

Week 9  
MATH 33A  
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5.3.33 Find all orthogonal  $2 \times 2$  matrices.

5.3.37 Is there an orthogonal transformation  $T$  from  $\mathbb{R}^3$  to itself such that  $T \begin{bmatrix} 2 \\ 3 \\ 0 \end{bmatrix} = \begin{bmatrix} 3 \\ 0 \\ 2 \end{bmatrix}$  and

$$T \begin{bmatrix} -3 \\ 2 \\ 0 \end{bmatrix} = \begin{bmatrix} 2 \\ -3 \\ 0 \end{bmatrix}?$$

5.3.44 Consider an  $n \times m$  matrix  $A$ . Find  $\dim(\text{Im}(A)) + \dim(\ker(A^T))$  in terms of  $m$  and  $n$ .

5.4.18 Does the equation  $\text{rank}(A^T A) = \text{rank}(A A^T)$  hold for all  $n \times m$  matrices  $A$ ?

5.4.22 Find the least squares solution  $x^*$  of the system  $Ax = b$ , where  $A = \begin{bmatrix} 3 & 2 \\ 5 & 3 \\ 4 & 5 \end{bmatrix}$  and

$b = \begin{bmatrix} 5 \\ 9 \\ 2 \end{bmatrix}$ . Determine the error  $\|b - Ax^*\|$ .

6.1.30 Let  $A = \begin{bmatrix} 4 & 2 & 0 \\ 4 & 6 & 0 \\ 5 & 2 & 3 \end{bmatrix}$ . Find  $\lambda$  such that  $A - \lambda I$  fails to be invertible.