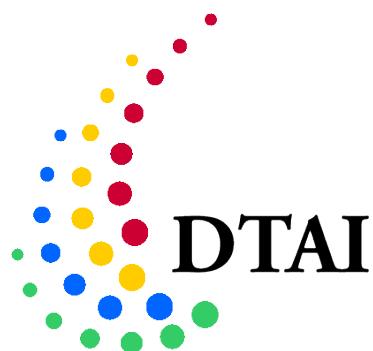


# Positive and Unlabeled Relational Classification through Label Frequency Estimation

Jessa Bekker

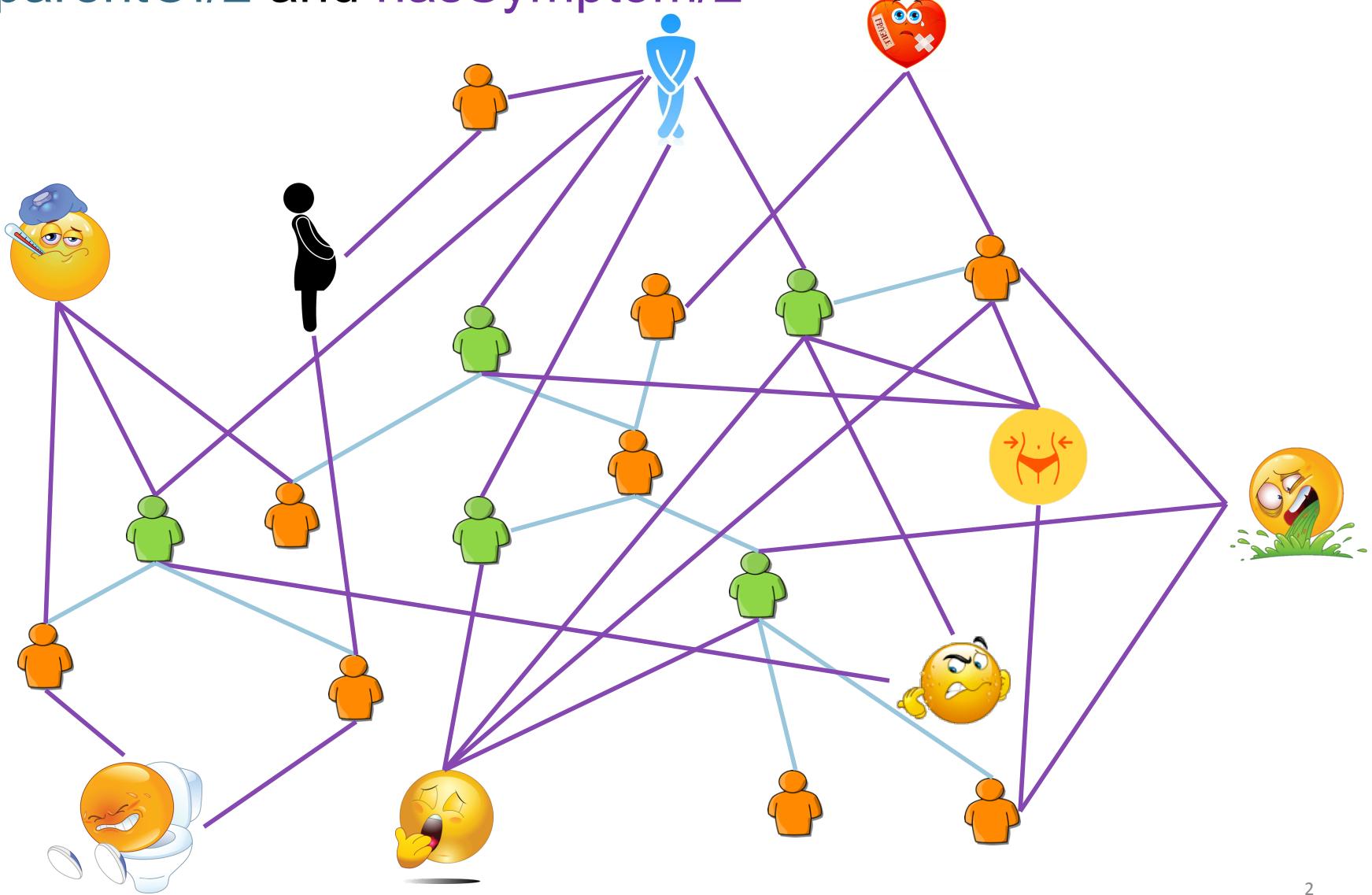
Jesse Davis

ILP 2017

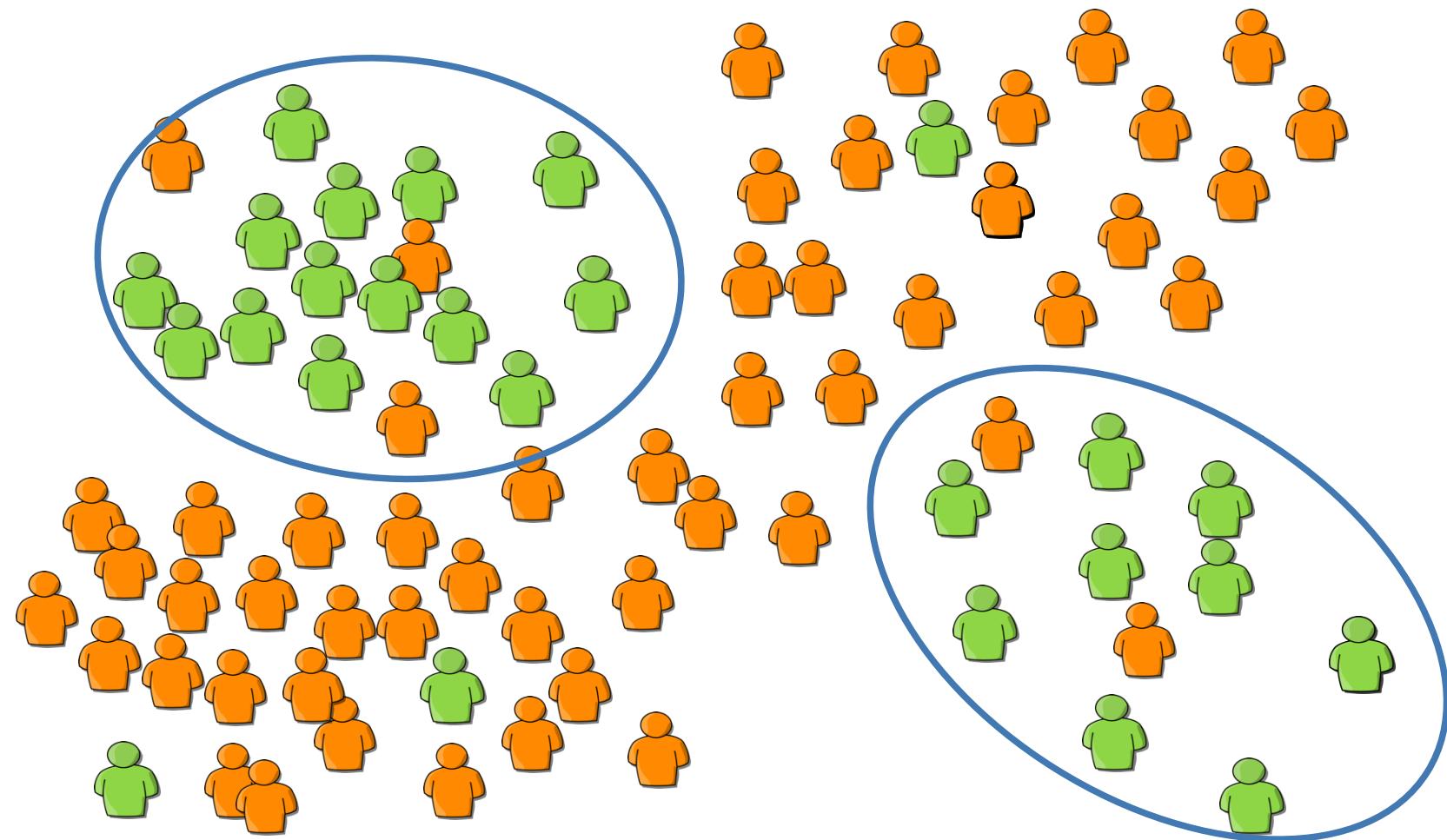


# Diabetes network

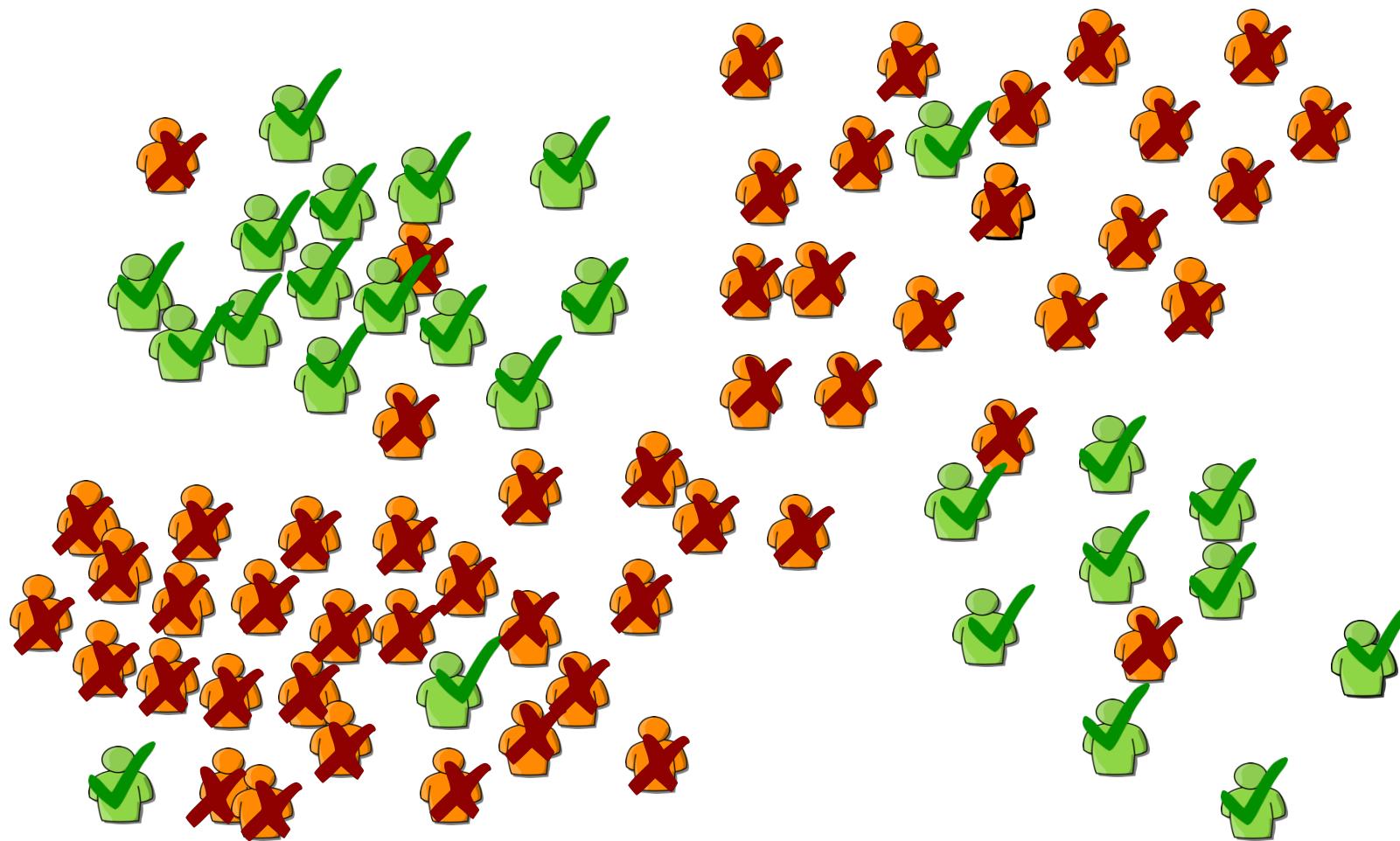
parentOf/2 and hasSymptom/2



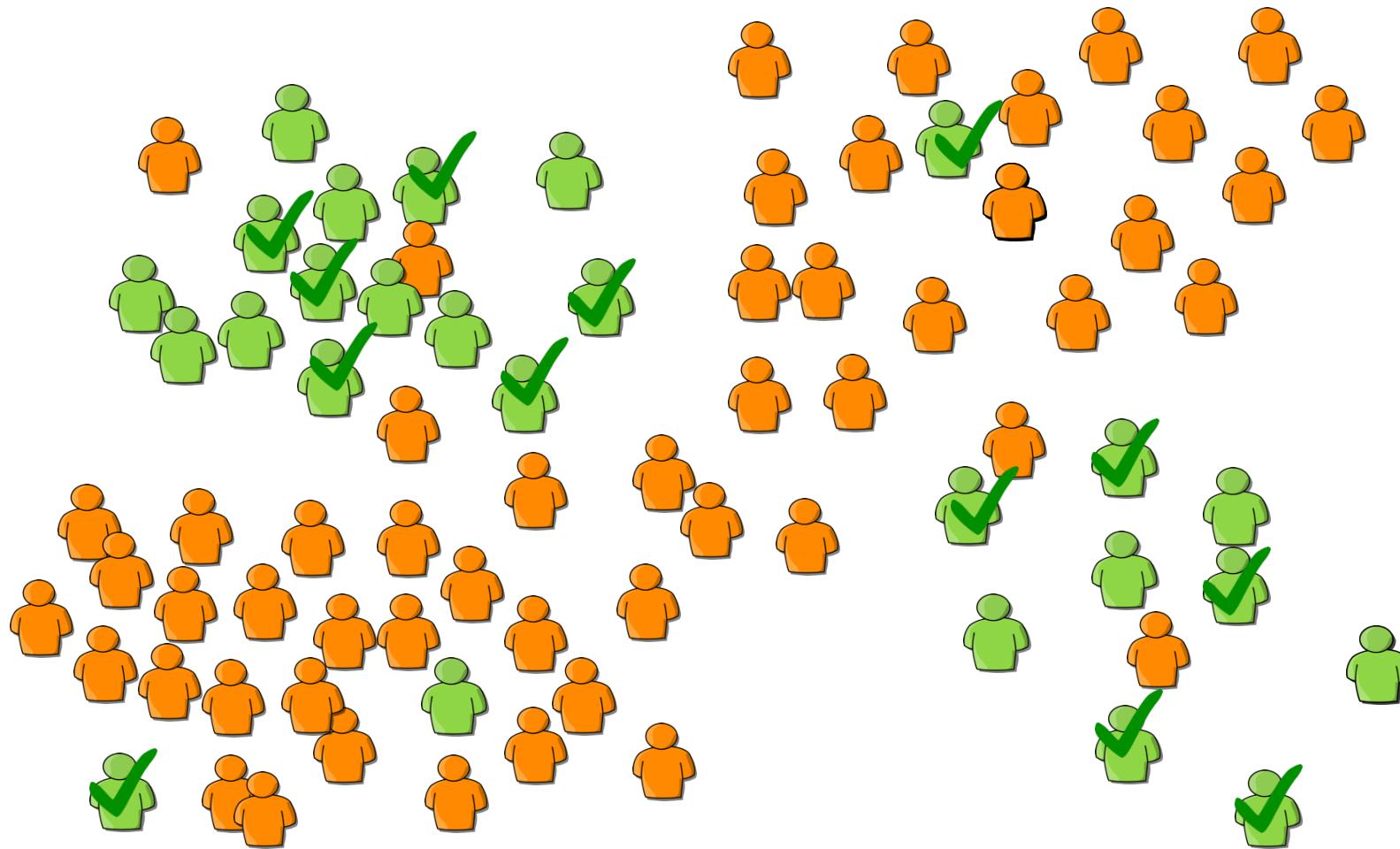
# Classification



# Supervised Data



# Positive and Unlabeled Data

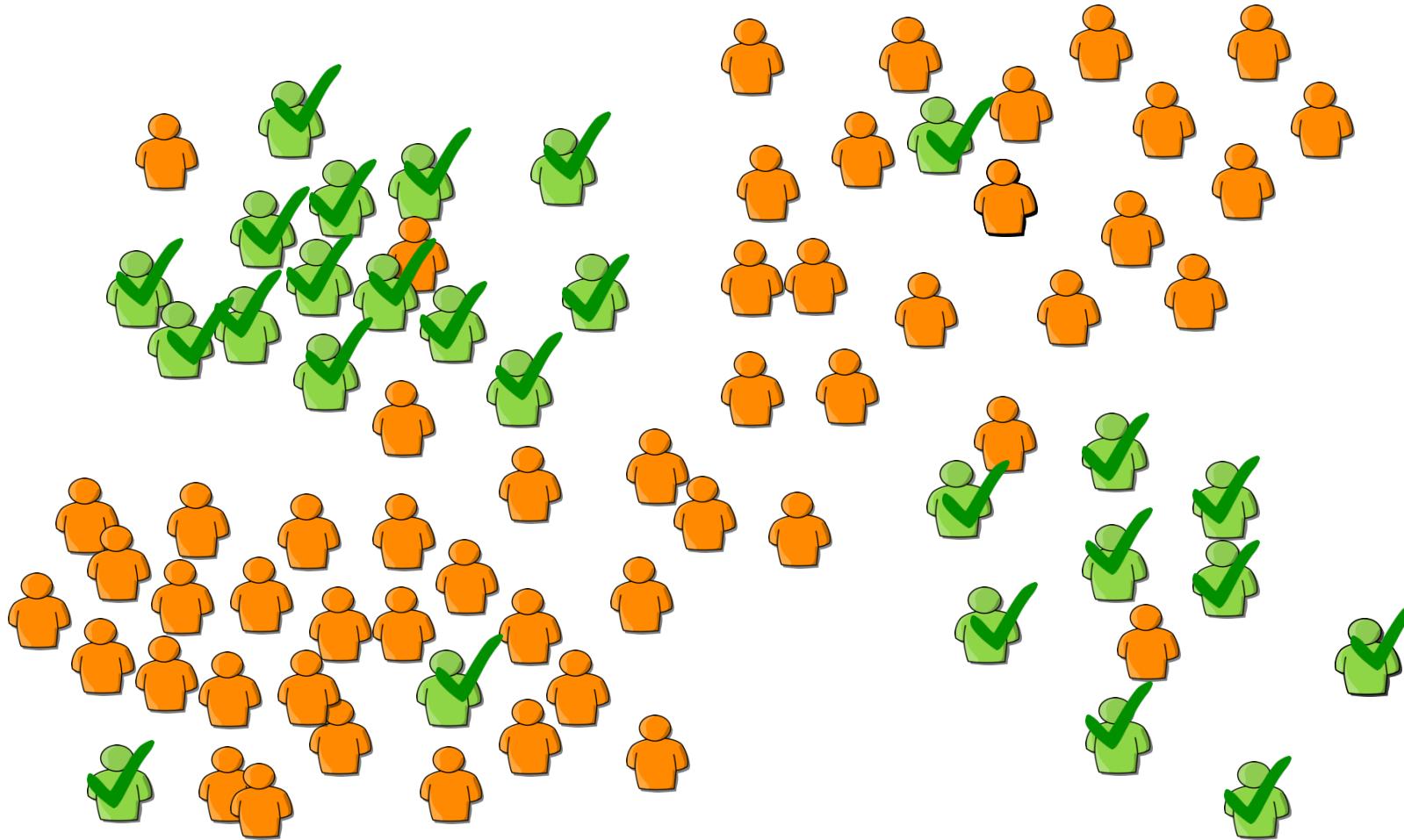


# Positive and Unlabeled Data: Label Frequency $c$

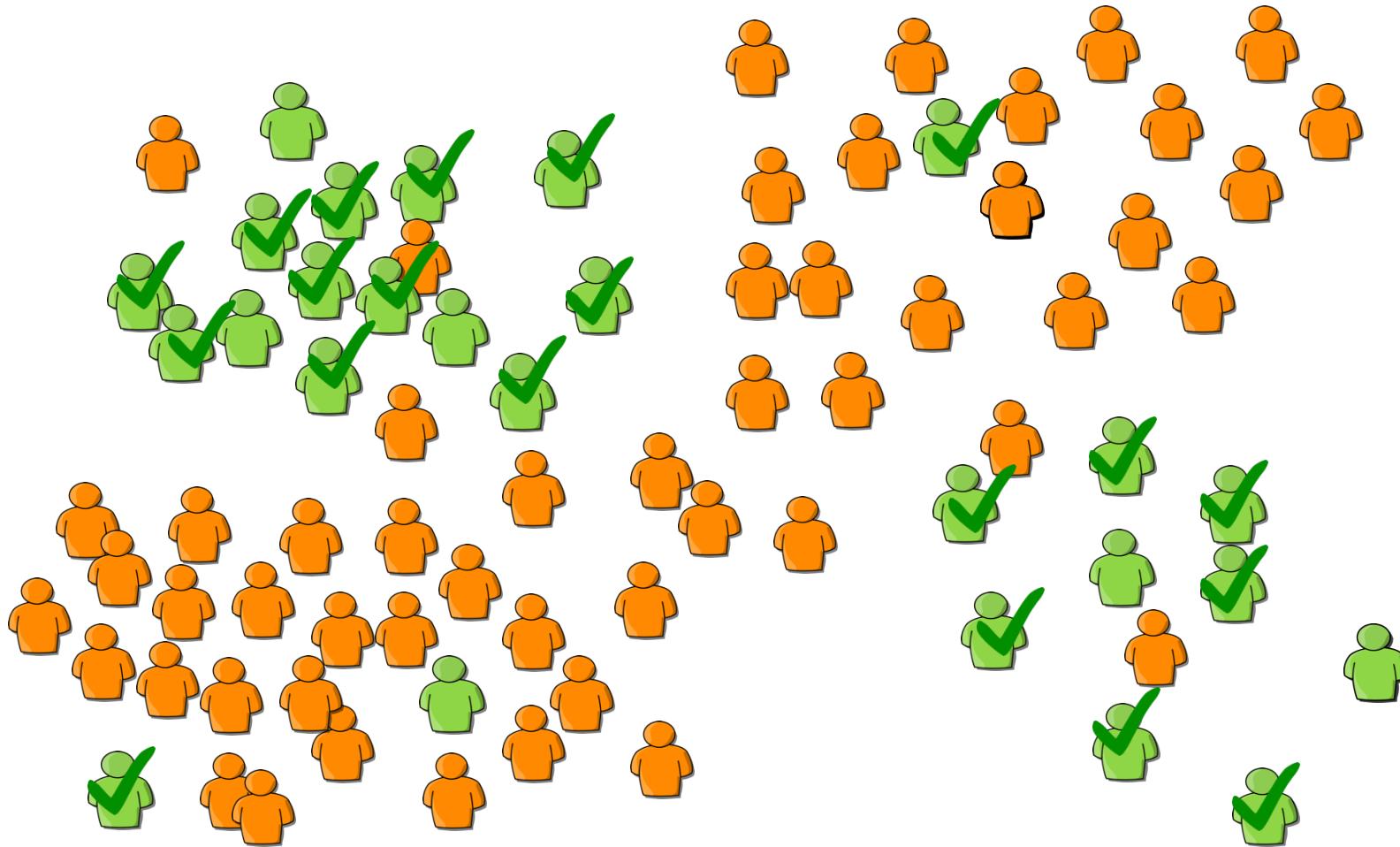
- Positive examples get labeled with constant probability  $c$

$$\begin{aligned} c &= P(\text{labeled} \mid \text{positive, facts}) \\ &= P(\text{labeled} \mid \text{positive}) \end{aligned}$$

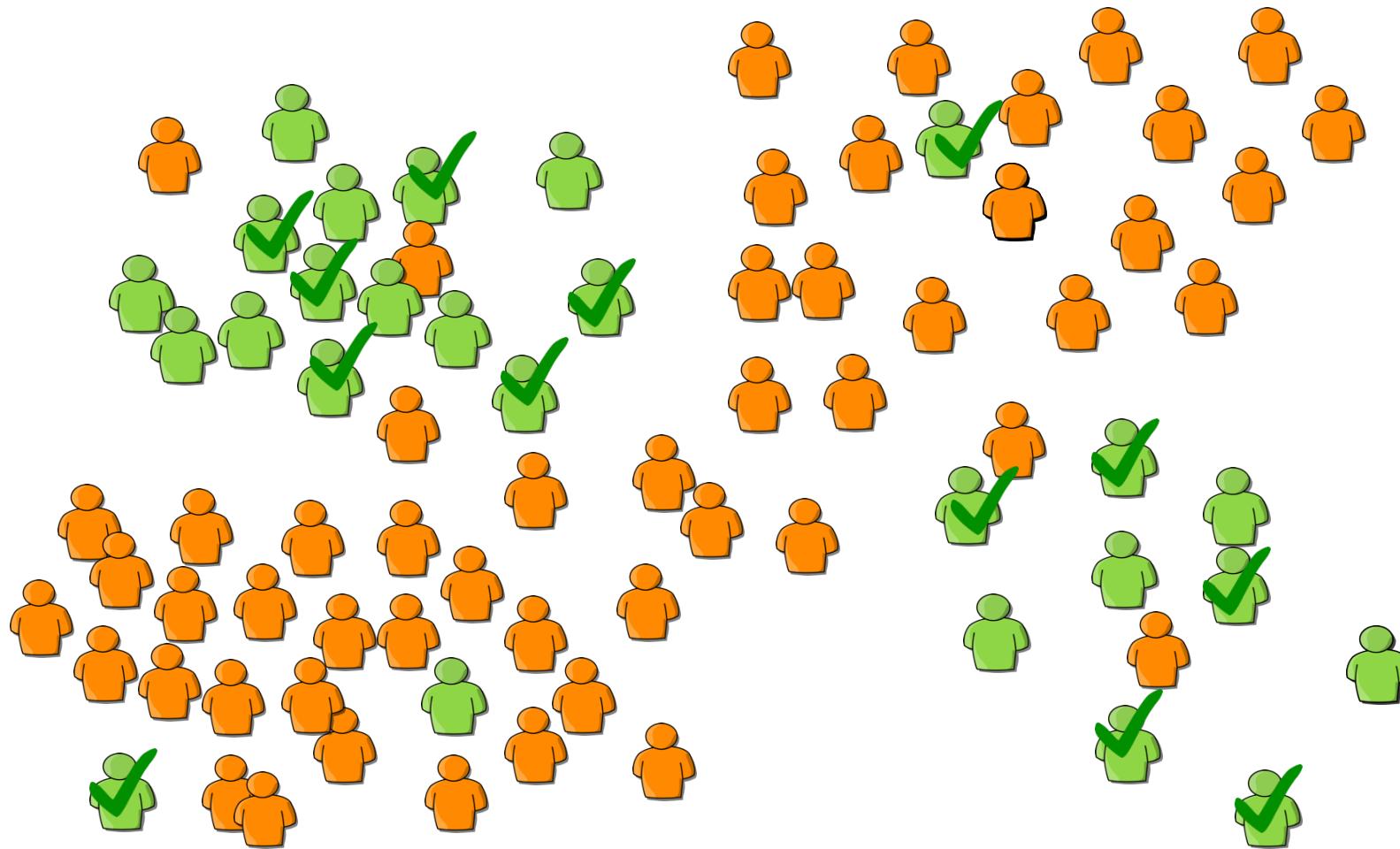
Label Frequency  $c = 1.0$  (= Supervised data)



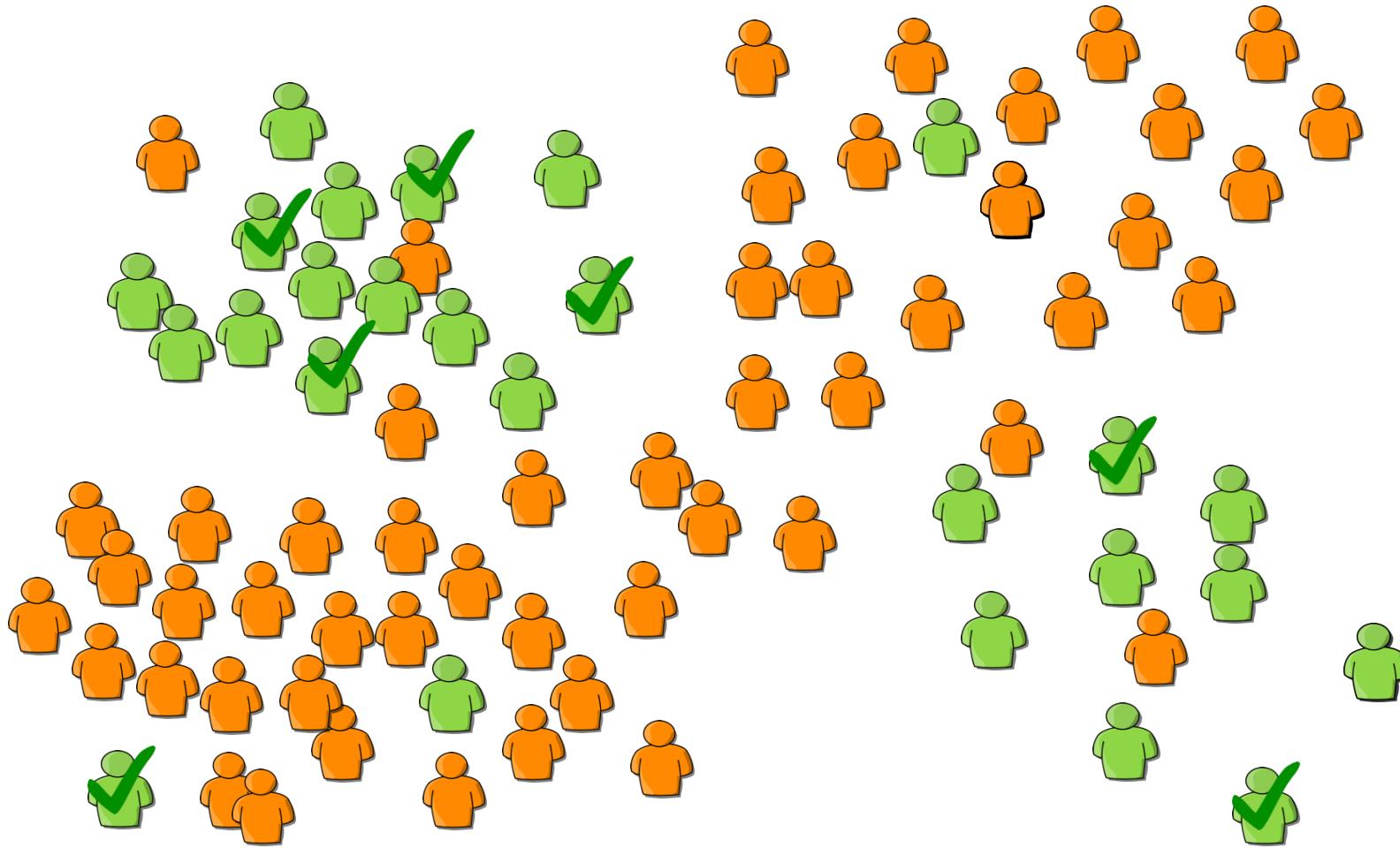
# Label Frequency $c = 0.75$



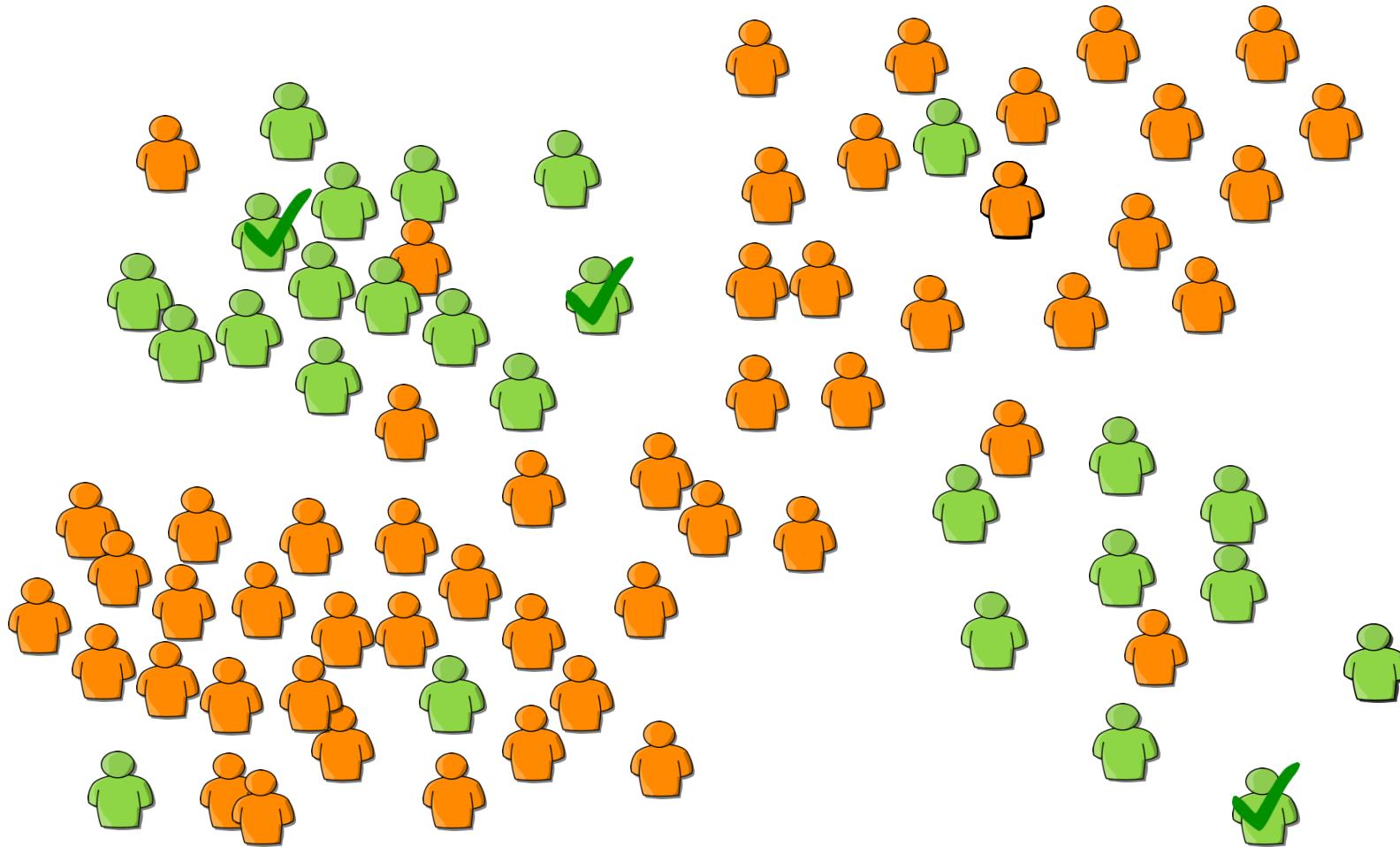
# Label Frequency $c = 0.5$



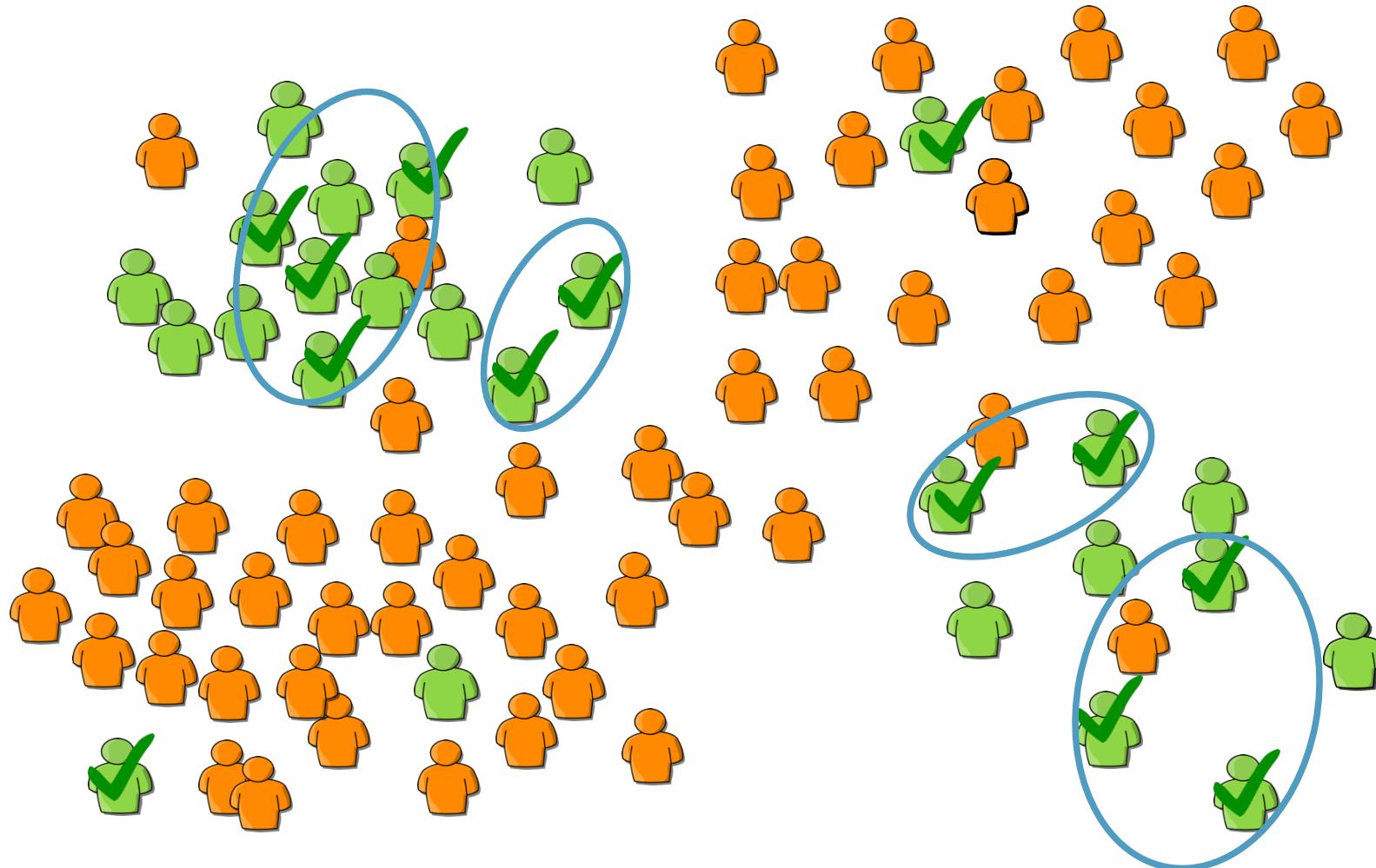
# Label Frequency $c = 0.25$



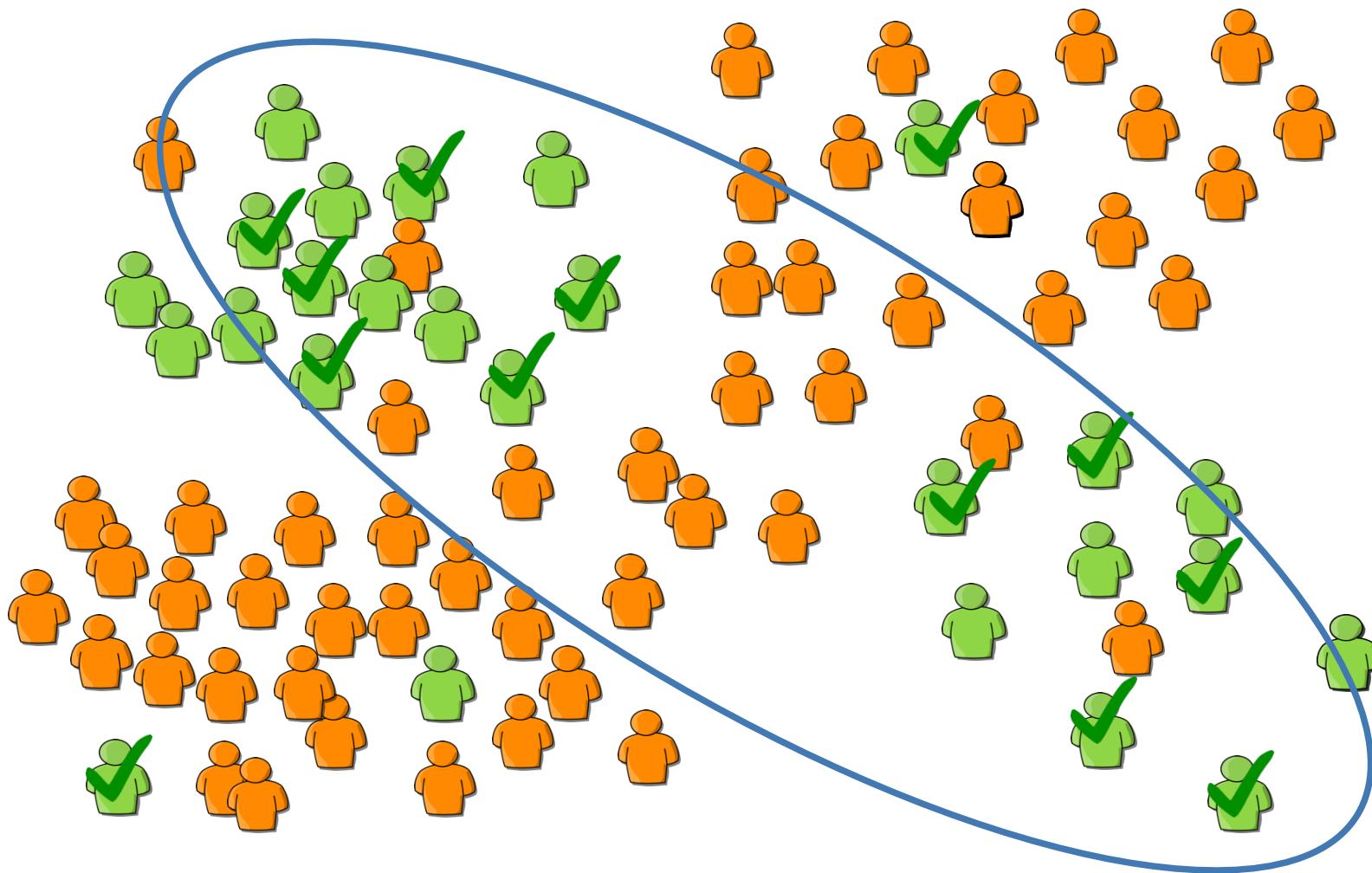
# Label Frequency $c = 0.1$



# Naïve Classification: Unlabeled = Negative



# Common Solution: Conjunctive Concept



[Muggleton, 1996]

# State of the Art in Propositional PU

*Knowing the label frequency  $c$   
makes PU learning easy*

[Elkan and Noto, 2008]

# Using the Label Frequency $c$

- 

$$P(\text{positive}|\text{facts}) = \frac{P(\text{labeled}|\text{facts})}{c}$$

Method 1: Probabilistic classifier that learns  $P(\text{labeled}|\text{facts})$

E.g. Tilde: Probabilistic Relational Decision Trees

Method 2: Adjust learning algorithm using  $c$ :

$$P=L/c \text{ and } N=T-P$$

E.g. Aleph: adjust score function

Supervised: Coverage =  $P-N$

PU: Coverage =  $L/c - (T-L/c) = 2L/c - T$

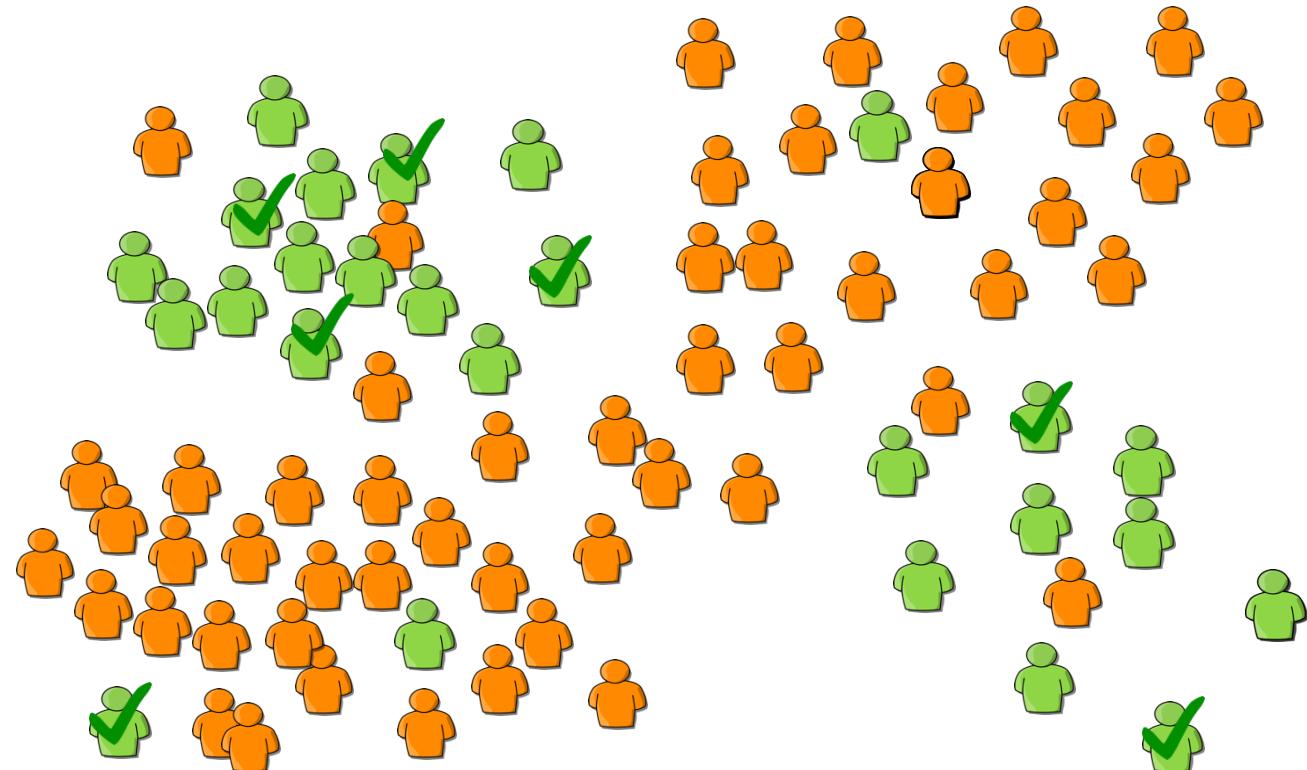
# How Can we Know the Label Frequency $c$ ?

1. Domain knowledge of class proportions
  2. Sample and label subset of the data
  3. Estimate directly from the data
    - Only propositional methods exist
    - Recent method is adaptable for relational settings
- [Bekker&Davis, under review]

# Lower bound on $c$ from Data

$$P \leq T \quad \rightarrow \quad c = \frac{L}{P} \geq \frac{L}{T}$$

$$\begin{aligned} T &= 78 \\ L &= 7 \\ c &\geq \frac{7}{78} = 0.09 \end{aligned}$$



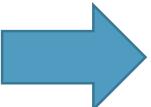
# Estimate $c$ from Data (TlcER)

- Insight 1: Data subset implies lower bound on  $c$

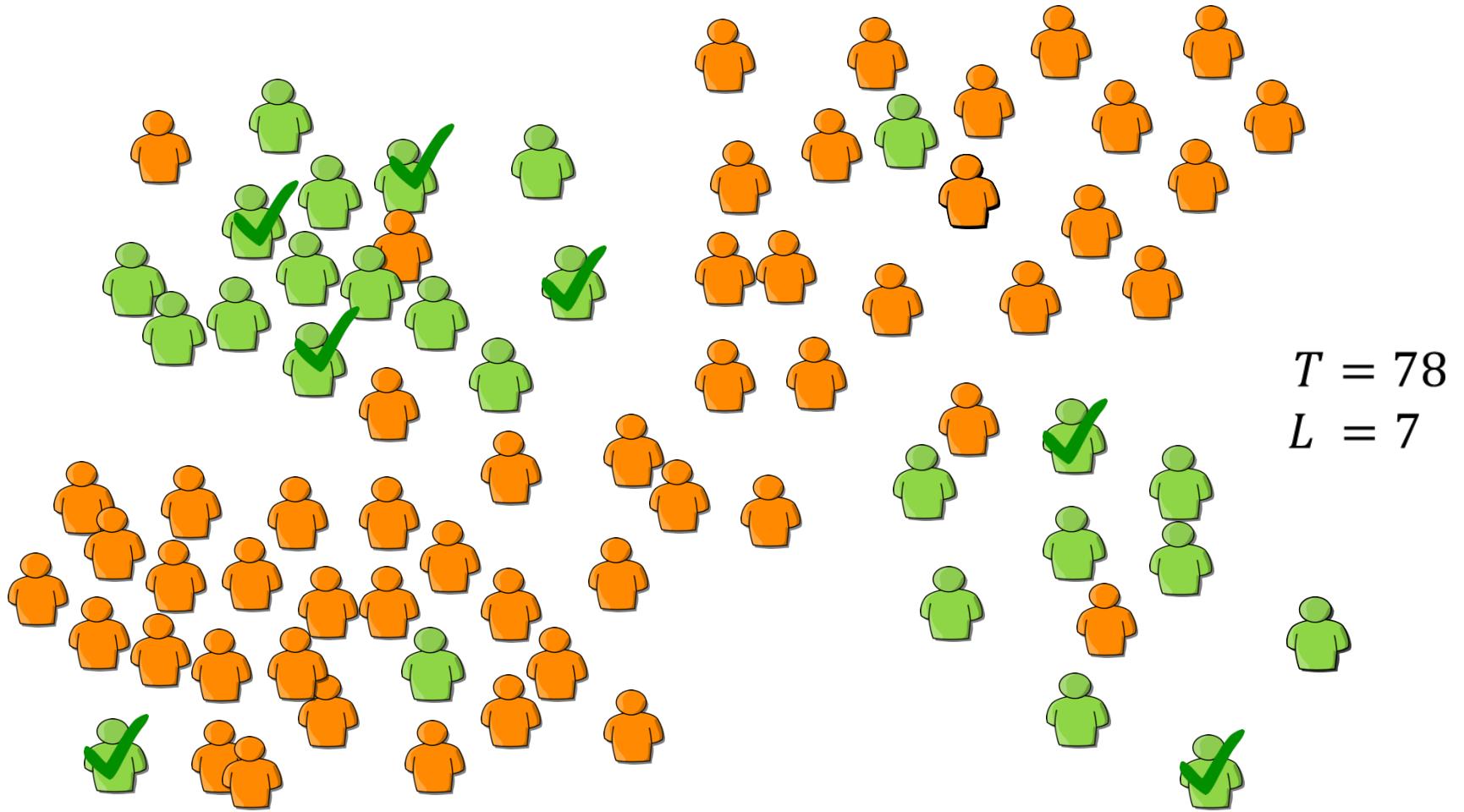
$$c \geq \frac{L}{T} - \varepsilon(T)$$

  
Error term from 1-sided  
Chebyshev inequality

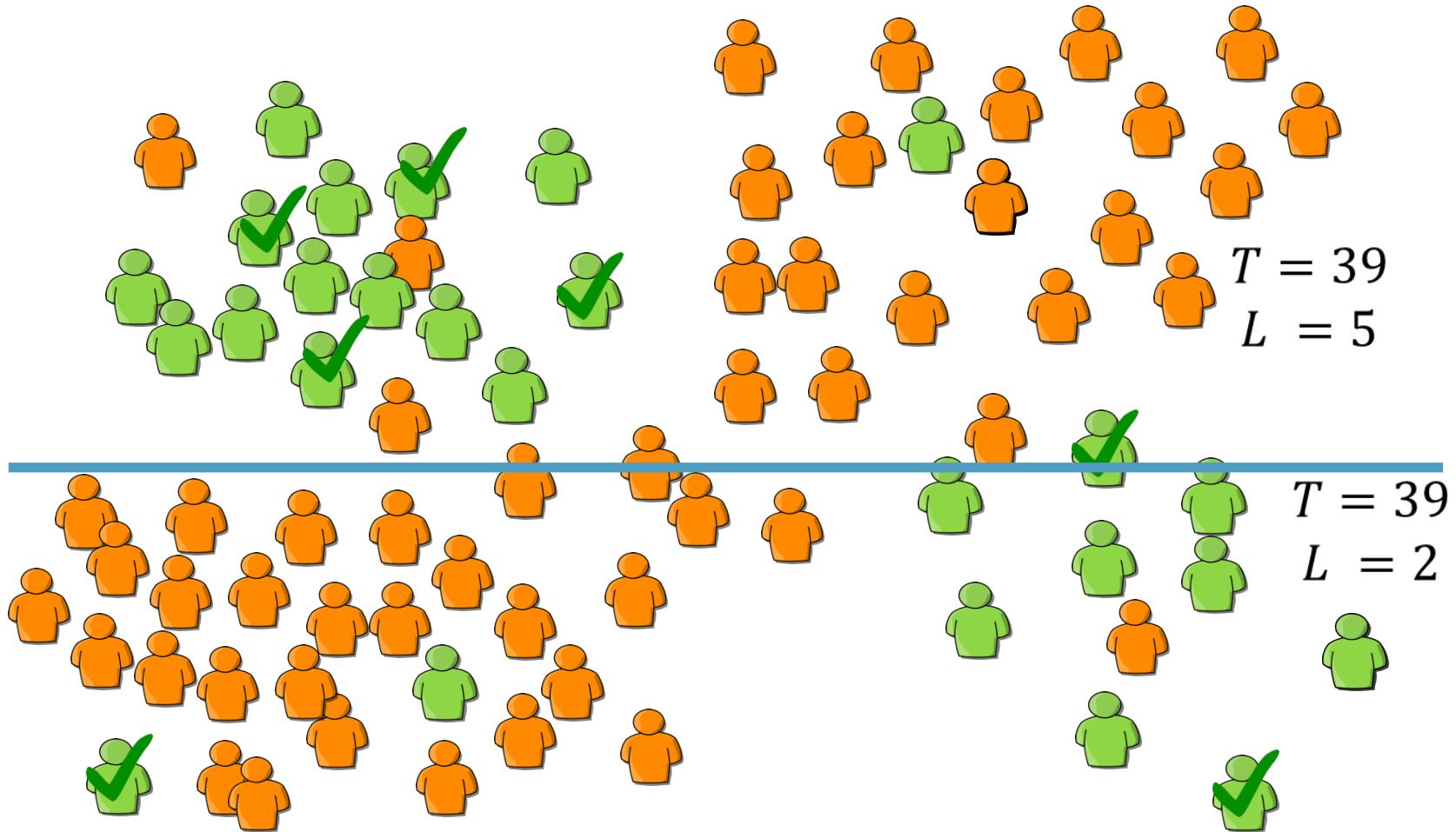
- Insight 2: Positive subsets give very tight bounds
- Insight 3: Highly labeled subsets are likely positive

 Look for those through decision tree induction (Tilde)  
Use subsets to tighten lower bound

# Intuition of TlcER

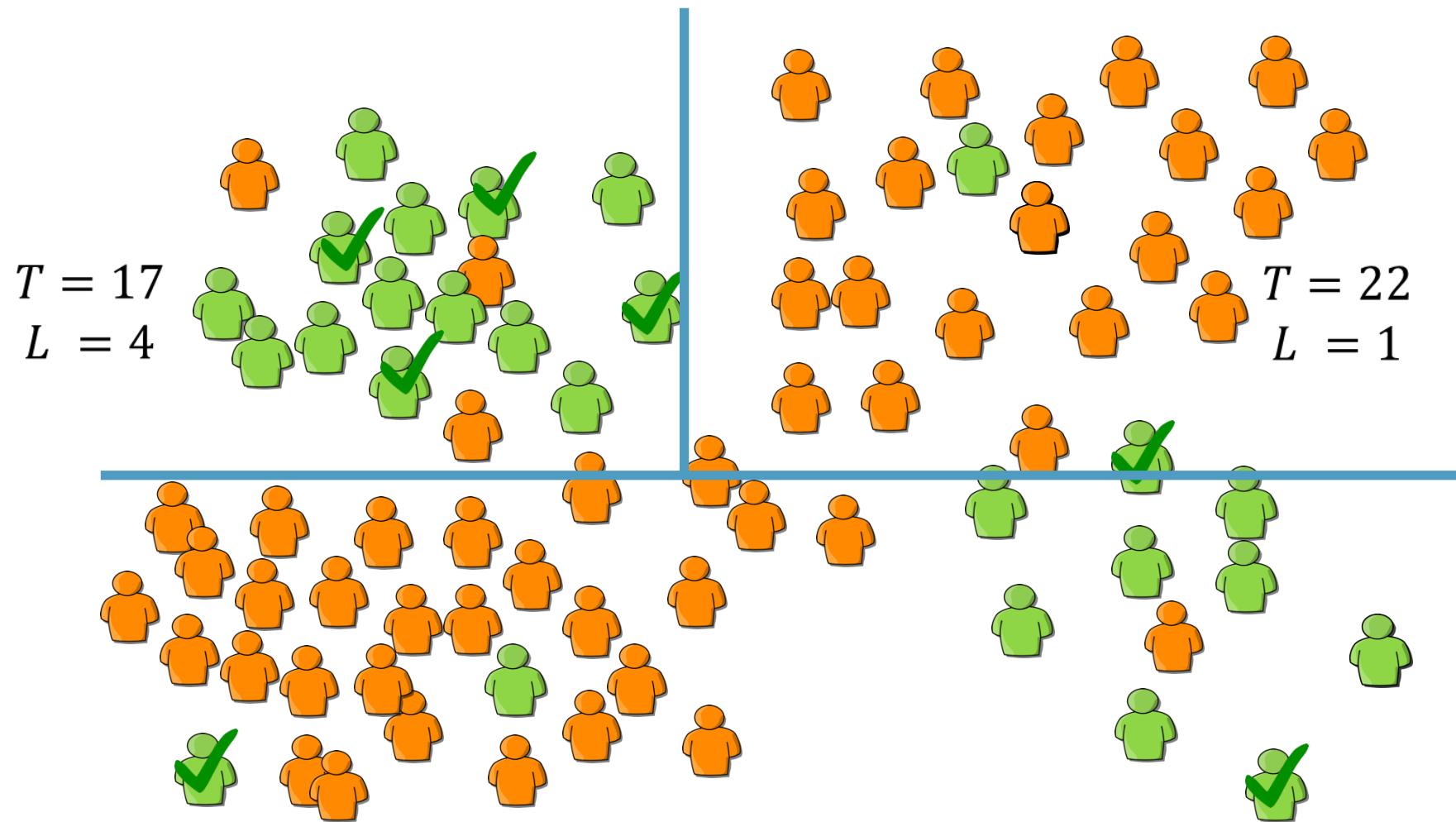


# Intuition of TlcER



$$c \geq \frac{5}{39} - \varepsilon(39) = 0.13 - \varepsilon_{20}(39)$$

# Intuition of TlcER



$$c \geq \frac{4}{17} - \varepsilon(17) = 0.24 - \varepsilon_{^{21}}(17)$$

# TlcER: Practical issues

Selecting subsets based on labels

→ likely to find subsets with a higher empirical label frequency.

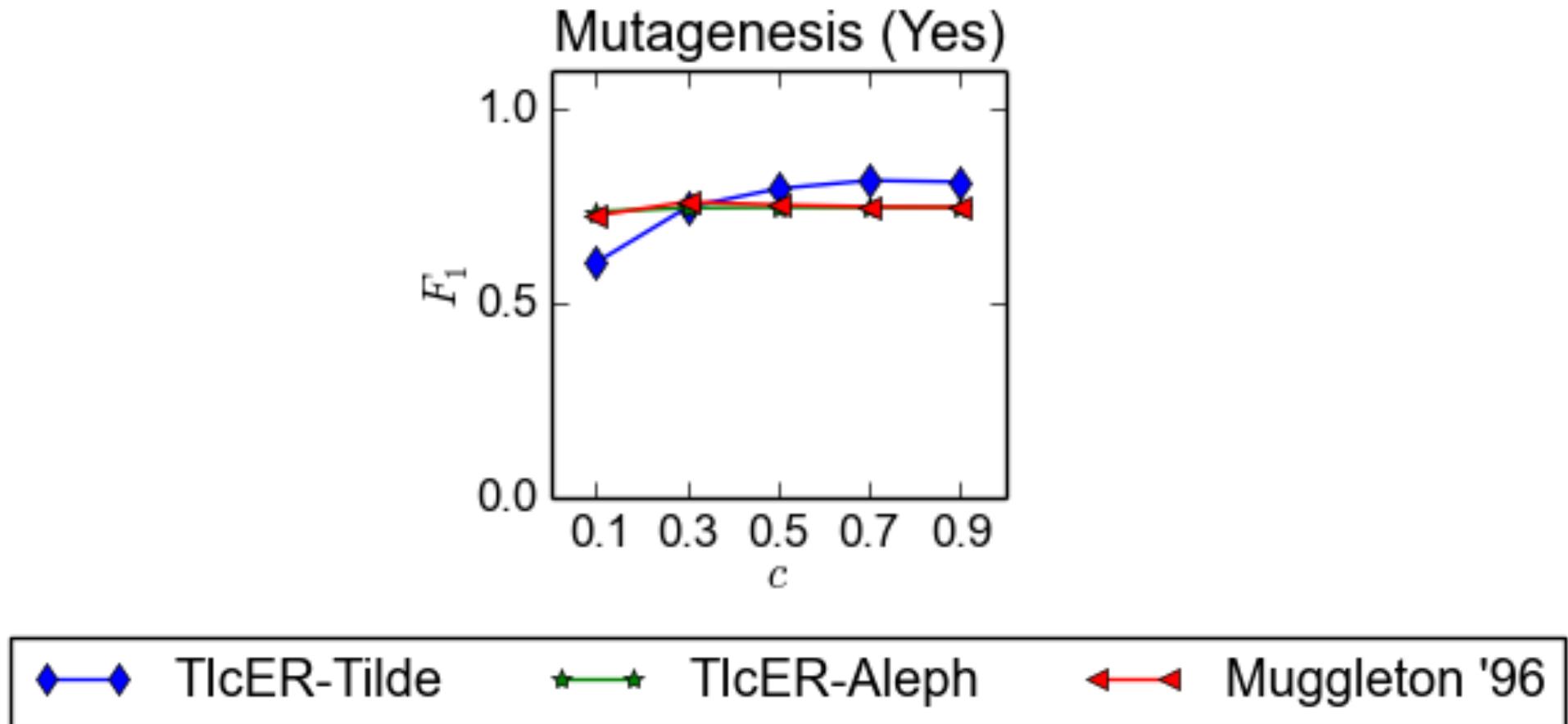
Solution:

Different datasets for tree induction and c estimation  
~ k-fold cross validation

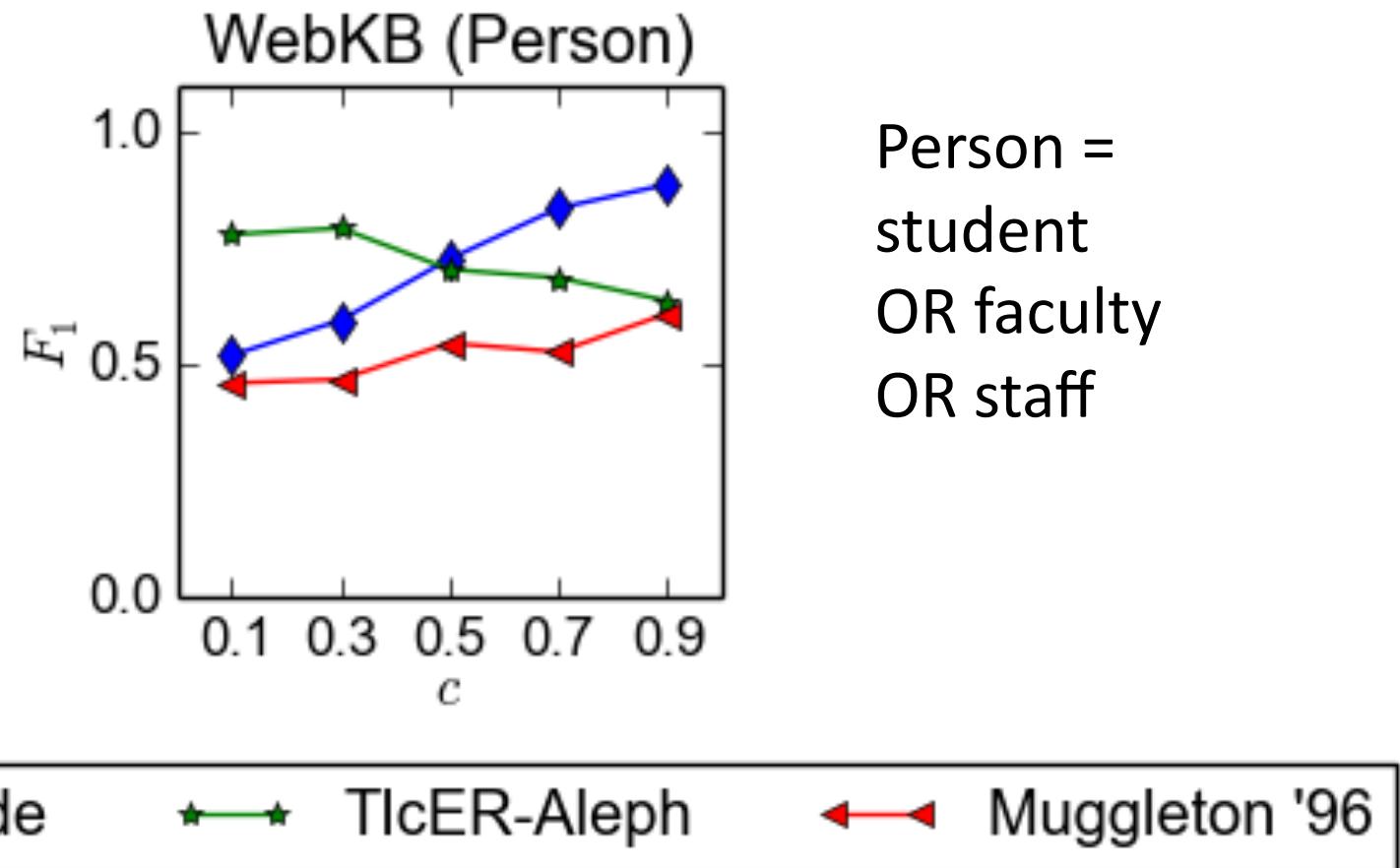
# Experimental results

- Estimate  $c$  from subsets found with Tilde
- use  $c$  to adjust 1) Tilde and 2) Aleph
- Compare with [Muggleton, 1996]

# Experimental results



# Experimental results



# Conclusion

- Knowing the label frequency makes PU learning easier
- Our method is capable of learning disjunctive concepts

# References

- Muggleton, Stephen. Learning from positive data. ILP, 1996.
- Elkan, Charles, and Noto, Keith. Learning classifiers from only positive and unlabeled data. KDD, 2008.
- Bekker, Jessa, and Davis, Jesse. Estimating the Class Prior in Positive and Unlabeled Data through Decision Tree Induction. Under review.

# Questions?