

Sage Basics

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

Python & SageMath. Python is a programming language. It is easy to use and flexible for various purposes. SageMath is an open-source mathematics software built on Python and stands for “System for Algebra and Geometry Experimentation”. It provides plenty of functions for mathematical computation and research.


How to install. CoCalc is an online platform for Linux, L^AT_EX, Python, Sage, R, etc. It is free, but you may subscribe to get better performance. Use CoCalc to experience the power of programming first.

CoCalc Python SageMath

Register an account of CoCalc, create a project, and create a Sage worksheet. Then embrace the wonder of SageMath!

Your best friends.

 evaluate the cell


 autocomplete or show the possible completions

object. press tab to see functions under *object*

func? evaluate this line to read the document of *func*

func?? evaluate this line to read the source code of *func*

Google the answers are likely available online or in Sage Reference Manual

Assign a value.

`a = 1` set the value of `a` as 1

Print. Run `print a` or `print(a)` to print the value of `a`. Python 3 only accepts the second syntax.

Data types.

`int` integers, such as 2, 3, 5, ...
Integer is more common in Sage

`str` strings, such as "235"

`bool` boolean values, namely, True and False

`tuple` tuples, such as (2,3,5)

`list` lists, such as [2,3,5]

`dict` dictionaries, such as
{ "two":2, "three":3, "five":5 }
defined by { *key* : *value* }

`type(a)` return the type of `a`

Boolean tests.

`in` 1 in [2,3,5] returns False

`not in` 1 not in [2,3,5] returns False

`relation` 2==3 returns False
options: >, >=, <, >=, and !=
!= means not equal

`isinstance` check the type
`isinstance("235",str)` returns True

Arithmetic operators.

`+ - * /` addition, subtraction, and multiplication, division

`**` or `^` exponent, `**` for Python, `^` for Sage
`2^3` returns 8

`%` modulus, `23%4` returns 3

`//` floor division, `23//4` returns 5

Layout. Line breaks and indents are both sensitive in Python. Conventionally, an indent is four spaces. On CoCalc, I suggest go to “Account” and check the box of “Spaces instead of tabs”. If you put several commands in a line, then use semi-colons “;” to separate them. Otherwise, semi-colons are optional.

The if statement. The following code decides the letter grade of the input score.

```
score = 90;
if score >= 80 and score <= 100:
    print "A";
elif score >= 70 and score < 80:
    print "B";
elif score >= 60 and score < 70:
    print "C";
elif score >= 0 and score < 60:
    print "D";
else:
    print "Input score not valid";
```

The for loop. The following code prints the positive integers less than or equal to 100 that is a multiple of 5 or 7.

```
for i in range(1,101):
    if i%5==0 or i%7==0:
        print i;
```

You may use generator or list in a for loop.

`range(b)` the list $0, 1, \dots, b-1$.

`range(a,b)` the list $a, a+1, \dots, b-1$

`TreeIterator(n)` the generator of trees on n vertices, run the next line first

from `sage.graphs.trees` import `TreeIterator`

The while loop. The following code is a primitive way to find the least common multiple of 5 and 7.

```
i=1;
while True:
    if i%5==0 and i%7==0:
        print i;
        break;
    else:
        i=i+1;
```

Here `break` means to stop the loop.

Define a function. The following function will return the value of $\sum_{k=1}^n k^p$.

```
def power_sum(n,p,summand=False):
    total=0;
    for k in range(1,n+1):
        total += k^p;
        if summand:
            print k^p;
    return total;
```

Thus, `power_sum(10,1)` returns 55. The variable `summand` has a default value `False` so it is optional; when it is `True`, the function will print the summands. For example, `power_sum(10,2,True)` will print $1, 4, 9, \dots, 100$ and then return 385.

Call values.

`f(a,b)` return the value of the function `f` with given inputs `a` and `b`

`L[k]` return the value of the k -th element in the list `L`

`D[k]` return the value that corresponds to the the key `k` in the dictionary `D`

Shorthand and string formatting.

`[k^2 for k in range(6) if k%2==1]`

means [1,9,25]

`{k:k^2 for k in range(6) if k%2==1}`

means {1:1,3:9,5:25}

`n=5; print "%s+1=%s"%(n,n+1);`

prints 5+1=6

`n=5; print "{0}+1={1}".format(n,n+1);`

prints 5+1=6

Operations on a list. Suppose `a=[0,1,2,3,4]`.

`a[-2]` returns 3

`a[1:-2]` returns [1,2]

`a[2:]+a[:2]` returns [2,3,4,0,1]

Matrix. To assign

$$M = \begin{bmatrix} 0 & 1 & 2 \\ 3 & 4 & 5 \end{bmatrix},$$

the following two lines do the same work.

```
M=matrix([[0,1,2],[3,4,5]]);
```

```
M=matrix(2,range(6));
```

Get information of a matrix M by the following ways.

`M[i,j]` the i,j-entry

`M[[0,1],[1,2]]` the submatrix induced on rows indexed by [0,1] and columns indexed by [1,2].

`M[[1],:]` the row with index 1

`M[:,[2]]` the column with index 2

Graph. To assign $G = K_{2,3}$, each of the following three lines achieve the task, but only the first line assigns the positions of the vertices. (Try `G.show()` to see the differences.)

```
G=graphs.CompleteBipartiteGraph(2,3);
```

```
G=Graph({0:[2,3,4],1:[2,3,4]});
```

```
G=Graph("D)o");
```

Here "D)o" is the graph6 string of $K_{2,3}$.

Use nauty to search graphs. The following code prints the graph6 string for all connected graphs on 4 vertices.

```
n=4;
```

```
for g in graphs.nauty_geng("%s -c"%n):  
    print g.graph6_string();
```

You may check the isomorphism by first giving them a "standard" labeling and then compare their strings. The following code checks if G and H are isomorphic.

```
stgG=G.canonical_label().graph6_string();
```

```
stgH=H.canonical_label().graph6_string();
```

```
stgG==stgH;
```