

Theorem 1. *f is injective if and only if $f(A \cap B) = f(A) \cap f(B)$, for all $A, B \subseteq X$.*

Proof. proof here

□