

Week 9 11/10

2. 价格变动的所得与替代效果

$$\text{Mr. Lee 消费决策} = \text{Max } U = f(x, y) = x^{\frac{2}{3}} y^{\frac{1}{3}}$$

$$\text{subject to } 300 = 10x + 20y$$

$$\text{最適消費量} = x = 20, y = 5$$

⇒ 奶茶供不應求、價格提高為 20 元。

$$\Rightarrow \text{消費決策} = \text{Max } U = f(x, y) = x^{\frac{2}{3}} y^{\frac{1}{3}}$$

$$\text{subject to } 300 = 20x + 20y$$

根據最適消費條件 =

$$MRS_{xy} = \frac{2y}{x} = \frac{p_x}{p_y} = \frac{20}{20} = 1$$

$$\text{可得 } y = \frac{1}{2}x \Rightarrow \text{最適消費量} = x = 10, y = 5$$

Mr. Lee 總效用 =

$$U = x^{\frac{2}{3}} y^{\frac{1}{3}} = (20)^{\frac{2}{3}} (5)^{\frac{1}{3}} = (2000)^{\frac{1}{3}} \quad \text{代入}$$

$$\Rightarrow U = x^{\frac{2}{3}} y^{\frac{1}{3}} = \left(\frac{1}{2}x\right)^{\frac{1}{3}} = (2000)^{\frac{1}{3}}$$

$$\Rightarrow x = (4000)^{\frac{1}{3}} \approx 15.874, y = (500)^{\frac{1}{3}}$$

$$\text{① 替代效果} = \text{由 } (x, y) = (20, 5) \text{ 到 } [(4000)^{\frac{1}{3}}, (500)^{\frac{1}{3}}]$$

$$x \text{ 的替代效果} = (4000)^{\frac{1}{3}} - 20 < 0$$

$$\text{② 所得效果} = \text{由 } (x, y) = [(4000)^{\frac{1}{3}}, (500)^{\frac{1}{3}}] \text{ 到 } (10, 5)$$