Addition/Subtraction Principle

Addition Principle and Disjoint Unions

Definition: Two sets are said to be *disjoint* if $X \cap Y = \emptyset$. Similarly, a collection X_1, \ldots, X_n of sets are said to be disjoint if any pair of them is disjoint.

Note that one can have 3 sets A, B, and C with $A \cap B \cap C = \emptyset$ but A, B, and C are not disjoint.

Proposition: Let X_1, X_2, \dots, X_n be a disjoint collection of finite sets. Then

$$|X_1 \cup X_2 \cup \dots \cup X_n| = \sum_{i=1}^n |X_i|.$$

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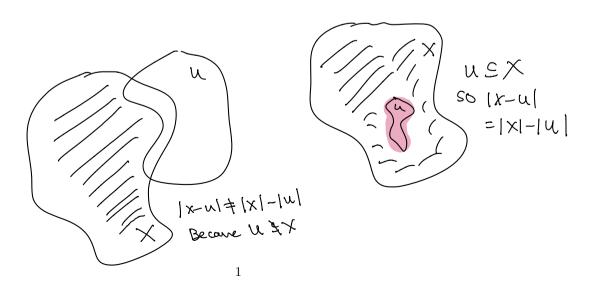
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Proposition: Suppose that $U \subseteq X$. Then |X - U| = |X| - |U|



Problem 3

(Problem 3 from section 3.3) Five cards are dealt from a 52-card deck and lined up in a row. How many such lineups are there in which all five cards are the same color (i.e. black or red)?

26 red 26 black

Total Number =

where all are red: 26 in position 1

where all are black

same frall black

26.25.24.23.22.21

Problem 9

(Problem 9 from Section 3.3) Consider "words" of length 6 made from the letters A, B, C, D, E, F, G, H. How many such words are possible if each letter can occur at most one time, and the word must contain two consecutive vowels?

> AE CONTAINS [, YORD OR CONTAINE EA

How may words of length 6 contain AE and He letters chosen from B, C,D, F, G, H, each only occurring once.

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A E choice 5 4 3

A E A E A E A E group has 6.5.4.3 elements

5 (6.5.4.3) Same thing with EA: same count. Final #: 2.5.(6.5.4.3)