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Ollo

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En particular hay ∞'s primos

$$\sum_{i=1}^{n} \frac{1}{i} = O(\log$$

$$\#\{p \le n\} = O($$

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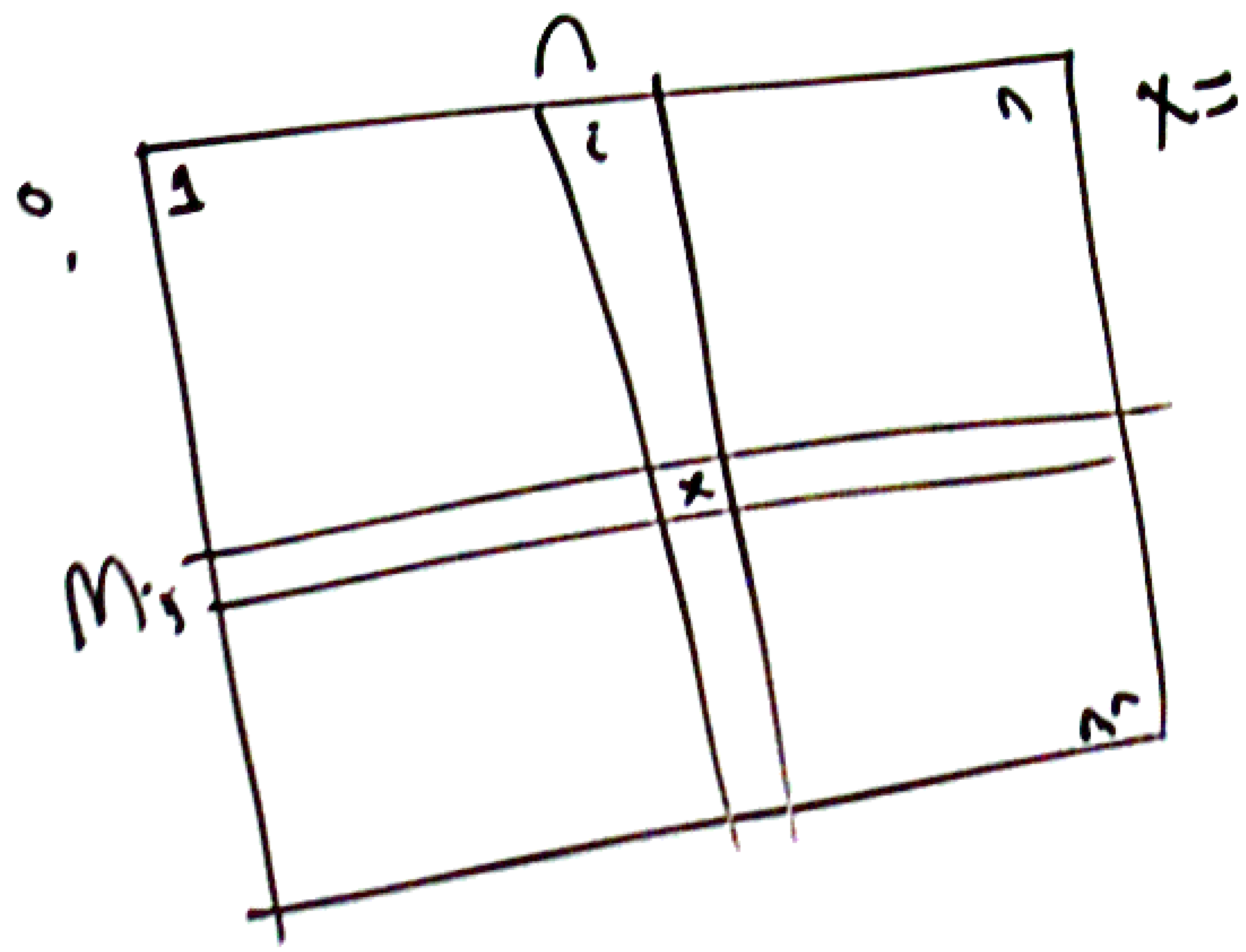
$= \# \{ b \in [r+1, \ldots, r+n] : (b,n) = 1 \}$.



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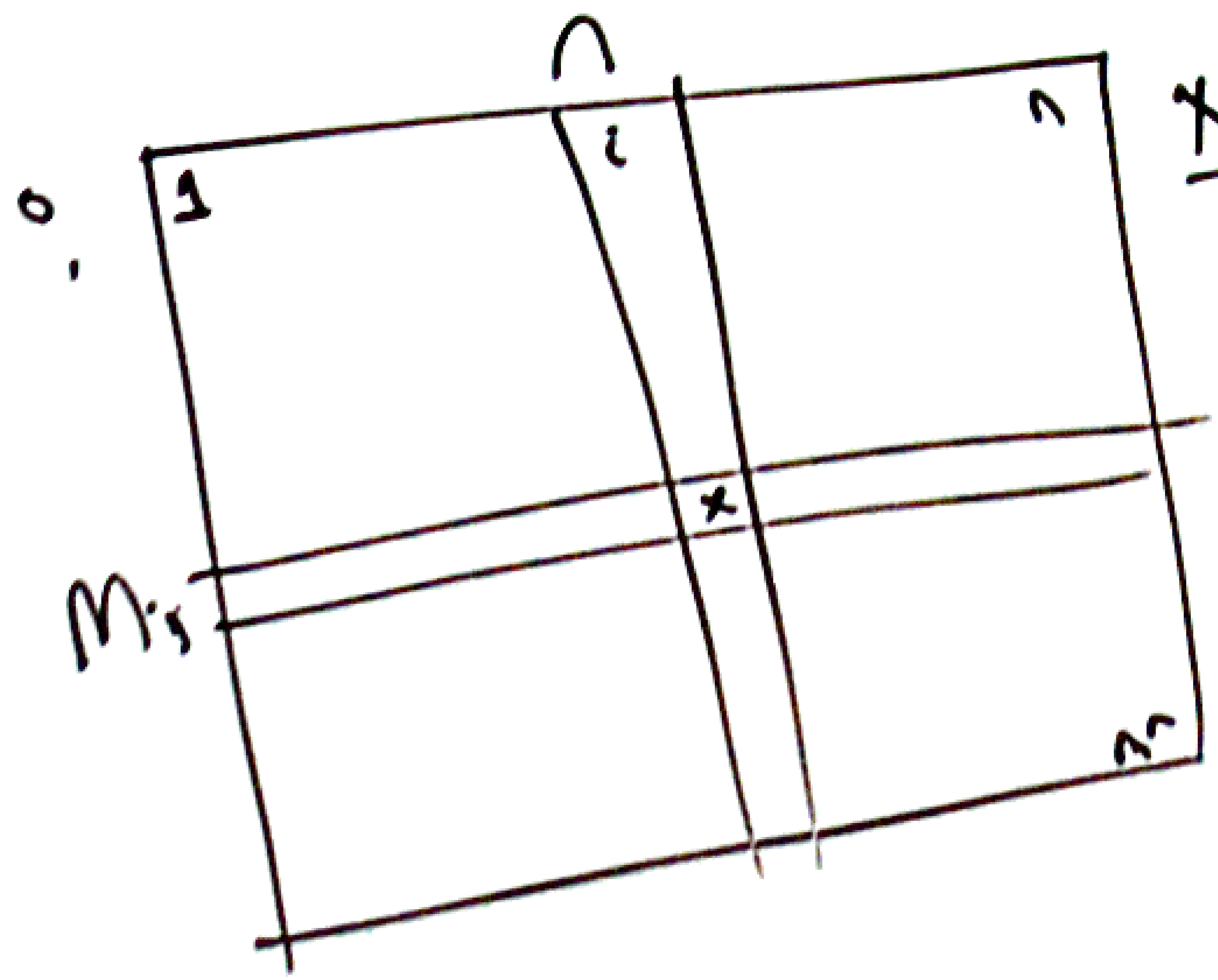

$\underline{x = n \cdot j + i}$

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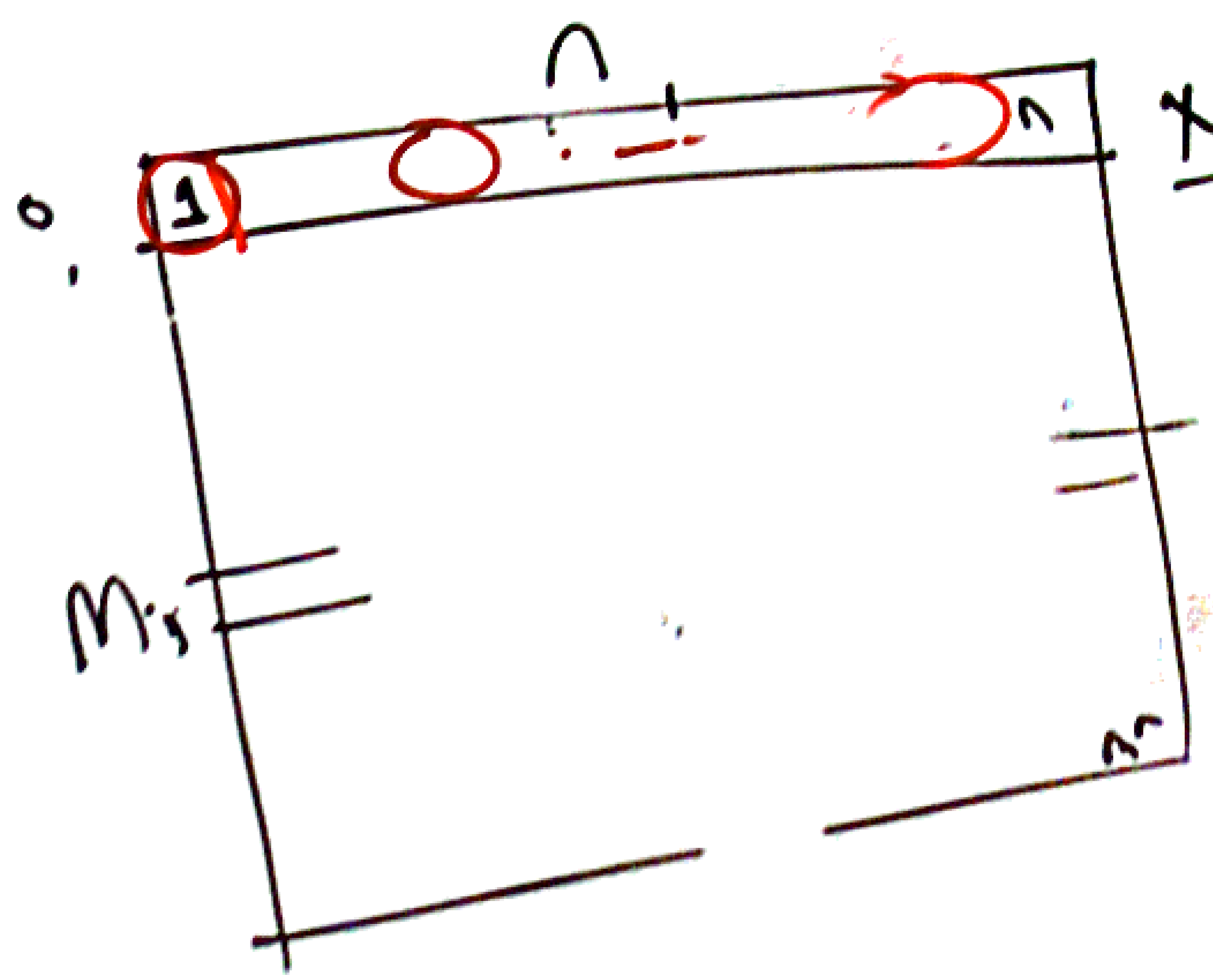

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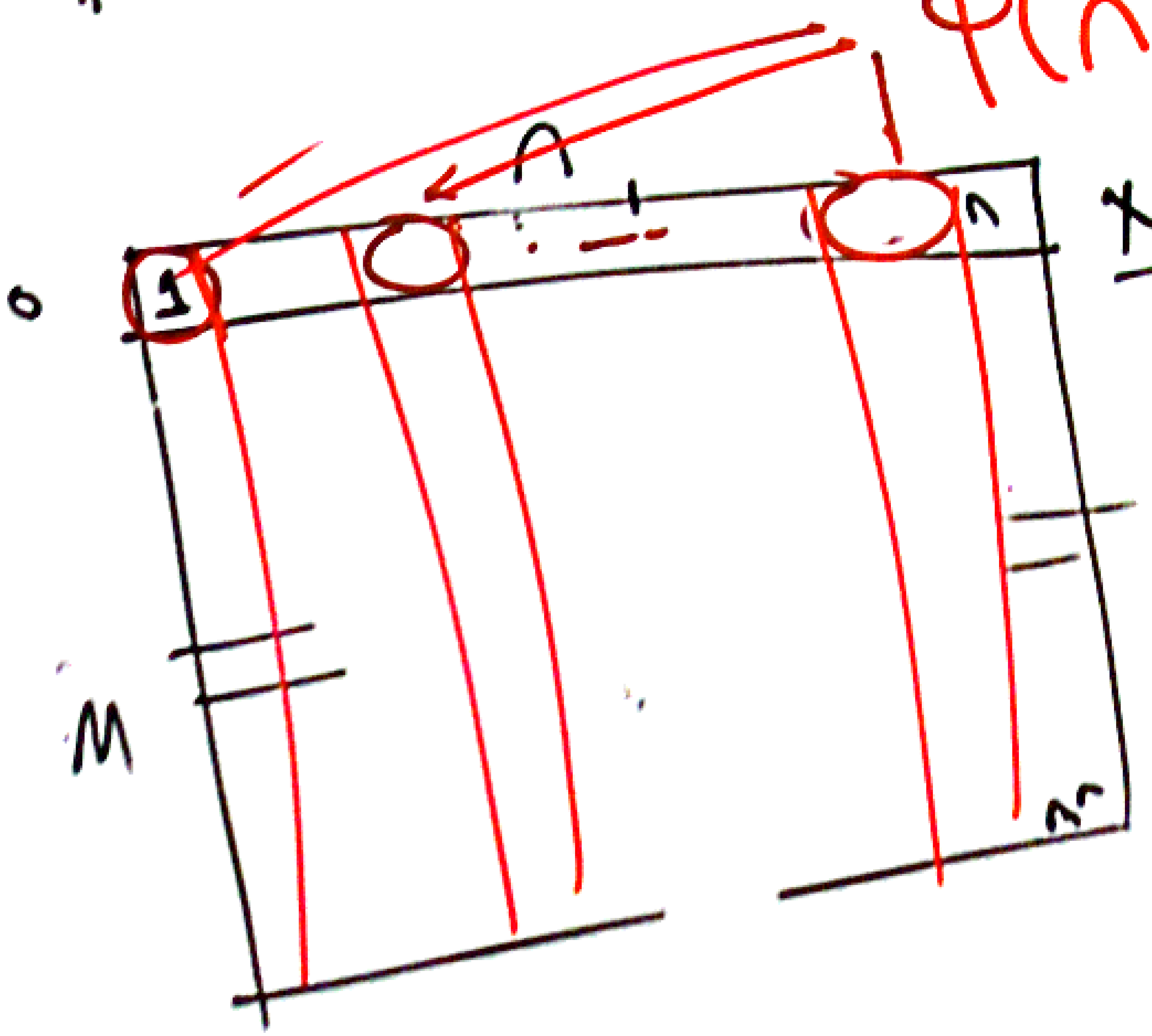
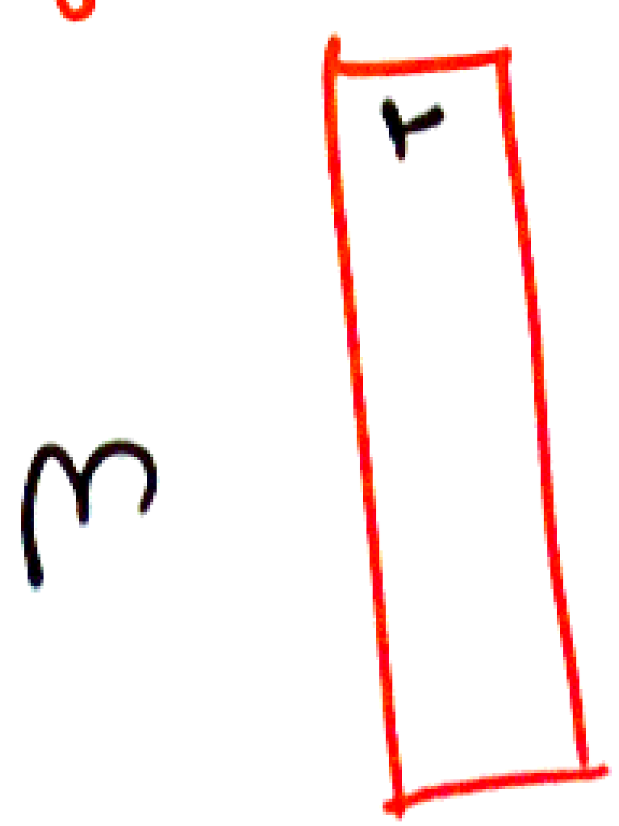


$x = n \cdot j + i$

$(\underset{d}{b},\underset{d}{n})=1 \Rightarrow (\underset{d}{b+nk},\underset{d}{n})=1$



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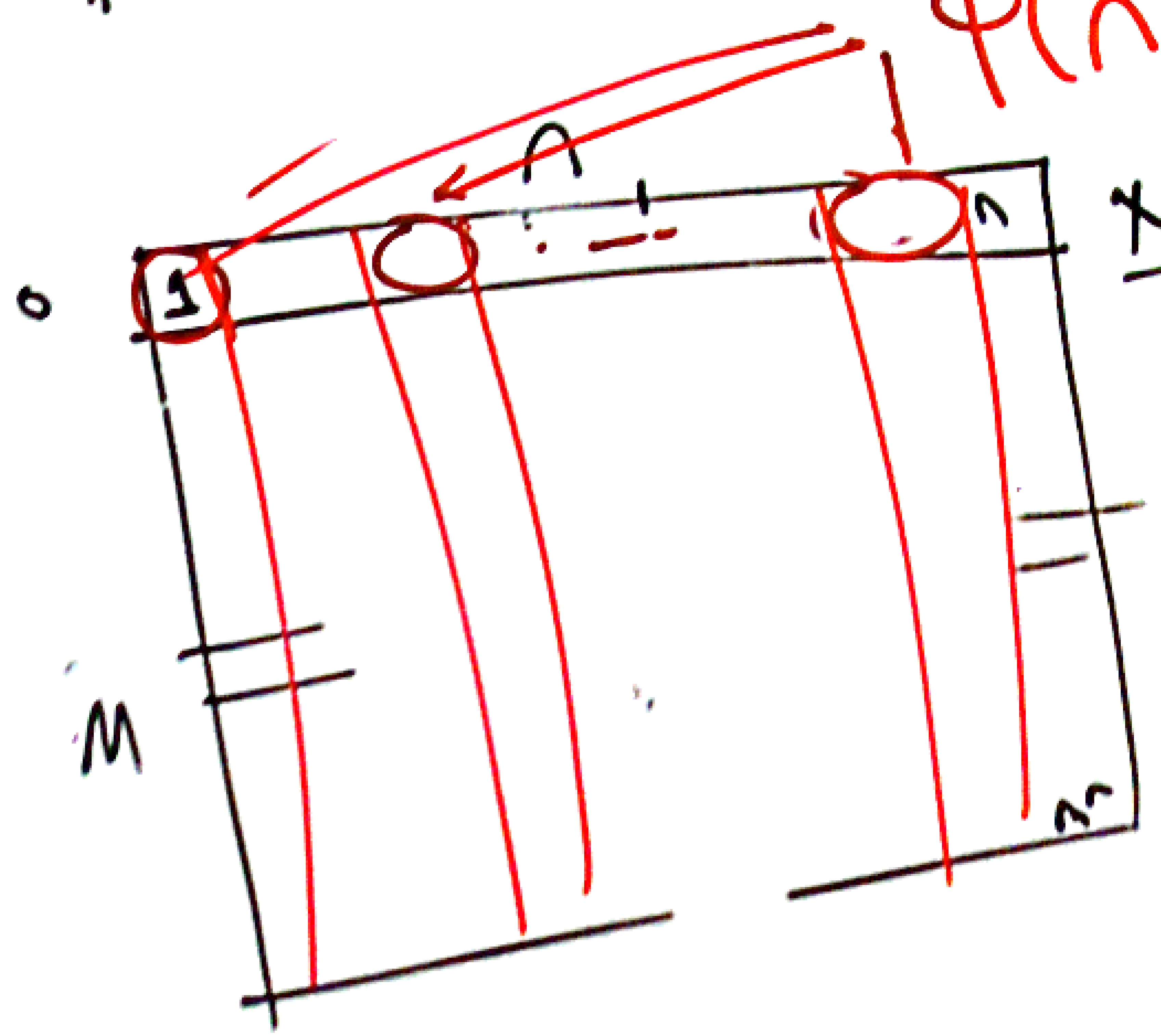
Todos los residuos % m en S son distintos



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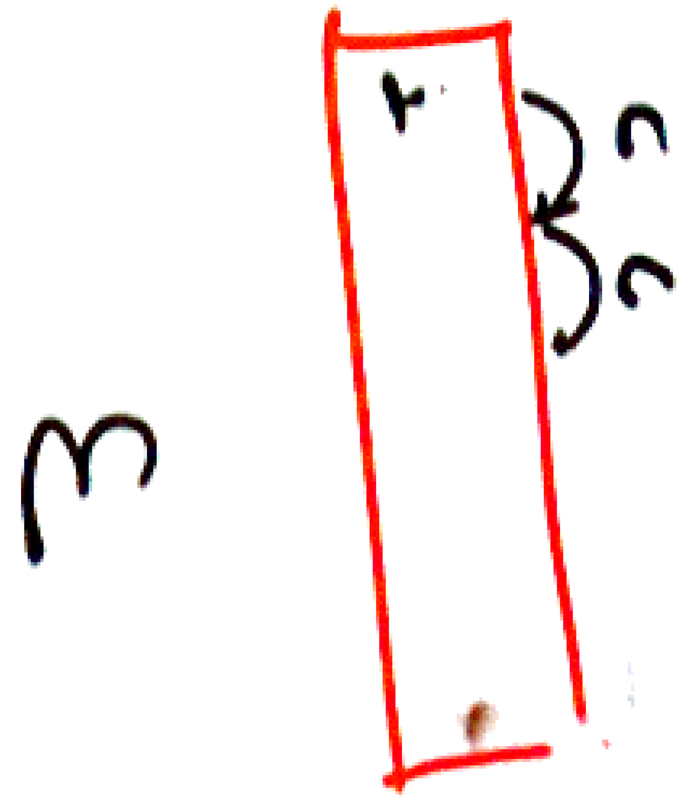
$(b, n) = 1 \Rightarrow (b + nk, n) = 1$



$S = \{r + 0 \cdot n, r + 1 \cdot n, \dots, r + (m-1)n\}$

$(r + jn) \% m = (r + in) \% m$

$(i-j) \cdot n \% m = 0 \rightarrow (i-j) \% m = 0$

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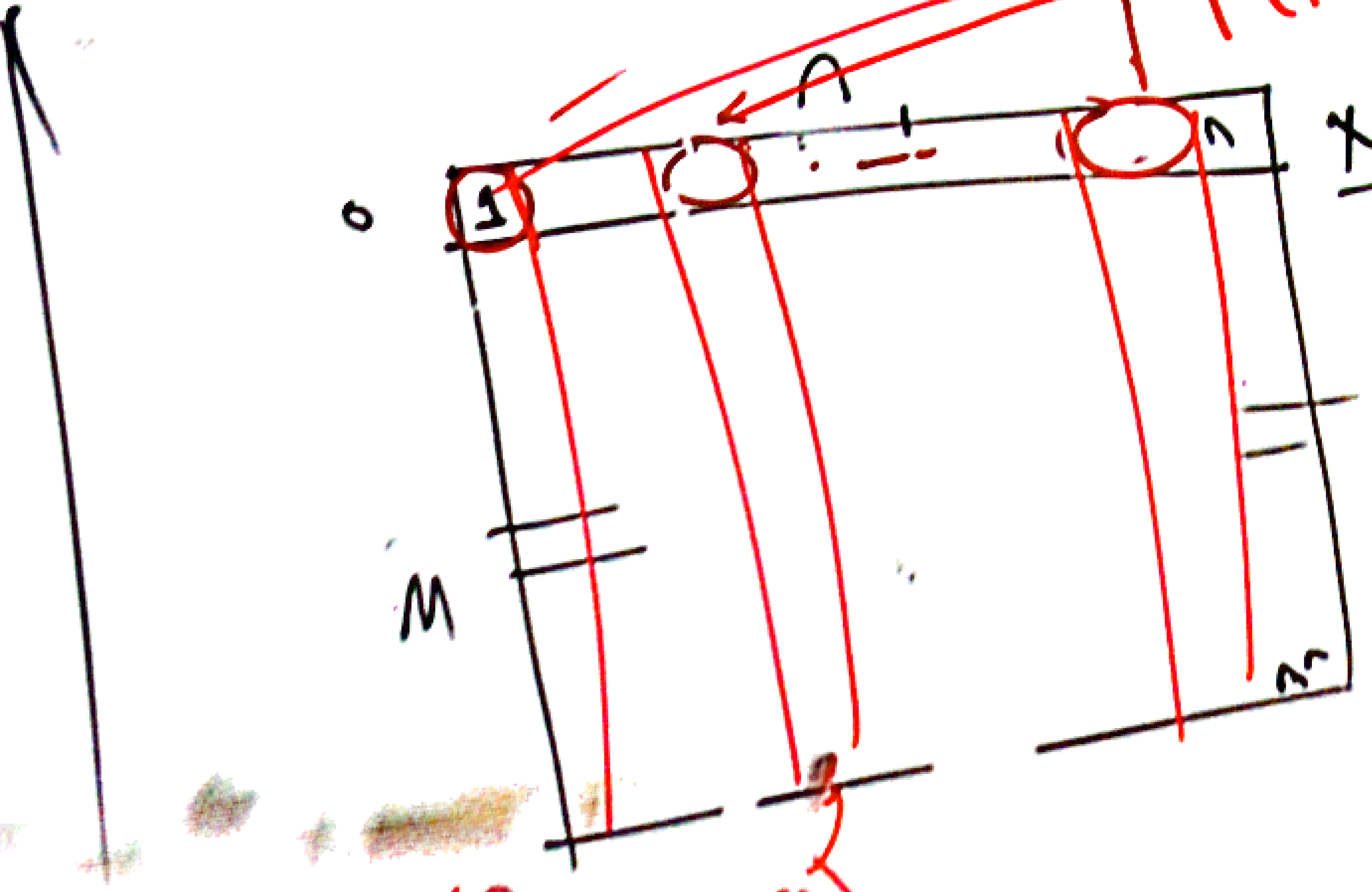

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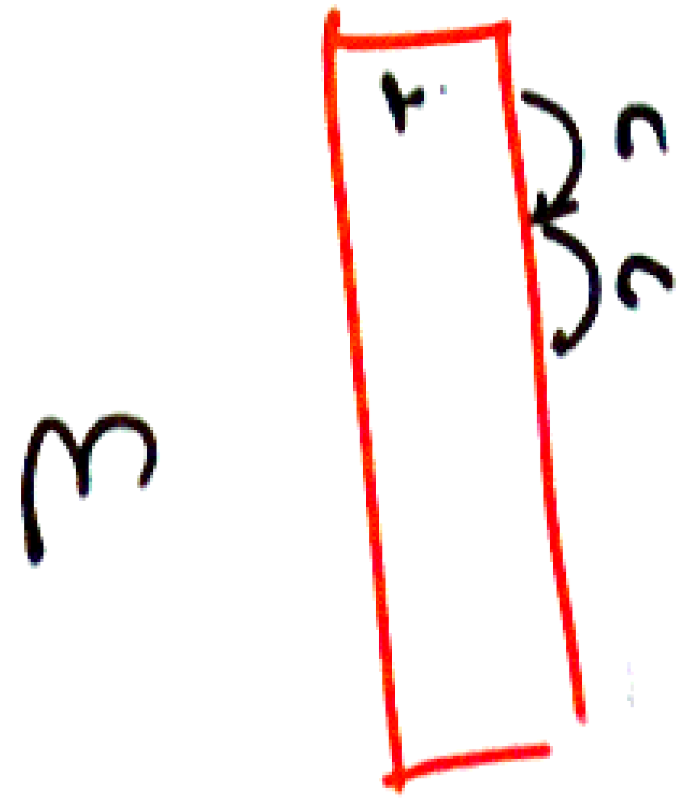

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$[1, \_\_\_, m]$

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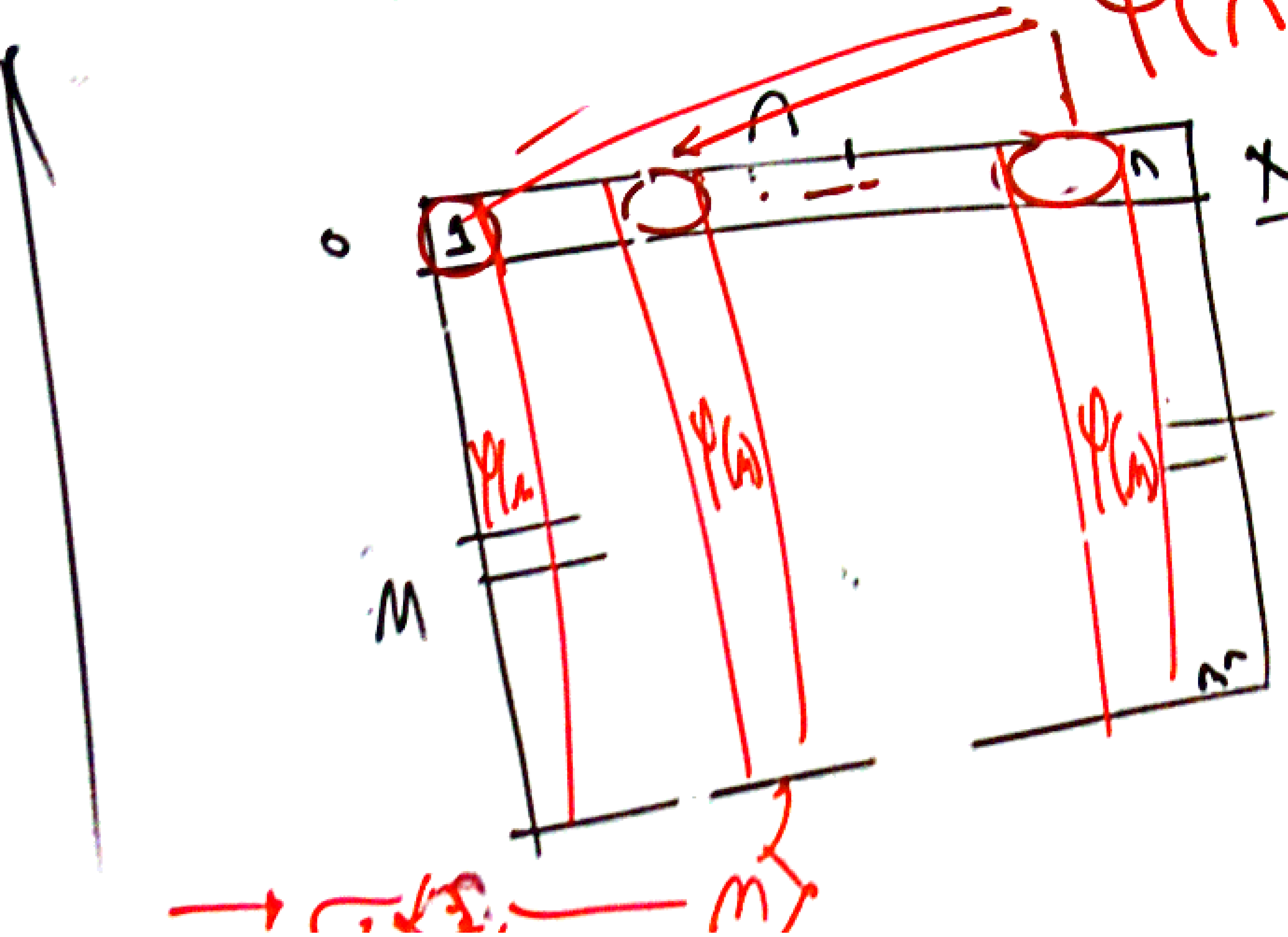

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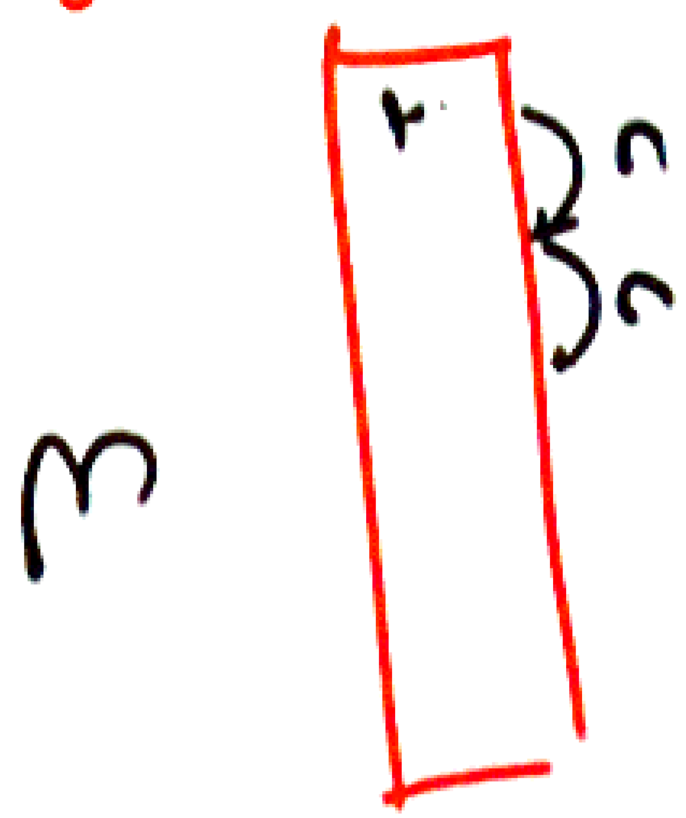

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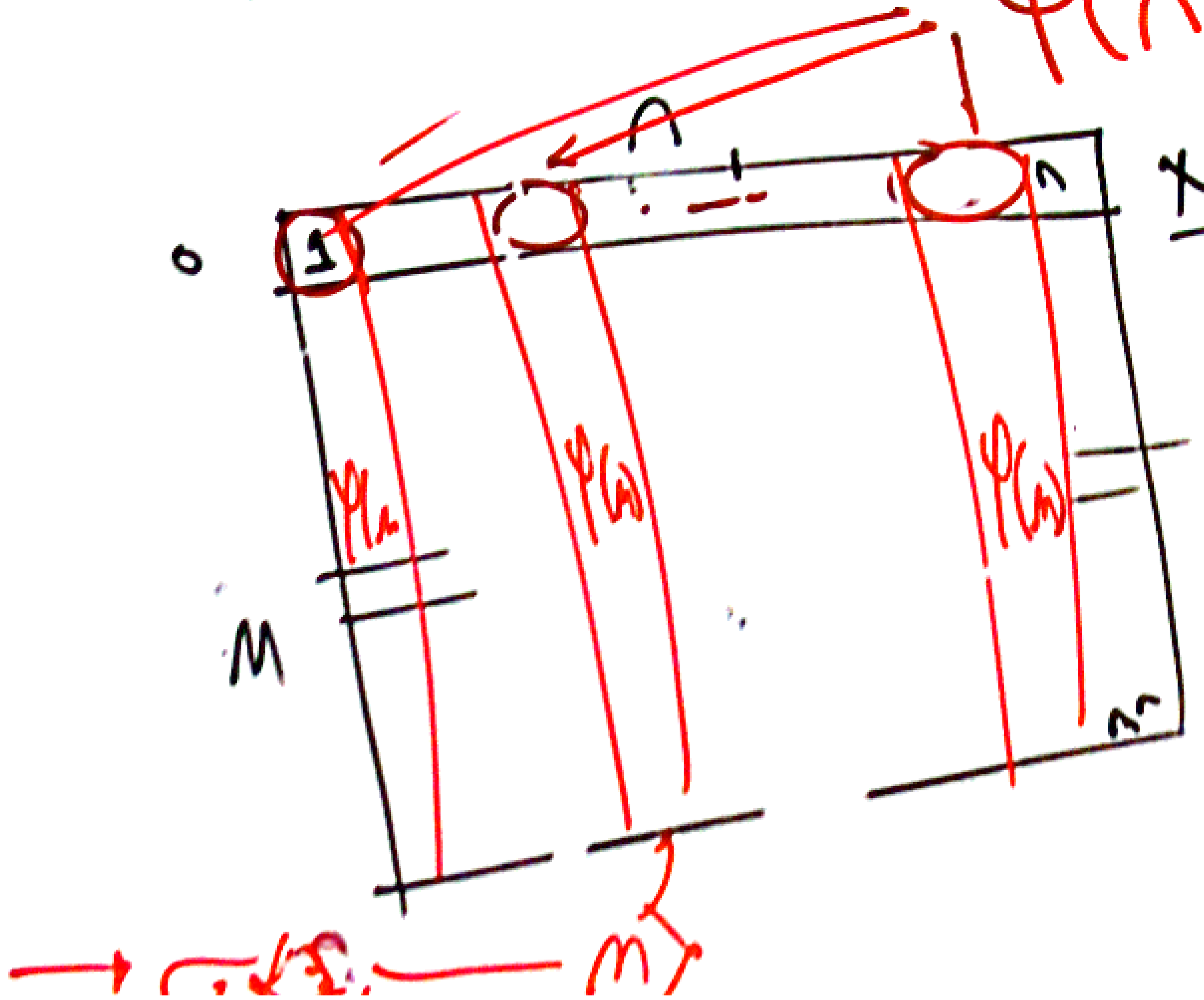

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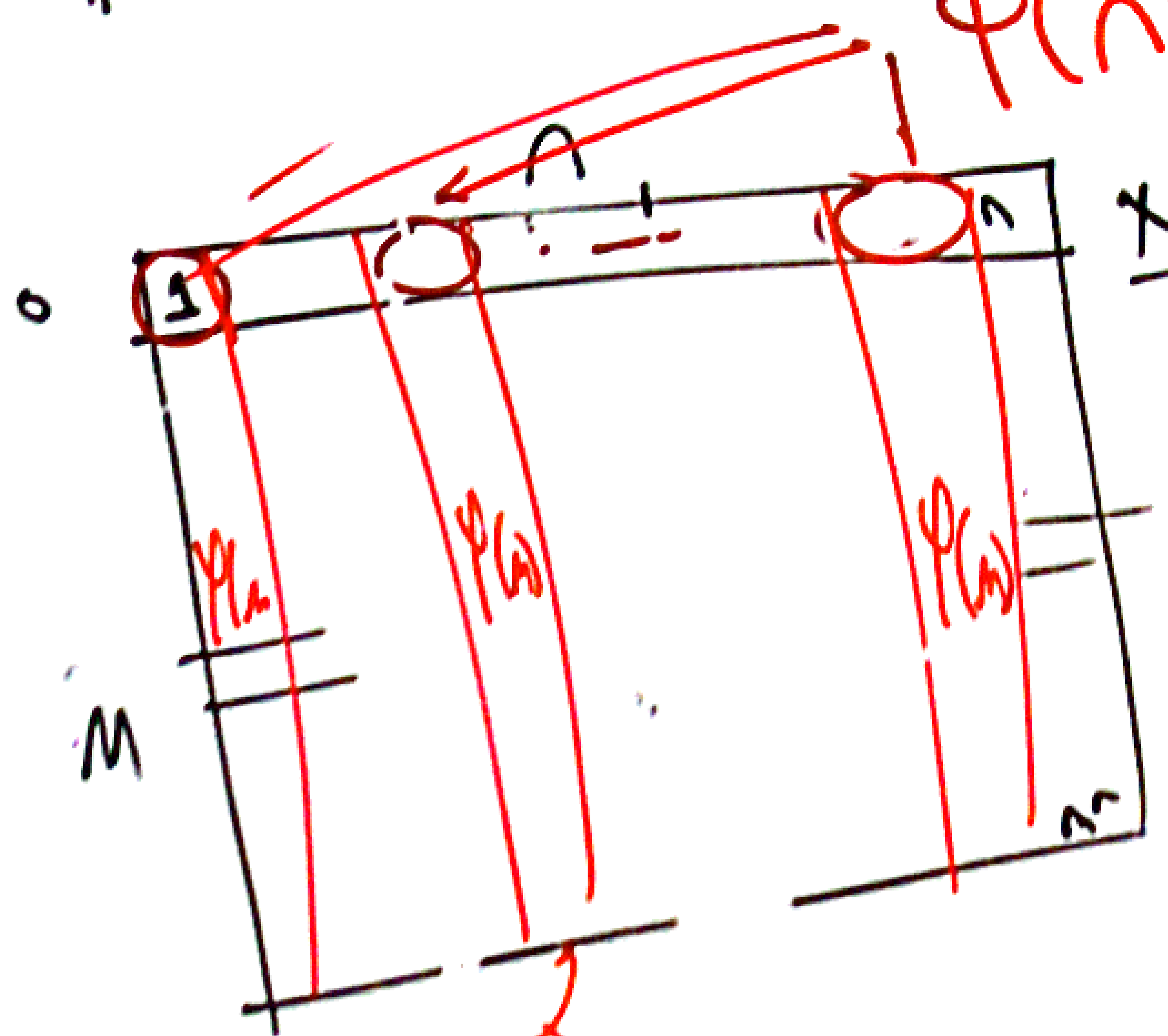

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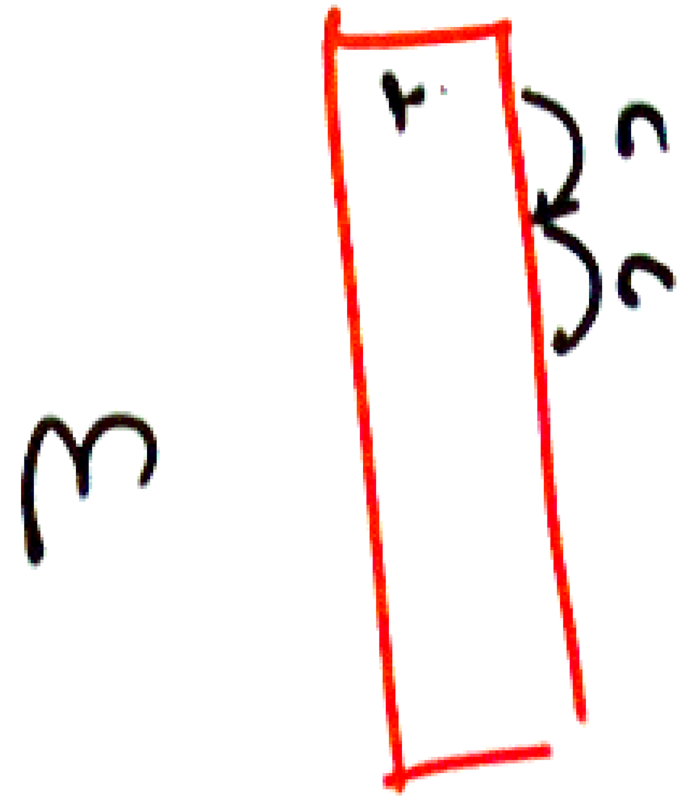

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