

**MATH 271.2 E, F**  
**Problem Set #1**

**DUE: 10 Jun 2024**  
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**General Instructions:** *Show all pertinent and relevant solutions. Answers do not magically appear in papers. So do not give them without solutions or explanations. Submit your problem set (as **.pdf** file) and codes (as **.R** or **.Rmd** file) via Canvas on or before June 10, 2024, 23:59. GOODLUCK!*

1. Let  $S_t$  be the sales at time  $t$  for the gadget IG-11, with the data in `Item2.csv`. Using  $X_t = \ln S_t$ , do the following in R. **[25pts]**
  - (a) Is the data stationary? Use appropriate test(s) to justify your answer. If the data is not stationary, perform the necessary transformation to make the data stationary. Verify that the transformed data is indeed stationary.
  - (b) Let  $Y_t$  be the transformed data in (a). Is there serial correlation? Use appropriate test(s) to justify your answer.
  - (c) Generate correlograms of the ACF and PACF of the transformed data  $Y_t$ , and use these to identify one possible  $AR(p)$ , one  $MA(q)$ , and one  $ARMA(p, q)$  model, where  $p$  and  $q$  are both less than or equal to 5. Justify your choices.
  - (d) For each of these models, write down the resulting models in functional form.
  - (e) Given only the three models in (c), which should you choose? Explain.