A Population Model of Polygenic Inheritance

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Abstract

This work describes and presents the results from a model based on the linear regression equation of polygenic inheritance. When applied to intergenerational movement between quintiles, the model obtained an R^2 of 0.92 and 0.93 with the Brookings Institution measures of intergenerational education and income mobility, respectively. The model better predicted measures of education and income mobility than those measures predicted one another: $R^2 = 0.84$. One original question motivated the creation of the model: consider the tallest one fifth of trees in a forest. Under polygenic inheritance, are a majority of them the offspring of the previous generation's tallest one fifth of trees or are a majority of them the offspring of the previous generation's shorter four fifths of trees? While tall trees are more likely to have tall offspring, there are far more average/short trees than tall trees. It is not immediately clear whether or at what point the effect of a higher probability of tall offspring outweighs the effect of a far greater number of offspring. A simulation of the model showed that a minority (43%) of trees above the 80th percentile are the offspring of the previous generation's tallest one fifth. The 72nd percentile is the equilibrium point at which the proportion is 50%. That is, of the trees above the 72nd percentile, half are the offspring of parents also above the 72nd percentile and half are the offspring of parents below the 72nd percentile.

1 Introduction

In biology, a phenotypic trait is a measurable trait that results from the expression of genes. As an example, the phenotype of hair color is the observed color while the genotype is the underlying genes that determine the color. The phenotypic traits Mendel studied in pea plants were unique in that they were determined single genes [Schacherer, 2016]. However, important phenotypic traits are often determined by many genes - in some cases hundreds or thousands. These traits are termed polygenic traits. In general, the phenotypic population distribution for polygenic traits follows a normal distribution. This phenomenon has been observed by plotting the frequency of phenotypes for a polygenic trait and finding a close approximation to a normal distribution. As described by Lange in his work on polygenic inheritance models, as the number of genes influencing a trait increases, the phenotypes in a population tend towards normality [Lange, 1997a, Lange, 1997b]. The approximation of normality is thought to occur because of the many possible allelic combinations among individual genes. In this additive genetic model, genes code for alleles with either positive or negative effects on a measurement of the trait [Rieger et al., 1968].

Human stature is known to be a non-sex-linked, nondominant, polygenic trait [Preece, 1996]. There are roughly 700 genes known to influence human height, each of which has a very small positive or negative effect on the measured trait [Wood and Esko, 2014]. The resultant population distribution of height is then Gaussian. Note that the Gaussian shape of the distribution is not contingent on how the individual gene effects are distributed. This is because the central limit theorem implies a normal population distribution about the average of the individual gene effects - the optimal phenotype - regardless of the distribution of the individual gene effects - uniform, normal, etc. The inheritance of height can be compared to flipping 700 coins and recording the number of heads minus the number of tails. (In this case, the individual gene effects fall into a shifted Bernoulli distribution.) If one were to run this experiment many times - once for each member in the population - the distribution of experimental results would fall into a normal distribution. That is, the experiments would most frequently result in a balanced number of heads versus tails and occasionally result in a largely imbalanced number of heads versus tails. It is worth noting that in the case of height, the phenotype is univariate, meaning that it is measured by one value. However, traits are sometimes multivariate, and the work presented here does not discuss such cases.

As the phenotypes of a population follow a normal distribution, their frequencies can be modeled by the equation for a normal distribution (1). In this equation, the parameter μ is the mean of the distribution (and also its median and mode); σ is its standard deviation.

$$f(x) = \frac{1}{\sigma\sqrt{2\pi}}e^{-\frac{1}{2}(\frac{x-\mu}{\sigma})^2} \tag{1}$$

When the population being described is the parent generation, the distribution is made up of all the parent phenotypic values x_p and their corresponding frequencies $f(x_p)$ are given by equation 2. The parameters μ_{pd} and σ_{pd} are the mean and standard deviation of the parent generation population.

$$f(x_p) = \frac{1}{\sigma_{pd}\sqrt{2\pi}} e^{-\frac{1}{2}\left(\frac{x_p - \mu_{pd}}{\sigma_{pd}}\right)^2}$$
 (2)

It is important to be precise about what is meant by the parent generation. When discussing intergenerational mobility and inheritance, it is common to separate the parent generation from the offspring/child generation for individual families [Becker et al., 2018, Mulligan, 1999]. For inheritance within a family, the phenotype of a single parent (the father or the mother) is distinguished from average phenotype of the parents, i.e., the mid-parental phenotype [Luo et al., 1998]. The calculation of mid-parental height has been a standard procedure for assessing the heights of individual children since it was first described by Tanner [Tanner et al., 1970]. The paradigm of considering the parent generation apart from the offspring generation can be extended to a population as a whole. Then, the distribution of the single parent phenotypes is distinguished from the distribution of the mid-parental phenotypes. In the latter case, the parents in the population are already matched to one another and their phenotypic values are averaged. The mid-parental phenotype distribution has a smaller variance than the pre-matched parent generation due to the regression that occurs in parent to parent matching. Parameter values on mid-parental phenotypes can be estimated from the data on the heights of adult children and their parents for 197 families collected by Francis Galton

in 1885. In this dataset, the standard deviation scores (SDSs) of fathers and mothers are not found to correlate (r = 0.074, p = 0.304) and the distribution of mid-parental phenotypes is found to have roughly one half (0.54) the variance of the distribution of individual parent phenotypes [Galton, 2017].

To the extent that polygenic traits are heritable, there exists a correlation between the phenotypes of parents and offspring. Previous studies have sought to measure the correlation between mid-parental and child SDSs for height. A pediatric growth study of English children found the correlation to be 0.47 (p < 0.01) [Wright and Cheetham, 1999]. An additional pediatric growth study of Swedish children found the correlation to be 0.59 (p < 0.01) [Luo et al., 1998]. To the extent that parent and offspring generation populations have the same variance, the correlation coefficient can be used to estimate the expected offspring/child height from the mid-parental height. This results from linear regression, in which there is a straight regression line (3) that provides the 'best' fit for related data points.

$$\hat{y} = \hat{\alpha} + \hat{\beta}x\tag{3}$$

In the case of polygenic inheritance, x refers to a mid-parental phenotypic value and \hat{y} refers to the expected phenotypic value of the offspring of the parents (which from now on will be indicated by \bar{x}_o). The parameters α and β are found by minimizing the sum of squared residuals between the mid-parental and offspring phenotypes. It can be shown that \hat{y} is given by equation 4, in which r is the correlation coefficient given by equation 5 and s_x , s_y denote the standard deviations of the x and y data, respectively.

$$\frac{\hat{y} - \bar{y}}{s_y} = r \, \frac{x - \bar{x}}{s_x} \tag{4}$$

$$r = \frac{Cov[x, y]}{\sqrt{Var[x]Var[y]}} \tag{5}$$

In polygenic inheritance, the x data are the mid-parental heights of the parent generation population. Mid-parental height can be calculated by taking the arithmetic mean of the mother's and father's height [Tanner et al., 1970]. Alternatively, male and female heights can first be normed by adding to all female heights the positive difference between the average male and average female height, then the arithmetic mean of the father's and adjusted mother's height can be taken [Wright and Cheetham, 1999]. This method used by Wright and Cheetham to normalize male and female heights can be applied to the parents and adult children in the Galton dataset to compare the mean and standard deviation of the parents and adult children. Then, the mean and standard deviation of the normalized adult children is found to be 0.00583% less than and 4.98% greater than those of the normalized parents, respectively. That is, the distribution of the parent generation appears to be more or less identical to the offspring generation, implying a stable population between generations. Nevertheless, the distribution of mid-parental heights will necessarily have a smaller standard deviation than the distribution of offspring heights because the mid-parental heights regress to the mean in parent to parent matching, as discussed earlier. However, assuming the offspring generation population exhibits similar levels of regression in offspring to offspring matching as the parent generation does, the mean and standard deviation of the post-matched offspring generation population and the postmatched parent generation population are equal. Furthermore, because offspring to offspring matching involves a simple linear transformation, the well measured correlation between post-matched (mid-parental) heights and offspring heights is the same between the post-matched parent heights and the post-matched offspring heights.

With this understanding, the expected post-matched phenotypic value for the offspring of the parents at the post-matched phenotypic value x_p is given by equation 6 and is similar to previous linear regression equations [Luo et al., 1998, Wright and Cheetham, 1999].

$$\bar{x}_o = \mu_{pd} + r(x_p - \mu_{pd}) \tag{6}$$

The parameter μ_{pd} is the mean phenotype of the parent population and the parameter r is the well-measured correlation coefficient between the mid-parental (post-matched) and child/offspring phenotypes. It is worth reiterating that this correlation will be the same between the post-matched parent generation and the post-matched offspring generation, assuming the offspring generation exhibits similar amounts of regression in

mother-father pairings. Therefore, when comparing the parent generation to the offspring generation, it is equivalent to compare the post-matched generations with one another, and the pre-matched generations with one another. The conversion from pre-matched to post-matched consists of a linear transformation of reducing the variance by the same proportion, about one-half. Then, \bar{x}_o can be considered pre-matched or post-matched, as long as x_p is considered the same. While equation 6 gives the mean of the distribution of the post-matched phenotypic values of the offspring of parents at x_p , it fails to describe the shape of the distribution. An analysis of the Galton data reveals the distribution to be closely approximated by a normal distribution about the expected offspring value \bar{x}_o , displayed in Figure 1. The offspring height in the Galton data is predicted with equation 4, in which the correlation between mid-parental and offspring height is found to be 0.51 (p < 0.01) [Galton, 2017]. Furthermore, when combining the residuals of the male and female adult children using the Wright and Cheetham normalization method, the standard deviation of the residuals is found to be 2.15 in, which compares to the parent generation standard deviation of 2.39 in. The ratio of the standard deviation of the offspring distribution residuals to the standard deviation of the parent generation distribution is then 0.90. This quantity will from now on be indicated by r_s .

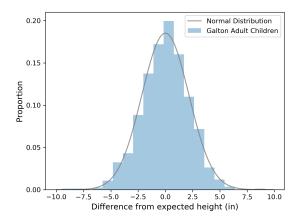


Figure 1: Combined residuals for all adult children in the Galton dataset. Male and female heights normalized with the Wright and Cheetham method [Galton, 2017, Wright and Cheetham, 1999].

A linear regression equation of the form of equation 6 dates back at least to Francis Galton. From the data he collected on height, Galton concluded that a person's characteristics are positively correlated with those of his parents. However, personal characteristics also "regress to mediocrity" so that, on average, the personal characteristics of a child are less extreme (i.e., closer to the mean) than those of his parents [Galton, 1877]. Galton's model can be represented as equation 7 in which x denotes an adult's personal characteristic such as height, and ϵ represents determinants of the adult's personal characteristic that is uncorrelated with the parent's personal characteristic.

$$x_{t+1} = \alpha + \beta x_t + \epsilon_{t+1} , \ \beta \in (0,1)$$
 (7)

Galton suggested that the appropriate model of inheritance has $\beta \in (0,1)$ and estimated β for height to be about 2/3 when x_t was measured as an average of maternal and paternal characteristics and 1/3 when x_t was measured as a single parent's characteristic. Galton even suggested that the same 2/3 dictates the inheritance of any personal characteristic [Galton, 1889]. Indeed, Mulligan writes that Galton's model gives similar predictions to other models of intergenerational income mobility. Mulligan concludes that "...the challenge facing economists is to produce a model of intergenerational mobility with predictions that are (a) distinct from Galton's, and (b) true." [Mulligan, 1999]. Any population model of polygenic inheritance should thus be assed by how well it predicts the mobility of socioeconomic characteristics in addition to polygenic ones.

In the population model proposed in this paper, the individual offspring distributions from each x_p are distributed normally about the expected offspring value \bar{x}_o with a standard deviation $r_s \sigma_{pd}$. These

distributions sum to form the distribution of the offspring generation. By integrating the contributions from sections of the parent distribution to sections of the total offspring distribution, important predictions can be made about the intergenerational movement of traits for populations that reproduce with regression to the mean. The model can be assessed by how closely its constructed offspring generation aligns with the measured offspring generation from the Galton data, assuming the measured parameter values for r and r_s in the Galton data. Furthermore, the model can be assessed by how well it predicts the intergenerational mobility of characteristics both for height and for income. Finally, the model can provide a theoretical answer to the original question that motivated the creation of the model: Consider the tallest members of a population; are most of them the children of the last generation's tallest members or shorter/average members? Although the tall members of the last generation have a higher probability of having tall children, there are many more average/short members than tall members. More specifically, at what SDS are those above the SDS equally the children of parents above the SDS and parents below the SDS? The population model can be validated by how well its answer to this question corresponds to the measured value in the Galton data.

2 Derivation of a Model

Individual Offspring Distribution

In the proposed model, the post-matched phenotypic values for the offspring of parents at x_p is normally distributed about \bar{x}_o , from equation 6, with a standard deviation $r_s \sigma_{pd}$. The frequencies are scaled by the frequency of the matched parent phenotypic value $f(x_p)$, from equation 2, to reflect the frequency of the mid-parental phenotype x_p . The distribution is then given by equation 8.

$$g(x) = f(x_p) \frac{1}{r_s \sigma_{pd} \sqrt{2\pi}} e^{-\frac{1}{2} (\frac{x - \bar{x}_o}{r_s \sigma_{pd}})^2}$$
 (8)

If r_s were to be 1, then the variance of the offspring from parents at x_p would be equal to the variance of the parent generation population. Instead, the measured $r_s = 0.90$ from the Galton data is used. Furthermore, if r were to be 1, then the center of the individual offspring distribution would be at the phenotype of the parents x_p , this would indicate complete inheritance and no regression toward the mean. On the other hand, if r were to be 0, then then parents at x_p would have offspring centered at the population mean, which would indicate no effect of inheritance and complete regression toward the mean. Instead, the value r = 0.50 is used, similar to the measured value of 0.51 from the Galton data. An example of an individual offspring distribution is displayed in Figure 2. It is important to note that g(x) does not indicate the absolute frequency but rather the relative frequency of the individual offspring. When the individual offspring distributions are combined to form the combined offspring generation distribution, they are scaled by a multiplicative factor m in equation 12, such that the size of offspring generation is equal to the size of the parent generation, for a stable population across generations.

The phenotypic value x_p corresponds to the z-score z_p - relative to the parent generation population. A complete description of the individual offspring distribution can then be made with equations 9, 10 and the following statement: The distribution of the offspring of parents at x_p is a normal distribution with frequencies proportional to $f(x_p)$.

$$z_o = r z_p \tag{9}$$

$$\sigma_o = r_s \, \sigma_{vd} \tag{10}$$

The statement and two equations provide an alternative - perhaps simpler - way of describing the individual offspring distribution than equation 8 and elucidates the role of r and r_s .

Offspring Generation Distribution

While g(x) describes the distribution of offspring from only one x_p , a function is needed to describe the distribution of the entire offspring-generation population. This distribution is made up of the combined individual offspring distributions from each x_p in the parent generation population. The frequencies of the

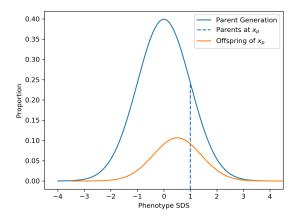


Figure 2: The individual offspring distribution of parents with the mid-parental SDS of 1. Parameters of r = 0.50 and $r_s = 0.90$ are used from the Galton data measured parameters [Galton, 2017].

phenotypes of the offspring-generation population can then be described the probability density function in equation 11.

$$G(x) = m \int_{-\infty}^{\infty} g(x) dx_p$$
 (11)

$$m = \frac{\int_{-\infty}^{\infty} f(x_p) dx_p}{\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} g(x) dx_p dx}$$
 (12)

Parent Generation Offspring Generation

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The frequency of each phenotype x in the offspring generation population is obtained by summing the frequency at x from the individual offspring distribution g(x) of each x_p in the parent generation. In order for the size of the offspring generation to be equal to the size of the parent generation, each frequency in the offspring generation distribution is scaled by the multiplicative factor m in equation 12. Figure 3

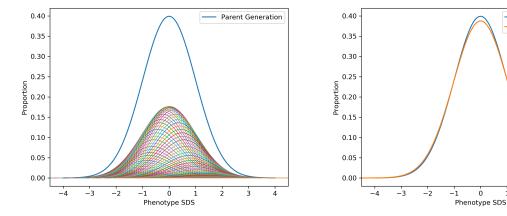


Figure 3: The individual offspring distribution of parents with the mid-parental SDS of 1. Parameters of r = 0.50 and $r_s = 0.90$ are used from the Galton data measured parameters [Galton, 2017].

It is important to remark that this distribution G(x) appears by all measures to be a normal distribution. This lends credence to the model as the offspring-generation population should indeed be normally distributed, and in most cases have a mean and standard deviation equal to those of the parent generation

distribution. The mean of the total offspring distribution is always equal the mean of the (total) parent distribution. On the other hand, the standard deviation of the total offspring distribution varies proportionally with both r and r_s .

3 Answer to the Motivating Question

At this point, it would seem to be possible to answer the motivating question: Are a majority of the tallest one fifth of trees in a forest the offspring of the previous generation's tallest one fifth? It is important to recognize that the area under a specific section of a population distribution bounded by phenotypic values represents the size of the population with those phenotypic values. In the case of the tallest one fifth of trees in a forest, the section is bound by k_2 and ∞ , where k_2 represents the phenotypic value (height) at the 80th percentile of the population distribution. For a given phenotypic value x_p in the parent generation population, it is necessary to find the size of its offspring population that is located in the top quintile. This is achieved by integrating x_p 's individual offspring distribution from k_2 to ∞ :

$$f(x_p) \frac{1}{\sigma_o \sqrt{2\pi}} \int_{k_2}^{\infty} e^{-\frac{1}{2} \left(\frac{x - \bar{x}_o}{\sigma_o}\right)^2} dx \tag{13}$$

The integral provides the amount of offspring with a phenotypic value above k_2 from parents with the phenotypic value x_p .

To find what proportion of the offspring in the top fifth of the offspring-generation population are from parents in the top fifth of the parent generation population, it is necessary to divide the amount of top fifth offspring from only those x_p in the top fifth of the parent population by the amount of top fifth offspring from all x_p in the parent population. This fraction gives the proportion of top fifth offspring from top fifth parents, the answer to the motivating question. The x_p in the top fifth of the parent distribution are bounded by k_1 and ∞ , where k_1 represents the height at the 80th percentile of the parent distribution. The following expression gives the amount of top fifth offspring from the top fifth parents.

$$\int_{k_1}^{\infty} f(x_p) \frac{1}{\sigma_o \sqrt{2\pi}} \int_{k_2}^{\infty} e^{-\frac{1}{2} (\frac{x - \bar{x}_o}{\sigma_o})^2} dx \, dx_p \tag{14}$$

This expression is then divided by the amount of top fifth offspring from all parents, which is a similar expression. The only difference is that the outer integral ranges over all members of the parent distribution $(-\infty \text{ to } +\infty)$. The inner integral can be simplified with the cumulative distribution function.

4 Intergenerational Movement of Two Forms

The calculations involved in answering the motivating question can be generalized to answer two types of questions.

The first type of question is to ask what proportion of an arbitrary section of the total offspring distribution is from another arbitrary section of the parent distribution. For example, one could ask what proportion of the offspring-generation population with z-scores of between 1 and 1.5 are the offspring of members of the parent generation population with z-scores of between -0.5 and 0. The motivating question was of this type, as it asked what proportion of a top section of the total offspring distribution was from the same top section of the parent distribution.

The second type of question is to ask what proportion of the offspring of parents in an arbitrary section of the parent distribution end up in another arbitrary section of the total offspring distribution. For example, one could ask what proportion of the offspring from parents with z-scores of between -2 and -1, have z-scores of between 1 and 2.

In answering these questions, it is helpful to define a Φ term as follows.

$$\Phi(k_1, k_2, k_3, k_4) \equiv \int_{k_1}^{k_2} f(x_p) \frac{1}{\sigma_0 \sqrt{2\pi}} \int_{k_3}^{k_4} e^{-\frac{1}{2} (\frac{x - \bar{x}_0}{\sigma_0})^2} dx \, dx_p \tag{15}$$

This term gives the size of the population with phenotypic values between k_3 and k_4 that are the offspring of members of the parent generation with phenotypic values between k_1 and k_2 . In other words, it provides the amount of a specific section of the offspring-generation population from a specific section of the parent generation population.

Proportion Attributable

To answer the first type of question, it is necessary to find the ratio of the Φ term for the specific section of the parent and offspring-generation population divided by the Φ term for the specific section of the offspring-generation population, but the entire parent generation population. This gives the proportion of the arbitrary section of the total offspring distribution that is the offspring of or 'attributable to' the arbitrary section of the parent distribution. The proportion is equivalent to the probability that a given member of the arbitrary section of the total offspring distribution is the offspring of a member of the arbitrary section of the parent distribution. The proportion attributable is given by the following equation.

$$P_a(k_1, k_2, k_3, k_4) = \frac{\Phi(k_1, k_2, k_3, k_4)}{\Phi(-\infty, \infty, k_3, k_4)}$$
(16)

The parameters k_3 and k_4 give the bounds of the arbitrary section of the total offspring distribution and the parameters k_1 and k_2 give the bounds of the arbitrary section of the parent distribution.

Proportion Destined

To answer the second type of question, it is necessary to find the ratio of the Φ term for the specific section of the parent and offspring-generation population divided by the Φ term for the specific section of the parent generation population, but the entire offspring-generation population. This gives the proportion of the offspring from the arbitrary section of the parent distribution that end up in or are 'destined to' the arbitrary section of the total offspring distribution. The proportion is equivalent to the probability that a given offspring of a parent in the arbitrary section of the parent distribution is a member of the arbitrary section of the total offspring distribution. The proportion destined is given by the following equation.

$$P_d(k_1, k_2, k_3, k_4) = \frac{\Phi(k_1, k_2, k_3, k_4)}{\Phi(k_1, k_2, -\infty, \infty)}$$
(17)

The parameters k_3 and k_4 give the bounds of the arbitrary section of the total offspring distribution and the parameters k_1 and k_2 give the bounds of the arbitrary section of the parent distribution.

5 Discussion

While the equations in the model do not have closed form solutions, they can be simulated with code. As a result, the answers to the questions presented here are approximations as the simulations are limited by computational speed.

To obtain values for intergenerational movement between quintiles, P_d was obtained for each quintile of the parent and total offspring distributions. The P_d 's were then compared to the measured values for education and income mobility provided by the Brookings Institution. If income and education are normally distributed in the population with regression towards the mean between parent and offspring, then a high correlation between the values provided by this model and those provided by the Brookings Institution might indicate that the equations presented here provide a good model of reproducing normal population distributions with regression towards the mean.

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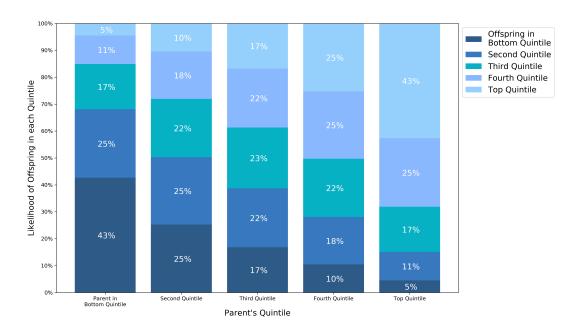


Figure 4: Intergenerational Mobility.

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References

[Becker et al., 2018] Becker, G. S., Kominers, S. D., Murphy, K. M., and Spenkuch, J. L. (2018). A theory of intergenerational mobility. *Journal of Political Economy*, 126(S1):S7–S25.

[Galton, 1877] Galton, F. (1877). Typical laws of heredity. *Proceedings of the Royal Institution*, 339(8):282–301.

[Galton, 1889] Galton, F. (1889). Natural inheritance. Macmillan, London.

[Galton, 2017] Galton, F. (2017). Galton height data. Harvard Dataverse.

[Lange, 1997a] Lange, K. (1997a). An approximate model of polygenic inheritance. Genetics, 147(3):1423–1430.

[Lange, 1997b] Lange, K. (1997b). The Polygenic Model. In: Mathematical and Statistical Methods for Genetic Analysis. Statistics for Biology and Health. Springer, New York, NY.

[Luo et al., 1998] Luo, Z. C., Albertsson-Wikland, K., and Karlberg, J. (1998). Target height as predicted by parental heights in a population-based study. *Pediatric Research*, 44(4):563–571.

[Mulligan, 1999] Mulligan, C. B. (1999). Galton versus the human capital approach to inheritance. *Journal of Political Economy*, 107(S6):S184–S224.

[Preece, 1996] Preece, M. A. (1996). The genetic contribution to stature. *Hormone Research in Pediatrics*, 45(Suppl. 2):56–58.

[Rieger et al., 1968] Rieger, R., Michaelis, A., and Green, M. (1968). A Glossary of Genetics and Cytogenetics. Springer, New York, NY.

[Schacherer, 2016] Schacherer, J. (2016). Beyond the simplicity of mendelian inheritance. Comptes Rendus Biologies, 339(7):284 – 288.

- [Tanner et al., 1970] Tanner, J. M., Goldstein, H., and Whitehouse, R. H. (1970). Standards for children's height at ages 2-9 years allowing for height of parents. *Archives of Disease in Childhood*, 45(244):755–762.
- [Wood and Esko, 2014] Wood, A. R. and Esko, T., e. a. (2014). Defining the role of common variation in the genomic and biological architecture of adult human height. *Nature Genetics*, 46(11):1173–1186.
- [Wright and Cheetham, 1999] Wright, C. M. and Cheetham, T. D. (1999). The strengths and limitations of parental heights as a predictor of attained height. *Archives of Disease in Childhood*, 81(3):257–260.