The formal definition of the unilateral or one-sided Laplace integral is:

$$\mathcal{L}{f(t)} = F(S) = \int_0^\infty f(t) e^{-st} dt$$

In case f(0) does not exists, one can use

$$\mathcal{L}{f(t)} = F(s) = \lim_{\varepsilon \downarrow 0} \int_{\varepsilon}^{\infty} f(t) e^{-st} dt$$

Linearity:

$$\mathcal{L}\{af(t) + bg(t)\} = aF(s) + bF(s)$$

Convolution:

$$\mathcal{L}\lbrace f(t) * g(t)\rbrace = \int_0^\infty f(\tau) g(t-\tau) d\tau = F(s) \cdot G(s)$$

Initial value theorem:

$$f(0^+) = \lim_{s \to \infty} sF(s)$$

Final value theorem:

$$f(\infty) = \lim_{s \to \infty} sF(s)$$

if all poles of sF(s) are in the left half-plane.

Table 1: Laplace transforms.			
Function	f(t)	F(s)	Convergence
Unit impulse	$\delta(t)$	1	For all s
Delayed unit impulse	$\delta(t- au)$	$e^{-\tau s}$	$\Re(s) > 0$
Unit step (Heaviside)	H(t)	$\frac{1}{s}$	$\Re(s) > 0$
Delayed unit step (Heaviside)	H(t- au)	$\frac{1}{s}e^{-\tau s}$	$\Re(s) > 0$
Ramp	t	$\frac{1}{s^2}$	$\Re(s) > 0$
Power (n integer)	t^n	$\frac{n!}{s^{n+1}}$	$\Re(s) > 0, n > -1$
Exponential decay	e^{-at}	$\frac{1}{s+a}$	$\Re(s) > -a$
Exponential approach	$1 - e^{-at}$	$\frac{1}{s(s+a)}$	$\Re(s) > -a$
Sine	$\sin(\omega t)$	$\frac{\omega}{s^2 + \omega^2}$	$\Re(s) > 0$
Cosine	$\cos(\omega t)$	$\frac{s}{s^2 + \omega^2}$	$\Re(s) > 0$
Hyperbolic sine	$sinh(\alpha t)$	$\frac{\alpha}{s^2 - \alpha^2}$	$\Re(s) > \alpha $
Hyperbolic cosine	$\cos(\alpha t)$	$\frac{s}{s^2 - \alpha^2}$	$\Re(s) > \alpha $
Exponential decay sine	$e^{-at}\sin(\omega t)$	$\frac{\omega}{(s+a)^2+\omega^2}$	$\Re(s) > -a$
Exponential decay cosine	$e^{-at}\sin(\omega t)$	$\frac{s+a}{(s+a)^2+\omega^2}$	$\Re(s) > -a$
nth root	$\sqrt[n]{t}$	$\frac{1}{s^{\frac{1}{n}+1}}\Gamma\left(\frac{1}{n}+1\right)$	$\Re(s) > 0$
Natural logarithm	ln t	$\frac{-\ln(s)-\gamma}{s}$	$\Re(s) > 0$