

1.a. Between 1111 and 0000.

b. Between 1000 and 0111.

2.a.  $(2^{11} + 2^{10} + 2^7 + 2^4 + 2^2 + 2^0)/2^4 = 3221/16 = 201.3125$

b.  $(-2^{11} + 2^{10} + 2^7 + 2^4 + 2^2 + 2^0)/2^4 = -875/16 = -54.6875$

3.a.  $-2^5 + 2^3 + 2^2 + 2^0 = -19$

b.  $B \Rightarrow 1011 \quad E \Rightarrow 1110 \quad E \Rightarrow 1110 \quad F \Rightarrow 1111$

$$-2^{15} + 2^{13} + 2^{12} + 2^{11} + 2^{10} + 2^9 + 2^7 + 2^6 + 2^5 + 2^3 + 2^2 + 2^1 + 2^0 = -16657$$

4.a. N	Quotient	Remainder	Result
150	75	0	0
75	37	1	10
37	18	1	110
18	9	0	0110
9	4	1	10110
4	2	0	010110
2	1	0	0010110
1	0	1	10010110

b. N	Quotient	Remainder	Result
1500	93	12	C
93	5	13	DC
5	0	5	5DC

5.a. N	Prod	Whole	Fraction	Result
.9	1.8	1	.8	.1
.8	1.6	1	.6	.11
.6	1.2	1	.2	.111
.2	.4	0	.4	.1110
.4	.8	0	.8	.11100

b. N	Prod	Whole	Fraction	Result
.9	14.4	14	.4	.E
.4	6.4	6	.4	.EE

6.a.  $A \Rightarrow 1010 \quad C \Rightarrow 1100 \quad . \quad E \Rightarrow 1110 \quad 5 \Rightarrow 0101$   
 $= 1010110011100101$

b.  $F \Rightarrow 1111 \quad A \Rightarrow 1010 \quad . \quad C \Rightarrow 1100 \quad E \Rightarrow 1110$   
 $= 11111010.11001110$

c.  $0010 \Rightarrow 2 \quad 1011 \Rightarrow B \quad . \quad 0110 \Rightarrow 6 \quad 1000 \Rightarrow 8 \quad = 2B.68$

7.a.  $2^6 + 2^4 + 2^2 + 2^0 = 85$  b.  $-2^7 + 2^5 + 2^3 + 2^1 = -86$

c.  $(-2^7 + 2^0)/2^4 = -127/16 = -7.9375$  d.  $(-2^7 + 2^4 + 2^2 + 2^1)/2^4 = -106/16 = -6.625$

e.  $(2^6 + 2^5 + 2^4 + 2^3 + 2^2 + 2^1)/2^4 = 126/16 = 7.875$

8.a.  $6=0110.$

N	Prod	Whole	Fraction	Result
.7	1.4	1	.4	.1
.4	.8	0	.8	.10
.8	1.6	1	.6	.101
.6	1.2	1	.2	.1011
.2	.4	0	.4	.10110
.4	.8	0	.8	.101100

$6.7=0110.1011 \Rightarrow 1001.0100 \Rightarrow 1001.0101$

b. N	Quotient	Remainder	Result
37	18	1	1
18	9	0	01
9	4	1	101
4	2	0	0101
2	1	0	00101
1	0	1	100101

$37 \Rightarrow 100101$

N	Prod	Whole	Fraction	Result
.1	.2	0	.2	.0
.2	.4	0	.4	.00
.4	.8	0	.8	.000
.8	1.6	1	.6	.0001
.6	1.2	1	.2	.00011

$37.1 \Rightarrow 0100101.00011 \Rightarrow 1011010.11100 \Rightarrow 1011010.11101$

c. N	Quotient	Remainder	Result
100	50	0	0
50	25	0	00
25	12	1	100
12	6	0	0100
6	3	0	00100
3	1	1	100100
1	0	1	1100100

$100 \Rightarrow 01100100 \Rightarrow 1011011 \Rightarrow 10011100$

d. N	Quotient	Remainder	Result
7	3	1	1
3	1	1	11
1	0	1	111

$7 \Rightarrow 0111$      $.7 \Rightarrow .1011$      $7.7 \Rightarrow 0111.1011 \Rightarrow 1000.0100 \Rightarrow 1000.0101$

9.a.  $01010101 \Rightarrow 10101010 \Rightarrow 10101011$

b.  $10101010 \Rightarrow 01010101 \Rightarrow 01010110$

c.  $1000.0001 \Rightarrow 0111.1110 \Rightarrow 0111.1111$

d.  $1001.0110 \Rightarrow 0110.1001 \Rightarrow 0110.1010$

e.  $0111.1110 \Rightarrow 1000.0001 \Rightarrow 1000.0010$

10.a.  $\frac{1}{2}^{(n-2)}$

b.  $\frac{1}{2}(8-2) \Rightarrow 1/64$

11. Most positive:  $011111 \Rightarrow 2^4 + 2^3 + 2^2 + 2^1 + 2^0 = 31$

Most negative:  $100000 \Rightarrow -2^5 = -32$

12. Min:  $000000 \Rightarrow 0$

Max:  $111111 \Rightarrow 2^5 + 2^4 + 2^3 + 2^2 + 2^1 + 2^0 = 63$

13. If it is unsigned.

14. No, because positive values always start with a zero so their max absolute value is always one less than the max absolute value of negative values.

17. N	Prod	Whole	Fraction	Result
1/6	2/6	0	2/6	.0
2/6	4/6	0	4/6	.00
4/6	8/6	1	2/6	.001
2/6	4/6	0	4/6	.0010
4/6	8/6	1	2/6	.00101
2/6	4/6	0	4/6	.001010
4/6	8/6	1	2/6	.0010101
2/6	4/6	0	4/6	.00101010

$.00101010 \Rightarrow (2^5 + 2^3 + 2^1)/2^8 = 42/256 = 0.1640625$

18. max value of 3 fractional decimal digits = .999

$.5 + .25 + (.25/2) + (.125/2) + .03125 + .015625 + .0078125 + .00390625 + .001953125 + (.001953125/2) = .9990234375$

10 fractional binary digits are needed to have the same resolution as 3 fractional decimal digits.