Linked List

Data Structures C++ for C Coders

한동대학교 김영섭 교수 idebtor@gmail.com

Singly Linked List

Self-referenced structures – review

```
who
                                                                               who
                                                                         data
                                                                                      who
Exercise: Link a, b and c nodes;
                                                                               data
                                                          List a, b, c;
                                                                         *link
                                                                                      data
struct List {
                                                                               *link
                                                                                      *link
       string who;
       char data;
                                                          a.data = 'A';
                                                                         who
       List *link;
                                                                               who
                                                          b.data = 'B';
                                                                         data
};
                                                                                      who
                                                          c.data = 'C';
                                                                               data
               allocation이 아니라 이미 메모리에 정해져 있는것
                                                                         *link
                                                                                      data
                                                                               *link
List a, b, c; 메모리를 할당하기 전에는 주^{4}만 저장가능
                                                                                      *link
a.data = 'A'; 구조체의 멤버데이터는 저장할 수 없다.
b.data = 'B';
                                                          a.link = b.link = c.link = nullptr;
c.data = 'C';
a.link = b.link = c.link = nullptr;
                                                                         who
                                                                               who
                                                                         data
                                                                                      who
                                                                               data
                                                                         *link
                                                                                           С
                                                                                      data
                                                                               *link
                                                                                      *link
                                                                                            nullptr
```

Self-referenced structures - review

```
who
                                                                                  data
                                                                                                 who
Exercise: Link a, b and c nodes;
                                                                                         data
                                                                  List a, b, c;
                                                                                  *link
                                                                                                 data
struct List {
                                                                                         *link
                                                                                                 *link
        string who;
        char data;
                                                                  a.data = 'A';
                                                                                  who
        List *link;
                                                                                          who
                                                                  b.data = 'B';
                                                                                  data
};
                                                                                                 who
                                                                  c.data = 'C';
                                                                                          data
                                                                                  *link
                                                                                                 data
                                                                                          *link
List a, b, c;
                                                                                                 *link
a.data = 'A';
b.data = 'B';
                                                                  a.link = b.link = c.link = nullptr;
c.data = 'C';
a.link = b.link = c.link = nullptr;
                                                                                  who
                                                                                          who
                                                                                  data
                                                                                                 who
                                                                                          data
                                                                                  *link
                                                                                                       С
                                                                                                 data
                                                                                          *link
                                                                                                 *link
                                                                                                        nullptr
                                                      who
                                                                                          who
                    who
                                                      data
                                                                                                C
                                                                                          data
                    data
                          Α
                                                             В
                                                      *link
                                                                                                nullptr
                                                                                          *link
                    *link
```

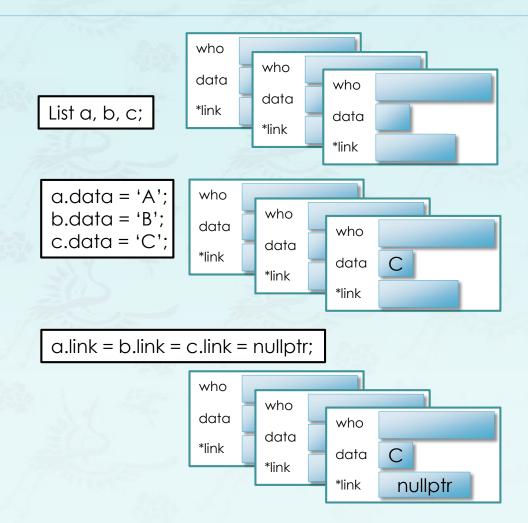
who

Self-referenced structures – review

```
Exercise: Link a, b and c nodes;

struct List {
    string who;
    char data;
    List *link;
};

List a, b, c;
List *p, *q, *r;
```



Self-referenced structures - review



```
Exercise: Link a, b and c nodes;

struct List {
    string who;
    char data;
    List *link;
};

List a, b, c;
List *p, *q, *r;
```

```
who
                                    who
                            data
                                             who
     p = &a;
                                    data
    q = &b;
                            *link
                                             data
                                    *link
     r = &c:
                                             *link
   p->data = 'X';
                            who
   q->data = 'Y';
                                    who
                            data
                                              who
(2) r->data = 'Z';
                                    data
                            *link
                                              data
                                     *link
     p->link = q;
                                              *link
```

who

data

*link

who

data

who

data

С

- (1) Let each p, q, and r points to a, b, and c;
- (2) Store each 'X', 'Y', and 'Z' in data
- (3) Connect them using p, q and r as shown below:

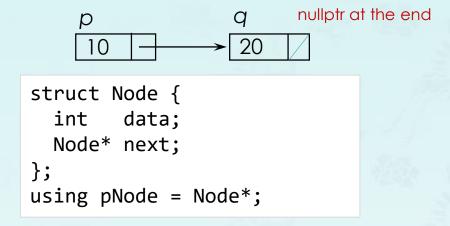


q->link = r;

(3) r->link = nullptr;

Linked List

TASK: Code a function that returns the head of following linked list.



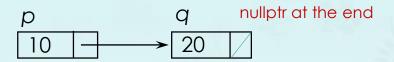
Write a function that creates a node and returns pNode.

```
pNode newNode(int val) {
 pNode node = (pNode)malloc(sizeof(Node));
 node->data = val;
 node->next = nullptr;
 return node;
pNode newNode(int val) {
 pNode node = new Node;
 node->data = val;
 node->next = nullptr;
 return node;
```

```
pNode node = new Node {0, nullptr};
```

Linked List

TASK: Code a function that returns the head of following linked list.



```
struct Node {
  int data;
  Node* next;
};
using pNode = Node*;
```

```
pNode newList2(int a, int b) {
   pNode p = new Node {a, nullptr};
   pNode q = new Node {b, nullptr};
   p->next = q;
   return p;
}
```

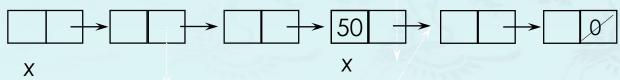
```
pNode newList2(int a, int b) {
   pNode q = new Node {b, nullptr};
   pNode p = new Node {a, q};
   return p;
}
```

```
pNode newList2(int a, int b) {
   pNode q = new Node {b, nullptr};
   return new Node {a, q};
}
```

Linked List - find()

TASK: Code a function that returns the first node **data = 50** if any, otherwise nullptr.





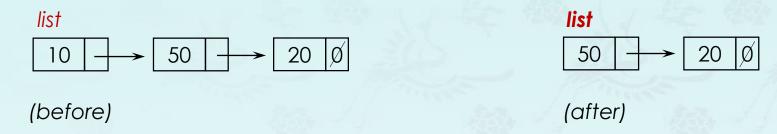
```
pNode find(pNode list, int val)
if (empty(list)) return nullptr;

pNode x = list
while (x != nullptr) {
  if (x->data == val) return x;
  x = x->next;
}
return x;
```

```
bool empty(pNode list)
return list == nullptr;
```

Linked List - pop_front()

TASK: Code a function that deletes the first node and returns the new first node.



```
pNode pop_front(pNode list)
if (empty(list)) return list;
list = list->next;
return list;
What's wrong?
```

```
pNode pop_front(pNode list)

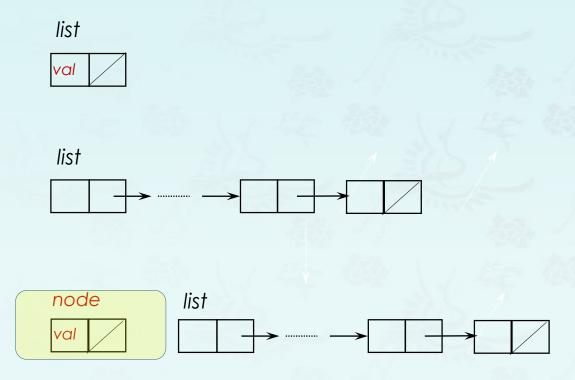
if (empty(list)) return list;

pNode x = list;
list = list->next;
delete x;
return list;
```

Linked List - push_front()

TASK: Code a function that add a node at the beginning of the list.

- If the list is empty, the new node becomes the head node.



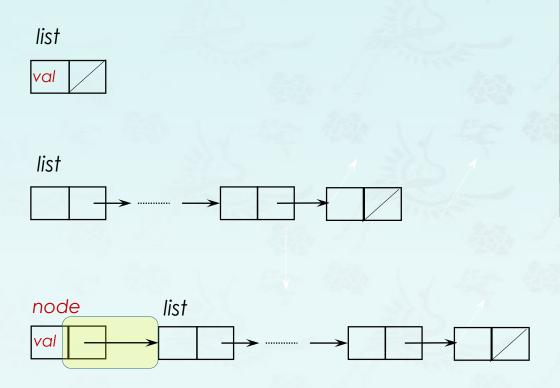
```
pNode push_front(pNode list, int val)
if (empty(list))
  return new Node{val, nullptr};

pNode node = new Node{val, nullptr};
```

Linked List - push_front()

TASK: Code a function that add a node at the beginning of the list.

- If the list is empty, the new node becomes the head node.



```
pNode push_front(pNode list, int val)
if (empty(list))
  return new Node{val, nullptr};

pNode node = new Node{val, nullptr};

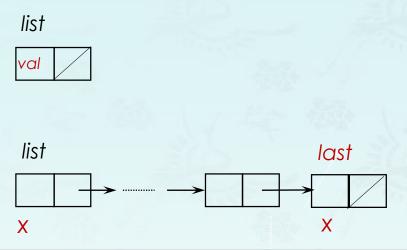
node->next = list;
return node;
```

return new node{val, nullptr}

Linked List - push_back()

TASK: Code a function that appends a node at the end of the list.

- If the list is empty, the new node becomes the head node.



```
pNode last(pNode list)

pNode x = list;
while (x != nullptr)
   x = x->next;
return x'
```

```
pNode push_back(pNode list, int val)

if (empty(list))
  return new Node{val, nullptr};
```

```
pNode last(pNode list)

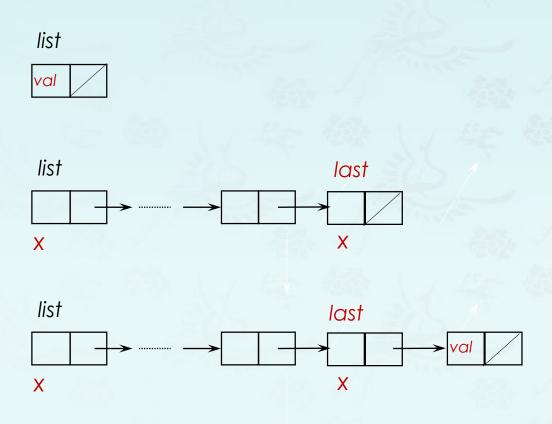
pNode x = list;
while (x->next != nullptr)
   x = x->next;
return x;
```

Q: Which one is correct?

Linked List - push_back()

TASK: Code a function that appends a node at the end of the list.

- If the list is empty, the new node becomes the head node.



```
pNode push_back(pNode list, int val)
if (empty(list))
  return new Node{val, nullptr};

return list;
```

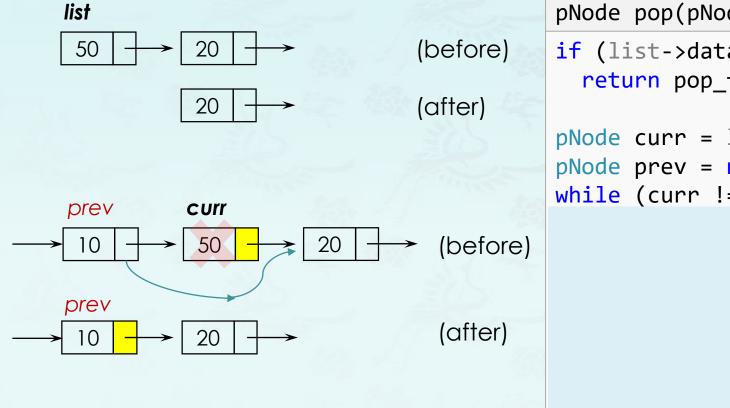
```
pNode last(pNode list)

pNode x = list;
while (x->next != nullptr)
   x = x->next;
return x;
```

Linked List - pop()

TASK: Code a function that deletes a node with a value specified.

- If the first node (or **head**) is the one to delete, then just invoke **pop_front()**.
- As observed below, we must to know the pointer x which is stored in the previous node of node x.



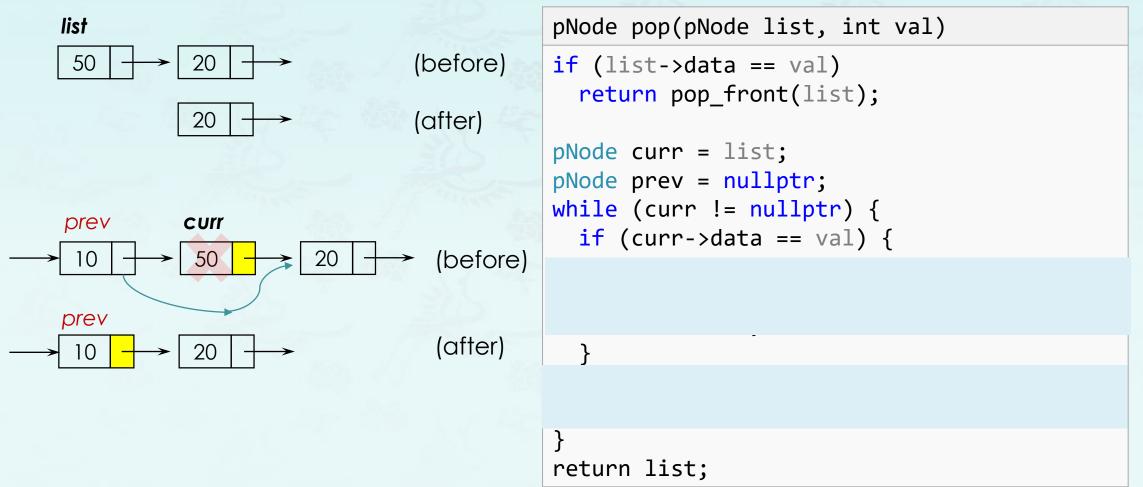
```
pNode pop(pNode list, int val)
if (list->data == val)
  return pop_front(list);
pNode curr = list;
pNode prev = nullptr;
while (curr != nullptr) {
return list;
```

14

Linked List - pop()

TASK: Code a function that deletes a node with a value specified.

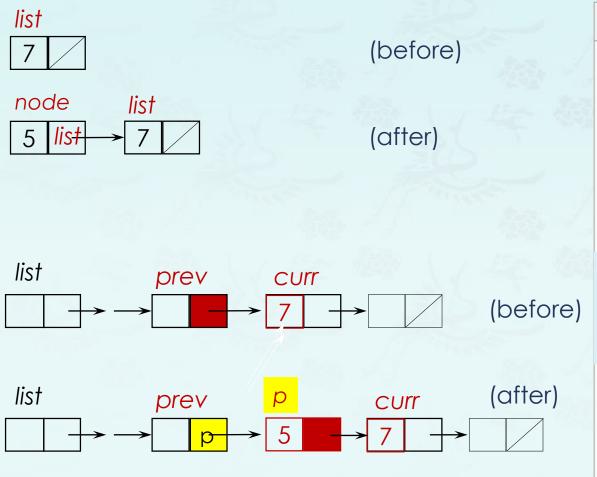
- If the first node(or head) is the one to delete, then just invoke pop_front().
- As observed below, we must to know the pointer x which is stored in the previous node of node x.



Linked List - insert()

TASK: Code a function that inserts a node(5) at a node position x specified by a value(7).

- If the first node(or head) is the position, then just invoke push_front().
- As observed below, we must to know the pointer x which is stored in the previous node of node x.



```
pNode insert(pNode list, int val, int x)
if (list->data == x)
pNode curr = list;
pNode prev = nullptr;
while (curr != nullptr) {
  if (curr->data == x) {
  prev = curr;
  curr = curr->next;
return list;
```

Linked List

* resizing array vs. linked list

Tradeoffs. Can implement a stack with either resizing array or linked list; client can use interchangeably. Which one is better?

Linked-list implementation

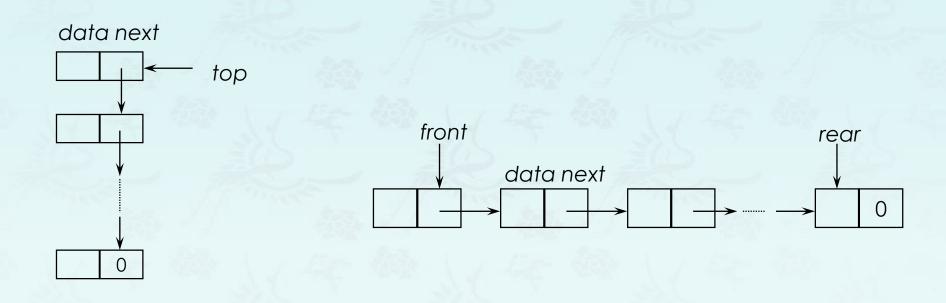
- Every operation takes constant time in the worst case.
- Uses extra time and space to deal with the links.

Resizing-array implementation

- Every operation takes constant amortized time.
- Less waste space

Linked List

Using linked lists, stacks and queues facilitate easy insertion and deletion of nodes.



(a) linked stack

(b) linked queue

Polynomials

Polynomials representation

$$A(X) = a_{m-1}X^{e_{m-1}} + \cdots + a_0X^{e_0}$$

 a_i = nonzero coefficients
 e_i = nonnegative integer exponents such as
 $e_{m-1} > e_{m-2} > \dots > a_0 \ge 0$

We may draw a poly node as

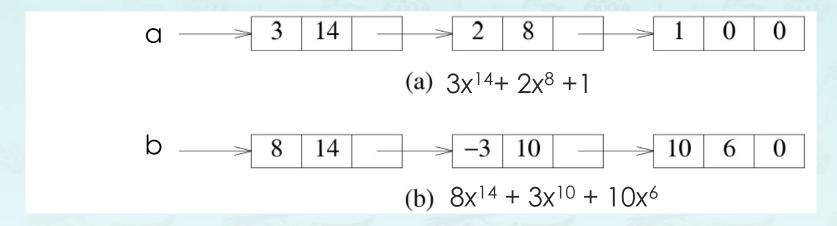
coef	ехро	next
------	------	------

Type definition

```
struct Poly {
    double coef;
    double expo;
    Poly* next;
};
using pPoly = Poly*;
```

Polynomials

❖ Example:



Q: How to add two polynomials? c = a + b

Polynomials

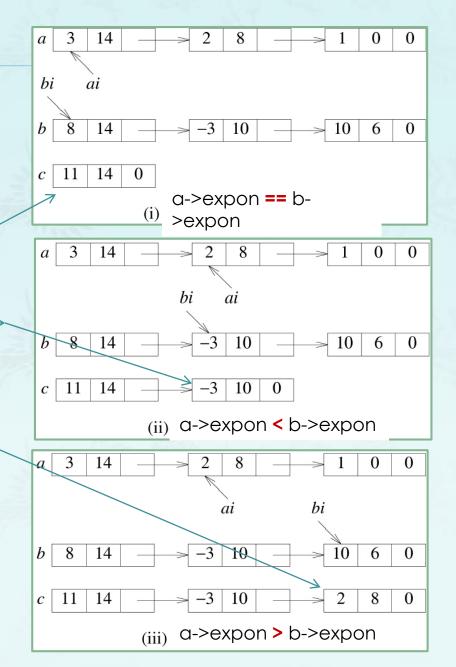
Q: How to add two polynomials?

$$a = 3x^{14} + 2x^{8} + 1$$

$$b = 8x^{14} - 3x^{10} + 10x^{6}$$

$$c = a + b$$

$$= 11x^{14} - 3x^{10} + 2x^{8} + 10x^{6} + 1$$



Doubly Linked lists

Doubly linked list: each node contains, besides the next-node link, a second link field pointing to the previous node in the sequence. The two links may be called forward and backward, or next and prev(ious).



Type definition

```
struct Node {
    int    data;
    Node* prev;
    Node* next;
};
using pNode = Node*;
```

Q. Array vs. Singly linked list vs. Doubly linked list, Why?

Doubly Linked lists

Q. Array vs. Singly linked list vs. Doubly linked list, Why?

Advantages of linked list:

- Dynamic structure (Memory Allocated at run-time)
- Have more than one data type.
- Re-arrange of linked list is easy (Insertion-Deletion).
- It doesn't waste memory.

Disadvantages of linked list:

- In linked list, if we want to access any node it is difficult.
- It uses more memory.

Advantages of doubly linked list:

- A doubly linked list can be **traversed in both directions** (forward and backward). A singly linked list can only be traversed in one direction.
- Most operations are O(1) instead of O(n).

Pointer Linked - Lab

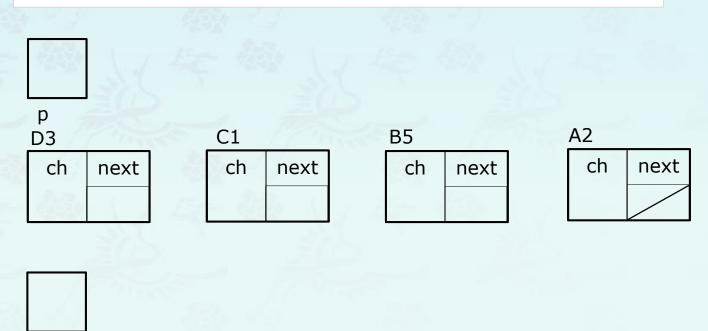
```
#include <iostream>
using namespace std;
class Node {
public:
  char ch;
  Node* next;
};
int main( ) {
  Node* p = nullptr, *q = nullptr;
  char ch;
  while (cin.get(ch) && ch != '\n') {
    p = new Node;
    p->ch = ch;
    p \rightarrow next = q;
    q = p;
  while (p != nullptr) {
    cout.put(p->ch);
    p = p \rightarrow next;
  cout << endl;</pre>
```

Pointer Linked – Lab

```
#include <iostream>
using namespace std;
class Node {
public:
  char ch;
  Node* next;
};
int main( ) {
  Node* p = nullptr, *q = nullptr;
  char ch;
  while (cin.get(ch) && ch != '\n') {
    p = new Node;
    p \rightarrow ch = ch;
    p \rightarrow next = q;
    q = p;
  while (p != nullptr) {
    cout.put(p->ch);
    p = p \rightarrow next;
  cout << endl;</pre>
```

Assuming the input A, B, C, D to this program, what would be the data structure after the input?

Draw a figure to represent the data structure in memory. Use a mnemonic memory address to represent each node such as A2, B5, C1, ..., etc.



What is missing in the figure?

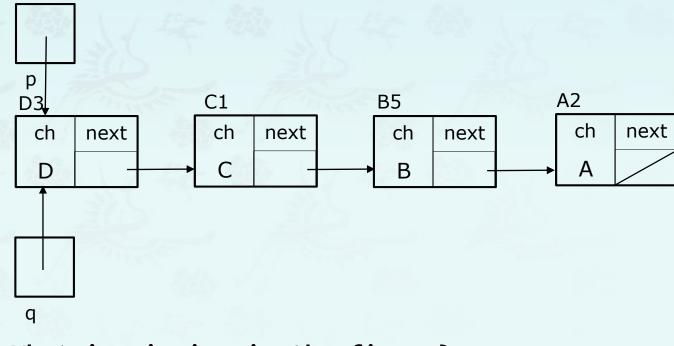
q

Pointer Linked

```
#include <iostream>
using namespace std;
class Node {
public:
  char ch;
  Node* next;
};
int main( ) {
  Node* p = nullptr, *q = nullptr;
  char ch;
  while (cin.get(ch) && ch != '\n') {
    p = new Node;
    p \rightarrow ch = ch;
    p \rightarrow next = q;
    q = p;
  while (p != nullptr) {
    cout.put(p->ch);
    p = p \rightarrow next;
  cout << endl;</pre>
```

Assuming the input A, B, C, D to this program, what would be the data structure after the input?

Draw a figure to represent the data structure in memory. Use a mnemonic memory address to represent each node such as A2, B5, C1, ..., etc.



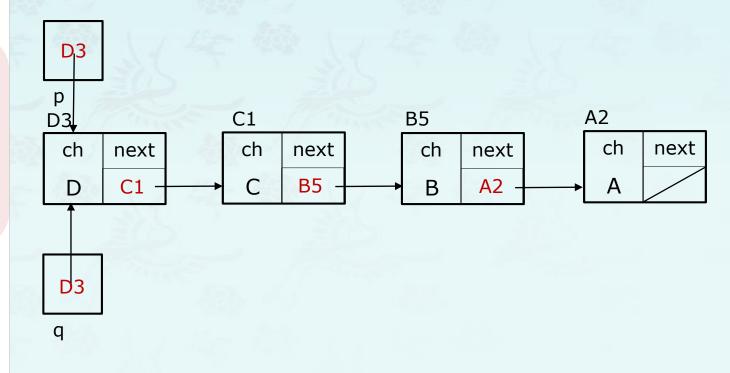
What is missing in the figure?

Pointer Linked

```
#include <iostream>
using namespace std;
class Node {
public:
  char ch;
  Node* next;
};
int main( ) {
  Node* p = nullptr, *q = nullptr;
  char ch;
  while (cin.get(ch) && ch != '\n') {
    p = new Node;
    p \rightarrow ch = ch;
    p \rightarrow next = q;
    q = p;
  while (p != nullptr) {
    cout.put(p->ch);
    p = p->next;
  cout << endl;</pre>
```

Assuming the input A, B, C, D to this program, what would be the data structure after the input?

Draw a figure to represent the data structure in memory. Use a mnemonic memory address to represent each node such as A2, B5, C1, ..., etc.



Pointer Linked

```
#include <iostream>
using namespace std;
class Node {
public:
  char ch;
  Node* next;
};
int main( ) {
  Node* p = nullptr, *q = nullptr;
  char ch;
  while (cin.get(ch) && ch != '\n') {
    p = new Node;
    p \rightarrow ch = ch;
    p \rightarrow next = q;
    q = p;
  while (p != nullptr) {
    cout.put(p->ch);
    p = p->next;
  cout << endl;</pre>
```

After executing the while loop, What is the output? What is the values of p and q?

