Hsymptotic Notation are used to tell the complexity of an algorithm when the infect is very large. i) Big O Natalion f(n) = O(g(n))g(n) is 'tight' upper bound of f(n) f(m) = O(g(n))iff f(m) 5 cglm) + n >n₀ and same constants (70

ii) Big Omega Notation (12)  $f(n) = \mathcal{L}g(n)$ g(n) is 'tight' lower bound of f(n)  $f(n) = \mathcal{N}(g(n))$ y f(n) > cgln) I no le some constant Theta Notation (0)  $f(n) = \theta(g(n))$ theta given both 'tight' upper & 'tight' lower bour f(n) = O(g(n)) and  $f(n) = \mathcal{N}(g(n))$ f(n)=0(g(n)) iff cag(n) > f(n)>/c1g(n) 4 m 7/ mar(n1, n2) and some constants C1, c2 70 Notation iv) Small 0 f(m) = O(g(m))gladisupper bound of fin) f(n) < cg(n)
for all constant
of n >= no and some constant ĺδ v) Small anega Notation (w) g(n) is lower bound of f(n)  $f(n) = \mathfrak{p}(g(n))$ f(n) >c gen) all constant C70

for (i=1; i <=n; i=i\*2) n= 1 + 2 k-1 1/2 ax k-1  $dn = 2^{k}$   $\log_{a}(2n) = k \log_{a} 2$ Kz loga dn z loga d + loga n kz lt logg n 0 t log on)

for (i=1 ton) for (j=1) j <= n; j=j+1) { print (" x") 1=1,2,3,4--. J21, 3, 6, 10 - - · 1=1 n times , n/a times n/3 times time complexity = o(nlogn)

ind i=1, s=1, While (sc=n) i++; S=S+i Drivel (" 4"); i= 1, 2, 3, 4, 5, .....n S = 1, 3, 6, 10, 15 - ... 21 S= i(i+1) iliti) san i² + i-2m 50 i. i <-1+JI+8n time complaity tourn) void function (intn) inti, cound = 0; ... for(i=1; i+i<=n;i++) loop soutinues until i² becomes greates kann i = 1, 2, 3, 4 - - - 5ni² = 1, 4, 9, 16 - - n2 time complainty = OSn

3. 
$$T(n) = \{3T(n-1) \text{ if } m \neq 0 \text{ otherwise } \}$$
 $T(0) = \}$ 
 $n = 1 \Rightarrow T(1) = 3T(1) = 3$ 
 $n = 2 \Rightarrow T(2) = 3T(1) = 3^{2}$ 
 $n = 3 \Rightarrow T(3) = 3T(2) = 3 \cdot 3 \cdot 3^{2} = 3^{3}$ 
 $n = k \Rightarrow T(k) = 3^{k}$ 
 $T(n) = 3^{n}$ 

time complexity =  $O(3^{k})$ 

4.  $T(n) = \{3T(n-1) - 1 \text{ if } m \neq 0, \text{ otherwise } 1\}$ 
 $T(n) = \{3T(n-2) - 1\} - 1$ 
 $= 2^{n}T(n-k) - (2^{n} + 2^{n} + \dots + 2^{n-1})$ 

When,  $n - k \neq 0$ 
 $k \geq n$ 
 $Substitute = k = n$ 
 $T(n) = \{3^{n}T(0) - (3^{n} + 2^{n} + \dots + 2^{n-1})$ 
 $T(n) = \{3^{n}T(0) - (3^{n} + 2^{n} + \dots + 2^{n-1})\}$ 
 $T(n) = \{3^{n}T(0) - (3^{n} + 2^{n} + \dots + 2^{n-1})\}$ 

