Theorem 1. f is injective if and only if $f(A \cap B) = f(A) \cap f(B)$, for all $A, B \subseteq X$.

Proof. proof here

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