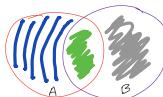
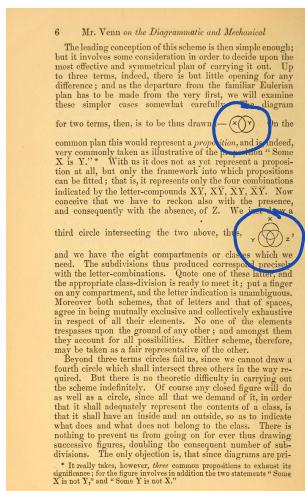
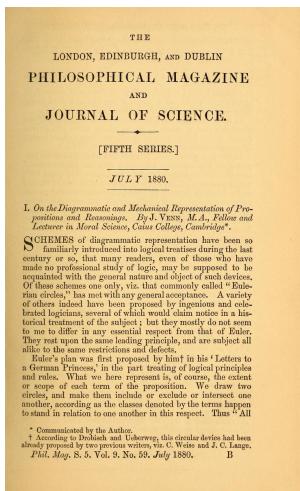


# Venn Diagrams

# What is a Venn Diagram?

J. Venn M.A. (1880) I. On the diagrammatic and mechanical representation of propositions and reasonings, *The London, Edinburgh, and Dublin Philosophical Magazine and Journal of Science*, 10:59, 1-18, DOI: 10.1080/14786448008626877



$A \cup B$

$x \in A \text{ but } x \notin B$   
 $A - B$

$x \in A \text{ and } x \in B$

$A \cap B$

$x \notin B \text{ and } x \in A$

$A \cup B$  is whole diagram

I. On the Diagrammatic and Mechanical Representation of Propositions and Reasonings. By J. VENN, M.A., Fellow and Lecturer in Moral Science, Caius College, Cambridge

SCHEMES of diagrammatic representation have been so much discussed in late years that it would be tedious to repeat what has been said on the subject in the last century or so, that many readers, even those who have made no professional study of logic, may be supposed to be acquainted with the principal schemes of this class of devices. Of these schemes one only, viz. that commonly called "Boolean's circles," has not with my general acceptance. A variety of other ingenious schemes have been proposed by logicians and delineated logicians, several of which would claim notice in a historical review of the subject; but they all seem to me to differ in any essential respect from that of Boole. They rest upon the same leading principle, and are subject all alike to the same difficulties.

Boole's plan was first proposed by him in his "Letters to a German Princess," in the part treating of logical principles and methods. He did not, however, indicate the exact extent or scope of each term of the proposition. We draw two circles, and make them include or exclude or intersect one another, according to the relations denoted by the terms happen to stand in relation to one another in this respect. Thus "All

\* Communicated by the author.

† According to DeMorgan, this circular device had been already proposed by two persons written, Dr. A. White and J. C. Lange, Phil. Mag. 5, 9, Vol. 3, No. 20, July 1850.

Mr. Venn on the Diagrammatic and Mechanical  
Representation of Propositions and Reasonings.  
The existing conception of this scheme is then simply this:—  
That it involves some consideration in order to decide upon the most effective and symmetrical plan of carrying it out. Up to three terms, indeed, there is but little opening for any choice. When we come to consider a plan for four terms, we will examine these simpler cases somewhat carefully. In the diagram for two terms, there is to be thus drawn a circle on the common plan this would represent a *proposition*, and is usually taken as illustrative of the expression "Some X is Y." With us it does not as yet represent a proposition at all, but only the framework into which propositions are to be fitted. We have now to find four terms corresponding to the letter-combinations XY, XY, XY, XY. Now conceive that we have to re-arrange also with the process, and consequently with the absence, of Z. We have to find a third circle intersecting the two above, the (XY)²,

and we have the eight compartments or cells, which we need. The subdivisions thus produced correspond respectively with the letter-combinations. Quoto one of these letters, and the appropriate class-division is ready to meet it; put a finger into the compartment, and you have your proposition.

Moreover both schemes, that of letters and that of spaces, agree in being mutually exclusive and collectively exhaustive, and in being such as to give no opportunity for any trespasses upon the ground of any other; and amongst them they account for all possibilities. Either scheme, therefore, may be taken as a basis for our purpose.

Beyond three terms circles fail us, since we cannot draw a fourth circle which shall intersect three others in the way required. But there is no theoretical difficulty in carrying out the idea of indefinitely many classes. Of course any class we can conceive of must be represented by a circle, or by a circle-like figure, since all that we demand of it is, in order that it shall adequately represent the contents of a class, is that it shall contain all the elements of the class, and nothing else, and that what does not belong to the class. There is nothing to prevent us from going on, or even thus drawing a fifth circle, and so on ad infinitum; the consequent number of class-divisions.

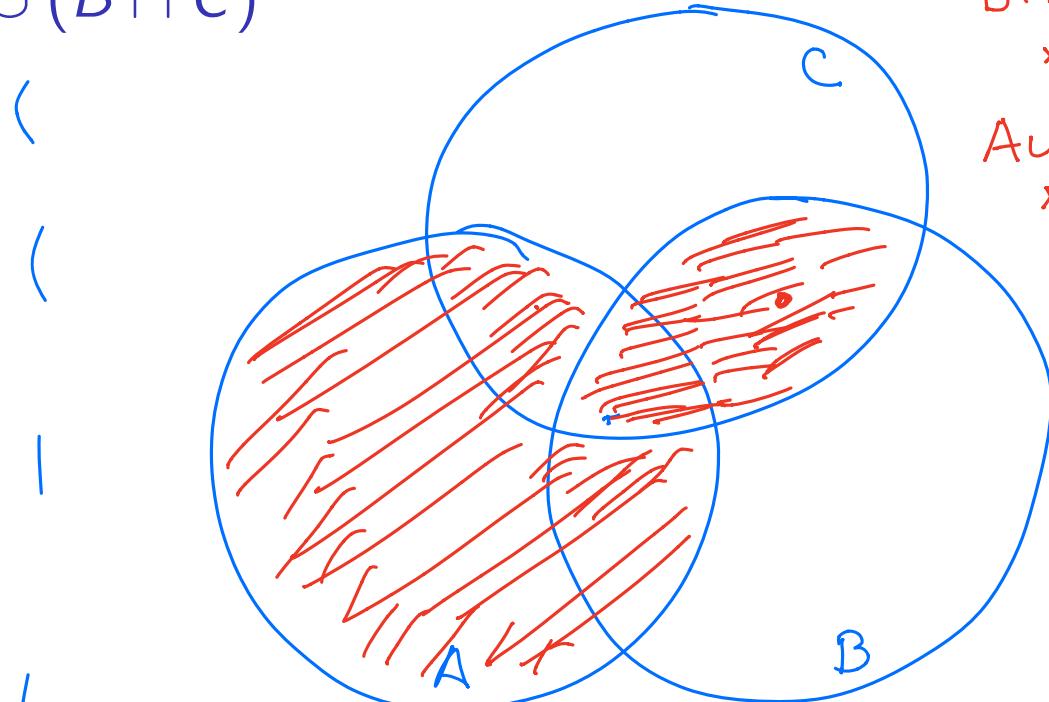
The only objection is, that since diagrams are physical, they are liable to error, and to the consequent number of class-divisions.

\* It really takes, however, three common propositions to exhaust its possibilities; for the given five we get only the two statements "Some X is not A" and "Some Y is not B."

## Venn Diagrams continued

- ▶ Graphical representation of set operations
- ▶ Convenient as check or for presentation and explanation but (like any diagram) not conclusive without explanation.

$A \cup (B \cap C)$



$B \cap C$

$x \in B \text{ and } x \in C$

$A \cup (B \cap C)$

$x \in A$

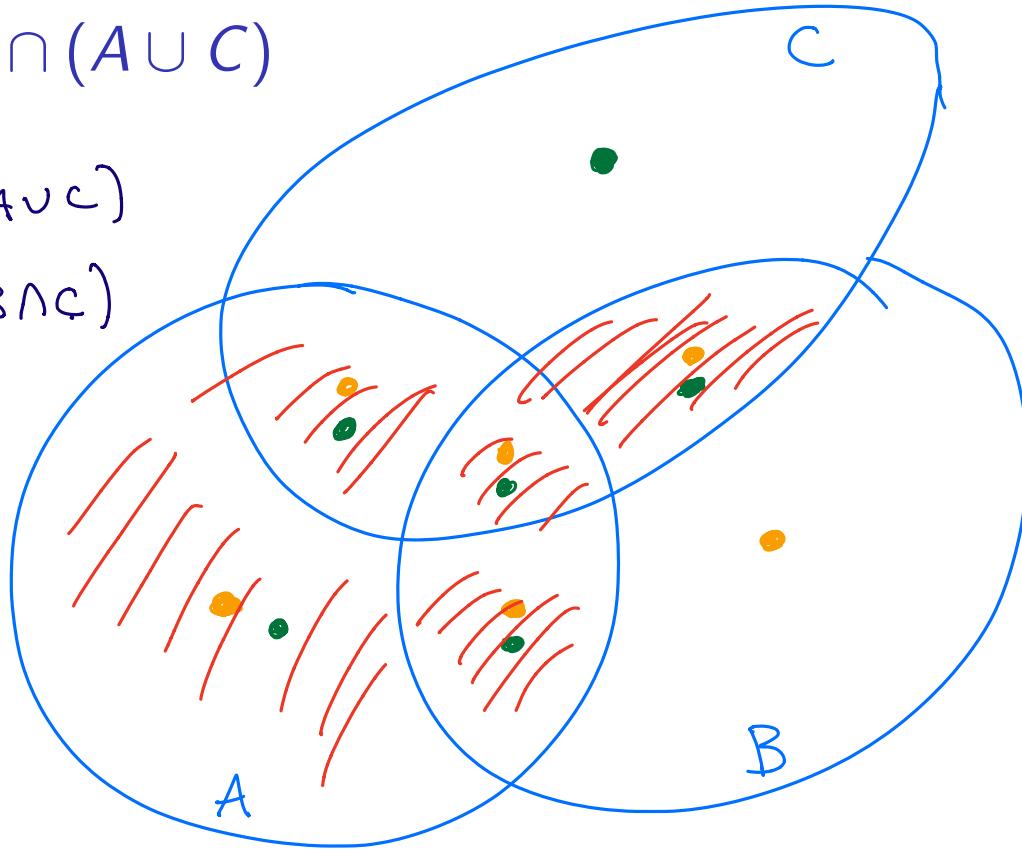
OR

$x \in B \cap C$

$$(A \cup B) \cap (A \cup C)$$

$$(A \cup B) \cap (A \cup C)$$

$$= A \cup (B \cap C)$$

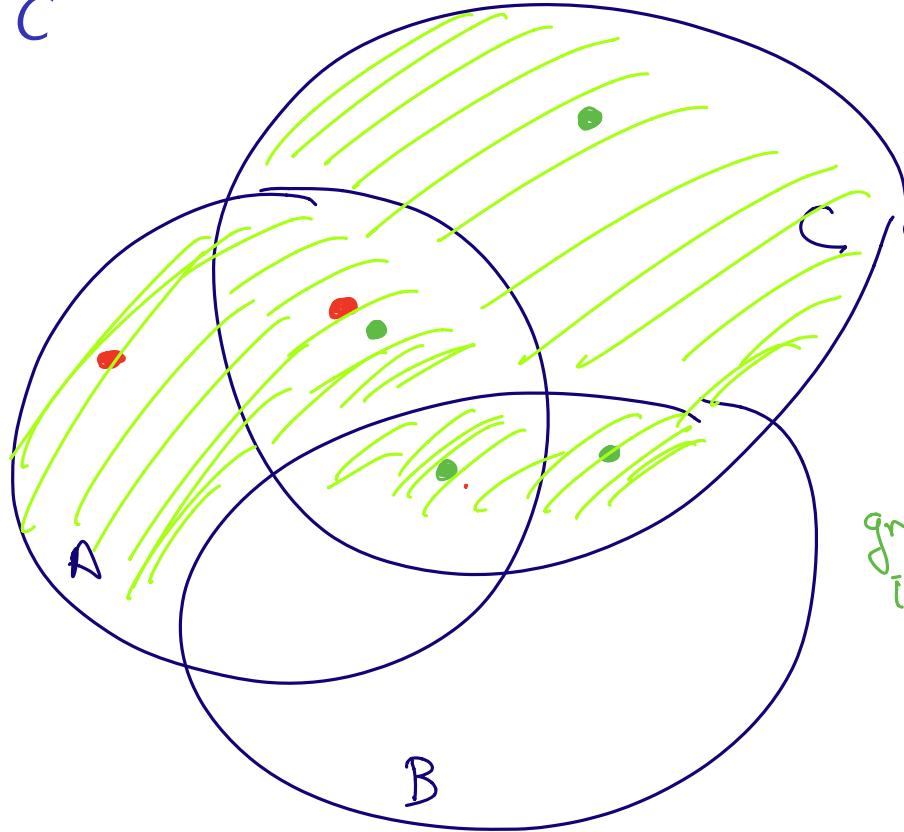


$$A \cup B = \{x: x \in A \text{ or } x \in B\}$$

$$A \cup C = \{x: x \in A \text{ or } x \in C\}$$

Both orange  
and green

$$(A - B) \cup C$$

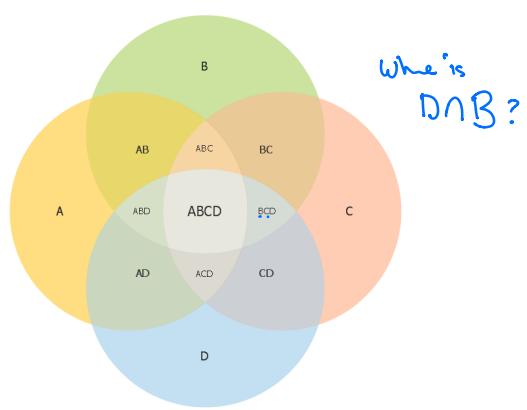


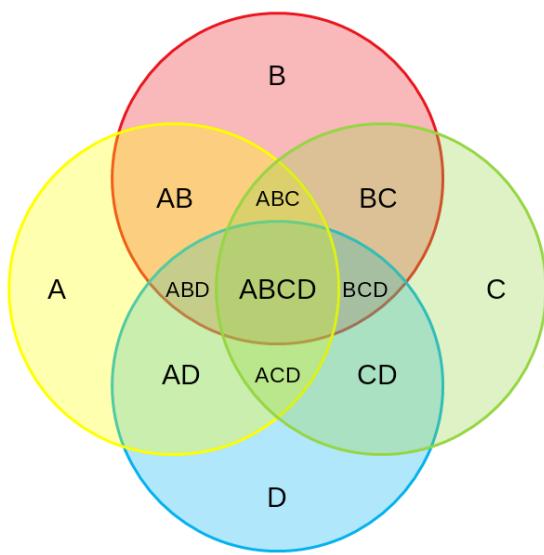
$$(A - B) \cup C$$

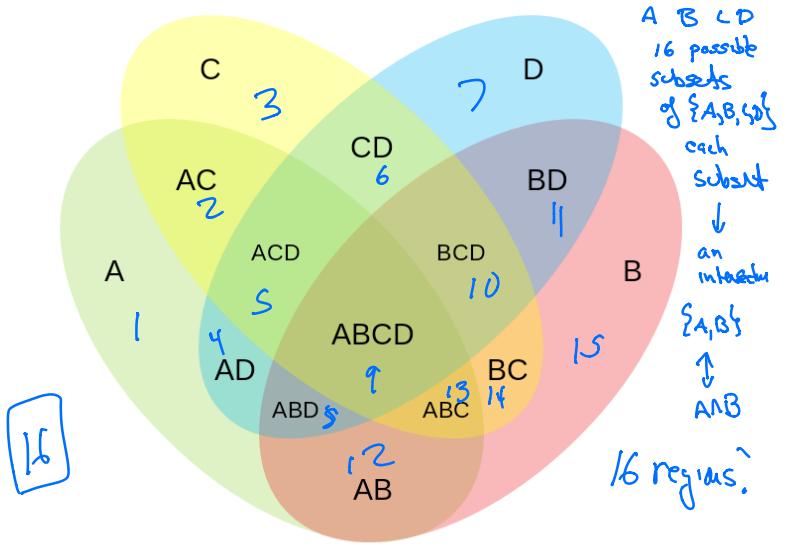
green or red dot  
is in  $(A - B) \cup C$

$$A - B = \{x \in A \text{ but } x \notin B\}$$

$$(A - B) \cup C = \{x : x \in C \text{ or } x \in A - B\}$$







$A \cup B \cup C \cup D$   
16 possible  
subsets  
of  $\{A, B, C, D\}$

each  
subset  
 $\downarrow$   
an  
intersection  
 $\{A, B\}$   
 $\uparrow$   
 $A \cap B$

16 regions.

16