

Induce Pedagogical Strategy Using Reinforcement Learning

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591/791: ML for User Adaptive System

March, 2017

Reinforcement Learning in practice

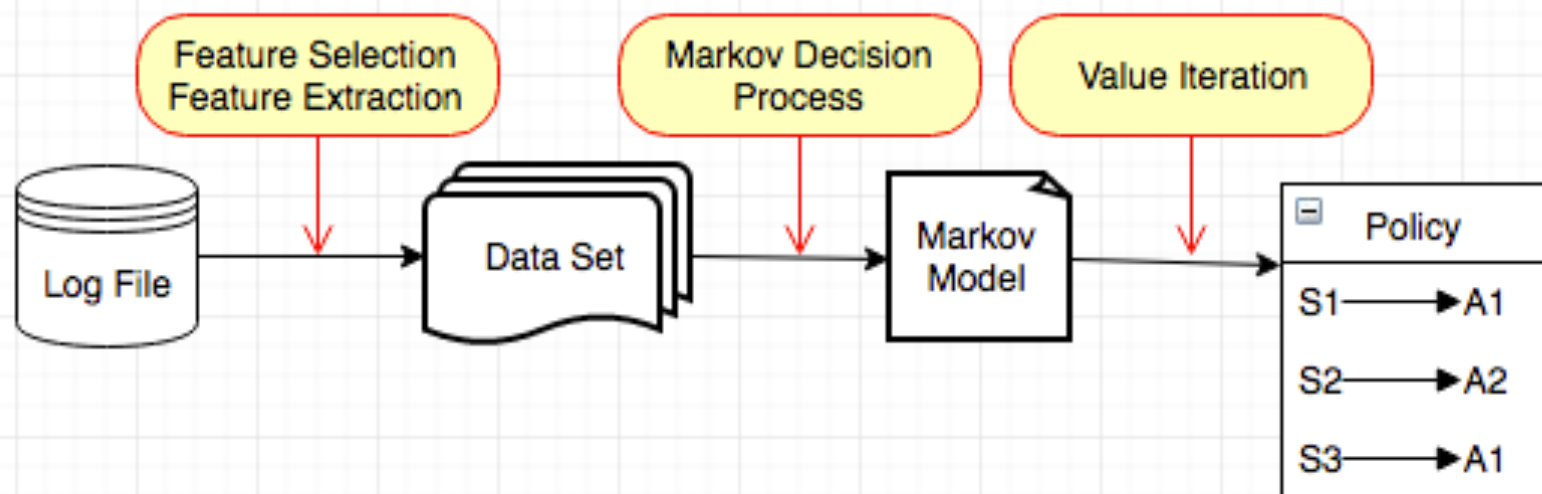
- Induce policy to make Intelligent Tutoring Systems:
 - Adaptive
 - Effective

- Reinforcement Learning in practice:

What is the best **action** for the **agent** (*tutor*)
to take in any **state** (*learning context*)
in order to maximize **reward** (*student learning*)

- Real dataset
- Including all the necessary steps for RL project

Process



Markov Decision Processes (MDPs)

$S = \{S_1, \dots, S_n\}$ state space;

Student Competence, Concept Difficulty

$A = \{A_1, \dots, A_m\}$ action space;
{Elicit, Tell}

R : reward

Student Learning Gain

T : is a set of transition probabilities between states.

Output:

$\pi: S \rightarrow A$ is defined as a policy.

An Example Log File

Pretest =0

t1	T: Which principle will help you calculate the KE of the rock?
t2	S: Definition of energy.
t3	T: No, we should apply the Definition of Kinetic Energy
t4	T: Please write the equation....
t5	S: KE=0.5*m*v1^2
t6	T: Go ahead calculate the equation.
t7	S: 0.5*0.6kg*2.0 m/s^2 = 1.2 J
...	
t423	T: Since the kinetic energy...

Posttest =0.8

NO **State:**

Action: *{Elicit, Tell}*

Reward:

t1	T: Which principle will help you calculate the KE of the rock?	Elicit
t2	S: Definition of energy.	
t3	T: No, we should apply the Definition of Kinetic Energy	
t4	T: Please write the equation....	Elicit
t5	s: $KE = 0.5 * m * v^2$	
t6	T: Go ahead calculate the equation.	Elicit
t7	S: $0.5 * 0.6kg * 2.0 m/s^2 = 1.2 J$	
...		
t423	T: Since the kinetic energy...	Tell

Posttest =0.8

State feature:

Student Competence

Pretest =0

t1	T: Which principle will help you calculate the KE of the rock?	Elicit
t2	S: Definition of energy.	✗
t3	T: No, we should apply the Definition of Kinetic Energy	
t4	T: Please write the equation....	Elicit
t5	S: $KE = 0.5 * m * v^2$	✓
t6	T: Go ahead calculate the equation.	Elicit
t7	S: $0.5 * 0.6 \text{ kg} * 2.0 \text{ m/s}^2 = 1.2 \text{ J}$	✓
...		
t423	T: Since the kinetic energy...	Tell

Posttest =0.8

Pretest =0

t1	T: Which principle will help you calculate the KE of the rock?	Elicit
t2	S: Definition of energy.	✗
t3	T: No, we should apply the Definition of Kinetic Energy	
t4	T: Please write the equation....	Elicit
t5	S: $KE = 0.5 * m * v^2$	✓
t6	T: Go ahead calculate the equation.	Elicit
t7	S: $0.5 * 0.6 \text{ kg} * 2.0 \text{ m/s}^2 = 1.2 \text{ J}$	✓
...		
t423	T: Since the kinetic energy...	Tell

Posttest =0.8

Number of Correct

Pretest =0

t1	T: Which principle will help you calculate the KE of the rock?	Elicit
t2	S: Definition of energy.	✗
t3	T: No, we should apply the Definition of Kinetic Energy	
t4	T: Please write the equation....	Elicit
t5	s: $KE = 0.5 * m * v^2$	✓
t6	T: Go ahead calculate the equation.	Elicit
t7	S: $0.5 * 0.6 \text{ kg} * 2.0 \text{ m/s}^2 = 1.2 \text{ J}$	✓
...		
t423	T: Since the kinetic energy...	Tell

0

0

1

...

55

Posttest =0.8

Number Correct → Student Competence

if ≤ 40 , *Low*; otherwise, *High*

t1	T: Which principle will help you calculate the KE of the rock?	Elicit	0	Low
t2	S: Definition of energy.			
t3	T: No, we should apply the Definition of Kinetic Energy			
t4	T: Please write the equation....	Elicit	0	Low
t5	S: $KE=0.5*m*v1^2$			
t6	T: Go ahead calculate the equation.	Elicit		
t7	S: $0.5*0.6kg*2.0\text{ m/s}^2 = 1.2\text{ J}$		1	Low
...				
...				
t423	T: Since the kinetic energy...	Tell	55	High

Posttest =0.8

State: Student Competence {*Low, High*}

t1	T: Which principle will help you calculate the KE of the rock?	Elicit
t2	S: Definition of energy.	
t3	T: No, we should apply the Definition of Kinetic Energy	
t4	T: Please write the equation....	Elicit
t5	S: $KE = 0.5 * m * v^2$	
t6	T: Go ahead calculate the equation.	Elicit
t7	S: $0.5 * 0.6 \text{ kg} * 2.0 \text{ m/s}^2 = 1.2 \text{ J}$	
...		
t423	T: Since the kinetic energy...	Tell

Low

Low

Low

...

High

Posttest = 0.8

State: Student Competence {*Low, High*}

Action: {*Elicit, Tell*}

Reward:

t1	T: Which principle will help you calculate the KE of the rock?	Elicit
t2	S: Definition of energy.	
t3	T: No, we should apply the Definition of Kinetic Energy	
t4	T: Please write the equation....	Elicit
t5	S: $KE=0.5*m*v1^2$	
t6	T: Go ahead calculate the equation.	Elicit
t7	S: $0.5*0.6kg*2.0\text{ m/s}^2 = 1.2\text{ J}$	
...		
t423	T: Since the kinetic energy...	Tell

Posttest =0.8

Low

↓ Elicit

Low

↓ Elicit

Low

↓ Elicit

...

High

⊥ Tell

Reward: Normalized Learning Gain (NLG) X100

Pretest =0

t1	T: Which principle will help you calculate the KE of the rock?	Elicit
t2	S: Definition of energy.	
t3	T: No, we should apply the Definition of Kinetic Energy	
t4	T: Please write the equation....	Elicit
t5	S: $KE=0.5*m*v1^2$	
t6	T: Go ahead calculate the equation.	Elicit
t7	S: $0.5*0.6kg*2.0\text{ m/s}^2 = 1.2\text{ J}$	
...		
t423	T: Since the kinetic energy...	Tell

Posttest =0.8

$$NLG = \frac{\text{Posttest} - \text{Pretest}}{1 - \text{Pretest}}$$

$$\begin{aligned} & NLG \times 100 \\ &= \frac{0.8 - 0}{1 - 0} \times 100 = 80 \end{aligned}$$

State: Student Competence {*Low, High*}

Action: {*Elicit, Tell*}

Reward: NLG \times 100

t1	T: Which principle will help you calculate the KE of the rock?	Elicit
t2	S: Definition of energy.	
t3	T: No, we should apply the Definition of Kinetic Energy	
t4	T: Please write the equation....	Elicit
t5	S: $KE=0.5*m*v1^2$	
t6	T: Go ahead calculate the equation.	Elicit
t7	S: $0.5*0.6kg*2.0\text{ m/s}^2 = 1.2\text{ J}$	
...		
t423	T: Since the kinetic energy...	Tell

Posttest =0.8

Low

↓ Elicit,0

Low

↓ Elicit,0

Low

↓ Elicit,0

...

High

⊥ Tell,80

One student's Log File → One Trajectory

Low $\xrightarrow{\text{Elicit, 0}}$ *Low* $\xrightarrow{\text{Elicit, 0}}$ *Low* $\xrightarrow{\text{Elicit, 0}}$ *High* $\xrightarrow{\text{Tell, 80}}$ •

Training Dataset → Trajectories

Low $\xrightarrow{\text{Elicit, 0}}$ *Low* $\xrightarrow{\text{Elicit, 0}}$ *Low* $\xrightarrow{\text{Elicit, 0}}$ *High* $\xrightarrow{\text{Tell, 80}}$ •

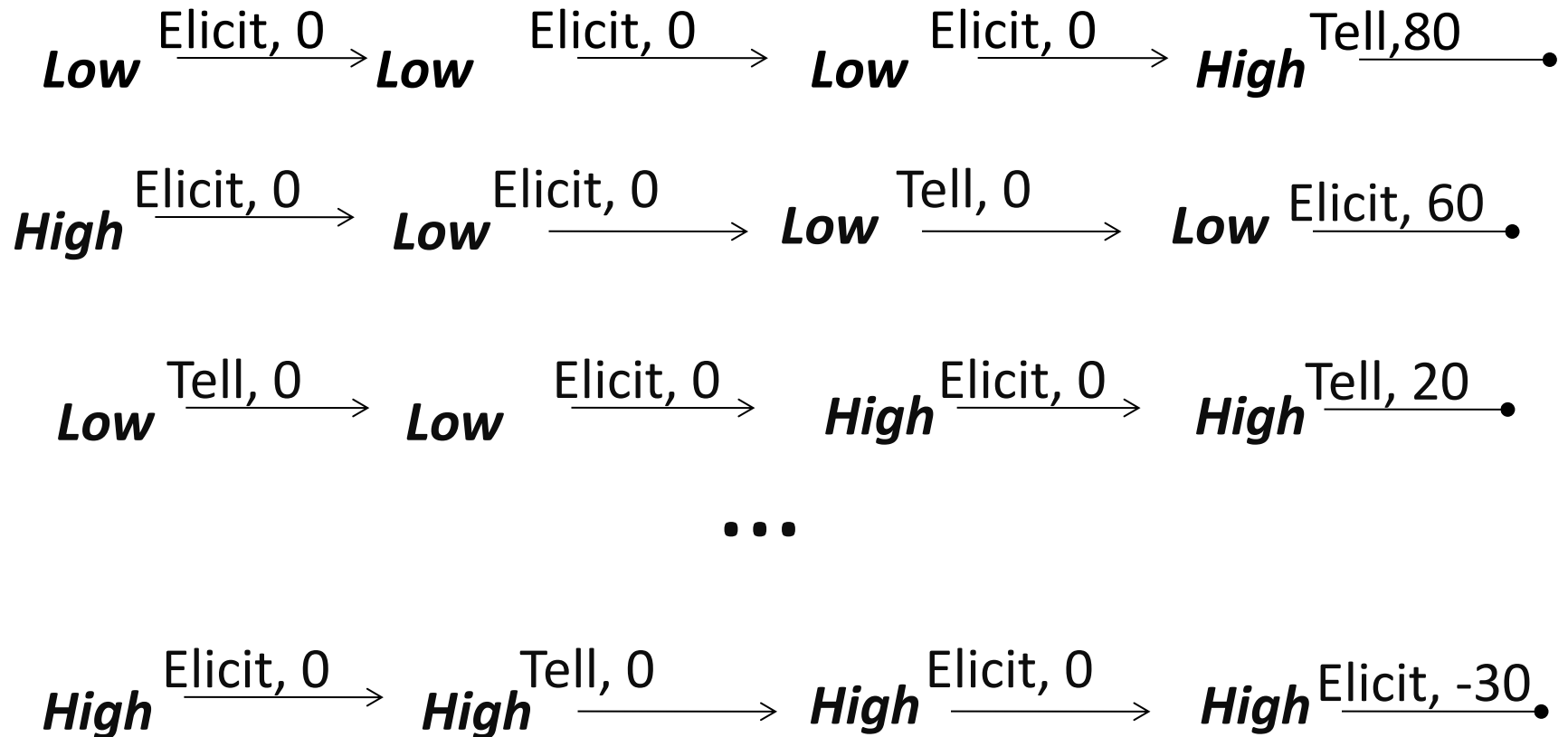
High $\xrightarrow{\text{Elicit, 0}}$ *Low* $\xrightarrow{\text{Elicit, 0}}$ *Low* $\xrightarrow{\text{Tell, 0}}$ *Low* $\xrightarrow{\text{Elicit, 60}}$ •

Low $\xrightarrow{\text{Tell, 0}}$ *Low* $\xrightarrow{\text{Elicit, 0}}$ *High* $\xrightarrow{\text{Elicit, 0}}$ *High* $\xrightarrow{\text{Tell, 20}}$ •

...

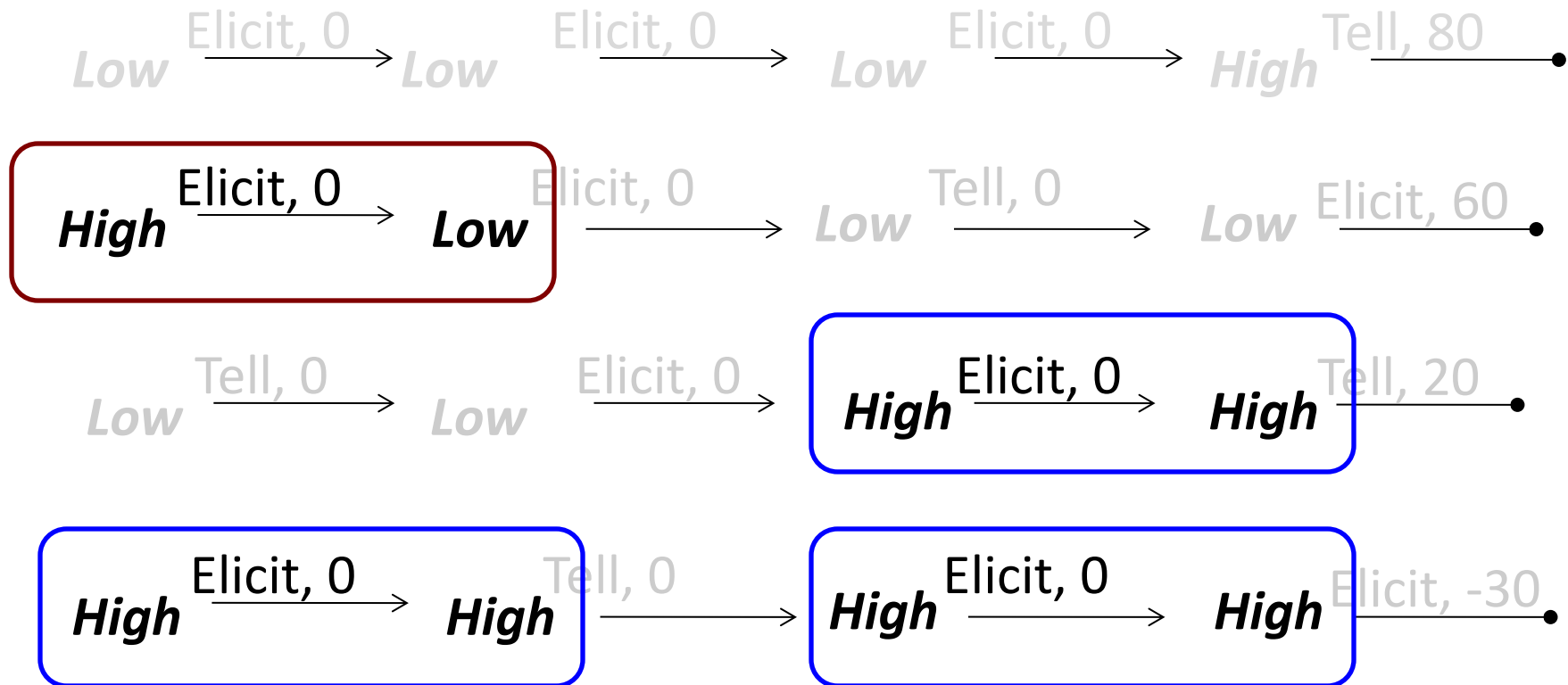
High $\xrightarrow{\text{Elicit, 0}}$ *High* $\xrightarrow{\text{Tell, 0}}$ *High* $\xrightarrow{\text{Elicit, 0}}$ *High* $\xrightarrow{\text{Elicit, -30}}$ •

Training Dataset → Trajectories



Transition Probabilities **T** estimated from
Training Dataset.

An Example of $P(\text{Low}|\text{High}, \text{Elicit})$



$$P(\text{Low}|\text{High}, \text{Elicit}) = \frac{\# \text{High} \xrightarrow{\text{Elicit}} \text{Low}}{\# \text{High} \xrightarrow{\text{Elicit}} \text{Low} + \# \text{High} \xrightarrow{\text{Elicit}} \text{High}} = \frac{1}{4}$$

An Example **Single-feature** Policy

$\langle Low \rangle \rightarrow Tell$
 $\langle High \rangle \rightarrow Elicit$

Two state features:

Competence; **Difficulty**

4 states:

{<Low, **Easy**>, <Low, **Difficult**>,
<High, **Easy**>, <High, **Difficult**>}

t3	T: No, we should apply the Definition of Kinetic Energy	
t4	T: Please write the equation....	Elicit
t5	s: $KE=0.5*m*v1^2$	
t6	T: Go ahead calculate the equation.	Elicit
t7	S: $0.5*0.6kg*2.0\text{ m/s}^2 = 1.2\text{ J}$	
...		
t423	T: Since the kinetic energy...	Tell

Posttest =0.8

ile

<Low, **Easy**>

↓ Elicit, 0

<Low, **Difficult**>

↓ Elicit, 0

<Low, **Easy**>

↓ Elicit, 0

<High, **Difficult**>

⊥ Tell, 80

A Two-Feature Policy Example

$\langle Low, Easy \rangle$	\rightarrow	<i>Elicit</i>
$\langle High, Difficult \rangle$	\rightarrow	<i>Elicit</i>
$\langle High, Easy \rangle$	\rightarrow	<i>Tell</i>
$\langle Low, Difficult \rangle$	\rightarrow	<i>Tell</i>

Value Iteration

1. Initial value of each state: $V(s)$

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1. Initial value of each state: $V(s)$
2. Update each state's $V(s)$ using neighboring $V(s')$ s:

$$V(s) = \max_a \sum_{s'} P(s'|s, a) [R(s, a, s') + \gamma \cdot V(s')]$$

**Probability of
landing on a
neighboring state.**

**Reward/Cost of going
to the neighboring
state.**

**Value of the
neighboring state**

Value Iteration

1. Initial value of each state: $V(s)$
2. Update each state's $V(s)$ using neighboring $V(s')$ s:

$$V(s) = \max_a \sum_{s'} P(s'|s, a) [R(s, a, s') + \gamma \cdot V(s')]$$

**Probability of
landing on a
neighboring state.**

**Reward/Cost of going
to the neighboring
state.**

**Value of the
neighboring state**

3. Induce the policy:

$$\pi(s) = \operatorname{argmax}_a \sum_{s'} P(s'|s, a) [R(s, a, s') + \gamma \cdot V(s')]$$

**For any state s , take an action to
the neighboring s' with highest $V(s')$**

γ :: Discount factor 0.9.

Adapted from: Sutton & Barto (1998)

Purpose

- Induce policy to make Intelligent Tutoring System:
 - Adaptive: **Feature Discretization/Selection/Extraction**
 - Effective: **ECR**
- Reinforcement Learning in practice:
 - What is the best **action** for the **agent** (*tutor*)
to take in any **state** (*learning context*)
in order to maximize **reward** (*student learning*)
 - Real dataset
 - Including all the necessary steps for RL project.

Policy Evaluation

- Expected Cumulative Reward (Tetreault, 2006)

$$ECR = \sum_{i=1}^m \frac{N_i}{N_1 + N_2 + \dots + N_m} \times V^{\pi}(S_i)$$

Where S_i is the starting state, N_i is the times that S_i exists as starting state

- The higher ECR of the policy means the better policy

Shitian's Work

Deep Thought (Dr. Barnes, 2015)

- A rule-based tutoring system for teaching logic proof problems
- Student solves 1-3 problems per level (Total 6 levels)
- Level score ($LevelScore_i, i \in [1,6]$) is given for each student based on his/her performance on the last problem in the level i

Problem Solving

1: $A \rightarrow (B \wedge C)$ 2: $A \vee D$ 3: $\neg D \wedge E$

Level: 1/6
Problem: 1/3

Problem Code: 1.0.1.0

C: ? B

Rules

MP ?
Modus Ponens

MT ?
Modus Tollens

DS ?
Disjunctive Syllogism

Add ?
Addition

Simp ?
Simplification

Conj ?
Conjunction

HS ?
Hypothetical Syllogism

CD ?
Constructive Dilemma

Hypothetical Syllogism

$p \rightarrow q$
 $q \rightarrow r$
 $\swarrow \searrow$
 $p \rightarrow r$

$q \rightarrow r$ $p \rightarrow q$
 $\swarrow \searrow$
 $p \rightarrow r$

Commutative

Assocative

Dist ?
Distributive

Abs ?
Absorption

Exp ?
Exportation

Taut ?
Tautology

	Expression	Antecedent Lines	Rule Used
1	$A \rightarrow (B \wedge C)$		Given
2	$A \vee D$		Given
3	$\neg D \wedge E$		Given

	For	Type	For	Type
C	$A \wedge B$	$A * B$	$A \rightarrow B$	$A > B$
B	$A \vee B$	$A + B$	$A \leftrightarrow B$	$A = B$
	$\neg A$	$\neg A$		

Message Box

No blocks selected. Rule requires two justified premises

☒ Symbolic ☐ English

Delete Node

Change to Indirect Proof

Restart Current Problem

Skip Current Problem

Deep Thought

A Logic Proof Tutor

Version 2.0

August 15, 2014

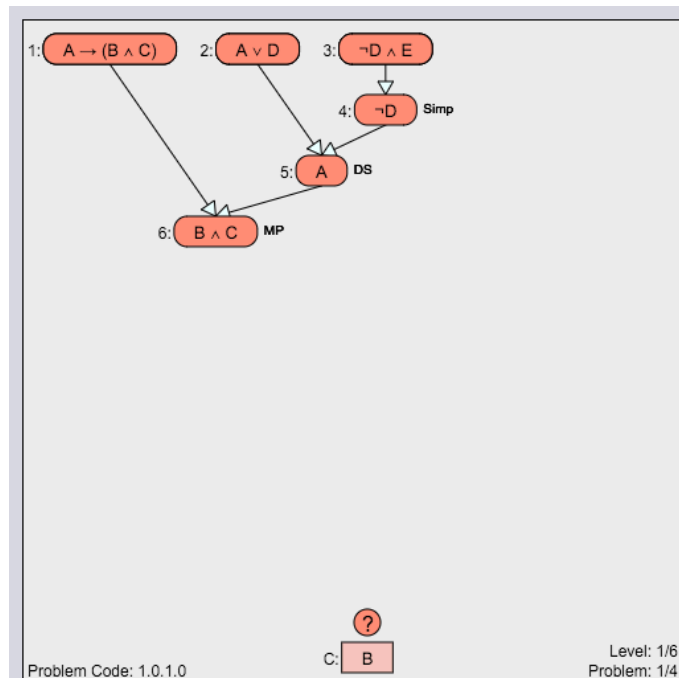
North Carolina State University

Instructions

Window Information

Contact/Version Information

Work Example



Extract B from 6 using Simp

Message Box

EXAMPLE

Click the arrow next to the Hint Box to step through the example.

Representation

☒ Symbolic ☐ English

	Expression	Antecedent Lines	Rule Used
1	$A \rightarrow (B \wedge C)$		Given
2	$A \vee D$		Given
3	$\neg D \wedge E$		Given
4	$\neg D$	3	Simplification
5	A	2, 4	Disjunctive Syllogism
6	$B \wedge C$	1, 5	Modus Ponens

C B

For

$A \wedge B$

$A \vee B$

$\neg A$

Type

$A \wedge B$

$A \vee B$

$\neg A$

For

$A \rightarrow B$

$A \leftrightarrow B$

$A = B$

Type

$A \wedge B$

$A \vee B$

$A = B$

Deep Thought

A Logic Proof Tutor

Version 6

January 19, 2016

North Carolina State University

Instructions

Window Information

Contact/Version Information

Deep Thought Data Sets

- Total 303 students
- Average time spend in tutor is 416.60 minutes
- Total 4 categories and 124 features
- Action set
 - should it ask student to solve the next problem (PS)
 - should it provide an example to show the student how to solve the next problem (WE)

Four categories: 124 State Features

- **Autonomy:** the amount of work done by the student
 - PSCount,
 - PercPS
- **Temporal Situation:** the time related information about the work process
 - TotalTime,
 - avgPSTime,
- **Student Action:** the statistical measurement of student's behavior
 - AppCount,
 - hintCount
- **Performance:** Students' performance on current problem
 - ruleScore,
 - wrongApp

Feature Discretization

- Median split

TotalTime [0: ≤ 172.34 , 1: > 172.34]

avgTime [0: ≤ 6.25 , 1: > 6.25]

hint [0: ≤ 0.04 , 1: > 0.04]

- Kmeans

- Data points didn't uniformly distribute
- Particular data points may group together
- Avoid unbalanced clustering

CurrPro_NumProbRule [0: close to 4.1, 1: close to 6.4]

Feature-Selection: Correlation Metrics

Given labeled data, we can compute some simple score $S(i)$ that measures how informative each feature X is about class labels Y .

- Chi-square (CHI) (Zibran, 2007)

$$\chi^2 = \sum_i \frac{(X_i - Y_i)^2}{Y_i}$$

- Information Gain (IG) (C. Lee, 2010)

$$IG(X, Y) = H(Y) - H(Y|X)$$

Feature-Selection: Correlation Metrics

- Information Gain Ratio (IGR) (J. T. Kent, 1983)

$$IGR(X, Y) = \frac{H(Y) - H(Y|X)}{H(X)}$$

- Symmetric Uncertainty (SU) (L. Yu, H. Liu, 2003)

$$SU(X, Y) = \frac{H(Y) - H(Y|X)}{H(X) + H(Y)}$$

- Weighted Information Gain (WIG) (We proposed)

$$WIG(X, Y) = \frac{H(Y) - H(Y|X)}{(H(X) + H(Y))H(X)}$$

Correlation-based Feature Selection Methods

- Feature Selection for model-based RL
- Apply correlation between current optimal feature set and potential feature as the feature selection criteria
- Forward feature selection strategy

10 Correlation-based Methods

- Explore both high and low correlation
- Obtain 10 correlation-based feature selection methods (5 correlation metrics \times 2 correlation types)

	High	Low
CHI	CHI-High	CHI-Low
IG	IG-High	IG-Low
IGR	IGR-High	IGR-Low
SU	SU-High	SU-Low
WIG	WIG-High	WIG-Low

Correlation-based Methods: Algorithm

Algorithm

Require: Ω : Feature Space; \mathcal{D} : Training Data;
 \mathcal{N} : Maximum Number of Selected Features;

Ensure: \mathcal{S}^* : Optimal Feature Set

```

1:  for  $f_i$  in  $\Omega$  do
2:     $ECR_i \leftarrow \text{CalculateECR}(\mathcal{D}, f_i)$ 
3:  end for
4:  Add  $f^*$  with highest  $ECR$  to  $\mathcal{S}^*$ 

```

```

5:  while  $SIZE(\mathcal{S}^*) < \mathcal{N}$  do

```

```

6:    for  $f_i$  in  $\Omega - \mathcal{S}^*$  do
7:       $C_i \leftarrow \text{CalculateCORRELATION}(\mathcal{S}^*, f_i, m)$ 
8:    end for
9:     $\mathcal{F} \leftarrow \text{SelectTop}(C, 5, \text{reverse})$ 

```

```

10:   for  $f_i$  in  $\mathcal{F}$  do
11:      $ECR_i \leftarrow \text{CalculateECR}(\mathcal{D}, \mathcal{S}^* + f_i)$ 
12:   end for
13:   Replace  $\mathcal{S}^*$  by  $\mathcal{S}^* + f_i$  with highest  $ECR$ 
14: end while

```

Initialization

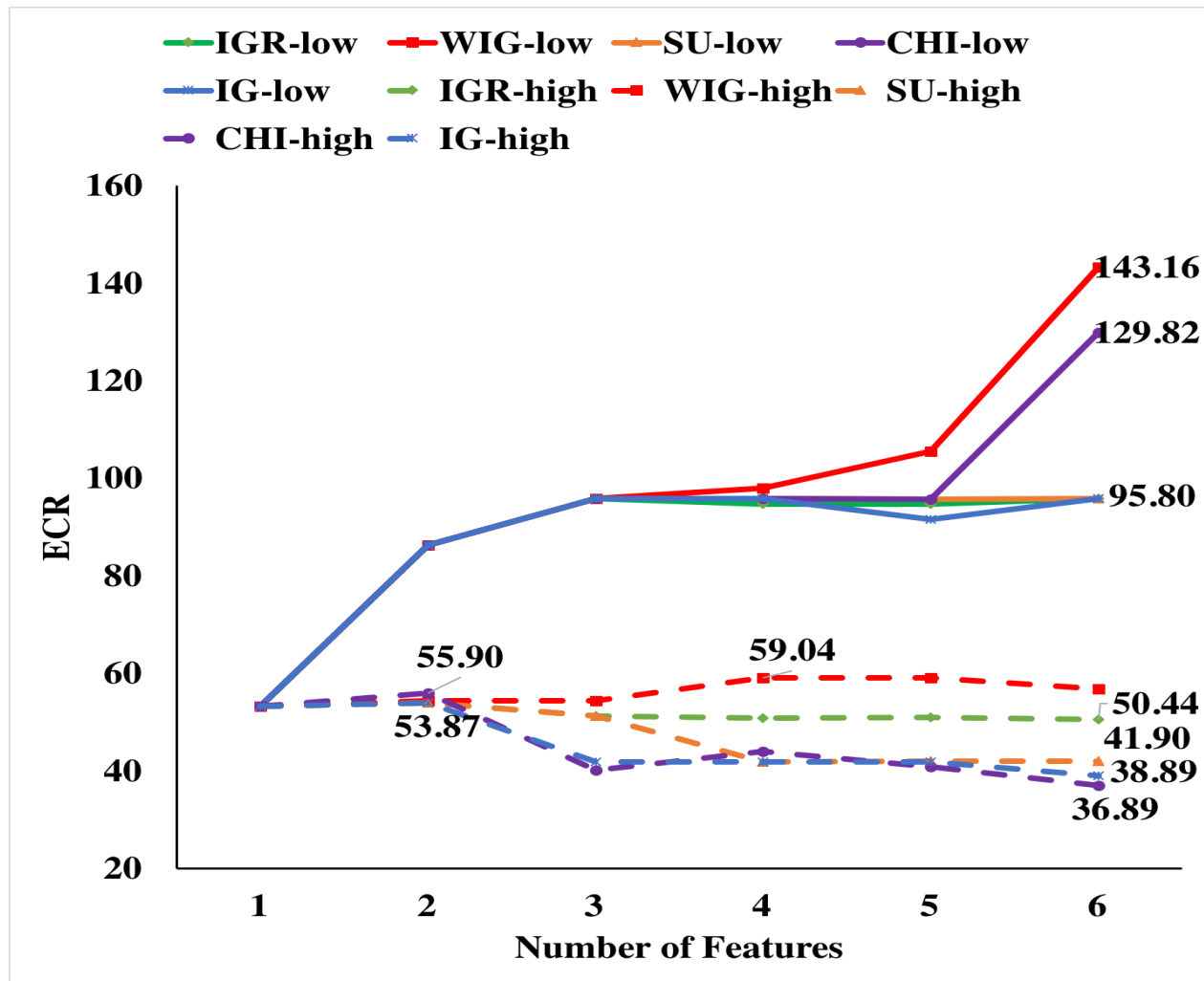
Feature
Selection

Updating
Feature Set

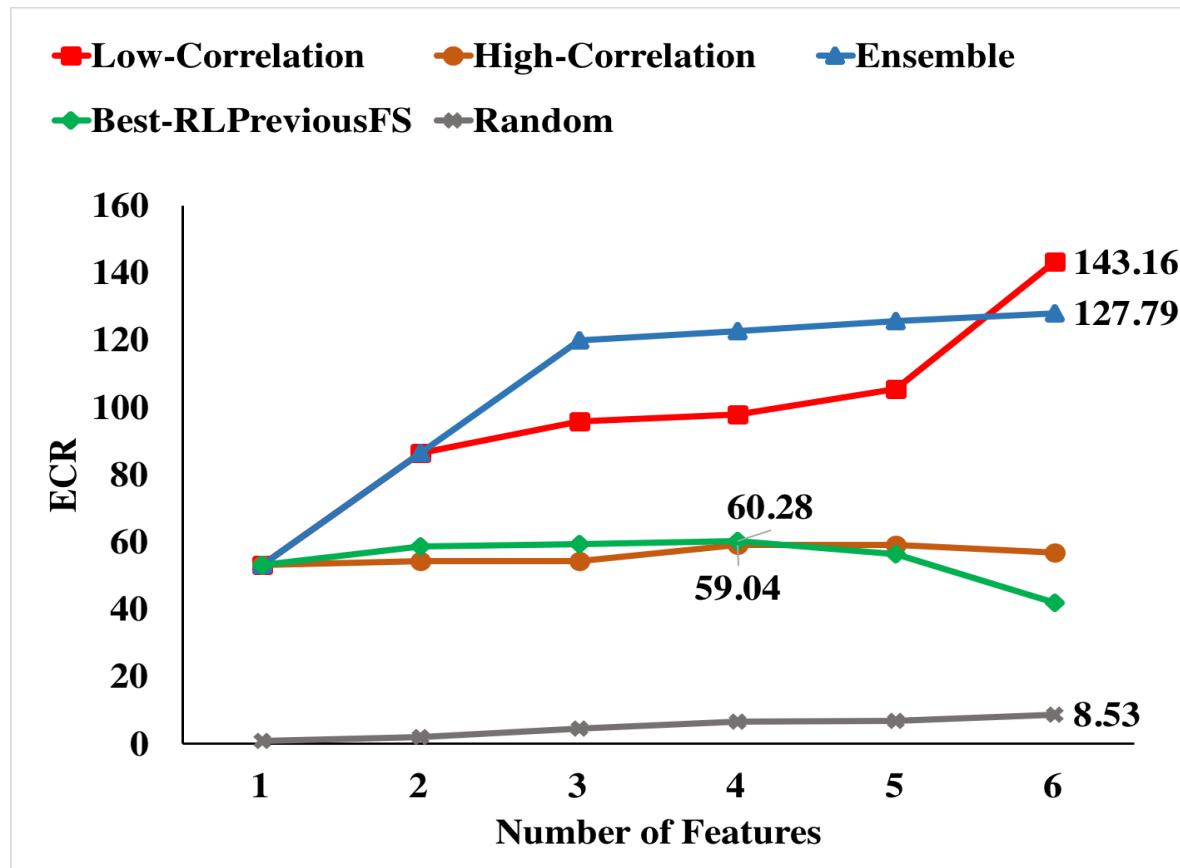
Ensemble Methods

- Integrate multiple selection methods
- 10 correlation-based methods
- 4 other RL based methods

Result: High vs Low correlation

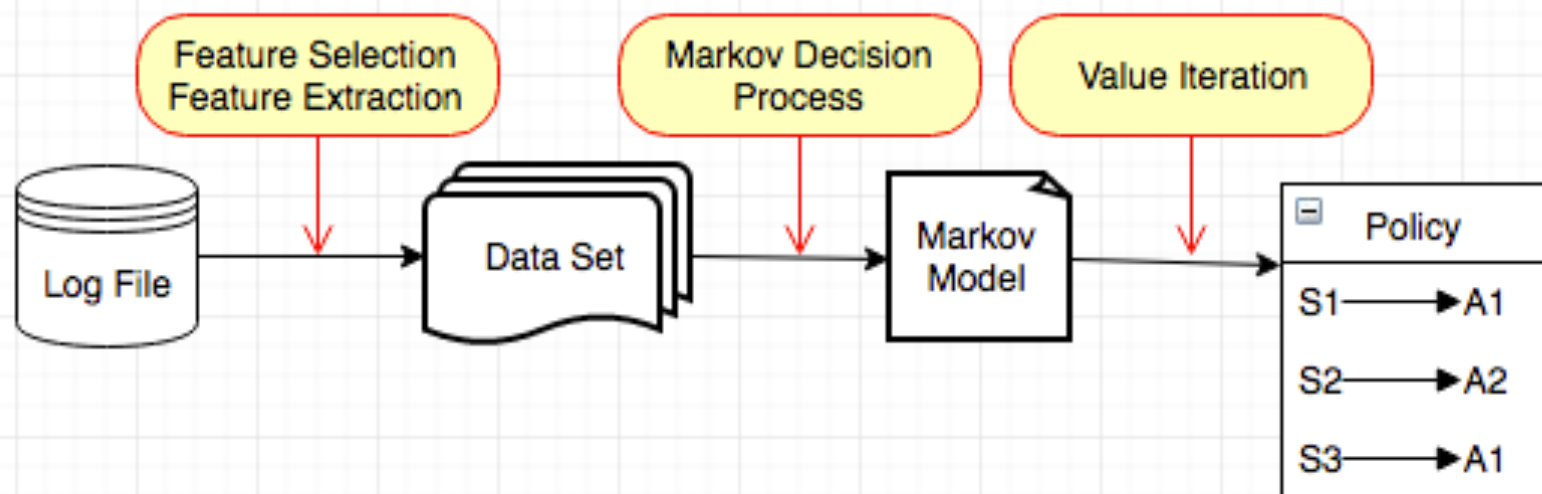


Results: Overall Evaluation

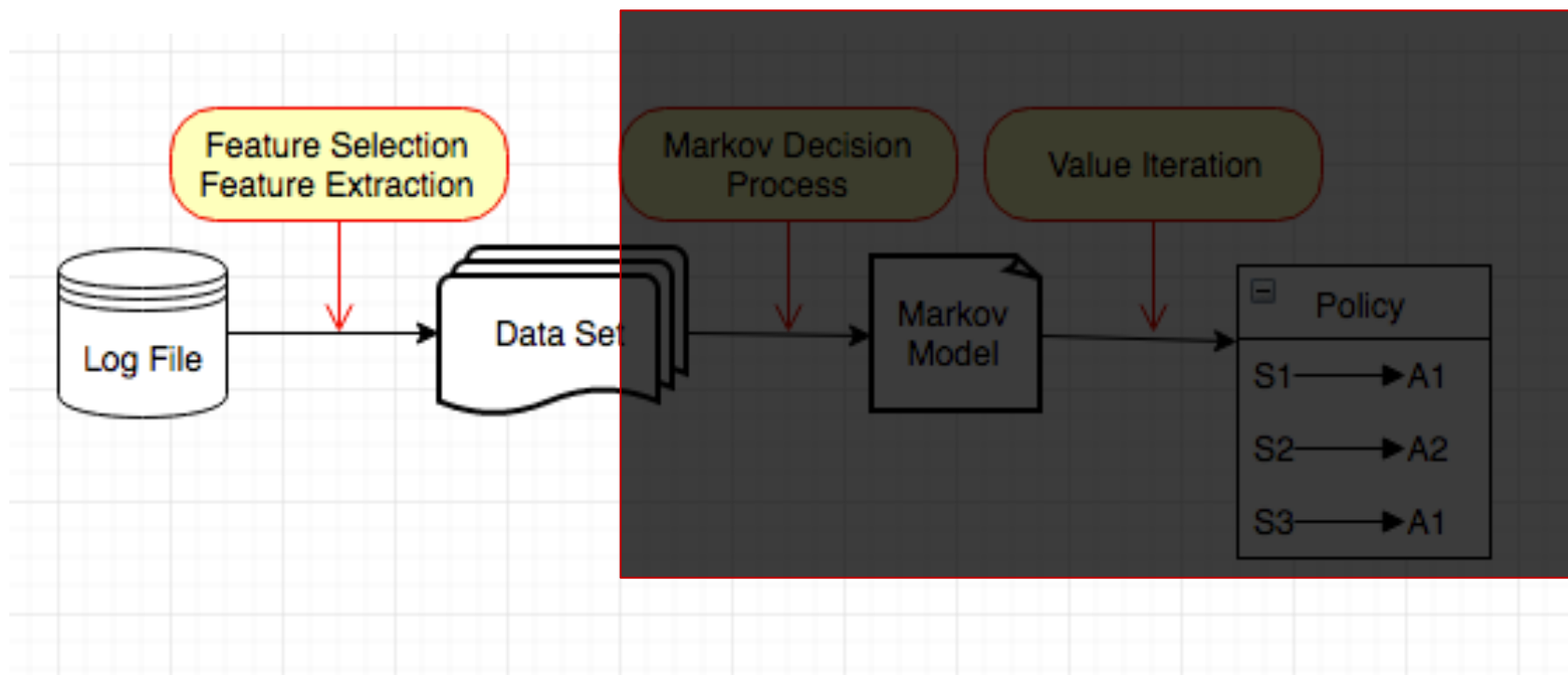


The Assigned Project:

Process



Process



Goals for Feature Selection or Extraction

- Representing interactive environment effectively (Maximize ECR)
- Please Note:
 - Discrete features
 - Maximum feature size is 8

Suggestion: Discretization Procedure

- Feature Selection
 - Discretize features first
 - Explain how to discretize features in report
 - Keep the original names of selected features
- Feature Extraction
 - Not necessary to discretize features first
 - Explain how to extract features in report
 - Get a new name the extracted features: f1, f2....

To run MDP package, all features must be discretized.

Suggested: Feature Selection

- Discrete features (median split, distribution)
- Filtering approach
 - Design a ranking function and select top n features
 - ECR of each single-feature policy
- Forward feature selection
 - Good selection strategy
 - Use ECR as a selection standard
 - Maintain a limited search space
 - Apply correlation, mutual information gain as the condition

Try other methods.

Additional points for exploring novel methods.

Suggested: Feature Extraction

- PCA
 - How to deal with discrete features
 - Factor analysis of mixed data (FAMD)
- Fuzzy Clustering
 - Data point can belong to multiple clusters
 - Specify distance function, handling continuous and discrete features
- Autoencoder
 - Do Not recommend
- Output Discrete Features
 - Explain how to extract features in report
 - Transfer extracted features into discrete ones

Suggested: Feature Extraction

- Unsupervised feature extraction
- Construct connection between feature extraction with reinforcement learning
- Apply ECR as the condition in the feature extraction process

Markov Decision Process

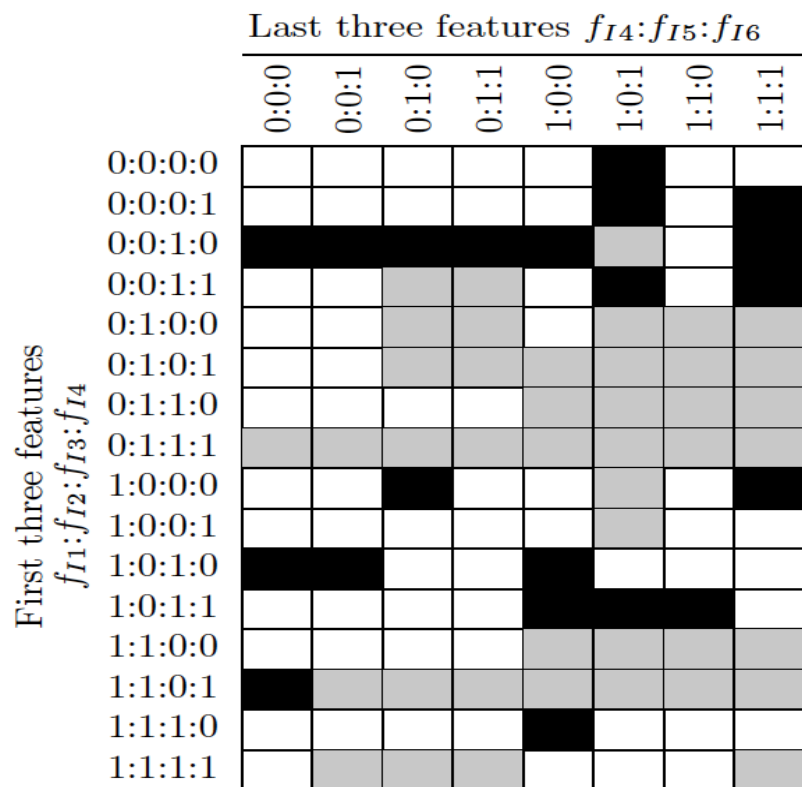
1	student	currProb	course	session	priorTutorAc	reward	Level	probDiff	
2	0006-F14	1.0.1.0	226-001-BAR	1	PS	0	1	0	
3	0006-F14	1.0.2.0	226-001-BAR	1	WE	0	1	0	
4	0006-F14	1.0.3.0	226-001-BAR	1	WE	0	1	0	
5	0006-F14	1.0.4.0	226-001-BAR	1	PS	-94.078947	1	0	
6	0006-F14	2.1.1.0	226-001-BAR	1	PS	0	2	1	
7	0006-F14	2.1.2.0	226-001-BAR	1	WE	0	2	1	
8	0006-F14	2.1.3.0	226-001-BAR	1	PS	161.81004	2	1	
9	0006-F14	3.1.1.0	226-001-BAR	1	WE	0	3	1	
10	0006-F14	3.1.2.0	226-001-BAR	1	WE	0	3	1	
11	0006-F14	3.1.3.0	226-001-BAR	1	PS	-43.265073	3	1	

- States:
 - Level=1, probDiff=0, then state = '1:0',
 - Level=2, probDiff=1, then state = '2:1',
 - Level=3, probDiff=1, then state = '3:1'

Policy Example

```
Policy:
state -> action, value-function
1:0 -> WE, 36.2980141792
2:1 -> PS, 50.6234894691
3:-1 -> WE, 30.7327270058
4:1 -> PS, 38.0276536834
5:1 -> PS, 31.1271670497
6:1 -> PS, 38.7017874912
3:1 -> PS, 37.5870989962
2:-1 -> WE, 28.4686139413
4:-1 -> WE, 26.6276418488
5:-1 -> WE, 26.4065388562
6:-1 -> WE, 0.0
ECR value: 36.2980141792
```

Policy Visualization- For your Presentation

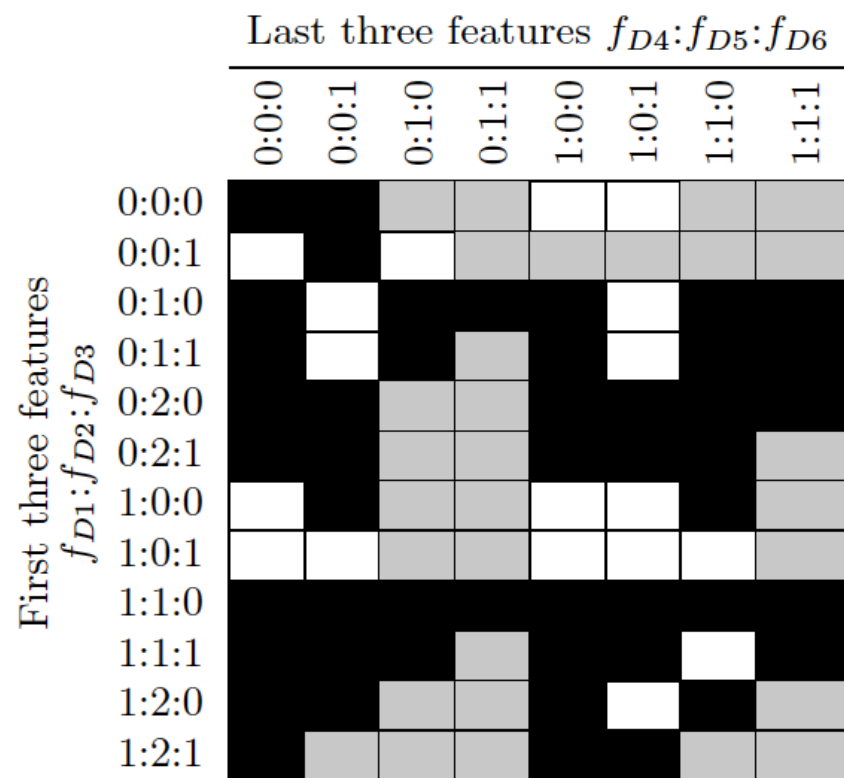


Policy 1

64 rules associated with WE (White)

21 rules associated with PS (Black)

43 no rules (Gray)



Policy 2

18 rules associated with WE

48 rules associated with PS

30 no rules

Demo

Q & A

Thank you !