## Pairs of Quantifiers

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## Paired quantifiers $\exists$ , $\exists$

▶ There exists  $x \in A$  so that there exists  $y \in B$  so that P(x, y)

There exists  $x \in \mathbb{N}$  so that there exists  $y \in \mathbb{N}$  so that x + y = 5.

$$\forall$$
,  $\forall$ 

▶ For all  $x \in A$  and for all  $x \in B$ , P(x, y).

For all  $x \in \mathbb{N}$  and for all  $y \in \mathbb{N}$ , xy > 0.

For all  $x \in \mathbb{Z}$  and for all  $y \in \mathbb{N}$ , xy > 0.

$$\forall$$
,  $\exists$ 

▶ For all  $x \in A$  there exists  $y \in B$  so that P(x, y).

For all  $x \in \mathbb{N}$  there exists  $y \in \mathbb{N}$  so that 2y = x.

For all  $x \in \mathbb{Z}$  there exists  $y \in \mathbb{Q}$  so that 2y = x.

For all  $\epsilon \in \mathbb{R}$  with  $\epsilon > 0$ , there exists  $\delta \in \mathbb{R}$  with  $\delta > 0$  so that  $x^2 < \epsilon$  when  $x < \delta$ .

## $\exists, \forall$

▶ There exists  $x \in A$  so that for all  $y \in B$  we have P(x, y).

There exists  $x \in \mathbb{N}$  so that for all  $y \in \mathbb{N}$  we have xy > 1.

There exists  $x \in \mathbb{Q}$  so that for all  $y \in \mathbb{Q}$  we have xy < y.