# Artificial Neural Network: An Exploration Jericho McLeod CSI-873 Midterm

#### Data

The dataset used for this project is a sampling of NMIST handwritten digits, ingested as vectors of 785 numbers. The first number indicates the class, and the remaining 784 digits represent the 28x28 matrix of pixel values from 0 to 255. These were scaled to a range of 0 to 1, and then a function was created to visually inspect the data, shown below in figure 1. The dataset contained 60,000 training examples and 10,000 validation examples, all of which were used in this implementation.

#### **Neural Network Functions and Parameters**

The Artificial Neural Network created to classify handwritten digits utilized a sigmoid activation function:

$$output = \frac{1}{1 + e^{-z}}$$

Thus the weights were updated using:

$$w_{ii} \leftarrow w_{ii} + \Delta w_{ii}$$

Where the updates to weights, with momentum, are calculated by:

$$\Delta w_{ji}(n) = \eta \delta_k x_{ji} + \alpha \Delta w_{ji}(n-1)$$

And the error terms for output and hidden nodes, respectively, are:

$$\delta_k = o_k (1 - o_k)(t_k - o_k)$$

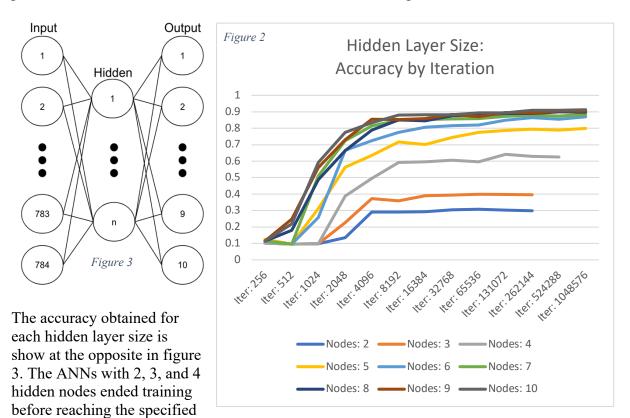
$$\delta_h = o_h (1 - o_h) \sum_{k \in outputs} w_{kh} \delta_k$$

The initial value for momentum ( $\alpha$ ) is 0.6, and the initial value for the learning rate ( $\eta$ ) is 0.3. Weights were initialized randomly between -0.1. and 0.1, and bias weights were included in the model.

For stopping conditions, several different implementations were tested. It was discovered that waiting for accuracy to converge to some amount tended to be an insufficient measure for this model; either the acceptable range was too broad, and training ended early, or it was unreachable, and accuracy continually shifted by small amounts slightly greater than the stopping condition allowed. Another tested method was moving averages; this however, also led to occasionally early stops. The final selection was for a simpler method; if accuracy decreased twice successively across two iterations, training concluded, and the model reverted to the prior weights. As an additional stopping condition for time concerns, an upper limit of 2^20 iterations of training was implemented.

## Neural Network Design Exploration and Results

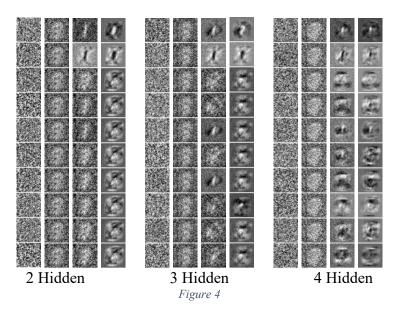
The network created contained an input for each pixel in the provided arrays, for a total of 784. The hidden layer requirements were for a single layer containing 2, 3, and 4 neurons in each of 3 separate cases. In this implementation, a test was run that used 2 through 10 hidden neurons in order to compare a broader set of results. The output layer chosen was 10, or one for each possible outcome. The network itself is visualized below in figure 2.



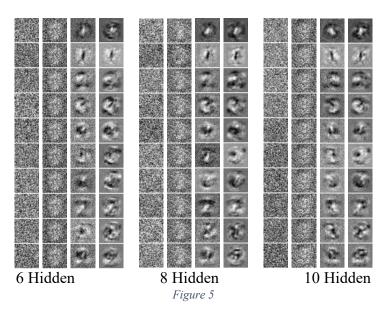
upper limit, demonstrating that the stopping condition functioned as intended. Time constraints prevented this from being the only possible stopping condition, thus the true limits of accuracy from larger hidden layers remains unknown from this exploration.

### **Network Weights Exploration**

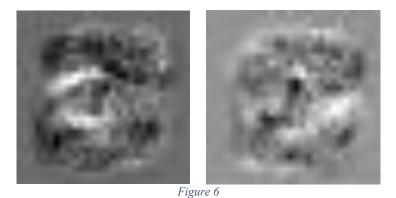
In training the networks, visualizing the weights helps to understand what is being learned. In. figure 4 the training weights for 2, 3, and 4 node hidden layers are shown at 0, 256, 8192, and 32768 iterations of training from left to right, and from top to bottom, 0 to 9, respectively. In these, grey indicates a weigh of 0, while lighter tints indicate negative weights and darker tints indicate positive weights.



It is easy to see that the initial weights were random, and the limitations of having fewer hidden neurons in terms of how many classifications can be made. Reviewing larger hidden layers shows more easily human-interpretable results. In figure 5 the hidden layers are made up of 6, 8, and 10 nodes, and shown at earlier iterations 0, 256, 2048, and 8192, in figure 5.



This helps to highlight what visual information may be useful in separating digits. An important distinction to make in reviewing the weights is the expectation is not to see representation of a digit; we are not training a machine to write digits but to recognize them. For this purpose, the location of white space is just as important as black space. Compare, for instance, 3 and 8. The black pixels included in a 3 are also included in an 8; thus, the only way to separate the to is to examine the left side of the digit; if it is black, the digit is an 8, and if white, it is a 3. This is represented in very late training iterations for these digits in figure 6, showing 3 at the left and 8 and the right. Note that digits are considered to be 'not 3' if they contain black pixels enclosing the left side, and digits are considered '8' if they contain such pixels.



## **Network Classification Results Exploration**

Using two nodes in the hidden layer leads to a relatively low accuracy of approximately 30%, as shown in figure 7. Of this, however, it is noteworthy that two digits are being classified, and essentially all remaining digits are given a single classification that is identical. The true classes represented are "is 0", "is 1", and "is not 0 or 1,"; the fact that 3 is successfully classified is incidental.

	Classifed As												
		0	1	2	3	4	5	6	7	8	9	-	
	0	913	0	0	67	0	0	0	0	0	0	93.2%	
	1	0	1108	0	27	0	0	0	0	0	0	97.6%	
	2	3	2	0	1027	0	0	0	0	0	0	0.0%	
SS	3	1	0	0	1009	0	0	0	0	0	0	99.9%	
Actual Class	4	0	2	0	980	0	0	0	0	0	0	0.0%	
ctua	5	13	5	0	874	0	0	0	0	0	0	0.0%	
Ă	6	8	2	0	948	0	0	0	0	0	0	0.0%	
	7	3	9	0	1016	0	0	0	0	0	0	0.0%	
	8	5	5	0	964	0	0	0	0	0	0	0.0%	
	9	1	5	0	1003	0	0	0	0	0	0	0.0%	
		96.4%	97.4%	0.0%	12.7%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	30.3%	

Figure 7

Comparing this to figure 8 we can see that now 3 classes are being well classified when using 3 nodes in the hidden layer, with all remaining objects being classified as a fourth class. This gives approximately 40% accuracy, but one of the classes remains very low in terms of the percentage of correct classifications.

Classifed As												
		0	1	2	3	4	5	6	7	8	9	•
	0	938	0	0	41	0	0	0	1	0	0	95.7%
	1	0	1099	0	35	0	0	0	1	0	0	96.8%
	2	8	4	0	1004	0	0	0	16	0	0	0.0%
SS	3	3	0	0	995	0	0	0	12	0	0	98.5%
Actual Class	4	0	1	0	979	0	0	0	2	0	0	0.0%
ctua	5	22	4	0	854	0	0	0	12	0	0	0.0%
Ă	6	13	3	0	942	0	0	0	0	0	0	0.0%
	7	2	10	0	81	0	0	0	935	0	0	91.0%
	8	10	5	0	955	0	0	0	4	0	0	0.0%
	9	2	5	0	986	0	0	0	16	0	0	0.0%
		94.0%	97.2%	0.0%	14.5%	0.0%	0.0%	0.0%	93.6%	0.0%	0.0%	39.7%

Figure 8

Once the number of nodes in the hidden layer reaches 4, shown in figure 9, we begin to see a greater rate of classifications than nodes; the model is now attempting to classify 7 digits, with remaining outputs falling to one of the presently unused classes.

Classifed As												
		0	1	2	3	4	5	6	7	8	9	•
	0	857	0	7	1	9	0	3	103	0	0	87.4%
	1	0	1079	1	6	0	0	42	5	2	0	95.1%
	2	29	23	828	19	8	0	77	45	3	0	80.2%
SS	3	7	21	14	831	2	0	10	122	3	0	82.3%
l Cla	4	2	1	3	3	889	0	40	44	0	0	90.5%
Actual Class	5	13	9	4	32	28	0	39	761	6	0	0.0%
ď	6	5	2	12	0	36	0	871	30	2	0	90.9%
	7	6	17	11	22	9	0	32	915	16	0	89.0%
	8	0	6	0	19	20	0	125	785	19	0	2.0%
	9	3	1	1	4	64	0	6	926	4	0	0.0%
		93.0%	93.1%	94.0%	88.7%	83.5%	0.0%	70.0%	24.5%	34.5%	0.0%	62.9%

And at hidden layer sizes of 5 or greater we begin to see all classifications being utilized, as shown in figure 10. It is possible that training for a greater length of time would improve the results such that the maximum information that could be contained in the hidden layer, 2^n where n is the number of nodes, could be reached; however, the marginal return for training times is not ideal. Training 1,000,000 iterations with a smaller number of nodes takes much longer than adding hidden neurons and training for a much shorter time period to reach the same or better results.

Classifed As												
		0	1	2	3	4	5	6	7	8	9	
	0	908	1	0	10	7	31	15	1	7	0	92.7%
	1	0	1114	1	7	0	2	1	4	6	0	98.1%
	2	19	73	694	137	17	10	43	3	33	3	67.2%
SS	3	5	69	33	776	0	100	4	18	2	3	76.8%
l Cla	4	0	3	6	0	806	0	12	15	5	135	82.1%
Actual Class	5	106	30	7	44	14	593	4	18	71	5	66.5%
Ă	6	26	7	16	7	51	3	816	4	27	1	85.2%
	7	9	45	11	17	8	1	16	893	0	28	86.9%
	8	15	269	19	10	19	36	6	7	578	15	59.3%
	9	15	16	0	3	95	17	3	35	11	814	80.7%
٦.	10	82.3%	68.5%	88.2%	76.8%	79.3%	74.8%	88.7%	89.5%	78.1%	81.1%	79.9%

Figure 10

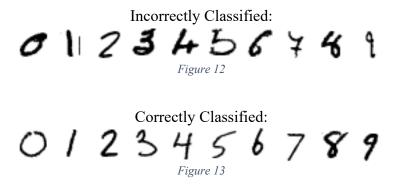
Examining the results of a neural network with 10 nodes in the hidden layer shows much better results overall, as seen in figure 11. It is possible that neural networks perform best when the hidden layer size is greater than or equal to the output layer size; however, the scope of that question is beyond this exploration.

Classifed As												
		0	1	2	3	4	5	6	7	8	9	
	0	948	0	4	3	7	5	8	3	2	0	96.7%
	1	0	1105	2	6	0	2	6	2	12	0	97.4%
	2	12	13	902	21	8	7	29	9	30	1	87.4%
SS	3	4	4	22	877	0	41	4	9	48	1	86.8%
Actual Class	4	4	0	3	1	908	0	21	2	13	30	92.5%
tua	5	16	5	5	33	2	777	16	6	28	4	87.1%
Ă	6	24	1	9	1	7	9	904	0	3	0	94.4%
	7	0	15	27	16	7	1	0	936	2	24	91.1%
	8	9	8	5	27	4	31	23	6	856	5	87.9%
	9	7	3	2	9	23	5	4	6	36	914	90.6%
		92.6%	95.8%	91.9%	88.2%	94.0%	88.5%	89.1%	95.6%	83.1%	93.4%	91.3%

Figure 11

### Misclassification Exploration

Visually comparing data that was accurately classified with misclassified data helps to understand misclassifications. For this purpose, the 10-hidden-node network was used. In the two arrays below, figures 12 and 13, one can see that the digits that are misclassified are atypical, yet still recognizable to humans for the most part. In contrast to these, correctly classified digits tend to be written in more typical forms. This highlights that the Artificial Neural Network is classifying with limited features and is not able to easily identify digits with additional or missing serifs, altered angles, or extra pixels entered as noise.



To create a more model that is more resilient to misclassifications, one may wish to consider deleting blocks of pixels from training data, apply transformations to stretch or skew images, or to add additional blocks of pixels. Doing this for the entire data set, while also retaining the original, and training on the augmented collection of training examples, would force the network to expand the features being used to classify digits, thus potentially increasing performance. However, this would also increase training times, and may be of limited benefit without also expanding the size of the hidden layer and even the depth of the network via additional hidden layers.

#### Code Appendix

Notes on running this algorithm:

- 1) The input data must be located in the same director as this file, and must not be encrypted or compressed.
- 2) The algorithm will provide 3 sets of output, with output files located in the directory from which the script is run:
  - a. Printing summary results in the console
  - b. Saving a .csv copy of the results summary
  - c. Saving an image of the weights at each checkpoint for each hidden node quantity
- 3) Libraries required:
  - a. CSV
  - b. Random
  - c. Math
  - d. Decimal
  - e. Copy
  - f. Numpy
  - g. PIL

```
#!/usr/bin/env python3
# -*- coding: utf-8 -*-
Created on Sat Oct 5 15:41:29 2019
@author: jmcleod
CSI-873: Computational Learning
This is an Artificial Neural Network with a single hidden layer of some
specified size. I used it to classify NMIST data for handwritten digits, thus
this file also contains image generation functions to convert the numeric
arrays back into graphics for human review.
The activation function is sigmoid: 1 / 1 + e^{-z}
import csv, random, math, decimal, copy
import numpy as np
from PIL import Image
decimal.getcontext().prec = 100
def data_import(file):
    This function imports the data from a particular file
    and returns an array of arrays
    data = []
    with open(file, 'r') as csvfile:
        csv r = csv.reader(csvfile,delimiter=' ')
        for row in csv r:
            row nums = []
            for i in range(len(row)):
                    val = float(row[i])
                    if i > 0:
```

```
val = round(val/255, 4)
                        # The above line scales the data imported
                    row nums.append(val)
                except:
                    print('ERROR on import: non-numerical data:',row[i])
                    break
            data.append(row nums)
    return (data)
def data import loop(string, denom):
    '''This function loops the data import across all files of the chosen type,
    which is specified by the string argument passed to the function.
    It then uses the first value in the set to add the imported arrays
    to the correct dictionary key, created with values 0-9.
    The resulting dictionary is returned.
    files = []
    data dict = {}
    for i in range(10):
        file name = string+str(i)+'.txt'
        files.append(file name)
        data_dict[i]=[]
    for i in files:
        data = data_import(i)
        for j in range(len(data)):
            if j%denom==0: # SUBSET data
                data dict[data[j][0]].append(data[j][1:])
    return(data dict)
def create_image_data(char_matrix):
    This function outputs a human-viewable copy of an input from matrix form
    data = np.zeros( (len(char matrix),len(char matrix[0]),3), dtype=np.uint8 )
    for row in range(len(char matrix)):
        for col in range(len(char_matrix[row])):
            val = 255 - char_matrix[col][row]
            data[row,col] = [val,val,val]
    return (data)
def create large image(data dict):
    '''This function creates an NxN image of 10 examples of 10 classes'''
    shortest = 1000000
    for k, v in data dict.items():
        if len(v) < shortest:
            shortest = len(v)
    big matrix data = []
    for m in range(10):
        medium matrix data = []
        for i in range (28):
            medium_matrix_data.append([])
        for i in range(10):
            random num = random.randint(0, shortest-1)
            array = data dict[m][random num]
            for j in range(len(array)):
                medium_matrix_data[j%28].append((array[j]*255))
        for i in medium matrix data:
            big matrix data.append(i)
    big image = create image data(big matrix data)
    image = Image.fromarray(big image)
    image.show()
def randomize_data_arrays(data_dict):
```

```
''' This is a function to randomize the order of training and test data'''
    data array = []
    data result = []
    for k,v in data dict.items():
        for i in v:
            data_result.append(k)
            data array.append(i)
    random_index = []
    for i in range(len(data array)):
        random index.append(random.random())
    random index copy = copy.deepcopy(random index)
    rand data array = []
    rand data result = []
    for i in range(len(random_index)):
        min_val = min(random_index_copy)
        random index copy.pop(random index copy.index(min val))
        index val = random index.index(min val)
        rand data array.append(data array[index val])
        rand data result.append(data result[index val])
    data array = rand data array
    data result = rand data result
    return(data_array, data_result)
class neuron:
    def init (self,input count, starting weight, learn rate):
        self.weights = [starting weight]*(input count+1)
        self.delta weights = [0]^{*} (input count+1)
        for i in range(input count+1):
            rando = random.uniform(-starting_weight, starting_weight)
            self.weights[i] = rando
        self.learn rate=learn rate
        self.output = 0
class output neuron (neuron):
    def feed forward(self,input array):
        x = \overline{self.weights[0]}
        for i in range(len(input array)):
            x += float(input array[i])*float(self.weights[i+1])
        x out =
decimal.Decimal(1)/(decimal.Decimal(1)+(decimal.Decimal(math.e) ** (decimal.Decimal(-
x)))) # Sigmoid output
        x \text{ out = float(round(x out, 16))}
        self.output = x_out
        return(x out)
    def back prop(self, t o, inputs, momentum):
        error = self.output * (1 - self.output) * (t o - self.output)
        for i in range(len(self.weights)):
            try: xji = inputs[i-1]
            except: xji = 1
            prior weight delta = self.delta weights[i]
            self.weights[i] = (self.learn_rate * error * xji) + self.weights[i] +
(momentum * prior weight delta)
            self.delta weights[i] = self.learn rate * error * xji
class hidden neuron (neuron):
    def feed forward(self,input array):
        x = self.weights[0]
        for i in range(len(input array)):
            x += float(input array[i])*float(self.weights[i+1])
        x out =
decimal.Decimal(1)/(decimal.Decimal(1)+(decimal.Decimal(math.e)**(decimal.Decimal(-
x)))) # Sigmoid output
        x \text{ out = float(round(x out, 16))}
```

```
self.output = x out
        return(x out)
    def back prop(self, w e term, inputs, momentum):
        error = w e term * self.output*(1-self.output)
        for i in range(len(self.weights)):
            try: xji = inputs[i-1]
            except: xji = 1
            prior_weight_delta = self.delta_weights[i]
            self.weights[i] = (self.learn rate * error * xji) + self.weights[i] +
(prior_weight_delta * momentum)
            self.delta weights[i] = self.learn rate * error * xji
class neural network:
    def __init__(self,dataset,classes,hidden_neurons,output_neurons,\
                starting weight=0.1, learn rate=0.3, momentum = 0.6):
        self.inputs = len(dataset[0])
        self.dataset = dataset
        self.classes = classes
        self.starting weight = starting weight
        self.learn rate = learn rate
        self.momentum = momentum
        self.hidden_layer = []
        self.output_layer = []
        self.output_errors = []
        for i in range (hidden neurons):
            self.hidden layer.append(hidden neuron(self.inputs,\
                                                self.starting weight,\
                                                self.learn rate))
        for i in range(output_neurons):
            self.output_layer.append(output_neuron(len(self.hidden_layer),\
                                                self.starting weight,\
                                                self.learn rate))
        self.hidden x = []
        self.output x = []
    def feed forward(self,epoch):
        data_instance = self.dataset[(epoch % len(self.dataset))]
        self.hidden x = []
        for n in self.hidden layer:
            self.hidden x.append(n.feed forward(data instance))
        self.output x = []
        for n in self.output layer:
            self.output_x.append(n.feed_forward(self.hidden_x))
    def back prop(self, iteration):
        self.output errors = []
        hidden errors = []
        target class = self.classes[(iteration%len(self.dataset))]
        target_outputs = [0.01]*len(self.output_layer)
        delta weights = []
        for i in range(len(self.output layer)):
            if i==target class:
                target outputs[i] +=0.98
        for n in range(len(self.output layer)):
            neuron = self.output layer[n]
            self.output_errors.append(neuron.output * (1 - neuron.output) * \
                                  (target outputs[n] - neuron.output))
        for n in range(len(self.hidden layer)):
            neuron = self.hidden layer[n]
            output = neuron.output
            pre error = output * (1-output)
            wk = 0
            for n2 in range(len(self.output layer)):
```

```
o neuron = self.output layer[n2]
                \overline{wk} += (o neuron.weights[n+1] * self.output errors[n2])
            hidden errors.append(wk * pre error)
        for n in range(len(self.output layer)):
            neuron = self.output layer[n]
            for w in range(len(neuron.weights)):
                try: xji = self.hidden x[w-1]
                except: xji = 1
                delta_w = neuron.learn_rate * self.output_errors[n] * xji
                delta weights.append(delta w)
                neuron.weights[w] += (delta w + self.momentum *
neuron.delta weights[w])
                neuron.delta weights[w] = delta w
        for n in range(len(self.hidden layer)):
            neuron = self.hidden layer[n]
            for w in range (len (neuron.weights)):
                try: xji = self.dataset[(iteration%len(self.dataset))][w-1]
                except: xji = 1
                delta w = neuron.learn rate * hidden errors[n] * xji
#self.output errors[n]
                delta weights.append(delta w)
                neuron.weights[w] += (delta_w + self.momentum *
neuron.delta weights[w])
                neuron.delta weights[w] = delta w
        return(delta weights)
    def classify(self,array):
        self.hidden x = []
        for n in self.hidden layer:
            self.hidden x.append(n.feed forward(array))
        self.output x = []
        for n in self.output layer:
            self.output x.append(n.feed forward(self.hidden x))
        classification = 0
        value = 0
        for i in range(len(self.output_x)):
            if self.output x[i]>=value:
                classification = i
                value = self.output x[i]
        return(classification)
def measure model(test set, test answers, model):
    '''This function determines the accuracy of a model by classifying the
    test data'''
    total = 0
    correct = 0
    for n in range(len(test answers)):
        rando = random.random()
        if rando > 0: #set to higher value to subset data
            classification = model.classify(test set[n])
            actual_class = test_answers[n]
            if classification == actual class:
                correct+=1
            total+=1
    return(correct/total)
def conf matrix shell():
    '''This function just returns an empty NxN matrix'''
    matrix = []
    for i in range(10):
        row=[]
        for j in range(10):
            row.append(0)
```

```
matrix.append(row)
    return (matrix)
def get conf matrix(test set, test answers, model):
    '''This function uses the NxN matrix created above and adds
    observed classifications'''
    matrix = conf matrix shell()
    for n in range(len(test answers)):
        rando = random.random()
        if rando > 0: #adjust to subset data
            classification = model.classify(test set[n])
            actual class = test answers[n]
            matrix[actual class][classification]+=1
    return (matrix)
def get weights image vector(model):
    hidden weights = []
    output weights = []
    pixel weights = {}
    for i in model.hidden layer:
        hidden_weights.append(i.weights[1:])
    for i in model.output_layer:
        output weights.append(i.weights[1:])
    for out in range(len(output weights)):
        vector = []
        for i in range(len(hidden_weights[0])):
            vals, val = [], 0
            for h in hidden weights:
                vals.append(h[i])
            for o in range(len(output weights[out])): #
                vals[o] = vals[o] * output weights[out][o] #
            for v in vals:
                val += v
            vector.append(val)
        pixel weights[out] = vector
    return(pixel weights)
def min max array(array):
    out = []
    for i in array:
        v = (i-min(array)) / (max(array)-min(array))
        out.append(v)
    return(out)
def alt min max(array):
    out, temp = [], []
    for i in array:
        if i \ge 0:
            temp.append(i)
        else:
            temp.append(i*-1)
    for i in temp:
        v = (i-min(temp)) / (max(temp)-min(temp))
        out.append(v)
    return(out)
```

def create\_small\_image\_data(char\_matrix):

```
''' Create an image of a specific input
    Useful after the above classification command
    in order to see the image being classified'''
    data = np.zeros( (len(char matrix),len(char matrix[0]),3), dtype=np.uint8 )
    for row in range(len(char matrix)):
        for col in range(len(char matrix[row])):
            #print(col,row,len(char matrix),len(char matrix[0]))
            val = 255- (255 * char_matrix[row][col])
            data[row,col] = [val,val,val]
    return (data)
def create image(data array, name):
    matrix = []
    for i in range(int(len(data array)/28)):
        row = data array[i*28:i*28+28]
        matrix.append(row)
    image matrix = create small image data(matrix)
    image = Image.fromarray(image matrix)
    filename = str(name) + '.jpg'
    image.save(filename)
def create single array (model, i):
    ''' Creates the array for weights images'''
    pixel weights = get weights image vector(model)
    blank row = [0]*28
    temp_vec1 = min_max_array(pixel_weights[0])
    temp_vec2 = min_max array(pixel weights[1])
    temp vec3 = min max array(pixel weights[2])
    temp vec4 = min max array(pixel weights[3])
    temp vec5 = min max array(pixel weights[4])
    temp vec6 = min max array(pixel weights[5])
    temp_vec7 = min_max_array(pixel_weights[6])
    temp_vec8 = min_max_array(pixel_weights[7])
    temp_vec9 = min_max_array(pixel_weights[8])
    temp vec10 = min max array(pixel weights[9])
    temp array = temp vec1+blank row+\
                 temp_vec2+blank_row+\
                 temp vec3+blank row+\
                 temp vec4+blank row+\
                 temp_vec5+blank_row+\
                 temp vec6+blank row+\
                 temp_vec7+blank_row+\
                 temp vec8+blank row+\
                 temp vec9+blank row+\
                 temp vec10+blank row
    create_image(temp_array,i)
def main():
    '''Data Import'''
    denom = 1
    data dict = data import loop('train',denom)
    denom = 1
    test dict = data import loop('test',denom)
    '''Create sample image of data'''
    create large image(data dict)
    '''Randomize the order of the data'''
    data array, data result = randomize data arrays(data dict)
    test array,test result = randomize data arrays(test dict)
    file output = []
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for i in range (2,11):
       prior ann = 0
       prior accuracy = 0
       prior accs = []
       stop = 0
       powers = 8
       data instance = 0
       ann = neural_network(data_array,data_result,i,10)
       name = str(i)+'_nodes_'+str(data_instance)+'_iters'
       create single array(ann, name)
       while stop < 1:
           for n in range(2**powers-data instance):
               ann.feed forward(data instance)
               ann.back_prop(data_instance)
               data instance+=1
           name = str(i)+' nodes '+str(data instance)+' iters'
           create single array(ann, name)
           result = measure model(test array, test result, ann)
           prior accs.append(result)
           print('Nodes: %d Iterations: %d
                                             Accuracy:
%4f'%(i,data instance,result))
            %4f'%(i,data_instance,result)])
           powers+=1
           delta acc = result - prior accuracy
           print(result, prior accuracy, delta acc)
           if delta_acc < 0: delta_acc = delta_acc * -1
           if delta acc < .005 and data instance > 8200: #stopping condition on drop
in accuracy
               stop+=1
           elif len(prior accs) > 2:
               if prior accs[-1] < prior accs[-2] and prior accs[-2] < prior accs[-3]:
#stopping condition for 10% decrease in accuracy with rewind to prior ANN
                   stop+=1
                   ann = prior_ann
           else:
               prior accuracy = result
           prior ann = copy.deepcopy(ann)
            if powers > 15: #upper bound on iterations to train
               stop+=1
        confusion matrix = get conf matrix(test array,test result,ann)
       print()
       print('Hidden Nodes:',i)
       print('Accuracy:',result)
       print('Confusion Matrix:')
       for i in confusion matrix:
           print(i)
       print()
       file output.append([])
       file output.append(['Hidden Nodes:',i])
       file_output.append(['Accuracy:',result])
       file_output.append(['Confusion Matrix:'])
        for \overline{i} in confusion matrix:
           file output.append(i)
        file output.append([])
   with open('output filename.csv', mode='w') as csvfile:
       csv r = csv.writer(csvfile,delimiter=',')
        for row in file output:
           csv r.writerow(row)
if name == ' main ':
   main()
```