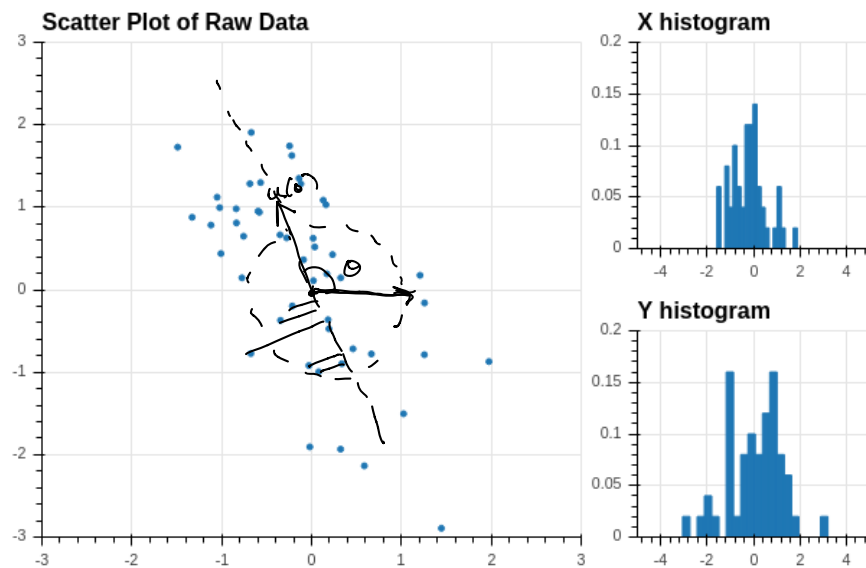


# Change of variance with direction

## Change of variance



50%  $\text{var}$

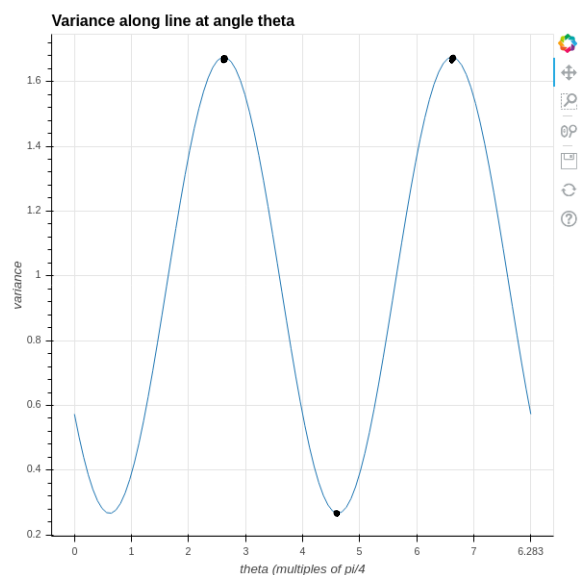
$$X = \begin{pmatrix} x_1 \\ \vdots \\ x_n \end{pmatrix}$$

$$u(\theta) = \begin{bmatrix} \cos \theta \\ \sin \theta \end{bmatrix}$$

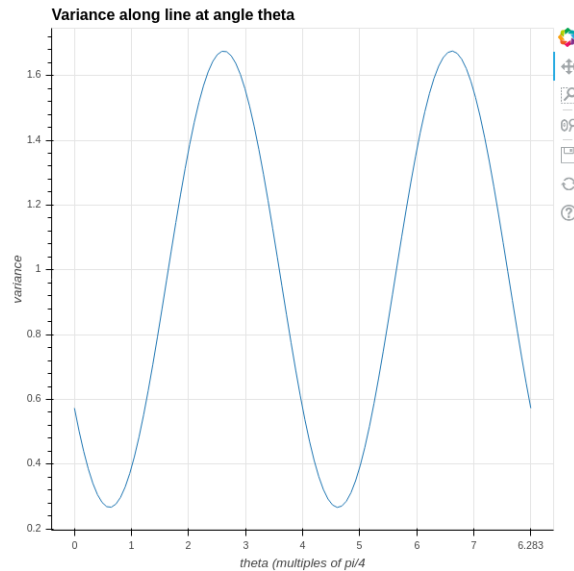
$$\|u(\theta)\|^2 = 1$$

$$\sigma_\theta^2 = \frac{1}{n} S(\theta)^T S(\theta) = \frac{1}{n} u(\theta)^T D_0 u(\theta)$$

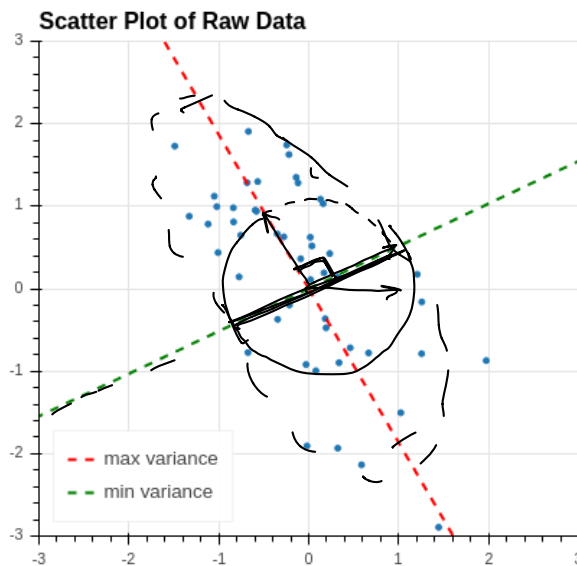
$X u(\theta)$  = points along  $\theta$  line  $S(\theta)$



## principal directions



principal directions are the critical points where variance along  $u$  is a max or a min.



2 principal directions  
 - variance minimal  
 - variance maximum