$$q_R = \left[cos(\frac{\theta}{2}), \frac{\omega_x}{l_\omega} sin(\frac{\theta}{2}), \frac{\omega_y}{l_\omega} sin(\frac{\theta}{2}), \frac{\omega_z}{l_\omega} sin(\frac{\theta}{2}) \right]$$