

What is probability theory?

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How is it related to statistics?

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Physics: Physics uses math to create models of nature [i.e., hypotheses]. Physics tests the models based on measured data.

Probability Theory: The branch of mathematics concerned with the analysis of random phenomena.¹

¹source: Encyclopedia Britannica

²source: <https://www.stat.uci.edu/what-is-statistics/>

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Statistics: Statistics is the science of collecting, analyzing, presenting, and interpreting data.²

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Probability Theory: The branch of mathematics concerned with the analysis of random phenomena.¹

Statistics: Statistics is the science of collecting, analyzing, presenting, and interpreting data.²

Statistics uses probability theory to create models/hypotheses for how data is generated. Statistics uses these models and data to infer conclusions or make predictions.

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Example 1.1: We all throw our hat into the center of the room, and pick one back at random. What is the probability that at least one of us gets our hat back?

Is this probability theory or statistics?

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Answer: [Probability Theory]

Example 1.2: In a radar system there are two possibilities (or hypotheses): there is a plane, or there is no plane. For each hypothesis, you create a model for how the data you collect should behave.

You now collect data, and from this, infer which hypothesis you believe to be true.

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Second Ans: Probability theory is used to model how data is generated in each case.

Example 1.3: In an election, $x\%$ of voters will vote for candidate A, and $(100 - x)\%$ will vote for B.

A polling company asks 1000 people their voting intention and based on this, makes an estimate \hat{x} of x .

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In this example, we can also use probability theory to compute the prob. that estimate is within a tolerance of the true value x , i.e.,
prob. that $|x - \hat{x}| < 3\%$

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From this data, they try to infer what else you might be interested in buying.

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Example 1.5: In a certain bank, there is one common line for all tellers, whereas in a grocery store, each checkout counter has its own line.

Which is more efficient and why?

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Answer: Probability Theory

Example 1.6: A radar system measures the position of a car at various times, and makes a prediction of where the car will be over the next 2 seconds.

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Answer: Statistics

Example 1.7: In a room of 100 people, the odds that 2 people share the same birthday is not $100/365$ but $\approx 99.99997\%$.

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Answer: Probability Theory