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The University of Texas at Austin

# Machine Learning at TACC

## Unsupervised Learning

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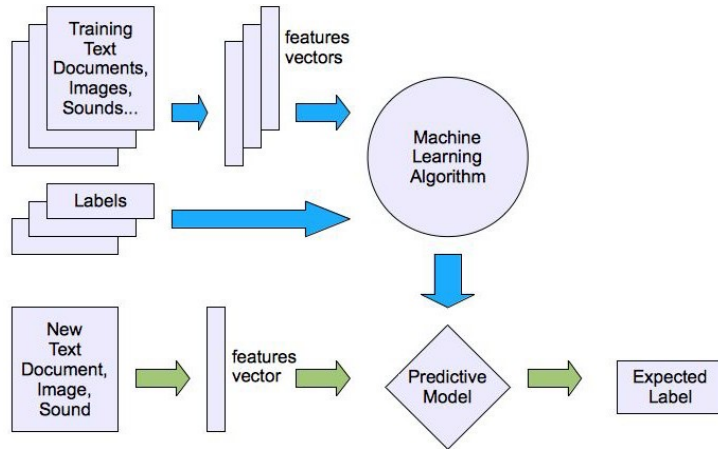
# Unsupervised Learning

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## Overview

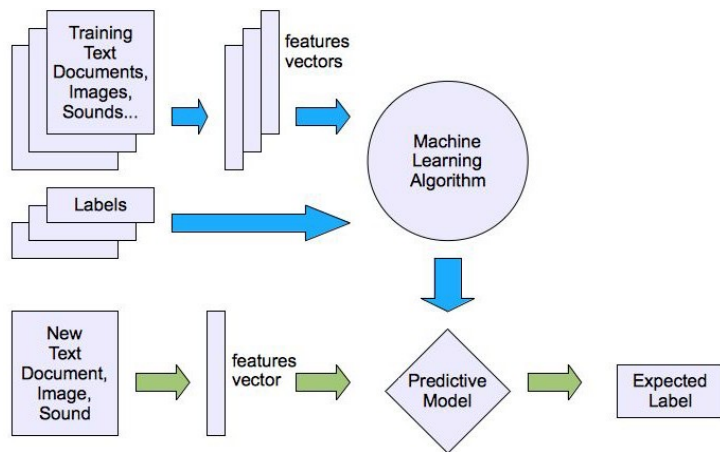
# Machine Learning Taxonomy

## Supervised learning learn data model

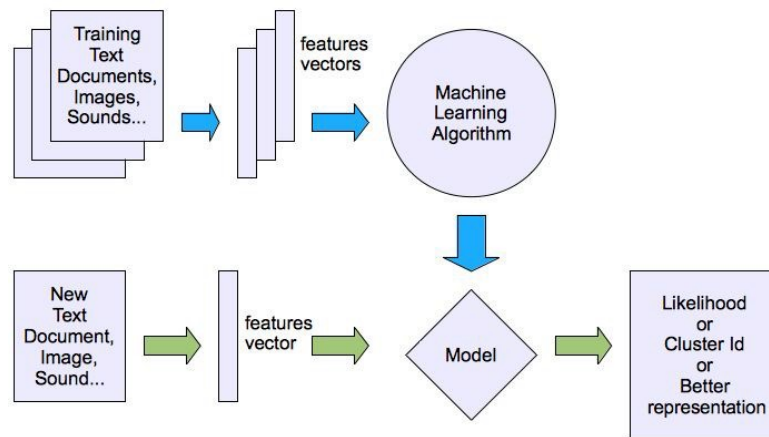


# Machine Learning Taxonomy

## Supervised learning learn data model



## Unsupervised learning learn data structure



# Unsupervised Learning - Overview

Unsupervised learning tools allow you to **explore the structure of your data**.

- How are the data best **represented**?
- Are there **clusters** within the data?
- Can we estimate the **density** of the data?

# Unsupervised Learning Applications

- Recommendation systems
- Image segmentation and compression
- Life sciences
- ...

# Data Representation

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## Overview

# Learning Data Representation

By changing how your data are represented, you can

- Identify patterns in your data.
- Learn which variables drive those patterns.

When should you think about data representation?

- When you have high-dimension data ( $>3$  variables).
- As a pre-processing step before clustering or other machine learning workflows.



# Data Representation

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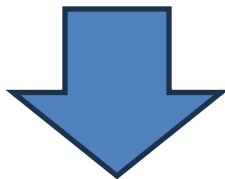
## Dimensionality Reduction

# Manifold Hypothesis

Many high-dimensional data sets describing processes from the real world have low-dimensional representations (manifolds).

# Manifold Hypothesis

Many high-dimensional data sets describing processes from the real world have low-dimensional representations (manifolds).



**Dimensionality reduction** algorithms compress information contained in a dataset by transforming it onto a low-dimensional subspace while maintaining most of the relevant information.

# Principal Component Analysis (PCA)

PCA helps to find a new low-dimensional coordinate system (basis) and projects the data onto it (i.e., changes its representation).

*PCA's implementation is based on either eigendecomposition (eigenvectors and eigenvalues) or Singular Value Decomposition (SVD).*

# Principal Component Analysis (PCA)

The resulting basis is **orthogonal** and its axes can be interpreted as the directions of **maximum variance** such that the direction of the *first coordinate* corresponds to the *greatest variance*, the second coordinate – *second-greatest variance*, ..., and so on for  $n$  dimensions.

# Principal Component Analysis (PCA)

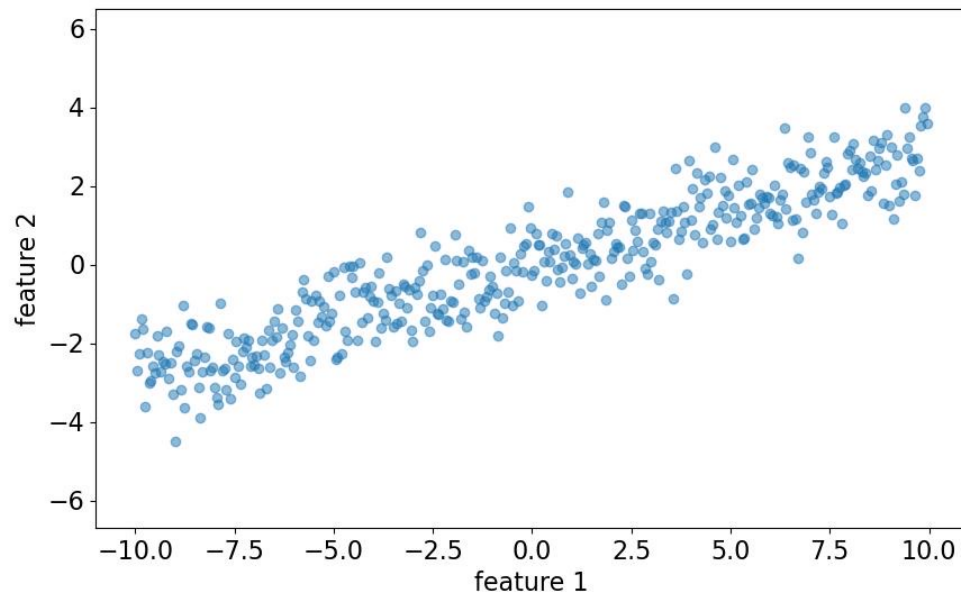
**orthogonal**  $\approx$  no correlation (between projected features)

**larger variance**  $\approx$  more information

!!! The axes with *smaller variance* can be neglected, hence low-dimensional (reduced) basis !!!

# Principal Component Analysis (PCA)

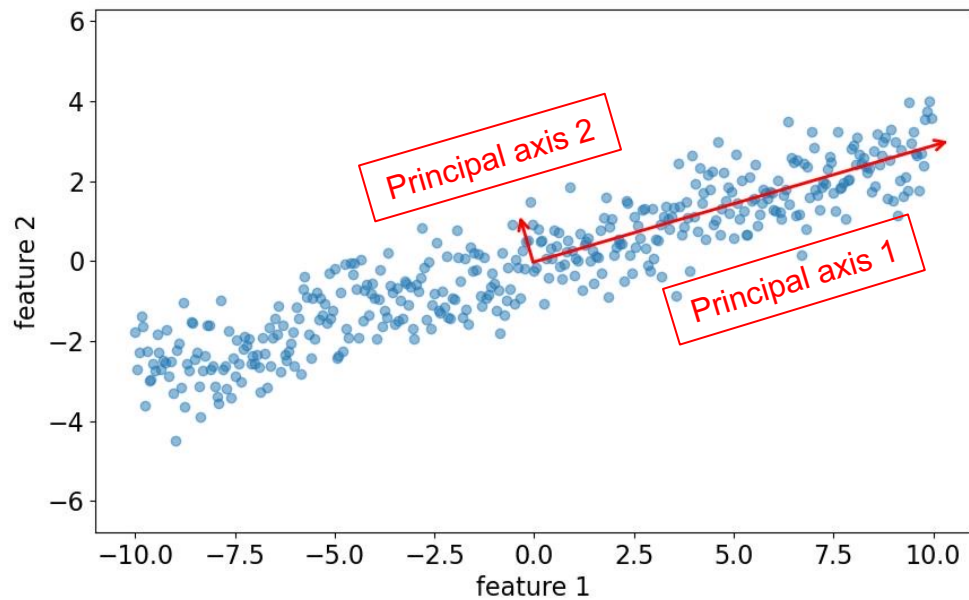
## “Toy” Example #1



Question: Can we reduce the dimensions from 2 to 1?

# Principal Component Analysis (PCA)

## “Toy” Example #1

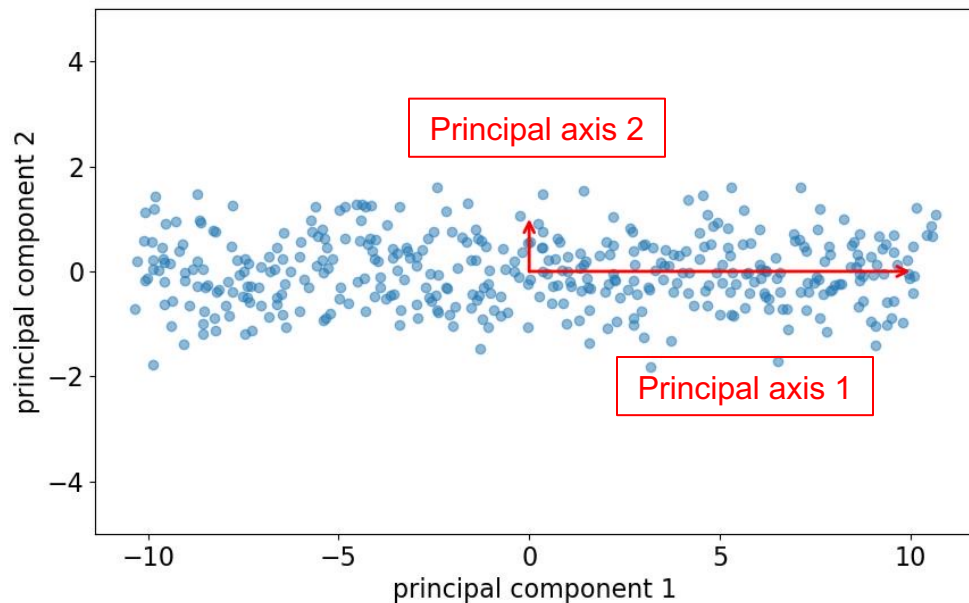


Question: Can we reduce the dimensions from 2 to 1?



# Principal Component Analysis (PCA)

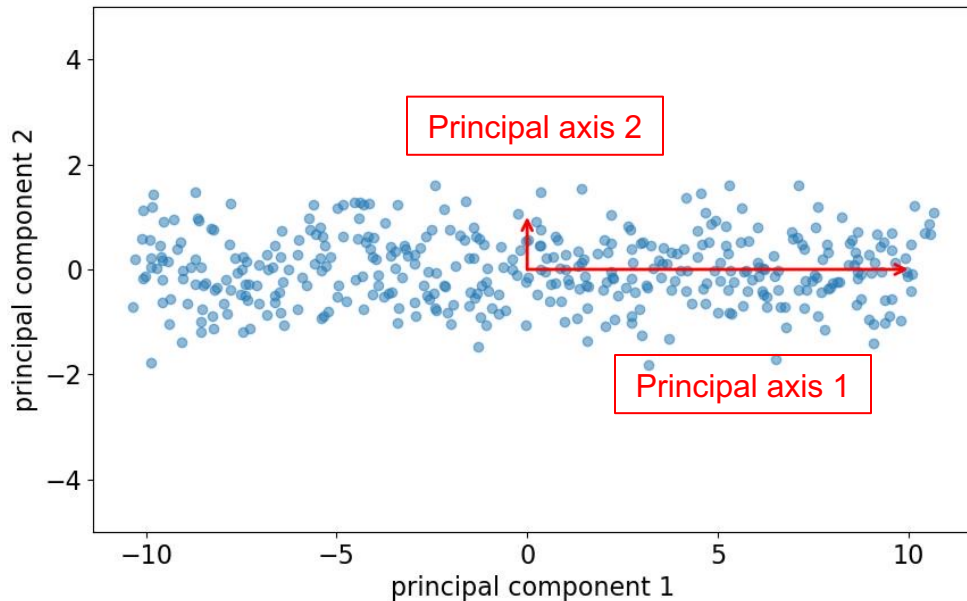
## “Toy” Example #1



Question: Can we reduce the dimensions from 2 to 1?

# Principal Component Analysis (PCA)

## “Toy” Example #1

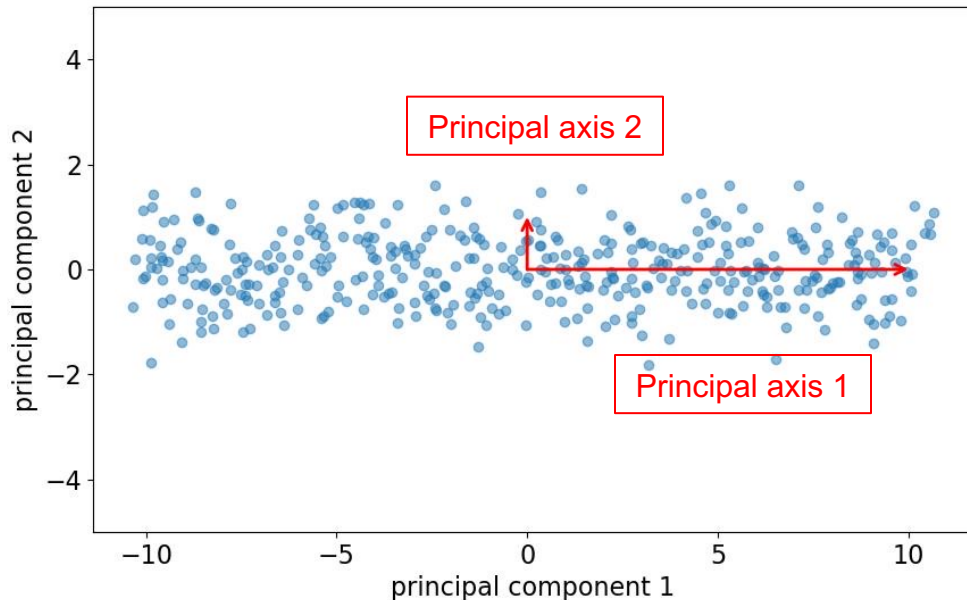


```
pca.explained_variance_ratio_  
array([0.98806067, 0.01193933])
```

Question: Can we reduce the dimensions from 2 to 1?

# Principal Component Analysis (PCA)

## “Toy” Example #1



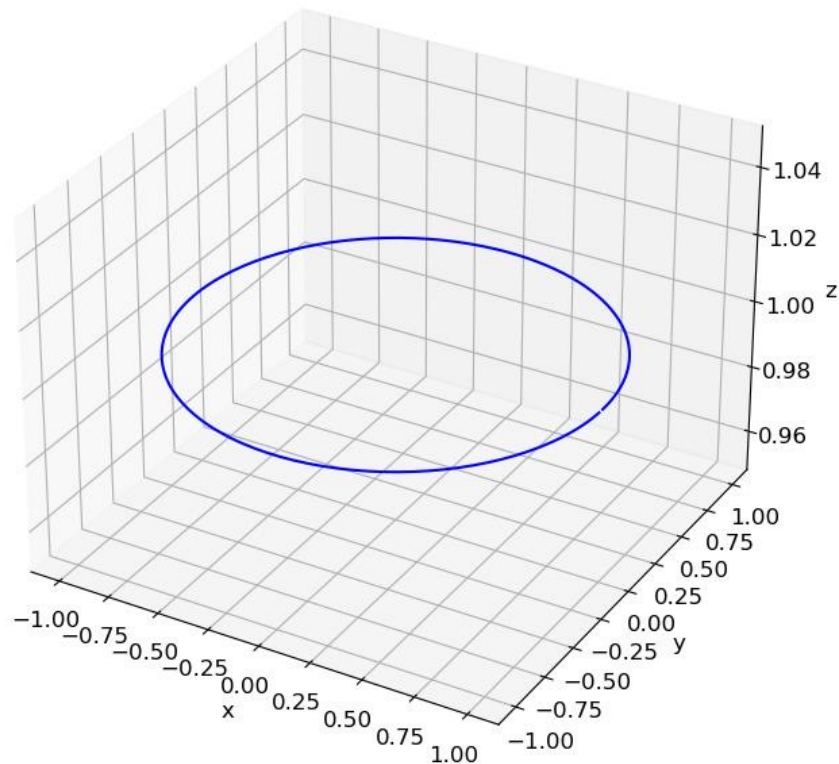
```
pca.explained_variance_ratio_  
array([0.98806067, 0.01193933])
```

**Answer:** Yes, we can by keeping only the first PC describing 98.8% of the variance of the original dataset.

# Principal Component Analysis (PCA)

## “Toy” Example #2

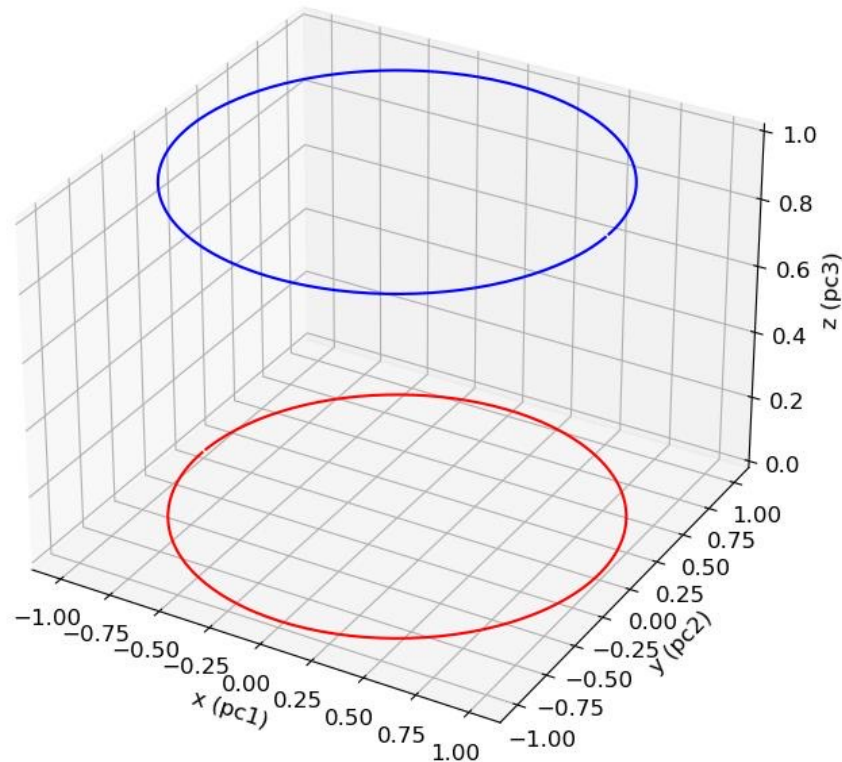
	x	y	z
<b>0</b>	1.000000	0.000000	1.0
<b>1</b>	0.999507	0.031411	1.0
<b>2</b>	0.998027	0.062791	1.0
<b>3</b>	0.995562	0.094108	1.0
<b>4</b>	0.992115	0.125333	1.0
...	...	...	...
<b>195</b>	0.987688	-0.156434	1.0
<b>196</b>	0.992115	-0.125333	1.0
<b>197</b>	0.995562	-0.094108	1.0
<b>198</b>	0.998027	-0.062791	1.0
<b>199</b>	0.999507	-0.031411	1.0



# Principal Component Analysis (PCA)

## “Toy” Example #2

	pc1	pc2	pc3
<b>0</b>	-0.999737	0.022943	0.0
<b>1</b>	-0.998523	0.054334	0.0
<b>2</b>	-0.996323	0.085672	0.0
<b>3</b>	-0.993141	0.116925	0.0
<b>4</b>	-0.988978	0.148063	0.0
...	...	...	...
<b>195</b>	-0.991017	-0.133732	0.0
<b>196</b>	-0.994729	-0.102538	0.0
<b>197</b>	-0.997459	-0.071242	0.0
<b>198</b>	-0.999205	-0.039876	0.0
<b>199</b>	-0.999964	-0.008471	0.0



# Limitations

- **Spurious clustering** may appear under different visualization strategies
- **Outliers** may inflate variance and influence the direction of the principal components
- **Loss of interpretability** from representation in a feature space that doesn't map directly to measured variables

# Data Representation

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## Manifold Learning

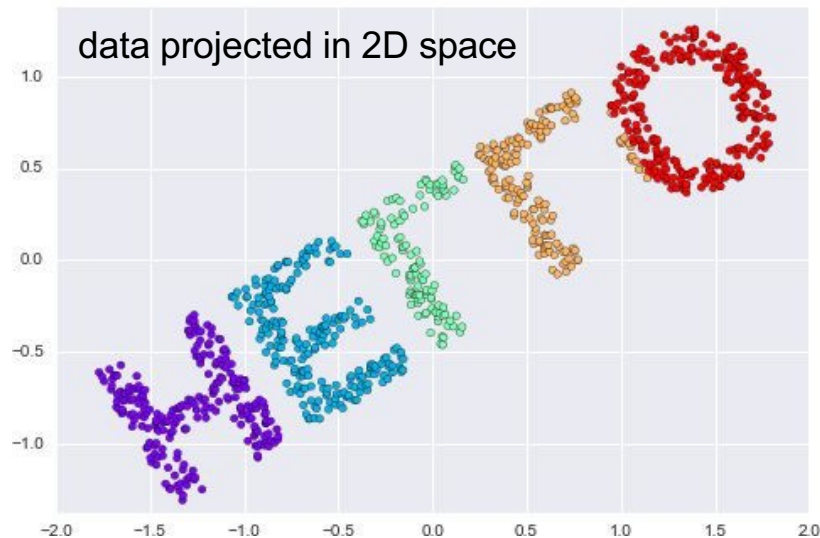
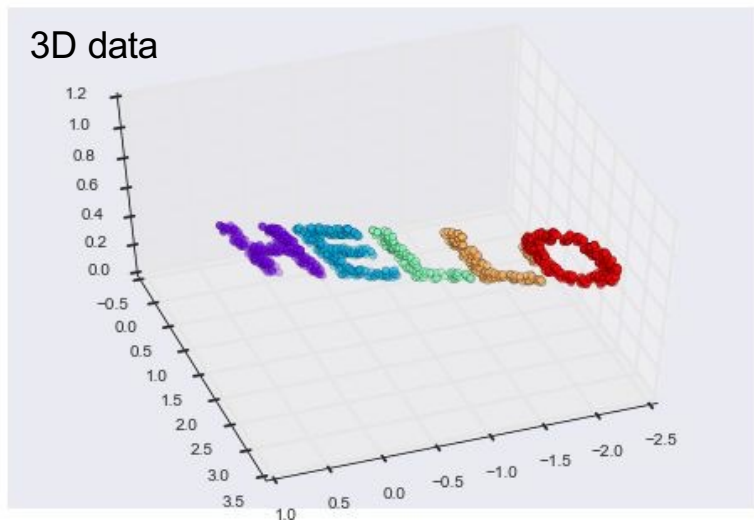
# Manifold Learning

- Describe data as low-dimensional manifolds embedded in high-dimensional spaces
  - Viewing  $n$ -dimensional space through  $k$  dimensional space. ( $k < n$ )
  - e.g. a three dimensional space as a surface.
- Common methods:
  - Multidimensional Scaling (MDS)
  - Locally Linear Embedding (LLE)



# Multidimensional Scaling

Find best low-dimensional data representation that preserves all spatial relationships.

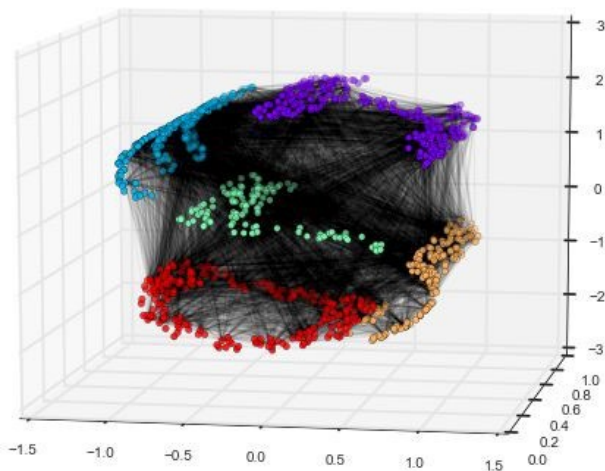


[image source](#)

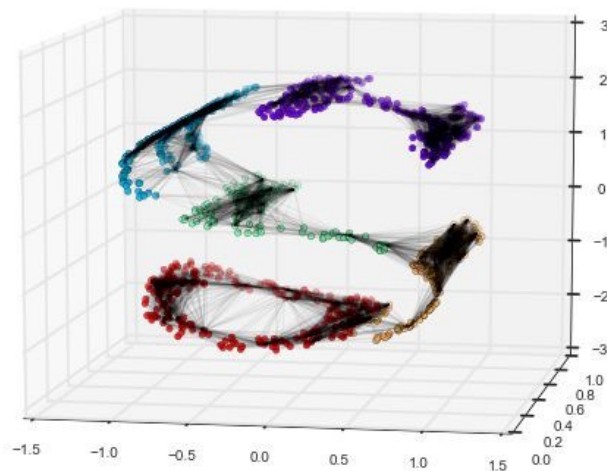
# Locally Linear Embedding

Handles nonlinear embeddings by preserving only local distances in neighborhoods of  $n$  points.

MDS Linkages



LLE Linkages (100 NN)



[image source](#)

# Manifold Learning Summary

Sensitive to noisy and/or missing data

Pairwise distance computation incurs high computational cost

Requires more tuning; LLE sensitive to the choice of neighbors

Other methods:

- Isometric Mapping (isomap)
- t-distributed stochastic neighbor embedding (t-SNE)

# Manifold Learning Useful Links

- [Wikipedia: Nonlinear Dimensionality Reduction](#)
- [“Manifold learning: what, how, and why”  
by Marina Meila, Hanyu Zhang](#)
- [“Locally Linear Embedding and its Variants: Tutorial and Survey”  
by Benyamin Ghojogh, Ali Ghodsi, Fakhri Karray, Mark Crowley](#)
- [Comparison of Manifold Learning Techniques](#)

## Hands-On Exercise

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# Jupyter Set-Up and Data Representation

# Hands-on break #1

## Setup Materials

- Package Installation
- Plotting Utilities

## Data Representation

- Principal Components Analysis (PCA) Example 1: Tumor Classification
  - Exercise 1
- PCA Example 2: Flower Identification
- PCA Example 3: Noise Reduction
- Multidimensional Scaling
- Locally Linear Embedding
- T-SNE