

Bayesian Econometrics: Homework 1

Jerin Varghese

February 1, 2019

Problem 1

Download and install R and R-Studio from <https://cran.r-project.org> and <https://www.rstudio.com/products/rstudio/download/>

Problem 2

Use R to calculate the following:

1. Create a vector called x containing the number 2 5 8 12 16

```
x <- c(2,5,8,12,16)
```

2. Create a vector called y containing the number from 5 to 9

```
y <- c(5:9)
```

3. Calculate $z = x - y$

```
z <- x-y
```

```
## [1] -3 -1  1  4  7
```

Problem 3

1. Create a vector x of 100 values starting at 2 and increasing by 3 each time

```
x <- seq(from=2,by=3,length.out=100)
```

2. Extract the values at positions 5,10,15 and 20 in the vector of values from x

```
x[seq(5,20,5)]
```

```
## [1] 14 29 44 59
```

3. Extract the values at positions 10 to 20.

```
x[10:20]
```

```
## [1] 29 32 35 38 41 44 47 50 53 56 59
```

4. Create 25 by 4 matrix x3 from x (first 4 elements go to the first row, next 4 elements go to 2nd row, etc.)

```
x3 <- matrix(data=x, nrow=25, ncol=4)
```

5. Create 25 by 2 matrix from 2nd and 3rd column of matrix x3.

```
matrix(data=x3[,2:3], nrow=25, ncol=2)
```

```
##      [,1] [,2]
## [1,]   77  152
## [2,]   80  155
## [3,]   83  158
## [4,]   86  161
## [5,]   89  164
## [6,]   92  167
## [7,]   95  170
## [8,]   98  173
## [9,]  101  176
## [10,] 104  179
## [11,] 107  182
## [12,] 110  185
## [13,] 113  188
## [14,] 116  191
## [15,] 119  194
## [16,] 122  197
## [17,] 125  200
## [18,] 128  203
## [19,] 131  206
## [20,] 134  209
## [21,] 137  212
## [22,] 140  215
## [23,] 143  218
## [24,] 146  221
## [25,] 149  224
```

Problem 4

1. Save a tap delimited file, called sample file.txt in a directory and set your working directory to where your data is stored. Then read the file into a new structure using read.delim command and check (print) the row 11.

```
working_dir <- "C:/Users/jerin/OneDrive/Documents/JHU/Bayesian Econometrics/Homeworks"
setwd(working_dir)
sample_file <- read.delim('sample_file.txt')
sample_file[11,]
```

```
##      Sample Length Category
## 11    x_11         80         C
```

2. Calculate the mean of the column named Length.

```
mean(sample_file$Length)
```

```
## [1] 73.325
```

3. Find out how many rows in sample file have a Length which is < 65 .

```
nrow(sample_file[sample_file$Length > 65,])
```

```
## [1] 24
```

4. Print the values of Length less than 65.

```
sample_file[sample_file$Length > 65,"Length"]
```

```
## [1] 82 81 96 85 96 80 98 78 100 79 84 68 99 98 83 81 69  
## [18] 72 87 84 80 68 95 93
```

Problem 5.

1. Generate a sequence of x variable from 0 to 10 by 0.5 increment.

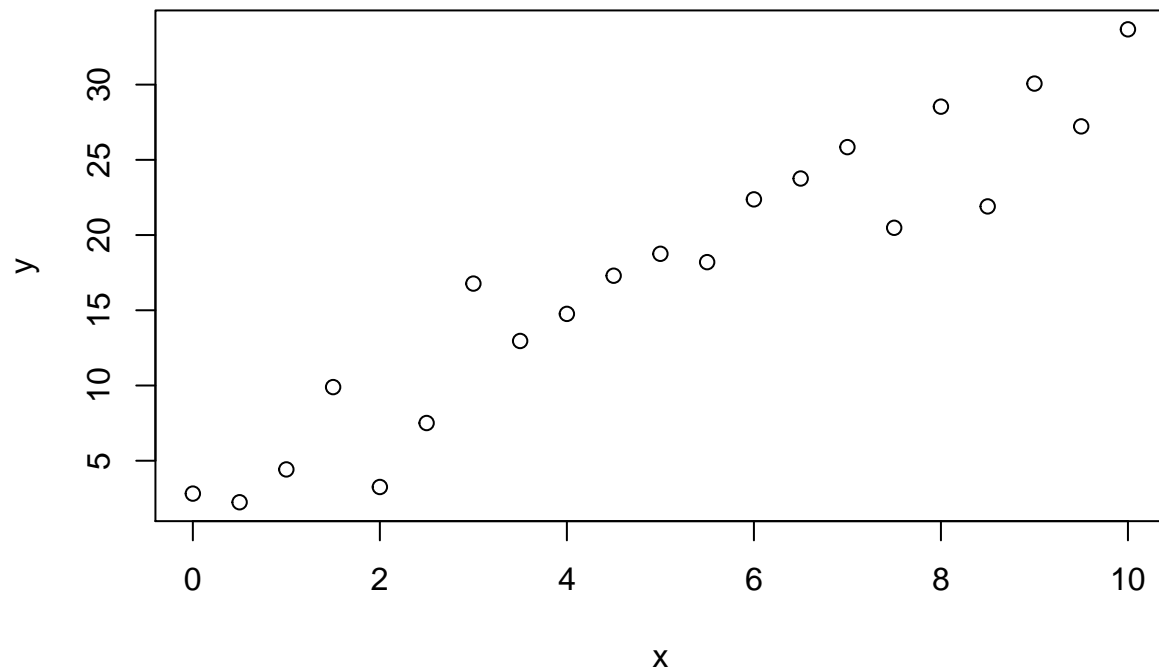
```
x <- seq(0, 10, 0.5)
```

2. Generate $y_i = 2 + 3 \cdot x_i + e_i$ where $e_i \sim \text{i.i.d.} N(0, 3^2)$.

```
y <- 2 + 3*x + rnorm(length(x),mean=0,sd=3)
```

3. Plot x and y.

```
plot(x,y)
```

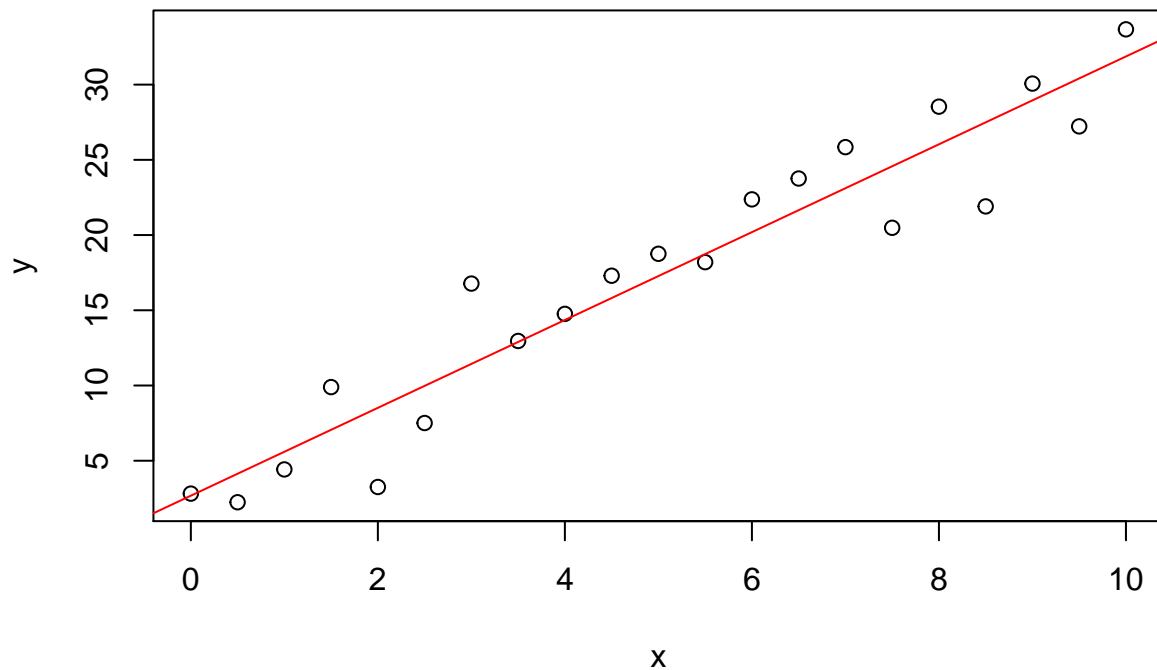


4. Fit a linear regression model for y on x using command lm

```
lm.fit <- lm(y~x)
```

5. Draw the fitted regression line.

```
plot(x,y) + abline(lm.fit, col="red")
```



```
## integer(0)
```

Problem 6.

1. Draw a sample of 100 observations from gamma distribution with shape parameter =1 and rate parameter=4.

```
set.seed(42)
gsample <- rgamma(100, shape=1, rate=4)
```

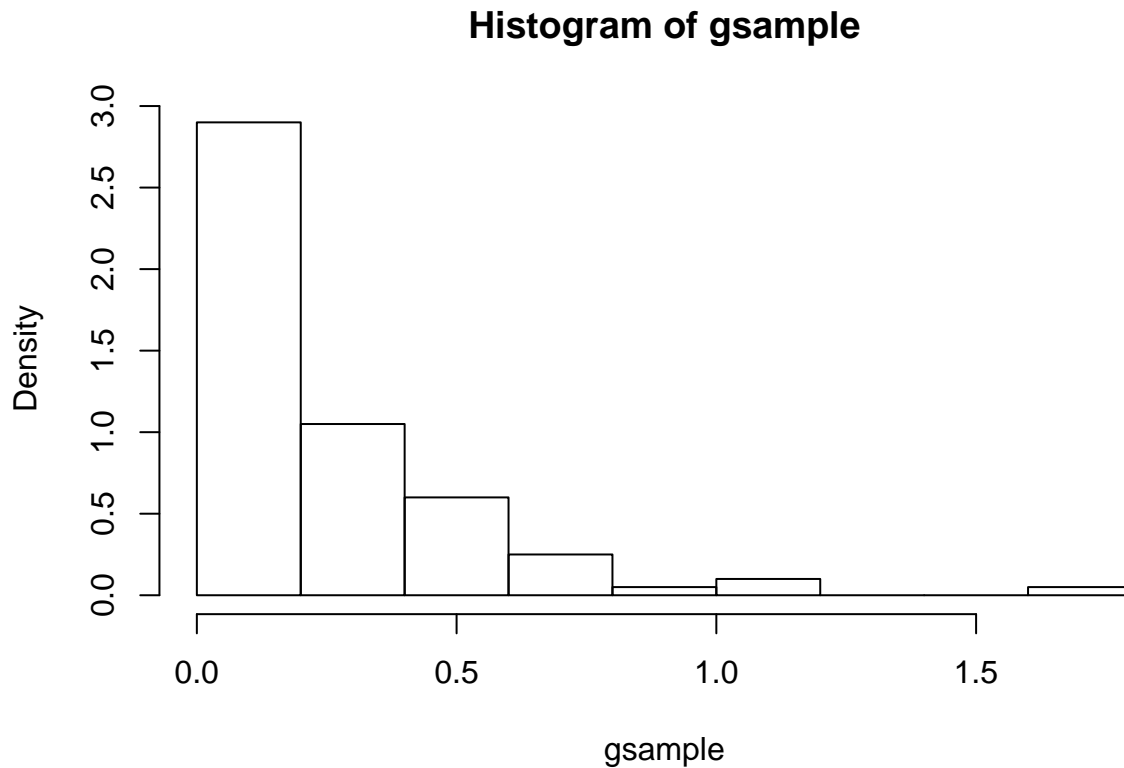
2. calculate the mean and compare with the theoretical mean.

```
# sample mean is .246, which is very close to theoretical mean of 1/4
mean(gsample)
```

```
## [1] 0.2460118
```

3. Draw histogram and density of the sample

```
hist(gsample, prob=TRUE)
```



Problem 7

Generate 1000 observations of an AR process and draw graphs:

1. generate a standard normal random variable for the initial value x_1 .

```
set.seed(42)
n <- 1000
white_noise <- rnorm(n)
# initialize first value
ar1 <- c(white_noise[1])
```

2. for x_i from $i=2$ to 1000, $x_i = .09 \cdot x_{i-1} + e_i$ where $e_i \sim \text{i.i.d.} N(0, 1)$

```
for (i in 2:n){
  ar1[i] <- .09*ar1[i-1] + white_noise[i]
}
```

3. plot x and cumulative sum of x (use command `cusum`) over i

```
plot(ar1, cusum(ar1))
```

