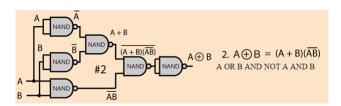
Proof XOR from nands

The schematic of the NANDS and formula:



$$f = a \oplus b \qquad \text{the function}$$

$$= (a+b) \cdot (\overline{a} \cdot \overline{b}) \qquad \text{the form}$$

$$= (a+b) \cdot (\overline{a} + \overline{b}) \qquad \text{De Morgan}$$

$$= a \cdot \overline{a} + a \cdot \overline{b} + b \cdot \overline{a} + b \cdot \overline{b} \qquad \text{multiply out}$$

$$= 0 + a \cdot \overline{b} + b \cdot \overline{a} \qquad \text{reduce}$$

$$= a \cdot \overline{b} + b \cdot \overline{a} \qquad \text{skip 0}$$

$$= a \cdot \overline{b} + \overline{a} \cdot b \qquad \text{commutative law}$$

$$= \overline{a} \cdot b + a \cdot \overline{b} \qquad \text{commutative law}$$

$$= a \oplus b \qquad \text{the XOR}$$