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# How to Look Clever and Have Envious Neighbors: Average Variance Managed Investment

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# Background

- Risk (Portfolio Variance) = Reward : Markowitz (1952)
- Variance != Reward : Haugen and Heins (1972), Campbell (1987), French et al. (1987), Golsten et al. (1993)
- Moreira and Muir (2017) scaling month t+1 investment in the market index by month t daily return variance
- Stock market return variance : SV<sub>t</sub> =  $\sum_{m=1}^{N} \sum_{n=1}^{N} w_{m,t} w_{n,t} cov(r_{m,t}, r_{n,t})$
- Pollet and Wilson (2010) decomposition of market variance into a compensated and uncompensated component
  - average variance (AV) :  $\bar{\sigma}_t^2 = \sum_{m=1}^N w_{m,t} \sigma_t^2$  average correlation (AC) :  $\bar{\rho}_t = \sum_{m=1}^N \sum_{n=1}^N w_{m,t} w_{n,t} \rho_{m,n,t}$

  - $SV_t \approx AV * AC$  Anadu and Tierens (2004)
  - $r_{t+1} = \alpha_1 + \beta_1 AC_t + \epsilon_{1,t}$ ,  $\beta_1$  positive and significant
  - $r_{t+1} = \alpha_2 + \beta_2 AV_t + \epsilon_{2,t}$ ,  $\beta_2$  insignificant

#### Central Idea I

- If  $SV_t \approx AV^*AC$ , there maybe something to looking at AV and/or AC separately
- Moreira and Muir (2017): weight =  $\frac{c_{SV}}{SV_A}$ , c is scaling factor to match buy and hold volatility
- Me : weight =  $\frac{c_{AV}}{AV_*}$ ,  $c_{AV}$  to match buy and hold volatility
- $SV_{t+1} = \alpha_3 + \beta_3 AV_t + \epsilon_{3,t}$ ,  $\beta_3$  positive and significant
- AV<sub>t</sub> management decreases investment when AV<sub>t</sub> is high
- AV<sub>t</sub> management avoids decreasing investment when SV<sub>t</sub> is high because AC is high
- Should find AV management outperforms SV management

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Risk and Reward

# More Pollet and Wilson (2010)

- Roll (1972): relevant for time-series, variance-in-mean relation of stock market return
- Variance of observed returns ≠ variance of "market" returns  $\neq$  variance of aggregate wealth
- Shocks to true market returns are positively related to the common observed component, AC
- AC is positively related to the covariance of stock market returns and aggregate wealth,  $cov(r_{s,t+1}, r_{u,t+1})$
- AV is not
- The relationships depend on the proportion of the true market observed,  $w_{s,t}$ , and the aggregate wealth  $\beta_t$  for the index

#### Central Idea II

- If AC = systematic, when AC is high  $\Rightarrow$  higher  $r_{u,t+1}$  is expected
- r<sub>u,t</sub> is not observable through index returns
- Suggestive evidence is support of Pollet and Wilson (2010) relation
  - In a subset where daily returns are unrepresentative, AC won't predict  $r_{s,t+1}$ , AV management wont' perform
  - AV management should work globally
  - Equity AV management has higher investment in times of higher  $cov(r_{s,t+1}, r_{u,t+1})$ , so it should work across asset classes

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#### Preview Results

- AV management outperforms SV management returns, ratios, turnover, drawdowns, and utility
- AV management works better under practical investment constraints
- AV management works globally
- AV management works because changes in AV and AC signal changes in the systematic and unsystematic risk in the economy
  - In and Out-of-sample tests show changes in AV have more information about future risk and return than changes in SV
  - AV managed returns depend on the relationship of the proxy daily returns and aggregate wealth in time-series and cross-sectionally
  - The AV of equity returns can be used to manage investment in other assets across the economy

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#### Contribution

#### Variance Management

- Moreira and Muir (2017) and Hocquard, Ng, and Papageorgiou (2013)
- AV is a better dynamic volatility management signal
- AV management works globally and across asset classes (SV does not)

#### Risk Dynamics

- Gonzlez-Urteaga and Rubio (2016) and Bollerslev, Hood, Huss, and Pedersen (2017)
- AV comes from the foundations of investment risk
- AV management informs about the risk mix across the economy

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# **Equity Data**

#### **Equity Data**

-				
Country	Start	Months	Index	Assets
USA	1926 - 8	1085	CRSP	500
AUS	2000 - 5	212	ASX	200
BRA	1995 - 2	275	iShares MSCI Brazil ETF	60
CHN	2005 - 5	152	CSI 300	300
DEU	1993 - 11	290	HDAX	110
FRA	1993 - 9	292	SBF 120	120
IND	2000 - 5	212	Nifty 50	50
ITA	2003 - 8	173	FTSE MIB	40
JPN	1993 - 6	295	Nikkei	255
UK	1993 - 6	295	FTSE	100
World	1995 - 3	274	MSCI ACWI	1735

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# Non-Equity Data

#### Other Asset Data

Index	Start	Months	Asset Class
Bloomberg US Spot	2005 - 6	158	Currency
Deutsche Bank Currency	2005 - 6	158	Currency
Deutsche Bank Carry	2005 - 6	158	Currency
Deutsche Bank Momentum	2005 - 6	158	Currency
S&P REIT Index	2005 - 6	158	Real Estate
Bloomberg Commodity	2005 - 6	158	Commodities
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# AV Managed Investment

- $SV_t = \sigma_{S,t}^2$
- With m assets in the market,  $AV_t = \sum_{m=1}^{M} w_{m,t} \sigma_{m,t}^2$
- $W_t = \frac{c_{target}}{V}$  is the investment weight in the portfolio, where  $X \in \{AV_{t-1}, SV_{t-1}\}$
- The constant c<sub>target</sub> is used to control the volatility of the strategy
- c<sub>BH</sub> matching the buy and hold
- For robustness,  $c_{10}$  and  $c_{12}$  targeting 10% or 12% annual return volatility

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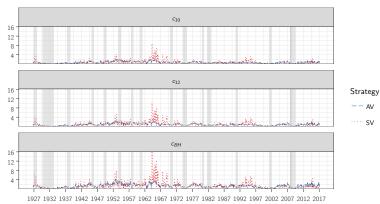
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# Investment Weights

#### Strategy Investment Weight



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# Investment Weight Again Again

CRSP Market Portfolio Investment Weights

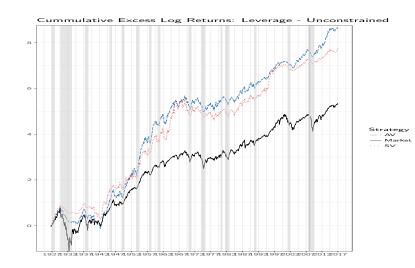
Portfolio	Target	Mean	St. Dev.	Min	Pctl(25)	Median	Pctl(75)	Max
SV	C <sub>10</sub>	0.697	0.762	0.009	0.246	0.512	0.874	8.743
AV	c <sub>10</sub>	0.702	0.383	0.018	0.425	0.667	0.915	2.296
SV	c <sub>12</sub>	0.841	0.920	0.011	0.297	0.618	1.055	10.552
AV	C <sub>12</sub>	0.848	0.463	0.022	0.513	0.805	1.104	2.772
SV	$c_{BH}$	1.290	1.412	0.017	0.455	0.948	1.619	16.193
AV	CBH	1.301	0.710	0.033	0.787	1.235	1.694	4.253

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### **US** Equity Performance



AV: 9.68% SV: 8.60% BH: 5.93%

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#### Performance Measures

- RET = annualized average log excess return
- Sharpe =  $\frac{\mathbb{E}[R_x]}{\sigma(R_x)}$ , dollar of returns for dollar of variance
- Sortino =  $\frac{\mathbb{E}[R_x-0]}{\sqrt{\int_{-\infty}^0 (0-R_x)^2 f(R_x) dR}}$ , return for downside
- Kappa $_n = \frac{\mathbb{E}[R_x 0]}{\sqrt[n]{LPM_n}}$ , where LPM is lower partial moment Kappa $_2 =$  Sortino
- Drawdown peak to valley loss in portfolio value
- Break Even trading costs, basis points, which erase gains
- Certainty Equivalent Return gain (CER) = Average utility from AV Average utility from SV for mean-variance investor with risk aversion  $\gamma$

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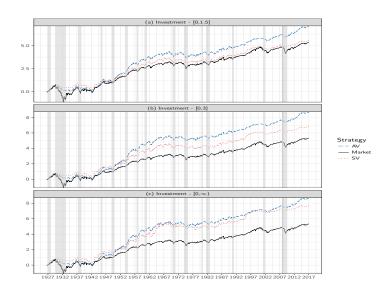
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#### Returns



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#### Performance

#### Unconstrained

- Outperforms with higher returns for the same variance
- Outperforms with other risk specifications downside, skewness, kurtosis,  $\boldsymbol{\alpha}$

1926:07-2016:12 c<sub>BH</sub>: Unconstrained

	Return	Sharpe	Sortino	$Kappa_3$	$Kappa_4$	$\alpha_{FF3}$	$lpha_{\mathit{FF3+Mom}}$
ВН	5.934	0.319	0.129	0.082	0.061		
SV	8.589	0.462	0.208	0.132	0.097	5.477	3.201
AV	9.676***	0.520*	0.225	0.150*	0.112*	5.594***	3.164

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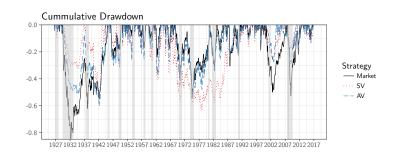
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### Drawdowns: c<sub>BH</sub>



Strategy	N	Max DD	Avg DD	Max Length	Avg Length	Max Recovery	Avg Recovery
ВН	82	-84.803	-8.069	188	11.549	154	7.207
SV	65	-63.637	-11.196	246	14.954	135	7.446
AV	87	-60.264	-9.026	205	10.851	135	5.034

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	c <sub>BH</sub> : Constraint - 1.5						
Portfolio	Return	Sharpe	Sortino	$Kappa_3$	$Kappa_4$		
ВН	5.932	0.319	0.129	0.082	0.061		
SV	6.171	0.467	0.200	0.128	0.091		
AV	7.885***	0.486	0.204	0.133	0.097		

c<sub>BH</sub>: Constraint - 3 Portfolio Return Sharpe Sortino Kappa<sub>3</sub> Kappa<sub>4</sub> BH 5.932 0.319 0.129 0.082 0.061 SV 7.606 0.456 0.199 0.129 0.096 0.112\*\* ΑV 9.677\*\*\* 0.522\*\* 0.226\*\* 0.150\*\*

Notes: \*\*\*, \*\*, and \* Significant at the 1, 5, and 10 percent levels.

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# Drawdown Insurance: Unconstrained

#### Knockout

- Drawndown large enough to shutter fund (investor pull-out), cost manager job
- Assuming 45% loss in a 12-month period as knockout
- SV 1.06% and AV .55% using Pav (2016)
- AV  $\approx$  half the cost to insure, Carr, Zhang, and Hadjiliadis (2011)

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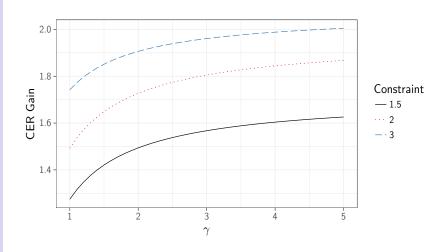
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# Investor Utility



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# Suggestively Systematic

- Check for performance across markets globally
- Test the dependence of AC and AV on the relationship of index daily returns and aggregate wealth in US equity time series
- Test the dependence of AV managed return performance on the relationship of daily returns and aggregate wealth -US time series and global cross section
- Test the ability of AV calculated from equity returns to manage investment in other asset classes

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### Global Performance

	AV		S	V	ВН	
Country	RET	Sharpe	RET	Sharpe	RET	Sharpe
AUS	12.477***	0.981	11.993	0.943	7.805	0.614
BRA	11.000***	0.291	9.037	0.240	6.163	0.164
CHN	27.381	0.868	24.926	0.790	12.286	0.390
DEU	11.064***	0.537*	7.633	0.371	5.399	0.262
FRA	7.243***	0.404	6.128	0.341	4.904	0.273
IND	14.893***	0.633	12.256	0.521	11.460	0.487
ITA	3.838	0.194	3.912	0.198	1.451	0.073
JPN	1.375***	0.068	0.129	0.006	-0.775	-0.038
UK	6.591***	0.485	5.984	0.441	5.111	0.376
World	8.603***	0.551	8.306	0.536	4.484	0.290

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# AC/AV and Systematic Risk

- Pollet and Wilson (2010) AC is positively related to the correlation of market returns and aggregate wealth, including the unobserved component of the "true market"
- AC signal changes in systematic risk when the daily returns used are a good proxy for the "true market" and the market is a significant part of aggregate wealth.
- This is similar to the difference in results between Goyal and Santa Clara (2003) and Bali et all (2005) when the latter removes a significant number of daily returns and the forecasting ability of idiosyncratic volatility disappears
- Thus we can run a placebo-like test on a sub-sample where the daily returns are not representative

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# Regressions

- Expect AC not to predict returns in the pre-1962 data but it should post-1962
- In-sample regression coefficients can be corrected for possible "volatility feedback" - Campbell and Hentschel (1992)
- Amihud and Hurvich (2004) bias correction
- Omit variance  $(SV_{t+1})$  prediction by AV as it works in both sub-samples
- Goyal and Welch (2008) forecasting relationships maybe unstable and quite sensitive to sample period choice; they may not respond dynamically with the limited information available to investors in real-time and may not explain or support a trading strategy

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# In-sample Sub-samples

AV	0.061			0.121	0.315
AC		-0.032		-0.099	
SV			-0.028		-0.264
$R^2$	0.004	0.001	0.001	0.010	0.026
Adjusted R <sup>2</sup>	0.002	-0.002	-0.002	0.005	0.021

#### $RET_{t+1}$ - 1962M6:2016M12

AV	-0.131			-0.168**	0.016
AC		0.047***		0.106***	
SV			-0.109		0.254
$R^2$	0.017	0.002	0.012	0.027	0.017
Adjusted R <sup>2</sup>	0.015	0.001	0.010	0.024	0.014

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# Out of Sample Stats

### Diebold-Marino Statistic (1995)

• DM = 
$$\frac{\bar{d}}{\sqrt{\frac{2\pi f_d(0)}{T}}}$$

 Asymptotically normally statistic comparing significance of accuracy ratio

### MSE-F Mcracken (2004)

• MSE-F = 
$$T \times \frac{\frac{1}{T} \sum_{1}^{T} (e_{b,t}^2 - e_{x,t}^2)}{MSFE_x}$$

• MSE-F = F-type test for significance in squared residual

### ENC-HLN Harvey, Lebourne and Newbold (1998)

- Optimal forecast  $= \hat{y}_t^* = (1 \lambda)\hat{y}_{b,t} + \lambda\hat{y}_{x,t}$
- $\lambda =$  measure of the optimal combination of forecasts

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# Out of Sample Results

Table: Sample 1939:12 to 2016:12

	DM	MSE-F	ENC-HLN
$AC_{t+1}$	1.604*	46.251***	1**
$SV_{t+1}$	1.041	21.57***	0.956**
$AV_{t+1}$	3.104***	198.267***	1***
$RET_{t+1}$	-2.027	-8.702	0

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### Robust Out of Sample Results

Table: Sample 1939:12 to 2016:12

Stat	Variable	DM	ENC-HLN
$R_T$	$SV_{t+1}$	8.874***	1.838***
$R_T$	$RET_{t+1}$	29.124***	4.871***
$A_T$	$SV_{t+1}$	2.647***	0.949***
$A_T$	$RET_{t+1}$	13.347***	1.68***

Notes: \*\*\*,\*\*, and \* Significant at the 1, 5, and 10 percent levels.

- AC fails when it "should"
- AV forecasts better than SV with robust in and out-of-sample performance
- These results compare the use AV to SV in forecasting not case either is good (RET) but AV is better

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# Systematic Performance

- Use a proxy for the weight of stock returns in the return on aggregate wealth,  $w_{s,t}$
- Form long/short portfolios for above and below median countries

Global Long - Short Ratio of Market RET to Wealth $\dagger$  RET  $(w_{s,t})$ 

	RET	Sharpe	$lpha_{ extit{FF3}}$	$lpha_{\it FF5}$	$lpha_{\it FF5+Mom}$
Long	12.601	0.747	9.484**	7.909*	7.725*
Short	7.537	0.562	5.038*	5.422*	5.318*
Long - Short	5.065	0.405	4.446***	2.488***	2.407**

- † Credit Suisse annual reports on global wealth (2000-2017)
  - Market Capt to GDP is also used to form long/short portfolios for robustness

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# Economy-Wide Performance

- Equity SV does not manage Currency investments -Moreira and Muir (2017)
- Equity AV should still signal unsystematic risk and manage other assets

Investment weight = 
$$\frac{c_{Asset}}{AV_{MSCI}}$$

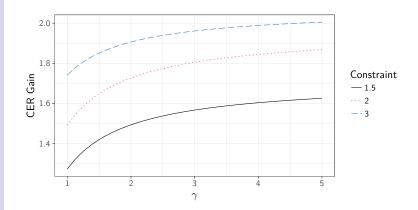
	AV		S	V	ВН		
Index	RET	Sharpe	RET	Sharpe	RET	Sharpe	
Dollar <sub>BB</sub>	1.324***	0.170	0.606	0.078	-0.296	-0.038	
Curr <sub>DB</sub>	1.195***	0.272*	-0.668	-0.152	-0.244	-0.056	
Carry <sub>DB</sub>	1.440***	0.134	-0.361	-0.033	-2.071	-0.192	
$Mom_{DB}$	1.942***	0.214	0.413	0.045	1.095	0.120	
REIT <sub>S&amp;P</sub>	26.706***	0.995	14.980	0.558	5.302	0.198	
Comm <sub>BB</sub>	-5.579***	-0.303	-6.431	-0.349	-5.279	-0.286	
$Bond_{\mathit{Univ}}$	3.951***	1.168***	1.436	0.425	3.276	0.969	

Conclusion

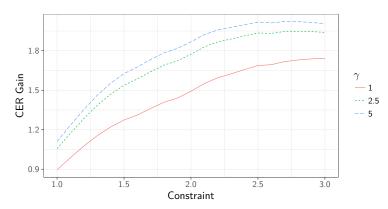
#### Conclusion

- AV management is better than SV: higher returns, better ratios. lower costs
- AV management is better because it times moving in and out of investments to changes in systematic risk which is compensated and non-systematic risk which is not
- As such, AV management is a useful signal both globally and across assets classes where SV management does not perform
- Thank you

# Leverage



# Leverage



Risk averse, mean-variance investors see substantial utility gains switching from the SV to AV managed portfolio and these gains increase with leverage usage and risk aversion

#### Return Prediction

#### 1962:07 - 2016:12

			$RET_{t+1}$		
AV	-0.131 p = 0.166			-0.168** $p = 0.020$	0.016 $p = 0.739$
AC		$0.047^{***}$ $p = 0.001$		$0.106^{***}$ $p = 0.0001$	
SV			-0.109 p = 0.746		0.254 $p = 0.893$
Constant	-0.000 $p = 1.000$	-0.000 $p = 1.000$	-0.000 $p = 1.000$	-0.000 $p = 1.000$	-0.000 $p = 1.000$
$N$ $R^2$ Adjusted $R^2$	655 0.017 0.015	655 0.002 0.001	655 0.012 0.010	655 0.027 0.024	655 0.017 0.014

Notes:

<sup>\*\*\*</sup>Significant at the 1 percent level.

<sup>\*\*</sup>Significant at the 5 percent level.

<sup>\*</sup>Significant at the 10 percent level.

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### Return Prediction

1926:08 - 1962:07

 $RET_{t+1}$  - 1926M7:1962M6

AV	0.061			0.121	0.315
AC		-0.032		-0.099	
SV			-0.028		-0.264
$R^2$	0.004	0.001	0.001	0.010	0.026
Adjusted R <sup>2</sup>	0.002	-0.002	-0.002	0.005	0.021

# Global Equity

- If AV management times investment to compensated risk because it changes in response to changes in systematic vs non-systematic risk it should work outside the US
- World AV and SV are market cap weighted averages of country values, US included

	Д	AV		V	ВН	
Country	RET	Sharpe	RET	Sharpe	RET	Sharpe
AUS	12.477	0.981	11.993	0.943	7.805	0.614
BRA	11.000	0.291	9.037	0.240	6.163	0.164
CHN	27.381	0.868	24.926	0.790	12.286	0.390
DEU	11.064	0.537	7.633	0.371	5.399	0.262
FRA	7.243	0.404	6.128	0.341	4.904	0.273
IND	14.893	0.633	12.256	0.521	11.460	0.487
ITA	3.838	0.194	3.912	0.198	1.451	0.073
JPN	1.375	0.068	0.129	0.006	-0.775	-0.038
UK	6.591	0.485	5.984	0.441	5.111	0.376
World	8.604	0.551	8.306	0.536	4.484	0.290

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# Global Equity Again

#### Drawdown Statistics

	AV				SV		ВН			
Country	Avg DD	Avg Length	Avg Recovery	Avg DD	Avg Length	Avg Recovery	Avg DD	Avg Length	Avg Recovery	
AUS	-6.302	7.174	3.348	-5.322	9.263	5.421	-6.318	8.600	4.550	
BRA	-8.059	9.560	4.208	-17.469	15.235	5.500	-15.064	17.067	4.286	
CHN	-9.511	10.333	5.917	-10.074	10.583	3.727	-19.374	27.400	2.000	
DEU	-11.051	10.625	5.783	-12.587	16.812	9.933	-10.706	17.125	12.333	
FRA	-10.263	14.111	5.941	-15.260	18.267	10.214	-11.590	19.071	15.077	
IND	-8.170	6.500	2.885	-12.545	12.467	5.733	-10.862	8.318	4.500	
ITA	-14.625	19.500	2.143	-18.174	22.571	2.333	-8.919	15.400	1.667	
JPN	-30.655	72.750	41.750	-78.514	294.000	175.000	-40.792	148.00	2.000	
UK	-6.060	11.609	4.652	-7.872	14.158	8.158	-6.018	10.560	7.240	
World	-6.982	9.909	7.333	-9.776	12.500	7.059	-8.209	10.091	6.429	

# Global Equity Again Again

### **Trading Costs**

		AV			SV				
Country	RET	$ \Delta\omega $	Break Even	RET	$ \Delta\omega $	Break Even	RET <sub>BH</sub>		
AUS	12.477	0.486	80.139	11.993	0.466	74.914	7.805		
BRA	11.000	0.253	159.118	9.037	0.623	38.462	6.163		
CHN	27.381	0.305	412.715	24.926	0.538	195.972	12.286		
DEU	11.064	0.499	94.545	7.633	0.581	32.052	5.399		
FRA	7.243	0.468	41.656	6.128	0.536	19.041	4.904		
IND	14.893	0.710	40.316	12.256	0.507	13.097	11.460		
ITA	3.838	0.448	44.366	3.912	0.603	33.991	1.451		
JPN	1.375	0.442	40.518	0.129	0.551	13.675	-0.775		
UK	6.591	0.473	26.113	5.984	0.509	14.287	5.111		
World	8.604	0.439	78.113	8.306	0.642	49.586	4.484		

#### Asset Classes

- If AV management times to changes systematic vs non-systematic risk, equity AV should provide a management signal for more than equities
- Moriera and Muir (2017) show that equity SV does not work as a signal for currency investment
- World AV and SV used with c calculated to match buy and hold for each index

	AV		S	V	ВН	
Index	RET	Sharpe	RET	Sharpe	RET	Sharpe
Bloomberg Dollar	1.324	0.170	0.606	0.078	-0.296	-0.038
DB Currency	1.195	0.272	-0.668	-0.152	-0.244	-0.056
DB Carry	1.440	0.134	-0.361	-0.033	-2.071	-0.192
DB Mom	1.942	0.214	0.413	0.045	1.095	0.120
S&P REIT	26.706	0.995	14.980	0.558	5.302	0.198
Bloomberg Commodity	-5.579	-0.303	-6.431	-0.349	-5.279	-0.286

J. Poland

# Asset Classes Again

#### Drawdown Statistics

AV					SV		ВН		
Index	Avg DD	Avg Length	Avg Recovery	Avg DD	Avg Length	Avg Recovery	Avg DD	Avg Length	Avg Recovery
Bloomberg Dollar	-8.393	29.000	12.750	-10.632	39.333	21.333	-13.565	60.000	27.000
DB Currency	-2.236	9.750	2.667	-10.471	59.500	20.500	-8.839	59.500	41.500
DB Carry	-7.336	14.250	7.375	-33.972	121.000	98.000	-30.332	60.000	21.000
DB Mom	-4.748	11.900	3.300	-14.679	59.000	17.000	-12.278	38.333	18.333
S&P REIT	-7.692	4.400	1.800	-15.016	9.455	5.000	-17.004	15.143	9.286
Bloomberg Commodity	-9.784	12.222	2.111	-31.116	39.000	12.333	-26.638	39.333	4.333

#### J. Poland

# Asset Classes Again Again

### **Trading Costs**

		AV		SV			
Index	RET	$ \Delta\omega $	Break Even	RET	$ \Delta\omega $	Break Even	RET <sub>BH</sub>
Bloomberg Dollar	1.324	0.411	32.846	0.606	0.620	12.126	-0.296
DB Currency	1.195	0.430	27.851	-0.668	0.482	-7.339	-0.244
DB Carry	1.440	0.427	68.600	-0.361	0.510	27.947	-2.071
DB Mom	1.942	0.441	16.010	0.413	0.599	-9.501	1.095
S&P REIT	26.706	0.592	301.254	14.980	0.807	99.908	5.302
Bloomberg Commodity	-5.579	0.460	-5.430	-6.431	0.555	-17.285	-5.279

#### Conclusion

- AV management is better than SV: higher returns, better ratios, lower costs
- AV management is better because it times moving in and out of investments to changes in systematic risk which is compensated and non-systematic risk which is not
- As such, AV management is a useful signal both globally and across assets classes where SV management does not perform
- Thank you

# More Pollet and Wilson (2010)

#### PW Details

- Start with Campbell and Viceira (2002) :  $r_{i,t+1} \approx \gamma \sigma_{i,m,t} \frac{\sigma_{i,t}^2}{2}$ , m is true market
- holds for i = s, stock market portfolio
- $r_{s,t+1} \approx \gamma cov_t(r_{s,t+1},r_{m,t+1}) \frac{\sigma_{s,t}^2}{2}$
- $r_{s,t+1} \approx \gamma cov_t(r_{s,t+1}, w_{s,t}r_{s,t+1} + (1-w_{s,t})r_{u,t+1}) \frac{\sigma_{s,t}^2}{2}$ , u is observable component
- $r_{s,t+1} \approx \gamma cov_t(r_{s,t+1}, w_{s,t}r_{s,t+1} + (1 w_{s,t})r_{u,t+1}) \frac{\sigma_{s,t}^2}{2}$
- $r_{s,t+1} \approx \gamma w_{s,t} var_t(r_{s,t+1}) + cov(r_{s,t}, (1-w_{s,t})r_{u,t+1}) \frac{\sigma_{s,t}^2}{2}$

# More Pollet and Wilson (2010)

- assume shocks to stock returns :  $\bar{\epsilon}_{z,t+1} + \epsilon_{i,t+1}$ , z common i idiosyncratic
- $r_{s,t+1} = \beta_t r_{m,t} + \overline{\epsilon}_{z,t+1}$
- $\operatorname{var}(\overline{\epsilon}_{z,t+1} + \epsilon_{i,t+1}) = \sigma_{z,t}^2 = \theta_t \sigma_{z,t}^2 + (1 \theta_t) \sigma_{i,t}^2$ ,  $\theta$  common part
- $r_{u,t+1} = \frac{1 w_{s,t}\beta_t}{1 w_{s,t}} r_{m,t} \frac{w_{s,t}\beta_t}{1 w_{s,t}}$
- substitute and simplify (many steps)
- $cov(r_{s,t}, r_{u,t+1}) = \frac{1 w_{s,t}\beta_t}{1 w_{s,t}} \frac{\bar{\sigma}_t^2}{\beta_t} \frac{\bar{\rho}_t \theta_t}{1 \theta_t} \bar{\rho}_t \frac{w_{s,t}\theta_t}{1 w_{s,t}} \frac{\bar{\sigma}_t^2}{\beta_t} \frac{1 \bar{\rho}_t}{1 \theta_t} \bar{\sigma}_t^2$
- more simplification
- $cov(r_{s,t}, r_{u,t+1}) = \pi_0 + \zeta_1 \bar{\rho_t} + \zeta_2 \bar{\sigma}_t^2$
- $\zeta_1$  positive but small for plausible values of  $w_{s,t}$  and  $\beta_t$ ,  $\zeta_2$  negative but small for plausible values
- Return