

CompSci/ECE.350L.001.Sp21 Midterm 2

Rishi Salwi

TOTAL POINTS

98 / 100

QUESTION 1

1 5-Variable K-map and function 14 / 15

K-Map

✓ + 3 pts *Correct entries on K-map*

+ 2 pts Mainly right but minority of cells

wrong/transposed

+ 2 pts missed one entry

+ 1 pts badly transposed / many wrong

+ 2 pts right pattern but axes transposed

+ 1 pts left off don't cares, adds significantly to complexity

+ 1 pts Made the "don't cares" into 1s, adds significantly to complexity

Prime Implicants (given map used)

+ 6 pts all 9 prime implicants identified

✓ + 5 pts *8 PI identified out of 9*

+ 4 pts 7 PI identified out of 9

+ 3 pts 6 PI identified out of 9

+ 2 pts 5 PI identified out of 9

+ 1 pts 4 PI identified out of 9

+ 0 pts 3 or fewer PI identified out of 9

+ 0 pts Not capturing

Function

✓ + 6 pts *Plausible given map used (for correct map*

7 terms

$x_0'x_2x_3' + x_1'x_2'x_3 + x_2'x_3x_4' + x_2x_3'x_4' + x_0'x_1x_2x_4 + x_0x_1$

$x_3'x_4 + (\text{either } x_0x_1'x_3'x_4' \text{ or } x_0x_1'x_2'x_4')$

+ 2 pts Unfinished or significantly incorrect

+ 5 pts 1 term too many

+ 4 pts 1 term too few

+ 0 pts Click here to replace this description.

QUESTION 2

Short Answer 20 pts

2.1 Structural Hazard 4 / 4

✓ - 0 pts *Correct*

- 1 pts Pipelining actually exacerbates structural hazards (compared with a single-cycle machine) rather than solving them, but the pipeline structure overcomes this.

- 1 pts Pipelines are a source but not the only possible source of structural hazards - more generally any attempt to use the same resource twice

2.2 Data Hazard 3 / 4

- 0 pts *Correct*

- 1 Point adjustment

Not always on the same cycle, might not even be computed yet much less written back

2.3 Control Hazard 4 / 4

✓ - 0 pts *Correct*

2.4 Path Sensitization 4 / 4

✓ - 0 pts Correct

- 2 pts More specifically by setting other inputs so that a change of the input value on the current path of focus is reflected by a change in value on an observable output

- 1 pts important to include setting other inputs so that a change of the input on the selected path is reflected by a change of value on an observable output

2.5 Code Distance 4 / 4

✓ - 0 pts Correct

QUESTION 3

3 Pizza Emergency Button 40 / 40

✓ - 0 pts [15 pts] Correct State Diagram (11 states, reset functionality)

✓ - 0 pts [9 pts] Correct State Table

- 9 pts missing state table

✓ - 0 pts [9 pts] Correct State Transition Table

- 9 pts missing state transition table

- 3 pts missing output encodings in state transition table

✓ - 0 pts [7 pts] Plausible Equations

- 2 pts missing output equations

- 5 pts missing next state equations

QUESTION 4

4 FSM Minimization 25 / 25

✓ - 0 pts Correct

- 15 pts started

- 6 pts right initial table, incorrect processing

- 5 pts Correct grid, no final state table

1. Minimization

00010	01010	10010	01101
00011	01100	10011	11101
00100	01111	10100	
00101	10000	11001	
		11010	
		11100	

[15 points] Given

$$f(x_0, x_1, x_2, x_3, x_4) = \sum m(2, 3, 4, 5, 10, 12, 15, 16, 18, 19, 20, 25, 26, 28) + D(13, 29)$$

15 6789

Note carefully the labeling of the K-map. Use this 5-variable K-map to write a (possibly the) minimal SOP form of this function

x_3x_4	00	01	11	10
x_1x_2	00	01	11	10
00	0	0	1	1
01	1	1	0	0
11	1	0	1	0
10	0	0	0	1

x_3x_4	00	01	11	10
x_1x_2	00	01	11	10
00	1	0	1	1
01	1	0	0	0
11	1	0	0	0
10	0	1	0	1

$x_0=0$

$x_0=1$

Indicate prime implicants by circling them on the K-map, and write out the minimized function below

$$f(x_0, x_1, x_2, x_3, x_4) = \overline{x_1} \overline{x_2} x_3 + \overline{x_2} x_3 \overline{x_4} + \overline{x_0} x_2 \overline{x_3} + x_2 \overline{x_3} \overline{x_4}$$

$$+ \overline{x_0} x_1 x_2 x_4 + x_0 x_1 \overline{x_3} x_4 + x_0 \overline{x_1} \overline{x_3} \overline{x_4}$$

1 5-Variable K-map and function 14 / 15

K-Map

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+ 0 pts Not capturing

Function

✓ + 6 pts *Plausible given map used (for correct map 7 terms*

$x0'x2x3'+x1'x2'x3+x2'x3x4'+x2x3'x4'+x0'x1x2x4+x0x1x3'x4+(either\ x0x1'x3'x4'\ or\ x0x1'x2'x4')$

+ 2 pts Unfinished or significantly incorrect

+ 5 pts 1 term too many

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+ 0 pts Click here to replace this description.

2. Short Answer

In 1-2 sentences, and in the space available or on comparable space on your own paper, describe the concepts listed below

4 points - Structural Hazard

This occurs when multiple instructions need the same resource such as the read/write port on the register, memory, or the ALU.

4 points - Data Hazard

Data hazards are data dependencies in processors. They occur when you are trying to read or write from a register that is currently being read/written to.

4 points - Control Hazard

Control hazards occur when you execute the wrong instructions after a branch because you don't know where to branch yet.

4 points - Path Sensitization

It is an algorithm used to

identify the minimal test set for a circuit.

It shows what path or inputs need to be taken for a specific input to reach the output.

4 points - Code Distance

It is a term used in error correcting/defecting codes. It is the number of bits that need to change in a code to produce another valid code.

2.1 Structural Hazard 4 / 4

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- 1 pts Pipelining actually exacerbates structural hazards (compared with a single-cycle machine) rather than solving them, but the pipeline structure overcomes this.

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2.2 Data Hazard 3 / 4

- **0 pts** Correct

- **1 Point adjustment**

- Not always on the same cycle, might not even be computed yet much less written back

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2.3 Control Hazard 4 / 4

✓ - 0 pts Correct

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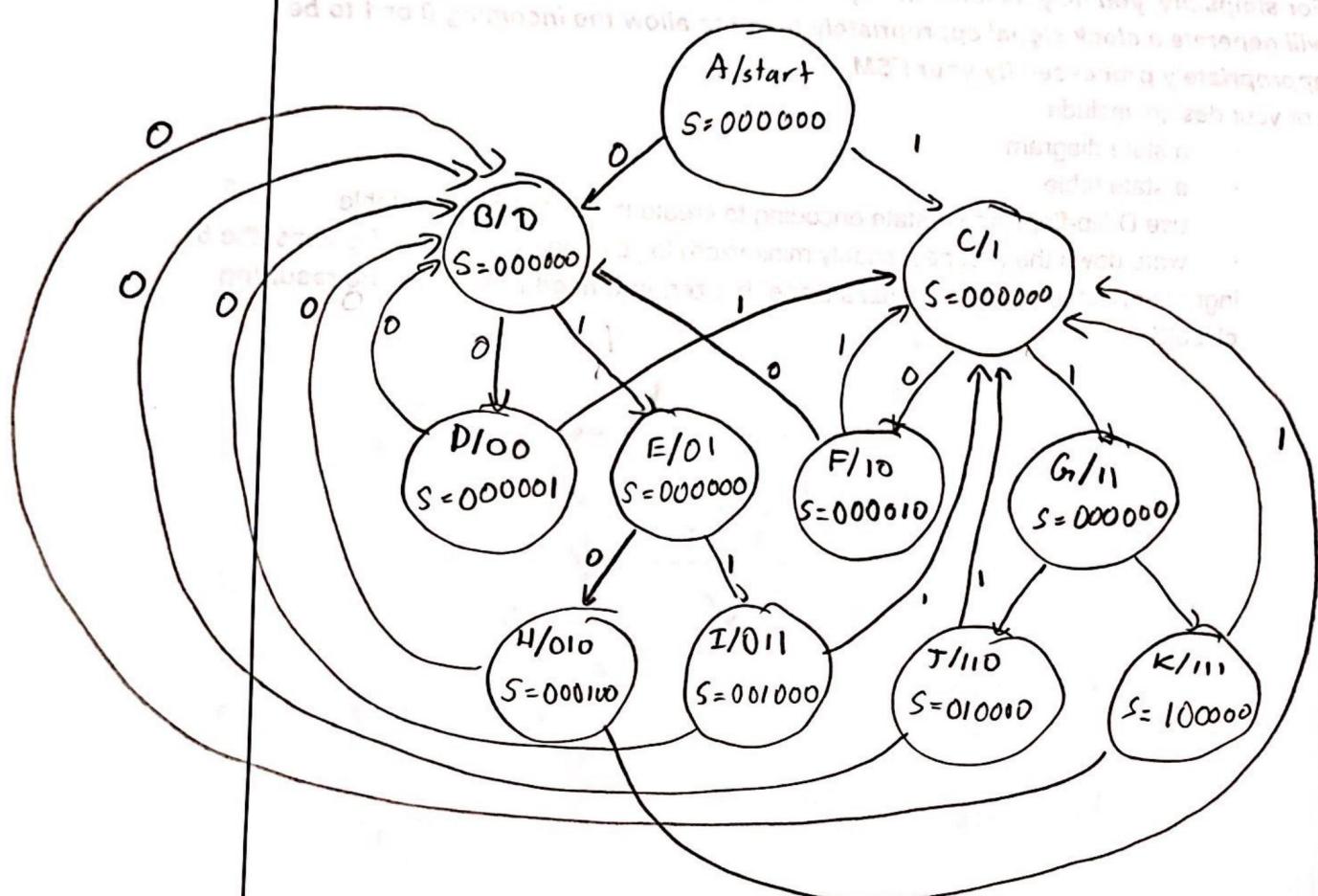
4 points - Code Distance

It is a term used in error correcting/defecting codes. It is the number of bits that need to change in a code to produce another valid code.

2.5 Code Distance 4 / 4

✓ - 0 pts Correct

State Diagram



Output $S = \underline{X} \ \underline{X} \ \underline{X} \ \underline{X} \ \underline{X} \ \underline{X}$

↑ ↑ ↑ ↑ ↑ ↑

end of pizza onions sausage pineapple extra cheese pepperoni.

State Table (Symbolic)

Present State	Next State $w=0$	State $w=1$	Output
A	B	C	000 000 nothing
B	D	E	000 000 nothing
C	F	G	000 000 nothing
D	B	C	000 001 extra cheese
E	H	I	000 000 nothing
F	B	K	000 010 pepperoni
G	J	C	000 000 nothing
H	B	C	000 010 sausage
I	B	C	001 000 pineapple
J	B	C	010 000 onions
K	B	C	100 000 eww eww

State Transition Table (State encoding, D flip flops)

Present State $y_3\ y_2\ y_1\ y_0$	Next State $w=0$ $y_3\ y_2\ y_1\ y_0$	Next State $w=1$ $y_3\ y_2\ y_1\ y_0$	Output $S_3\ S_4\ S_5\ S_2\ S_1\ S_0$
0 0 0 0	0 0 0 1	0 0 1 0	0 0 0 0 0 0
0 0 0 1	0 0 1 1	0 1 0 0	0 0 0 0 0 0
0 0 1 0	0 1 0 1	0 1 1 0	0 0 0 0 0 0
0 0 1 1	0 0 0 1	0 0 1 0	0 0 0 0 0 1
0 1 0 0	0 1 1 1	1 0 0 0	0 0 0 0 0 0
0 1 0 1	0 0 0 1	0 0 1 0	0 0 0 0 1 0
0 1 1 0	1 0 0 1	1 0 1 0	0 0 0 0 0 0
0 1 1 1	0 0 0 1	0 0 1 0	0 0 0 1 0 0
1 0 0 0	0 0 0 1	0 0 1 0	0 0 1 0 0 0
1 0 0 1	0 0 0 1	0 0 1 0	0 1 0 0 0 0
1 0 1 0	0 0 0 1	0 0 1 0	1 0 0 0 0 0

Equations

$$Y_3 = D_3 = \bar{y}_3 y_2 \bar{y}_1 \bar{y}_0 + \bar{y}_3 y_2 \bar{y}_1 \bar{y}_0 w$$

$$Y_2 = D_2 = \bar{y}_3 \bar{y}_2 y_1 \bar{y}_0 \bar{w} + \bar{y}_3 y_2 \bar{y}_1 \bar{y}_0 \bar{w} + \bar{y}_3 \bar{y}_2 \bar{y}_1 y_0 w + \bar{y}_3 \bar{y}_2 y_1 \bar{y}_0 w$$

$$Y_1 = D_1 = \bar{y}_3 \bar{y}_2 \bar{y}_1 y_0 \bar{w} + \bar{y}_3 y_2 \bar{y}_1 \bar{y}_0 \bar{w} + \bar{y}_3 \bar{y}_2 \bar{y}_1 y_0 w + \bar{y}_3 y_2 \bar{y}_1 \bar{y}_0 w$$

$$Y_0 = D_0 = \bar{w}$$

$$S_0 = \text{extra cheese} = \bar{y}_3 \bar{y}_2 y_1 y_0$$

$$S_1 = \text{pepperoni} = \bar{y}_3 y_2 \bar{y}_1 y_0$$

$$S_2 = \text{sausage} = \bar{y}_3 y_2 y_1 y_0$$

$$S_3 = \text{pineapple} = y_3 \bar{y}_2 \bar{y}_1 \bar{y}_0$$

$$S_4 = \text{onions} = y_3 \bar{y}_2 \bar{y}_1 y_0$$

$$S_5 = \text{end of pizza} = y_3 \bar{y}_2 y_1 \bar{y}_0$$

3 Pizza Emergency Button 40 / 40

✓ - 0 pts [15 pts] *Correct State Diagram (11 states, reset functionality)*

✓ - 0 pts [9 pts] *Correct State Table*

- 9 pts missing state table

✓ - 0 pts [9 pts] *Correct State Transition Table*

- 9 pts missing state transition table

- 3 pts missing output encodings in state transition table

✓ - 0 pts [7 pts] *Plausible Equations*

- 2 pts missing output equations

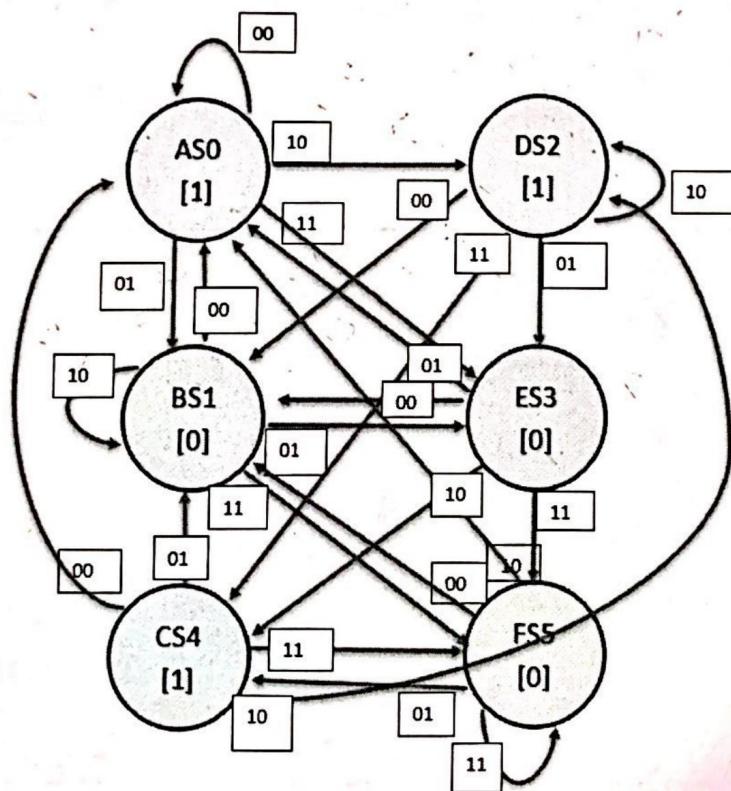
- 5 pts missing next state equations

4. FSM Minimization

[25 pts] Given the following finite state machine (the state diagram is admittedly confusing so go by the state table for the "official" definition), use the implication chart method to see if it can be reduced to an equivalent machine with fewer states. Give the reduced state table if so. A blank implication chart is provided on the next page. Score will be based on completion of the implication chart and the final state table.

Implication chart method to minimize this Moore FSM

Present State	Next State: w0 w1				Output
	00	01	10	11	
A	A	B	D	E	1
B	A	E	B	F	0
C	A	B	D	F	1
D	B	E	D	C	1
E	B	A	C	F	0
F	B	C	A	F	0



B	$A \rightarrow A$ B → C C → D			
C	$A = A$ $B = B$ $D = D$ $E \leftarrow F$	X		
D	$\cancel{A = B}$ $\cancel{B = E}$ $\cancel{D = D}$ $E \leftarrow C$	X	$A = B$ B → E D = D $F \leftarrow C$	
E	X	$A = B$ E = A B = C $F = F$	X	X
F	X	$A = B$ E = C B = A $F = F$	X	X $B = B$ $A = C$ $C = A$ $F = F$
	A	B	C	D

$$A = C$$

$$E = F$$

Final State Table

Present State	Next state when				Output
	00	01	10	11	
A, C	A	B	D	E	I
B	A	E	B	E	O
D	B	E	D	A	I
F, F	B	A	A	E	O

4 FSM Minimization 25 / 25

✓ - 0 pts Correct

- 15 pts started

- 6 pts right initial table, incorrect processing

- 5 pts Correct grid, no final state table

Rishi Sgwi

CompSci/ECE350 Spring 2021 Midterm Examination 2 – 4/15/21

This is an open book, open notes, open internet exam designed to take 75 minutes, but you have 90 minutes to work (including time needed to deal with the logistics of accessing and submitting this exam). Please answer all 4 questions, and note that question 3 is worth more than the others (about double). If you can print and scan your exam, you can use the spaces provided (augmented with scratch paper), but you may also just answer on your own paper and submit your responses by scanning those instead. You may/should use extra pages to show your work; scan those too!

Please, if accurate, sign this statement before turning in your exam¹:
(or summarize on your own paper)

I have neither given nor received any unauthorized help on this examination.

I will be on the usual class lecture Zoom during the exam windows to answer any mid test questions. If you want to ask me a question over Zoom, I will move you to a breakout room as we did for the first midterm.

¹ If the statement is not accurate, we need to talk!

3. FSM Design

[40 points] A number of years ago (I am not making this up!), some MIT students designed a pizza-shaped Emergency Pizza Button which, when pressed, placed a pizza order on the early internet. Since there is just one button and not everyone wants the same pizza, they employ a Huffman code to encode desired ingredients, with more popular ingredients taking fewer button presses than less popular ones. Huffman codes have the property that, even though codewords are of different lengths, each can be unambiguously decoded. I presume the switch is a simple 2 position switch that can reliably send "0" or "1" (pressing the Pizza button down or up).



Given the following Huffman code:

00	extra cheese
10	pepperoni
010	sausage
011	pineapple
110	onions
111	EndOfPizza

a Pizza Emergency Code of 0010010111 would mean "send a pizza with extra cheese, pepperoni, and sausage;" note so also would 0100010111 as by construction all the shorter codes are distinct from all the longer codes so the sequence is unambiguous. The EndOfPizza code must be appended to the end of each message so we know when a pizza is complete. Sending the same code twice (or more) for the same pizza is ok, ..1010... will cause double pepperoni, and will have caused your FSM to fire the Pepperoni output twice.

Design a Moore-style finite state machine to process incoming pizza emergency messages, signaling via output signals which ingredients to include on the pizza. (Note a pizza code of 111 would indicate a plain pizza with no special ingredients, i.e. no ingredient output signals active.) Hint: You will need 6 separate 1-bit outputs, one for each ingredient, and "Pizza Done".

For simplicity, you may assume the system's clocking "just works," each button press will generate a clock signal appropriately timed to allow the incoming 0 or 1 to be appropriately processed by your FSM.

For your design, include

- a state diagram
- a state table
- use D flip-flops and a state encoding to create the state transition table
- write down the (not necessarily minimized) logic equations for your flip-flops, the 5 ingredient outputs, and the "Pizza Done" buzzer; you need NOT draw the resulting circuit!