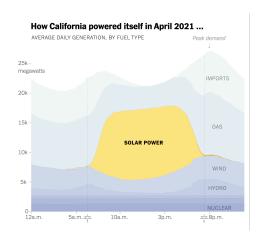
# BATTERY OPERATIONS IN ELECTRICITY MARKETS: STRATEGIC BEHAVIOR AND DISTORTIONS

Jerry Anunrojwong\*

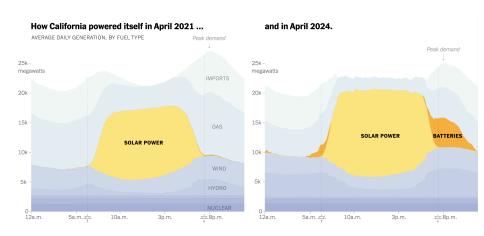
Columbia Business School

<sup>\*</sup>with Santiago R. Balseiro, Omar Besbes, and Bolun Xu

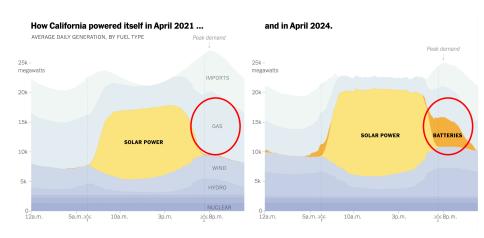
## THE GROWTH OF BATTERIES IN CALIFORNIA



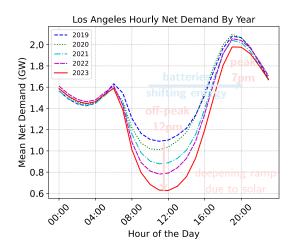
## THE GROWTH OF BATTERIES IN CALIFORNIA



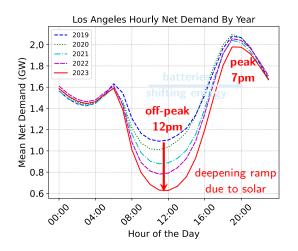
## THE GROWTH OF BATTERIES IN CALIFORNIA



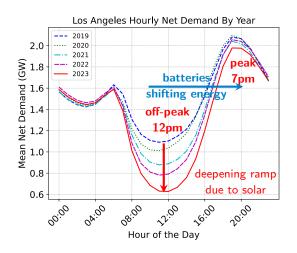
 $\underbrace{\mathsf{net}\;\mathsf{demand}}_{\mathsf{(constant)}} - \underbrace{\underbrace{\mathsf{renewables}}_{\mathsf{(increasing)}}} = \mathsf{conventional}\;\mathsf{generators}$ 



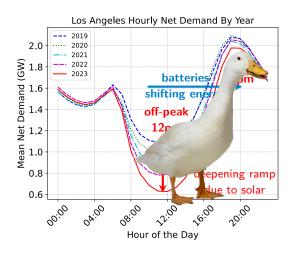
 ${\sf net\ demand} = \underbrace{{\sf system\ demand}}_{({\sf constant})} - \underbrace{{\sf renewables}}_{({\sf increasing})} = {\sf conventional\ generators}$ 



 ${\sf net\ demand} = \underbrace{{\sf system\ demand}}_{({\sf constant})} - \underbrace{{\sf renewables}}_{({\sf increasing})} = {\sf conventional\ generators}$ 



 ${\sf net\ demand} = \underbrace{{\sf system\ demand}}_{({\sf constant})} - \underbrace{{\sf renewables}}_{({\sf increasing})} = {\sf conventional\ generators}$ 



## RESEARCH QUESTIONS

Batteries are no longer price takers, so ...

## How do batteries operate in electricity markets?

How does the strategic behavior of decentralized batteries distort decisions compared to centralized batteries?

Electricity markets are highly complex

Our contribution: a **tractable analytical model** = economic intuition + rich enough to capture salient features.

## RESEARCH QUESTIONS

Batteries are no longer price takers, so ...

## How do batteries operate in electricity markets?

How does the strategic behavior of decentralized batteries distort decisions compared to centralized batteries?

Electricity markets are highly complex.

Our contribution: a tractable analytical model

= economic intuition + rich enough to capture salient features.

### THREE OPERATING REGIMES

## No Battery (NB)

"Status quo" benchmark.

## Centralized Battery (CN)

Minimizing generation cost.

## **Decentralized Battery (DCN)**

Maximizing battery profit.

## ELECTRICITY MARKETS CLEAR IN TWO STAGES

Day-Ahead Market (DA)

based on forecast

- (1) forward market reduces uncertainty
- (2) slow generators take time to start and ramp up

Real-Time Market (RT)

based on realized demand

demand must equal supply at all times

### ELECTRICITY MARKETS CLEAR IN TWO STAGES

Day-Ahead Market (DA)

Real-Time Market (RT)

based on forecast

based on realized demand

(1) forward market reduces uncertainty

demand must equal supply

(2) slow generators take time to start and ramp up

### ELECTRICITY MARKETS CLEAR IN TWO STAGES

Day-Ahead Market (DA)

based on forecast

- (1) forward market reduces uncertainty
- (2) slow generators take time to start and ramp up

Real-Time Market (RT)

based on realized demand

demand must equal supply at all times

## THE BATTERY DECIDES DISCHARGES z IN DA AND RT

# Day-Ahead Market (DA)

# Real-Time Market (RT)

T periods

demand

$$\mathbb{E}[D_1], \dots, \mathbb{E}[D_T]$$

DA demand (forecast)

decisions

$$z_1^{DA}, \dots, z_T^{DA}$$

$$\underbrace{D_1 - \mathbb{E}[D_1], \dots, D_T - \mathbb{E}[D_T]}_{\mathbf{Z} = \mathbf{Z} = \mathbf{$$

RT residual demand

$$z_1^{RT}(\cdot), \dots, z_T^{RT}(\cdot)$$

depending on realized demand history

Discharge (z > 0) or charge (z < 0)

Constraints: net discharge is zero.  $\sum_t z_t^{DA} = \sum_t z_t^{RT} = 0$ 

## THE BATTERY DECIDES DISCHARGES z IN DA AND RT

# Day-Ahead Market (DA)

# Real-Time Market (RT)

T periods

demand

$$\mathbb{E}[D_1], \dots, \mathbb{E}[D_T]$$

DA demand (forecast)

decisions

$$z_1^{DA}, \dots, z_T^{DA}$$

$$\underbrace{D_1 - \mathbb{E}[D_1], \dots, D_T - \mathbb{E}[D_T]}_{}$$

RT residual demand

$$z_1^{RT}(\cdot), \dots, z_T^{RT}(\cdot)$$

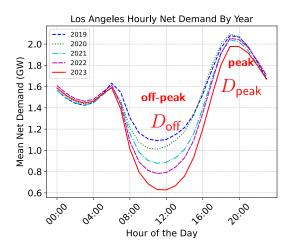
depending on realized demand history

Discharge (z > 0) or charge (z < 0)

Constraints: net discharge is zero.  $\sum_t z_t^{DA} = \sum_t z_t^{RT} = 0$ .

## T=2 Periods Captures the Duck Curve

 $(D_{\mathsf{peak}}, D_{\mathsf{off}}) \sim \pi$ 



Let  $p^{DA} = \mathsf{DA}$  price,  $p^{RT} = \mathsf{RT}$  price.

Assume **two types** of generators:

cost CDF (mass of gens w/ cost 
$$\leq p$$
)

"fast" (DA 
$$+$$
 RT, e.g. gas)

$$C_{s}(p) = l_{s} C(p)$$

$$k_f \equiv$$
 fraction of fast generators

For each time period t,

$$G_s(p_t^{DA})$$

$$+G_f(p_t)$$
 $+G_s(p_t)$ 

$$\mathbb{E}[D_t] - z_t$$

$$-z_t^{DA}$$
 (DA)

Let  $p^{DA} = \mathsf{DA}$  price,  $p^{RT} = \mathsf{RT}$  price.

## Assume two types of generators:

"fast" (DA 
$$+$$
 RT, e.g. gas)

cost CDF (mass of gens w/ cost  $\leq p$ 

$$G_s(p) = (1 - k_f)G(p)$$

$$G_f(p) = k_f G(p)$$

 $k_f \equiv$  fraction of fast generators

For each time period t,

$$G_s(p_t^{DA}) + G_f(p_t^{DA})$$

$$G_s(p_t^{DA}) + G_f(p_t^{RT})$$

supply from "slow" supply from "f

$$\mathbb{E}[D_t] - z_t^{DA} \tag{DA}$$

$$z D_t - z_t^{DA} - z_t^{RT}(\cdot)$$
 (RT)

net demand — battery discharge

Let  $p^{DA} = \mathsf{DA}$  price,  $p^{RT} = \mathsf{RT}$  price.

Assume two types of generators:

cost CDF (mass of gens w/ cost 
$$\leq p$$
)

"fast" (DA 
$$+$$
 RT, e.g. gas)

$$G_s(p) = (1 - k_f)G(p)$$

$$G_f(p) = k_f G(p)$$

 $k_f \equiv$  fraction of fast generators

For each time period t

$$G_s(p_t^{DA}) + G_f(p_t^{DA})$$

$$G_s(p_t^{DA}) + G_f(p_t^{RT})$$

supply from "slow"

upply from "fast"

$$\mathbb{E}[D_t] - z_t^{DA} \tag{DA}$$

$$P_t - z_t^{DA} - z_t^{RT}(\cdot)$$
 (RT)

net demand — battery discharge

Let  $p^{DA} = \mathsf{DA}$  price,  $p^{RT} = \mathsf{RT}$  price.

Assume two types of generators:

cost CDF (mass of gens w/ cost 
$$\leq p$$
)

"fast" (DA 
$$+$$
 RT, e.g. gas)

$$G_s(p) = (1 - k_f)G(p)$$

$$G_f(p) = k_f G(p)$$

 $k_f \equiv$  fraction of fast generators

For each time period t,

$$G_s(p_t^{DA}) + G_f(p_t^{DA})$$

$$+G_f(p_t^{RT})$$

$$= \mathbb{E}[D_t] - z_t^{DA}$$

$$=D_t-z_t^{DA}-z_t^{RI}\left(\cdot\right)$$

supply from "slow"

supply from "fast"

net demand — battery discharge

Let  $p^{DA} = \mathsf{DA}$  price,  $p^{RT} = \mathsf{RT}$  price.

Assume two types of generators:

cost CDF (mass of gens w/ cost 
$$\leq p$$
)

"fast" (DA 
$$+$$
 RT, e.g. gas)

$$G_s(p) = (1 - k_f)G(p)$$

$$G_f(p) = k_f G(p)$$

 $k_f \equiv$  fraction of fast generators

For each time period t,

$$G_s(p_t^{DA})$$
 $G_s(p_t^{DA})$ 

$$+G_f(p_t)$$
  
 $+G_s(n_t^{RT})$ 

$$\mathbb{E}[D_t] - z_t^{DA}$$

This gives prices  $p_t^{DA}$ ,  $p_t^{RT}$  in terms of battery decisions  $z_t^{DA}, z_t^{RT}(\cdot)$ .

(RT)

Let  $p^{DA} = \mathsf{DA}$  price,  $p^{RT} = \mathsf{RT}$  price.

Assume **two types** of generators:

cost CDF (mass of gens w/ cost 
$$\leq p$$
)

"fast" (DA 
$$+$$
 RT, e.g. gas)

$$G_s(p) = (1 - k_f)G(p)$$

$$G_f(p) = k_f G(p)$$

 $k_f \equiv$  fraction of fast generators

For each time period t,

$$G_s(p_t^{DA}) + G_f(p_t^{RT}) + G_f(p_t^{RT})$$

$$= \mathbb{E}[D_t] - z_t^{DA} \tag{}$$

$$= D_t - z_t^{DA} - z_t^{RT}(\cdot) \qquad (RT)$$

supply from "slow"

supply from "fast"

net demand — battery discharge

Let  $p^{DA} = \mathsf{DA}$  price,  $p^{RT} = \mathsf{RT}$  price.

Assume two types of generators:

cost CDF (mass of gens w/ cost 
$$\leq p$$
)

"slow" (DA only, e.g. coal & nuclear) 
$$G_s(p) = (1-k_f)G(p)$$

"fast" (DA 
$$+$$
 RT, e.g. gas)

$$G_f(p) = k_f G(p)$$

 $k_f \equiv \,$  fraction of fast generators

For each time period t,

$$G_s(p_t^{DA})$$
 +  $G_f(p_t^{DA})$  =  $\mathbb{E}[D_t] - z_t^{DA}$  (DA)

$$G_s(p_t^{DA}) + G_f(p_t^{RT}) = D_t - z_t^{DA} - z_t^{RT}(\cdot)$$
 (RT)

supply from "slow"

supply from "fast"

 ${\sf net\ demand-battery\ discharge}$ 

Let  $p^{DA} = DA$  price,  $p^{RT} = RT$  price.

Assume **two types** of generators:

cost CDF (mass of gens w/ cost 
$$\leq p$$
)

"slow" (DA only, e.g. coal & nuclear) 
$$G_s(p) = (1 - k_f)G(p)$$

$$G_f(p) = k_f G(p)$$

 $k_f \equiv$  fraction of fast generators

For each time period t,

$$G_s(p_t^{DA}) + G_f(p_t^{DA}) = \mathbb{E}[D_t] - z_t^{DA}$$

$$G_s(p_t^{DA}) + G_f(p_t^{RT}) = D_t - z_t^{DA} - z_t^{RT}(\cdot)$$
(RT)

supply from "slow" supply from "fast" net demand — battery discharge

## GENERATION COST FROM DA+RT SUPPLY CURVES

Slow generators clear in DA at price  $p_t^{DA}$ .

Fast generators clear in RT at price  $p_t^{RT}$ .

$$\text{generation cost} = \sum_t \left( \int_{p \leq p_t^{DA}} p dG_s(p) + \mathbb{E}\left[ \int_{p \leq p_t^{RT}} p dG_f(p) \right] \right)$$

**Centralized** battery chooses  $z^{DA}, z^{RT}(\cdot)$  to minimize this cost

## GENERATION COST FROM DA+RT SUPPLY CURVES

Slow generators clear in DA at price  $p_t^{DA}$ .

Fast generators clear in RT at price  $p_t^{RT}$ .

$$\text{generation cost} = \sum_t \left( \int_{p \leq p_t^{DA}} p dG_s(p) + \mathbb{E}\left[ \int_{p \leq p_t^{RT}} p dG_f(p) \right] \right)$$

**Centralized** battery chooses  $z^{DA}, z^{RT}(\cdot)$  to minimize this cost

## GENERATION COST FROM DA+RT SUPPLY CURVES

Slow generators clear in DA at price  $p_t^{DA}$ .

Fast generators clear in RT at price  $p_t^{RT}$ .

$$\text{generation cost} = \sum_t \left( \int_{p \leq p_t^{DA}} p dG_s(p) + \mathbb{E}\left[ \int_{p \leq p_t^{RT}} p dG_f(p) \right] \right)$$

**Centralized** battery chooses  $z^{DA}, z^{RT}(\cdot)$  to minimize this cost.

### BATTERY PROFIT - FROM ENERGY ARBITRAGE

**Decentralized** battery chooses  $z^{DA}, z^{RT}(\cdot)$  to maximize profit:

$$\text{profit} = p_{\text{peak}}^{DA} \, z_{\text{peak}}^{DA} + p_{\text{off}}^{DA} \, z_{\text{off}}^{DA} + \mathbb{E} \left[ p_{\text{peak}}^{RT} \, z_{\text{peak}}^{RT} + p_{\text{off}}^{RT} \, z_{\text{off}}^{RT} \right]$$

- forward markets
  - Allaz and Vila (1993), Ito and Reguant (2016), You et al. (2019)
- batteries and renewables operations
  - investments, locations, intermittency, ownership models, ...
  - Sioshansi (2010, 2014), Kaps et al. (2023), Peng et al. (2021),
     Peura and Bunn (2021), Acemoglu et al. (2017), Wu et al. (2023), ...
- flexible resources smoothing demand
  - Agrawal and Yücel (2022), Gao et al. (2024), Fattahi et al. (2023)
  - EVs Wu et al. (2022), Perakis and Thayaparan (2023)
- empirical work on batteries
  - Karaduman (2023), Butters et al. (2023

- forward markets
  - Allaz and Vila (1993), Ito and Reguant (2016), You et al. (2019)
- batteries and renewables operations
  - investments, locations, intermittency, ownership models, ...
  - Sioshansi (2010, 2014), Kaps et al. (2023), Peng et al. (2021),
     Peura and Bunn (2021), Acemoglu et al. (2017), Wu et al. (2023), ...
- flexible resources smoothing demand
  - Agrawal and Yücel (2022), Gao et al. (2024), Fattahi et al. (2023)
  - EVs Wu et al. (2022), Perakis and Thayaparan (2023)
- empirical work on batteries
  - Karaduman (2023), Butters et al. (2023

- forward markets
  - Allaz and Vila (1993), Ito and Reguant (2016), You et al. (2019)
- batteries and renewables operations
  - investments, locations, intermittency, ownership models, ...
  - Sioshansi (2010, 2014), Kaps et al. (2023), Peng et al. (2021),
     Peura and Bunn (2021), Acemoglu et al. (2017), Wu et al. (2023), ...
- flexible resources smoothing demand
  - Agrawal and Yücel (2022), Gao et al. (2024), Fattahi et al. (2023)
  - EVs Wu et al. (2022), Perakis and Thayaparan (2023)
- empirical work on batteries
  - Karaduman (2023), Butters et al. (2023

- forward markets
  - Allaz and Vila (1993), Ito and Reguant (2016), You et al. (2019)
- batteries and renewables operations
  - investments, locations, intermittency, ownership models, ...
  - Sioshansi (2010, 2014), Kaps et al. (2023), Peng et al. (2021),
     Peura and Bunn (2021), Acemoglu et al. (2017), Wu et al. (2023), ...
- flexible resources smoothing demand
  - Agrawal and Yücel (2022), Gao et al. (2024), Fattahi et al. (2023)
  - EVs Wu et al. (2022), Perakis and Thayaparan (2023)
- empirical work on batteries
  - Karaduman (2023), Butters et al. (2023)

### RESULTS: BATTERY BEHAVIOR

Both the centralized and decentralized problems are quadratic infinite-dimensional problems.

We prove that both problems are **convex** and solve them in **closed-form**.

The DCN solution shows 3 types of distortions from the CN solution:

- quantity withholding
- shift from day-ahead to real-time
- reduction in real-time responsiveness

We quantify each as a function of  $k_f$ , the share of fast generators.

### RESULTS: BATTERY BEHAVIOR

Both the centralized and decentralized problems are quadratic infinite-dimensional problems.

We prove that both problems are convex and solve them in closed-form.

The DCN solution shows 3 types of distortions from the CN solution:

- quantity withholding
- shift from day-ahead to real-time
- reduction in real-time responsiveness

We quantify each as a function of  $k_f$ , the share of fast generators.

### RESULTS: BATTERY BEHAVIOR

quantity withholding , shift to real-time, reduction in RT responsiveness.

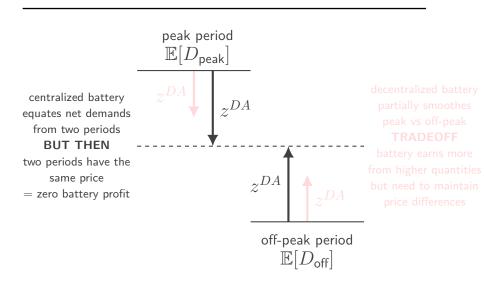
## Centralized Battery Discharge

$$\begin{split} z_{\rm peak}^{DA} &= \boxed{\frac{1}{2}(\mu_{\rm peak} - \mu_{\rm off})} \\ z_{\rm peak}^{RT}(D_{\rm peak}) &= \frac{1}{2}(D_{\rm peak} - \mu_{\rm peak}) - \frac{1}{2}(\mu_{\rm off}|_{D_{\rm peak}} - \mu_{\rm off}) \end{split}$$

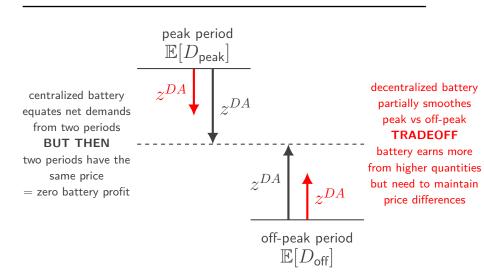
## Decentralized Battery Discharge

$$\begin{split} z_{\text{peak}}^{DA} &= \left\lfloor \frac{(2-k_f)}{2(4-k_f)} (\mu_{\text{peak}} - \mu_{\text{off}}) \right\rfloor \\ z_{\text{peak}}^{RT}(D_{\text{peak}}) &= \left\lfloor \frac{k_f}{2(4-k_f)} (\mu_{\text{peak}} - \mu_{\text{off}}) \right\rfloor + \frac{1}{4} (D_{\text{peak}} - \mu_{\text{peak}}) - \frac{1}{4} (\mu_{2|D_{\text{peak}}} - \mu_{\text{off}}) \end{split}$$

# DISTORTION 1: QUANTITY WITHHOLDING



# DISTORTION 1: QUANTITY WITHHOLDING



## DISTORTION 2: SHIFT FROM DAY-AHEAD TO REAL-TIME

## Structural consequence of **sequential market clearing**.

Simplest case: no randomness, identical markets with price function  $P(\cdot)$ .

$$\label{eq:maximize_profit} \text{Maximize profit} = z^{DA}P(z^{DA}) + z^{RT}P(z^{DA} + z^{RT})$$

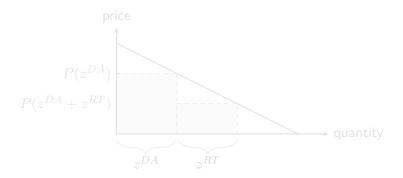


## DISTORTION 2: SHIFT FROM DAY-AHEAD TO REAL-TIME

Structural consequence of **sequential market clearing**.

Simplest case: no randomness, identical markets with price function  $P(\cdot)$ .

$$\label{eq:maximize_profit} \text{Maximize profit} = z^{DA}P(z^{DA}) + z^{RT}P(z^{DA} + z^{RT}).$$

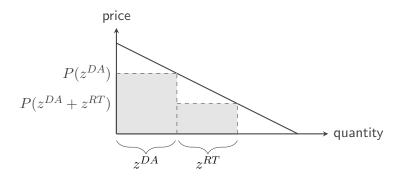


## DISTORTION 2: SHIFT FROM DAY-AHEAD TO REAL-TIME

Structural consequence of **sequential market clearing**.

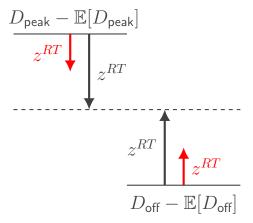
Simplest case: no randomness, identical markets with price function  $P(\cdot)$ .

$$\label{eq:maximize_profit} \text{Maximize profit} = z^{DA}P(z^{DA}) + z^{RT}P(z^{DA} + z^{RT}).$$



## DISTORTION 3: REDUCTION IN REAL-TIME RESPONSIVENESS

Same kind of tension between **centralized** and **decentralized** regimes, except the "quantity withholding" is on *real-time residual demand*.



#### RESULTS: GENERATION COSTS

Define the Price of Anarchy (PoA) as an incentive misalignment metric:

$$\mathsf{PoA} = \frac{\mathsf{GenCost}(\mathsf{NoBattery}) - \mathsf{GenCost}(\mathsf{Centralized})}{\mathsf{GenCost}(\mathsf{NoBattery}) - \mathsf{GenCost}(\mathsf{Decentralized})}$$

 $PoA \ge 1$ . Lower PoA means better alignment.

#### Theorem

Assume the demand is jointly normal, then

- PoA  $\in$  [9/8,4/3] for every market parameter. (12.5% to 33.3%)
- PoA is decreasing in  $k_f$ .

#### RESULTS: GENERATION COSTS

Define the Price of Anarchy (PoA) as an incentive misalignment metric:

$$\mathsf{PoA} = \frac{\mathsf{GenCost}(\mathsf{NoBattery}) - \mathsf{GenCost}(\mathsf{Centralized})}{\mathsf{GenCost}(\mathsf{NoBattery}) - \mathsf{GenCost}(\mathsf{Decentralized})}$$

 $PoA \ge 1$ . Lower PoA means better alignment.

## Theorem

Assume the demand is jointly normal, then

- PoA  $\in$  [9/8,4/3] for every market parameter. (12.5% to 33.3%)
- PoA is decreasing in  $k_f$ .

		distortion types		
	PoA	quantity	shift from	reduction in
	104	withholding	DA to RT	RT responsiveness
Los Angeles	15%	35%	47%	50%
Houston	25%	40%	33%	50%

$$\mathsf{PoA} = \frac{\mathsf{GenCost}(\mathsf{NoBattery}) - \mathsf{GenCost}(\mathsf{CN})}{\mathsf{GenCost}(\mathsf{NoBattery}) - \mathsf{GenCost}(\mathsf{DCN})} - 1$$

		distortion types		
	PoA	quantity	shift from	reduction in
	FOA	withholding	DA to RT	RT responsiveness
Los Angeles	15%	35%	47%	50%
Houston	25%	40%	33%	50%

$$\mbox{quantity withholding} = 1 - \frac{\mbox{total DCN discharge}}{\mbox{total CN discharge}}$$

		distortion types		
	PoA	quantity	shift from	reduction in
	FOA	withholding	DA to RT	RT responsiveness
Los Angeles	15%	35%	47%	50%
Houston	25%	40%	33%	50%

shift from DA to RT = 
$$\frac{\text{RT DCN discharge}}{\text{total (DA+RT) DCN discharge}}$$

If a battery achieves local monopoly, distortions can be significant! e.g. Los Angeles batteries (Apr'24): **355 MW**, 40 MW, fringe  $\sim$ 27 MW

		distortion types		
	PoA	quantity	shift from	reduction in
	POA	withholding	DA to RT	RT responsiveness
Los Angeles	15%	35%	47%	50%
Houston	25%	40%	33%	50%

 $\mbox{reduction in RT responsiveness} = 1 - \frac{\mbox{RT "random" DCN discharge}}{\mbox{RT "random" CN discharge}}$ 

		distortion types		
	PoA	quantity	shift from	reduction in
		withholding	DA to RT	RT responsiveness
Los Angeles	15%	35%	47%	50%
Houston	25%	40%	33%	50%

- We develop a **tractable analytical model** quantifying different forms of battery behavior in terms of market fundamentals.
- Incentive misalignment (PoA) from 3 forms of distortions
  - quantity withholding
  - shift from day-ahead to real-time
  - reduction in real-time responsiveness
- We calibrate the model to Los Angeles and Houston and show that incentive misalignment is practically significant.
- Our model is parsimonious = **building block** for future work.

- We develop a **tractable analytical model** quantifying different forms of battery behavior in terms of market fundamentals.
- Incentive misalignment (PoA) from 3 forms of distortions
  - quantity withholding
  - shift from day-ahead to real-time
  - reduction in real-time responsiveness
- We calibrate the model to Los Angeles and Houston and show that incentive misalignment is practically significant.
- Our model is parsimonious = **building block** for future work.

- We develop a **tractable analytical model** quantifying different forms of battery behavior in terms of market fundamentals.
- Incentive misalignment (PoA) from 3 forms of distortions
  - quantity withholding
  - shift from day-ahead to real-time
  - reduction in real-time responsiveness
- We **calibrate** the model to Los Angeles and Houston and show that *incentive misalignment* is **practically significant**.
- Our model is parsimonious = building block for future work.

- We develop a **tractable analytical model** quantifying different forms of battery behavior in terms of market fundamentals.
- Incentive misalignment (PoA) from 3 forms of distortions
  - quantity withholding
  - shift from day-ahead to real-time
  - reduction in real-time responsiveness
- We calibrate the model to Los Angeles and Houston and show that incentive misalignment is practically significant.
- Our model is parsimonious = **building block** for future work.