

# Repaso Parcial 2

**CS3102 EDA**



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2. Best First
3. R\*-Tree split
4. Celdas/mosaico
5. Hilbert-curve
6. Z-curve
7. Hilbert R-Tree
8. Dynamic Hilbert R-Tree





# 1. **Branch** and bound

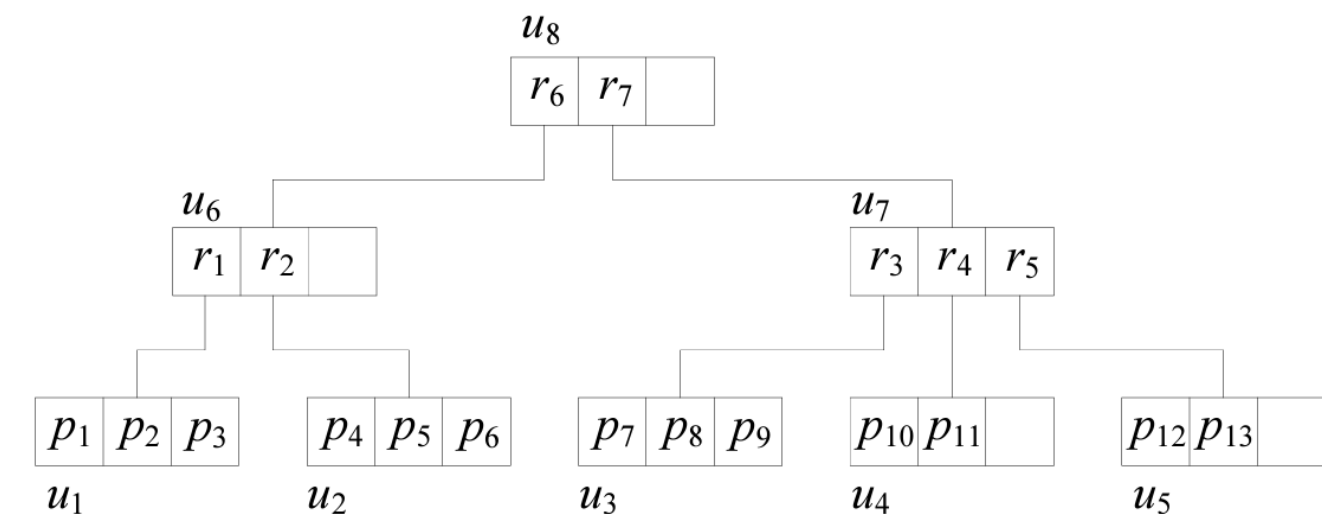
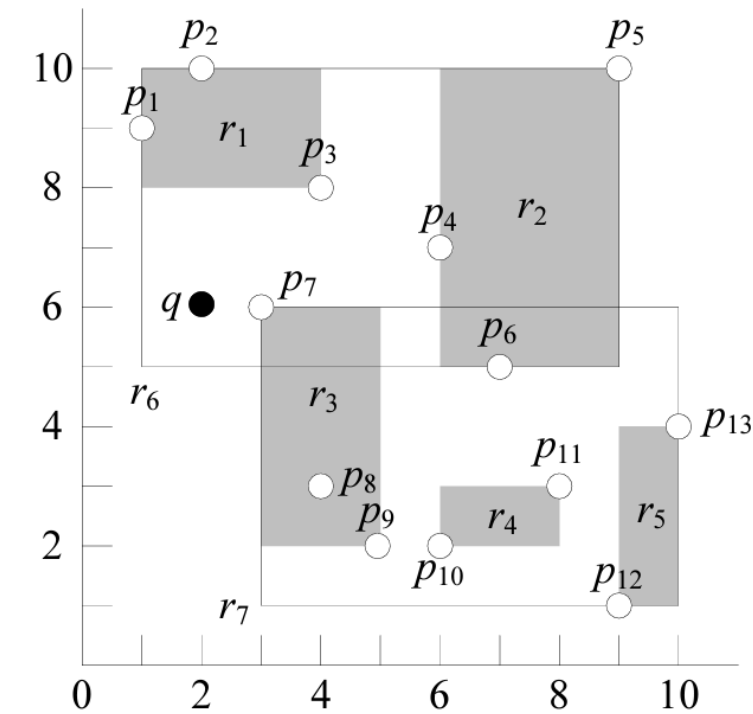


# Branch and bound

**algorithm** BaB( $u, q$ )

*/\*  $u$  is the node being accessed,  $q$  is the query point;  
 $p_{best}$  is a global variable that keeps the NN found so far;  
the algorithm should be invoked by setting  $u$  to the root \*/*

1. **if**  $u$  is a leaf node **then**
2.     **if** the NN of  $q$  in  $u$  is closer to  $q$  than  $p_{best}$  **then**
3.          $p_{best} =$  the NN of  $q$  in  $u$
4. **else**
5.     sort the MBRs in  $u$  in ascending order of their mindists to  $q$   
*/\* let  $r_1, \dots, r_f$  be the sorted order \*/*
6.     **for**  $i = 1$  to  $f$
7.         **if**  $\text{mindist}(q, r_i) < \|q, p_{best}\|$  **then**
8.             BaB( $u_i, q$ )  
*/\*  $u_i$  is child node of  $r_i$  \*/*



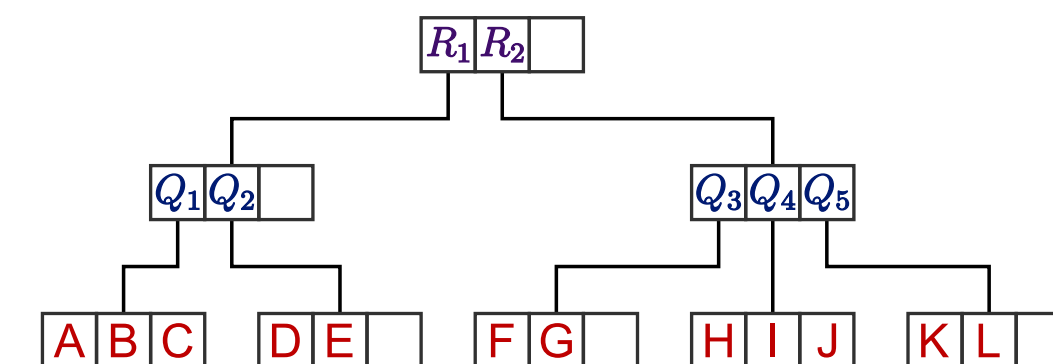
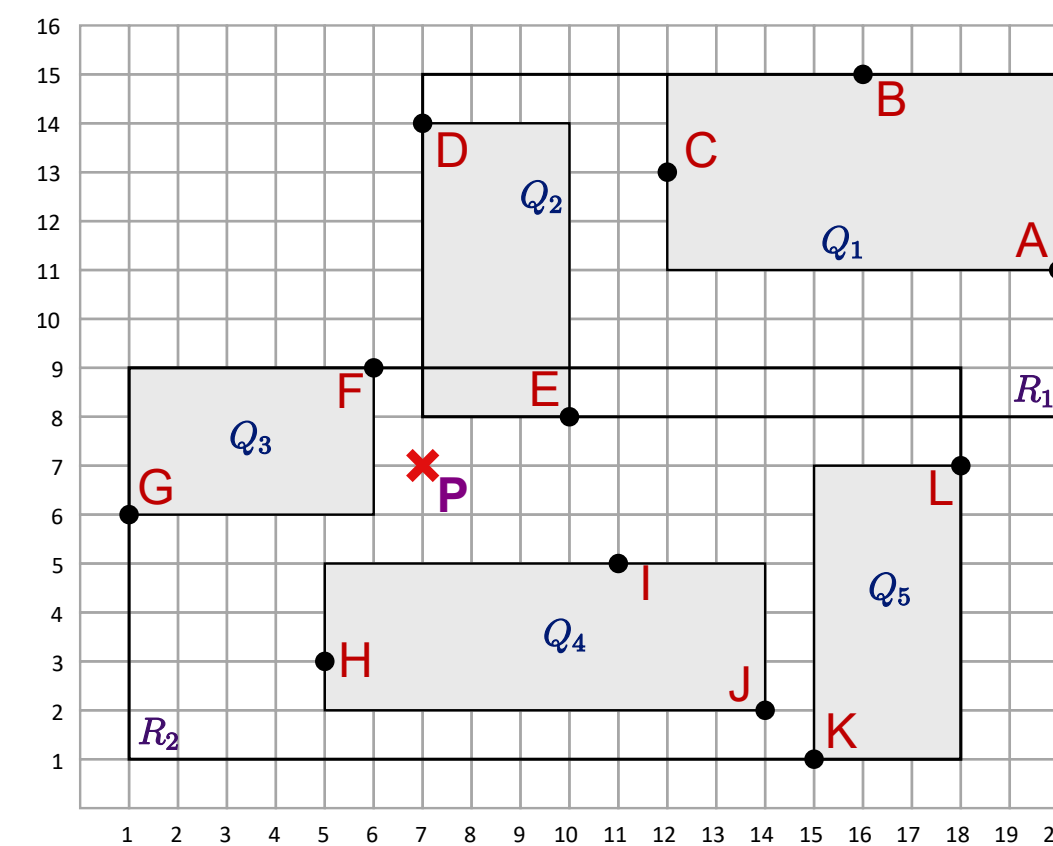
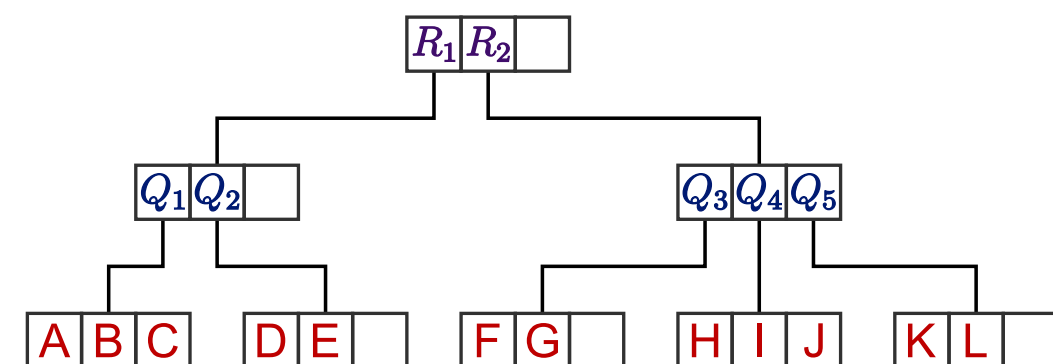
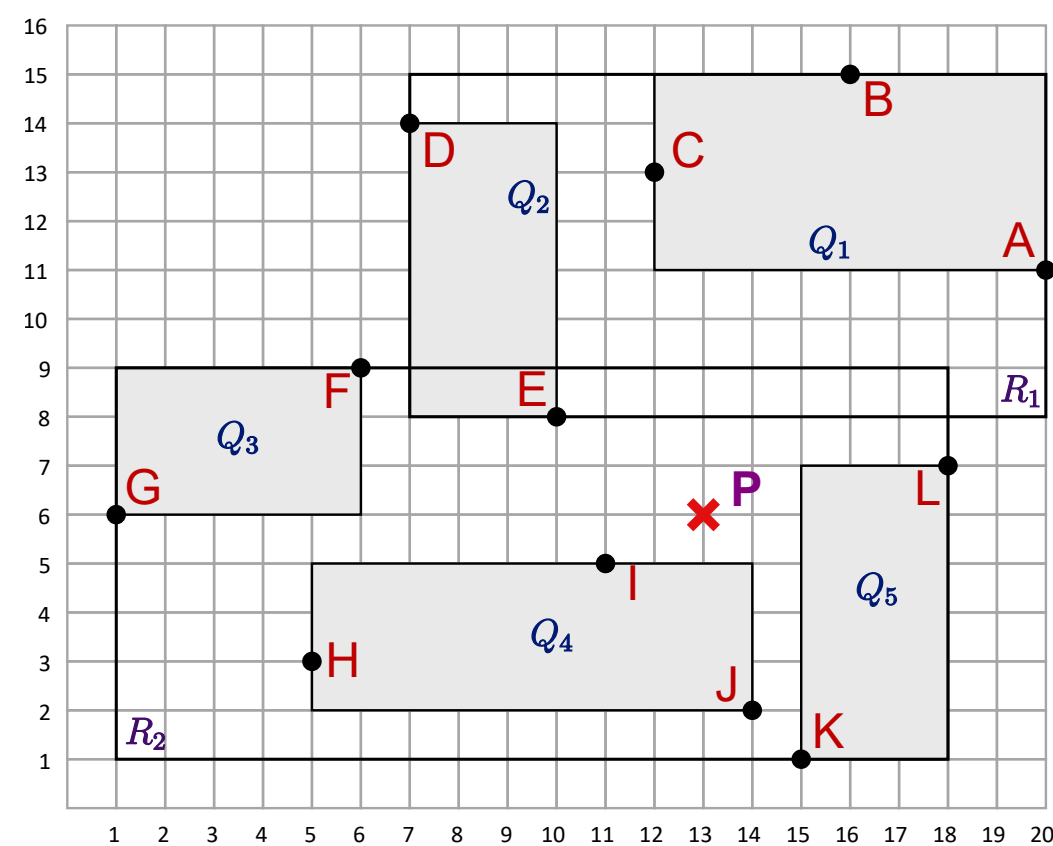
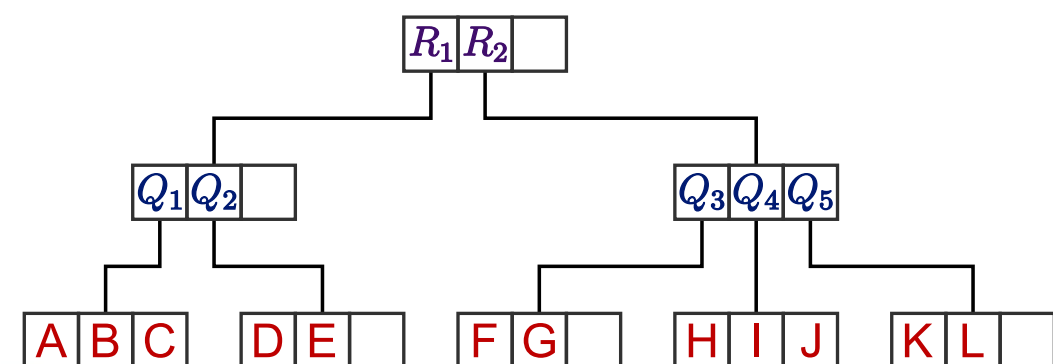
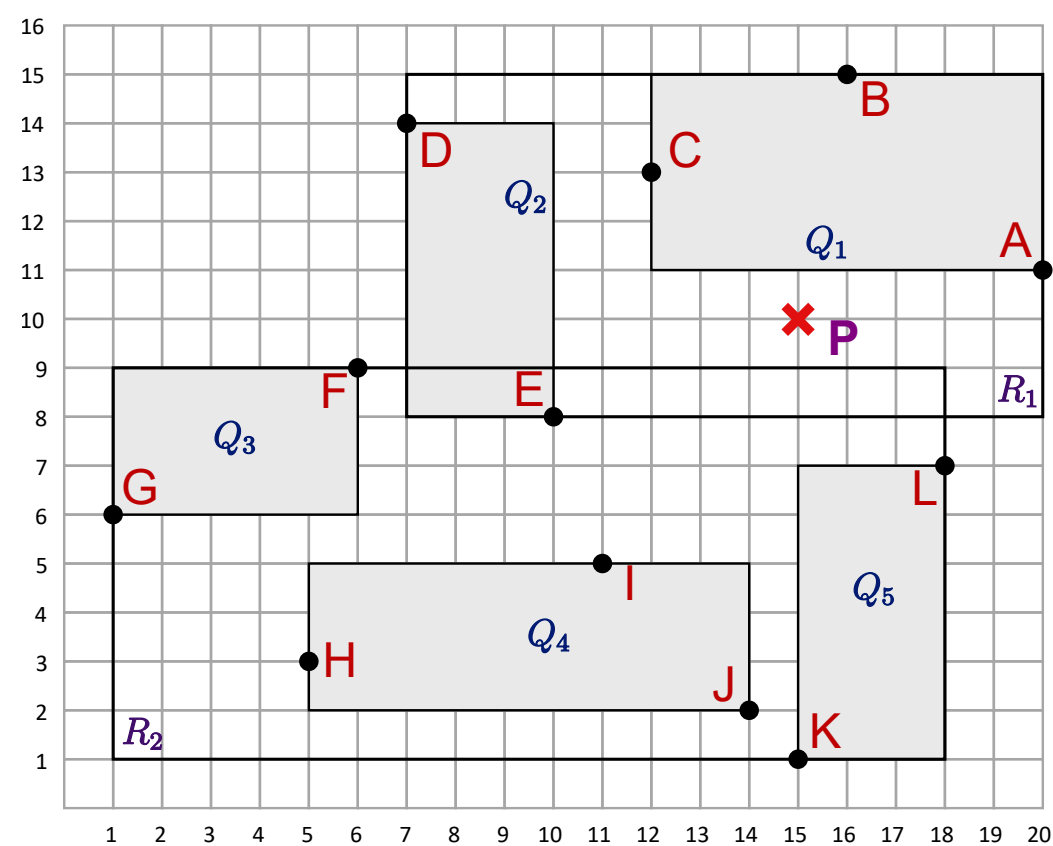
# Branch *and bound*

1

2

3

# Branch and bound





# 2. **Best** First



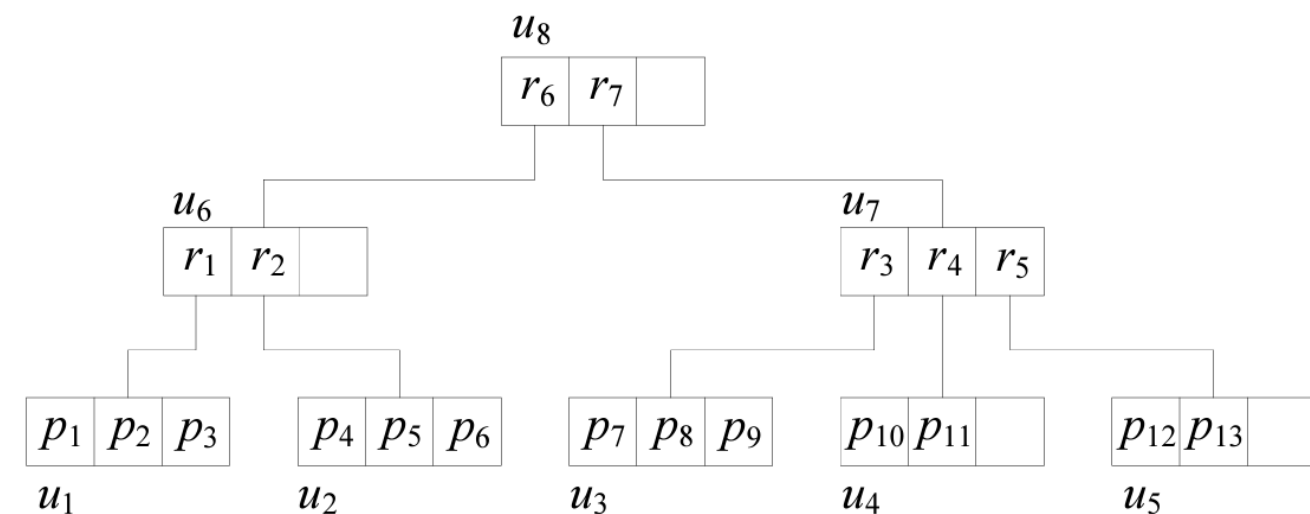
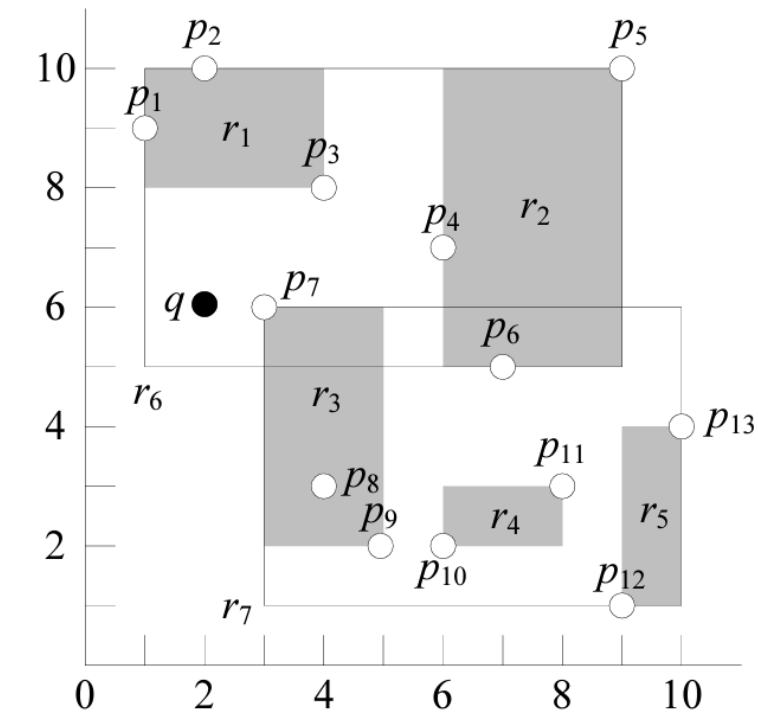
# Best First

## algorithm BF( $q$ )

/\* in the following  $H$  is a sorted list where each entry is an MBR whose sorting key in  $H$  is its mindist to  $q$ ;

$p_{best}$  is a global variable that keeps the NN found so far. \*/

1. insert the MBR of the root in  $H$
2. **while**  $\|q, p_{best}\|$  is greater than the smallest mindist in  $H$   
/\* if  $p_{best} = \emptyset$ ,  $\|q, p_{best}\| = \infty$  \*/
3.     remove from  $H$  the MBR  $r$  with the smallest mindist
4.     access the child node  $u$  of  $r$
5.     **if**  $u$  is an intermediate node **then**
6.         insert all the MBRs in  $u$  into  $H$
7.     **else**
8.         **if** the NN of  $q$  in  $u$  is closer to  $q$  than  $p_{best}$  **then**
9.              $p_{best} =$  the NN of  $q$  in  $u$





# Best *First*

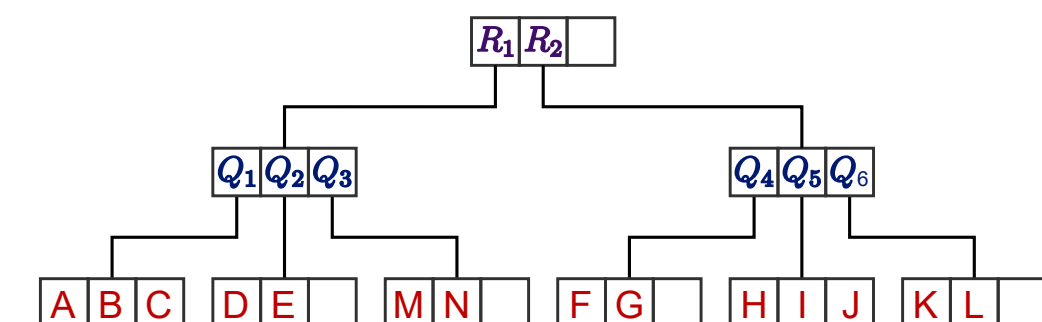
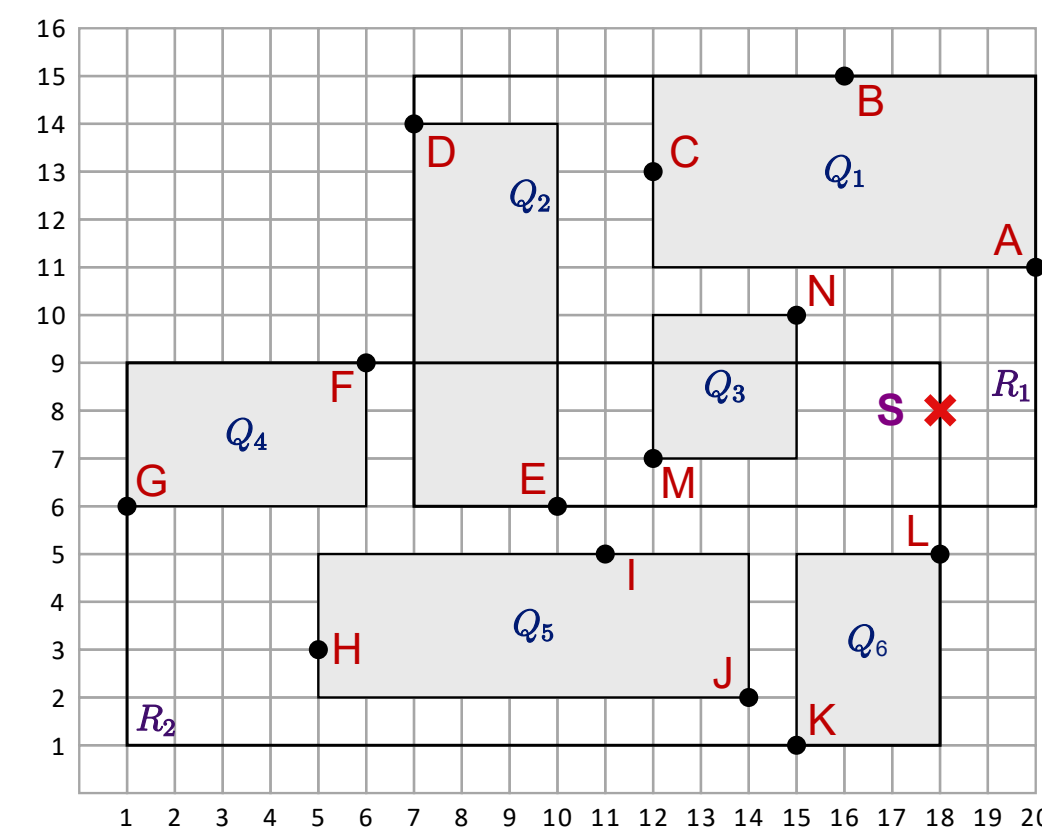
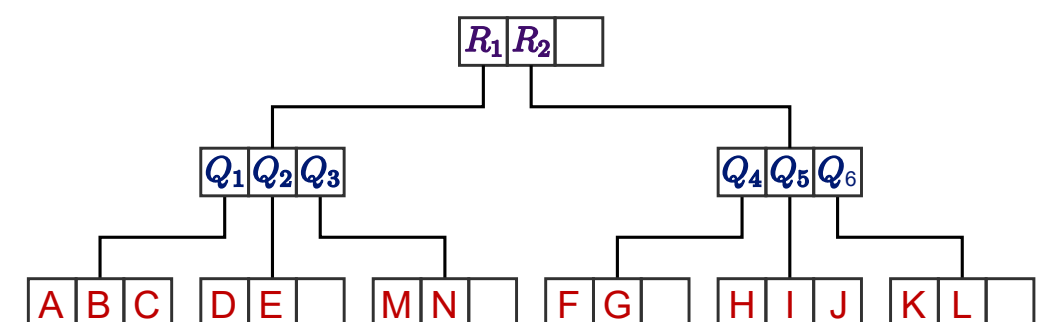
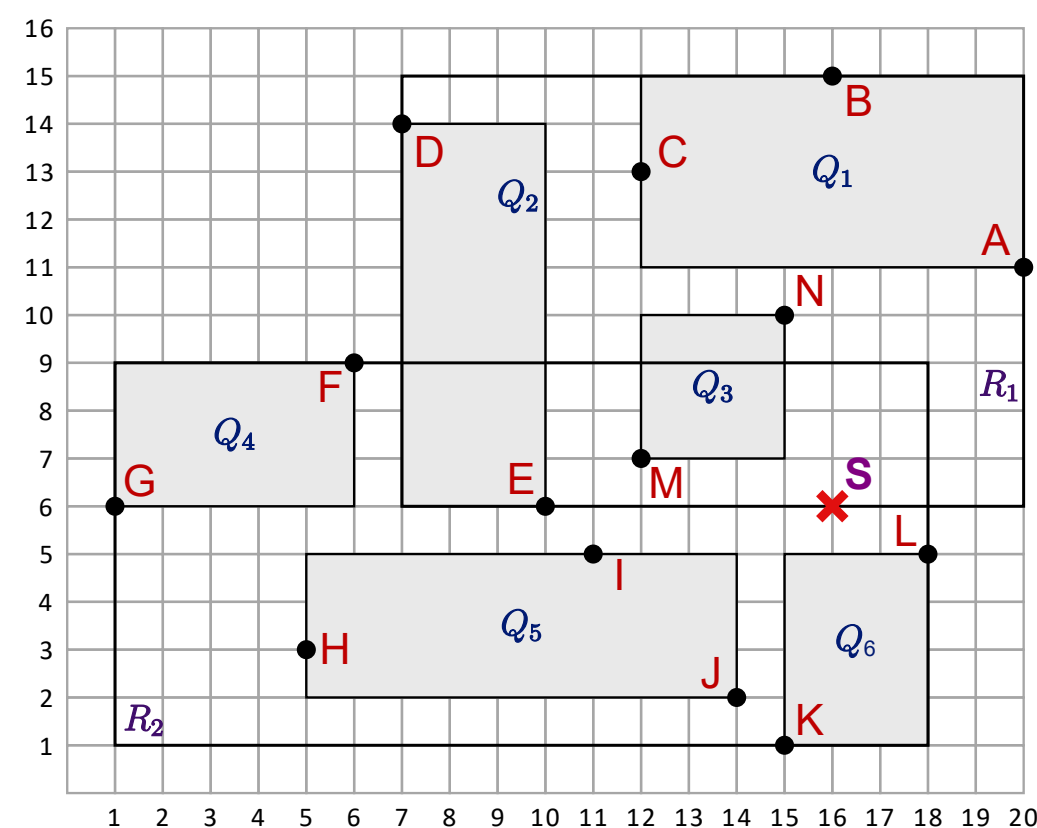
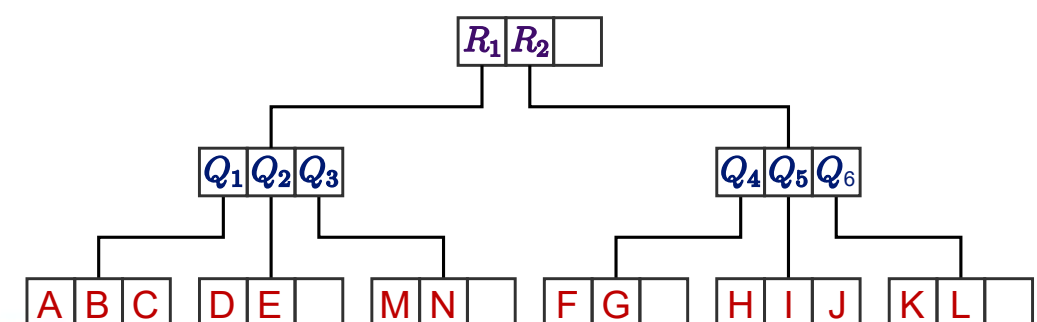
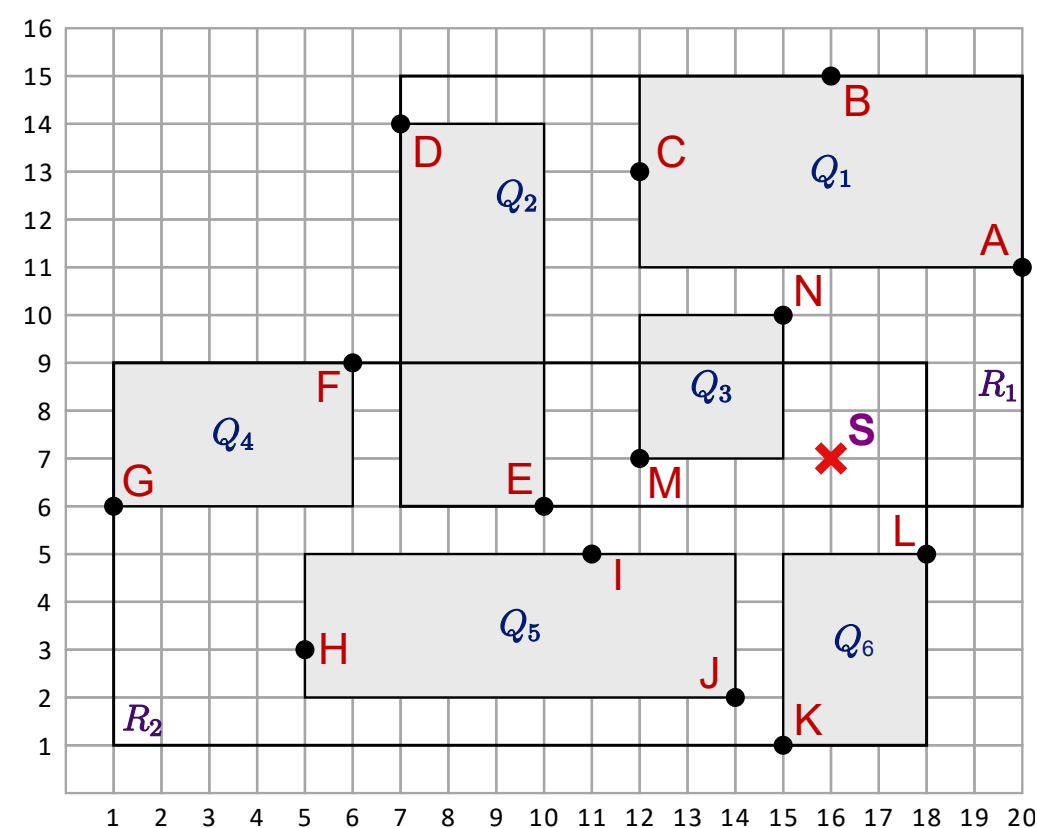
1

2

3



# Best First





# 3. $R^*$ -Tree: split

# R\*-Tree: *split*

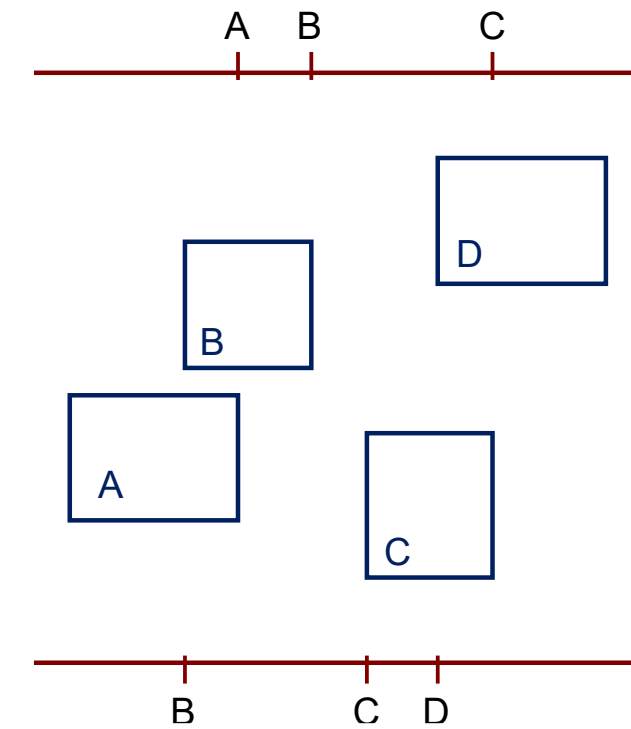
## Split

- Seleccionar eje

### a) Eje $x$

- Limite inferior
- Limite superior

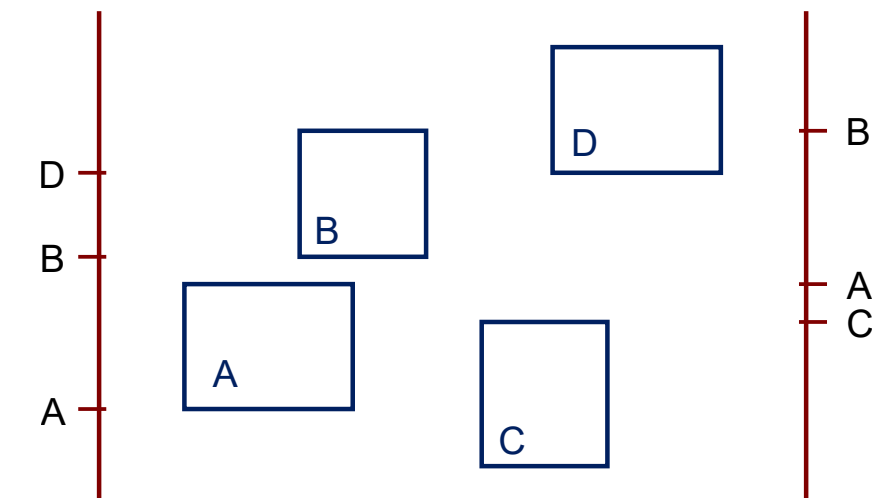
Suma de  
semiperímetros de  
las regiones



### b) Eje $y$

- Limite inferior
- Limite superior

Suma de  
semiperímetros de  
las regiones





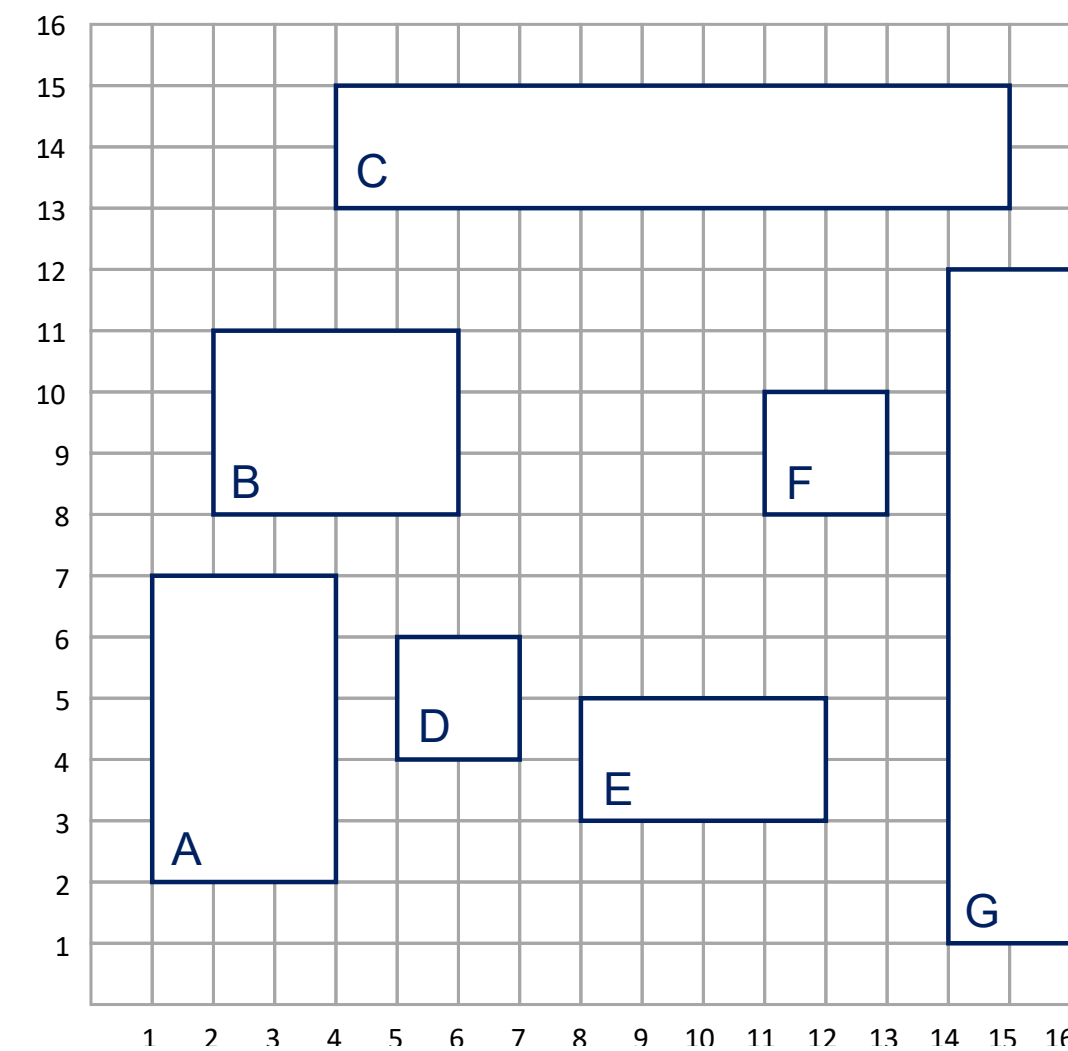
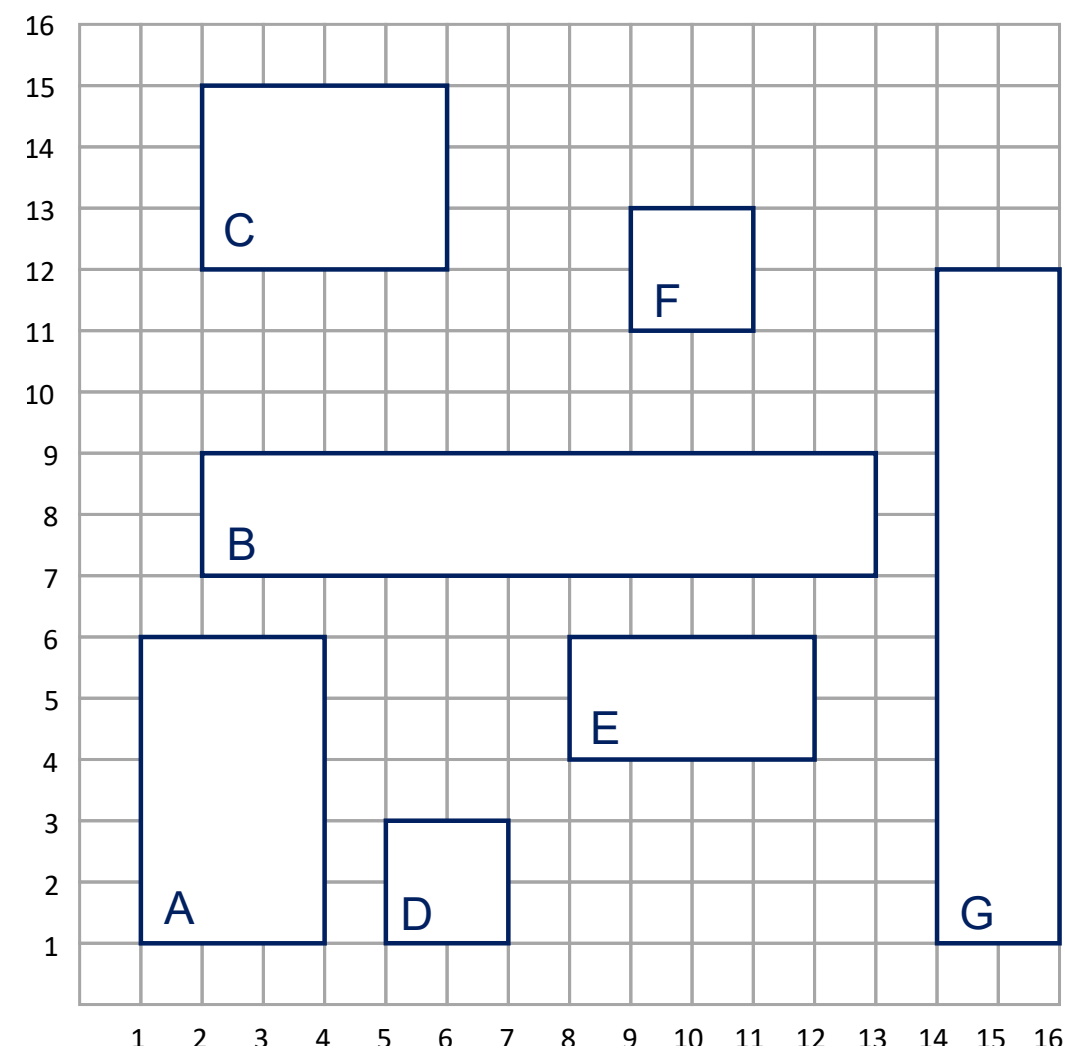
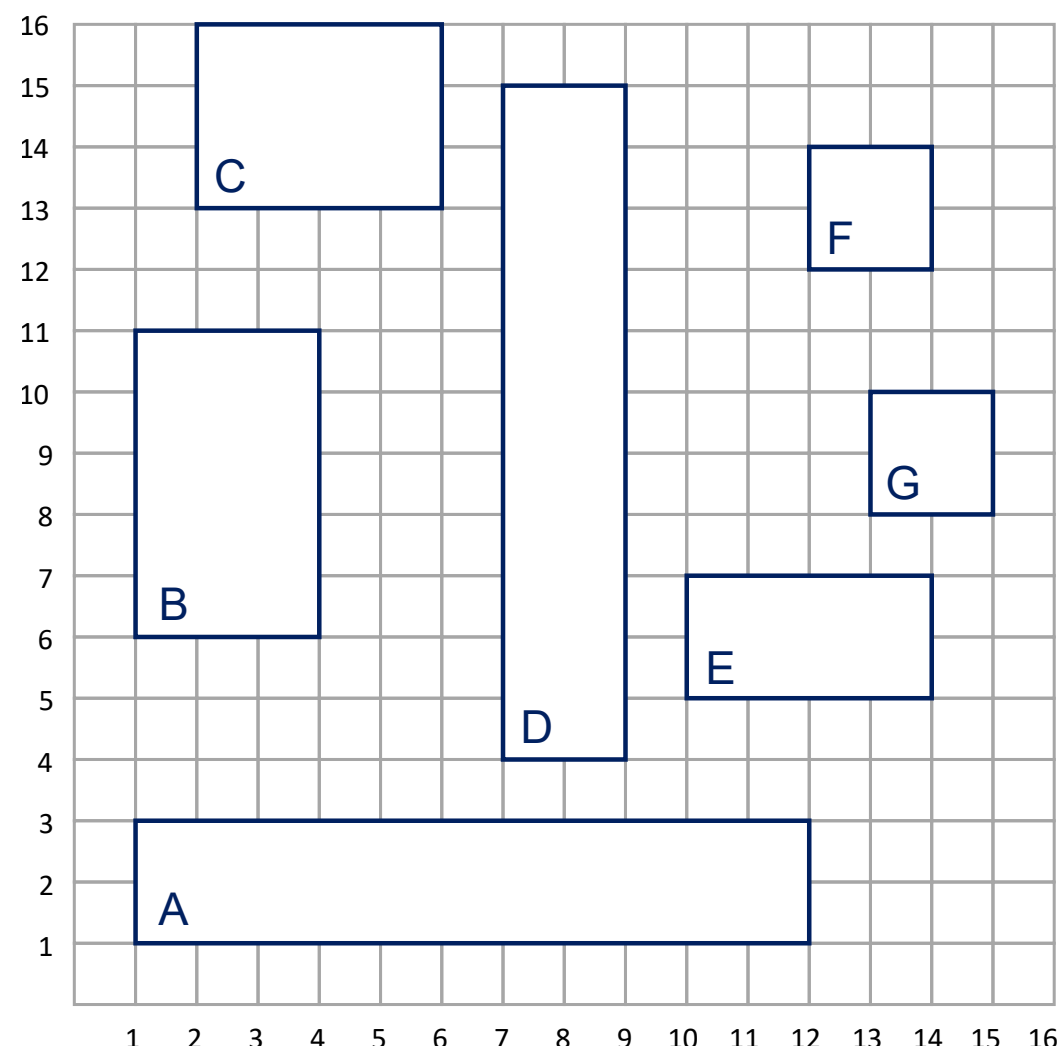
# R\*-Tree: *split*

1

2

3

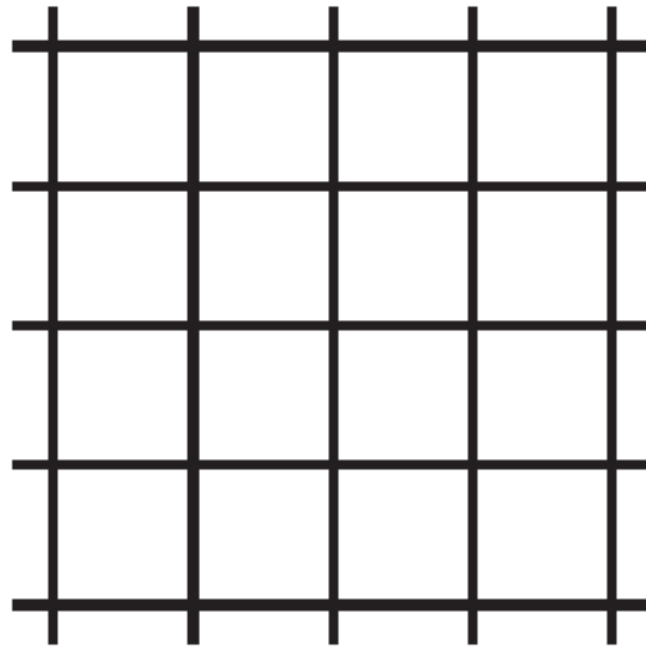
# R\*-Tree: *split*





# 4. Celdas/mosaico

# Celdas/*mosaico*



Notación

$[4^4]$

Regular tiling

Similar tiling

Mosaico ilimitado

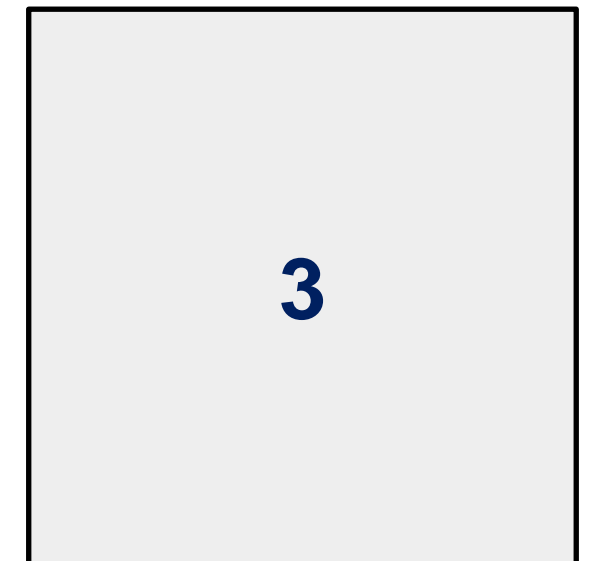
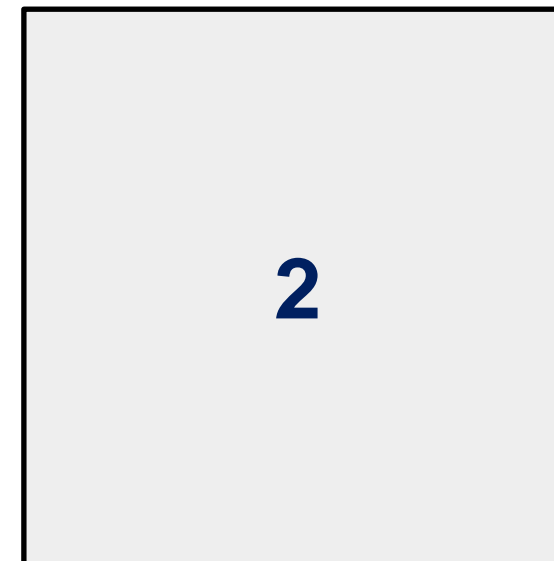
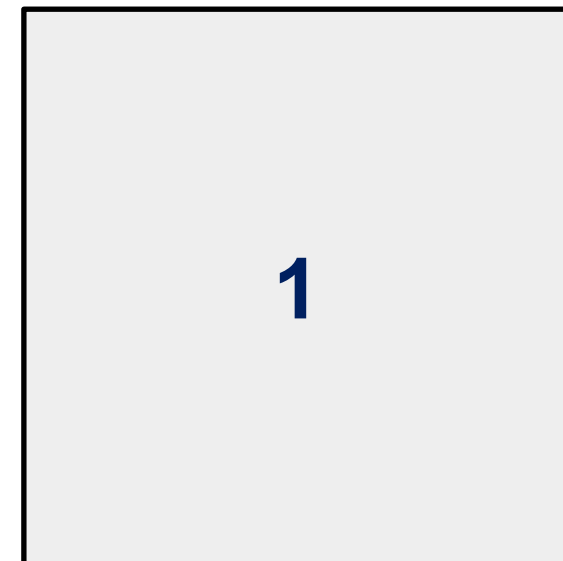
La celda atómica se puede descomponer

Número de adyacencia: 2

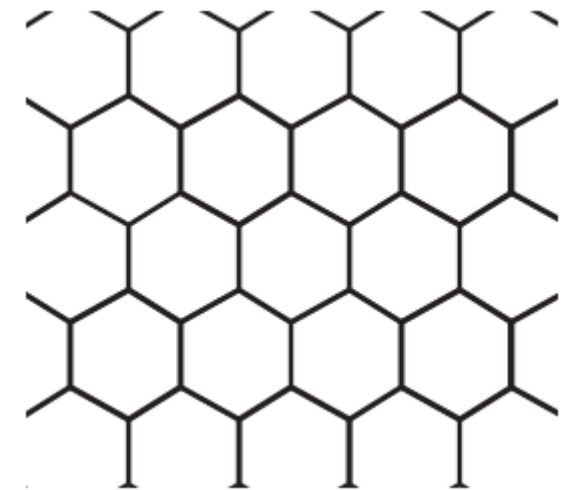
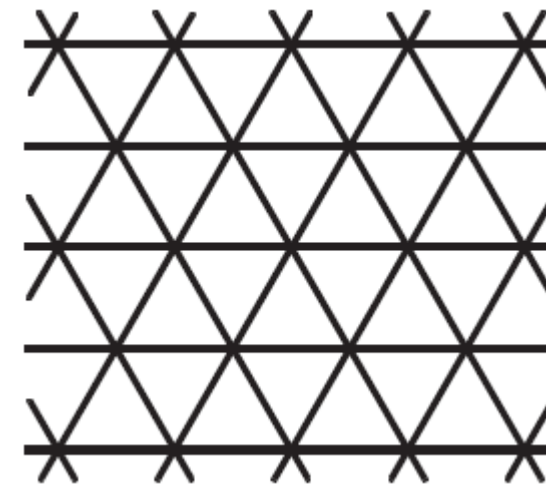
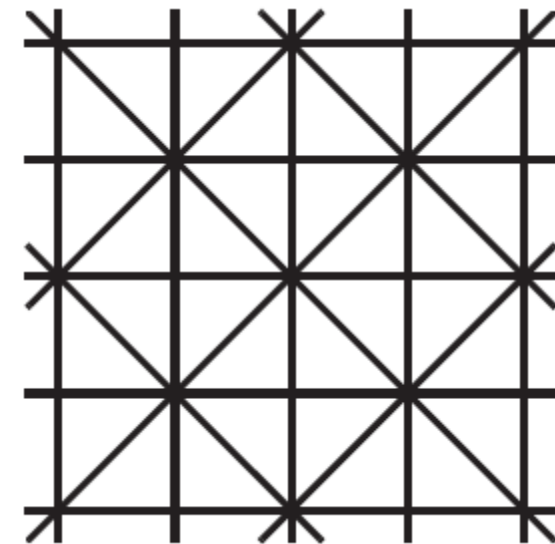
Orientación uniforme



# Celdas/*mosaico*



# Celdas/*mosaico*



Notación

Similar tiling?

Mosaico limitado?

Número de adyacencia:

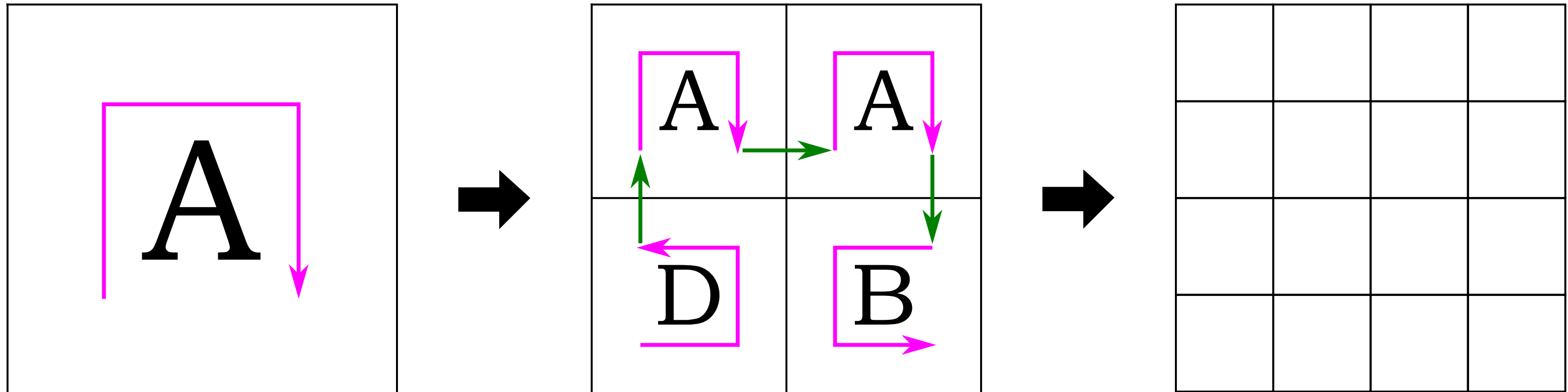
Orientación uniforme?:



# 5. Hilbert-curve



# Hilbert-curve



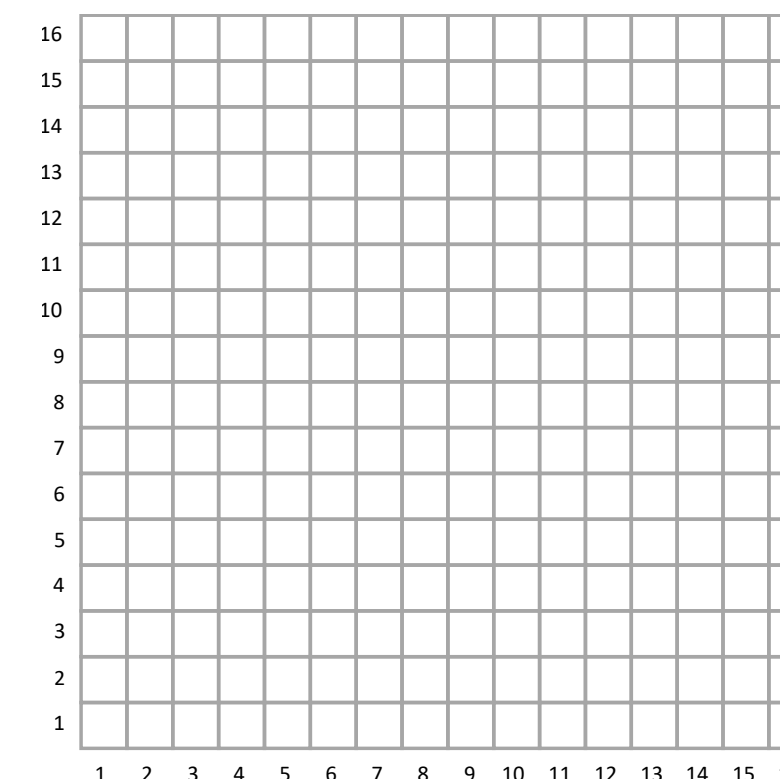
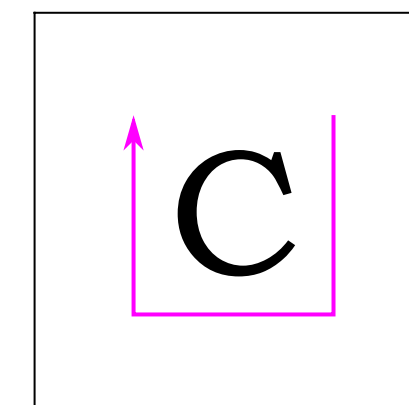
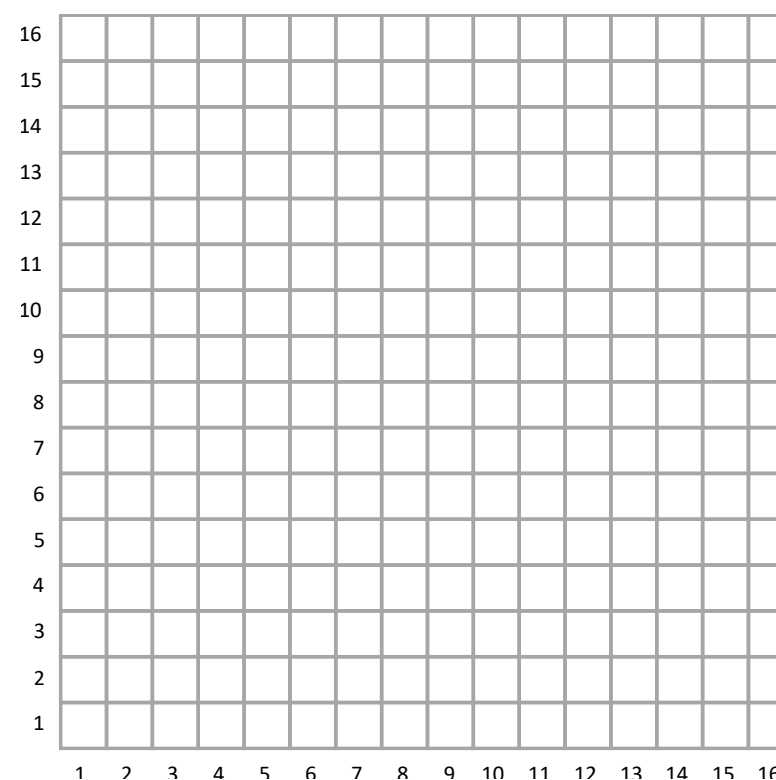
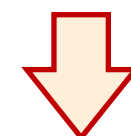
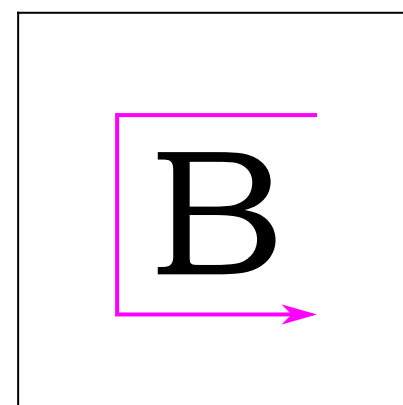
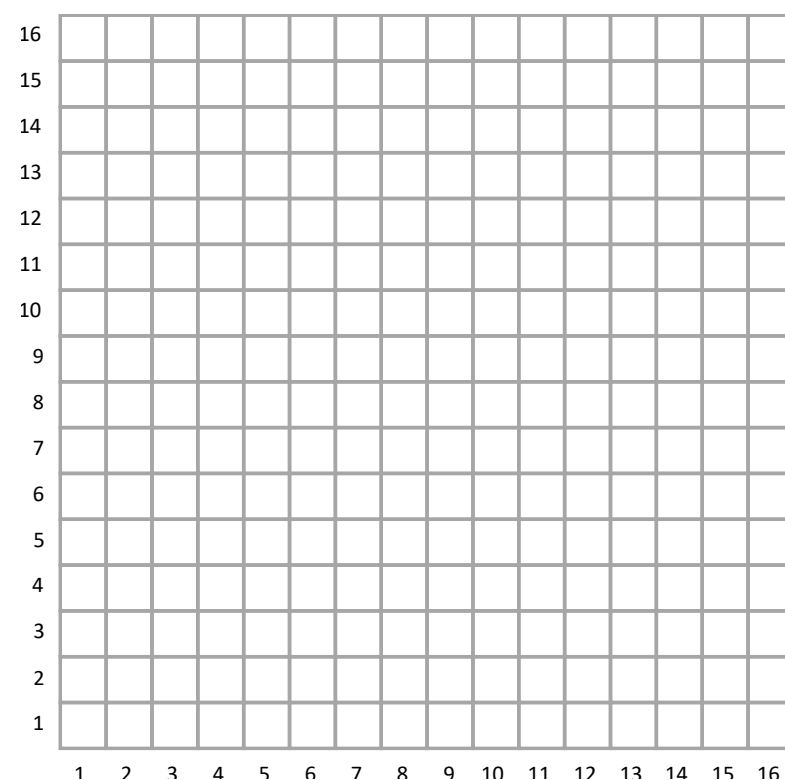
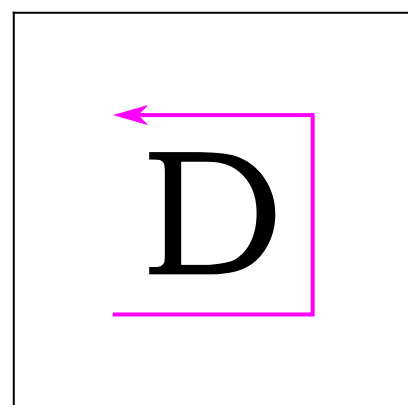
# Hilbert-curve

1

2

3

# Hilbert-curve

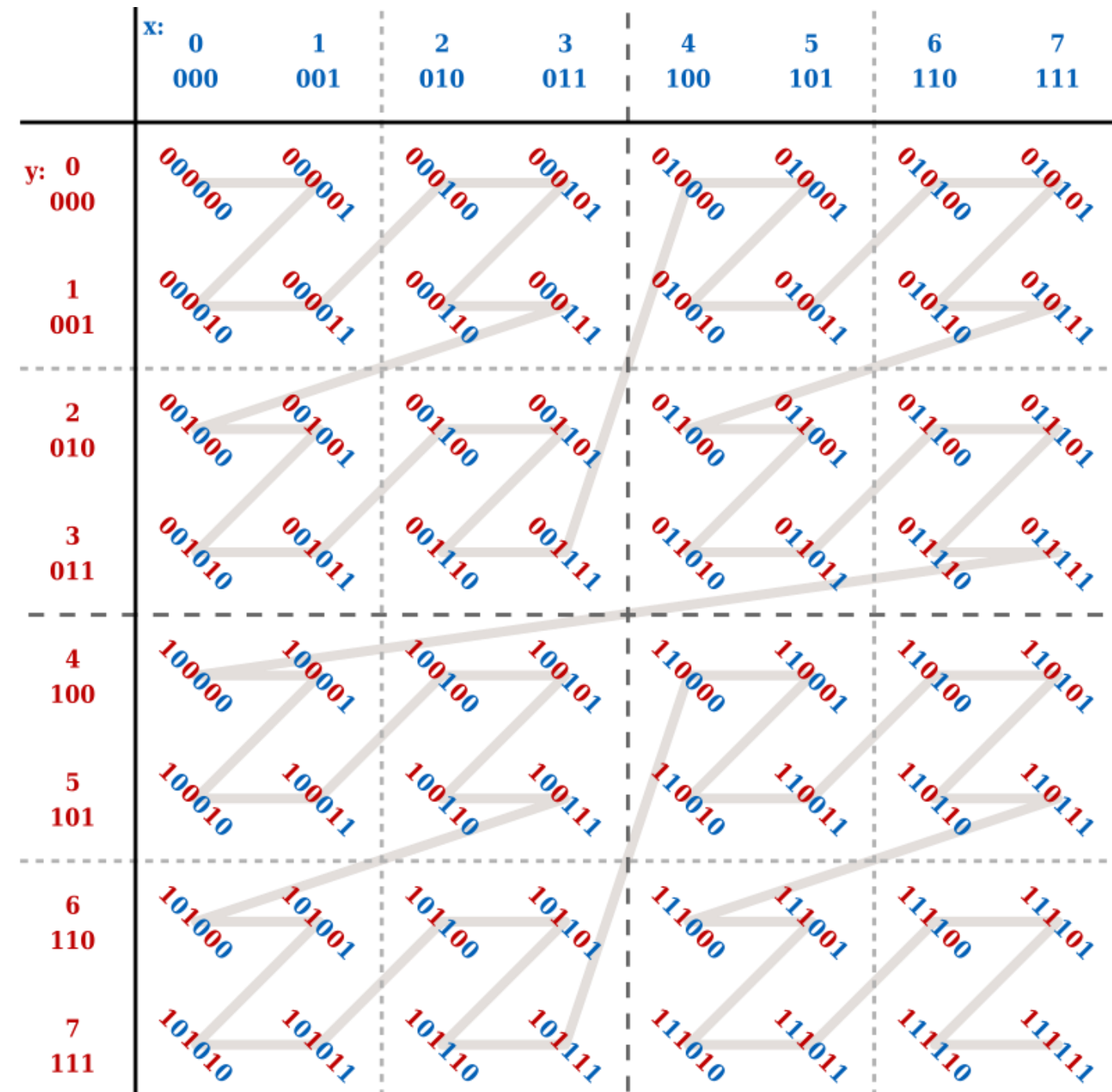




# 6. z-curve



# Z-curve





# **Z**-curve

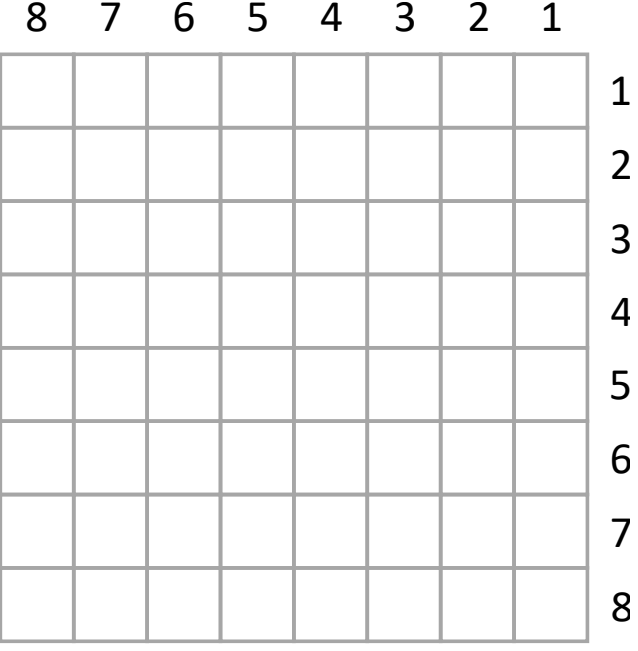
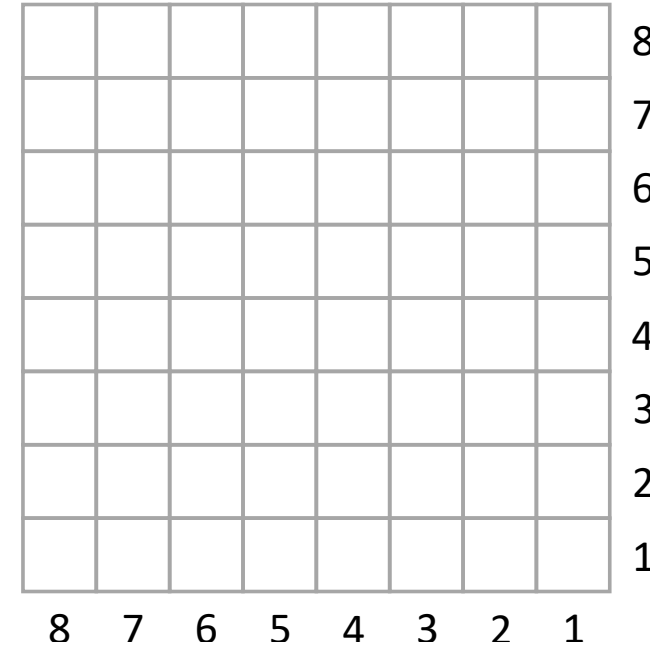
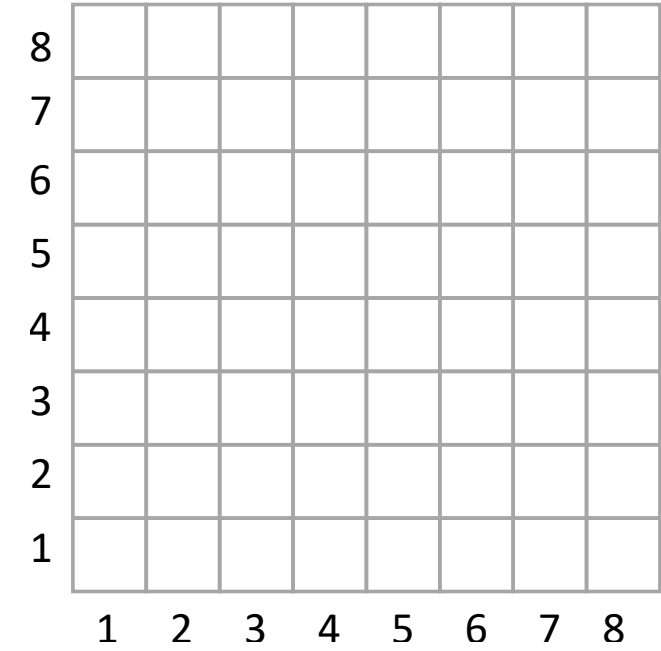
1

2

3



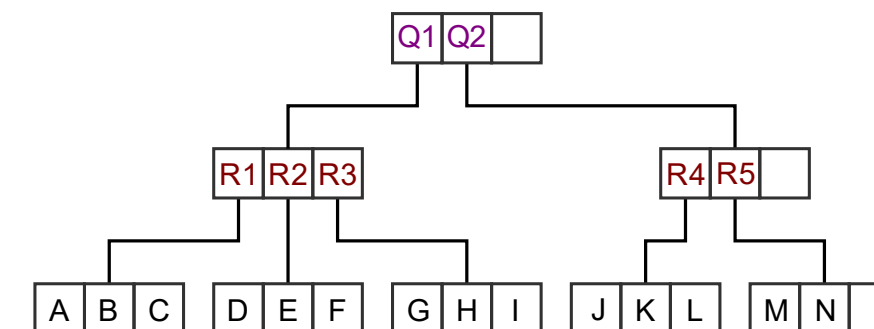
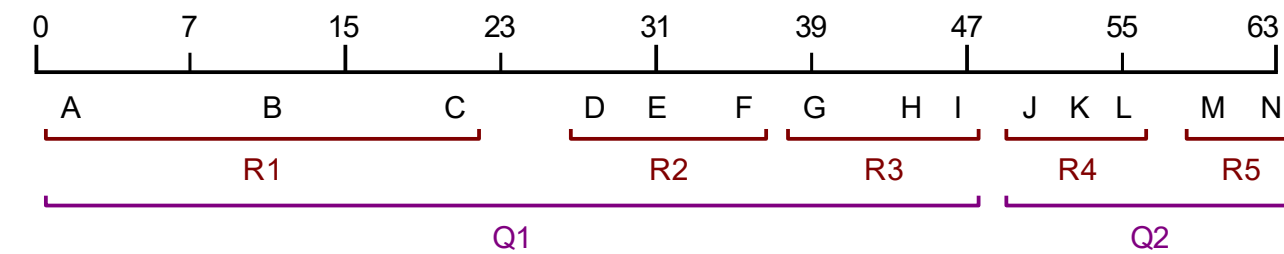
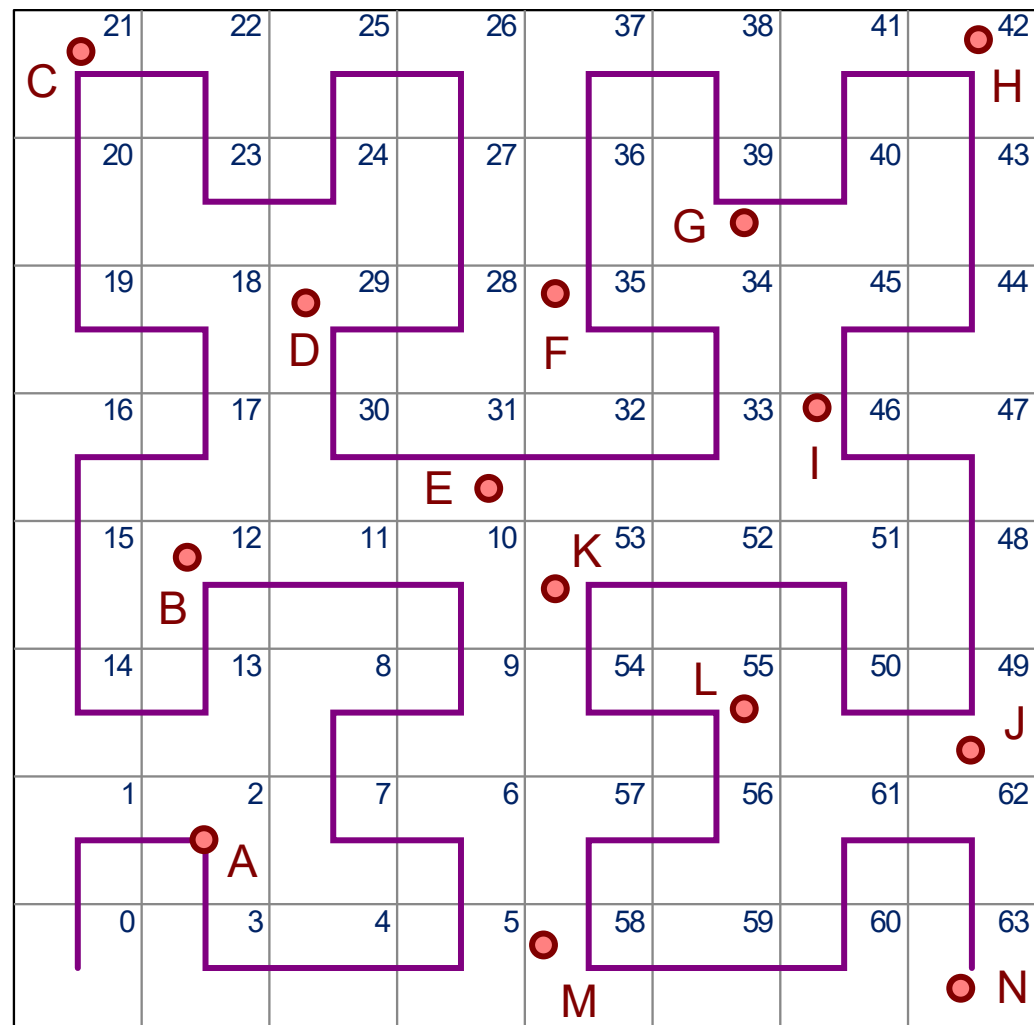
# Z-curve





# 7. Hilbert R-Tree

# Hilbert R-Tree





# Hilbert R-Tree

1

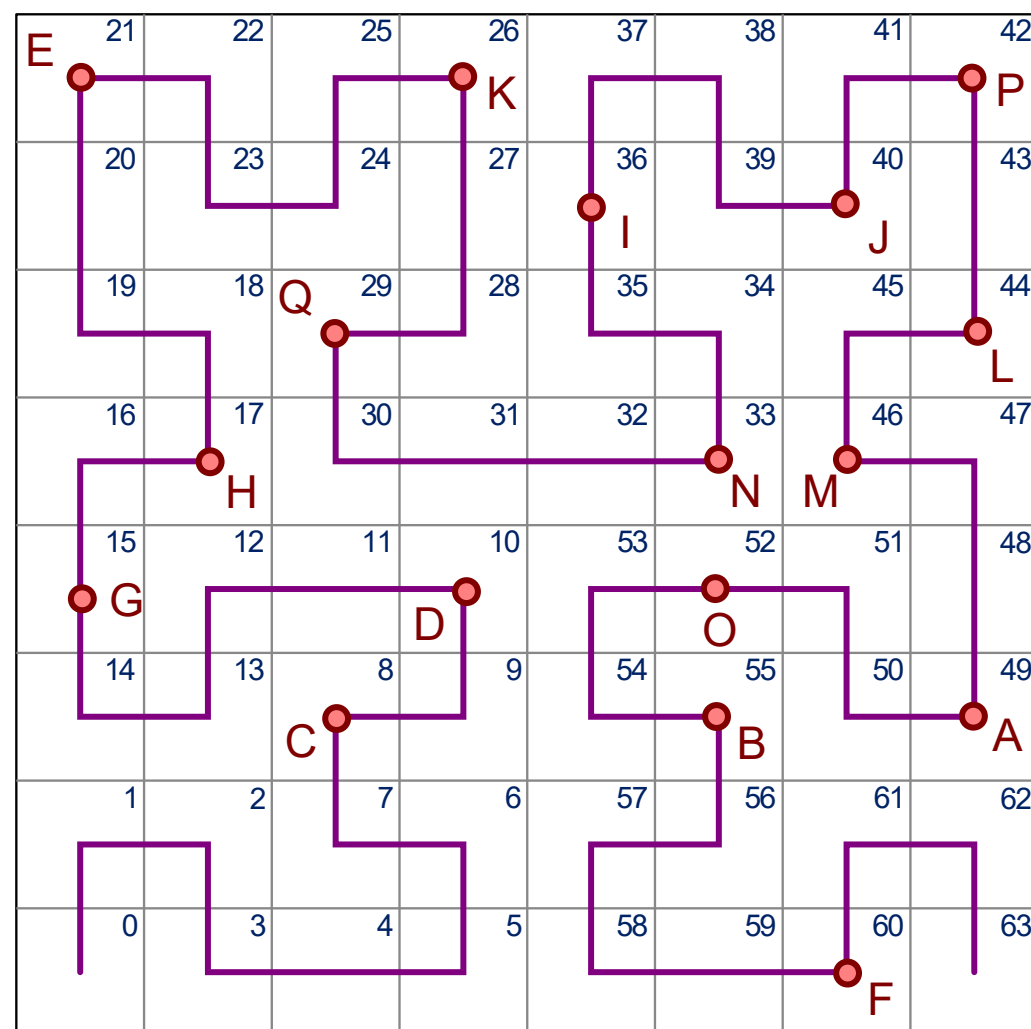
2

3

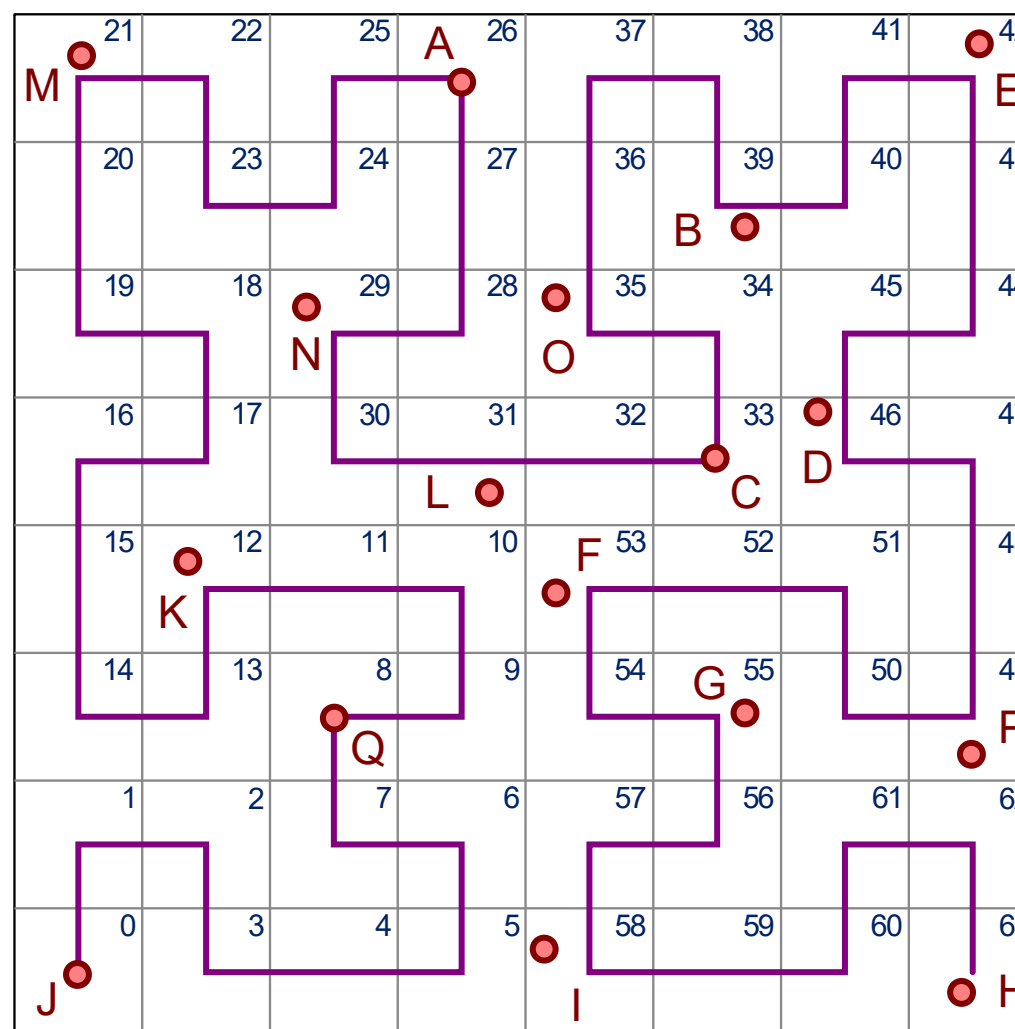


# Hilbert R-Tree

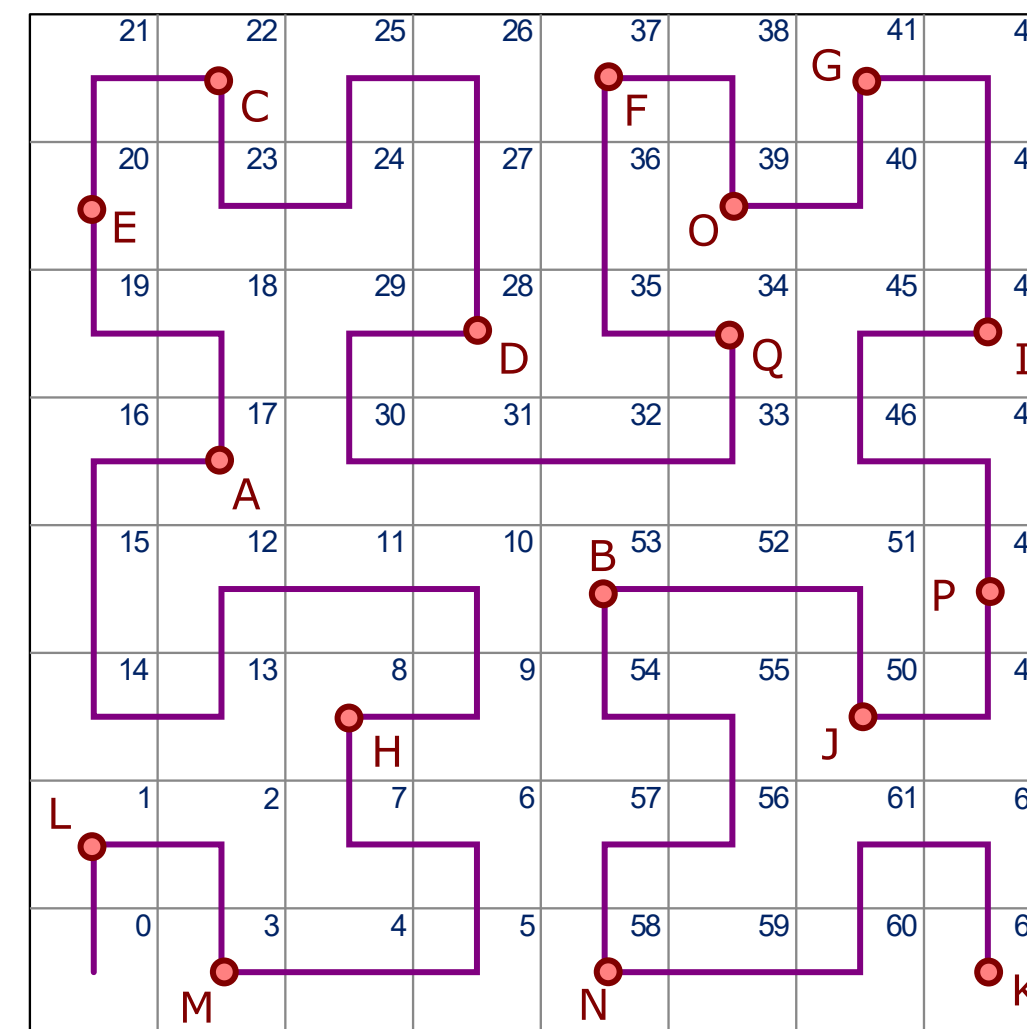
$M = 4$



$M = 3$



$M = 2$



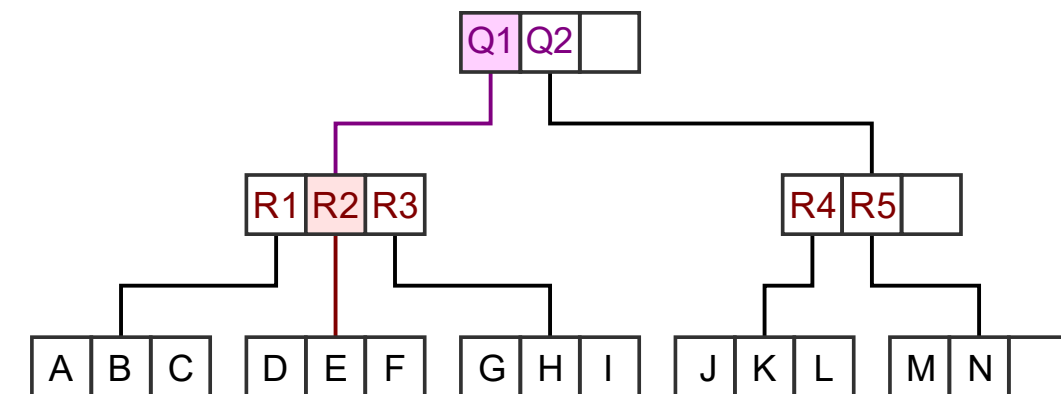
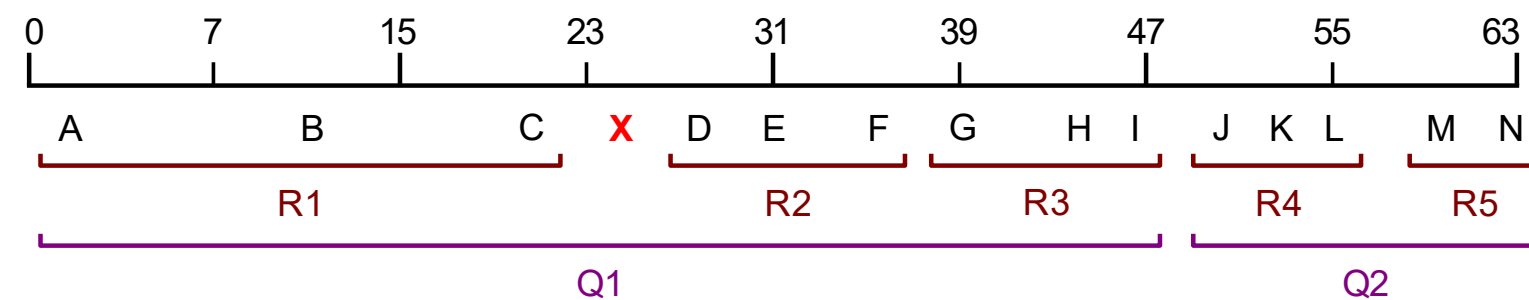


# 8. Dynamic Hilbert R-Tree

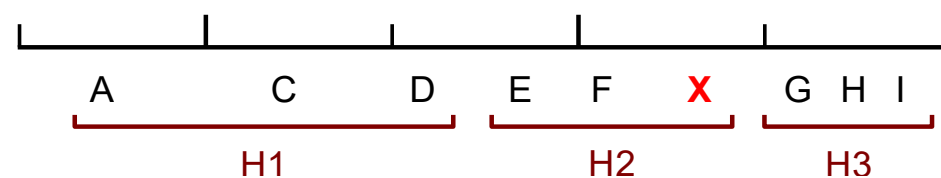


# Dynamic Hilbert *R-Tree*

Durante la inserción, se selecciona el nodo con **LHV mínimo que supera al h-index** del nuevo dato.



**Sobrecarga** Buscamos apoyo del hermano **izquierdo**.



Repartimos todos los datos entre **todos** los nodos

Pero, que hacemos si **todos** los nodos izquierdos están llenos?

Creamos nuevo nodo

... y repartimos todos los datos entre **todos** los nodos



# Dynamic Hilbert *R-Tree*

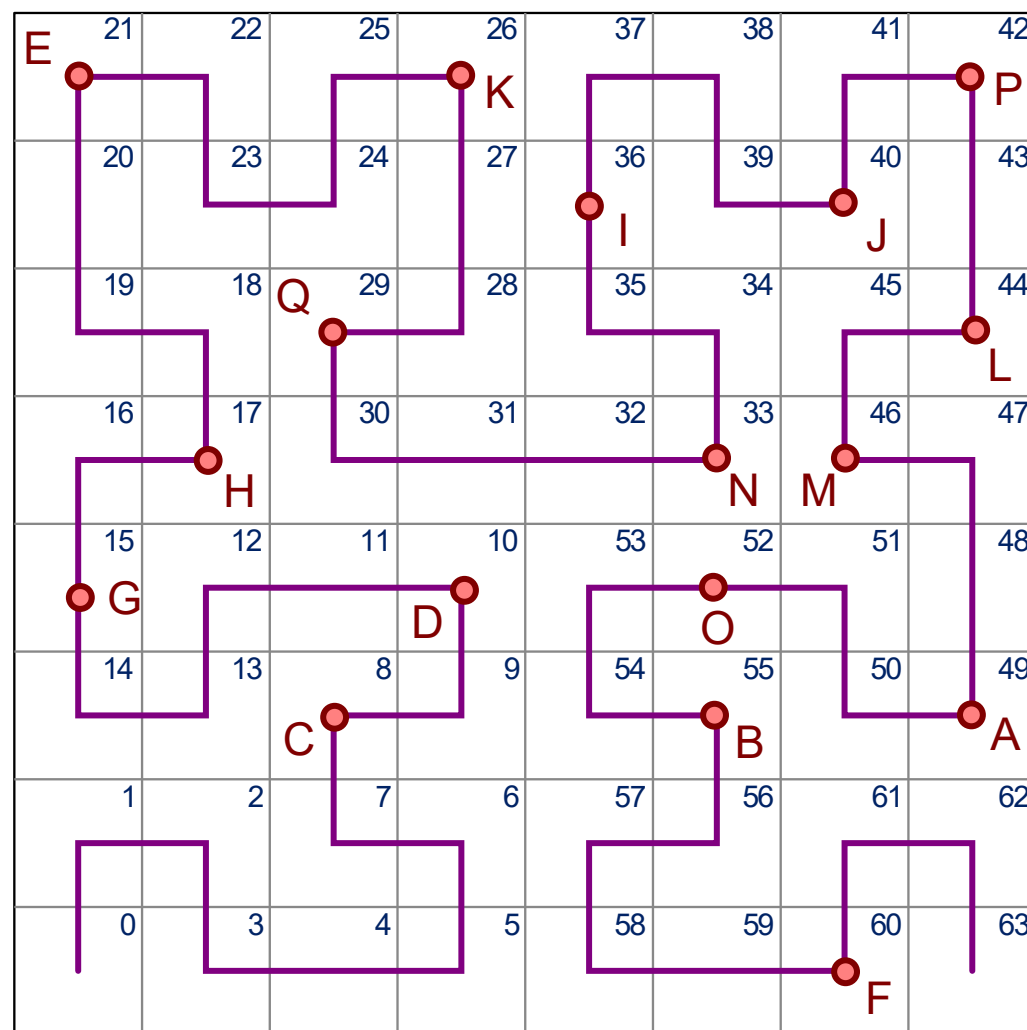
1

2

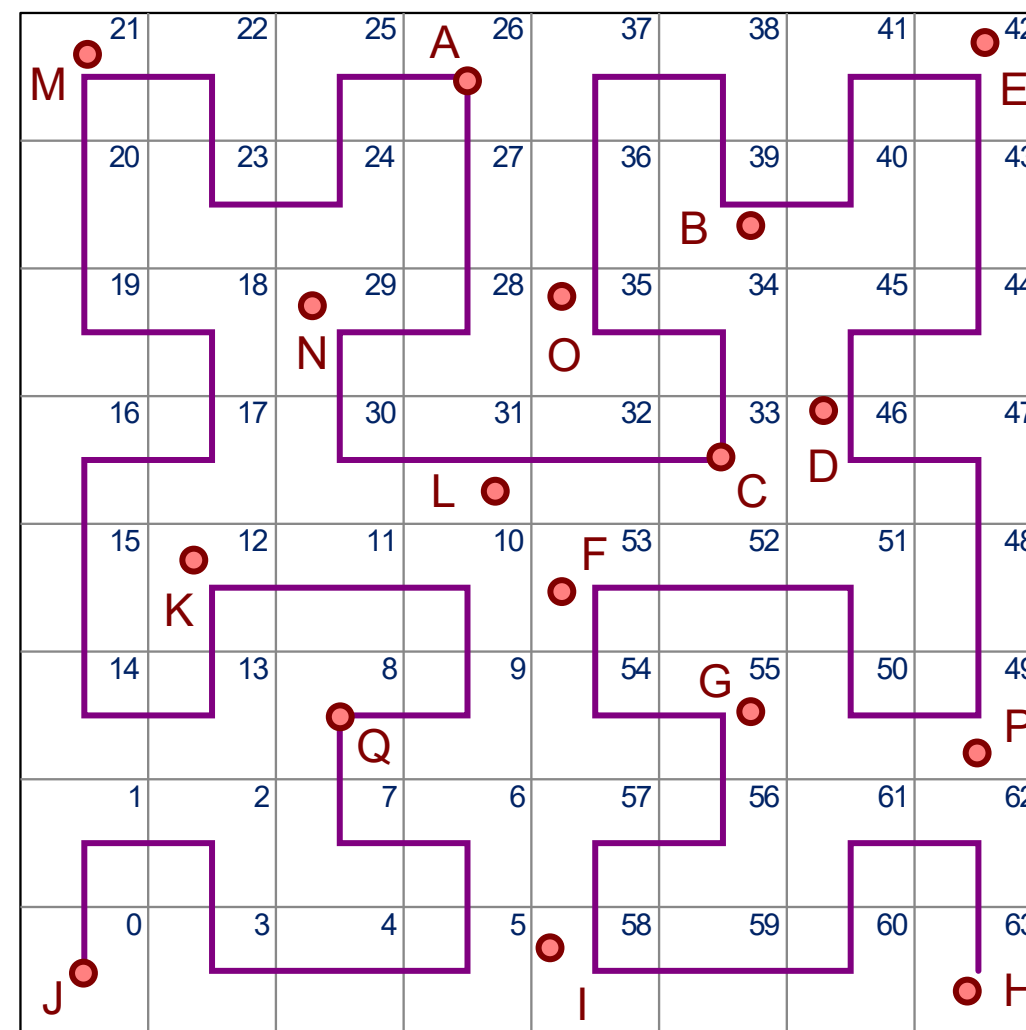
3

# Dynamic Hilbert *R-Tree*

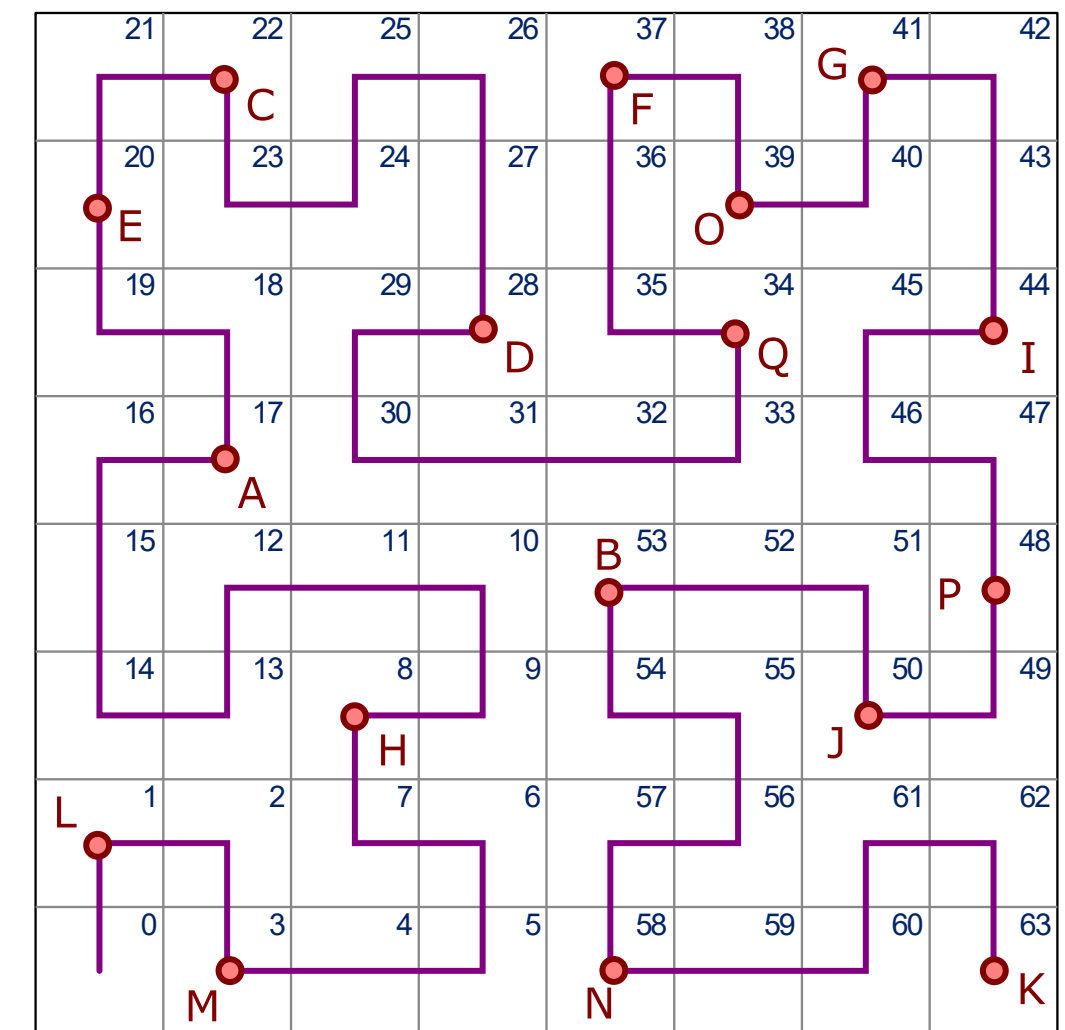
$M = 3$



$M = 3$



$M = 3$







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