

Some new test functions for global optimization and performance of repulsive particle swarm method

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23 August 2006

Online at https://mpra.ub.uni-muenchen.de/2718/MPRA Paper No. 2718, posted 13 Apr 2007 UTC

Some New Test Functions for Global Optimization and Performance of Repulsive Particle Swarm Method

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I. Introduction: In this paper we introduce some new multi-modal test functions to assess the performance of global optimization methods. These functions have been selected partly because several of them are aesthetically appealing and partly because a few of them are really difficult to optimize. We also propose to optimize some important benchmark functions already in vogue. Each function has been graphically presented to appreciate its geometrical appearance. To optimize these functions we have used the Repulsive Particle Swarm (RPS) method, with wider local search abilities and randomized neighbourhood topology.

II. The Particle Swarm Method of Global Optimization: This method is an instance of successful application of the philosophy of Simon's bounded rationality and decentralized decision-making to solve the global optimization problems (Simon, 1982; Bauer, 2002; Fleischer, 2005). As it is well known, the problems of the existence of global order, its integrity, stability, efficiency, etc. have been long standing. The laws of development of institutions have been sought in this order. Newton, Hobbes, Adam Smith and Locke visualized the global system arising out of individual actions. In particular, Adam smith (1759) postulated the role of *invisible hand* in establishing the harmony that led to the said global order. The neo-classical economists applied the tools of equilibrium analysis to show how this grand synthesis and order is established while each individual is selfish. The postulate of perfect competition was felt to be a necessary one in demonstrating that. Yet, Alfred Marshall limited himself to partial equilibrium analysis and, thus, indirectly allowed for the role of invisible hand (while general equilibrium economists hoped that the establishment of order can be explained by their approach). Thorstein Veblen (1899) never believed in the mechanistic view and pleaded for economics as an evolutionary science. F. A. Hayek (1944) believed in a similar philosophy and believed that locally optimal decisions give rise to the global order and efficiency. Later, Herbert Simon (1982) postulated the 'bounded rationality' hypothesis and argued that the hypothesis of perfect competition is not necessary for explaining the emergent harmony and order at the global level. Elsewhere, I. Prigogine (1984) demonstrated how the global 'order' emerges from chaos at the local level.

It is observed that a swarm of birds or insects or a school of fish searches for food, protection, etc. in a very typical manner (Sumper, 2006). If one of the members of the swarm sees a desirable path to go, the rest of the swarm will follow quickly. Every member of the swarm searches for the best in its locality - learns from its own experience. Additionally, each member learns from the others, typically from the best performer among them. The Particle Swarm method of optimization mimics this behaviour (see Wikipedia: http://en.wikipedia.org/wiki/Particle_swarm_optimization). Every individual of the swarm is considered as a particle in a multidimensional space that has a position and a velocity. These particles fly through hyperspace and remember the

best position that they have seen. Members of a swarm communicate good positions to each other and adjust their own position and velocity based on these good positions. There are two main ways this communication is done: (i) "swarm best" that is known to all (ii) "local bests" are known in neighborhoods of particles. Updating the position and velocity is done at each iteration as follows:

$$v_{i+1} = \omega v_i + c_1 r_1 (\hat{x}_i - x_i) + c_2 r_2 (\hat{x}_{gi} - x_i)$$

$$x_{i+1} = x_i + v_{i+1}$$

where,

- x is the position and v is the velocity of the individual particle. The subscripts i and i+1 stand for the recent and the next (future) iterations, respectively.
- ω is the inertial constant. Good values are usually slightly less than 1.
- c_1 and c_2 are constants that say how much the particle is directed towards good positions. Good values are usually right around 1.
- r_1 and r_2 are random values in the range [0,1].
- \hat{x} is the best that the particle has seen.
- \hat{x}_g is the global best seen by the swarm. This can be replaced by \hat{x}_L , the local best, if neighborhoods are being used.

The Particle Swarm method (Eberhart and Kennedy, 1995) has many variants. The Repulsive Particle Swarm (RPS) method of optimization (see Wikipedia, http://en.wikipedia.org/wiki/RPSO), one of such variants, is particularly effective in finding out the global optimum in very complex search spaces (although it may be slower on certain types of optimization problems). Other variants use a dynamic scheme (Liang and Suganthan, 2005; Huang et al., 2006).

In the traditional RPS the future velocity, v_{i+1} of a particle at position with a recent velocity, v_i , and the position of the particle are calculated by:

$$v_{i+1} = \omega v_i + \alpha r_1 (\hat{x}_i - x_i) + \omega \beta r_2 (\hat{x}_{hi} - x_i) + \omega \gamma r_3 z$$

$$x_{i+1} = x_i + v_{i+1}$$

where.

- x is the position and v is the velocity of the individual particle. The subscripts i and i+1 stand for the recent and the next (future) iterations, respectively.
- r_1 , r_2 r_3 are random numbers, $\in [0,1]$
- ω is inertia weight, $\in [0.01, 0.7]$
- \hat{x} is the best position of a particle
- x_h is best position of a randomly chosen other particle from within the swarm
- z is a random velocity vector
- α , β , γ are constants

Occasionally, when the process is caught in a local optimum, some perturbation of v may be needed. We have modified the traditional RPS method by endowing stronger

(wider) local search ability to each particle and the neighbourhood topology to each particle is randomized.

- **III.** The New Test Functions: We used RPS method for a fairly large number of established test problems (Mishra, 2006 (c) reports about 30 benchmark functions). Here we introduce the new functions and the results obtained by the RPS program (appended). These new functions are as follows.
- **1. Test tube holder function (a)**: This multi-modal function is defined as follows. We obtain $x^* \approx -10.8723$ in the domain $x_i \in [-10, 10]$, i = 1, 2.

$$f(x) = -4 \left| \sin(x_1) \cos(x_2) e^{|\cos((x_1^2 + x_2^2)/200)|} \right|.$$

2. Test tube holder function (b): This multi-modal function is defined as follows. We obtain $x^* \simeq -10.8723$ in the domain $x_1 \in [-9.5, 9.4], x_2 \in [-10.9, 10.9]$.

$$f(x) = -4 \left| \sin(x_1) \cos(x_2) e^{|\cos((x_1^2 + x_2^2)/200)|} \right|.$$

3. Holder table function: This 'tabular holder' function has multiple local minima with four global minima at $f(x^*) \approx 26.92$. This function is given as:

$$f(x) = -\left|\cos(x_1)\cos(x_2)e^{|1-[(x_1^2+x_2^2)^{0.5}]/\pi I}\right|$$

4. Carrom table function: This function has multiple local minima with four global minima at $f(x^*) \approx 24.1568155$ in the search domain $x_i \in [-10, 10]$, i = 1, 2. This function is given as:

$$f(x) = -\left[\left\{\cos(x_1)\cos(x_2)e^{|\mathbf{l}-[(x_1^2 + x_2^2)^{0.5}]/\pi \mathbf{l}}\right\}^2\right]/30$$

5. Cross in tray function: This function has multiple local minima with the global minima at $f(x^*) \approx -2.06261218$ in the search domain $x_i \in [-10, 10]$, i = 1, 2. This function is given as:

$$f(x) = -0.0001 \left[\left| \sin(x_1) \sin(x_2) e^{\left| 100 - \left[(x_1^2 + x_2^2)^{0.5} \right] / \pi \right|} \right| + 1 \right]^{0.1}$$

6. Crowned cross function: This function is the negative form of the cross in tray function. It has $f(x^*) \approx 0$ in the search domain $x_i \in [-10, 10]$, i = 1, 2. It is a difficult function to optimize. The minimal value obtained by us is approximately 0.1. This function is given as:

$$f(x) = 0.0001 \left[\left| \sin(x_1) \sin(x_2) e^{\left| 100 - \left[(x_1^2 + x_2^2)^{0.5} \right] / \pi \right|} \right| + 1 \right]^{0.1}$$

7. Cross function: This is a multi-modal function with $f(x^*) \simeq 0$. It is given as

$$f(x) = \left[\left| \sin(x_1) \sin(x_2) e^{\left| 100 - \left[(x_1^2 + x_2^2)^{0.5} \right] / \pi \right|} \right| + 1 \right]^{-0.1}$$

8. Cross-leg table function: This function is the negative form of the cross function and may also be called the 'inverted cross' function. It has $f(x^*) \approx -1$ in the search domain $x_i \in [-10, 10]$, i = 1, 2. It is a difficult function to optimize. We have failed to optimize this function. This function is given as:

$$f(x) = -\left[\left|\sin(x_1)\sin(x_2)e^{\left|100 - \left[(x_1^2 + x_2^2)^{0.5}\right]/\pi\right|}\right| + 1\right]^{-0.1}$$

9. Pen holder function: This is a multi-modal function with $f(x^*) \simeq -0.96354$ in the search domain $x_i \subseteq [-11, 11)$, given as

$$f(x) = -\exp\left[-\left|\cos(x_1)\cos(x_2)e^{\left|-\left[(x_1^2 + x_2^2)^{0.5}/\pi\right]\right|}\right|^{-1}\right]$$

10. Bird function: This is a bi-modal function with $f(x^*) \approx -106.764537$ in the search domain $x_i \in [-2\pi, 2\pi]$; i = 1, 2 given as

$$f(x) = \sin(x_1)e^{[(1-\cos(x_2))^2]} + \cos(x_2)e^{[(1-\sin(x_1))^2]} + (x_1 - x_2)^2$$

11. Modified Schaffer function #1: In the search domain $x_1, x_2 \in [-100, 100]$ this function is defined as follows and has $f_{\min}(0, 0) = 0$.

$$f(x) = 0.5 + \frac{\sin^2(x_1^2 + x_2^2) - 0.5}{[1 + 0.001(x_1^2 + x_2^2)]^2}.$$

12. Modified Schaffer function #2: In the search domain x_1 , $x_2 \in [-100, 100]$ this function is defined as follows and has $f_{\min}(0, 0) = 0$.

$$f(x) = 0.5 + \frac{\sin^2(x_1^2 - x_2^2) - 0.5}{[1 + 0.001(x_1^2 + x_2^2)]^2}.$$

13. Modified Schaffer function #3: In the search domain x_1 , $x_2 \in [-100, 100]$ this function is defined as follows and has $f_{\min}(0, 1.253115) = 0.00156685$.

$$f(x) = 0.5 + \frac{\sin^2 \left[\cos \left[\left|x_1^2 - x_2^2\right|\right]\right] - 0.5}{\left[1 + 0.001(x_1^2 + x_2^2)\right]^2}.$$

14. Modified Schaffer function #4: In the search domain x_1 , $x_2 \in [-100, 100]$ this function is defined as follows and has $f_{\min}(0, 1.253132) = 0.292579$.

$$f(x) = 0.5 + \frac{\cos^2 \left[\sin \left[\left| x_1^2 - x_2^2 \right| \right] \right] - 0.5}{\left[1 + 0.001 (x_1^2 + x_2^2) \right]^2}.$$

IV. Some Well-Established Benchmark Functions: As mentioned earlier, we have also tested the RPS in searching the optimum points of some well-established functions. These functions are:

1. Hougen function: Hougen function is typical complex test for classical non-linear regression problems. The Hougen-Watson model for reaction kinetics is an example of such non-linear regression problem. The form of the model is

$$rate = \frac{\beta_1 x_2 - x_3 / \beta_5}{1 + \beta_2 x_1 + \beta_3 x_2 + \beta_4 x_3}$$

where the betas are the unknown parameters, $x = (x_1, x_2, x_3)$ are the explanatory variables and 'rate' is the dependent variable. The parameters are estimated via the least squares criterion. That is, the parameters are such that the sum of the squared differences between the observed responses and their fitted values of rate is minimized. The input data given alongside are used.

$\mathbf{x_1}$	\mathbf{X}_{2}	X 3	rate
470	300	10	8.55
285	80	10	3.79
470	300	120	4.82
470	80	120	0.02
470	80	10	2.75
100	190	10	14.39
100	80	65	2.54
470	190	65	4.35
100	300	54	13.00
100	300	120	8.50
100	80	120	0.05
285	300	10	11.32
285	190	120	3.13

Best results are obtained by the Rosenbrock-Quasi-Newton method: $\hat{\beta}_1 = 1.253031$; $\hat{\beta}_2 = 1.190943$; $\hat{\beta}_3 = 0.062798$; $\hat{\beta}_4 = 0.040063$; $\hat{\beta}_5 = 0.112453$. The sum of squares of deviations (S²) is = 0.298900994 and the coefficient of correlation (R) between observed rate and expected rate is =0.99945. The second best results are obtained by Hooke-Jeeves-Quasi-Newton method with S² = 0.318593458. Most of the other methods do not perform well.

The Particle Swarm method too does not ordinarily perform well in estimating the betas of the Hougen function. However, with $\gamma(= a3) = 0.0005$ and $\omega=0.05$, run for 50,000 iterations we obtain: $\hat{\beta}_1 = 1.5575204$; $\hat{\beta}_2 = 0.0781010629$; $\hat{\beta}_3 = 0.050866667$; $\hat{\beta}_4 = 0.138796292$; $\hat{\beta}_5 = 0.955739322$. The sum of squares of deviations (S²) is = 0.301933528. A comparison of Rosenbrock-Quasi-Newton results with these (RPS) results indicates that the betas exhibit very high degree of instability in the neighbourhood of the minimal S².

2. Egg holder function: This function is in m $(m \ge 2)$ variables and given as:

$$f(x) = \sum_{i=1}^{m-1} \left(-(x_{i+1} + 47)\sin(\sqrt{|x_{i+1} + x_i/2 + 47|}) + \sin(\sqrt{|x_i - (x_{i+1} + 47)|})(-x_i) \right); -512 \le x_i \le 512; i = 1, 2, ..., m$$
We obtain $f_{\min}(512, 404.2319) \approx 959.64$. It is a difficult function to optimize.

3. Sine envelope sine wave function: The function, also referred as the Schaffer function (m=2), is given as:

$$f(x) = \sum_{i=1}^{m-1} \left(\frac{\sin^2 \left[\sqrt{x_{i+1}^2 + x_i^2} \right] - 0.5}{(0.001 \left(x_{i+1}^2 + x_i^2 \right) + 1)^2} + 0.5 \right); -100 \le x_i \le 100; i = 1, 2, ..., m$$

It is a difficult problem to optimize. For higher dimensions it gives repeating couplets of optimal values of x^* , except their sign.

4. Chichinadze function: In the search domain x_1 , $x_2 \in [-30, 30]$ this function is defined as follows and has $f_{min}(5.90133, 0.5) = -43.3159$.

$$f(x) = x_1^2 - 12x_1 + 11 + 10\cos(\pi x_1/2) + 8\sin(5\pi x_1) - (1/5)^{0.5}e^{-0.5(x_2-0.5)^2}$$

5. McCormick function: In the search domain $x_1 \in [-1.5, 4], x_2 \in [-3, 4]$ this function is defined as follows and has $f_{min}(-0.54719, -1.54719) = -1.9133$.

$$f(x) = \sin(x_1 + x_2) + (x_1 - x_2)^2 - 1.5x_1 + 2.5x_2 + 1.$$

6. Levy function (#13): In the search domain x_1 , $x_2 \in [-10, 10]$ this function is defined as follows and has $f_{\min}(1, 1) = 0$.

$$f(x) = \sin^2(3\pi x_1) + (x_1 - 1)^2 [1 + \sin^2(3\pi x_2)] + (x_2 - 1)^2 [1 + \sin^2(2\pi x_2)].$$

7. Three-humps camel back function: In the search domain $x_1, x_2 \in [-5, 5]$ this function is defined as follows and has $f_{\min}(0, 0) = 0$.

$$f(x) = 2x_1^2 - 1.05x_1^4 + x_1^6 / 6 + x_1x_2 + x_2^2$$
.

8. Zettle function: In the search domain x_1 , $x_2 \in [-5, 5]$ this function is defined as follows and has $f_{\min}(-0.0299, 0) = -0.003791$.

$$f(x) = (x_1^2 + x_2^2 - 2x_1)^2 + 0.25x_1$$

9. Styblinski-Tang function: In the search domain x_1 , $x_2 \in [-5, 5]$ this function is defined as follows and has $f_{\min}(-2.903534, -2.903534) \approx -78.332$.

$$f(x) = \frac{1}{2} \sum_{i=1}^{2} (x_i^4 - 16x_i^2 + 5x_i).$$

10. Bukin functions: Bukin functions are almost fractal (with fine seesaw edges) in the surroundings of their minimal points. Due to this property, they are extremely difficult to optimize by any method of global (or local) optimization. In the search domain $x_1 \in [-15, -5], x_2 \in [-3, 3]$ these functions are defined as follows.

$$f_4 = 100x_2^2 + 0.01|x_1 + 10| \quad ; \quad f_{\min}(-10, \ 0) = 0$$

$$f_6(x) = 100\sqrt{|x_2 - 0.01x_1^2|} + 0.01|x_1 + 10| \quad ; \quad f_{\min}(-10, \ 1) = 0$$

11. Leon function: In the search domain x_1 , $x_2 \in [-1.2, 1.2]$ this function is defined as follows and has $f_{\min}(1, 1) = 0$.

$$f(x) = 100(x_2 - x_1^2)^2 + (1 - x_1)^2$$

12. Giunta function: In the search domain x_1 , $x_2 \in [-1, 1]$ this function is defined as follows and has $f_{\min}(0.45834282, 0.45834282) \approx 0.0602472184$.

$$f(x) = 0.6 + \sum_{i=1}^{2} \left[\sin(\frac{16}{15}x_i - 1) + \sin^2(\frac{16}{15}x_i - 1) + \frac{1}{50}\sin(4(\frac{16}{15}x_i - 1)) \right].$$

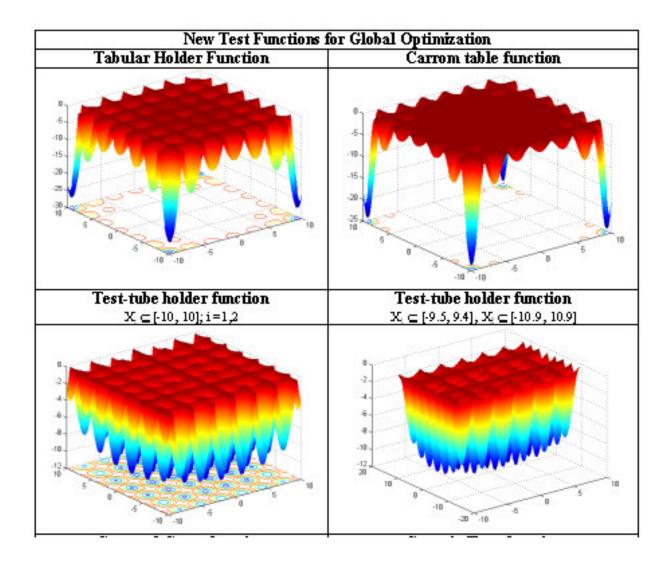
We have obtained f_{min} (0.4673199, 0.4673183) = 0.06447.

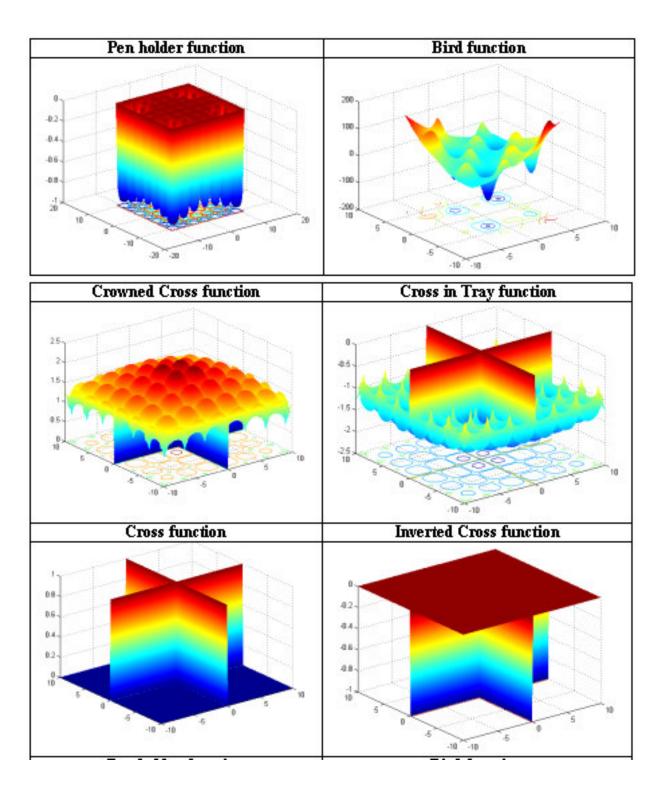
13. Schaffer function: In the search domain x_1 , $x_2 \in [-100, 100]$ this function is defined as follows and has $f_{\min}(0, 0) = 0$.

$$f(x) = 0.5 + \frac{\sin^2\left[\sqrt{x_1^2 + x_2^2}\right] - 0.5}{\left[1 + 0.001(x_1^2 + x_2^2)\right]^2}.$$

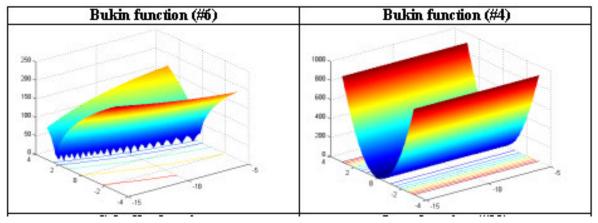
V. FORTRAN Program of RPS: We append a program of the Repulsive Particle Swarm method. The program has run successfully and optimized most of the functions. However, the crowned cross function and the cross-legged table functions have failed the program.

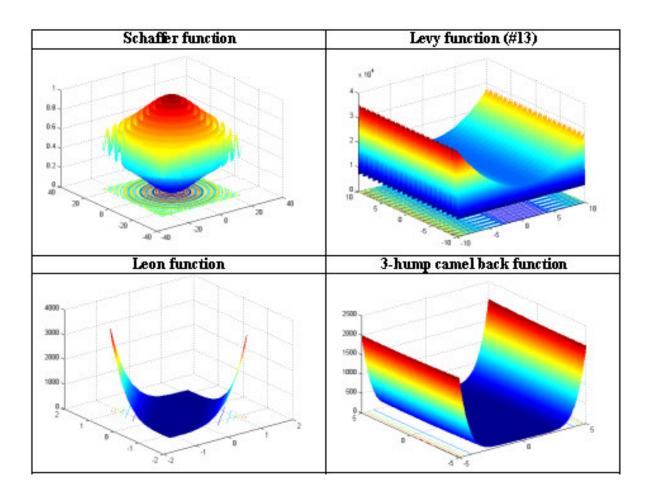
VI. Conclusion: Our program of the RPS method has succeeded in optimizing most of the established functions and the newly introduced functions. The functions (namely - Giunta, Bukin, cross-legged table, crowned cross and Hougen functions in particular) that have failed the RPS program miserably may be attractive to other methods such as Simulated Annealing, Genetic algorithms and tunneling methods. Improved versions of Particle Swarm method also may be tested.

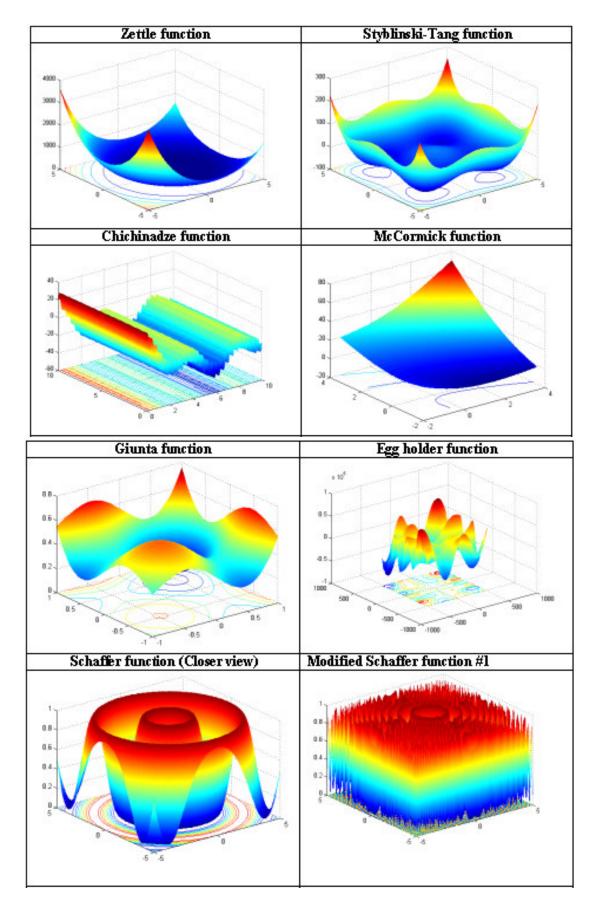


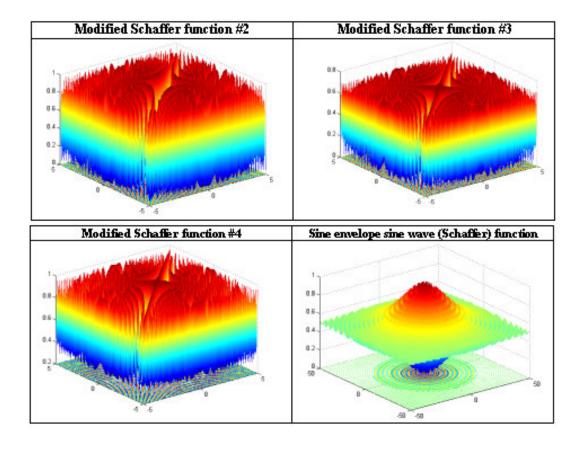


Some Well-established Benchmark Functions









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1: C
 2: C
 3:
          PARAMETER (N=50 , NN=25 , MX=100, NSTEP=21, ITRN=5000)
 4: C
 5: C
 6: C
 7: C
 8: C
 9: C
10: C
11: C
12: C
13: C
14:
15:
          IMPLICIT DOUBLE PRECISION (A-H, O-Z)
16:
          COMMON /RNDM/IU, IV
17:
          COMMON /KFF/KF
          INTEGER IU, IV
18:
19:
          DIMENSION X(N, MX), V(N, MX), A(MX), VI(MX), TIT(50)
20:
          DIMENSION XX(N, MX), F(N), R(3), V1(MX), V2(MX), V3(MX), V4(MX), BST(MX)
          CHARACTER *70 TIT
21:
22: C
23: C
24: C
25:
          DATA A1, A2, A3, W /.5D00, .5D00, .0005D00, .5D00/
          WRITE(*,*)'-----
26:
          DATA TIT(1)/'KF=1 TEST TUBE HOLDER FUNCTION(A) 2-VARIABLES M=2'/
27:
          DATA TIT(2)/'KF=2 TEST TUBE HOLDER FUNCTION(B) 2-VARIABLES M=2'/
28:
29:
          DATA TIT(3)/'KF=3 HOLDER TABLE FUNCTION 2-VARIABLES M=2'/
          DATA TIT(4)/'KF=4 CARROM TABLE FUNCTION 2-VARIABLES M=2'/
30:
          DATA TIT(5)/'KF=5 CROSS IN TRAY FUNCTION 2-VARIABLES M=2'/
31:
32:
          DATA TIT(6)/'KF=6 CROWNED CROSS FUNCTION 2-VARIABLES M=2'/
          DATA TIT(7)/'KF=7 CROSS FUNCTION 2-VARIABLES M=2'/
33:
          DATA TIT(8)/'KF=8 CROSS-LEGGED TABLE FUNCTION 2-VARIABLES M=2'/
34:
          DATA TIT(9)/'KF=9 PEN HOLDER FUNCTION 2-VARIABLES M=2'/
35:
          DATA TIT(10) / 'KF=10 BIRD FUNCTION 2-VARIABLES M=2'/
36:
37:
38:
          DATA TIT(11)/'KF=11 DE JONG SPHERE FUNCTION M-VARIABLE M=?'/
          DATA TIT(12)/'KF=12 LEON FUNCTION 2-VARIABLE M=2'/
39:
          DATA TIT(13)/'KF=13 GIUNTA FUNCTION 2-VARIABLE M=2'/
40:
          DATA TIT(14) / 'KF=14 SCHAFFER FUNCTION 2-VARIABLE M=2'/
41:
          DATA TIT(15)/'KF=15 CHICHINADZE FUNCTION 2-VARIABLE M=2'/
42:
          DATA TIT(16)/'KF=16 MCCORMICK FUNCTION 2-VARIABLE M=2'/
43:
44:
          DATA TIT(17)/'KF=17 LEVY # 13 FUNCTION 2-VARIABLE M=2'/
          DATA TIT(18)/'KF=18 3-HUMP CAMEL BACK FUNCTION 2-VARIABLE M=2'/
45:
          DATA TIT(19)/'KF=19 ZETTLE FUNCTION 2-VARIABLE M=2'/
46:
47:
          DATA TIT(20)/'KF=20 STYBLINSKI-TANG FUNCTION 2-VARIABLE M=2'/
48:
49:
          DATA TIT(21)/'KF=21 BUKIN-4 FUNCTION 2-VARIABLE M=2'/
          DATA TIT(22)/'KF=22 BUKIN-6 FUNCTION 2-VARIABLE M=2'/
50:
51:
          DATA TIT(23)/'KF=23 HOUGEN REGRESSION FUNCTION 5-VARIABLE M=5'/
52:
          DATA TIT(24)/'KF=24 SINE ENVELOPE SINE WAVE FUNCTION M=? '/
          DATA TIT(25)/'KF=25 EGG-HOLDER FUNCTION M=?'/
53:
          DATA TIT(26)/'KF=26 MODIFIED SCHAFFER FUNCTION #1 2-VARIABLE M=2'/
54:
          DATA TIT(27)/'KF=27 MODIFIED SCHAFFER FUNCTION #2 2-VARIABLE M=2'/
55:
56:
          DATA TIT(28)/'KF=28 MODIFIED SCHAFFER FUNCTION #3 2-VARIABLE M=2'/
57:
          DATA TIT(29) / 'KF=29 MODIFIED SCHAFFER FUNCTION #4 2-VARIABLE M=2'/
          DATA TIT(30)/'KF=30 QUARTIC(+NOISE) FUNCTION M-VARIABLE M=?'/
58:
59:
60:
          DO I=1,30
61:
          WRITE(*,*)TIT(I)
62:
          ENDDO
63:
          WRITE (*, *) '-----
          WRITE(*,*)'CHOOSE KF AND SPECIFY M'
64:
65:
          READ(*,*) KF,M
66:
          DSIGN=1.D00
          LCOUNT=0
67:
```

```
WRITE (*, *) '4-DIGITS SEED FOR RANDOM NUMBER GENERATION'
 68:
 69:
            READ(*,*) IU
 70:
            DATA ZERO, ONE, FMIN /0.0D00, 1.0D00, 1.0E30/
 71: C
 72:
            DO I=1, N
 73:
              DO J=1, M
 74:
              CALL RANDOM (RAND)
 75:
               X(I, J) = (RAND-0.5D00) *10
 76:
 77: C
 78: C
 79:
               ENDDO
 80:
              F(I) = 1.0E30
 81:
            ENDDO
 82: C
 83:
            DO I=1, N
 84:
            DO J=1, M
 85:
            CALL RANDOM (RAND)
 86:
             V(I, J) = (RAND - .5D + 00)
 87: C
 88:
            ENDDO
 89:
            ENDDO
 90:
            ZZZ=1.0E+30
 91:
            ICOUNT=0
 92:
            DO 100 ITER=1, ITRN
 93:
 94: C
 95:
              DO I=1, N
 96:
                 DO J=1, M
 97:
                  A(J) = X(I,J)
 98:
                  VI(J) = V(I, J)
 99:
                  ENDDO
100:
                  CALL LSRCH(A, M, VI, NSTEP, FI)
101:
                  \mathbf{IF}(FI.\mathbf{LT}.F(I)) THEN
102:
                   F(I) = FI
103:
                   DO IN=1, M
104:
                   BST(IN)=A(IN)
105:
                   ENDDO
106: C
107: C
108:
                    DO J=1, M
109:
                    XX(I,J) = A(J)
110:
                    ENDDO
111:
                    ENDIF
              ENDDO
112:
113:
114: C
115: C
116:
117:
            DO I=1, N
118: C
119:
                BEST=1.0E30
120:
                 DO II=1, NN
121:
                       CALL RANDOM (RAND)
122:
                       NF = INT (RAND*N) + 1
123.
                       IF (BEST.GT.F(NF)) THEN
124:
                       BEST=F(NF)
125:
                       NFBEST=NF
126:
                       ENDIF
127:
                  ENDDO
128: C
129: C
            INDIVIDUAL I WILL MODIFY HIS MOVE AS PER THE FOLLOWING CRITERION
130: C
131: C
132:
                 DO J=1, M
133:
                  CALL RANDOM (RAND)
134:
                  V1(J) = A1*RAND*(XX(I, J) - X(I, J))
```

```
135: C
            THEN BASED ON THE OTHER COLLEAGUES BEST EXPERIENCE WITH WEIGHT W
136: C
            HERE W IS CALLED AN INERTIA WEIGHT 0.01 < W < 0.7
137: C
138.
                 CALL RANDOM (RAND)
139:
                 V2(J) = V(I,J)
140:
                 IF (F (NFBEST) . LT . F (I) ) THEN
                 V2(J) = A2*W*RAND*(XX(NFBEST, J) - X(I, J))
141:
142:
143: C
144:
                 CALL RANDOM (RAND)
145:
                 RND1=RAND
146:
                 CALL RANDOM (RAND)
147:
                  V3(J) = A3*RAND*W*RND1
148: C
149: C
            THEN ON PAST VELOCITY WITH INERTIA WEIGHT W
                 V4(J) = W*V(I,J)
150:
151: C
152:
                 V(I, J) = V1(J) + V2(J) + V3(J) + V4(J)
153:
                 ENDDO
154:
            ENDDO
155: C
156:
            DO I=1, N
157:
            DO J=1, M
158:
            X(I,J)=X(I,J)+V(I,J)
159:
            ENDDO
160:
            ENDDO
161:
162:
             DO I=1, N
163:
               IF (F(I).LT.FMIN) THEN
164:
               FMIN=F(I)
165:
               TT=T
166:
               DO J=1, M
167:
               BST(J) = XX(II, J)
168:
               ENDDO
169:
               ENDIF
170:
               ENDDO
171:
            Z=FMIN
172:
            IF (LCOUNT.EQ. 100) THEN
173:
174:
            LCOUNT=0
175:
            WRITE(*, *) 'OPTIMAL SOLUTION UPTO THIS'
            WRITE (*, *) 'X = ', (BST(J), J=1, M), ' MIN F = ', FMIN
176:
177:
            ENDIF
178:
      999 FORMAT (5F15.6)
179:
            LCOUNT=LCOUNT+1
180:
       100 CONTINUE
181:
            WRITE(*,*)'OVER:',TIT(KF)
182.
183:
184:
            SUBROUTINE LSRCH(A, M, VI, NSTEP, FI)
185:
            IMPLICIT DOUBLE PRECISION (A-H,O-Z)
186:
            COMMON /KFF/KF
187:
            COMMON /RNDM/IU, IV
188:
            INTEGER IU, IV
189:
            DIMENSION A(*), B(100), VI(*)
190:
            AMN=1.0E30
191:
            DO J=1, NSTEP
192:
               DO JJ=1, M
193.
               B(JJ) = A(JJ) + (J-NSTEP/2-1) *VI(JJ)
194:
               ENDDO
195:
            CALL FUNC (B, M, FI)
196:
              IF (FI.LT.AMN) THEN
197:
              AMN=FI
198:
              DO JJ=1, M
199:
              A(JJ) = B(JJ)
200:
              ENDDO
201:
              ENDIF
```

```
202:
           ENDDO
203:
           FI=AMN
204:
           RETURN
205:
           END
206:
207:
           SUBROUTINE RANDOM (RAND1)
           DOUBLE PRECISION RAND1
208:
209:
            COMMON /RNDM/IU, IV
210:
           INTEGER IU, IV
211:
           RAND=REAL (RAND1)
212:
            IV=IU*65539
213:
            IF (IV.LT.0) THEN
214:
            IV=IV+2147483647+1
215:
            ENDIF
216:
            RAND=IV
217:
            IU=IV
218:
            RAND=RAND*0.4656613E-09
            RAND1=DBLE (RAND)
219:
220:
            RETURN
221 •
            END
222:
223:
           SUBROUTINE FUNC (X, M, F)
224: C
           New Test Function
225:
            IMPLICIT DOUBLE PRECISION (A-H, O-Z)
            COMMON /RNDM/IU, IV
226:
227:
            COMMON /KFF/KF
228:
            INTEGER IU, IV
229:
           DIMENSION X(*)
230:
           PI=4.D+00*DATAN(1.D+00)
231: C
232:
           IF (KF.EQ.1) THEN
233: C
234:
            FP=0.D00
235: C
236:
           F=0.D00
             237:
238:
239:
             IF (FP.GT.O.DOO) THEN
2.40:
            f=FP
241:
           ELSE
242:
           f=-4*dabs(dsin(X(1))*dcos(X(2))*dexp(dabs(dcos((X(1)**2+X(2)**2))
243:
          & 200))))
244:
           ENDIF
245:
           RETURN
246:
           ENDIF
247: C
248:
           IF (KF.EQ.2) THEN
249 . C
250:
           FP=0.D00
251:
           F = 0.000
252:
             if(x(1).lt.-9.5d00 .or. x(1).gt. 9.4d00) fp=fp+x(1)**2
253:
             if (x(2).1t.-10.9d00 .or. x(2).gt. 10.9d00) fp=fp+x(1)**2
254:
             IF (FP.GT.0.D00) THEN
255:
             F=FP
256:
           ELSE
257:
           f=-4*dabs(dsin(X(1))*dcos(X(2))*dexp(dabs(dcos((X(1)**2+X(2)**2)/
258:
          & 200))))
259:
           ENDIF
260:
           RETURN
261:
           ENDIF
262: C
263:
           IF (KF.EQ.3) THEN
264: C
265:
            FP=0.D00
266: C
267:
           F=0.D00
268:
             DO I=1, M
```

```
269:
             IF( DABS(X(I)).GT.10.D00) FP=FP+X(I)**2
270:
             ENDDO
271:
             IF (FP.GT.0.D00) THEN
272:
             F=FP
273:
           ELSE
           f = -dabs(dcos(X(1))*dcos(X(2))*dexp(dabs(1.d00-(dsqrt(X(1))**2+
274:
275:
          & x(2)**2)/pi))))
276:
           ENDIF
2.77:
           RETURN
278:
           ENDIF
279: C
280:
           IF (KF.EQ.4) THEN
281: C
282:
            FP=0.D00
283: C
           F=0.D00
284:
285:
             DO I=1, M
286:
             IF( DABS(X(I)).GT.10.D00) FP=FP+X(I)**2
287:
             ENDDO
288:
             IF (FP.GT.0.D00) THEN
289:
             F=FP
290:
           ELSE
           f=-1.d00/30*(dcos(X(1))*dcos(x(2))*dexp(dabs(1.d00-
291:
292:
          & (dsqrt(X(1)**2 + x(2)**2)/pi))))**2
293:
           ENDIF
294:
           RETURN
295:
           ENDIF
296: C
297:
           IF (KF.EQ.5) THEN
298:
             FP=0.D00
299: C
300: C
301:
           F=0.D00
302:
             DO I=1, M
303:
             IF( DABS(X(I)).GT.10.d00) FP=FP+X(I)**2
304:
305:
             IF (FP.GT.0.D00) THEN
306:
             F=FP
307:
           ELSE
308:
           f=-0.0001d00*(dabs(dsin(X(1))*dsin(X(2)))*dexp(dabs(100.d00-(dsqrt)))
309:
          & (X(1)**2+x(2)**2)/pi)))+1.d00)**(.1)
310:
           ENDIF
311:
           RETURN
312:
           ENDIF
313: C
314:
           IF (KF.EQ.6) THEN
315:
           FP=0.D00
316: C
317: C
           F=0.D00
318:
319:
             DO I=1, M
320:
             IF ( DABS(X(I)).GT.10.d00) FP=FP+dexp(dabs(X(I)))
321:
             ENDDO
322:
             IF (FP.GT.O.DOO) THEN
323:
             F=FP
324:
           ELSE
325:
           f=0.0001d00*(dabs(dsin(X(1))*dsin(X(2))*dexp(dabs(100.d00-
326:
          & (dsqrt(X(1)**2+x(2)**2)/pi)))+1.d00)**(.1)
327:
           ENDIF
328:
           RETURN
329:
           ENDIF
330: C
331:
           IF (KF.EQ.7) THEN
332:
             FP=0.D00
333: C
334: C
           F=0.D00
335:
```

```
336:
                                  DO I=1, M
337:
338:
                                   IF( DABS(X(I)).GT.10.d00) FP=FP+X(I)**2
339.
                                  ENDDO
340:
                                   IF (FP.GT.O.DOO) THEN
341:
                                  F=FP
342:
                             ELSE
343:
                             f = (dabs(dsin(X(1))*dsin(x(2))*dexp(dabs(100.d00-(dsqrt))))
344:
                           & (X(1)**2+x(2)**2)/pi)))+1.d00)**(-.1)
345:
                             ENDIF
346:
                             RETURN
347:
                             ENDIF
348: C
349:
                             IF (KF.EQ.8) THEN
350:
                             FP=0.D00
351: C
352: C
353:
                             F=0.D00
354:
                                 DO I=1, M
355:
356:
                                  IF( DABS(X(I)).GT.10.d00) FP=FP+X(I)**2
357:
                                   ENDDO
358:
                                   IF (FP.GT.0.D00) THEN
359:
                                  F=FP
360:
                             ELSE
361:
                            f=-(dabs(dsin(X(1))*dsin(x(2))*dexp(dabs(100.d00-(dsqrt)))
                          & (X(1)**2+x(2)**2)/pi)))+1.d00)**(-.1)
362:
363:
                             ENDIF
364:
                             RETURN
365:
                             ENDIF
366: C
367:
                             IF (KF.EQ.9) THEN
368: C
                                 FP=0.D00
369:
370: C
371:
                                  DO I=1, M
372:
                                   IF(DABS(X(I)).GT.11.D00) FP=FP+X(I)**2
373:
                                  ENDDO
374:
                                   IF (FP.GT.0.D00) THEN
375:
                                 F=FP
376:
                             f=-Dexp(-(Dabs(Dcos(X(1))*Dcos(X(2))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Dabs(1.D0-(Dsqrt)))*Dexp(Da
377:
378:
                           & (X(1)^{**2}+X(2)^{**2})/pi))))**(-1)))
379:
                             ENDIF
380:
                             RETURN
381:
                             ENDIF
382: C
                             IF (KF.EQ.10) THEN
383:
384: C
385:
                                 FP=0.D00
386: C
387:
                                  DO I=1, M
                                  IF (DABS(X(I)).GT.2*pi) FP=FP+X(I)**2
388:
389:
                                  ENDDO
390:
                                   IF (FP.GT.0.D00) THEN
391:
                                  F=FP
392:
                             ELSE
393:
                             f = (dsin(x(1))*dexp((1.d00-dcos(x(2)))**2) +
394:
                          & d\cos(x(2))*d\exp((1.d00-d\sin(x(1)))**2))+(x(1)-x(2))**2
395:
                             ENDIF
396:
                             RETURN
397:
                             ENDIF
398: C
399:
                             IF (KF.EQ.11) THEN
400: C
401:
                             F = 0.D00
402:
                             DO I=1, M
```

```
403:
           F=F+X(I)**2
404:
           ENDDO
405:
           RETURN
406:
           ENDIF
407: C
408:
           IF (KF.EQ.12) THEN
409: C
410:
             FP=0.D00
411: C
             DO I=1, M
412:
413:
             IF (DABS(X(I)).GT.1.2d00) FP=FP+X(I)**2
414:
             ENDDO
415:
             IF (FP.GT.O.DOO) THEN
416:
             F=FP
417:
           ELSE
418:
           f=100*(x(2)-x(1)**2)**2+(1.d00-x(1))**2
419:
           ENDIF
420:
           RETURN
421:
           ENDIF
422: C
423:
           IF (KF.EQ.13) THEN
424: C
425:
            FP=0.D00
426: C
427:
             DO I=1, M
428:
             IF(DABS(X(I)).GT.1.d00) FP=FP+X(I)**2
429:
             ENDDO
430:
             IF (FP.GT.0.D00) THEN
431:
             F=FP
432:
           ELSE
433:
           c=16.d00/15.d00
434:
           f = dsin(c*x(1)-1.d0) + dsin(c*x(1)-1.d0) **2 + dsin(4*(c*x(1)-1.d0)) /50 +
435:
          4\sin(c^*x(2)-1.d0)+\sin(c^*x(2)-1.d0)*^2+\sin(4^*(c^*x(2)-1.d0))/50+.6
436:
           ENDIF
437:
           RETURN
438:
           ENDIF
439: C
440:
           IF (KF.EQ.14) THEN
441: C
442:
             FP=0.D00
443: C
444:
             DO I=1, M
445:
             IF(DABS(X(I)).GT.100.d00) FP=FP+X(I)**2
446:
             ENDDO
447:
             IF (FP.GT.O.DOO) THEN
448:
             F=FP
           ELSE
449 •
           f1=dsin(dsqrt(x(1)**2+x(2)**2))**2-0.5d00
450:
451:
           f2=(1.d00+0.001*(x(1)**2+x(2)**2))**2
452:
           f=f1/f2 + 0.5d00
453:
           ENDIF
454:
           RETURN
455:
           ENDIF
456: C
457:
            IF (KF.EQ.15) THEN
458: C
459:
             FP=0.D00
460: 0
461:
             DO I=1, M
462:
             IF(DABS(X(I)).GT.30.d00) FP=FP+X(I)**2
463:
             ENDDO
464:
             IF (FP.GT.0.D00) THEN
465:
             F=FP
466:
           ELSE
467:
           f=X(1)**2-12*X(1)+11.D00+10*DCOS(PI*X(1)/2)+8*DSIN(5*PI*X(1))-
468:
          & (1/DSQRT(5.D00))*DEXP(-(X(2)-0.5D00)**2/2)
```

```
469:
           ENDIF
470:
           RETURN
471:
           ENDIF
472: C
473:
           IF (KF.EQ.16) THEN
474: C
475:
             FP=0.D00
476: C
             IF (X(1).LT. -1.5D00 .OR. X(1) .GT. 4.D00) FP=FP+X(1)**2
477:
             IF (X(2).LT. -3.D00 .OR. X(2) .GT. 4.D00) FP=FP+X(2)**2
478:
479:
              IF (FP.GT.0.D00) THEN
480:
             F=FP
481:
           ELSE
482:
           f = DSIN(X(1) + X(2)) + (X(1) - X(2)) **2 - 1.5 * X(1) + 2.5 * X(2) + 1.D00
483:
           ENDIF
484:
           RETURN
485:
           ENDIF
486: C
487:
           IF (KF.EQ.17) THEN
488: 0
           Levy #13 function
             FP=0.D00
489:
490: C
             DO I=1, M
491:
492:
             IF(DABS(X(I)).GT.10.d00) FP=FP+X(I)**2
493:
              ENDDO
494:
             IF (FP.GT.O.DOO) THEN
495:
             F=FP
496:
           ELSE
497:
           f = DSIN(3*PI*X(1))**2+(X(1)-1.D00)**2*(1.D00+DSIN(3*PI*X(2))**2) +
498:
          & (X(2)-1.D00)**2*(1.D00+DSIN(2*PI*X(2))**2)
499:
           ENDIF
500:
           RETURN
501:
           ENDIF
502: C
503:
           IF (KF.EQ.18) THEN
504: C
505:
            FP=0.D00
506: C
507:
             DO I=1, M
508:
             IF(DABS(X(I)).GT.5.d00) FP=FP+X(I)**2
509:
              ENDDO
510:
             IF (FP.GT.O.DOO) THEN
511:
             F=FP
512:
           ELSE
           f=2*X(1)**2-1.05*X(1)**4+X(1)**6/6 + X(1)*X(2)+X(2)**2
513:
514:
           ENDIF
515:
           RETURN
516:
           ENDIF
517: C
518:
           IF (KF.EQ.19) THEN
519: C
520:
             FP=0.D00
521: C
522:
             DO I=1, M
523:
              IF(DABS(X(I)).GT.5.d00) FP=FP+X(I)**2
524:
             ENDDO
525:
             IF (FP.GT.O.DOO) THEN
526:
             F=FP
527:
           ELSE
528:
           f = (X(1) **2 + X(2) **2 - 2 * X(1)) **2 + 0.25 * X(1)
529:
           ENDIF
530:
           RETURN
531:
           ENDIF
532: C
533:
           IF (KF.EQ.20) THEN
534: C
535:
             FP=0.D00
```

```
536: C
537:
              DO I=1.M
538:
              IF(DABS(X(I)).GT.5.d00) FP=FP+X(I)**2
539.
              ENDDO
540:
              IF (FP.GT.O.DOO) THEN
541:
             F=FP
542:
            ELSE
543:
            F=0.D00
544:
            DO I=1, M
           f=F+(X(I)**4-16*X(I)**2+5*X(I))
545:
546:
            ENDDO
547:
            F=F/2
548:
            ENDIF
549:
            RETURN
550:
            ENDIF
551: C
552:
            IF (KF.EQ.21) THEN
553: C
554:
              FP=0.D00
            -15. LE. X(1) .LE. -5 AND -3 .LE. X(2) .LE. 3
IF(X(1).LT. -15.D00 .OR. X(1) .GT. -5.D00) FP=FP+X(1)**2
555: C
556:
557:
              IF(DABS(X(2)).GT.3.D00) FP=FP+X(2)**2
558:
              IF(FP.GT.0.D00) THEN
559:
              F=FP
560:
            ELSE
            F=100*X(2)**2 + 0.01*DABS(X(1)+10.D0)
561:
562:
            ENDIF
563:
            RETURN
564:
            ENDIF
565: C
566:
            IF (KF.EQ.22) THEN
567: C
568:
             FP=0.D00
            -15. LE. X(1) .LE. -5 AND -3 .LE. X(2) .LE. 3
IF(X(1).LT. -15.D00 .OR. X(1) .GT. -5.D00) FP=FP+X(1)**2
569: C
570:
              IF (DABS(X(2)).GT.3.D00) FP=FP+X(2)**2
571:
572:
573:
              IF (FP.GT.O.DOO) THEN
574:
             F=FP
575:
            ELSE
576:
            F=100*DSQRT(DABS(X(2)-0.01D00*X(1)**2))+0.01*DABS(X(1)+10.D0)
577:
            ENDIF
578:
            RETURN
579:
            ENDIF
580: C
            IF (KF.EQ.23) THEN
581:
582: C
583 · C
584:
            CALL HOUGEN (M, X, F)
585:
            RETURN
586:
            ENDIF
587: C
            IF (KF.EQ.24) THEN
588:
            SINE ENVELOPE SINE WAVE FUNCTION (Generalized Schaffer)
589: C
            f=0.d00
590:
            fp=0.d00
591:
            f1=0.d00
592:
593:
            f2=0.d00
594:
            do I=1, m-1
595:
            f1=dsin(dsqrt(x(I+1)**2+x(i)**2))**2-0.5d00
            f2=(0.001d00*(x(I+1)**2+x(i)**2)+1.d00)**2
596:
            f=f+(f1/f2)+0.5d00
597:
598:
            enddo
599:
600:
            do I=1, m
601:
            if(dabs(x(i)).gt.100.d00) fp=fp+x(i)**2
602:
            enddo
```

```
603:
           if(fp.gt.0.d00) f=fp
604:
           return
605:
           endif
606: C
607:
           IF (KF.EQ.25) THEN
608: C
609:
           f=0.d00
610:
           fp=0.d00
611:
           do I=1, m-1
612:
           f1=-(x(I+1)+47.d00)
613:
           f2=dsin(dsqrt(dabs(x(I+1)+x(i)/2+47.d00)))
614:
           f3=dsin(dsqrt(dabs(x(i)-(x(I+1)+47.d00))))
615:
           f4=-x(i)
616:
           f=f+ f1*f2+f3*f4
617:
           enddo
618:
           do I=1, m
619:
           if(dabs(x(i)).gt.512.d00) fp=fp+x(i)**2
620:
           enddo
621:
           if(fp.gt.0.d00) f=fp
622:
           return
623:
           endif
624: C
625:
           IF (KF.EQ.26) THEN
626: C
          Modified Schaffer function #1
            FP=0.D00
627:
628: C
629:
           DO I=1, M
             IF(DABS(X(I)).GT.100.d00) FP=FP+X(I)**2
630:
631:
             ENDDO
632:
             IF (FP.GT.0.D00) THEN
633:
            F=FP
634:
           ELSE
635:
           f1=dsin(x(1)**2 + x(2)**2)**2-0.5d00
           f2=(1.d00+0.001*(x(1)**2+x(2)**2))**2
636:
           f=f1/f2 + 0.5d00
637:
638:
           ENDIF
639:
           RETURN
640:
           ENDIF
641: C
642:
           IF (KF.EQ.27) THEN
643: C
           Modified (Hyperbolized) Schaffer function #2
            FP=0.D00
644:
645: C
646:
           DO I=1, M
647:
             IF(DABS(X(I)).GT.100.d00) FP=FP+X(I)**2
648:
             ENDDO
649:
             IF (FP.GT.0.D00) THEN
650 •
            F=FP
651:
           ELSE
           f1=dsin(x(1)**2 - x(2)**2)**2-0.5d00
652:
653:
           f2=(1.d00+0.001*(x(1)**2+x(2)**2))**2
654:
           f=f1/f2 + 0.5d00
655:
           ENDIF
656:
           RETURN
657:
           ENDIF
658: C
659:
           IF (KF.EQ.28) THEN
660: C
           Modified (crossed) Schaffer function #3
           FP=0.D00
661:
662: C
663:
            DO I=1, M
664:
             IF(DABS(X(I)).GT.100.d00) FP=FP+X(I)**2
665:
             ENDDO
666:
             IF (FP.GT.O.DOO) THEN
667:
            F=FP
668:
           ELSE
                          dabs (x(1)**2 - x(2)**2) ))**2-0.5d00
669:
           f1=dsin(dcos(
```

```
670:
           f2=(1.d00+ 0.001*(x(1)**2 + x(2)**2))**2
671:
           f=f1/f2 + 0.5d00
672:
           ENDIF
673:
           RETURN
674:
           ENDIF
675: C
676:
           IF (KF.EQ.29) THEN
677: C
           Modified (crossed) Schaffer function #4
678:
             FP=0.D00
679: C
680:
             DO I=1, M
             IF(DABS(X(I)).GT.100.d00) FP=FP+X(I)**2
681:
682:
             ENDDO
683:
             IF (FP.GT.0.D00) THEN
684:
             F=FP
685:
           ELSE
686:
           f1=d\cos(d\sin(d\sin(x(1))) - x(2))
                                                         ))**2-0.5d00
687:
           f2=(1.d00+ 0.001*(x(1)**2 + x(2)**2))**2
688:
           f=f1/f2 + 0.5d00
689:
           ENDIF
690:
           RETURN
691:
           ENDIF
692: C
693:
           IF (KF.EQ.30) THEN
694: C
695:
           f=0.d00
           FP=0.D00
696:
697:
           DO I=1, M
           IF (DABS(X(I)).GT.4.28D00) FP=FP+DEXP(DABS(X(I)))
698:
699:
           ENDDO
700:
              IF (FP.NE.O.DOO) THEN
701:
           F=FP
702:
           RETURN
703:
               ELSE
704:
           DO I=1, M
705:
           CALL RANDOM (RAND)
706:
           F=F+(I*X(I)**4)+RAND
707:
           ENDDO
708:
           RETURN
709:
               ENDIF
710:
711: C
712:
           WRITE (*, *) 'FUNCTION NOT DEFINED. PROGRAM ABORTED'
713:
           STOP
714:
           END
715:
716:
           SUBROUTINE HOUGEN (M, A, F)
717:
           PARAMETER (N=13, K=3)
718:
           IMPLICIT DOUBLE PRECISION (A-H, O-Z)
719:
           DIMENSION X(N,K), RATE(N), A(*)
720: C
721: C
722: C
723:
724: C
725: C
726: C
727: C
728: C
729:
730: C
731: C
732: C
733: C
734: C
735: C
736:
           data x(1,1), x(1,2), x(1,3), rate(1) /470,300,10,8.55/
```

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```
737:
           data x(2,1), x(2,2), x(2,3), rate(2) /285, 80, 10, 3.79/
738:
           data x(3,1), x(3,2), x(3,3), rate(3) /470,300,120,4.82/
739:
           data x(4,1), x(4,2), x(4,3), rate(4) /470, 80, 120, 0.02/
740:
           data x(5,1), x(5,2), x(5,3), rate(5) /470,80,10,2.75/
741:
           data x(6,1),x(6,2),x(6,3),rate(6) /100,190,10,14.39/
           data x(7,1), x(7,2), x(7,3), rate(7) /100, 80, 65, 2.54/
742:
743:
           data x(8,1),x(8,2),x(8,3),rate(8) /470,190,65,4.35/
744:
           data x(9,1), x(9,2), x(9,3), rate(9) /100,300,54,13/
745:
           data x(10,1),x(10,2),x(10,3),rate(10) /100,300,120,8.5/
           data x(11,1),x(11,2),x(11,3),rate(11) /100,80,120,0.05/
746:
747:
           data x(12,1),x(12,2),x(12,3),rate(12) /285,300,10,11.32/
748:
           data x(13,1),x(13,2),x(13,3),rate(13) /285,190,120,3.13/
749: C
750: C
751:
752:
           F=0.D00
753:
           fp=0.d00
754:
           DO I=1, N
755:
           D=1.D00
756:
              DO J=1, K
757:
              D=D+A(J+1)*X(I,J)
758:
              ENDDO
759:
           FX = (A(1) *X(I, 2) -X(I, 3) /A(M)) /D
760: C
761: C
762:
           F=F+(RATE(I)-FX)**2
763:
           ENDDO
764:
           do j=1, m
765:
           if(dabs(a(j)).gt.5.d00) fp=fp+dexp(dabs(a(j)))
766:
           enddo
767:
           if(fp.gt.0.d00) f=fp
768:
           RETURN
769:
           END
```