# MACHINE LEARNING

## Notes on A. Ng lectures

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**Résumé** Notes on the Machine Learning lectures of A. Ng.

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## 1 LINEAR REGRESSION WITH ONE OR MULTIPLE VARIABLES

## 2 LOGISTIC REGRESSION

We focus on classification problems for which the output y is binary (bi-class classification problem, later on, we will speak about multiclass classification) :  $y \in \{0, 1\}$ . We call class-0 the negative class and class-1 the positive class but these are just arbitrary names. For example, one may seek to learn to classify a tumor to be malignant or not depending on its size, or filter mails as being spam or not depending on some measure.

With linear regression, we can define a boundary condition saying : "if  $h_{\theta}(x)$  is larger or equal than 0.5 then consider it as belonging to class-1, otherwise it belongs to class-0".

Note : il utilise le problème de classer des tumeurs, en ajoutant un outlier tends à déplacer la frontière de décision pour donner un mauvais classifieur. "I would not use linear regression for classification problems".

Il introduit la régression logistique pour contenir l'hypothèse  $h_{\theta}(x)$  dans [0,1] alors qu'avec la régression linéaire peut donner des valeurs bien au dela de ce domaine alors que les étiquettes valent disont 0 et 1... Mais il y a aussi la sensibilité aux outliers (à vérifier!!)

On introduit le modèle de régression logistique :

$$h_{\theta}(x) = g(\theta^T x) = \frac{1}{1 + e^{-\theta^T x}}$$
 (1)

On peut voir  $h_{\theta}(x)$  comme la probabilité estimée que y=1 pour l'entrée x. C'est à dire qu'on considère  $h_{\theta}(x)$  comme un modèle paramétré de  $P(y=1|x;\theta)$ . Pour trancher si une entrée x appartient à l'une ou l'autre des classes, il faut introduire un seuil sur cette probabilité. Par exemple, si on prédit y=1 quand  $h_{\theta}(x) \geq 0.5$ , cela correspond à prédire y=1 quand  $\theta^T x \geq 0$ . Le plan correspondant à  $\theta^T x=0$  est appelée "decision boundary". Comme le feature vector peut contenir des combinaisons non-linéaires de nos observations, e.g.  $x=[1,x_1,x_2,x_1^2,x_2^2]$ , la boundary decision peut être non-linéaire quand tracée dans l'espace des observations, e.g.  $x_1,x_2$ .

On doit maintenant dériver des algorithmes pour trouver les paramètres  $\theta$ . Partant d'une base d'apprentissage  $(x^{(i)}, y^{(i)})$  avec  $\forall i, y^{(i)} \in \{0, 1\}$ , on cherche les paramètres  $\theta$ . Pour la régression linéaire, on a quantifié la classification par une fonction quadratique  $J(\theta) = \frac{1}{2m} \sum_i (h_\theta(x^{(i)}) - y^{(i)})^2 = \frac{1}{m} \sum_i \cosh(h_\theta(x^{(i)}), y^{(i)})$ . La fonction de coût est donc une fonction des coûts de chaque exemple. Pour la régression linéaire, avec un coût quadratique, le coût  $J(\theta)$  était convexe et le problème d'optimisation avait donc un seul minimum. Avec une hypothèse  $h_\theta$  logistique, la fonction de coût n'est plus convexe si on utilise un coût quadratique ce qui a la conséquence fâcheuse d'introduire plusieurs minimums locaux à la fonction de coût (ce qui pose des problèmes pour la minimiser avec, par exemple, une descente de gradient). Pour la régression logisitique, on introduit le coût logarithmique :

$$cost(h_{\theta}(x), y) = \begin{cases}
-\log(h_{\theta}(x)) & \text{si } y = 1 \\
-\log(1 - h_{\theta}(x)) & \text{si } y = 0
\end{cases}$$
(2)

On remarque qu'on peut réécrire cette fonction de coût  $^1$  sous la forme  $cost(h_{\theta}(x), y) = -(1 - y) log(1 - h_{\theta}(x)) - y log(h_{\theta}(x))$ . Cette fonction de coût est convexe et donc sans minimums locaux. On en vient à introduire la fonction de coût  $J(\theta)$ :

$$J(\theta) = \frac{1}{m} \sum_{i} \operatorname{cost}(h_{\theta}(x^{(i)}), y^{(i)})$$
(3)

$$= -\frac{1}{m} \left( \sum_{i=1}^{m} y^{(i)} \log(h_{\theta}(x^{(i)})) + (1 - y^{(i)}) \log(1 - h_{\theta}(x^{(i)})) \right)$$
(4)

Pour trouver les paramètres qui minimise cette fonction de coût, on peut considérer une descente de gradient :

$$\theta_j \leftarrow \theta_j - \alpha \frac{\partial}{\partial \theta_j} J(\theta) \tag{5}$$

En calculant le gradient du coût par rapport aux paramètres, on obtient la règle de mise à jour des paramètres :

$$\theta_j \leftarrow \theta_j - \alpha \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) x_j^{(i)}$$
(6)

<sup>1.</sup> On aurait pu imaginer une autre formulation de la fonction de  $coût cost(h_{\theta}(x), y) = -\log((1-y)(1-h_{\theta}(x)) + yh_{\theta}(x))$  mais il y a des raisons théoriques pour préférer la version du texte, elle est convexe et est dérivée de principe de Maximum Likelihood estimation???????

Comme pour la régression linéaire, les paramètres sont mis à jour simultanément. On pourra remarquer que cette règle de mise à jour est identique à la règle de mise à jour des paramètres pour la régression linéaire, à ceci près que l'hypothèse  $h_{\theta}$  est différente (et la fonction de coût a été particulièrement bien choisie). Comme pour la régression linéaire, on peut ajuster l'échelle des features (feature scaling) pour améliorer la vitesse de convergence de la descente de gradient.

Tracer la fonction de coût quand y=1 pour montrer que si  $h_{\theta}(x)$  tend vers 1, le coût tends vers 0; Au contraire si  $h_{\theta}(x)$  tends vers 0 (alors que y=1 puisque que  $h_{\theta}(x)=P(y=1|x;\theta)$ ), le coût tends vers l'infini et l'algorithme est donc fortement pénalisé pour cette erreur. On peut mener un raisonnement similaire pour le cas y=0 dans lequel on pénalise fortement lorsque  $h_{\theta}(x) \to 1$ .

La descente de gradient est une des manières de minimiser notre fonction de coût. Il en existe d'autres, parfois plus rapide en terme du nombre d'itérations nécessaires pour atteindre le minimum. Une liste d'algorithmes alternatifs est donnée ci-dessous :

- gradient conjugué
- BFGS
- L-BFGS

Ces algorithmes ont un certain nombre d'avantages par rapport à la descente de gradient :

- il n'y a pas besoin de spécifier manuellement un taux d'apprentissage  $\alpha$ , celui-ci est ajusté automatiquement
- ils sont en général plus rapide à converger qu'une descente de gradient

Ils sont néanmoins plus compliqués à comprendre et mettre en œuvre. Cela dit, il existe un certain nombre d'implémentations clé-en-main de ces algorithmes.

With Octave, you would make use of the *fminunc* function with specific options setting which algorithm to use. We now go back to multi-class classification. Therefore, we suppose that the output y can take more than two values. One way to solve this problem is to consider multi-class classification problems as multiple binary classification problems. We then train as many binary classifiers as we have classes. Each of these classifier learns to recognize one class versus all the others. Given all the individual classifiers  $h_i$ , we may define label an input x as belonging to the class which maximizes the outputs  $h_i(x)$ ,  $\forall i \in [1..k]$ .

## 3 REGULARIZATION

## 3.1 Motivation

Sometimes, when trying to fit an hypothesis to a data set, we may run into a problem called overfitting. Overfitting arises because we have just a partial observation of the true model that generates the data we are trying to fit. We therefore make an hypothesis on the shape of this model. Obviously, when we fit a model on a dataset, we want to interpolate the output for unobserved inputs (inputs that are not in the training set). The hypothesis we consider define how different we can interpolate this output. The simplest example of overfitting can be seen when fitting a polynomial on data set. If we increase the degree of the polynomial, we introduce more flexibility to the model (indeed, with the Lagrange polynomials, we know that we can fit perfectly any data set if we don't constrain the degree of the polynomial). This flexibility can lead to more variability in the model which may impairs the ability of the model to generalize, i.e. to give the right answer on new data unavailable in the training set.

There are two options to adress overfitting. The first one is to reduce the number of features whether by manually selecting the features to keep or to use model selection algorithm. However, throwing away some features may throw away some information contained in the dataset. The second option is called regularization. Regularization is a technique which allows to balance the tendency to overfit the training set by a term which constrains the *complexity* of the model.

## Des données à fiter avec un polynôme

Suppose we consider linear regression with some polynomials of the inputs : $h_{\theta}(x) = \theta_0 + \theta_1 x + \theta_2 x^2 + \theta_3 x^3 + \theta_4 x^4$ . If we penalize the two parameters  $\theta_3$  and  $\theta_4$ , the polynomial  $h_{\theta}$  will be simpler. To penalize these two parameters we can modify the quadratic cost function by adding terms that increases the cost depending on the amplitude of these parameters, e.g.  $J(\theta) = \frac{1}{m}(h_{\theta}(x^{(i)}) - y^{(i)})^2 + 1000\theta_3^2 + 1000\theta_4^2$ . Minimizing this modified cost function will constrain the parameters  $\theta_3$  and  $\theta_4$  to be small. More generally, as we may not know which parameters influence overfitting, we introduce the following cost function for linear regression:

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2 + \lambda \sum_{i=1}^{n} \theta_j^2$$
 (7)

By convention,  $\theta_0$  is not regularized. The parameter  $\lambda$  balances the trade off between fitting the dataset and keeping the parameters  $\theta_i$  small. If  $\lambda$  is set too large, minimization of this cost function may unfortunately lead to underfitting, i.e. we even do not fit the training set. Fortunately, one may define algorithms automatically adjusting the penalization coefficient  $\lambda$ .

**Question** : est ce qu'introduire le terme de régularization ne rends pas la fonction de coût non convexe ? NON d'après une question du quizz, la fonction de coût reste convexe.

**Question** : pourquoi est ce qu'on s'en fout de ne pas régularizer le terme  $\theta_0$ .

Question : pourquoi ne pas pénaliser plus les termes de grand degré?

#### 3.2 REGULARIZED LINEAR REGRESSION

We remind the cost function for linear regression with L2 regularization:

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2 + \lambda \sum_{i=1}^{n} \theta_i^2$$
 (8)

Considering this regularized cost function, one must modify the gradient descent algorithm. The update of the parameters now reads :

TODO, calculer le gradient, d'après Ng : 
$$\theta_0 \leftarrow \theta_0 - \alpha/m \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) x_0^{(i)}$$
;  $\forall j \neq 0, \theta_j \leftarrow \theta_j - \alpha(1/m \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) x_j^{(i)} + \lambda/m\theta_j) = (1 - \alpha\lambda/m)\theta_j - \alpha/m...$ 

By isolating the terms depending on  $\theta_j$ , one gets an update rule of the form  $\theta_j \leftarrow \beta \theta_j - \alpha/m$ .., we see that we shrink the parameter and move in a direction minimizing the cost function (when considered without the regularization term).

We also saw that we can use normal equations for solving linear regression. Without regularization, the optimal parameters using normal equation was :  $\theta = (X^T X)^{-1} X^T y$ . We regularization inside, the normal equation now reads  $\theta = (X^T X + \lambda R)^{-1} X^T y$  where R is a diagnoal matrix filled in with 1, except for the first element which is set to 0. For e.g., with n = 2,  $R = \lceil 000; 010; 001 \rceil$ .

If you have less examples than features, the matrix  $X^TX$  is non invertible. If you use regularization, it is possible to prove that the matrix  $X^TX + \lambda R$  cannot be singular and that you can always invert it.**AH OUAIS???**.

## 3.3 REGULARIZED LOGISTIC REGRESSION

For logistic regression, the cost function reads:

$$J(\theta) = -\frac{1}{m} \sum_{i=1}^{m} (y^{(i)} \log(h_{\theta}(x^{(i)})) + (1 - y^{(i)}) \log(1 - h_{\theta}(x^{(i)})))$$
(9)

We can also add L2 regularization to this cost function to get:

$$J(\theta) = -\frac{1}{m} \sum_{i=1}^{m} (y^{(i)} \log(h_{\theta}(x^{(i)})) + (1 - y^{(i)}) \log(1 - h_{\theta}(x^{(i)}))) + \lambda/(2m) \sum_{j} \theta_{j}^{2}$$
(10)

The gradient descent update is then modified into  $\theta_0 \leftarrow \theta_0 - \alpha/m \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) x_0^{(i)}; \forall j \neq 0, \theta_j \leftarrow \theta_j - \alpha(1/m \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) x_j^{(i)} + \lambda/m \theta_j) = (1 - \alpha \lambda/m) \theta_j - \alpha/m...$ 

The update is very similar to regularized linear regression but remind that the hypothesis  $h_{\theta}$  is different for logistic regression.

## 4 IDÉES DE DÉMOS

Pour la régularisation, une appli dans laquelle on fit un polynôme sur des données et on règle dynamiquement la contribution  $\lambda$  de la régularisation pour voir la forme du modèle appris.

## **NEURAL NETWORKS: REPRESENTATION**

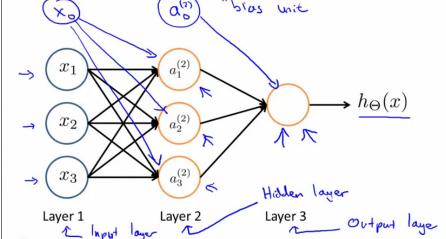
A vérifier: overfitting if we increase the number of features with a constant number of data?

Neural networks are the state of the art technique for several machine learning problems. To motivate neural networks, let us consider a non-linear classification problem. As we saw, we can use logistic regression with polynomial features (say  $x_1x_2, x_2^3x_3, ...$ ). However, given the size of our inputs, the size of the feature vector may be a polynomial of it which will certainly be quite big and increase the tendency to overfitting (if we consider too many features relative to the number of the data we have, we can easily encounter overfitting). To give on example, if one considers object recognition from images of size  $50 \times 50$ , one obtains images with n = 2500 pixels. If we just consider only quadratic terms  $x_i x_j$ , one gets around 3 million features, the number of features is indeed  $n^2/2$ . One may limit the number of features, but this selection is, there, somehow arbitrary. Neural networks are a much better way to define non-linear hypotheses than logistic regression with polynomial features.

Neural networks, while originally derived from the desire to mimick the brain, is used from an abstract viewpoint in Machine Learning where we consider simple massively interconnected entities. Each entity receives signal from others, process it locally and transmit a signal to other entities. The simple model we consider is a logistic unit, which receives inputs denotes  $x_i$ , computes a weighted sum of it and apply a sigmoid transfer function on it. This is nothing more than what we saw in the previous section  $y = h_{\theta}(x) = \frac{1}{1 + e^{-\theta^T x}}$ . We also add a bias unit to the inputs  $x_0 = 1$  in addition to the signals received from the other neurons  $x_i, i \ge 1$ . In the neural network literature,  $\theta$  are called the weights. We can build layers of such units and interconnect them. A multilayer neural network is shown on fig.1.

 $a_1^{(2)}$ 

FIGURE 1 – Representation of a feedforward neural network. Capture from the A. Ng lecture.



We will denote  $a_i^{(j)}$  the activation of the i-th unit of j-th layer. We denote  $\theta^{(j)}$  the matrix of weights from layer jto layer  $j + 1^2$ . The activation is computed according to :

$$\begin{cases} \forall i \geq 1, \forall j > 1, a_i^{(j)} = g(z_i^{(j)}) \\ \forall i \geq 1, \forall j > 1, z_i^{(j)} = \sum_k \theta_k^{(j-1)} a_k^{(j-1)} \\ \forall i \geq 1, a_i^{(1)} = x_i \\ \forall j, a_0^{(j)} = 1 \end{cases}$$
(11)

These equations tell nothing more than that the first neuron is the bias for the next layer, the activations  $a_i^{(1)}$  of the first layer equal our inputs and each neuron in a subsequent layer computes its activation  $a_i^{(j)}$  as a sigmoid of a weighted sum of the activations of the previous layer  $a_k^{(j-1)}$ . A vectorized notation for computing the activations of layer j+1 is simply  $a^{(j+1)}=g(\theta^{(j)}.a^{(j)})$  where  $\theta^{(j)}$  is a matrix of size  $|L_{j+1}|\times |L_j|$  with  $|L_j|$  the number of neurons in layer *j* (the bias being included). For regression, the last layer contains a single neuron of which the activation, if unfolded, is a function of the input x. Computing the activations in a layer-wise manner from the very first layer to the output is called the forward propagation. If we take a closer look to the 3-layers neural network depicted above, the hidden to output layer is nothing more than a logistic regression with Layer 2 representing the features. Now, if we include the very first layer with the weights projecting the inputs to the hidden layer, we can see it as building the

<sup>2.</sup> We here consider only feedforward neural networks were the connections always go from layer j to layer j+1

features feeding the logistic regression. And the nice thing there is that the features are learned through the weights from Layer 1 to Layer 2. It may not be completely clear that the features we compute that way (the activations of layer 1) can be arbitrary polynomials but indeed one may demonstrate that if we don't restrict ourselves to a single hidden layer, one can approximate any function (feedforward neural networks are universal approximators) so that feedforward neural networks have at least the expressiveness of logistic regression.

Now let us consider simple binary operations like and, or, not, xor. We can easily write a simple neural network with a single input layer and a single output for the and and *or* functions :

- and function :  $\theta = (-30, 20, 20)$ - or function :  $\theta = (-10, 20, 20)$
- *not* function :  $\theta = (10, -20)$

These are both linearly separable problems. The Xor function is not linearly separable and one needs to consider at least one hidden layer to compute it. To put it simply, we just need to write  $x_1xorx_2 = or(and(not(x1), x_2), and(x1, not(x_2)))$ . The functions not(x1) or x2, as well as x1 and not(x2) can be compute with a single layer. These are the input to hidden layer connections. Finally, we just connect the hidden to the output layer for computing the or function.

Before, we were speaking about a simple regression example. An example of multi-class classification is given by the LeNet 5 feedforward neural network developed by Y. LeCun which he trained for recognizing handwritten digits. The trained network is quite unsensitive to scale, orientation, and some forms of noise. For multi-class classification, we consider an output layer of the size of the number of classes. The output  $y^{(i)}$  for input  $x^{(i)}$  is set to  $y^{(i)}_j = \delta(j, l^{(i)})$  where  $\delta$  is the kronecker symbol and  $l^{(i)}$  is the class of the input  $x^{(i)}$ .

Ref pour l'approximateur universel?

## 6 10

In this section, few advices are given so as to know on which parameters one must play in order to improve the performances of the machine learning algorithm.

For example, when we test an hypothesis and find that it performs very badly on new unknown data, there are indeed various options one may be tempted to try, among which:

- get more training examples, it will probably better constrain the optimization of the hypothesis
- try smaller sets of features to avoid overfitting
- try getting additional features
- try adding polynomial features
- try decreasing or increasing the regularization parameter  $\lambda$

Instead of trying one of these options at random, we can diagnose what is going wrong with our algorithm. One possibility to diagnose how an hypothesis performs is, in low dimension (up to 3), to plot the decision boundary for classification or the hypothesis directly for regression. However, in higher dimensions, this is not possible.

#### 6.1 Training set/Test set and error measures

We would rather split the dataset in (at least) two datasets: a **training set** (70% of the data) and a **test set** (30% of the data). <sup>3</sup>. Then we optimize the parameters on the training set and measure the generalization error on the test set. For classification problems, one may also measure the misclassification error:

$$\operatorname{err}(h_{\theta}(x), y) = \begin{cases} 1 & \text{if } h_{\theta}(x) \ge 0.5, y = 0\\ & \text{or } h_{\theta}(x) < 0.5, y = 1\\ 0 & \text{otherwise} \end{cases}$$
 (12)

The test classification error is then just the mean over the test set of the misclassification error above which represents the proportion of the test set that is misclassified.

## 6.2 Model selection and train/validation/test sets

As we know already, the training error alone is not an appropriate measure for evaluating the performances of an hypothesis on unseen data since we might be overfitting. Instead, we should use the test set error. Suppose we wish to select among several polynomial hypothesis one that performs better. To do such a model selection, we will compare the test set errors and select the model with the lowest test error; However, to report the generalization ability of the model that we selected, we should use additional data as using the test set might overestimate the generalization

<sup>3.</sup> be sure that these sets are made of random samples of the datasets to avoid training on a specific region of the space while testing on another non-overlapping region

error of the model (the degree of polynomial was indeed selected so that the test set error is decreased). Therefore, we should split the dataset into three pieces: the training set (60%), the cross-validation (cv) or validation set (20%) and the test set (20%):

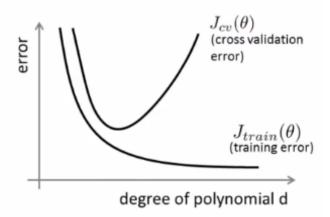
- the training set is used to optimize the parameters of the models
- the test set is used for selecting among the various that we have trained
- the validation set is used to estimate the generalization error of the selected model

## 6.3 Bias/variance issues

High bias issue is when the hypothesis is not sufficiently complex (underfit) while high variance is when the hypothesis is too complex (overfit). To better appreciate these issues, let us consider the case of polynomial hypothesis and plot both the training and validation errors as function of the degree of the polynomial (fig. 2).

As we increase the degree of the polynomial, we expect the training error to decrease as the model is more and more complex and we can overfit the training set more easily with higher degrees. The cross validation error will usually start as high as the training error, decrease and, then, at some point, increase as we overfit the training set and impair the generalization ability of the hypothesis.

FIGURE 2 – Typical curves of training and validation errors function of the degree of a polynomial hypothesis



Detecting whether we encounter a high variance or high bias problem is critical as we will not behave the same way in the two conditions. A high bias means a model that is not enough complex such that it cannot even fit the training set properly. A high variance means a model that is too complex so that it certainly fits perfectly the training set but performs poorly on the test set.

		Validation error	
		Low	High
Training error	Low	Good	High variance
	High	-	High bias

## 6.4 REGULARIZATION AND BIAS VARIANCE

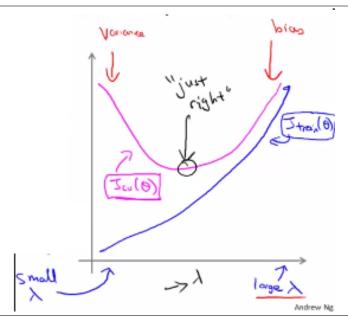
Varying the regularization parameter will affect the bias/variance. A very large parameter will penalize high values, leading to small parameters, leading to a high bias (fig. 3). If the regularization parameter is too small, say absent, a model that is too complex will not be penalized and we will probably run into high variance issues. Therefore, the regularization parameter must be correctly adjusted. This parameter must be choosen empirically, by testing different values for this parameter and checking both the training and cross validation errors. We then peak out the parameter giving a the lowest cross validation error and then evaluate the true performances on the test set.

We can also plot the training and cross validation errors as functions of the number of training examples (the learning curves). The training error usually increases as you use a larger training set as it is pretty easy to fit perfectly few examples while more complicated to fit more. The cross validation error will usually decrease as you more easily overfit small training set and you generalize better if you use more training examples that better constrain the hypothesis.

- if an algorithm is suffering from high bias (e.g. the hypothesis is not complex enough), getting more training data will not help much
- if an algorithm is suffering from high variance, getting more training data will help

Given the previous observations, below is a list of options to consider depending on whether we face a high bias or high variance issue :

FIGURE 3 – Skecthes of how the training and cross validation errors usually evolve as a function of the regularization parameter.



- Getting more training examples : will help fixing high variance problems
- try smaller sets of features : will help fixing high variance problems
- try getting additional features : will usually help fixing high bias
- try adding polynomial features : might help fixing high bias
- try decreasing  $\lambda$  for fixing high gbias, increasing  $\lambda$  for fixing high variance

## 7 Machine Learning System design

## 7.1 Prioritizing what to work on: Spam classification example

This section deals with various aspects of designing a machine learning system using the example of designing a spam classifier.

The first step is to decide what to use for the features. For example, we might use 100 words that we consider might be indicative of the spam/non-spam category or to actually pike the words appearing the most frequently in the emails. The feature vector will then be a binary vector indicating whether a word appears or not in the email to classify. Some specific sophisticated features might also be added (e.g. from the header of the email, the body, checking for mispelled words, ...).

### 7.2 Error analysis

To design a machine learning system, one should

- 1. start with a simple, quickly to implement, (dirty) algorithm and test it on a cross validation set
- 2. plot learning curves to decide whether we should focus on more data, more features, ...
- 3. error analysis: check which examples are misclassified from the cross validation set and why they are misclassified (what is particular about them)

In particular, error analysis is really critical as it will really help in adjusting the features to use. For spam classification, a stemming software (e.g. Porter Stemmer) can be usefull for deciding whether or not some variations of the same word should be considered the same word. In this situation, there is no other solutions than trying different solutions and comparing their performances with respect to the cross-validation and test errors.