

Indefinite Integration

1 Fundamental Definition of Indefinite Integration

If f and F are functions such that $\frac{d}{dx}(F(x)) = f(x)$ then F is anti-derivative of f w.r.t. x symbolically,

$$\int f(x) dx = F(x) + C$$

where C is constant of Integration

2 Anti-Derivatives of some standard functions

$$\text{i. } \int x^n dx = \frac{x^{n+1}}{n+1} + C \quad \forall n \in \mathbb{R} - \{1\}, x \in \mathbb{R}$$

$$\text{ii. } \int \frac{1}{x} dx = \ln|x| + C \quad \forall x \in \mathbb{R} - \{0\}$$

$$\text{iii. } \int e^x dx = e^x + C \quad \forall x \in \mathbb{R}$$

$$\text{iv. } \int a^x dx = \frac{a^x}{\ln a} + C \quad \forall a \in \mathbb{R}^+ - \{1\}, x \in \mathbb{R}$$

$$\text{v. } \int \sin x dx = -\cos x + C \quad \forall x \in \mathbb{R}$$

$$\text{vi. } \int \cos x dx = \sin x + C \quad \forall x \in \mathbb{R}$$

$$\text{vii. } \int \sec^2 x dx = \tan x + C \quad \forall x \in \mathbb{R} - \left\{(2n+1)\frac{\pi}{2} : n \in \mathbb{Z}\right\}$$

$$\text{viii. } \int \csc^2 x dx = -\cot x + C \quad \forall x \in \mathbb{R} - \{n\pi : n \in \mathbb{Z}\}$$

$$\text{ix. } \int \sec x \tan x dx = \sec x + C \quad \forall x \in \mathbb{R} - \left\{(2n+1)\frac{\pi}{2} : n \in \mathbb{Z}\right\}$$

x.	$\int \csc x \cot x \, dx = -\csc x + C$	$\forall x \in \mathbb{R} - \{n\pi : n \in \mathbb{Z}\}$
xi.	$\int \cot x \, dx = \ln \sin x + C$	$\forall x \in \mathbb{R} - \{n\pi : n \in \mathbb{Z}\}$
xii.	$\int \tan x \, dx = -\ln \cos x + C$	$\forall x \in \mathbb{R} - \left\{(2n+1)\frac{\pi}{2} : n \in \mathbb{Z}\right\}$
xiii.	$\int \sec x \, dx = \ln \sec x + \tan x + C$	$\forall x \in \mathbb{R} - \left\{(2n+1)\frac{\pi}{2} : n \in \mathbb{Z}\right\}$
xiv.	$\int \csc x \, dx = \ln \csc x - \cot x + C$	$\forall x \in \mathbb{R} - \{n\pi : n \in \mathbb{Z}\}$
xv.	$\int \frac{1}{\sqrt{a^2 - x^2}} \, dx = \sin^{-1} \left(\frac{x}{a} \right) + C$	$\forall a \in \mathbb{R} - \{0\}$
xvi.	$\int \frac{-1}{\sqrt{a^2 - x^2}} \, dx = \cos^{-1} \left(\frac{x}{a} \right) + C$	$\forall a \in \mathbb{R} - \{0\}$
xvii.	$\int \frac{1}{a^2 + x^2} \, dx = \frac{1}{a} \tan^{-1} \left(\frac{x}{a} \right) + C$	$\forall a \in \mathbb{R} - \{0\}$
xviii.	$\int \frac{-1}{a^2 + x^2} \, dx = \frac{1}{a} \cot^{-1} \left(\frac{x}{a} \right) + C$	$\forall a \in \mathbb{R} - \{0\}$
xix.	$\int \frac{1}{x\sqrt{x^2 - a^2}} \, dx = \frac{1}{a} \sec^{-1} \left(\frac{x}{a} \right) + C$	$\forall a \in \mathbb{R} - \{0\}$
xx.	$\int \frac{-1}{x\sqrt{x^2 - a^2}} \, dx = \frac{1}{a} \csc^{-1} \left(\frac{x}{a} \right) + C$	$\forall a \in \mathbb{R} - \{0\}$