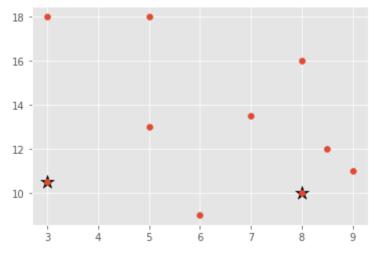
```
1
   import numpy as np
2
   from matplotlib import pyplot as plt
3
   plt.rcParams['figure.figsize'] = (12, 6)
4
   plt.style.use('ggplot')
5
   np.linalg.norm(np.array([8,10]) - np.array([3,10.5]))
   5.024937810560445
1
   np.sqrt((8-3)**2+(10-10.5)**2)
   5.024937810560445
1
   data = np.array([[8,10],[3,10.5],[7,13.5],[5,18],[5,13],[6,9],[9,11],[3,18],[8.5,
2
   C = np.array([[8,10],[3,10.5]])
3
4
   # Gráfica
5
   fig = plt.figure()
   plt.scatter(C[0][0], C[0][1], marker='*', s=200, c='#050505')
6
   plt.scatter(C[1][0], C[1][1], marker='*', s=200, c='#050505')
7
   plt.scatter(data[:, 0], data[:, 1])
8
9
```

## <matplotlib.collections.PathCollection at 0x7f2f39789dd0>



```
1 distances = []
 2 clusters = np.zeros(len(data))
 3
 4 \text{ def dist(a, b, ax=1)}:
 5
    return np.linalg.norm(a - b, axis=ax)
 6
 7 for i in range(len(data)):
 8
    distance = dist(data[i], C)
 9
    distances.append(distance)
10
   cluster = np.argmin(distance)
11
   clusters[i] = cluster
```

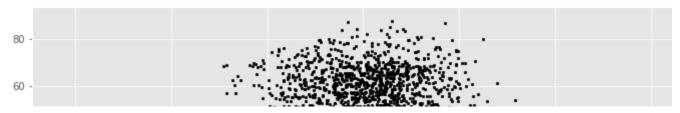
```
12
13 print(clusters)
14 distances
15
    [0. 1. 0. 1. 1. 0. 0. 1. 0. 0.]
               , 5.02493781]),
    [array([0.
     array([5.02493781, 0.
                                 1),
     array([3.64005494, 5.
                                  ]),
     array([8.54400375, 7.76208735]),
     array([4.24264069, 3.20156212]),
     array([2.23606798, 3.35410197]),
     array([1.41421356, 6.02079729]),
     array([9.43398113, 7.5
     array([2.06155281, 5.70087713]),
     array([6. , 7.43303437])]
 1 for i in range(len(C)):
 points = [data[j] for j in range(len(data)) if clusters[j] == i]
   C[i] = np.mean(points, axis=0)
 3
 5 print(C)
    [[ 7.75
                 11.91666667
    [ 4.
                  14.875 ]]
 1 # Gráfica
 2 fig = plt.figure()
 3 plt.scatter(C[0][0], C[0][1], marker='*', s=200, c='#050505')
 4 plt.scatter(C[1][0], C[1][1], marker='*', s=200, c='#050505')
 5 plt.scatter(data[:, 0], data[:, 1])
 6
```

<matplotlib.collections.PathCollection at 0x7f2f39707a10>
18 -

```
5 ' ' '
6 import numpy as np
7 import pandas as pd
8 from matplotlib import pyplot as plt
9 plt.rcParams['figure.figsize'] = (12, 6)
10 plt.style.use('ggplot')
1 # Conjunto de datos xclara
2 data = pd.read_csv('http://dicyg.fi-c.unam.mx:8080/lalo/pypcd/presentaciones/xcla
3 print(data.shape)
4 data.head()
    (3000, 2)
             V1
                        V2
        2.072345 -3.241693
     1 17.936710 15.784810
       1.083576 7.319176
     3 11.120670 14.406780
     4 23.711550 2.557729
1 # Gráfica
2 f1 = data['V1'].values
3 f2 = data['V2'].values
```

```
<matplotlib.collections.PathCollection at 0x7f2f321e9610>
```

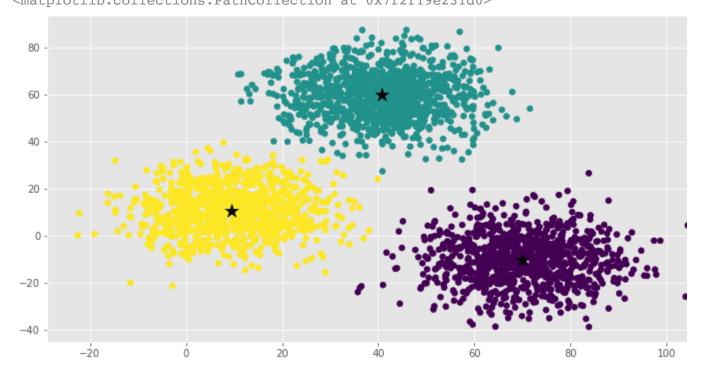
4 X = np.array(list(zip(f1, f2)))
5 plt.scatter(f1, f2, c='black', s=7)



```
1
2 from sklearn.cluster import KMeans
3
4 # Número de grupos
5 kmeans = KMeans(n_clusters=3)
6 # Ajuste
7 kmeans = kmeans.fit(X)
8 # Etiquetas de cada clase
9 y = kmeans.predict(X)
10 # Centroides
11 C_skl = kmeans.cluster_centers_
1 fig, ax = plt.subplots()
```

3 ax.scatter(C\_skl[:, 0], C\_skl[:, 1], marker='\*', s=200, c='#050505')

```
<matplotlib.collections.PathCollection at 0x7f2f19e231d0>
```

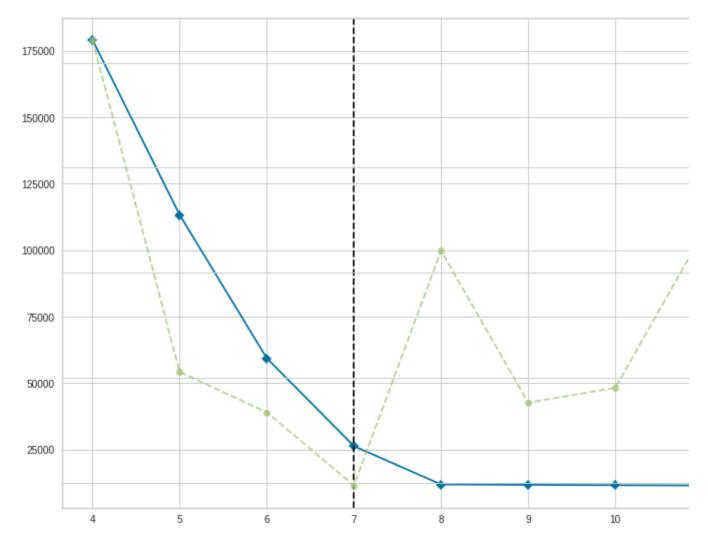


1 # ¿Cómo saber el valor inicial para K?

2 ax.scatter(X[:, 0], X[:, 1], c=y)

```
1 # Elección de k con la gráfica de codo KElbowVisualizer
2 # https://www.scikit-yb.org/en/latest/api/cluster/elbow.html
3 # By default, the scoring parameter metric is set to distortion,
4 # which computes the sum of squared distances from each point to its assigned cen
5 from sklearn.cluster import KMeans
6 from sklearn.datasets import make_blobs
7 from yellowbrick.cluster import KElbowVisualizer
8
9 X, y = make blobs(n samples=1000, n features=12, centers=8, random state=42)
```

```
10
11 visualizer = KElbowVisualizer(KMeans(), k=(4,12), timings=True)
12 visualizer.fit(X)
13 plt.xlabel('Número de grupos')
14 plt.ylabel('Distorsión')
15 plt.show()
```



1 # KMeans in depth

2 # https://github.com/jakevdp/PythonDataScienceHandbook/blob/master/notebooks/05.1

- 1 # bibliotecas
- 2 import pandas as pd
- 3 import numpy as np
- 4 import matplotlib.pyplot as plt
- 1 # datos
- 2 #https://archive.ics.uci.edu/ml/machine-learning-databases/00292/Wholesale%20cust
- 3 url = 'https://bit.ly/2COHM14'
- 4 data = pd.read\_csv(url)
- 5 data.head()

6

	Channel	Region	Fresh	Milk	Grocery	Frozen	Detergents_Paper	Delicassen
0	2	3	12669	9656	7561	214	2674	1338
1	2	3	7057	9810	9568	1762	3293	1776
2	2	3	6353	8808	7684	2405	3516	7844
3	1	3	13265	1196	4221	6404	507	1788
4	2	3	22615	5410	7198	3915	1777	5185

- 1 from sklearn.preprocessing import normalize
- 2 data scaled = normalize(data)
- 3 data\_scaled = pd.DataFrame(data\_scaled, columns=data.columns)
- 4 data\_scaled.head()

	Channel	Region	Fresh	Milk	Grocery	Frozen	Detergents_Paper	Delicas
0	0.000112	0.000168	0.708333	0.539874	0.422741	0.011965	0.149505	0.074
1	0.000125	0.000188	0.442198	0.614704	0.599540	0.110409	0.206342	0.111
2	0.000125	0.000187	0.396552	0.549792	0.479632	0.150119	0.219467	0.489
3	0.000065	0.000194	0.856837	0.077254	0.272650	0.413659	0.032749	0.115
4	0.000079	0.000119	0.895416	0.214203	0.284997	0.155010	0.070358	0.205

- 1 import scipy.cluster.hierarchy as shc
- 2 plt.figure(figsize=(10, 7))
- 3 plt.title("Dendrograma")
- 4 dend = shc.dendrogram(shc.linkage(data scaled, method='ward'))

## Dendrograma

```
plt.figure(figsize=(10, 7))
plt.title("Dendrograma")
dend = shc.dendrogram(shc.linkage(data_scaled, method='ward'))
plt.axhline(y=6, color='r', linestyle='--')
```

<matplotlib.lines.Line2D at 0x7f4513572c90>

12

## Dendrograma

1 from sklearn.cluster import AgglomerativeClustering

2 cluster = AgglomerativeClustering(n clusters=2, affinity='euclidean',

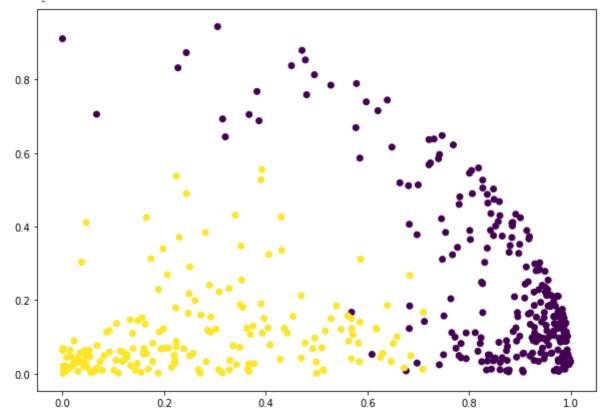
```
linkage='ward')
4 cluster.fit predict(data scaled)
   array([1, 1, 1, 0, 0, 1, 0, 1, 1, 1, 1, 0, 0, 0, 0, 0, 1, 1, 0, 0, 0, 0,
          0, 1, 0, 0, 0, 0, 1, 0, 0, 1, 0, 0, 1, 1, 0, 1, 1, 0, 0, 0, 1, 1,
          1, 1, 1, 1, 1, 1, 0, 1, 0, 1, 0, 1, 1, 1, 0, 1, 0, 1, 1, 1, 0, 1,
          1, 0, 1, 0, 0, 0, 0, 0, 1, 0, 0, 1, 0, 1, 0, 1, 1, 0, 0, 1, 1, 0,
          0, 0, 0, 0, 1, 0, 1, 1, 1, 0, 0, 0, 1, 1, 1, 0, 0, 0, 1, 1, 1, 1,
          0, 1, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0,
          0, 0, 0, 0, 1, 1, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 1, 0, 1,
          0, 1, 1, 0, 1, 1, 1, 0, 0, 1, 1, 1, 1, 1, 0, 0, 1, 1, 1, 1, 1, 1,
          0, 0, 0, 1, 0, 0, 1, 1, 1, 0, 0, 1, 1, 1, 0, 0, 0, 1, 0, 0, 0, 1,
          0, 0, 1, 1, 0, 1, 1, 1, 0, 1, 1, 1, 0, 1, 0, 1, 1, 1, 1, 1, 0, 1, 0,
          0, 1, 0, 0, 0, 0, 0, 1, 0, 0, 1, 0, 1, 0, 1, 0, 0, 0, 0, 0, 0,
          0, 0, 1, 1, 0, 0, 0, 0, 0, 1, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 1,
          1, 1, 1, 0, 1, 0, 0, 1, 1, 0, 1, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0,
          0, 0, 0, 0, 1, 0, 1, 1, 0, 0, 0, 0, 1, 1, 0, 1, 1, 1, 1, 1, 1, 0,
          0, 1, 0, 0, 1, 0, 0, 1, 0, 1, 0, 1, 1, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0,
          0, 1, 0, 1, 0, 0, 0, 0, 0, 1, 1, 1, 1, 0, 1, 1, 0, 1, 1, 0, 1,
          1, 1, 0, 1, 0, 1, 1, 1, 0, 0, 1, 0, 0, 1, 0, 0, 0, 0, 0, 0, 1, 0,
          0, 0, 1, 0, 1, 1, 0, 0, 0, 0, 1, 0, 1, 0, 0, 0, 0, 1, 1, 0, 0, 0,
          1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 1, 1, 0, 0, 1, 1, 1,
          1, 0, 1, 0, 0, 0, 0, 0, 1, 0, 1, 0, 1, 0, 0, 1, 0, 0, 0, 1, 0, 1])
1 plt.figure(figsize=(10, 7))
2 plt.scatter(data scaled['Milk'], data scaled['Grocery'], c=cluster.labels )
```

```
<matplotlib.collections.PathCollection at 0x7f451ba13550>
```

```
10
```

1 plt.figure(figsize=(10, 7))

<matplotlib.collections.PathCollection at 0x7f450bfe0410>



```
1 # Bibliotecas
```

- 2 import numpy as np
- 3 import matplotlib.pyplot as plt
- 4 import pandas as pd
- 1 # Dataset

 $\Box$ 

- 2 dataset = pd.read\_csv('http://dicyg.fi-c.unam.mx:8080/lalo/pypcd/presentaciones/N
- X = dataset.iloc[:, [3, 4]].values
- 4 dataset.head()

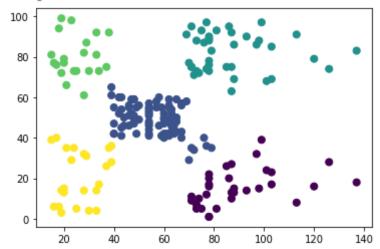
→		CustomerID	Genre	Age	Annual Income (k\$)	Spending Score (1-100)
	0	1	Male	19	15	39
	1	2	Male	21	15	81
	2	3	Female	20	16	6
	3	4	Female	23	16	77
	4	5	Female	31	17	40

- 1 # Dendrograma para determinar el número óptimo de grupos
- 2 import scipy.cluster.hierarchy as sch
- 3 dendrograma = sch.dendrogram(sch.linkage(X, method = 'ward'))
- 4 plt.title('Dendrograma')
- 5 plt.xlabel('Clientes')
- 6 plt.ylabel('Distancia euclideana')
- 7 plt.show()

```
Dendrograma
400 -
```

1 plt.scatter(X[:,0],X[:,1],s=50,c=y\_hc)

<matplotlib.collections.PathCollection at 0x7fbb7d03dd50>

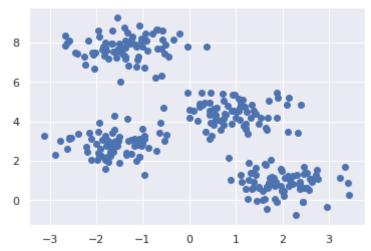


```
1 # Graficando los resultados
2 plt.scatter(X[y_hc == 0, 0], X[y_hc == 0, 1], s = 100, c = 'red', label = 'Grupo
3 plt.scatter(X[y_hc == 1, 0], X[y_hc == 1, 1], s = 100, c = 'blue', label = 'Grupo
4 plt.scatter(X[y_hc == 2, 0], X[y_hc == 2, 1], s = 100, c = 'green', label = 'Grupo
5 plt.scatter(X[y_hc == 3, 0], X[y_hc == 3, 1], s = 100, c = 'cyan', label = 'Grupo
6 plt.scatter(X[y_hc == 4, 0], X[y_hc == 4, 1], s = 100, c = 'magenta', label = 'Gr
7 plt.title('Grupos ')
8 plt.xlabel('Ingreso anual (k$)')
9 plt.ylabel('Nivel de gastos (1-100)')
10 plt.legend()
11 plt.show()
```

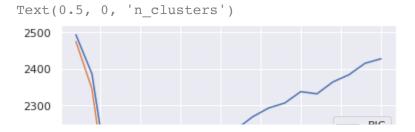


```
import numpy as np
1
  import matplotlib.pyplot as plt
2
3
  import seaborn as sns
  sns.set()
4
5
  from sklearn.mixture import GaussianMixture
  from sklearn.datasets import make blobs
6
                                  Code
   X, y = make blobs(n samples=300, centers=4, cluster std=0.6, random state=0)
1
   plt.scatter(X[:,0],X[:,1])
```

<matplotlib.collections.PathCollection at 0x7faf2360d890>



```
# The optimal number of clusters (K) is the value that minimizes the
1
   # Akaike information criterion (AIC) or the Bayesian information criterion (BIC)
2
   # https://en.wikipedia.org/wiki/Akaike information criterion
4
   # https://en.wikipedia.org/wiki/Bayesian information criterion
    n clusters = np.arange(1, 21)
5
    models = [GaussianMixture(n, covariance type='full',
6
7
                              random state=0).fit(X) for n in n clusters]
8
    plt.plot(n clusters, [m.bic(X) for m in models], label='BIC')
9
   plt.plot(n clusters, [m.aic(X) for m in models], label='AIC')
   plt.legend(loc='best')
10
    plt.xlabel('n clusters')
11
```



```
2200
2100
```

```
1 gmm = GaussianMixture(n_components=4)
```

2 gmm.fit(X)

GaussianMixture(n\_components=4)

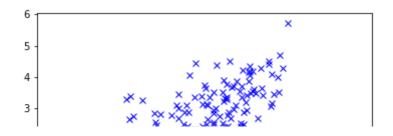
```
1 labels = gmm.predict(X)
2 plt.scatter(X[:, 0], X[:, 1], c=labels, cmap='viridis');
```



- 1 import numpy as np
- 2 import matplotlib.pyplot as plt
- 3 from sklearn.mixture import GaussianMixture

```
1 # https://bit.ly/3Bic3iu
2 X_train = np.load('data.npy')

1 plt.plot(X_train[:,0], X_train[:,1], 'bx')
2 plt.axis('equal')
3 plt.show()
```



```
2
    1
1 gmm = GaussianMixture(n_components=2)
2 gmm.fit(X_train)
4 print("Medias: \n", gmm.means_)
5 print('\n')
6 print("Covarianzas: \n",gmm.covariances_)
   Medias:
    [[3.04641134 3.10654272]
    [1.60718016 1.35251723]]
   Covarianzas:
    [[[ 0.83656079  0.37865596]
     [ 0.37865596  0.72727426]]
    [[ 0.74995307 -0.5010097 ]
     [-0.5010097 \quad 0.74377694]]]
1 X, Y = np.meshgrid(np.linspace(-1, 6), np.linspace(-1, 6))
2 XX = np.array([X.ravel(), Y.ravel()]).T
3 Z = gmm.score_samples(XX)
4 Z = Z.reshape((50,50))
5
6 plt.contour(X, Y, Z)
7 plt.scatter(X_train[:, 0], X_train[:, 1])
8 plt.show()
9
```

