

**PHYS 632: Quantum Mechanics II (Winter 2021)**  
**Exercises 19 January 2021 (Tuesday, Week 3)**  
**Due Monday, 25 January 2021**

**Exercise 1.** Compute numerical values for the following (squared) Clebsch–Gordan coefficients. Remember the notation convention for the coefficients is  $\langle j_1 m_1; j_2 m_2 | j_3 m_3 \rangle$ , where  $\mathbf{J}_3 = \mathbf{J}_1 + \mathbf{J}_2$ . Come up with a *physical* reason for your answer in each case.

(a)  $|\langle 1\ 1; 1\ 0 | 3\ 1 \rangle|^2$

(b)  $|\langle 1\ 1; 1\ 0 | 1\ (-1) \rangle|^2$

(c)  $|\langle 0\ 0; 1\ 0 | 1\ 0 \rangle|^2$

(d)  $|\langle 0\ 0; 1\ 0 | 0\ 0 \rangle|^2$

(e)  $|\langle 1\ 0; 1\ 0 | 0\ 0 \rangle|^2$

a)

$$|\langle 1\ 1; 1\ 0 | 3\ 1 \rangle|^2 = 0 \quad j_1 + j_2 \leq j_3$$

b)

$$|\langle 1\ 1; 1\ 0 | 1\ -1 \rangle|^2 = 0$$

$$m_1 + m_2 \neq m_3$$

c)

$$|\langle 0\ 0; 1\ 0 | 1\ 0 \rangle|^2 = 1$$

d)

$$|\langle 0\ 0; 1\ 0 | 0\ 0 \rangle|^2 = 0$$

e)

$$|\langle 1\ 0; 1\ 0 | 0\ 0 \rangle|^2 = \frac{1}{3}$$

since  $\rightarrow |\langle 1\ 0; 1\ 0 | 0\ 0 \rangle|^2 = |\langle 1\ -1; 1\ 1 | 0\ 0 \rangle|^2 = |\langle 1\ 1; 1\ -1 | 0\ 0 \rangle|^2$