  $C$  is positive, smooth, simple curve.  $D$  is region bounded by  $C$ .  

$$\oint_C (Ldx + Mdy) = \iint_D \left( \frac{\partial M}{\partial x} - \frac{\partial L}{\partial y} \right)$$

To calculate area,  $\frac{\partial M}{\partial x} - \frac{\partial L}{\partial y} = 1$ , common selection is  $M = \frac{1}{2}x$ ,  $L = -\frac{1}{2}y$ .

= Line integral function parametrized by  $x(\theta) = [(r_C + r_C \cos \theta, y_C + r_C \sin \theta)]$  in when  $\theta_i \leq \theta \leq \theta_f + (1 + t)\theta_f$ ,  
 is given as follows.:  $\frac{1}{2}(r_C(x_C(\sin \theta_f - \sin \theta_i) - y_C(\cos \theta_f - \cos \theta_i)) + (\theta_f - \theta_i)r_C^2)$ .

Line integral of line parametrized by  $(x, y) = t(x_1, y_1) + (1 - t)(x_2, y_2)$  is given as follows:  $\frac{1}{2}(x_1y_2 - x_2y_1)$ .

- $$P(w_1, \dots, w_n) = \frac{1}{|H|} \sum_{h \in H} \frac{1}{|G|} \sum_{g \in G} \prod_{m \geq 1} (\sum_{h^m(b)=b} (w_b^m))^{\text{cm}(g)}$$

Without the occurrence restriction:

```

iv = x.push_b(y) if (y) ret = mul(ret, piv, p); piv = mul(piv, piv, p); y >= 1; return ret; bool miller, abin(lintx, linta) if (x lintx =
lintx) v if (v) = 1; return c if (v) push_b(ack(2); rec(n/2, v); return; if (miller, abin :: isprime(n)) v.push_b(a

```

where  $c(g)$  could also be interpreted as the number of elements in  $X$  that are fixed up to  $g$ .

- **Pick's Theorem.**  $A = i + \frac{b}{2} - 1$ , where:  $P$  is a simple polygon whose vertices are grid points,  $A$  is area of  $P$ ,  $i$  is # of grid points in the interior of  $P$ , and  $b$  is # of grid points on the boundary of  $P$ . If  $h$  is # of holes of  $P$  ( $h + 1$  simple closed curves in total),  $A = i + \frac{b}{2} + h - 1$ . c++ number of (x, y) : (0 ≤ x ≤ n, 0 ≤ y ≤ k/d x + b/d) // argument should be positive

- **Xudyh Sieve.**  $F(n) = \sum_{d|n} f(d)$   
 $S(n) = \sum_{i \leq n} f(i) = \sum_{i \leq n} F(i) - \sum_{d=2}^{\lfloor \frac{n}{d} \rfloor} S(\lfloor \frac{n}{d} \rfloor)$   
Preprocess  $S(1)$  to  $S(M)$  (Set  $M = n^{\frac{2}{3}}$  for complexity)  
 $S(n) = \sum f(i) = \sum_{i \leq n} [F(i) - \sum_{j|i, j \neq i} f(j)] = \sum F(i) - \sum_{i/j=d=2}^n \sum_{dj \leq n} f(j)$   
 $S(n) = \sum if(i) = \sum_{i \leq n} i [F(i) - \sum_{j|i, j \neq i} f(j)] = \sum iF(i) - \sum_{i/j=d=2}^n \sum_{dj \leq n} djf(j)$   
 $\sum_{d|n} \varphi(d) = n$      $\sum_{d|n} \mu(d) = \text{if } (n > 1) \text{ then } 0 \text{ else } 1$      $\sum_{d|n} (\mu(\frac{n}{d}) \cdot \sum_{e|d} f(e)) = f(n)$

## 6.2 Popular Optimization Technique

- CHT. DnC optimization. Mo's algorithm trick (on tree). IOI 2016 Aliens trick. IOI 2009 Regions trick.

- Knuth’s  $O(n^2)$  Optimal BST : minimize  $D_{i,j} = \text{Min}_{i \leq k < j} (D_{i,k} + D_{k+1,j}) + C_{i,j}$ . Quadrangle Inequality :  $C_{a,c} + C_{b,d} \leq C_{a,d} + C_{b,c}$ ,  $C_{b,c} \leq C_{a,d}$ . Now monotonicity holds.
- Sqrt batch processing - Save queries in buffer, and update in every sqrt steps (cf : IOI 2011 Elephant. hyea calls it "ainta technique")
- Dynamic insertion in static set (Make  $O(\log n)$  copy. Merge like binomial heap.)
- Offline insertion / deletion in insert-only set (Pair insertion-deletion operation, and regard it as range query)
- Atcoder Median Pyramid : Reduce the input to binary, and solve the easier problem.
- LP Duality.  $\max c^T x$  s.t to  $Ax \leq b$ . Dual problem is  $\min b^T x$  s.t to  $A^T x \geq c$ . By strong duality, min max value coincides.

6.3 Fast LL Division / Modulo

```
cpp inline void fasterLLDivMod(unsigned long long x, unsigned y, unsigned out_d, unsigned out_m) unsigned xh = (unsigned)(x >> 32), xl = (unsigned)x, d, m; if def_GNUC asm("di\vl:"=a"
```

6.4 Bit Twiddling Hack

```
cpp int _b_uiltin_c_lz(int x); // number of leading zero int _b_uiltin_ctz(int x); // number of trailing zero int _b_uiltin_c_lzll(long long x); // number of leading zero int _b_uiltin_ctzll(long long x); // number of trailing zero int _b_uiltin_popcount(int x); // number of 1-bits in x int _b_u_lsb(n): (n - n); // last bit (smallest) floor(log2(n)): 31 - _b_uiltin_c_lz(n|1); floor(log2(n)): 63 - _b_uiltin_c_lzll(n|1); // compute next perm. ex) 00111, 01011, 01101, 01110, 10011, 10101.. long long next_perm(long long v) long long t = v|((v - 1); return(t + 1)|(((t - t) - 1) >> (_b_uiltin_ctz(v)+1));
```

6.5 Fast Integer IO

```
cpp static char buf[1024]; // size : any number geq than 1024 static int idx = 0; static int bytes = 0; static inline int read() if (!bytes || idx == bytes) bytes = (int) fread(buf, sizeof(buf[0]), sizeof(buf), stdin); idx = 0; return buf[idx + +]; static inline int readInt() int x = 0, s = 1; int c = read(); while (c <= 32) c = read(); if (c == '-' ) s = -1,
```

6.6 OSRank in g++

```
cpp include <ext/pb_ds/assoc_container.hpp> include <ext/pb_ds/tree_policy.hpp> using namespace _pbds; typedef tree<int, null_type, less<int>, rb_tree_tag, tree_order_statistics_node_update> ordered_set; ordered_set X; X.insert(1); X.insert(2); X.insert(4); X.insert(8); X.insert(16); cout<<*X.find_by_order(1) << endl; // 2 cout << *X.find_by_order(2) << endl; // 4 cout << *X.find_by_order(4) << endl; // 16 cout << (end(X) == X.find_by_order(6)) << endl; // true cout<<X.order_of_key(-5) << endl; // 0 cout << X.order_of_key(1) << endl; // 0 cout << X.order_of_key(3) << endl; // 2 cout << X.order_of_key(4) << endl; // 2 cout << X.order_of_key(400) << endl; // 5
```

6.7 Nasty Stack Hacks

```
cpp // 64bit ver. int main2() return 0; int main() size_t sz = 1 << 29; // 512 MB void * newstack = malloc(sz); void * spdest = newstack + sz - sizeof(void*); asm_volatile("movq" movq main2(); asm_volatile("pop" return 0;
```

6.8 C++ / Environment Overview

```
cpp // vimrc : set nu sc ci si ai sw=4 ts=4 bs=2 mouse=a syntax on // compile : g++ -o PROB PROB.cpp -std=c++11 -Wall -O2 // options : -fsanitize=address -Wfatal-errors struct StupidGCCCantEvenCompileThisSimpleCode pair<int, int> i; array<int, 1000000>; // https://gcc.gnu.org/bugzilla/show_bug.cgi?id=68203 // how to use rand (in 2018) mt19937 rng(0x14004); int randint(int lb, int ub) return uniform_int_distribution<int>(lb, ub)(rng); // comparator overload auto cmp = [&](seg a, seg b) return a.func() < b.func(); ; set<seg, decltype(cmp)> s(cmp); map<seg, int, decltype(cmp)> mp(cmp); priority_queue<seg, vector<seg>, decltype(cmp)> , pq(cmp)>; // max heap // hash func overload struct point { int x, y; bool operator==(const point p) const { return x == p.x && y == p.y; ; struct hasher { size_t operator()(const point p) const { return p.x * 2 + p.y * 3; ; unordered_map<point, int, hasher> hsh;
```

6.9 Credits

```
[noitemsep, nolistsep] cki86201, zigui, PavelKunyavskiy https://gist.github.com/msg555/4963794 https://github.com/niklasb/contest-algos/blob/master/convex_hull/dynamic.cpp https://github.com/jaehyunp/stanfordacm https://github.com/tzupengwang/PECaveros/blob/master/codebook/graph/BorrowedGeneralWeightedMatching.cpp https://github.com/tzupengwang/PECaveros/blob/master/codebook/math/DiscreteKthSqrt.cpp http://www-math.mit.edu/~etingof/groups.pdf
```