

# Razonamiento en Ontologías: Por qué y Cómo.

Basado en material de Ian Horrocks  
Dra. Pilar Bulacio  
[bulacio@cifasis-conicet.gov.ar](mailto:bulacio@cifasis-conicet.gov.ar)

# Bibliografia

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  - ▶ <http://www.w3.org/2001/sw/WebOnt/>





Repaso



# Orígenes: Lógicas descriptivas (DL)

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- ▶ Son una familia de formalismos basados en lógica de primer orden para la **Representación de Conocimiento**.
- ▶ Describen al **dominio** en función de **conceptos** (classes), **roles** (relationships) e **individuos**.
- ▶ Describen a la **semántica** que establece equivalencias entre *fórmulas lógicas de descripción* y *expresiones lógicas de predicados*.

# DL Basics

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- ▶ **Concepts (formulae)**
  - ▶ E.g., Person, Doctor, HappyParent, (Doctor  $\sqcap$  Lawyer)
- ▶ **Roles (modalities)**
  - ▶ E.g., hasChild, loves
- ▶ **Individuals (nominals)**
  - ▶ E.g., John, Mary, Italy
- ▶ **Operators (para formar conceptos y roles):**
  - ▶ Computables y si es posible, de baja complejidad



# DL: Ej. de **Constructores** de conceptos y roles

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- ▶ Restricciones numéricas de **cardinalidad** sobre roles, e.g.,  $\geq 3$  hasChild,  $\leq 1$  hasMother
- ▶ **Nominales** (conceptos *singleton*), e.g., {Italy}
- ▶ Dominios concretos (tipos de datos), e.g., hasAge.( $\geq 21$ )
- ▶ Roles **Inversos**, e.g., hasChild- (hasParent)
- ▶ Roles **Transitivos**, e.g., hasChild\* (descendant)
- ▶ Composición de roles, e.g., hasParent o hasBrother (uncle)



# The DL Family (1)

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- ▶ Smallest propositionally closed DL is *A<sub>L</sub>C* (Attributive Concept Language with Complements)
  - ▶ Concepts constructed using booleans
$$\sqcap, \sqcup, \neg$$
plus restricted quantifiers
$$\exists, \forall$$
  - ▶ Only atomic roles

E.g., Person all of whose children are either Doctors **or** have a child who is a Doctor:

$$\text{Person} \sqcap \forall \text{hasChild}.(\text{Doctor} \sqcup \exists \text{hasChild}.\text{Doctor})$$
$$\text{Person} \wedge [\text{hasChild}](\text{Doctor} \vee \cup \text{hasChild} \oplus \text{Doctor})$$


# Base de Conocimiento (KB) en LD

*F. Baader, W. Nutt*

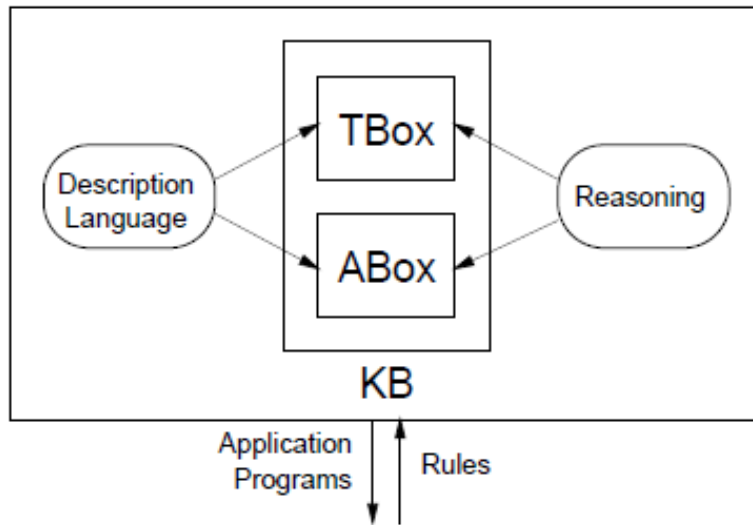



Fig. 2.1. Architecture of a knowledge representation system based on Description Logics.

- TBox (caja terminológica) contiene sentencias describiendo conceptos generales (i.e., relaciones entre conceptos).
- ABox (caja de aserciones) contiene sentencias "ground" indicando a donde pertenecen los individuos en la jerarquía (i.e., relaciones entre individuos y conceptos). Por ejemplo, las frases:
  - (1) Cada empleado es una persona (pertenece a la TBox),
  - (2) Bob es un empleado (pertenece a la ABox)





Razonamiento:  
Por qué lo necesitamos?



# Philosophical Reasons

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- ▶ Applications such as the Semantic Web aim at “machine understanding”
- ▶ Understanding is closely related to reasoning
  - ▶ Recognising semantic similarity in spite of syntactic differences
  - ▶ Recognising implicit consequences given explicitly stated facts



# Practical Reasons

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- ▶ Given key role of ontologies in many applications, it is essential to provide **tools** and **services** to help users:
  - ▶ Design and maintain high quality ontologies, e.g.:
    - ▶ **Meaningful** — all named classes can have instances
    - ▶ **Correct** — captured intuitions of domain experts
    - ▶ **Minimally redundant** — no unintended synonyms
    - ▶ **Richly axiomatised** — (sufficiently) detailed descriptions
  - ▶ Answer **queries** over ontology classes and instances, e.g.:
    - ▶ Find more general/specific classes
    - ▶ Retrieve individuals/tuples matching a given query
  - ▶ **Integrate** and align multiple ontologies



# Why Decidable Reasoning?

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- ▶ OWL constructors/axioms have been **restricted** so reasoning is decidable
- ▶ Consistent with Semantic Web's **layered architecture**
  - ▶ XML provides syntax **transport layer**
  - ▶ RDF(S) provides basic **relational language** and simple ontological primitives
  - ▶ OWL provides powerful but still decidable **ontology language**
  - ▶ ...
- ▶ W3C requirement for “**implementation experience**”
  - ▶ “Practical” algorithms for sound and complete reasoning



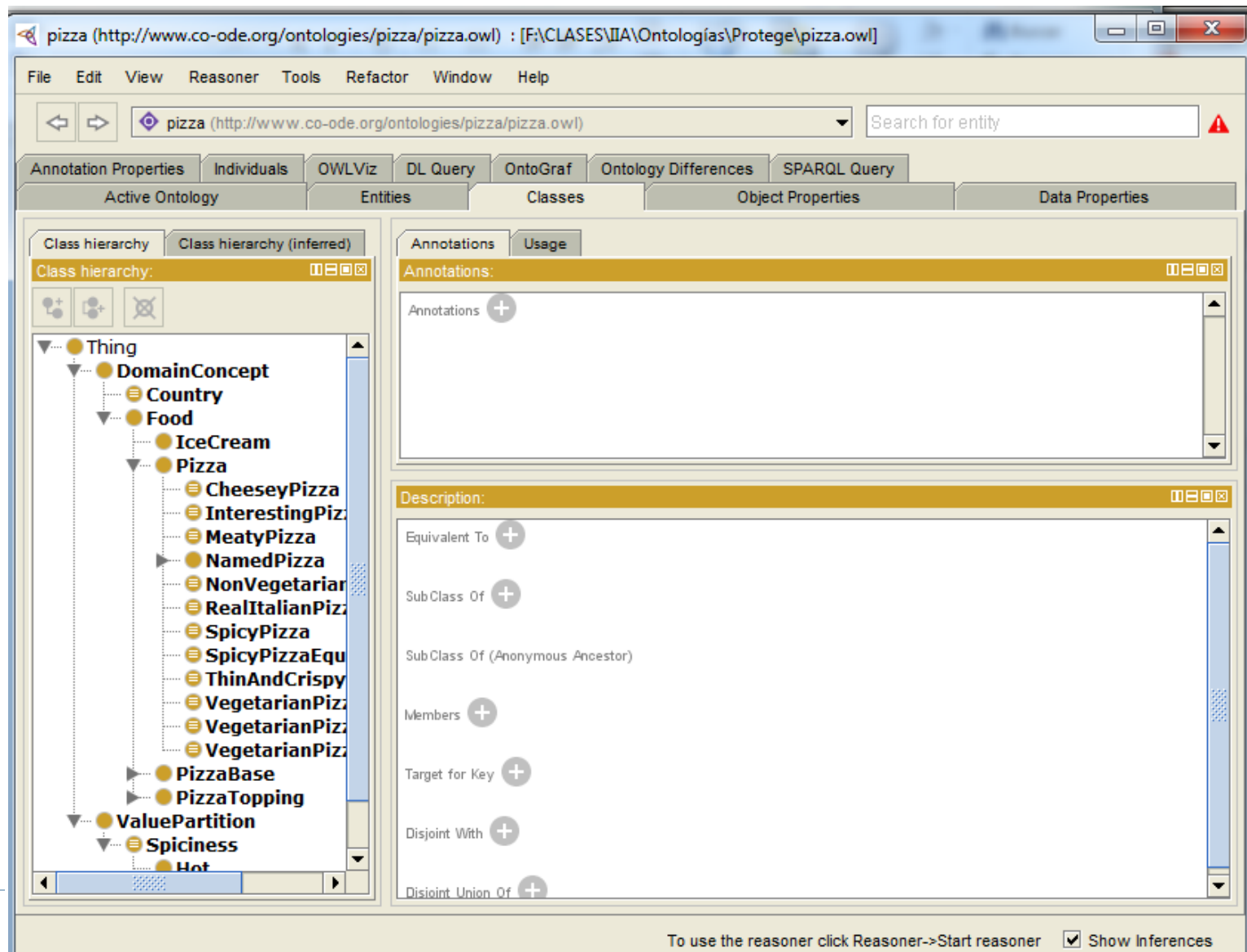
# Why Sound & Complete Reasoning?

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- ▶ Important for ontology **design**
  - ▶ Ontologists need to have complete **confidence** in reasoner
  - ▶ Otherwise they will cease to **trust** results
  - ▶ Doubting unexpected results makes reasoner useless
- ▶ Important for ontology **deployment**
  - ▶ Many realistic web applications will be **agent ↔ agent**
  - ▶ **No human intervention** to spot glitches in reasoning
- ▶ ...



# Protégé: Pizza





# Ontology Reasoning: How do we do it?



# Los razonadores DL brindan los siguientes servicios de inferencia

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- ▶ **Validación de la consistencia** de una ontología: el razonador puede comprobar si hay hechos contradictorios
- ▶ **Validación del cumplimiento de los conceptos** de la ontología: el razonador determina si es posible que una clase tenga instancias. *En el caso de que un concepto no sea satisfecho la ontología será inconsistente.*
- ▶ **Clasificación de la ontología**: el razonador computa a partir de los axiomas declarados en el TBox, las relaciones de subclase entre todos los conceptos declarados explícitamente a fin de construir la jerarquía de clases.
- ▶ **Resolución de consultas**: a partir de la jerarquía de clases se pueden formular consultas como *conocer todas las subclases de un concepto, inferir nuevas subclases de un concepto, las superclases directas, etc.*
- ▶ **Precisiones sobre los conceptos de la jerarquía**: el razonador puede inferir cuáles son las clases a las que directamente pertenece y mediante la jerarquía inferida obtener todas las clases a las cuales indirectamente pertenece una clase o individuo dentro de la ontología.





# Usando DL: Estándar DIG, DL Implementation Group

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- ▶ Smallest propositionally DL (conceptos booleanos + restricciones de existencia) es *ALC* *Attributive Concept Language with Complements*
  - ▶ *ALCR*+ (con roles transitivos) *ALCH* (con roles de inclusión) *ALCHR*+ es *SH* conocido como *SHOIQ*
- ▶ OWL DL based on *SHIQ* Description Logic
  - ▶ OWL extends *SHIQ* with datatypes and nominals (*SHOIN*( $D_n$ ))
  - ▶ In fact it is equivalent to *SHOIN*( $D_n$ ) DL
- ▶ OWL DL Benefits from many years of DL research
  - ▶ Well defined semantics
  - ▶ Formal properties well understood (complexity, decidability)
  - ▶ Known reasoning algorithms
  - ▶ Implemented systems (highly optimised)
- ▶ In fact there are three “species” of OWL (!)
  - ▶ OWL full is union of OWL syntax and RDF
  - ▶ OWL DL restricted to FOL fragment ( $\approx$  DAML+OIL)
  - ▶ OWL Lite is “simpler” subset of OWL DL



# Recordemos: OWL Class Constructors

Constructor	DL Syntax	Example	FOL Syntax
intersectionOf	$C_1 \sqcap \dots \sqcap C_n$	Human $\sqcap$ Male	$C_1(x) \wedge \dots \wedge C_n(x)$
unionOf	$C_1 \sqcup \dots \sqcup C_n$	Doctor $\sqcup$ Lawyer	$C_1(x) \vee \dots \vee C_n(x)$
complementOf	$\neg C$	$\neg$ Male	$\neg C(x)$
oneOf	$\{x_1\} \sqcup \dots \sqcup \{x_n\}$	{john} $\sqcup$ {mary}	$x = x_1 \vee \dots \vee x = x_n$
allValuesFrom	$\forall P.C$	$\forall$ hasChild.Doctor	$\forall y.P(x, y) \rightarrow C(y)$
someValuesFrom	$\exists P.C$	$\exists$ hasChild.Lawyer	$\exists y.P(x, y) \wedge C(y)$
maxCardinality	$\leq_n P$	$\leq 1$ hasChild	$\exists \leq_n y.P(x, y)$
minCardinality	$\geq_n P$	$\geq 2$ hasChild	$\exists \geq_n y.P(x, y)$

- ▶ XMLS **datatypes** as well as classes in  $\forall P.C$  and  $\exists P.C$ 
  - ▶ Restricted form of DL **concrete domains**

# Recordemos: RDFS Syntax

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E.g.,  $\text{Person} \sqcap \forall \text{hasChild.}(\text{Doctor} \sqcup \exists \text{hasChild.Doctor})$ :

```
<owl:Class>
  <owl:intersectionOf rdf:parseType=" collection">
    <owl:Class rdf:about="#Person"/>
    <owl:Restriction>
      <owl:onProperty rdf:resource="#hasChild"/>
      <owl:toClass>
        <owl:unionOf rdf:parseType=" collection">
          <owl:Class rdf:about="#Doctor"/>
          <owl:Restriction>
            <owl:onProperty rdf:resource="#hasChild"/>
            <owl:hasClass rdf:resource="#Doctor"/>
          </owl:Restriction>
        </owl:unionOf>
      </owl:toClass>
    </owl:Restriction>
  </owl:intersectionOf>
</owl:Class>
```



# Recordemos: OWL Axioms

Axiom	DL Syntax	Example
subClassOf	$C_1 \sqsubseteq C_2$	Human $\sqsubseteq$ Animal $\sqcap$ Biped
equivalentClass	$C_1 \equiv C_2$	Man $\equiv$ Human $\sqcap$ Male
disjointWith	$C_1 \sqsubseteq \neg C_2$	Male $\sqsubseteq \neg$ Female
sameIndividualAs	$\{x_1\} \equiv \{x_2\}$	{President_Bush} $\equiv$ {G_W_Bush}
differentFrom	$\{x_1\} \sqsubseteq \neg\{x_2\}$	{john} $\sqsubseteq \neg\{peter\}$
subPropertyOf	$P_1 \sqsubseteq P_2$	hasDaughter $\sqsubseteq$ hasChild
equivalentProperty	$P_1 \equiv P_2$	cost $\equiv$ price
inverseOf	$P_1 \equiv P_2^-$	hasChild $\equiv$ hasParent <sup>-</sup>
transitiveProperty	$P^+ \sqsubseteq P$	ancestor <sup>+</sup> $\sqsubseteq$ ancestor
functionalProperty	$\top \sqsubseteq \leq 1P$	$\top \sqsubseteq \leq 1$ hasMother
inverseFunctionalProperty	$\top \sqsubseteq \leq 1P^-$	$\top \sqsubseteq \leq 1$ hasSSN <sup>-</sup>

- ▶ Axioms (mostly) **reducible to inclusion** ( $\sqsubseteq$ )
  - ▶  $C \equiv D$  iff both  $C \sqsubseteq D$  and  $D \sqsubseteq C$
- ▶ Obvious **FOL (Lógica de Primer Orden) equivalences**
  - ▶ E.g.,  $C \equiv D \Leftrightarrow \forall x.C(x) \leftrightarrow D(x)$ ,  $C \sqsubseteq D \Leftrightarrow \forall x.C(x) \rightarrow D(x)$

# Basic Inference Tasks

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- ▶ Kw is **correct** (captures intuitions)
  - ▶ Does C **subsume** D w.r.t. ontology  $\mathcal{O}$ ? ( $C^{\mathcal{I}} \subseteq D^{\mathcal{I}}$  in **every model**  $\mathcal{I}$  of  $\mathcal{O}$ )
- ▶ Kw is **minimally redundant** (no unintended synonyms)
  - ▶ Is C **equivalent** to D w.r.t.  $\mathcal{O}$ ? ( $C^{\mathcal{I}} = D^{\mathcal{I}}$  in **every model**  $\mathcal{I}$  of  $\mathcal{O}$ )
- ▶ Kw is **meaningful** (classes can have instances)
  - ▶ Is C **satisfiable** w.r.t.  $\mathcal{O}$ ? ( $C^{\mathcal{I}} \neq \emptyset$  in **some model**  $\mathcal{I}$  of  $\mathcal{O}$ )
- ▶ **Querying** Kw
  - ▶ Is x an **instance** of C w.r.t.  $\mathcal{O}$ ? ( $x^{\mathcal{I}} \in C^{\mathcal{I}}$  in **every model**  $\mathcal{I}$  of  $\mathcal{O}$ )
  - ▶ Is  $\langle x, y \rangle$  an **instance** of R w.r.t.  $\mathcal{O}$ ? ( $(x^{\mathcal{I}}, y^{\mathcal{I}}) \in R^{\mathcal{I}}$  in **every model**  $\mathcal{I}$  of  $\mathcal{O}$ )
- ▶ Above problems can be solved using **highly optimised** DL reasoners



# DL Reasoning: Basics

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- ▶ Tableau algorithms used to test **satisfiability** (consistency)
  - ▶ Decompose  $C$  syntactically
    - ▶ Infer constraints on elements of model
  - ▶ Tableau rules correspond to constructors in logic ( $\sqcap, \sqcup$  etc)
  - ▶ Stop when no more rules applicable or **clash** occurs
    - ▶ Clash is an obvious contradiction, e.g.,  $A(x), \neg A(x)$
  - ▶ Cycle check (**blocking**) may be needed for termination
  - ▶  $C$  satisfiable **iff** rules can be applied such that a fully expanded clash free tree is constructed
- 
- ▶ Un razonador *tableaux* posee sólo la funcionalidad de verificar la satisfactibilidad de un ABox con respecto a un TBox. Todas las otras tareas de razonamiento pueden ser reducidas a pruebas de consistencia con la KB mediante la transformación apropiada.



# DL Reasoning: Advanced Techniques

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- ▶ Satisfiability w.r.t. an Ontology  $\mathcal{O}$ 
  - ▶ For each axiom  $C \sqsubseteq D \in \mathcal{O}$ , add  $\neg C \sqcup D$  to every node label
- ▶ More expressive DLs
  - ▶ Basic technique can be extended to deal with
    - ▶ Role inclusion axioms (role hierarchy)
    - ▶ Number restrictions
    - ▶ Inverse roles
    - ▶ Concrete domains/datatypes
    - ▶ Aboxes
    - ▶ etc.



# Comparison of Reasoners for large Ontologies in the OWL 2 EL Profile

	Reasoning Characteristics							
	CB	CHL	FaCT++	Hermit	Pellet	RP	SR	TrOWL (REL)
Methodology	consequence-based	completion rules	tableau-based	hypertableau	tableau-based	tableau-based	completion rules	approximation (completion rules)
Soundness	+	+	+	+	+	+	+	+ (+)
Completeness	+	+	+	+	+	+	+	- (+)
Expressivity	Horn $SHIF$	$EL^+$	$SROIQ(D)$	$SROIQ(D)$	$SROIQ(D)$	$SHIQ(D-)$	$EL^+$	third-party reasoner (approximating $SROIQ$ ; subset of $EL^{++}$ )
Incremental Classification (addition/removal)	$\pm$	$\pm$	$\pm$	$\pm$	$\pm$	$\pm$	$\pm$	$\pm$
Rule Support	-	-	-	+(SWRL)	+(SWRL)	+(SWRL, nRQL)	-	-
Justifications	-	+	-	-	+	+	-	-
ABox Reasoning	-	+	+	+	+(SPARQL)	+(SPARQL, nRQL)	-	+(SPARQL)





# DL Query:

[http://webont.org/owled/2006/acceptedLong/submission\\_9.pdf](http://webont.org/owled/2006/acceptedLong/submission_9.pdf)

Protege interface showing a DL query and its results.

URL: pizza (http://www.co-ode.org/ontologies/pizza/pizza.owl) : [F:\CLASES\IIA\Ontologías\Protege\pizza.owl]

Menu: File Edit View Reasoner Tools Refactor Window Help

Search for entity

Active Ontology: pizza (http://www.co-ode.org/ontologies/pizza/pizza.owl)

DL query: hasTopping some MozzarellaTopping

Execute Add to ontology

Query results

Sub classes (21)

Class	?
American	?
AmericanHot	?
Cajun	?
Capricciosa	?
Caprina	?
Fiorentina	?
FourSeasons	?
Giardiniera	?
LaReine	?
Margherita	?
Mushroom	?
Napoletana	?
Parma	?

Reasoner active ☒ Show Inferences

Class hierarchy: Thing

DL query: Query (class expression)

Query results: Sub classes (21)

Options: ☐ Super classes, ☐ Ancestor classes, ☐ Equivalent classes, ☒ Subclasses, ☐ Descendant classes, ☐ Individuals

## Ejemplos: DL Queries

- ▶ hasTopping only (MozzarellaTopping  
or PeperoniSausageTopping  
or TomatoTopping)
- ▶ hasTopping some MozzarellaTopping
- ▶ hasTopping some PeperoniSausageTopping
- ▶ hasTopping some TomatoTopping



# SPARQL



The image is a screenshot of a web browser window. The address bar shows the URL `skos.um.es/TR/rdf-sparql-query/`. The browser's toolbar includes icons for back, forward, and refresh, along with a search bar. Below the toolbar, there are several bookmarks: "Aplicaciones", "Google", "Disney Junior", "Poisson Rouge . Red...", and "Protocolos TCP/IP". On the right side of the toolbar, there is a star icon for bookmarks and a folder icon labeled "Otros marcadores".

The main content area of the browser displays the W3C logo at the top left. Below the logo, the title "SPARQL Lenguaje de consulta para RDF" is prominently displayed in a large, blue font. Underneath the title, the text "Recomendación del W3C de 15 de enero de 2008" is shown in a smaller, blue font. Further down, there are three sections of text, each starting with a bold label followed by a link:

- Versión original (en Inglés):** <http://www.w3.org/TR/2008/REC-rdf-sparql-query-20080115/>
- Última versión:** <http://www.w3.org/TR/rdf-sparql-query/>
- Versión anterior:** <http://www.w3.org/TR/2007/PR-rdf-sparql-query-20071112/>

At the bottom, the "Editores:" section lists two individuals: Eric Prud'hommeaux, W3C <[eric@w3.org](mailto:eric@w3.org)> and Andy Seahorne, Hewlett-Packard Laboratories, Bristol <[andy.seahorne@hp.com](mailto:andy.seahorne@hp.com)>.

# SPARQL

Form of the query atom	Condition on interpretation
Type( $a, C$ )	$\sigma(a) \in C^I$
PropertyValue( $a, p, v$ )	$\langle \sigma(a), \sigma(v) \rangle \in p^I$
SameAs( $a, b$ )	$\sigma(a) = \sigma(b)$
DifferentFrom( $a, b$ )	$\sigma(a) \neq \sigma(b)$
SubClassOf( $C_1, C_2$ )	$C_1^I \subseteq C_2^I$
EquivalentClass( $C_1, C_2$ )	$C_1^I = C_2^I$
DisjointWith( $C_1, C_2$ )	$C_1^I \cap C_2^I = \emptyset$
ComplementOf( $C_1, C_2$ )	$C_1^I = \Delta^I \setminus C_2^I$
SubPropertyOf( $p, q$ )	$p^I \subseteq q^I$
EquivalentProperty( $p, q$ )	$p^I = q^I$
Functional( $p$ )	$\langle x, y \rangle \in p^I$ and $\langle x, z \rangle \in p^I$ implies $y = z$
InverseFunctional( $p$ )	$\langle y, x \rangle \in p^I$ and $\langle z, x \rangle \in p^I$ implies $y = z$
Transitive( $p$ )	$\langle x, y \rangle \in p^I$ and $\langle y, z \rangle \in p^I$ implies $\langle x, z \rangle \in p^I$
Symmetric( $p$ )	$\langle x, y \rangle \in p^I$ implies $\langle y, x \rangle \in p^I$
Annotation( $s, p_a, o$ )	$\langle s, o \rangle \in p_a^I$

Table 2. Satisfaction of a SPARQL-DL query atom w.r.t. an interpretation

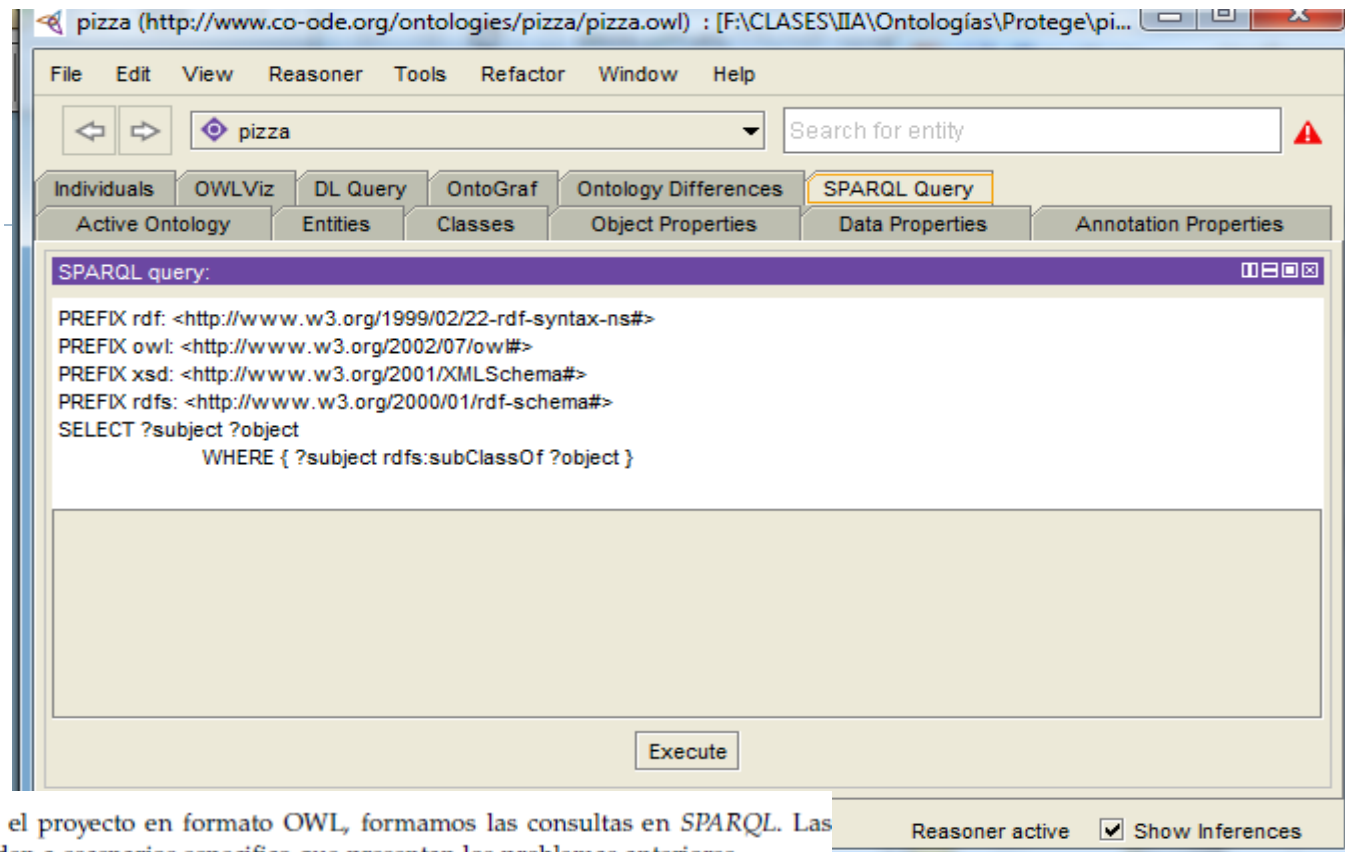
```

?C rdfs:subClassOf _:x .
_:x rdf:type owl:Restriction .
_:x owl:onProperty ex:q .
_:x ?p ?C .

```

# SPARQL:

## ► Ejemplo:



Trabajando sobre el proyecto en formato OWL, formamos las consultas en SPARQL. Las mismas se corresponden a escenarios específicos que presentan los problemas anteriores.

1. *Buscar las Personas que hayan creado alguna Pista en el año 1969.*

```
PREFIX cla: <http://www.owl-ontologies.com/Ontology1383937954.owl#>
PREFIX ind: <http://www.owl-ontologies.com/>
SELECT DISTINCT ?autor
WHERE {
  ?pista rdf:type cla:Pista .
  ?pista cla:Año_creación_obra ?año .
  ?pista cla:Autores ?autor .
}
HAVING (?año = 1969)
```

RESULT:

Otis\_Spann

# Research Challenges

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- ▶ Increased **expressive power**
  - ▶ Existing DL systems implement (at most)  $\mathcal{SHIQ}$
  - ▶ OWL extends  $\mathcal{SHIQ}$  with datatypes and nominals ( $\mathcal{SHOIN}(\mathbf{D_n})$ )
- ▶ **Scalability**
  - ▶ Very large ontologies
  - ▶ Reasoning with (very large numbers of) individuals
- ▶ Other reasoning tasks (**non-standard inferences**)
  - ▶ Querying
  - ▶ Matching
  - ▶ Least common subsumer
  - ▶ ...
- ▶ **Tools** and Infrastructure
  - ▶ Support for large scale ontological engineering and deployment



# Summary

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- ▶ An **Ontology** is an engineering artifact consisting of:
  - ▶ A **vocabulary** of terms
  - ▶ An **explicit specification** their **intended meaning**
- ▶ Ontologies are set to play a **key role** in many applications
  - ▶ e-Science, Medicine, Databases, Semantic Web, etc.
- ▶ **Reasoning is important** because
  - ▶ Understanding is closely related to reasoning
  - ▶ Essential for design, maintenance and deployment of ontologies
- ▶ **Reasoning support** based on DL systems
  - ▶ Sound and complete reasoning
  - ▶ Highly optimised implementations
- ▶ **Challenges remain**
  - ▶ Expressive power; scalability; new reasoning tasks; tools and infrastructure



# Select Bibliography

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- ▶ Ian Horrocks, Peter F. Patel-Schneider, and Frank van Harmelen. From SHIQ and RDF to OWL: The making of a web ontology language. *Journal of Web Semantics*, 2003.
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All available from <http://www.cs.man.ac.uk/~horrocks/Publications/>

