## $\mathbf{Sets}$

1. Let m and n be integers. Prove that

$$\{x \in \mathbb{Z} : mn|x\} \subseteq \{x \in \mathbb{Z} : m|x\} \cap \{x \in \mathbb{Z} : n|x\}.$$

When does equality hold?

- 2. Suppose A, B, C are sets. Show  $A \times (B \cap C) = (A \times B) \cap (A \times C)$ .
- 3. Suppose  $A \neq \emptyset$ . Prove that  $A \times B \subseteq A \times C$  if and only if  $B \subseteq C$ . What if A is empty?

## Euclid's algorithm and congruence equations

- 1. Solve  $7x \equiv 3 \pmod{41}$ .
- 2. Solve  $6x \equiv 2 \pmod{24}$ .