

# Laboratory 4

Due: before class, Wednesday, Oct. 11

- 25 pts (1) The following data was collected by one of your colleagues and your advisor has asked you to analyze it by looking for a *trend* in the data. You decide to analyze it in several ways. Specifically, find the least squares fit to these data using:

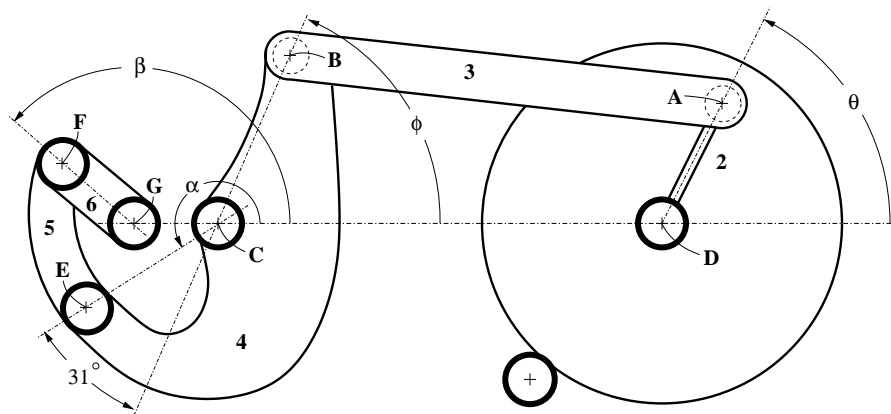
- a linear polynomial fit
- a cubic polynomial fit
- a linear polynomial fit to the “linearized” data

x	y
0	2.5237305e+03
5	2.0864229e+02
6	1.8697888e+02
13	3.9214807e+00
16	1.5271976e+00
22	6.8035297e-02
35	7.3126314e-05
38	1.4585192e-05
42	3.0299061e-06
44	8.6349502e-07
47	2.4089013e-07
50	4.6306127e-08

For the cubic least-squares fit, write down the normal equations and explain how you arrived at your solution for the best-fit cubic polynomial.

Finally, after presenting your results, your advisor asks you why you didn’t do a non-linear least-squares fit to the data and whether or not it will give you the same answer the “linearized” fit gave you. Answer your advisor’s question by either performing the non-linear fit or comparing the errors of an individual data point using both methods and demonstrating whether or not the best-fit non-linear functions are the same.

- 25 pts (2) An automatic washer transmission uses the linkage shown in the accompanying figure to convert rotary motion from the drive motor to a large oscillating output of the agitator shaft G. Links 2, 4, and 6 rotate or oscillate about fixed axes. Links 2, 3, and 4 (DA, AB, and BC) along with the fixed base (CD) constitute a four-bar linkage identical to that from *Laboratory 2, part 3* where  $\theta_4$  (from Lab2) =  $\theta$  (Fig below) +  $\pi$  (Note, however, that the order of the linkage numbers may be different). A second four-bar linkage involving links 4, 5, and 6 (CE, EF, and FG) along with a fixed base (GC) can also be identified and is also identical to that of *Laboratory 2, part 3* where  $\theta_4 = \alpha + \pi$ . It is of interest to find the angular velocity and the angular acceleration of the agitator shaft for design purposes. Note that for any given  $\theta$ , the angle  $\phi$  can be found by solving the first four-bar linkage. The angle  $\alpha$  is equal to the angle  $\phi$  plus a constant ( $149^\circ$ ) and given the angle  $\alpha$ , the angle  $\beta$  can be found using the second four-bar linkage system.



Automatic Washing Machine Drive

DA = 1.84 in	AB = 6.86 in	CB = 2.36 in	EF = 1.82 in
GF = 1.26 in	DC = 7.00 in	CG = 1.25 in	CE = 2.41 in

- 10 pts (i) Increment  $\theta$  from 0 to  $360^\circ$  in steps of  $1^\circ$  and compute  $\phi$  and  $d\phi/d\theta$  at each point. Report plots of  $\phi$  and  $d\phi/d\theta$  versus  $\theta$ . For the first derivative, compute both a first forward difference and a centered difference approximation and plot the two curves on the same graph. How do the two curves compare? Which do you expect to be more accurate? Also plot the *difference* between the forward and centered difference solution (probably on a log scale) and describe your findings.

When using your Newton algorithm from *Laboratory 2*, as you increment  $\theta$  use the previously found solution as an initial starting guess for the next value of  $\theta$ . Make sure your initial guess is physically reasonable and **be careful of your linkage order**.

- 15 pts (ii) Now solve the second linkage problem, by determining  $\alpha$  from your computed values of  $\phi$  and using Newton's method on the second linkage system to compute  $\beta$ ,  $d\beta/dt$  (i.e., the angular velocity in rad/sec) and  $d^2\beta/dt^2$  (i.e., the angular acceleration in rad/sec<sup>2</sup>). Make plots of these quantities as a function of  $\theta$  and in the case of the derivatives, compute and plot both forward and centered approximations as before. Note that

$$\frac{d\beta}{dt} = \omega \frac{d\beta}{d\theta} \quad \text{and} \quad \frac{d^2\beta}{dt^2} = \omega^2 \frac{d^2\beta}{d\theta^2}$$

where  $\omega$  is the rotating speed of the driving gear (assume that  $\omega = 550$  radians per minute). Again plot the difference between your two methods and comment on your results.

Watch your units!