Jointly Distributed Random Variables

Examples [Ross S6.1] **Example 23.1:** The joint pdf of X and Y is given by

$$f_{XY}(x,y) = \begin{cases} 2e^{-x}e^{-2y} & x > 0 \text{ and } y > 0 \\ 0 & \text{else} \end{cases}$$

b) P[X < Y]

Compute

c) P[X < a] (assume a > 0)

a) P[X > 1, Y < 1]

- Solution:

d) Find E[D]. *Note:* This is the uniform distribution on a disk of radius R.

Example 23.2: Given R > 0, consider the joint pdf

for some c > 0.

Find $P[D \leq a]$.

b) Find the marginal pdf of X.

a) Find c.

Solution:

 $f_{XY}(x,y) = \begin{cases} c & \text{if } x^2 + y^2 \le R^2 \\ 0 & \text{else} \end{cases}$

c) Let $D=\sqrt{X^2+Y^2}$ be the distance of the pair (X,Y) from the origin.

Example 23.3: The joint pdf of X and Y is

 $f_{XY}(x,y) = \begin{cases} e^{-(x+y)} & x>0 \text{ and } y>0 \\ 0 & \text{else} \end{cases}$

Find the pdf of Z = X/Y.

Solution: