

**Ex 2.1:**

The hypothesis space in EnjoySport is 973 because there are six attributes with a total of 18 possible values in the form: [3, 2, 2, 2, 2, 2]

A hypothesis space also contains “?” values meaning any possible value for the attribute is acceptable for a hypothesis, and a “Ø” value indicating no possible value for the attribute is acceptable.

Representing this in the vector showing possible values, the Ø only needs to appear once, as any appearance is semantically identical. This means that semantically distinct combinations are limited to:

[4,3,3,3,3,3]+1 possible combinations, as the “?” value is added to the possible values and the “Ø” is added a single time.

$$(4*3*3*3*3*3)+1 = 973.$$

An additional attribute,  $A$ , with  $k$  possible values, impacts the hypothesis space,  $H$ , as:

$$H_1 = ((H_0-1)*(k+1))+1$$

Or, the new hypothesis space,  $H_1$ , is equal to the old Hypothesis space,  $H_0$ , less the one possible expression containing any number of “Ø” values (-1), times the new variable’s quantity of possible values plus the possibility that any value will satisfy the hypothesis  $(*(k+1))$ , then adding back the possibility of a single “Ø” in any position, (+1).

In the example in the book, this is reflected by taking:

$$973-1 = 972$$

$$972 * 4 = 3,888$$

3,888+1 = 3,889, which is the new hypothesis space for an additional attribute, WaterCurrent, with possible values [Light, Moderate, Strong].

**Ex 2.2:**

$$S_0 = [\emptyset, \emptyset, \emptyset, \emptyset, \emptyset, \emptyset]$$

$$G_0 = [?, ?, ?, ?, ?, ?]$$

$$S_1 = [\text{Sunny}, \text{Warm}, \text{High}, \text{Strong}, \text{Cool}, \text{Change}]$$

$$G_1 = [?, ?, ?, ?, ?, ?]$$

$$S_2 = [\text{Sunny}, \text{Warm}, ?, ?, \text{Cool}, ?]$$

$$G_2 = [\text{Sunny}, ?, ?, ?, ?, ?], [\text{Cloud}, ?, ?, ?, ?, ?], [?, \text{Warm}, ?, ?, ?, ?], [?, ?, ?, ?, \text{Cool}, ?]$$

$$S_3 = [\text{Sunny}, \text{Warm}, ?, ?, ?, ?]$$

$$G_3 = [\text{Sunny}, ?, ?, ?, ?, ?], [\text{Cloud}, ?, ?, ?, ?, ?], [?, \text{Warm}, ?, ?, ?, ?]$$

$$S_4 = [\text{Sunny}, \text{Warm}, ?, ?, ?, ?]$$

$$G_4 = [\text{Sunny}, ?, ?, ?, ?, ?], [\text{Cloud}, ?, ?, ?, ?, ?], [?, \text{Warm}, ?, ?, ?, ?]$$

The final boundary sets will be identical because they are sets determined from each instance. If a set is [1,1] and you subtract one from a value, and then another, the final set [0,0] exists regardless of which value is changed first.

In this set, placing example 4 before example 3 would mean the general set would not split into a collection of 4 sets, which would reduce the size of the boundary sets if the training occurred in the original order.

## Ex 2.5 (a,b):

### Part A:

Data Dictionary for Table:

- Sex:
  - M = Male
  - F = Female
- Hair:
  - Bl = Black
  - Br = Brown
  - Blo = Blonde
- Height:
  - T = Tall
  - M = Medium
  - S = Short
- Nation:
  - US = US
  - FR = French
  - DE = German
  - IN = Indian
  - IE = Ireland
  - JP = Japanese
  - PT = Portugese

Person	P1				P2				Result
Attr	Sex	Hair	Height	Nation	Sex	Hair	Height	Nation	
Obs1	M	Br	T	US	F	Bl	S	US	+
Obs2	M	Br	S	FR	F	Bl	S	US	+
Obs3	F	Br	T	DE	F	Bl	S	IN	-
Obs4	M	Br	T	IE	F	Br	S	IE	+

S0 = [ $\emptyset, \emptyset, \emptyset, \emptyset$ ], [ $\emptyset, \emptyset, \emptyset, \emptyset$ ]

G0 = [ $\langle ?, ?, ?, ? \rangle$ ,  $\langle ?, ?, ?, ? \rangle$ ]

S1 = [ $\langle M, Br, T, US \rangle$ ,  $\langle F, Bl, S, US \rangle$ ]

G1 = [ $\langle ?, ?, ?, ? \rangle$ ,  $\langle ?, ?, ?, ? \rangle$ ]

S2 = [ $\langle M, Br, ?, ? \rangle$ ,  $\langle F, Bl, S, US \rangle$ ]

G2 = [ $\langle ?, ?, ?, ? \rangle$ ,  $\langle ?, ?, ?, ? \rangle$ ]

S3 = [ $\langle M, Br, ?, ? \rangle$ ,  $\langle F, Bl, S, US \rangle$ ]

G3 = [ $\langle M, ?, ?, ? \rangle$ ,  $\langle ?, ?, ?, ? \rangle$ ],

[ $\langle ?, ?, ?, US \rangle$ ,  $\langle ?, ?, ?, ? \rangle$ ], [ $\langle ?, ?, ?, FR \rangle$ ,  $\langle ?, ?, ?, ? \rangle$ ], [ $\langle ?, ?, ?, IN \rangle$ ,  $\langle ?, ?, ?, ? \rangle$ ],  
[ $\langle ?, ?, ?, IE \rangle$ ,  $\langle ?, ?, ?, ? \rangle$ ], [ $\langle ?, ?, ?, JP \rangle$ ,  $\langle ?, ?, ?, ? \rangle$ ], [ $\langle ?, ?, ?, PT \rangle$ ,  $\langle ?, ?, ?, ? \rangle$ ]

[ $\langle ?, ?, ?, ? \rangle$ ,  $\langle ?, ?, ?, US \rangle$ ], [ $\langle ?, ?, ?, ? \rangle$ ,  $\langle ?, ?, ?, FR \rangle$ ], [ $\langle ?, ?, ?, ? \rangle$ ,  $\langle ?, ?, ?, DE \rangle$ ],  
[ $\langle ?, ?, ?, ? \rangle$ ,  $\langle ?, ?, ?, IE \rangle$ ], [ $\langle ?, ?, ?, ? \rangle$ ,  $\langle ?, ?, ?, JP \rangle$ ], [ $\langle ?, ?, ?, ? \rangle$ ,  $\langle ?, ?, ?, PT \rangle$ ]

S4 = [ $\langle M, BR, ?, ? \rangle$ ,  $\langle F, ?, S, ? \rangle$ ]

G4 = [ $\langle M, ?, ?, ? \rangle$ ,  $\langle ?, ?, ?, ? \rangle$ ],

[ $\langle ?, ?, ?, US \rangle$ ,  $\langle ?, ?, ?, ? \rangle$ ], [ $\langle ?, ?, ?, FR \rangle$ ,  $\langle ?, ?, ?, ? \rangle$ ], [ $\langle ?, ?, ?, IN \rangle$ ,  $\langle ?, ?, ?, ? \rangle$ ],  
[ $\langle ?, ?, ?, IE \rangle$ ,  $\langle ?, ?, ?, ? \rangle$ ], [ $\langle ?, ?, ?, JP \rangle$ ,  $\langle ?, ?, ?, ? \rangle$ ], [ $\langle ?, ?, ?, PT \rangle$ ,  $\langle ?, ?, ?, ? \rangle$ ]

[ $\langle ?, ?, ?, ? \rangle$ ,  $\langle ?, ?, ?, US \rangle$ ], [ $\langle ?, ?, ?, ? \rangle$ ,  $\langle ?, ?, ?, FR \rangle$ ], [ $\langle ?, ?, ?, ? \rangle$ ,  $\langle ?, ?, ?, DE \rangle$ ],  
[ $\langle ?, ?, ?, ? \rangle$ ,  $\langle ?, ?, ?, IE \rangle$ ], [ $\langle ?, ?, ?, ? \rangle$ ,  $\langle ?, ?, ?, JP \rangle$ ], [ $\langle ?, ?, ?, ? \rangle$ ,  $\langle ?, ?, ?, PT \rangle$ ]

## Part B:

Given the set [ $\langle M, Bl, S, PT \rangle$ ,  $\langle F, Blo, T, IN \rangle$ ], there can be no " $\emptyset$ " values. A hypothesis containing any other value than those listed would not be consistent, thus the only acceptable values are those shown and "?".

$$2^8 = 256$$

## Ex 2.7:

There are infinitely many numbers between 4.5 and 6.1.

If I were to claim that 4.51 is the lowest number  $> 4.5$ , I could disprove my claim by showing that 4.501 is  $> 4.5$ , then show an even lower number 4.5001 is  $> 4.5$ .

The use of  $\leq$  or  $\geq$  instead of inequalities alone would solve this.

