

# Math 2710

Aug 26-28

## Course Info

# Key links

- ▶ Syllabus
- ▶ Tests
- ▶ Homework
- ▶ Piazza

# Grading

- ▶ Two midterms (25 points) tentatively Sep 30 and Nov 5.
  - ▶ Notify me by Sep 20 if you need an alternate date for the first exam because of Rosh Hashanah.
- ▶ Final Exam (40 points)
- ▶ Homework (8 points)
- ▶ Piazza participation (2 points)

# Homework

- ▶ daily assignments
- ▶ periodically collected and graded with short lead time
- ▶ assorted short quizzes or other assignments from time to time

What is this course about?

# Mathematics as a discipline

This course is about

- ▶ *how mathematics is done*
- ▶ *how mathematics is communicated.*

The actual mathematics we will learn in this course is less important than the approach

## A very simple example

**Assertion:** The sum of two even numbers is an even number.

Question: why is this true?



# Mathematical Proof

A *mathematical proof* of this assertion is an argument that starts from known facts and definitions and establishes the the truth of the assertion using the tools of logic.

A good mathematical proof is

- ▶ *rigorous*, meaning it gives a complete logical argument,
- ▶ *informative*, meaning that it provides enough information to explain why the assertion is true
- ▶ *efficient*, meaning that it is as short as possible while still being rigorous and informative.

## Example, continued

To construct a proof of this assertion, we need:

- ▶ to know exactly what the terms mean (what is an even integer?)
- ▶ to establish in our own minds that the assertion IS true, and figure out why
- ▶ communicate our understanding of why the assertion is true rigorously and efficiently.

# Discussion

- ▶ Define *even number*.
- ▶ Explain why the assertion about even numbers is true, as rigorously and efficiently as you can.

# Key Vocabulary

theorem, lemma, proposition, corollary, example, algorithm,  
definition, proof, statement, proposition, converse, contrapositive,  
conditional statement