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## Decision Boundary

In order to get our discrete 0 or 1 classification, we can translate the output of the hypothesis function as follows:

$$\begin{aligned}h_{\theta}(x) &\geq 0.5 \rightarrow y = 1 \\h_{\theta}(x) &< 0.5 \rightarrow y = 0\end{aligned}$$

The way our logistic function  $g$  behaves is that when its input is greater than or equal to zero, its output is greater than or equal to 0.5:

$$\begin{aligned}g(z) &\geq 0.5 \\ \text{when } z &\geq 0\end{aligned}$$

Remember.

$$\begin{aligned}z = 0, e^0 = 1 &\Rightarrow g(z) = 1/2 \\ z \rightarrow \infty, e^{-\infty} &\rightarrow 0 \Rightarrow g(z) = 1 \\ z \rightarrow -\infty, e^{\infty} &\rightarrow \infty \Rightarrow g(z) = 0\end{aligned}$$

So if our input to  $g$  is  $\theta^T X$ , then that means:

$$\begin{aligned}h_{\theta}(x) = g(\theta^T x) &\geq 0.5 \\ \text{when } \theta^T x &\geq 0\end{aligned}$$

From these statements we can now say:

$$\begin{aligned}\theta^T x &\geq 0 \Rightarrow y = 1 \\ \theta^T x &< 0 \Rightarrow y = 0\end{aligned}$$

The **decision boundary** is the line that separates the area where  $y = 0$  and where  $y = 1$ . It is created by our hypothesis function.

**Example:**

$$\theta = \begin{bmatrix} 5 \\ -1 \\ 0 \end{bmatrix}$$

$$y = 1 \text{ if } 5 + (-1)x_1 + 0x_2 \geq 0$$

$$5 - x_1 \geq 0$$

$$-x_1 \geq -5$$

$$x_1 \leq 5$$

In this case, our decision boundary is a straight vertical line placed on the graph where  $x_1 = 5$ , and everything to the left of that denotes  $y = 1$ , while everything to the right denotes  $y = 0$ .

Again, the input to the sigmoid function  $g(z)$  (e.g.  $\theta^T X$ ) doesn't need to be linear, and could be a function that describes a circle (e.g.  $z = \theta_0 + \theta_1 x_1^2 + \theta_2 x_2^2$ ) or any shape to fit our data.

✓ 完成

