

Objectives

The primary object of this lab was to be familiar with the signals properties by using MATLAB. And also do the convolution of LTI systems.

Questions

Q1 a): By running these codes, we got the graph of $x(t)$ over a time interval of 1 second, with 0.001 resolution. The graph shown below:

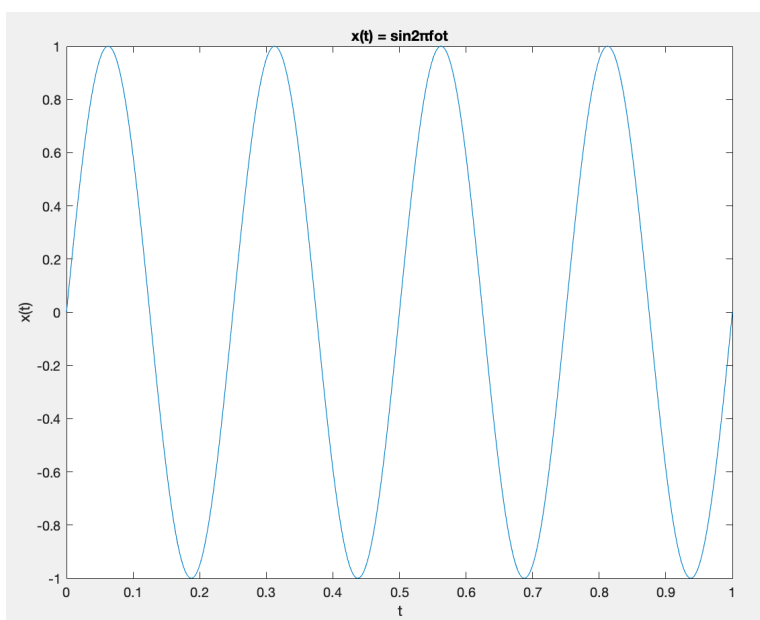


Fig. 1

b): By doing the Matlab code on the right, And combine with the code of question a. We can get the graph shown in fig. 2.

In fig.2, blue line represent $x(t)$, red one represent $x_1[n]$ and yellow one represent $x_2[n]$. In the graph, we can see every 8 red points are a period($N=8$) of $x_1[n]$, and every 5 yellow points are a period($N=5$) of $x_2[n]$.

```
1 %Question 1
2 %(a)
3 t = 0:0.001:1;
4 f0 = 4;
5 xt = sin(2*pi*f0*t);
6 plot(t,xt);
```

```
8 %(b)
9 n1 = 1:1:32;
10 fs1 = 8*f0;
11 ts1 = 1/fs1;
12 x1n = sin(2*pi*n1*f0*ts1);
13 hold on
14 stem((n1*ts1),x1n)
15 n2 = 1:1:10;
16 fs2 = 5*f0/2;
17 ts2 = 1/fs2;
18 x2n = sin(4*pi*n2*f0*ts2);
19 hold on
20 stem((n2*ts2),x2n)
```

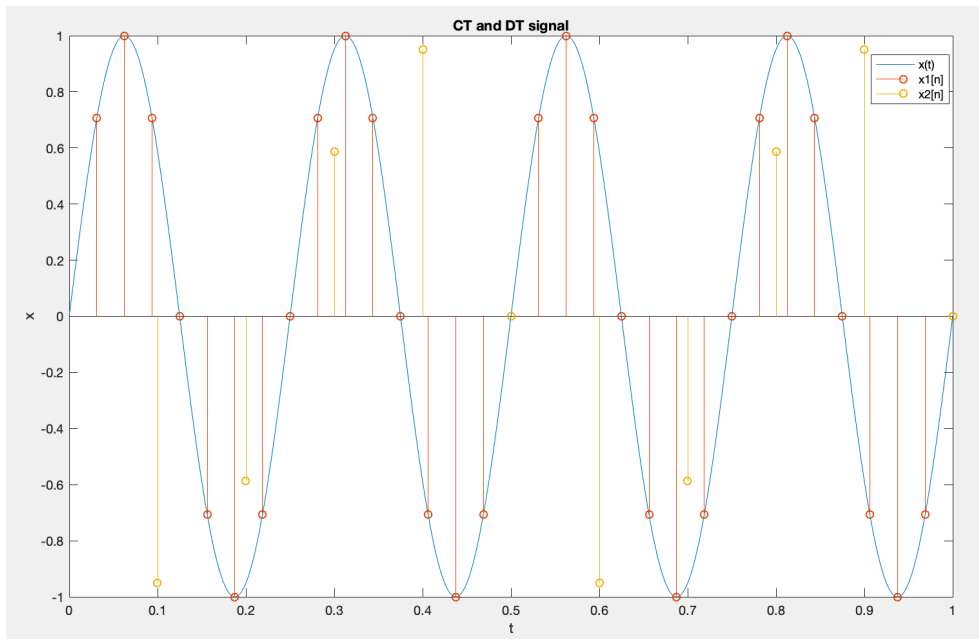


Fig. 2

c): For $x(t)$, $T_0 = 2\pi / \omega_0 = 2\pi / 8\pi = 1 / 4$

For $x_1[n] = \omega_0 / 2\pi = 2\pi / 8 / 2\pi = 1 / 8 = m / N$, $m = 1$, $N = 8$,
 $x_1[n]$ repeats after $m = 1$ cycle of $x(t)$ in step with each other.

For $x_2[n] = \omega_0 / 2\pi = 4\pi / 5 / 2\pi = 2 / 5 = m / N$, $m = 2$, $N = 5$
 $x_2[n]$ repeats after $m = 2$ cycles of $x(t)$ in step with each other.

As we can see in fig.2, blue line represent $x(t)$, red one represent $x_1[n]$ and yellow one represent $x_2[n]$. We can see that every 8 red points are a period ($N=8$) of $x_1[n]$, and every 5 yellow points are a period ($N=5$) of $x_2[n]$.

Q2:

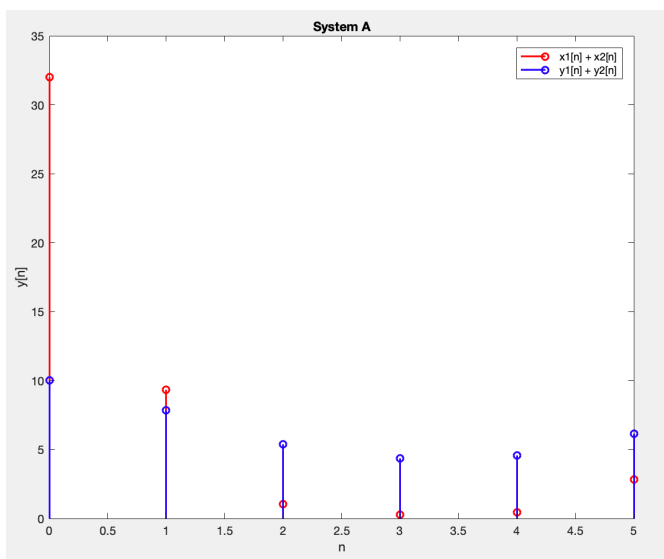


fig. 3

For a linear system, there are two properties: additivity and homogeneity.

Put them together: $ax_1(t) + bx_2(t) \rightarrow ay_1(t) + by_2(t)$. $ax_1[n] + bx_2[n] \rightarrow ay_1[n] + by_2[n]$

```

22 %Question 2
23 %System A
24 n=0:5;
25 a = 2;
26 b = 3;
27 x1n = 0.8.^n;
28 x2n = cos(n);
29 z = a * x1n + b * x2n;
30 yA1 = 2.^z;
31 stem(n,yA1,'r', 'linewidth',1.5)
32 hold on
33 y1 = 2.^(0.8.^n);
34 y2 = 2.^(cos(n));
35 yA2 = a * y1 + b * y2;
36 stem(n,yA2,'b', 'linewidth',1.5)
37 hold off

```

According to this properties, we firstly added input two signals, then went through system A, and plot a graph. Secondly, we let these two signal went through system A individually, then added them together, and plot a graph as well.

We can see in fig.3, input(red line) is a weighted sum of several signal, the output(blue line) is the superposition (weighted sum) of responses to each of the signals. So system A is a linear system.

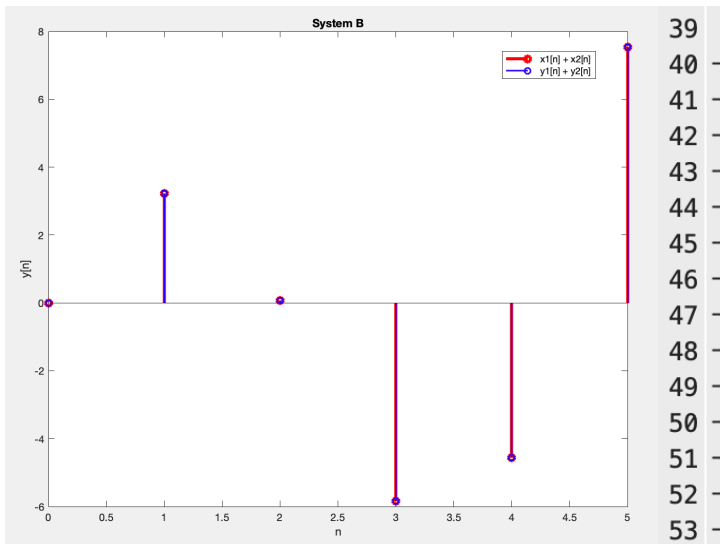


fig. 4

For system B, we follow the same procedure with system A. The output graph shown in fig.4, which prove system B is linear as well.

Q3: a)

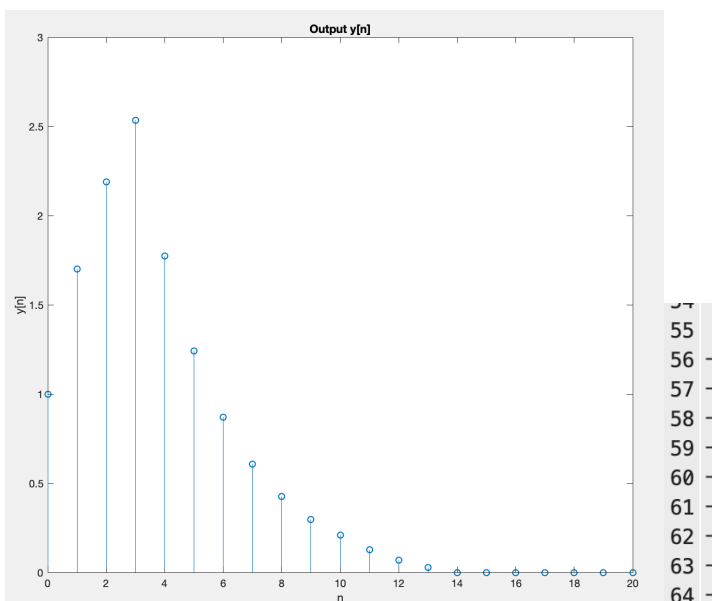


fig. 5

%System B

```

39 n=0:5;
40 a = 2;
41 b = 3;
42 x1n = 0.8.^n;
43 x2n = cos(n);
44 z = a * x1n + b * x2n;
45 yB1 = n.* z;
46 stem(n,yB1,'r','linewidth',3)
47 hold on
48 y1 = n.* (0.8.^n);
49 y2 = n.* (cos(n));
50 yB2 = a * y1 + b * y2;
51 stem(n,yB2,'b','linewidth',1.5)
52 hold off
53

```

%Question 3

```

55 n = 0:10;
56 n1 = 0:20;
57 hn = 0.7.^n;
58 oldparam = sympref('HeavisideAtOrigin',1);
59 u1 = heaviside(n);
60 u2 = heaviside(n-4);
61 xn = u1-u2;
62 y = conv(hn,xn);
63 stem(n1,y)
64

```

In this question, we used heaviside() to return a step function $u(t)$. However, by using this function, the first value of $u(t)$ wasn't 1, so we have to write

`oldparam = sympref('HeavisideAtOrigin',1);`

to change it into 1.

We set $n1$ and use it to plot instead of using n , because the X value must have same length with Y value.

Output $y[n]$ shown in fig.5.

b)

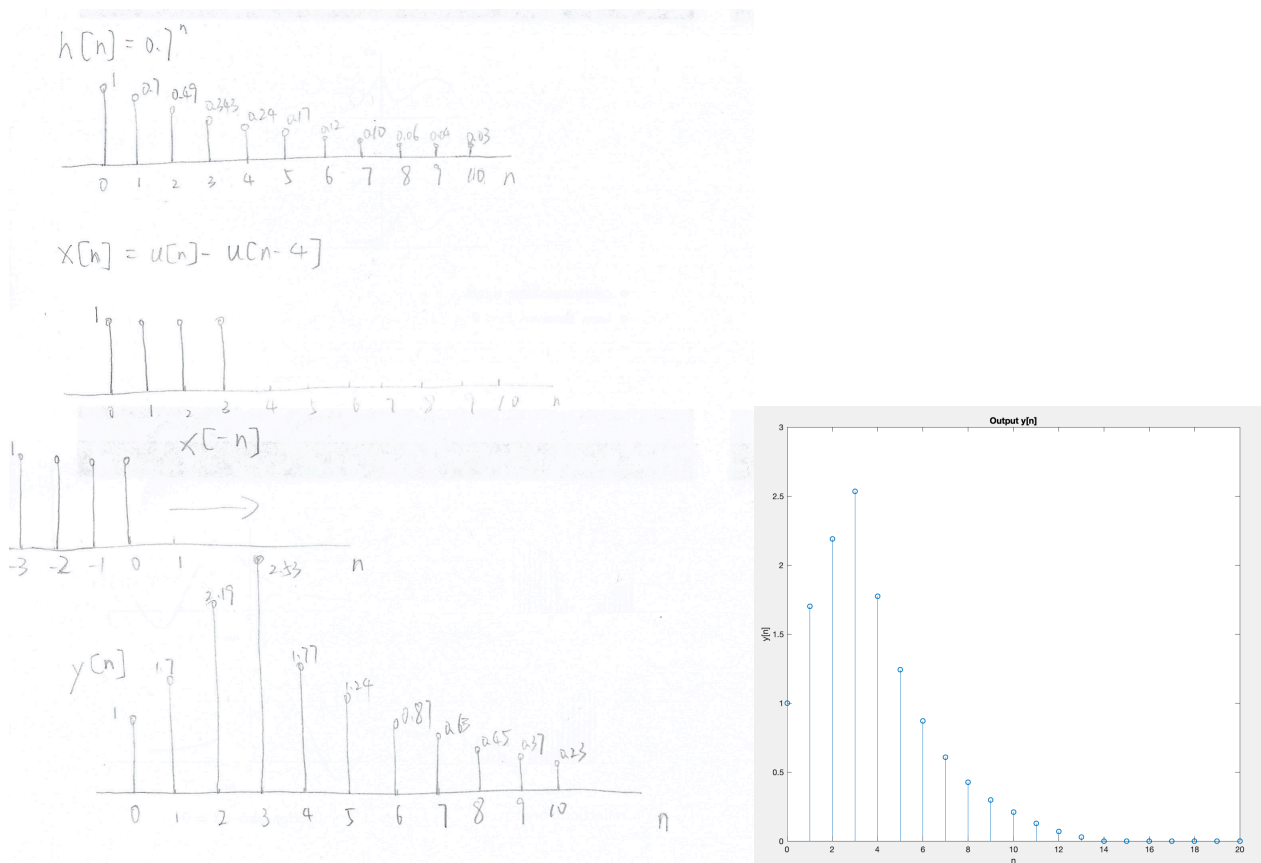


fig. 6

Solving the convolution by hand, the result shown in fig. 6. It is same with the result of MATLAB.