

Core Equations — asdf

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$$144p_xV_x = RT_x \quad (1.9)$$

$$\frac{1}{2gJ}(v_x^2 - v_i^2) = C_p(T_i - T_x) \quad (1.10)$$

$$\frac{A_i v_i}{144V_i} = \frac{A_x v_x}{144V_x} \quad (1.11)$$

$$p_i V_i^\gamma = p_x V_x^\gamma \quad (1.12)$$

$$\frac{(p_{cijn})}{(p_{cns})} = \frac{(1 + \gamma M_i^2)}{(1 + \frac{\gamma-1}{2} M_i^2)^{\frac{\gamma}{(\gamma-1)}}} \quad (1.14)$$

$$\frac{p_{inj}}{p_i} = 1 + \gamma M_i^2 \quad (1.15)$$

$$\frac{p_t}{(p_{cns})} = \left(\frac{2}{(\gamma+1)}\right)^{\frac{\gamma}{\gamma-1}} \quad (1.16)$$

$$v_e = \sqrt{\frac{2g\gamma}{\gamma-1}RT_i\left(1 - \frac{p_e}{p_i}\right)^{\frac{(\gamma-1)}{\gamma}} + v_i^2} \quad (1.17)$$

$$v_e = \sqrt{\frac{2g\gamma}{\gamma-1}RT_{cns}\left(1 - \frac{p_e}{(p_{cns})}\right)^{\frac{(\gamma-1)}{\gamma}}} \quad (1.18)$$

$$Wdot = A_t p_{cns} \sqrt{\frac{g\gamma(\frac{2}{\gamma+1})^{\frac{(\gamma+1)}{\gamma-1}}}{RT_{cns}}} \quad (1.19)$$

$$\frac{A_e}{A_t} = \frac{\left(\frac{2}{\gamma+1}\right)^{\left(\frac{1}{\gamma-1}\right)} \left(\frac{p_{cns}}{p_e}\right)^{\frac{1}{\gamma}}}{\sqrt{\frac{\gamma+1}{\gamma-1} \left(1 - \left(\frac{p_e}{(p_{cns})}\right)\right)^{\frac{(\gamma-1)}{\gamma}}}} \quad (1.20)$$

$$p_t = (p_{cns}) \left(\frac{2}{\gamma+1}\right)^{\frac{\gamma}{\gamma-1}} \quad (1.21)$$

$$v_t = \sqrt{\frac{2g\gamma}{\gamma+1} RT_{cns}} \quad (1.22)$$

$$\frac{A_x}{A_t} = \frac{1}{M_x} \left(\frac{2}{\gamma+1} \left(1 + \frac{\gamma-1}{2} M_x^2 \right) \right)^{\frac{\gamma+1}{2(\gamma-1)}} \quad (1.24)$$

$$\frac{A_x}{A_t} = \frac{\left(\frac{2}{\gamma+1} \right)^{\frac{1}{\gamma-1}} \left(\frac{p_{cns}}{p_x} \right)^{\frac{1}{\gamma}}}{\sqrt{\frac{\gamma+1}{\gamma-1} \left(1 - \left(\frac{p_x}{p_{cns}} \right)^{\frac{\gamma-1}{\gamma}} \right)}} \quad (1.25)$$

$$v_x = \sqrt{\frac{2g\gamma}{\gamma-1} RT_{cns} \left(1 - \left(\frac{p_x}{p_{cns}} \right)^{\frac{\gamma-1}{\gamma}} \right)} \quad (1.26)$$

$$\frac{v_x}{v_t} = \sqrt{\frac{\gamma+1}{\gamma-1} \left(1 - \frac{p_x}{(p_{cns})^{\frac{\gamma-1}{\gamma}}} \right)} \quad (1.27)$$