

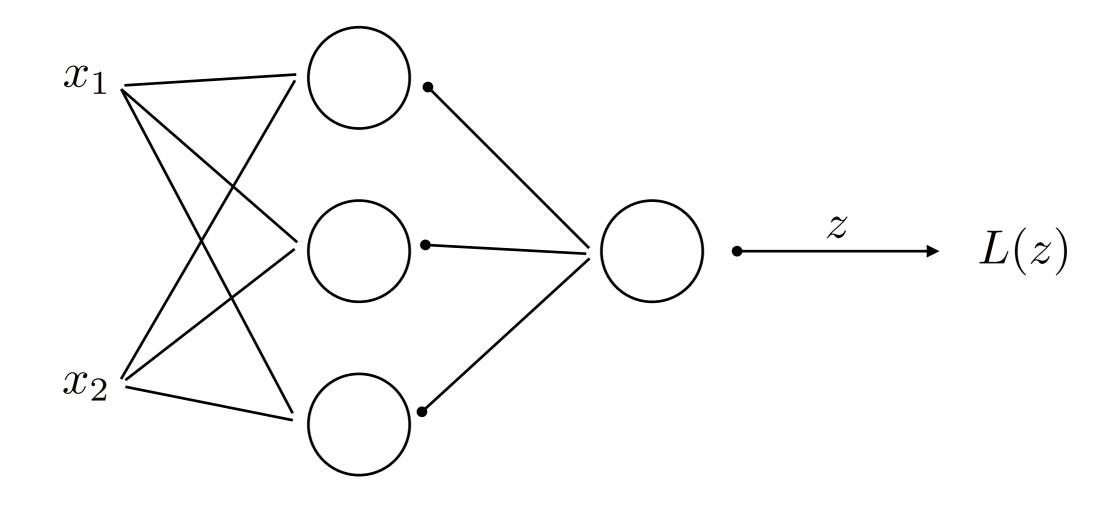
# Convolutional Neural Networks and Applications in the NEXT Experiment

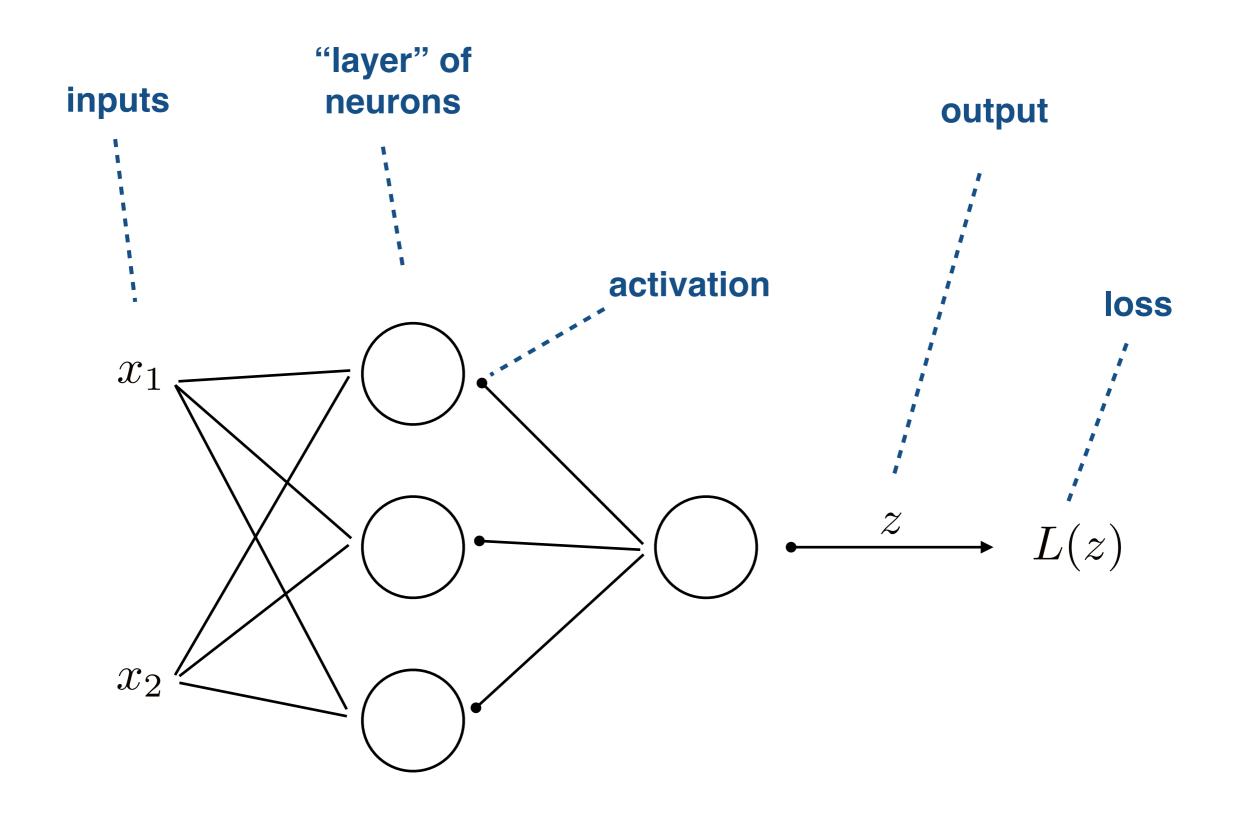
G. Díaz, J.A. Hernando, M. Kekic, J. Renner IFGAE / Universidade de Santiago de Compostela

Advanced Computing and Machine Learning

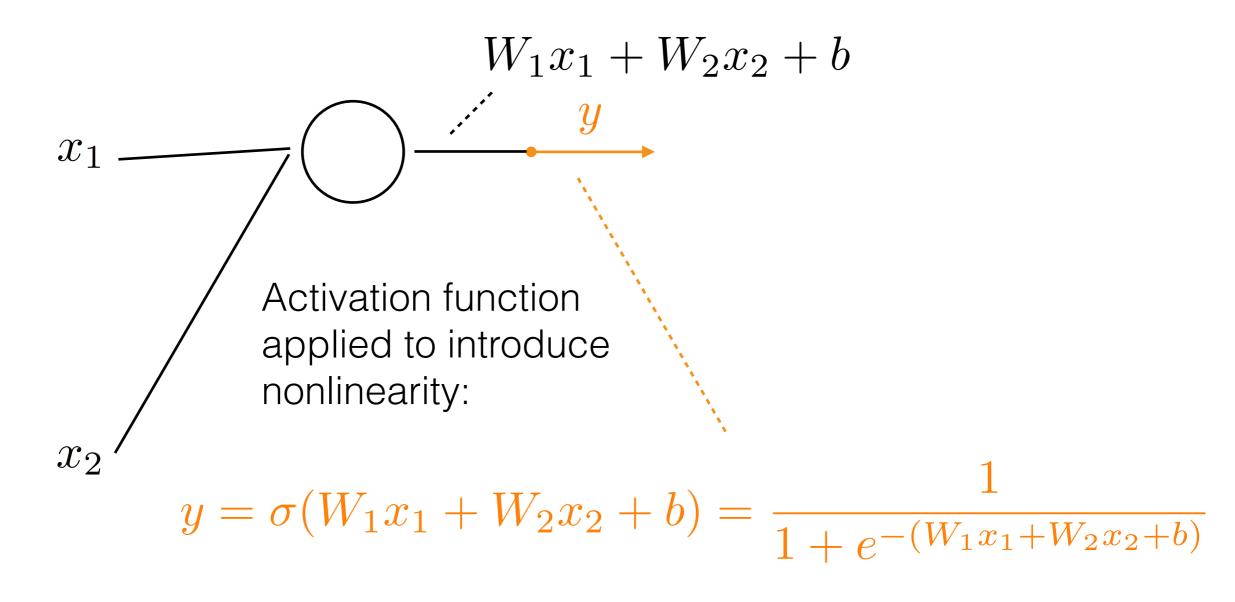
June 1, 2020

#### Review: last week



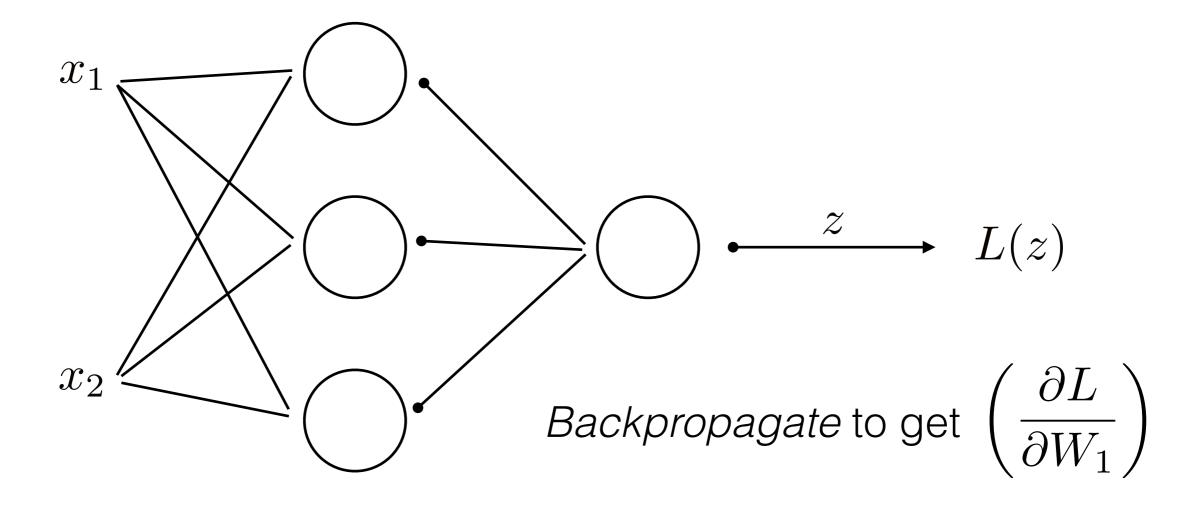


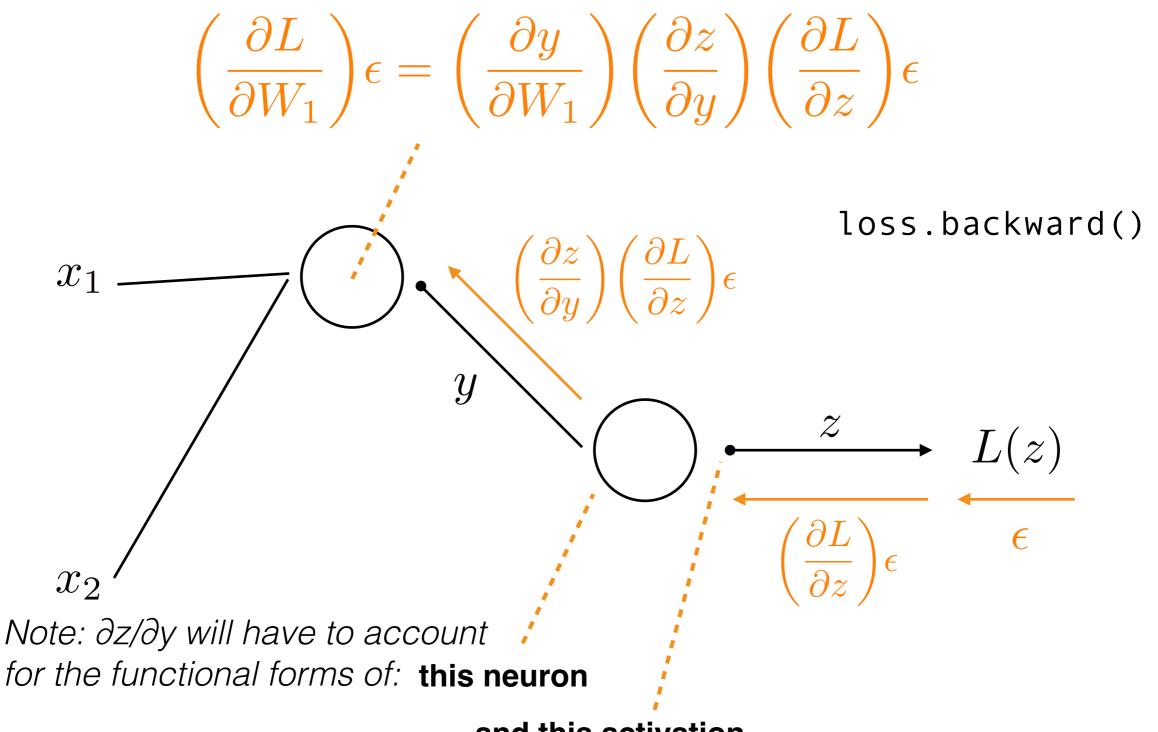
Each neuron contains a **weight** corresponding to each input, and a **bias**:



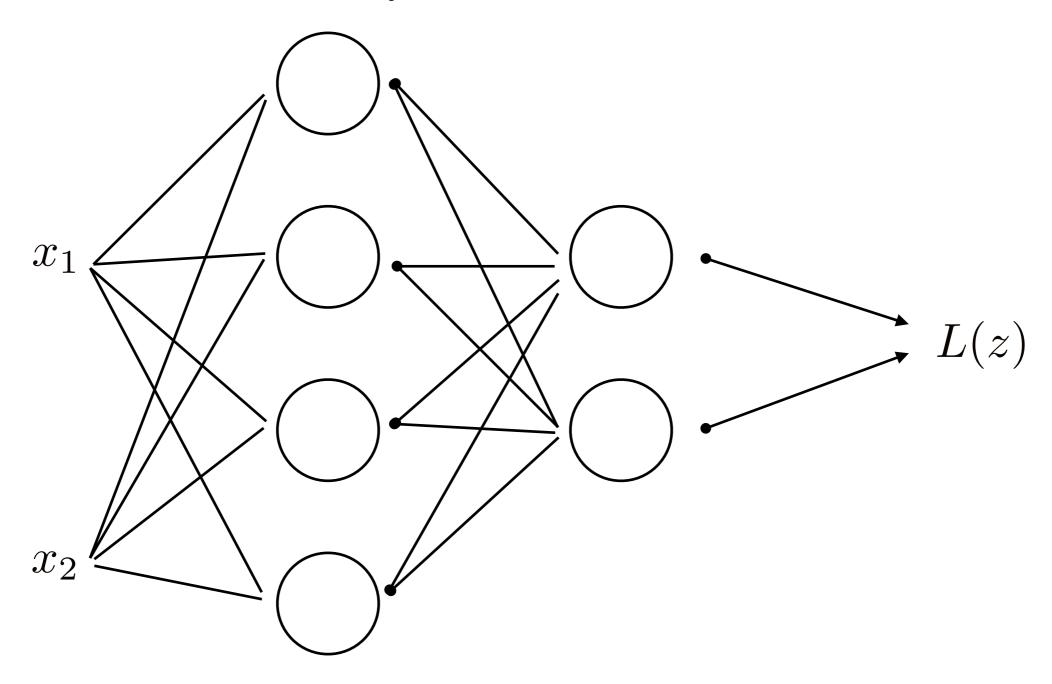
To minimize L, we want to push the entire network (all parameters) in the direction of -gradient(L):

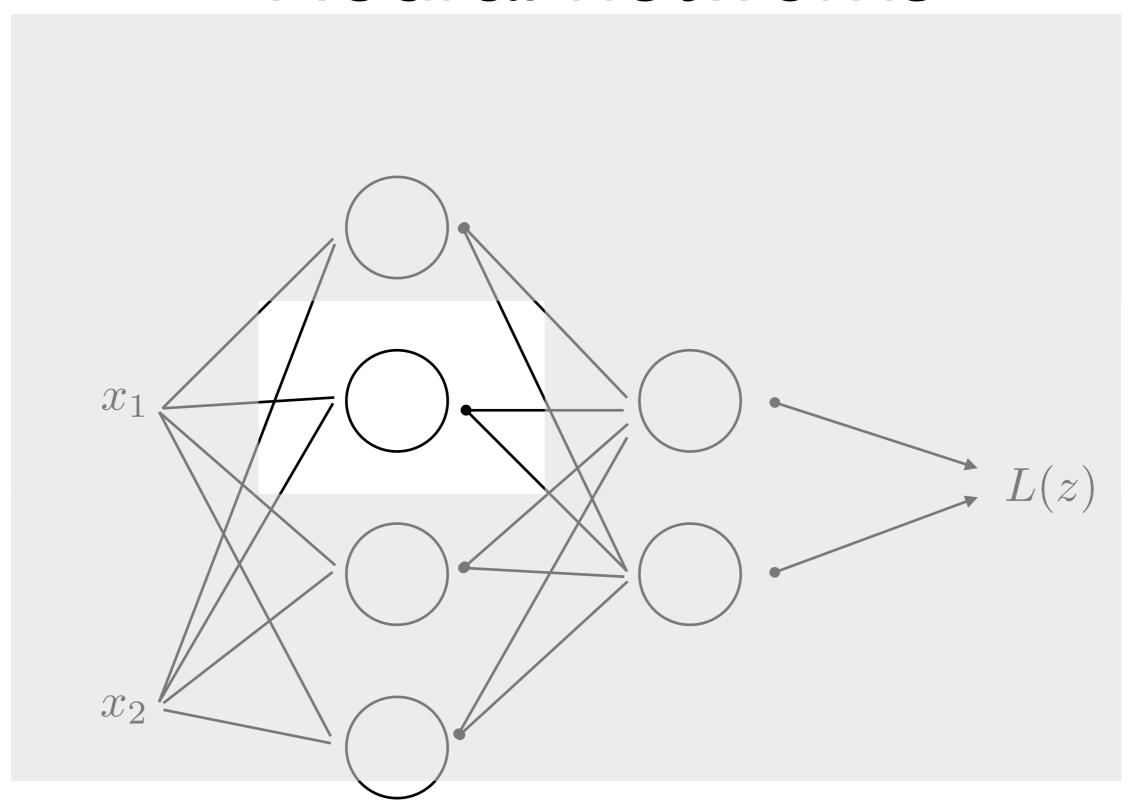
$$W_1 \to W_1 - \left(\frac{\partial L}{\partial W_1}\right) \epsilon$$

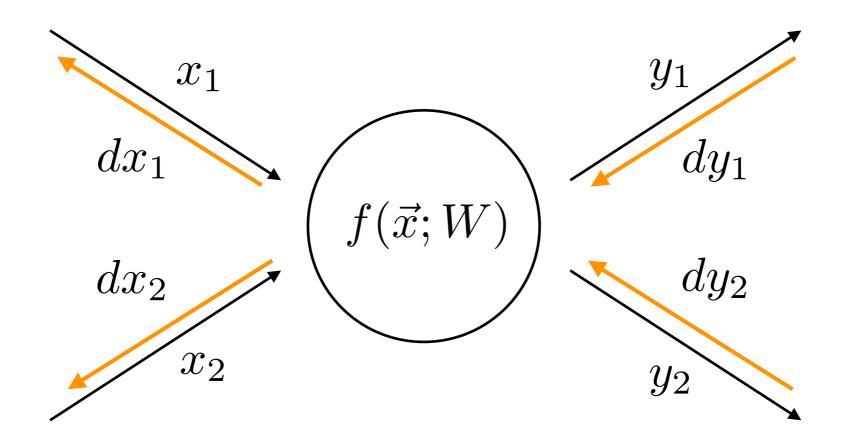




 Note that backpropagation on graphs can be performed on a node-by-node basis:



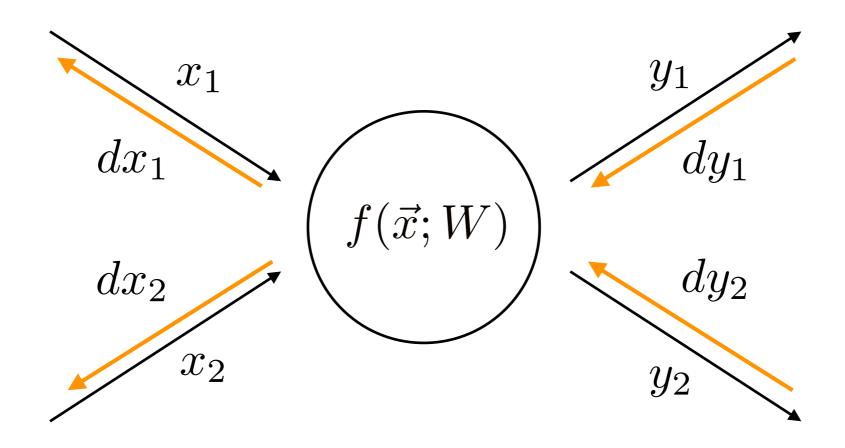




- Given gradients dy<sub>1</sub> and dy<sub>2</sub>
- Given f differentiable
- Compute gradients dW for parameter updates, and gradients dx<sub>1</sub> and dx<sub>2</sub> to continue backpropagation

$$dx_i = \sum_{k} \frac{\partial y_k}{\partial x_i} dy_k$$

Libraries such as PyTorch handle the mechanics of this automatically

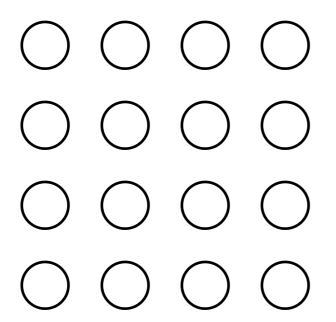


• So far, we've considered:

$$f(\vec{x}, W) = W\vec{x} + \vec{b}$$

Let's try something else!

Convolutional Neural Networks (CNNs)



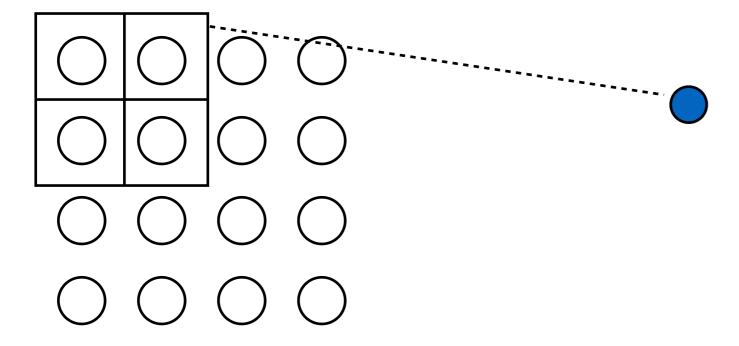
Inputs, arranged in a 2D matrix

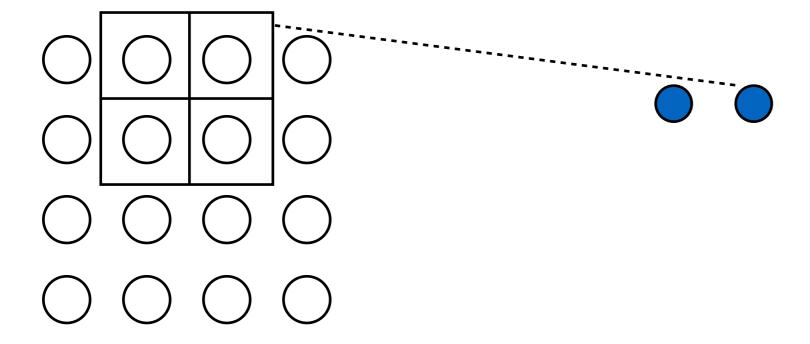
$W_{11}$	$W_{12}$
$W_{21}$	$W_{22}$

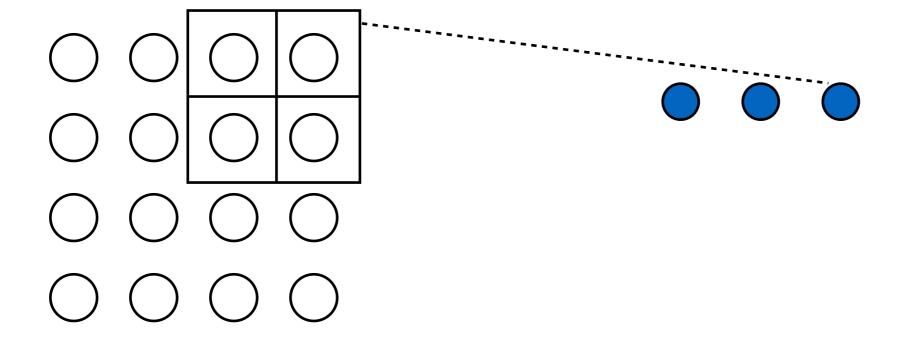
KxL kernel of weights (in this case 2x2)

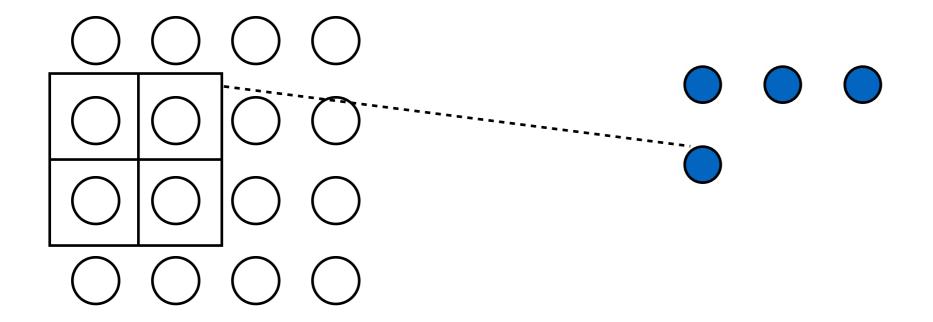
Multiply and add:

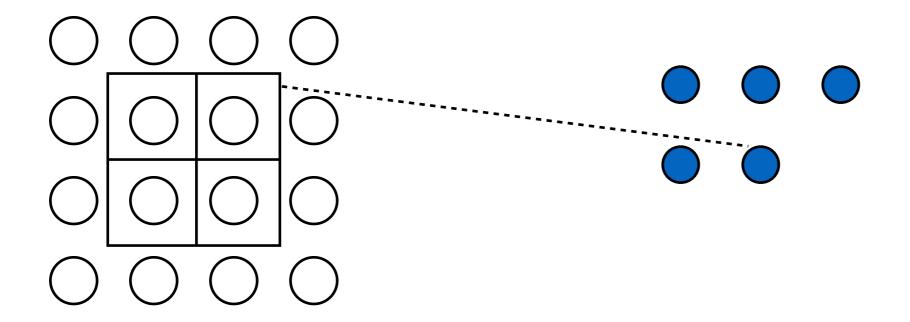
$$z_{11} = W_{11}x_{11} + W_{12}x_{12} + W_{21}x_{21} + W_{22}x_{22}$$

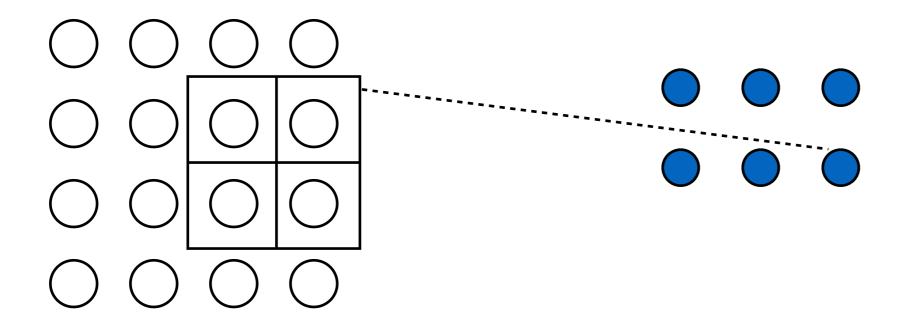


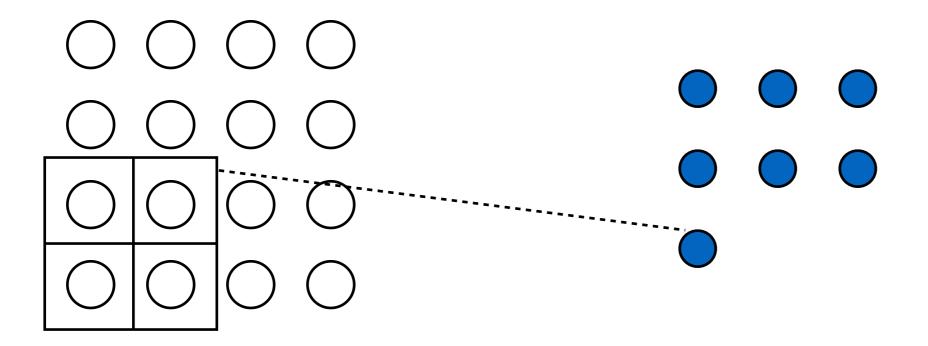


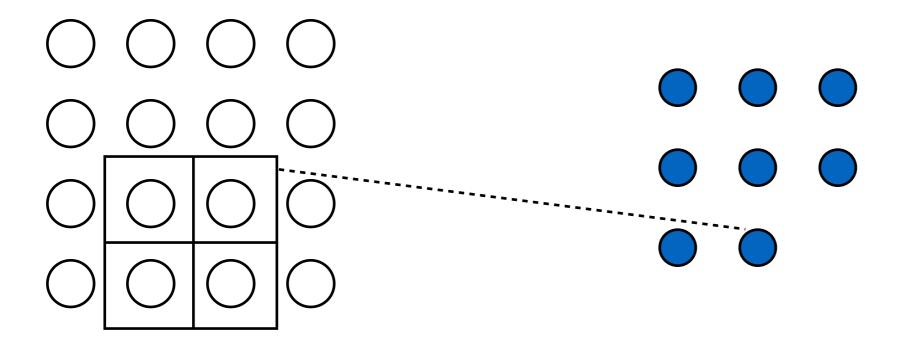


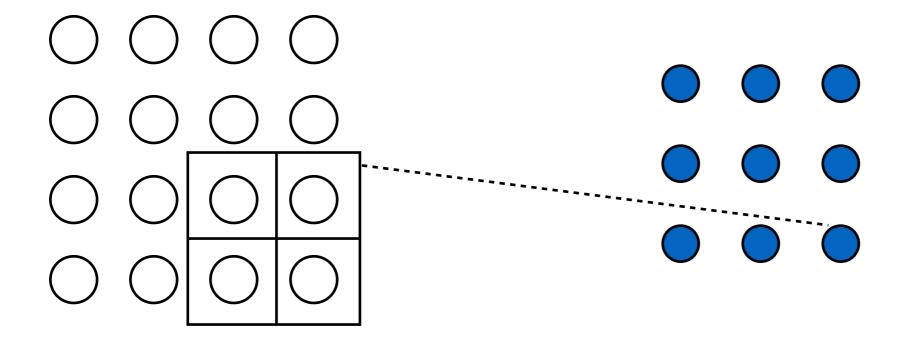


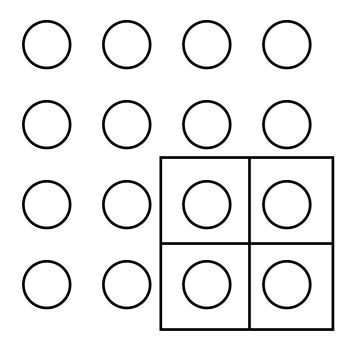




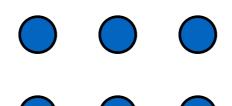




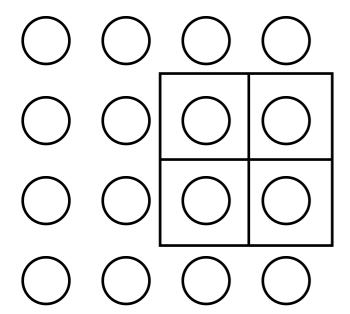


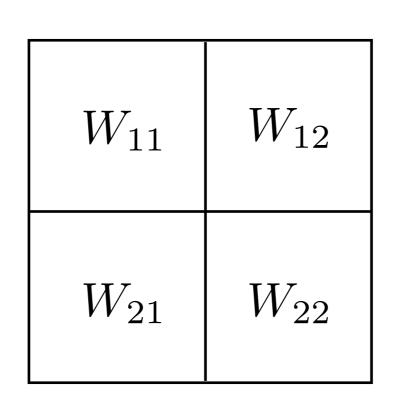


"feature map"





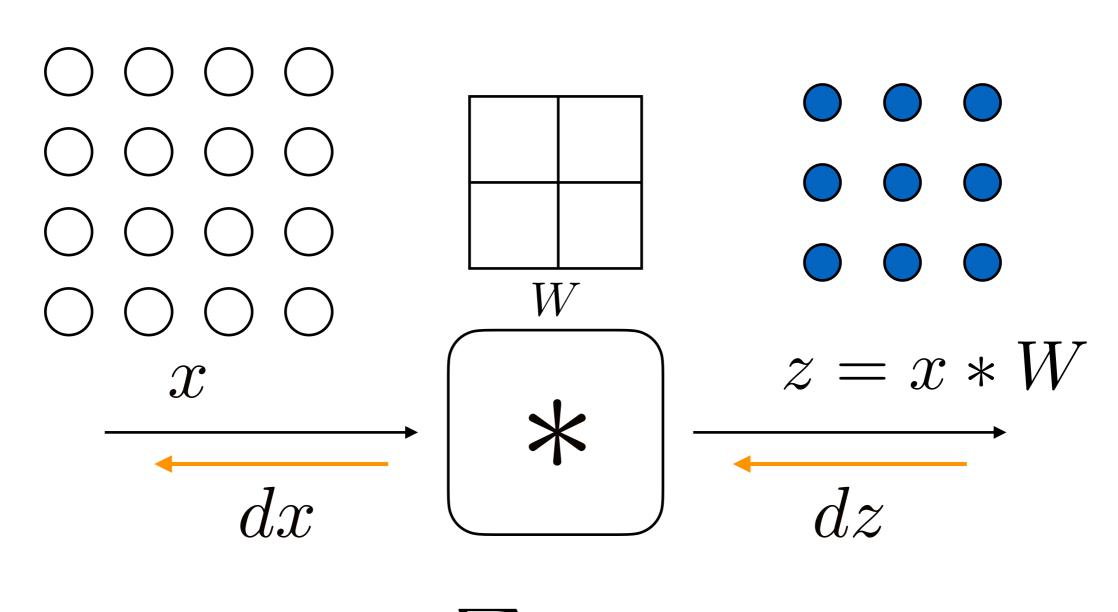




#### Note that we used the same weight matrix for the entire operation:

The idea that nearby input values are related is **built-in** to CNNs via "weight tying".

How do you "take the derivative" of that?



$$z_{ij} = \sum_{kl} W_{kl} x_{i+k,j+l}$$

$$z_{ij} = \sum_{kl} W_{kl} x_{i+k,j+l}$$

Note:  $\frac{\partial W_{ij}}{\partial W_{mn}} = \delta_{im}\delta_{jn}$ 

(weights are independent variables)

Let's find the values used to update weights W<sub>ij</sub>:

$$dW_{mn} = \left(\frac{\partial L}{\partial W_{mn}}\right) \epsilon = \sum_{ij} dz_{ij} \frac{\partial z_{ij}}{\partial W_{nm}}$$

$$= \sum_{ij} dz_{ij} \frac{\partial W_{kl}}{\partial W_{nm}} x_{i+k,j+l}$$

$$= \sum_{ij} dz_{ij} \delta_{kn} \delta_{lm} x_{i+k,j+l}$$

$$= \sum_{ij} dz_{ij} x_{i+n,j+m}$$

$$= \sum_{ij} dz_{ij} x_{n+i,m+j} = (x * dz)_{nm}$$

$$z_{ij} = \sum_{kl} W_{kl} x_{i+k,j+l}$$

Let's find the values used to update weights Wij:

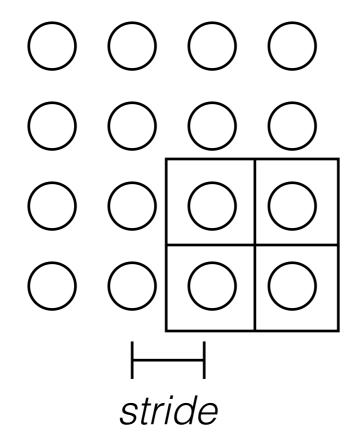
$$dW_{mn} = \left(\frac{\partial L}{\partial W_{mn}}\right) \epsilon = \sum_{ij} dz_{ij} \frac{\partial z_{ij}}{\partial W_{nm}}$$
$$= \sum_{ij} dz_{ij} \frac{\partial W_{kl}}{\partial W_{nm}} x_{i+k,j+l}$$

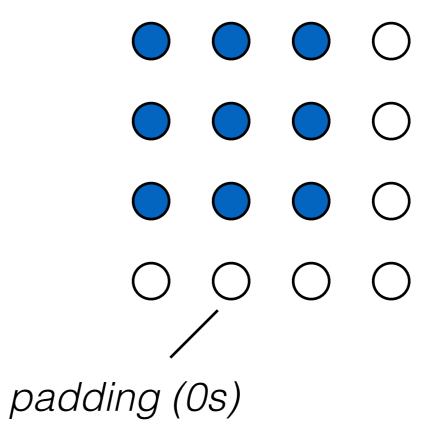
The gradients for the weights in a convolution  $=\sum_{i}dz_{ij}\delta_{kn}\delta_{lm}x_{i+k,j+l}$ can be found by convolving the output  $=\sum_{i}dz_{ij}x_{i+n,j+m}$ gradients with the input.

$$egin{aligned} &= \sum_{ij} dz_{ij} \delta_{kn} \delta_{lm} x_{i+k,j} \ &= \sum_{ij} dz_{ij} x_{i+n,j+m} \ &= \sum_{ij} dz_{ij} x_{i+n,j+m} \end{aligned}$$

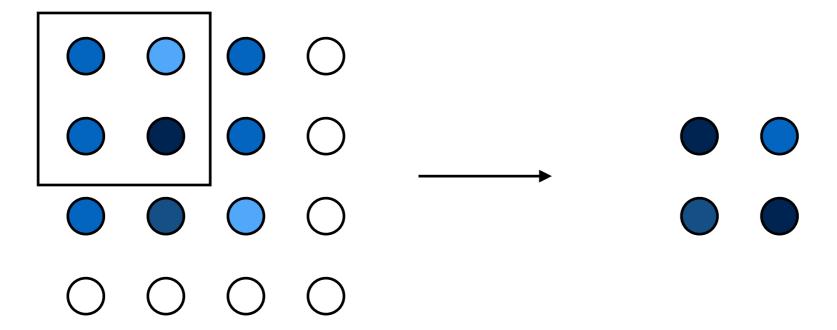
$$= \sum_{i,j} dz_{ij} x_{n+i,m+j} = (x * dz)_{nm}$$

Some additional terminology:

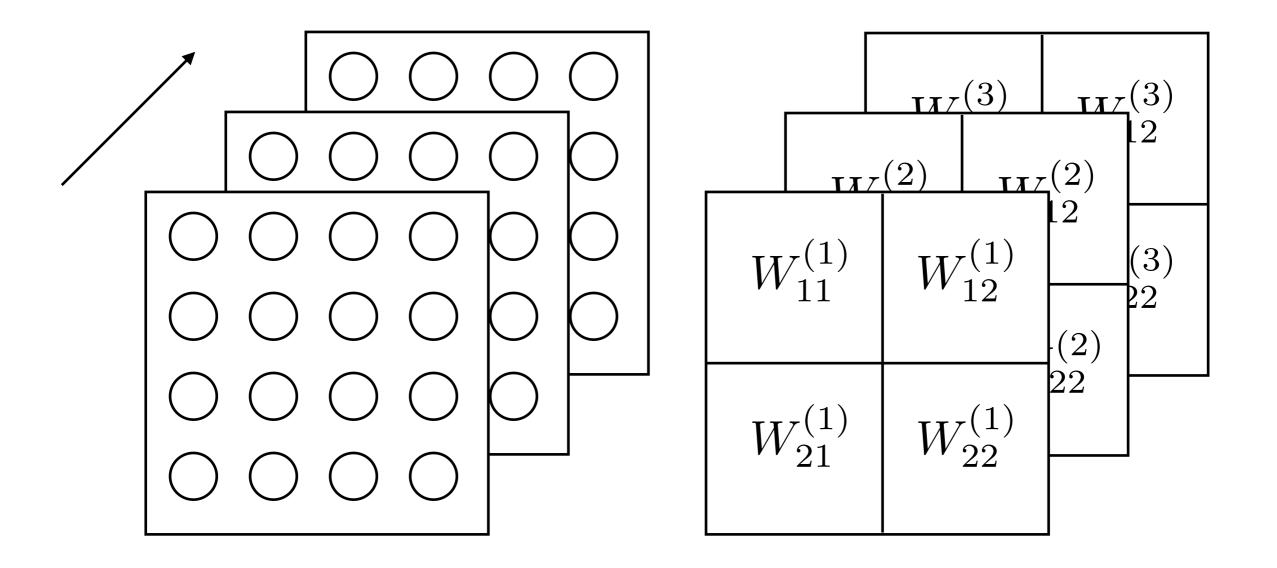




(max/average) pooling



Selects only the maximum value, or averages all values over a KxL interval



Inputs and kernels can also have multiple *channels* (for example, 3 channels in an RGB image)

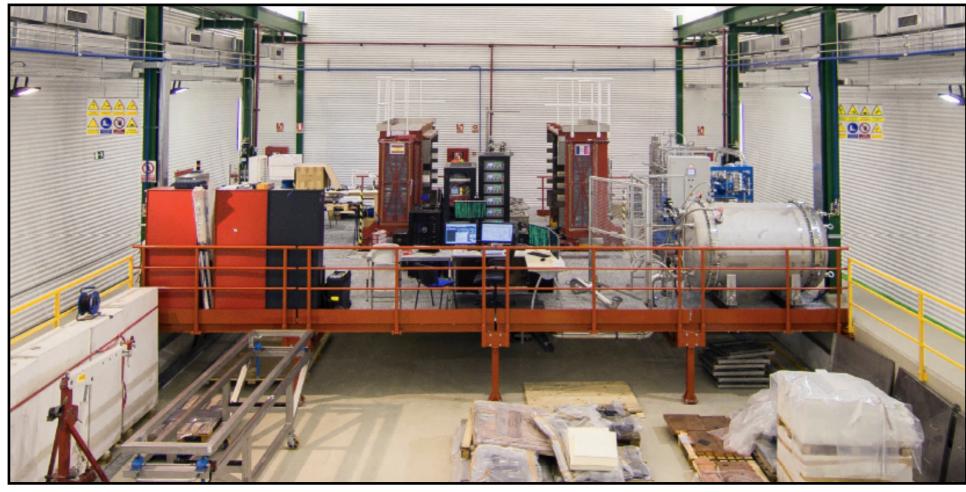
# NEXT

#### **N**eutrino

#### Experiment with a

Xenon TPC





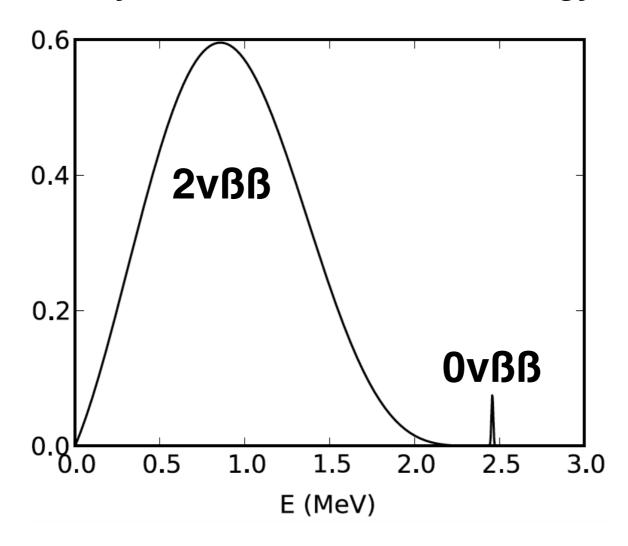
**NEXT at Canfranc** 

- search for neutrinoless double-beta decay (0vßß)
- to be commissioned in 2020: 100 kg Xe, enriched to <sup>136</sup>Xe (90%)
- high pressure gas, electroluminescent TPC: capable of measuring energy of an interaction and reconstructing particle tracks

32

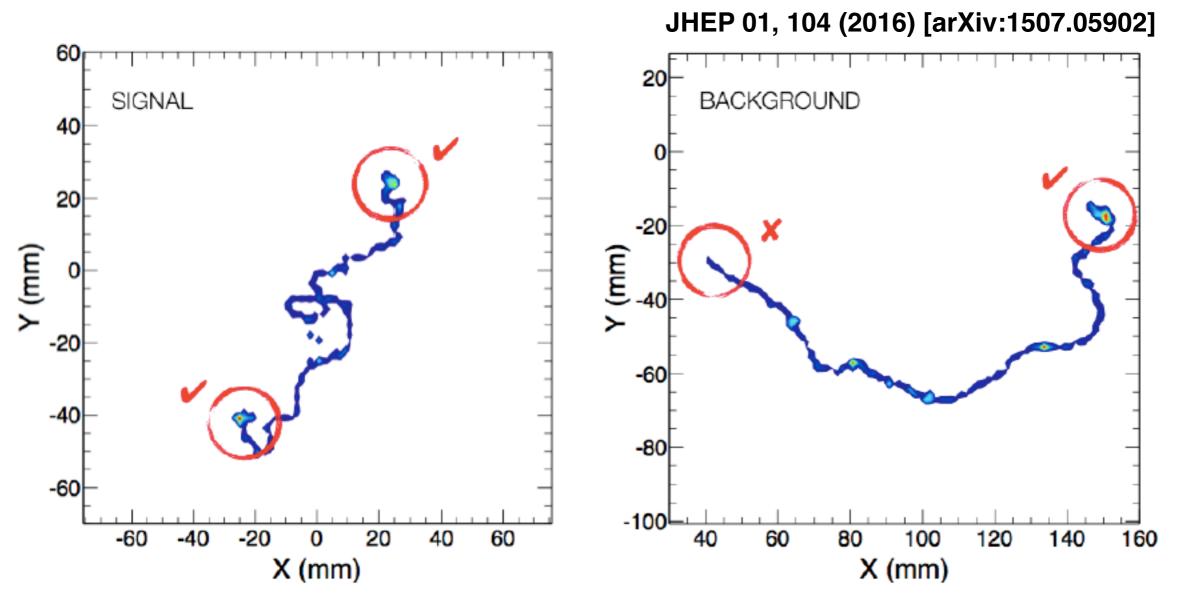
## What are we looking for?

**OvBB** would yield 2 electrons of total energy =  $Q_{BB}$ 



 But we could still get background events that are not 0v88 but still fall into the energy peak

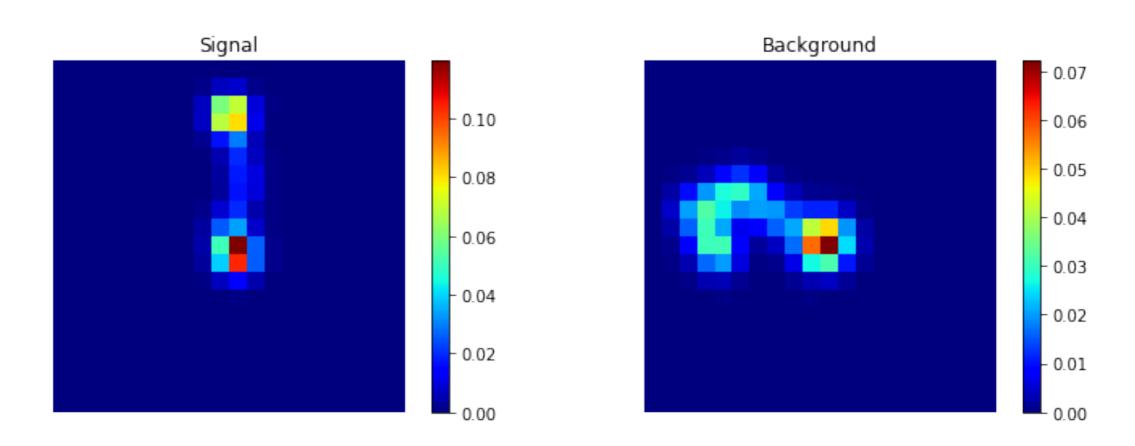
## Topological signature in NEXT



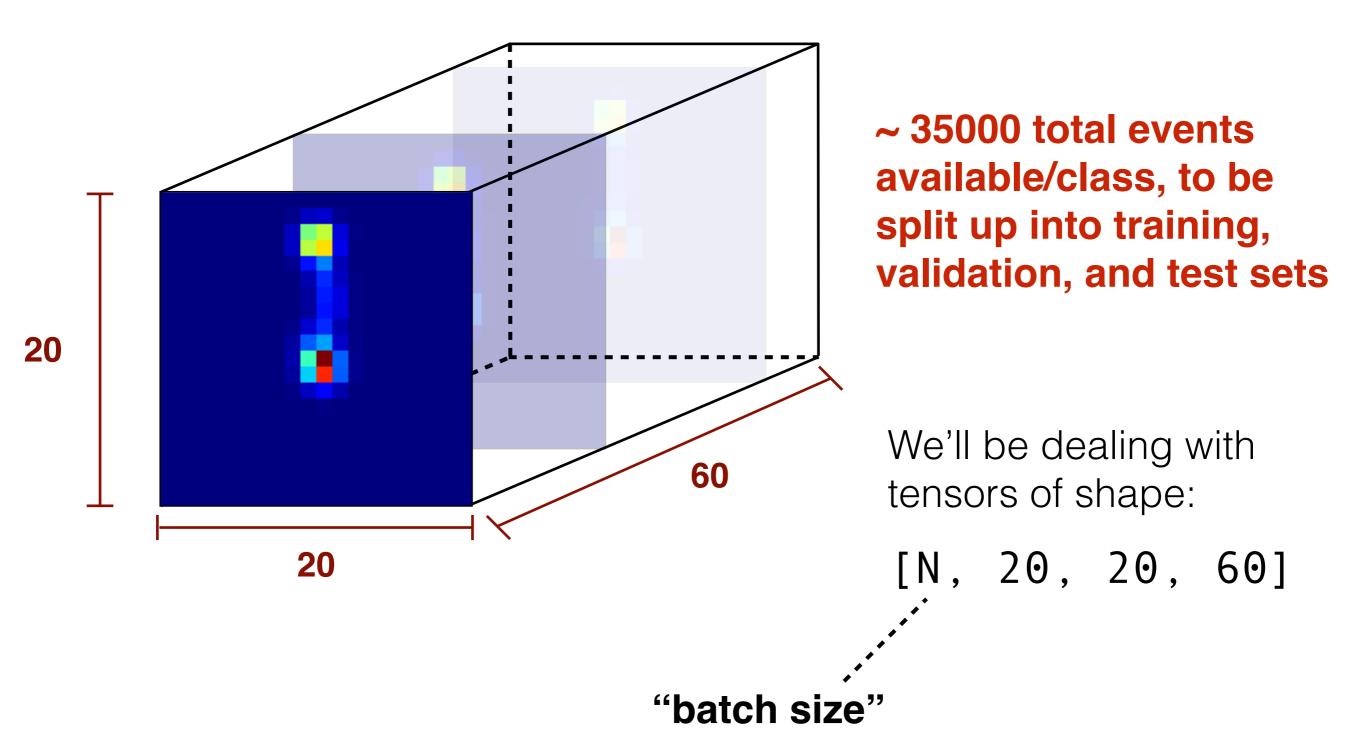
- Energetic electron leaves a high-density deposition at the end of its track (Bragg peak)
- Results in distinct topological signatures for signal and background events of the same energy

NEXT simulation dataset (20x20x60 particle tracks):

 Note these are actually e+e- pair events (similar topology and can be produced experimentally)



NEXT simulation dataset (20x20x60 particle tracks):



#### Note: Batches

Gradient descent steps are commonly performed with smaller subsets of the full training set called *minibatches* (or "batches").

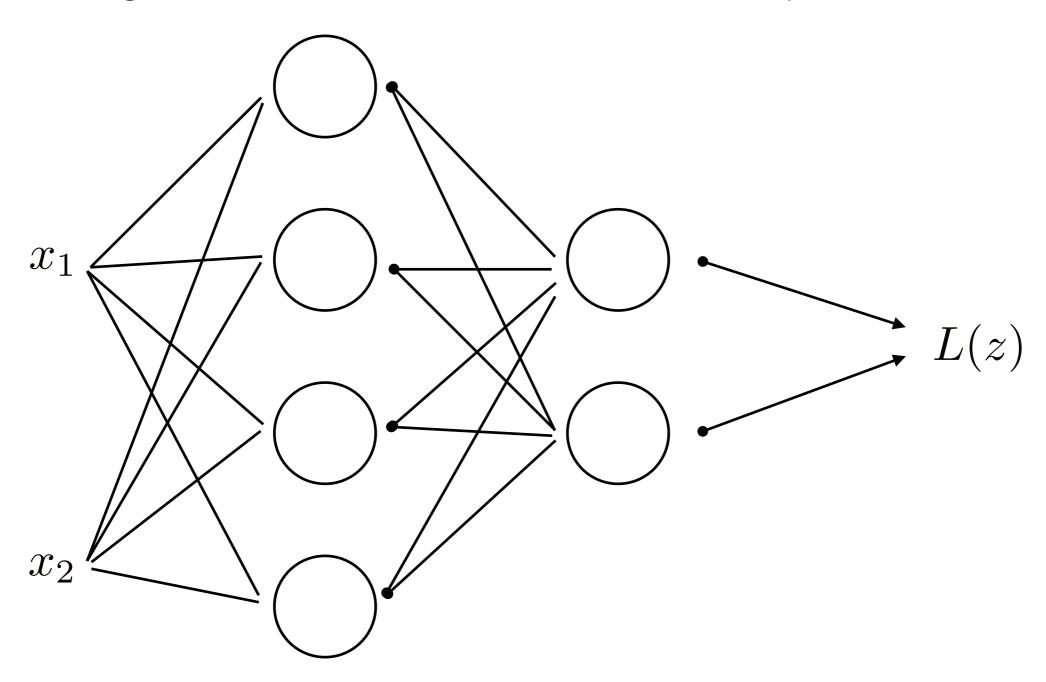
```
# Create a new Dataset
dataset train = NEXTDataset(datafile signal,
datafile background, nstart train, nend_train)
# Create a new DataLoader
train loader = DataLoader(dataset train,
batch_size=batch size, shuffle=True)
```

At each step, the loss and gradients will be computed using batch size data samples:

```
for batch idx, (data, target) in enumerate(train loader):
 optimizer.zero grad()
 outputs = model(data)
 loss = criterion(outputs, target)
 loss.backward()
 optimizer.step()
```

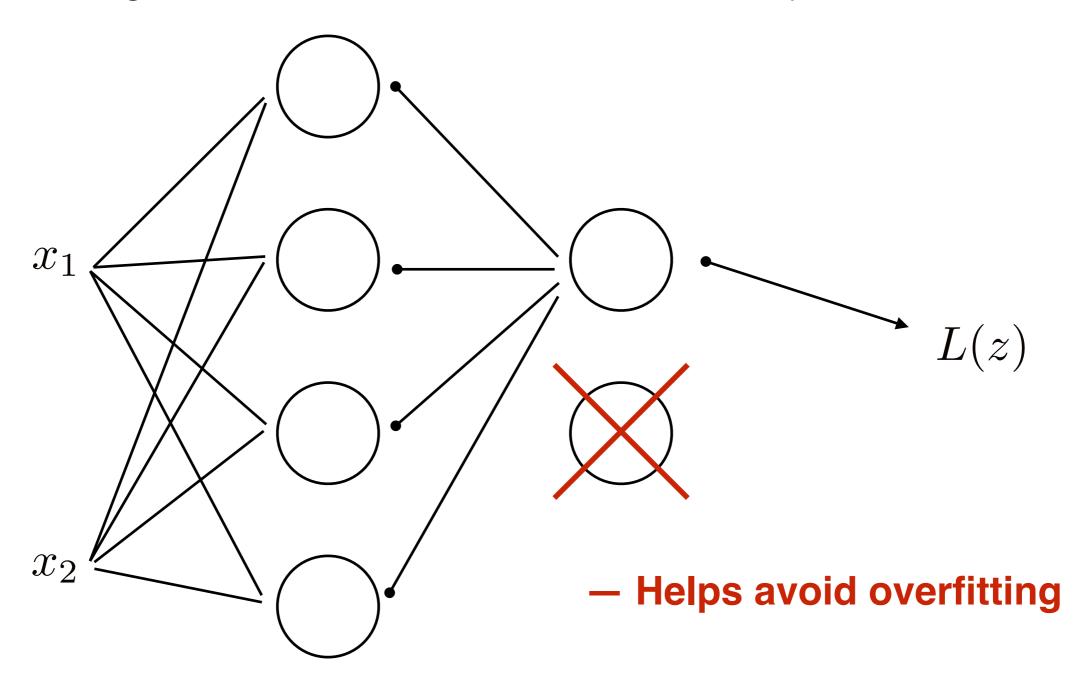
## Note: Dropout

During training/backpropagation, some specified probability of removing all connections to a neuron for a step:



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Some relevant layers/commands (see also <a href="https://pytorch.org/docs/stable/nn.html">https://pytorch.org/docs/stable/nn.html</a>):

```
# Create a new linear (Wx + b) layer
nn.Linear(in_features, out_features)
# Create a new 2D convolutional layer
torch.nn.Conv2d(C in, C out, kernel size, stride, padding)
# Create a new 2D max pooling layer
torch.nn.MaxPool2d(kernel size, stride)
# Dropout layer with the specified probability
torch.nn.Dropout(prob)
# Apply the sigmoid function
torch.sigmoid(x)
# Apply the ReLU function
torch.relu(x)
# Flatten a tensor (starting after the batch dimension)
torch.flatten(x, start dim=1)
```

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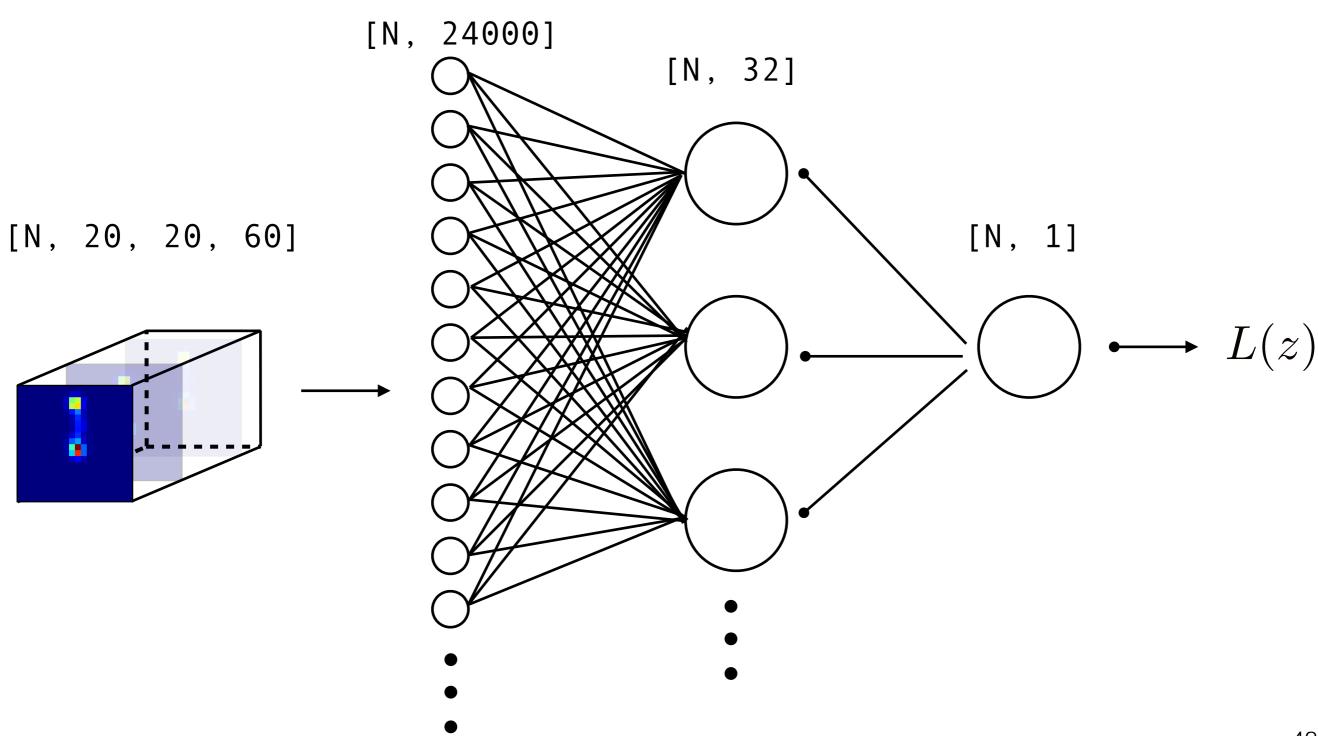
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torch.nn.MaxPool2d(kernel size, stride)
# Dropout layer with the specified probability
                                                ReLU (rectified linear
torch.nn.Dropout(prob)
                                                units) is another common
                                                activation used in CNNs
# Apply the sigmoid function
torch.sigmoid(x)
                                                relu(x) = max(0,x)
# Apply the ReLU function
torch.relu(x)
# Flatten a tensor (starting after the batch dimension)
torch.flatten(x, start dim=1)
```

An example net (not a CNN):

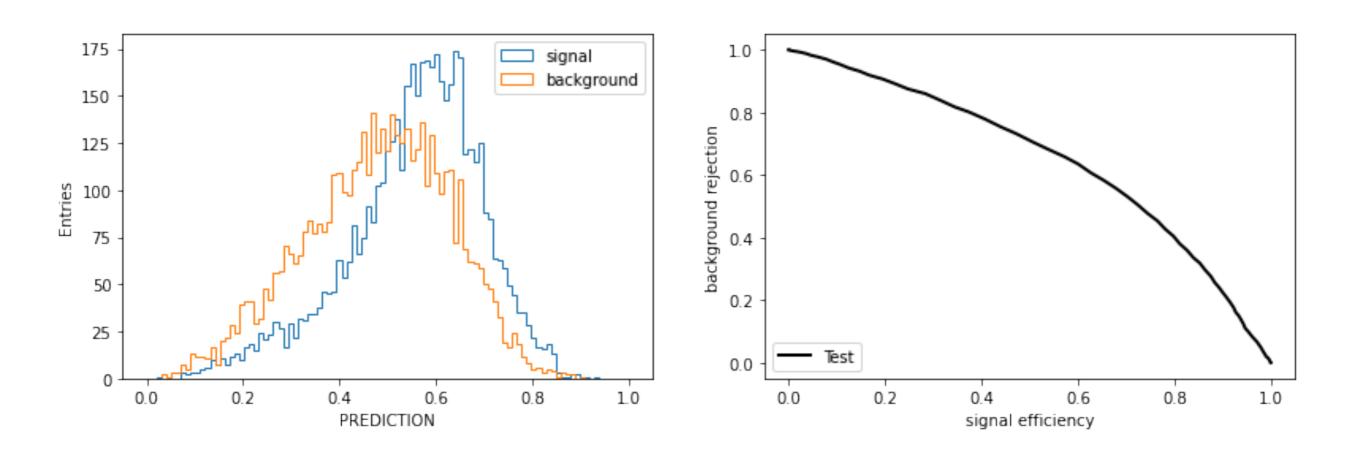
```
class FCNet(nn.Module):
    def __init__(self):
        super(FCNet, self).__init__()
        self.fc1 = nn.Linear(xdim*ydim*zdim, 32)
        self.fc2 = nn.Linear(32, 1)

def forward(self, x):
        x = torch.flatten(x, start_dim=1)
        x = self.fc1(x)
        x = torch.sigmoid(x)
        x = self.fc2(x)
        return x
```

An example net (not convolutional):



Performance: can this be improved with a CNN?



https://colab.research.google.com/github/jerenner/uscnncourse/blob/master/next/NEXT\_classification.ipynb

## EXTRA SLIDES

Backpropagation on a graph is essentially the chain rule:

$$\frac{\partial L}{\partial W_i} = \sum_j \frac{\partial L}{\partial z_j} \sum_k \frac{\partial z_j}{\partial y_k} \frac{\partial y_k}{\partial W_i} = \sum_{j,k} \frac{\partial L}{\partial z_j} \frac{\partial z_j}{\partial y_k} \frac{\partial y_k}{\partial W_i} = \sum_{j,k} \frac{\partial y_k}{\partial W_i} \frac{\partial z_j}{\partial y_k} \frac{\partial L}{\partial z_j}$$

$$= \sum_{j,k} \frac{\partial y_k}{\partial W_i} \left[ \frac{\partial z_j}{\partial y_k} \left( \frac{\partial L}{\partial z_j} \right) \right] = \sum_k \frac{\partial y_k}{\partial W_i} \sum_j \left[ \frac{\partial z_j}{\partial y_k} dz_j \right], \text{ where } dz_j = \frac{\partial L}{\partial z_j}$$

$$=\sum_{k} \frac{\partial y_{k}}{\partial W_{i}} dy_{k}$$
, where  $dy_{k} = \sum_{j} \left[ \frac{\partial z_{j}}{\partial y_{k}} dz_{j} \right]$