

0.1 /code

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```
1  #coding=utf-8
2
3  import matplotlib
4  matplotlib.use('ps')
5  import matplotlib.pyplot as plt
6  import numpy as np
7  from scipy.integrate import solve_ivp
8
9
10 def plot_phase_trajectories(f, inits, xbound, ybound, t=(0, 10), steps=100,
11                             axis=None,
12                             sipv_kwargs={}, plt_kwargs={'c': 'b', 'lw': .7}):
13     """Plots phase trajectory of given ODE with scipy.integrate.solve_ivp
14     Returns list of matplotlib-artist objects"""
15     if axis is None:
16         axis = plt.gca()
17
18     def f_neg(t, x):
19         # for solution backwards in time
20         return -f(t, x)
21
22     artists = []
23     tt = np.linspace(*t, steps)
24     for ff in (f, f_neg):
25         for i in inits:
26             # solve_ivp(..., dense_output=True).sol holds a OdeSolution object
27             # which interpolates the solution and allows its evaluation at
28             # arbitrary points
29             # Returns array with shape(n,) corresponding to the RHS of the
30             # given ODE
31             sol = solve_ivp(ff, t, i, dense_output=1, **sipv_kwargs).sol
32             sol_eval = sol(tt)
33             sol_x_ma = np.ma.masked_outside(sol_eval[0], *xbound)
34             sol_y_ma = np.ma.masked_outside(sol_eval[1], *ybound)
35             artists.append(axis.plot(sol_x_ma, sol_y_ma, **plt_kwargs))
36
37     plt.xlim(xbound)
38     plt.ylim(ybound)
39     return artists
40
41
42 ppt = plot_phase_trajectories
43
```

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44
45     inits = np.array([(i, j) for i in np.arange(-10, 11, 2) for j in np.arange(-1.5, 2, 1)])
46
47     def funcs(s, n):
48         def func(t, x):
49             """ $f(t, x) = s \cdot x(t)^n \cdot (1 - x(t)^2)$ """
50             return np.array([1, s*x[1]**n*(1-x[1]**2)])
51         return func
52
53     fs = [(funcs(s, n), (s, n)) for s in (1, -1) for n in (1, 2)]
54
55
56
57     def make_plot(name='plot', filetype='ps'):
58         f, axarr = plt.subplots(4, sharex=True, figsize=(8, 12))
59         for i in range(4):
60             plt.subplot(4, 1, i+1)
61             ppt(fs[i][0], inits, (-5, 5), (-1.5, 1.5))
62             plt.title('s = {0}, n = {1}'.format(*fs[i][1]))
63             plt.ylabel('x')
64             plt.setp([a.get_xticklabels() for a in f.axes[:-1]], visible=False)
65             plt.xlabel('t')
66             plt.tight_layout()
67             plt.savefig(name+'.'+filetype, dpi=100)

```