

sources: wikipedia K-d_tree

You are asked to complete the pseudocode draft below to realize the KD tree construction over a set of points $P = \{p_1, p_2, \dots, p_n\}$ and the coordinates of point p_i is $(p_i.x, p_i.y)$. The algorithm should satisfy the following requirements:

1. Start with X-axis when choosing the first division.
2. Divide the space until there is at most one point in each sub-panel
3. Do not divide further if there is only one point left in a panel
4. Assume there exists a function `mid(Points s, boolean byX_axis)` that returns the point that is the middle point by either X_axis or Y_axis
5. Each KD tree node has a value field pointing to the dividing point, one left child and one right child.

Algorithm 1 Construct the KD tree from a set of points

1. **procedure** `KD(P, byX_axis)` . *• If byX_axis is true, then divide the points by X_axis. Otherwise divide by Y_axis. P is the set of points.: //This algorithm constructs a KD tree based on a points set P and the first division is*
2. *by X_axis if the parameter byX_axis is true. It returns the KD root tree node.*
- 3.
4. *if !p {return NULL} //If there are no points in list, return NULL*
5. *if P.len==1 {return root = P} //If there is only one point, return the one point as KD Tree*
6. *P.sort(X_axis); //Sorts points*
7. *p = mid(Points s, boolean byX_axis) //Sets the correct median point by X axis*
8. *KDnode root.point = p //Sets KDnode to mid point*
9. *Node //Create node and construct subtrees*
10. (
11. *left_child=KD(P[1...med]), !byX_axis, //Creates left child from left half of P*
12. *right_child=KD(P[med+(1...n)], !byX_axis) //Creates right child from right half of P*
13. *);*
- 14.
15. *root = Node; //Sets root to Node*
16. **return** root
17. **end procedure**