

MARSS model checking

###2020 MARSS model outputs: July 7 - July 28 2020 (airtemp as a covariate, but not z scored. No seasonal correction)

```
mod1.fit.2020 <- readRDS("2020_mod1.fit.rds")
mod1.params.2020 <- readRDS("2020_mod1.params.rds")
mod2.fit.2020 <- readRDS("2020_mod2.fit.rds")
mod2.params.2020 <- readRDS("2020_mod2.params.rds")
mod3.fit.2020 <- readRDS("2020_mod3.fit.rds")
mod3.params.2020 <- readRDS("2020_mod3.params.rds")
mod4.fit.2020 <- readRDS("2020_mod4.fit.rds")
mod4.params.2020 <- readRDS("2020_mod4.params.rds")
```

```
#Model 1, hypothesis 1 (all separate)
mod1.params.2020
```

```
##
## MARSS fit is
## Estimation method: kem
## Convergence test: conv.test.slope.tol = 0.5, abstol = 0.001
## Estimation converged in 350 iterations.
## Log-likelihood: -333.3257
## AIC: 844.6514   AICc: 880.6514
##
##           ML.Est Std.Err   low.CI   up.CI
## R.diag    0.132351 0.00973  0.113287  0.15142
## Q.(1,1)    0.169511 0.06546  0.041211  0.29781
## Q.(2,1)    0.269266 0.09725  0.078654  0.45988
## Q.(3,1)    0.551157 0.21646  0.126904  0.97541
## Q.(4,1)    0.320063 0.13377  0.057874  0.58225
## Q.(5,1)    0.206263 0.08157  0.046388  0.36614
## Q.(6,1)    0.189997 0.07636  0.040334  0.33966
## Q.(7,1)    0.181741 0.06591  0.052554  0.31093
## Q.(8,1)    0.039687 0.03210 -0.023227  0.10260
## Q.(9,1)    0.129886 0.05633  0.019474  0.24030
## Q.(10,1)   0.158694 0.09329 -0.024150  0.34154
## Q.(11,1)   0.199095 0.07911  0.044036  0.35415
## Q.(2,2)    0.458918 0.16361  0.138243  0.77959
## Q.(3,2)    1.023548 0.36209  0.313857  1.73324
## Q.(4,2)    0.568621 0.21974  0.137936  0.99931
## Q.(5,2)    0.340651 0.13281  0.080351  0.60095
## Q.(6,2)    0.294280 0.12139  0.056354  0.53221
## Q.(7,2)    0.287451 0.10312  0.085341  0.48956
## Q.(8,2)    0.060401 0.05159 -0.040714  0.16152
## Q.(9,2)    0.229238 0.09072  0.051434  0.40704
## Q.(10,2)   0.238323 0.14519 -0.046246  0.52289
```

## Q.(11,2)	0.326268	0.12495	0.081368	0.57117
## Q.(3,3)	2.791892	0.92486	0.979201	4.60458
## Q.(4,3)	1.429326	0.53298	0.384709	2.47394
## Q.(5,3)	0.734407	0.30632	0.134021	1.33479
## Q.(6,3)	0.620703	0.27956	0.072772	1.16863
## Q.(7,3)	0.609604	0.23297	0.152988	1.06622
## Q.(8,3)	0.229998	0.13244	-0.029583	0.48958
## Q.(9,3)	0.661732	0.23183	0.207356	1.11611
## Q.(10,3)	0.734578	0.35787	0.033168	1.43599
## Q.(11,3)	0.668870	0.28340	0.113410	1.22433
## Q.(4,4)	1.004484	0.39173	0.236716	1.77225
## Q.(5,4)	0.502737	0.20510	0.100740	0.90473
## Q.(6,4)	0.416306	0.18364	0.056385	0.77623
## Q.(7,4)	0.379788	0.14891	0.087924	0.67165
## Q.(8,4)	0.109839	0.08146	-0.049814	0.26949
## Q.(9,4)	0.406402	0.14972	0.112960	0.69984
## Q.(10,4)	0.325371	0.22041	-0.106627	0.75737
## Q.(11,4)	0.442714	0.18375	0.082562	0.80287
## Q.(5,5)	0.291020	0.13224	0.031827	0.55021
## Q.(6,5)	0.256269	0.10805	0.044495	0.46804
## Q.(7,5)	0.229627	0.08874	0.055702	0.40355
## Q.(8,5)	0.053372	0.04613	-0.037035	0.14378
## Q.(9,5)	0.190825	0.08223	0.029663	0.35199
## Q.(10,5)	0.198902	0.13404	-0.063804	0.46161
## Q.(11,5)	0.247582	0.10705	0.037764	0.45740
## Q.(6,6)	0.247937	0.11479	0.022954	0.47292
## Q.(7,6)	0.210706	0.08308	0.047876	0.37354
## Q.(8,6)	0.070173	0.04447	-0.016988	0.15733
## Q.(9,6)	0.168353	0.07629	0.018836	0.31787
## Q.(10,6)	0.257721	0.13323	-0.003402	0.51884
## Q.(11,6)	0.194530	0.09693	0.004544	0.38452
## Q.(7,7)	0.201739	0.07634	0.052110	0.35137
## Q.(8,7)	0.049511	0.03553	-0.020128	0.11915
## Q.(9,7)	0.159521	0.06330	0.035454	0.28359
## Q.(10,7)	0.175293	0.10050	-0.021679	0.37227
## Q.(11,7)	0.227486	0.08704	0.056884	0.39809
## Q.(8,8)	0.060126	0.02908	0.003129	0.11712
## Q.(9,8)	0.074594	0.03801	0.000103	0.14909
## Q.(10,8)	0.182634	0.07120	0.043090	0.32218
## Q.(11,8)	0.010282	0.04342	-0.074828	0.09539
## Q.(9,9)	0.196877	0.07175	0.056258	0.33750
## Q.(10,9)	0.202934	0.09863	0.009613	0.39625
## Q.(11,9)	0.179402	0.07832	0.025904	0.33290
## Q.(10,10)	0.613988	0.21605	0.190540	1.03744
## Q.(11,10)	0.017973	0.11857	-0.214422	0.25037
## Q.(11,11)	0.344855	0.12651	0.096901	0.59281
## x0.X1	-0.242124	0.68975	-1.594005	1.10976
## x0.X2	1.192021	1.16661	-1.094495	3.47854
## x0.X3	6.321549	2.79007	0.853112	11.78999
## x0.X4	1.943099	1.93640	-1.852179	5.73838
## x0.X5	-0.301160	1.23304	-2.717864	2.11555
## x0.X6	-0.166793	1.17772	-2.475074	2.14149
## x0.X7	-0.146467	0.68792	-1.494759	1.20183
## x0.X8	-0.799341	0.45245	-1.686133	0.08745

```
## x0.X9      -0.153413  0.48484 -1.103677  0.79685
## x0.X10     2.739076  1.34954  0.094034  5.38412
## x0.X11    -0.822383  0.67862 -2.152451  0.50768
## C.X1       0.000722  0.00136 -0.001943  0.00339
## C.X2      -0.000399  0.00222 -0.004753  0.00395
## C.X3      -0.004292  0.00544 -0.014954  0.00637
## C.X4      -0.001681  0.00330 -0.008152  0.00479
## C.X5       0.000566  0.00185 -0.003056  0.00419
## C.X6       0.000356  0.00173 -0.003029  0.00374
## C.X7       0.000511  0.00148 -0.002396  0.00342
## C.X8       0.001427  0.00085 -0.000239  0.00309
## C.X9       0.000755  0.00144 -0.002061  0.00357
## C.X10     -0.001746  0.00261 -0.006865  0.00337
## C.X11      0.000697  0.00191 -0.003045  0.00444
## Initial states (x0) defined at t=0
##
## CIs calculated at alpha = 0.05 via method=hessian
```

```
par(mfrow=c(5,2), mai=c(0.1,0.5,0.2,0.1), omi=c(0.5,0,0,0))
for (j in 1:5) {
  plot.ts(residuals<-MARSSresiduals(mod1.fit.2020, type = "tt1")$model.residuals[j, ],
          ylab = "Residual")
  abline(h = 0, lty = "dashed")
  acf(residuals,na.action = na.pass)
}
```

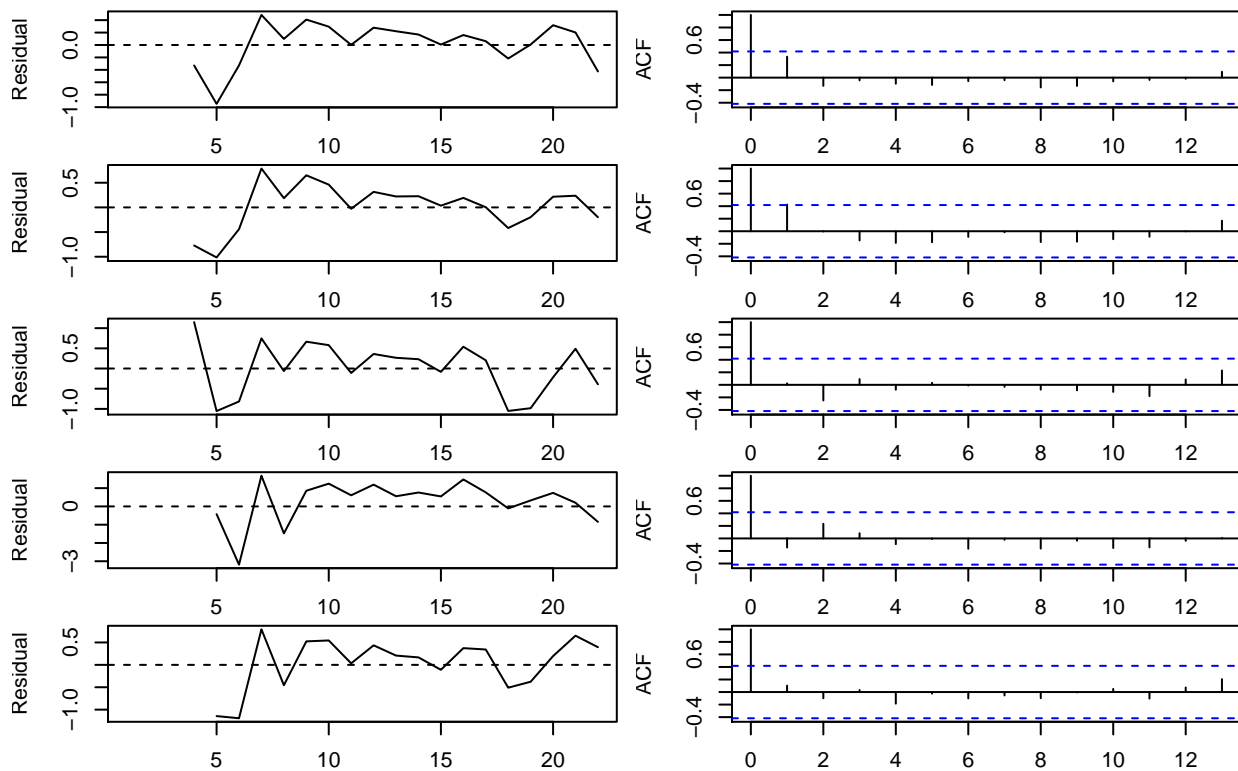
```
## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.
```

```
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```

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```

```
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```

```
## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.
```



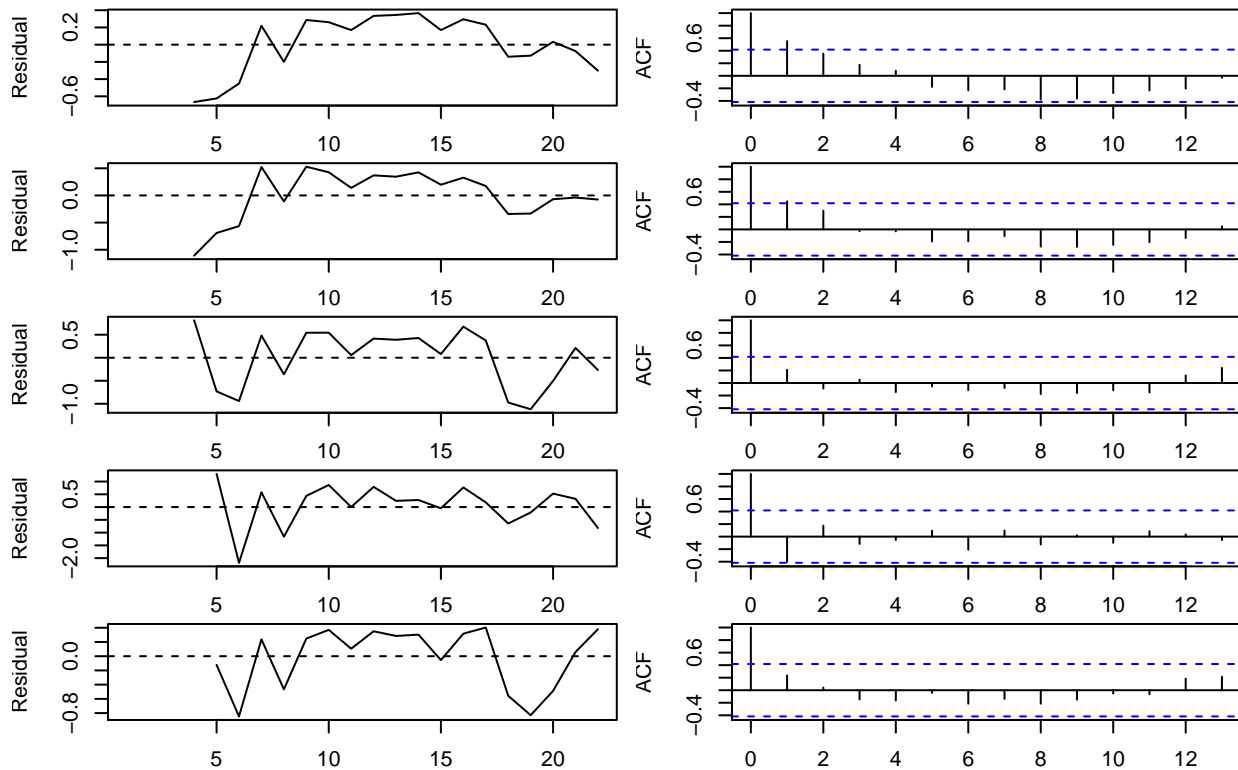
```
#Model 2, hypothesis 2 (creeks vs ponds)
mod2.params.2020
```

```
##
## MARSS fit is
## Estimation method: kem
## Convergence test: conv.test.slope.tol = 0.5, abstol = 0.001
## Algorithm ran 15 (=minit) iterations and convergence was reached.
## Log-likelihood: -445.091
## AIC: 906.1821   AICc: 906.4559
##
##          ML.Est Std.Err  low.CI  up.CI
## R.diag   0.256155 0.01629  0.22424 0.28807
## Q.(1,1)   0.181217 0.06157  0.06053 0.30190
## Q.(2,1)   0.294661 0.10878  0.08145 0.50787
## Q.(2,2)   0.718379 0.24935  0.22967 1.20709
## x0.X1    -0.308081 0.48608  -1.26078 0.64462
## x0.X2    -0.615078 0.96876  -2.51381 1.28365
## C.X1       0.000513 0.00137  -0.00217 0.00320
## C.X2     -0.000112 0.00273  -0.00545 0.00523
## Initial states (x0) defined at t=0
##
## CIs calculated at alpha = 0.05 via method=hessian
```

```

par(mfrow=c(5,2), mai=c(0.1,0.5,0.2,0.1), omi=c(0.5,0,0,0))
for (j in 1:5) {
  plot.ts(residuals<-MARSSresiduals(mod2.fit.2020, type = "tt1")$model.residuals[j, ],
    ylab = "Residual")
  abline(h = 0, lty = "dashed")
  acf(residuals,na.action = na.pass)
}

```



```

#Model 3, hypothesis 3 (trib vs. trib)
mod3.params.2020

```

```

##
## MARSS fit is
## Estimation method: kem
## Convergence test: conv.test.slope.tol = 0.5, abstol = 0.001
## Estimation converged in 279 iterations.
## Log-likelihood: -419.1611
## AIC: 876.3223   AICc: 877.798
##
##           ML.Est Std.Err  low.CI  up.CI
## R.diag   0.217524 0.01412  0.18984  0.24520
## Q.(1,1)   0.319266 0.11019  0.10330  0.53523
## Q.(2,1)   0.825437 0.28866  0.25967  1.39121
## Q.(3,1)   0.222331 0.07825  0.06896  0.37570
## Q.(4,1)   0.243680 0.09351  0.06041  0.42695

```

```
## Q.(2,2) 2.664947 0.89986 0.90125 4.42865
## Q.(3,2) 0.657191 0.22573 0.21476 1.09962
## Q.(4,2) 0.510457 0.23805 0.04388 0.97703
## Q.(3,3) 0.196872 0.06786 0.06388 0.32987
## Q.(4,3) 0.131236 0.06394 0.00591 0.25656
## Q.(4,4) 0.226662 0.09534 0.03980 0.41352
## x0.X1 -0.537949 0.71215 -1.93374 0.85784
## x0.X2 5.123978 2.61182 0.00490 10.24306
## x0.X3 -0.212596 0.50179 -1.19608 0.77089
## x0.X4 -0.942995 0.61044 -2.13944 0.25345
## C.X1 0.000643 0.00182 -0.00293 0.00421
## C.X2 -0.003497 0.00532 -0.01391 0.00692
## C.X3 0.000691 0.00143 -0.00212 0.00350
## C.X4 0.000722 0.00156 -0.00234 0.00378
## Initial states (x0) defined at t=0
##
## CIs calculated at alpha = 0.05 via method=hessian
```

```
par(mfrow=c(5,2), mai=c(0.1,0.5,0.2,0.1), omi=c(0.5,0,0,0))
for (j in 1:5) {
  plot.ts(residuals<-MARSSresiduals(mod3.fit.2020, type = "tt1")$model.residuals[j, ],
          ylab = "Residual")
  abline(h = 0, lty = "dashed")
  acf(residuals,na.action = na.pass)
}
```

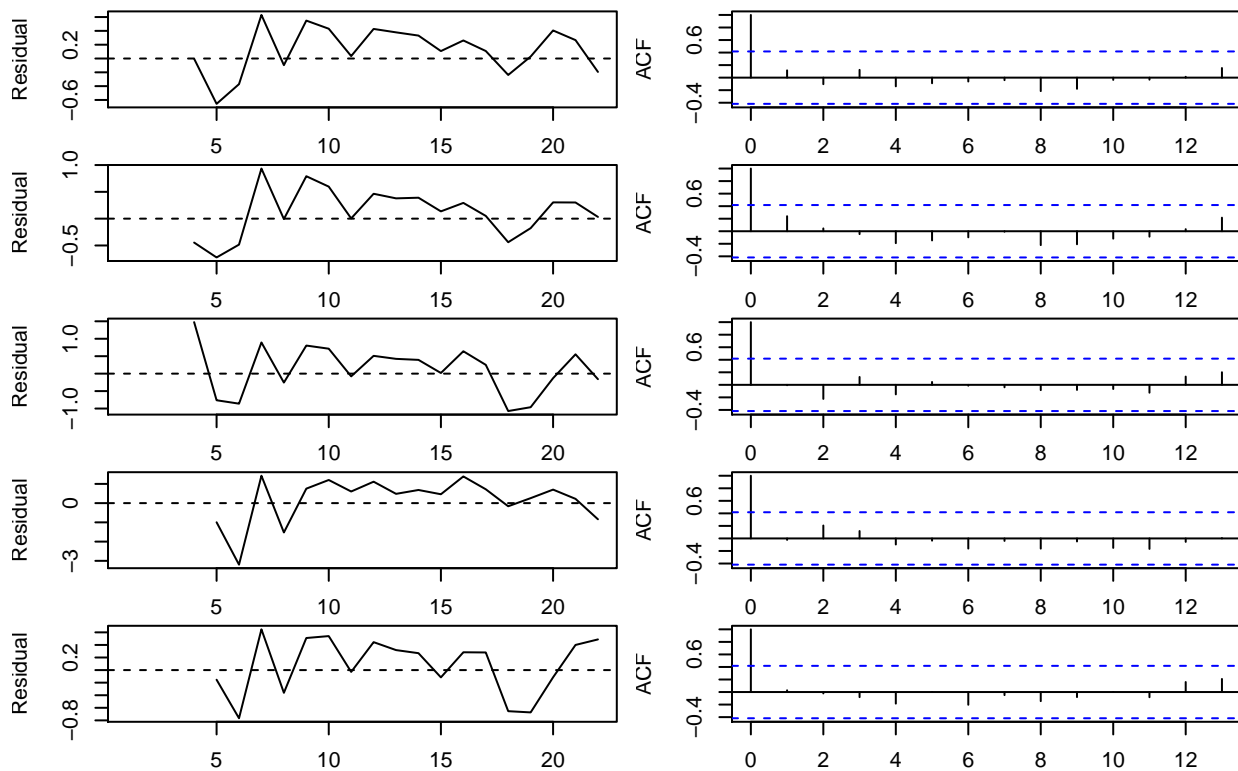
```
## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.
```

```
## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.
```

```
## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.
```

```
## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.
```

```
## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.
```



```
#Model 4, hypothesis 4 (all same)
mod4.params.2020
```

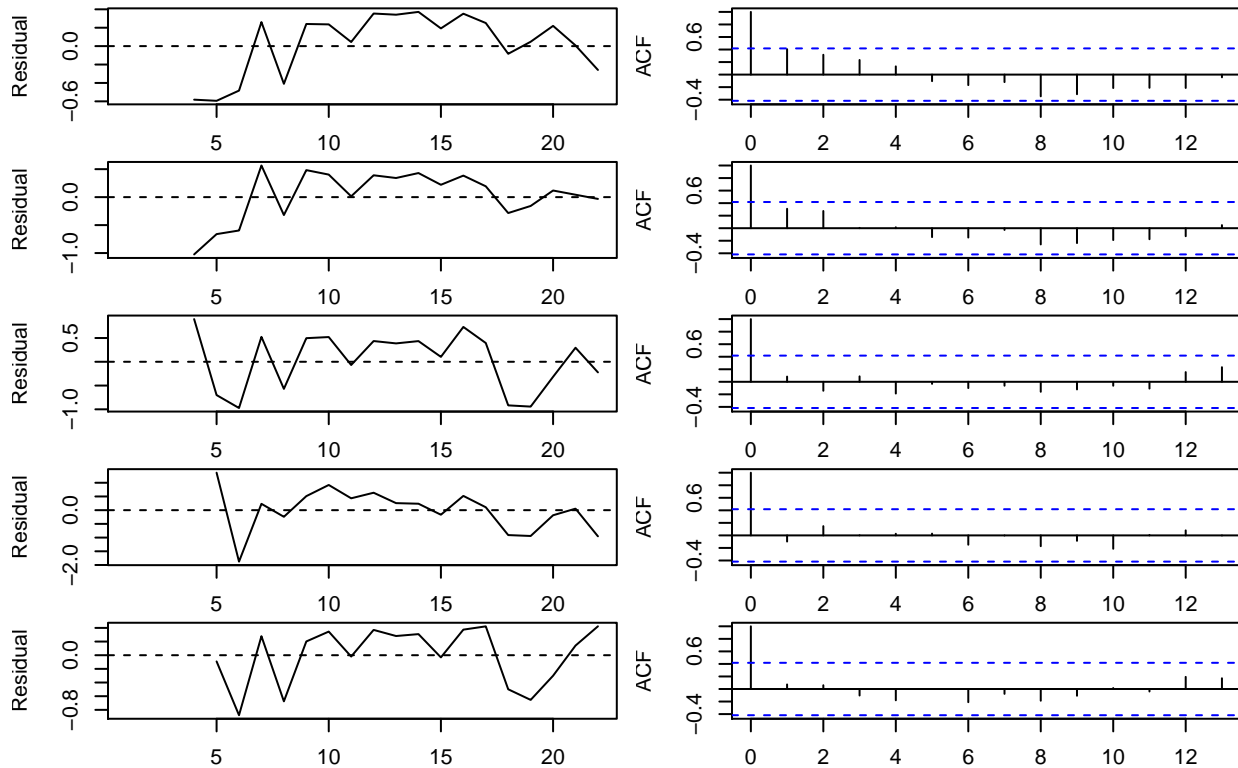
```
##
## MARSS fit is
## Estimation method: kem
## Convergence test: conv.test.slope.tol = 0.5, abstol = 0.001
## Algorithm ran 15 (=minit) iterations and convergence was reached.
## Log-likelihood: -466.3489
## AIC: 940.6978   AICc: 940.7733
##
##           ML.Est Std.Err  low.CI  up.CI
## R.diag  0.296242 0.01849  0.26001 0.33248
## Q.Q      0.233722 0.07791  0.08102 0.38643
## x0.x0    -0.346204 0.54456 -1.41351 0.72111
## C.C       0.000415 0.00155 -0.00263 0.00346
## Initial states (x0) defined at t=0
##
## CIs calculated at alpha = 0.05 via method=hessian
```

```
par(mfrow=c(5,2), mai=c(0.1,0.5,0.2,0.1), oml=c(0.5,0,0,0))
for (j in 1:5) {
  plot.ts(residuals<-MARSSresiduals(mod4.fit.2020, type = "tt1")$model.residuals[j, ],
    ylab = "Residual")
  abline(h = 0, lty = "dashed")
}
```

```

    acf(residuals, na.action = na.pass)
  }

```



#...these models are actually okay, but short

###Comparing 2020 AICc values

```

data.frame(Model=c("Model1", "Model2", "Model3", "Model4"),
  AICc=round(c(mod1.fit.2020$AICc,
    mod2.fit.2020$AICc,
    mod3.fit.2020$AICc,
    mod4.fit.2020$AICc),1))

```

```

##      Model  AICc
## 1 Model1 880.7
## 2 Model2 906.5
## 3 Model3 877.8
## 4 Model4 940.8

```

###Original MARSS model outputs (using airtemp as a covariate, airtemp not transformed, no Fourier Series correction for seasonality)


```

mod1.fit <- readRDS("mod1.fit.rds")
mod1.params <- readRDS("mod1.params.rds")
mod2.fit <- readRDS("mod2.fit.rds")
mod2.params <- readRDS("mod2.params.rds")
mod3.fit <- readRDS("mod3.fit.rds")
mod3.params <- readRDS("mod3.params.rds")
mod4.fit <- readRDS("mod4.fit.rds")
mod4.params <- readRDS("mod4.params.rds")

```

```

#Model 1, hypothesis 1 (all separate)
mod1.params

```

```

##
## MARSS fit is
## Estimation method: kem
## Convergence test: conv.test.slope.tol = 0.5, abstol = 0.001
## Estimation converged in 3251 iterations.
## Log-likelihood: 311.9935
## AIC: -445.987   AICc: -444.0914
##
##          ML.Est  Std.Err  low.CI  up.CI
## R.diag    4.66e-02 0.000765  4.51e-02 0.048146
## Q.(1,1)    1.08e-02 0.001547  7.79e-03 0.013853
## Q.(2,1)    9.58e-03 0.001222  7.18e-03 0.011974
## Q.(3,1)    1.01e-02 0.001347  7.46e-03 0.012739
## Q.(4,1)    9.63e-03 0.001243  7.19e-03 0.012062
## Q.(5,1)    9.21e-03 0.001261  6.74e-03 0.011681
## Q.(6,1)    1.11e-02 0.001649  7.82e-03 0.014285
## Q.(7,1)    6.48e-03 0.001058  4.41e-03 0.008558
## Q.(8,1)    1.68e-03 0.000590  5.27e-04 0.002839
## Q.(9,1)    4.73e-03 0.000690  3.38e-03 0.006086
## Q.(10,1)   3.34e-03 0.000646  2.07e-03 0.004607
## Q.(11,1)   1.05e-02 0.001379  7.75e-03 0.013159
## Q.(2,2)    1.04e-02 0.001281  7.88e-03 0.012899
## Q.(3,2)    1.02e-02 0.001268  7.70e-03 0.012676
## Q.(4,2)    1.02e-02 0.001240  7.81e-03 0.012674
## Q.(5,2)    9.73e-03 0.001239  7.30e-03 0.012155
## Q.(6,2)    1.28e-02 0.001720  9.45e-03 0.016192
## Q.(7,2)    6.86e-03 0.001020  4.86e-03 0.008859
## Q.(8,2)    1.64e-03 0.000548  5.62e-04 0.002711
## Q.(9,2)    5.15e-03 0.000678  3.82e-03 0.006484
## Q.(10,2)   3.57e-03 0.000618  2.36e-03 0.004778
## Q.(11,2)   1.08e-02 0.001313  8.19e-03 0.013339
## Q.(3,3)    1.46e-02 0.001731  1.12e-02 0.018015
## Q.(4,3)    1.04e-02 0.001335  7.82e-03 0.013057
## Q.(5,3)    9.66e-03 0.001318  7.07e-03 0.012241
## Q.(6,3)    1.02e-02 0.001652  7.00e-03 0.013474
## Q.(7,3)    7.21e-03 0.001153  4.95e-03 0.009474
## Q.(8,3)    2.68e-03 0.000683  1.35e-03 0.004022
## Q.(9,3)    5.84e-03 0.000791  4.29e-03 0.007395
## Q.(10,3)   4.80e-03 0.000766  3.30e-03 0.006303
## Q.(11,3)   1.50e-02 0.001688  1.17e-02 0.018303
## Q.(4,4)    1.02e-02 0.001342  7.54e-03 0.012802

```

## Q.(5,4)	9.69e-03	0.001254	7.23e-03	0.012142
## Q.(6,4)	1.23e-02	0.001680	9.05e-03	0.015640
## Q.(7,4)	6.73e-03	0.001017	4.73e-03	0.008720
## Q.(8,4)	1.78e-03	0.000551	7.05e-04	0.002863
## Q.(9,4)	5.13e-03	0.000681	3.80e-03	0.006468
## Q.(10,4)	3.61e-03	0.000620	2.40e-03	0.004828
## Q.(11,4)	1.10e-02	0.001377	8.28e-03	0.013677
## Q.(5,5)	9.63e-03	0.001415	6.85e-03	0.012399
## Q.(6,5)	1.16e-02	0.001665	8.36e-03	0.014887
## Q.(7,5)	6.19e-03	0.000996	4.24e-03	0.008145
## Q.(8,5)	1.61e-03	0.000547	5.41e-04	0.002686
## Q.(9,5)	4.65e-03	0.000648	3.38e-03	0.005923
## Q.(10,5)	3.44e-03	0.000627	2.21e-03	0.004671
## Q.(11,5)	1.03e-02	0.001396	7.55e-03	0.013027
## Q.(6,6)	1.79e-02	0.002708	1.26e-02	0.023167
## Q.(7,6)	7.88e-03	0.001378	5.18e-03	0.010581
## Q.(8,6)	1.23e-03	0.000759	-2.58e-04	0.002719
## Q.(9,6)	5.99e-03	0.000938	4.15e-03	0.007829
## Q.(10,6)	3.37e-03	0.000818	1.76e-03	0.004972
## Q.(11,6)	1.11e-02	0.001744	7.73e-03	0.014565
## Q.(7,7)	6.65e-03	0.001153	4.39e-03	0.008907
## Q.(8,7)	1.65e-03	0.000485	7.03e-04	0.002604
## Q.(9,7)	3.78e-03	0.000595	2.61e-03	0.004944
## Q.(10,7)	2.94e-03	0.000557	1.85e-03	0.004035
## Q.(11,7)	7.95e-03	0.001232	5.54e-03	0.010368
## Q.(8,8)	1.91e-03	0.000383	1.16e-03	0.002664
## Q.(9,8)	1.83e-03	0.000367	1.12e-03	0.002553
## Q.(10,8)	1.82e-03	0.000360	1.12e-03	0.002529
## Q.(11,8)	2.80e-03	0.000708	1.42e-03	0.004189
## Q.(9,9)	3.36e-03	0.000483	2.41e-03	0.004304
## Q.(10,9)	2.70e-03	0.000416	1.88e-03	0.003512
## Q.(11,9)	6.07e-03	0.000812	4.47e-03	0.007658
## Q.(10,10)	2.74e-03	0.000457	1.85e-03	0.003640
## Q.(11,10)	4.92e-03	0.000785	3.39e-03	0.006461
## Q.(11,11)	1.57e-02	0.001843	1.21e-02	0.019280
## x0.X1	8.12e-01	0.321857	1.81e-01	1.442374
## x0.X2	1.01e+00	0.311113	3.97e-01	1.617014
## x0.X3	1.03e+00	0.354114	3.32e-01	1.720270
## x0.X4	1.03e+00	0.308485	4.28e-01	1.637267
## x0.X5	1.36e+00	0.312260	7.45e-01	1.969097
## x0.X6	1.25e+00	0.438070	3.89e-01	2.106327
## x0.X7	8.37e-01	0.258043	3.31e-01	1.342717
## x0.X8	7.08e-01	0.143317	4.27e-01	0.988510
## x0.X9	1.02e+00	0.170085	6.88e-01	1.355067
## x0.X10	9.43e-01	0.162580	6.25e-01	1.261890
## x0.X11	1.08e+00	0.362198	3.68e-01	1.787971
## C.X1	1.99e-04	0.000386	-5.58e-04	0.000955
## C.X2	1.35e-04	0.000377	-6.03e-04	0.000873
## C.X3	2.92e-04	0.000446	-5.82e-04	0.001165
## C.X4	1.45e-04	0.000373	-5.86e-04	0.000876
## C.X5	-1.64e-04	0.000365	-8.78e-04	0.000551
## C.X6	6.89e-05	0.000503	-9.16e-04	0.001054
## C.X7	2.24e-04	0.000305	-3.73e-04	0.000821
## C.X8	5.23e-04	0.000166	1.98e-04	0.000847

```
## C.X9      3.51e-04 0.000215 -7.00e-05 0.000771
## C.X10     3.40e-04 0.000196 -4.36e-05 0.000724
## C.X11     2.73e-04 0.000461 -6.30e-04 0.001177
## Initial states (x0) defined at t=0
##
## CIs calculated at alpha = 0.05 via method=hessian
```

```
par(mfrow=c(5,2), mai=c(0.1,0.5,0.2,0.1), omi=c(0.5,0,0,0))
for (j in 1:5) {
  plot.ts(residuals<-MARSSresiduals(mod1.fit, type = "tt1")$model.residuals[j, ],
    ylab = "Residual")
  abline(h = 0, lty = "dashed")
  acf(residuals,na.action = na.pass)
}
```

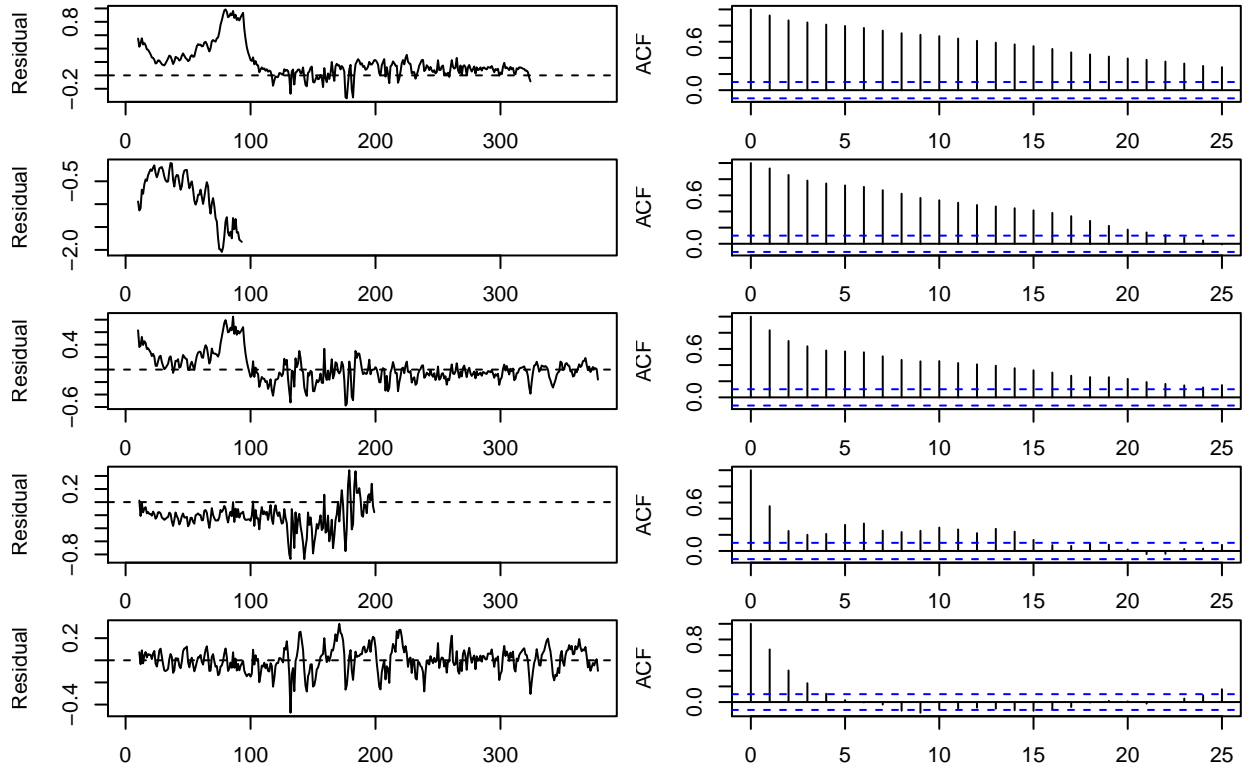
```
## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.
```

```
## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.
```

```
## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.
```

```
## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.
```

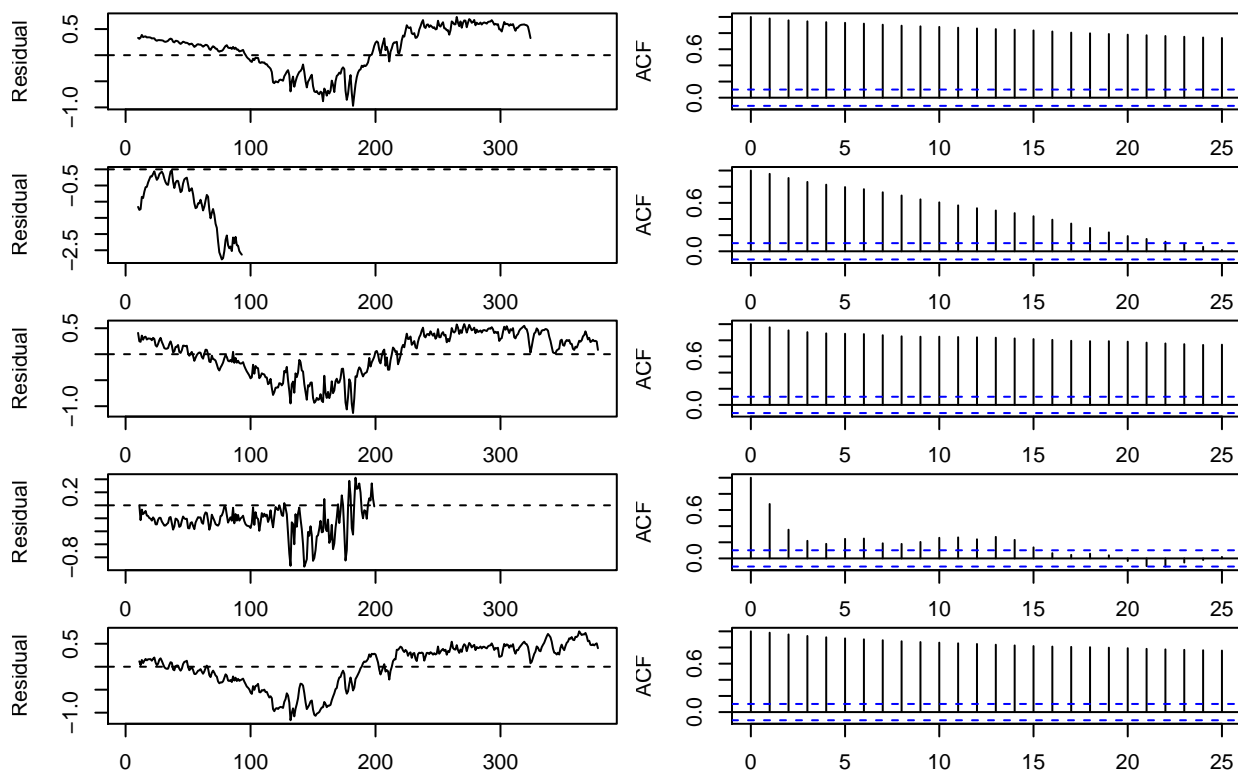
```
## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.
```



```
#Model 2, hypothesis 2 (creeks vs ponds)
mod2.params
```

```
##
## MARSS fit is
## Estimation method: kem
## Convergence test: conv.test.slope.tol = 0.5, abstol = 0.001
## Estimation converged in 91 iterations.
## Log-likelihood: -4891.9
## AIC: 9799.801   AICc: 9799.817
##
##           ML.Est  Std.Err   low.CI   up.CI
## R.diag  0.176657 0.002753  0.171261 0.182053
## Q.(1,1) 0.004101 0.000690  0.002748 0.005453
## Q.(2,1) 0.005458 0.000909  0.003676 0.007240
## Q.(2,2) 0.008550 0.001468  0.005672 0.011428
## x0.X1   0.933060 0.198706  0.543604 1.322515
## x0.X2   1.055530 0.293369  0.480537 1.630523
## C.X1    0.000300 0.000239 -0.000168 0.000768
## C.X2    0.000325 0.000346 -0.000353 0.001003
## Initial states (x0) defined at t=0
##
## CIs calculated at alpha = 0.05 via method=hessian
```

```
par(mfrow=c(5,2), mai=c(0.1,0.5,0.2,0.1), omi=c(0.5,0,0,0))
for (j in 1:5) {
  plot.ts(residuals<-MARSSresiduals(mod2.fit, type = "tt1")$model.residuals[j, ],
          ylab = "Residual")
  abline(h = 0, lty = "dashed")
  acf(residuals,na.action = na.pass)
}
```



```
#Model 3, hypothesis 3 (trib vs. trib)
mod3.params
```

```
##
## MARSS fit is
## Estimation method: kem
## Convergence test: conv.test.slope.tol = 0.5, abstol = 0.001
## Estimation converged in 2518 iterations.
## Log-likelihood: -1836.822
## AIC: 3711.645   AICc: 3711.734
##
##           ML.Est  Std.Err   low.CI   up.CI
## R.diag  0.082798  0.001311  8.02e-02  0.085368
## Q.(1,1)  0.010326  0.001421  7.54e-03  0.013112
## Q.(2,1)  0.009662  0.001319  7.08e-03  0.012248
## Q.(3,1)  0.003657  0.000625  2.43e-03  0.004882
## Q.(4,1)  0.009611  0.001286  7.09e-03  0.012132
## Q.(2,2)  0.012367  0.001709  9.02e-03  0.015717
## Q.(3,2)  0.004285  0.000690  2.93e-03  0.005637
## Q.(4,2)  0.011955  0.001590  8.84e-03  0.015070
## Q.(3,3)  0.002523  0.000420  1.70e-03  0.003347
## Q.(4,3)  0.004213  0.000667  2.91e-03  0.005520
## Q.(4,4)  0.011584  0.001559  8.53e-03  0.014640
## x0.X1    0.992099  0.320593  3.64e-01  1.620449
## x0.X2    1.076092  0.339679  4.10e-01  1.741850
```

```
## x0.X3    0.918146 0.153676 6.17e-01 1.219345
## x0.X4    1.083917 0.326099 4.45e-01 1.723059
## C.X1     0.000116 0.000377 -6.23e-04 0.000854
## C.X2     0.000300 0.000412 -5.08e-04 0.001108
## C.X3     0.000373 0.000187 5.91e-06 0.000741
## C.X4     0.000293 0.000398 -4.88e-04 0.001074
## Initial states (x0) defined at t=0
##
## CIs calculated at alpha = 0.05 via method=hessian
```

```
par(mfrow=c(5,2), mai=c(0.1,0.5,0.2,0.1), omi=c(0.5,0,0,0))
for (j in 1:5) {
  plot.ts(residuals<-MARSSresiduals(mod3.fit, type = "tt1")$model.residuals[j, ],
          ylab = "Residual")
  abline(h = 0, lty = "dashed")
  acf(residuals,na.action = na.pass)
}
```

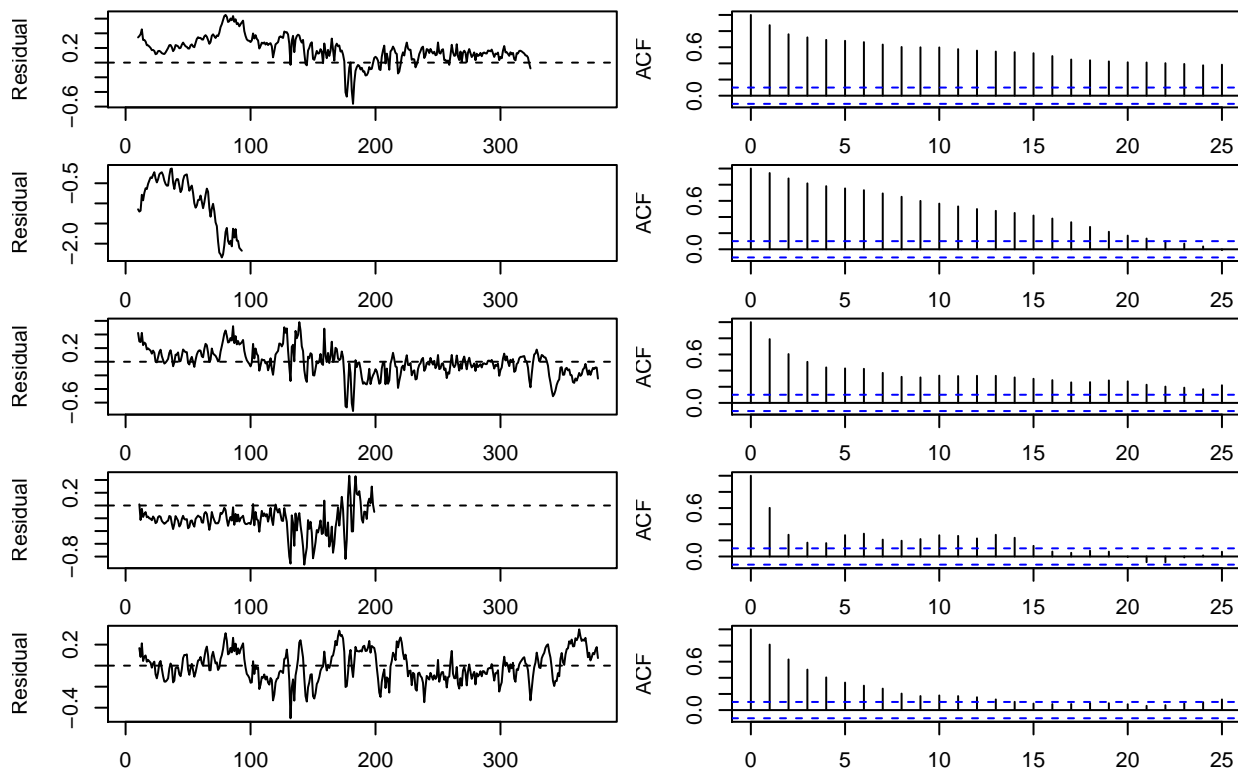
```
## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.

## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.

## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.

## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.

## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.
```



```
#Model 4, hypothesis 4 (all same)
mod4.params
```

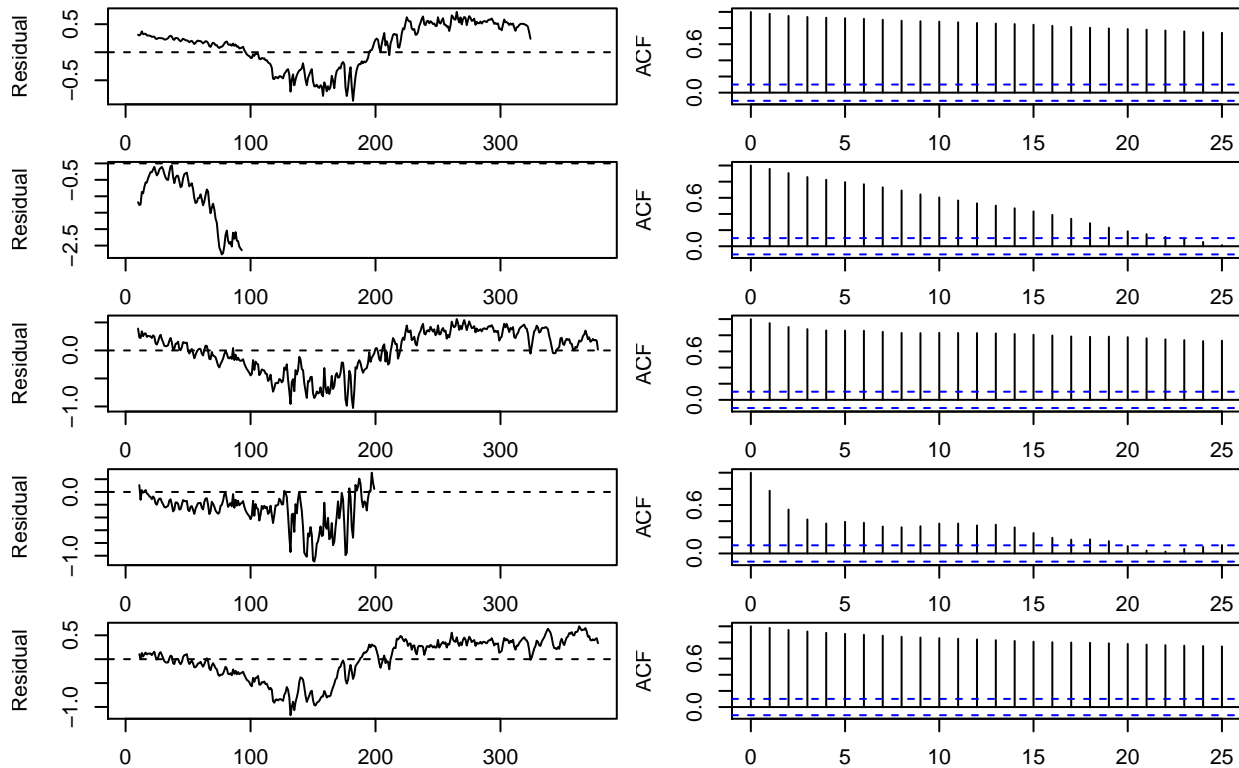
```
##
## MARSS fit is
## Estimation method: kem
## Convergence test: conv.test.slope.tol = 0.5, abstol = 0.001
## Estimation converged in 36 iterations.
## Log-likelihood: -5032.398
## AIC: 10072.8   AICc: 10072.8
##
##          ML.Est Std.Err   low.CI  up.CI
## R.diag 0.184194 0.002858 0.178593 0.18980
## Q.Q     0.004608 0.000759 0.003121 0.00610
## x0.x0    0.936723 0.210525 0.524102 1.34934
## C.C      0.000314 0.000253 -0.000182 0.00081
## Initial states (x0) defined at t=0
##
## CIs calculated at alpha = 0.05 via method=hessian
```

```
par(mfrow=c(5,2), mai=c(0.1,0.5,0.2,0.1), omi=c(0.5,0,0,0))
for (j in 1:5) {
  plot.ts(residuals<-MARSSresiduals(mod4.fit, type = "tt1")$model.residuals[j, ],
          ylab = "Residual")
  abline(h = 0, lty = "dashed")
}
```

```

    acf(residuals, na.action = na.pass)
  }

```



#...these models are not good

###Comparing Original AICc values

```

data.frame(Model=c("Model1", "Model2", "Model3", "Model4"),
           AICc=round(c(mod1.fit$AICc,
                        mod2.fit$AICc,
                        mod3.fit$AICc,
                        mod4.fit$AICc),1))

```

```

##   Model   AICc
## 1 Model1 -444.1
## 2 Model2 9799.8
## 3 Model3 3711.7
## 4 Model4 10072.8

```

###correct for seasonality using Fourier Series, and z-scoring airtemperature as an additional covariate
 ###Question: Did I do the period correctly?

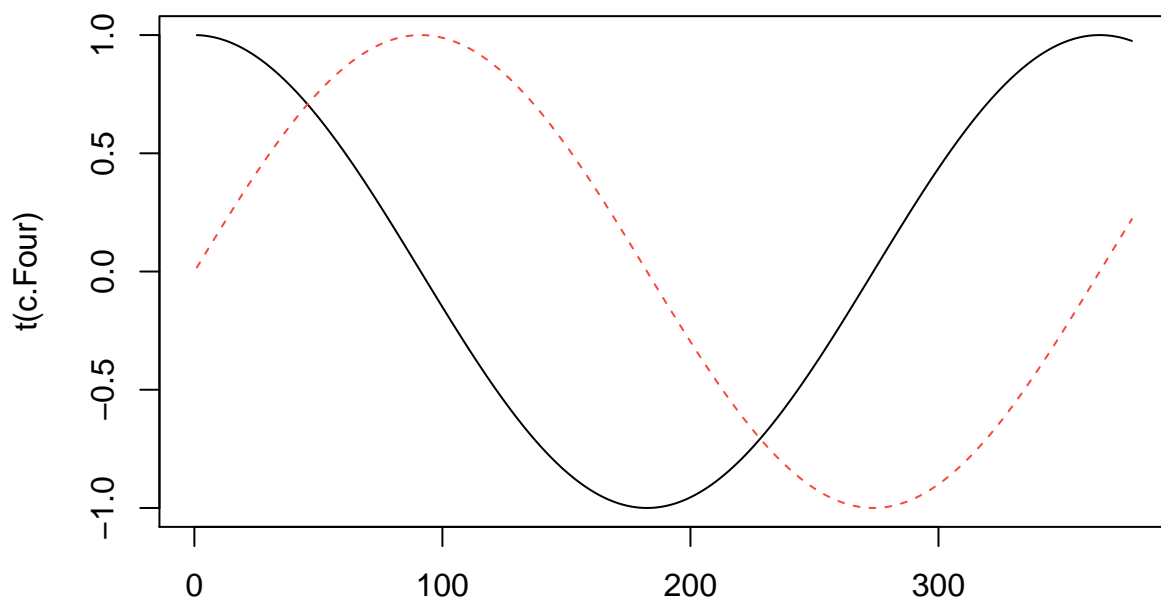

```
#Correct for seasonality using Fourier Series
TT = ncol(transformed_dat) # number of time periods/samples
period = 365 # number of "seasons" (e.g., 12 months per year)
per.1st = 1 # first "season" (e.g., Jan = 1, July = 7)
c = diag(period) # create factors for seasons
for(i in 2:(ceiling(TT/period))) {c = cbind(c,diag(period))}
dim(c)
```

```
## [1] 365 730
```

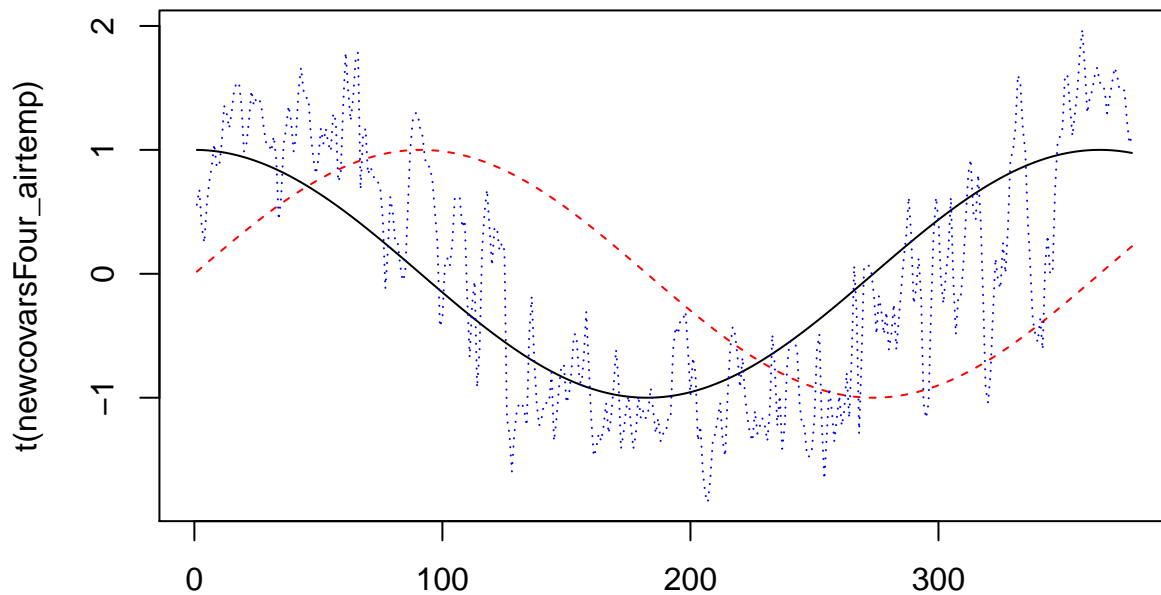
```
#Create Fourier Series
cos.t = cos(2 * pi * seq(TT) / period)
sin.t = sin(2 * pi * seq(TT) / period)
c.Four = rbind(cos.t,sin.t)
cor(c.Four[1,],c.Four[2,]) # not correlated!
```

```
## [1] 0.007872561
```

```
matplot(t(c.Four), type="l")
```



```
#Now fit model with seasonality AND an additional covariate (airtemp from above)
airtemp_z <- zscore(airtemp$TAVG)
newcovarsFour_airtemp <- rbind(c.Four, "airtemp"=airtemp_z)
matplot(t(newcovarsFour_airtemp), type="l", col=c("black","red","blue"))
```



###Checking model results and residuals when log transformed

```
mod5.fit <- readRDS("mod5.fit.rds")
mod5.params <- readRDS("mod5.params.rds")
mod6.fit <- readRDS("mod6.fit.rds")
mod6.params <- readRDS("mod6.params.rds")
mod7.fit <- readRDS("mod7.fit.rds")
mod7.params <- readRDS("mod7.params.rds")
mod8.fit <- readRDS("mod8.fit.rds")
mod8.params <- readRDS("mod8.params.rds")
```

#Model 5, hypothesis 1 (all separate)
mod5.params

```
##
## MARSS fit is
## Estimation method: kem
## Convergence test: conv.test.slope.tol = 0.5, abstol = 0.001
## Estimation converged in 2833 iterations.
## Log-likelihood: 386.5636
## AIC: -551.1273   AICc: -548.1774
##
##           ML.Est Std.Err low.CI up.CI
## R.diag    0.046473 0.000759 4.50e-02 0.047961
## Q.(1,1)    0.010158 0.001506 7.21e-03 0.013110
## Q.(2,1)    0.009165 0.001216 6.78e-03 0.011549
```

## Q.(3,1)	0.009139	0.001270	6.65e-03	0.011629
## Q.(4,1)	0.008580	0.001184	6.26e-03	0.010900
## Q.(5,1)	0.008557	0.001234	6.14e-03	0.010974
## Q.(6,1)	0.011278	0.001651	8.04e-03	0.014514
## Q.(7,1)	0.005811	0.001014	3.82e-03	0.007798
## Q.(8,1)	0.000830	0.000477	-1.05e-04	0.001766
## Q.(9,1)	0.004203	0.000609	3.01e-03	0.005397
## Q.(10,1)	0.002646	0.000550	1.57e-03	0.003725
## Q.(11,1)	0.010720	0.001434	7.91e-03	0.013530
## Q.(2,2)	0.010017	0.001353	7.37e-03	0.012669
## Q.(3,2)	0.009388	0.001231	6.97e-03	0.011801
## Q.(4,2)	0.009248	0.001201	6.89e-03	0.011602
## Q.(5,2)	0.009075	0.001228	6.67e-03	0.011482
## Q.(6,2)	0.012821	0.001729	9.43e-03	0.016210
## Q.(7,2)	0.006211	0.000999	4.25e-03	0.008170
## Q.(8,2)	0.000715	0.000454	-1.75e-04	0.001606
## Q.(9,2)	0.004508	0.000607	3.32e-03	0.005697
## Q.(10,2)	0.002712	0.000533	1.67e-03	0.003757
## Q.(11,2)	0.011067	0.001394	8.34e-03	0.013799
## Q.(3,3)	0.013393	0.001641	1.02e-02	0.016610
## Q.(4,3)	0.009152	0.001256	6.69e-03	0.011614
## Q.(5,3)	0.008776	0.001280	6.27e-03	0.011285
## Q.(6,3)	0.010262	0.001630	7.07e-03	0.013456
## Q.(7,3)	0.006238	0.001091	4.10e-03	0.008375
## Q.(8,3)	0.001496	0.000552	4.14e-04	0.002578
## Q.(9,3)	0.004957	0.000687	3.61e-03	0.006304
## Q.(10,3)	0.003860	0.000651	2.58e-03	0.005135
## Q.(11,3)	0.015018	0.001701	1.17e-02	0.018353
## Q.(4,4)	0.008663	0.001352	6.01e-03	0.011312
## Q.(5,4)	0.008441	0.001184	6.12e-03	0.010761
## Q.(6,4)	0.011778	0.001645	8.55e-03	0.015002
## Q.(7,4)	0.005720	0.000954	3.85e-03	0.007589
## Q.(8,4)	0.000853	0.000435	2.70e-07	0.001706
## Q.(9,4)	0.004265	0.000599	3.09e-03	0.005439
## Q.(10,4)	0.002588	0.000515	1.58e-03	0.003598
## Q.(11,4)	0.010750	0.001427	7.95e-03	0.013546
## Q.(5,5)	0.008782	0.001465	5.91e-03	0.011652
## Q.(6,5)	0.011434	0.001663	8.17e-03	0.014694
## Q.(7,5)	0.005485	0.000970	3.58e-03	0.007386
## Q.(8,5)	0.000821	0.000443	-4.68e-05	0.001689
## Q.(9,5)	0.004152	0.000608	2.96e-03	0.005344
## Q.(10,5)	0.002672	0.000543	1.61e-03	0.003736
## Q.(11,5)	0.010456	0.001475	7.56e-03	0.013348
## Q.(6,6)	0.017758	0.002693	1.25e-02	0.023036
## Q.(7,6)	0.007440	0.001336	4.82e-03	0.010058
## Q.(8,6)	0.000452	0.000606	-7.34e-04	0.001639
## Q.(9,6)	0.005568	0.000825	3.95e-03	0.007185
## Q.(10,6)	0.002661	0.000688	1.31e-03	0.004009
## Q.(11,6)	0.012286	0.001848	8.66e-03	0.015908
## Q.(7,7)	0.005763	0.001094	3.62e-03	0.007908
## Q.(8,7)	0.000596	0.000373	-1.35e-04	0.001328
## Q.(9,7)	0.002840	0.000494	1.87e-03	0.003807
## Q.(10,7)	0.001981	0.000454	1.09e-03	0.002870
## Q.(11,7)	0.007796	0.001271	5.31e-03	0.010287

## Q.(8,8)	0.000707	0.000217	2.82e-04	0.001133
## Q.(9,8)	0.000548	0.000227	1.03e-04	0.000992
## Q.(10,8)	0.000664	0.000214	2.45e-04	0.001083
## Q.(11,8)	0.001822	0.000631	5.85e-04	0.003059
## Q.(9,9)	0.002243	0.000386	1.49e-03	0.003000
## Q.(10,9)	0.001554	0.000288	9.90e-04	0.002119
## Q.(11,9)	0.005728	0.000773	4.21e-03	0.007243
## Q.(10,10)	0.001559	0.000342	8.89e-04	0.002229
## Q.(11,10)	0.004413	0.000730	2.98e-03	0.005845
## Q.(11,11)	0.017198	0.002019	1.32e-02	0.021156
## x0.X1	1.004073	0.318263	3.80e-01	1.627856
## x0.X2	1.127373	0.312950	5.14e-01	1.740745
## x0.X3	1.171648	0.345779	4.94e-01	1.849363
## x0.X4	1.239960	0.289868	6.72e-01	1.808091
## x0.X5	1.380072	0.301517	7.89e-01	1.971035
## x0.X6	1.342542	0.438404	4.83e-01	2.201798
## x0.X7	0.833946	0.249183	3.46e-01	1.322335
## x0.X8	0.589145	0.098786	3.96e-01	0.782761
## x0.X9	0.870386	0.143302	5.90e-01	1.151253
## x0.X10	0.840911	0.128746	5.89e-01	1.093248
## x0.X11	1.175008	0.386189	4.18e-01	1.931925
## C.(X1,cos.t)	-0.024999	0.016304	-5.70e-02	0.006956
## C.(X2,cos.t)	-0.004857	0.015634	-3.55e-02	0.025785
## C.(X3,cos.t)	-0.017093	0.017866	-5.21e-02	0.017923
## C.(X4,cos.t)	-0.007122	0.014761	-3.61e-02	0.021809
## C.(X5,cos.t)	-0.005733	0.015306	-3.57e-02	0.024266
## C.(X6,cos.t)	0.016513	0.021392	-2.54e-02	0.058440
## C.(X7,cos.t)	0.000410	0.013149	-2.54e-02	0.026181
## C.(X8,cos.t)	0.014757	0.005707	3.57e-03	0.025944
## C.(X9,cos.t)	0.014909	0.007670	-1.25e-04	0.029942
## C.(X10,cos.t)	0.017251	0.007092	3.35e-03	0.031152
## C.(X11,cos.t)	-0.008135	0.020074	-4.75e-02	0.031208
## C.(X1,sin.t)	-0.033801	0.009749	-5.29e-02	-0.014694
## C.(X2,sin.t)	-0.027244	0.009508	-4.59e-02	-0.008608
## C.(X3,sin.t)	-0.032358	0.010931	-5.38e-02	-0.010933
## C.(X4,sin.t)	-0.028507	0.008907	-4.60e-02	-0.011050
## C.(X5,sin.t)	-0.026807	0.009112	-4.47e-02	-0.008948
## C.(X6,sin.t)	-0.016866	0.012844	-4.20e-02	0.008307
## C.(X7,sin.t)	-0.021720	0.007615	-3.66e-02	-0.006794
## C.(X8,sin.t)	-0.012635	0.003042	-1.86e-02	-0.006673
## C.(X9,sin.t)	-0.016143	0.004585	-2.51e-02	-0.007155
## C.(X10,sin.t)	-0.015757	0.004046	-2.37e-02	-0.007826
## C.(X11,sin.t)	-0.028513	0.012338	-5.27e-02	-0.004331
## C.(X1,airtemp)	0.027508	0.012689	2.64e-03	0.052378
## C.(X2,airtemp)	0.010778	0.012049	-1.28e-02	0.034393
## C.(X3,airtemp)	0.024818	0.013737	-2.11e-03	0.051741
## C.(X4,airtemp)	0.012634	0.011413	-9.74e-03	0.035004
## C.(X5,airtemp)	0.007170	0.011941	-1.62e-02	0.030575
## C.(X6,airtemp)	-0.010031	0.016617	-4.26e-02	0.022538
## C.(X7,airtemp)	0.010245	0.010376	-1.01e-02	0.030582
## C.(X8,airtemp)	0.006441	0.004683	-2.74e-03	0.015620
## C.(X9,airtemp)	0.003239	0.005980	-8.48e-03	0.014960
## C.(X10,airtemp)	0.000764	0.005654	-1.03e-02	0.011845
## C.(X11,airtemp)	0.016581	0.015404	-1.36e-02	0.046773

```
## Initial states (x0) defined at t=0
##
## CIs calculated at alpha = 0.05 via method=hessian
```

```
par(mfrow=c(5,2), mai=c(0.1,0.5,0.2,0.1), omi=c(0.5,0,0,0))
for (j in 1:5) {
  plot.ts(residuals<-MARSSresiduals(mod5.fit, type = "tt1")$model.residuals[j, ],
          ylab = "Residual")
  abline(h = 0, lty = "dashed")
  acf(residuals,na.action = na.pass)
}
```

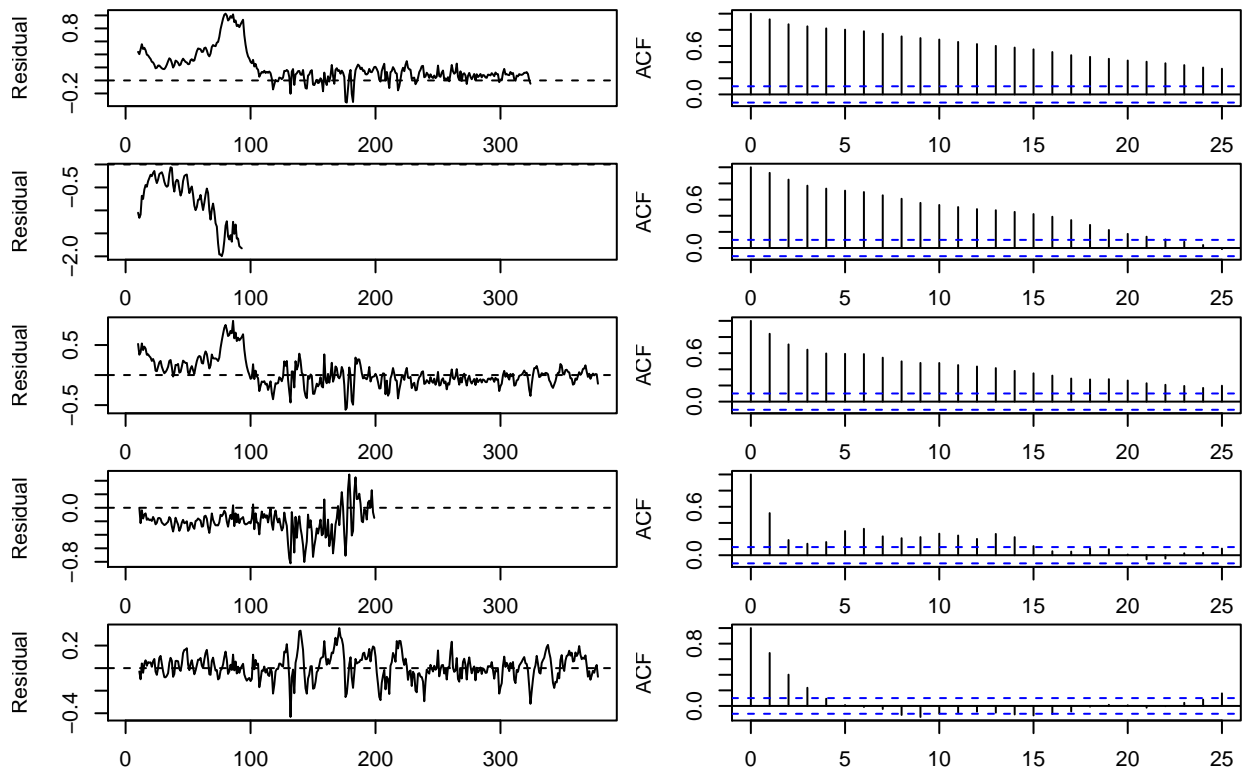
```
## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.
```

```
## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.
```

```
## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.
```

```
## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.
```

```
## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.
```

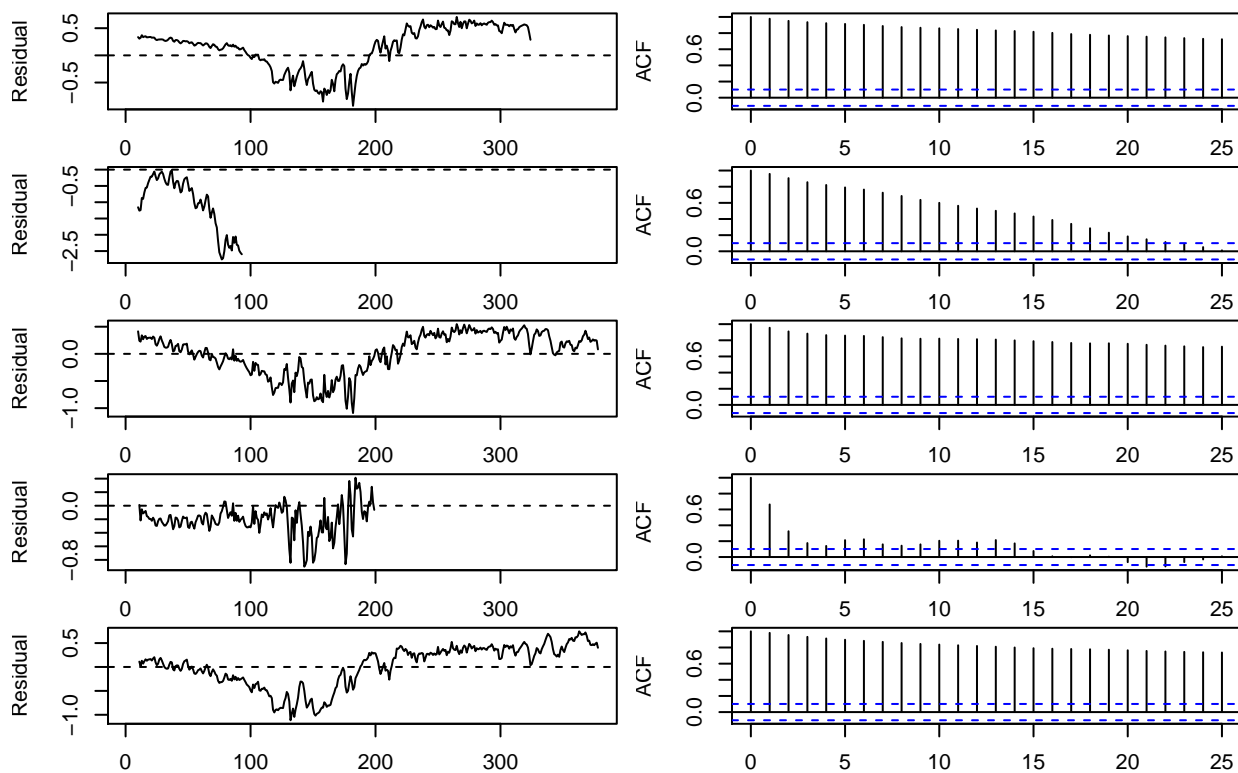


```
#Model 6, hypothesis 2 (creeks vs ponds)
```

```
mod6.params
```

```
##
## MARSS fit is
## Estimation method: kem
## Convergence test: conv.test.slope.tol = 0.5, abstol = 0.001
## Estimation converged in 196 iterations.
## Log-likelihood: -4871.922
## AIC: 9767.843   AICc: 9767.88
##
##           ML.Est  Std.Err  low.CI  up.CI
## R.diag      1.77e-01 0.002751  0.17150 0.18228
## Q.(1,1)      2.97e-03 0.000550  0.00189 0.00405
## Q.(2,1)      4.67e-03 0.000798  0.00310 0.00623
## Q.(2,2)      7.84e-03 0.001417  0.00506 0.01061
## x0.X1        9.19e-01 0.175447  0.57535 1.26309
## x0.X2        1.14e+00 0.288131  0.57517 1.70463
## C.(X1,cos.t) -3.69e-05 0.009149 -0.01797 0.01789
## C.(X2,cos.t) -2.06e-02 0.014972 -0.04996 0.00873
## C.(X1,sin.t) -2.25e-02 0.005374 -0.03301 -0.01194
## C.(X2,sin.t) -3.41e-02 0.008765 -0.05130 -0.01695
## C.(X1,airtemp) 1.18e-02 0.007176 -0.00223 0.02590
## C.(X2,airtemp) 2.87e-02 0.011763 0.00567 0.05178
## Initial states (x0) defined at t=0
##
## CIs calculated at alpha = 0.05 via method=hessian
```

```
par(mfrow=c(5,2), mai=c(0.1,0.5,0.2,0.1), omi=c(0.5,0,0,0))
for (j in 1:5) {
  plot.ts(residuals<-MARSSresiduals(mod6.fit, type = "tt1")$model.residuals[j, ],
          ylab = "Residual")
  abline(h = 0, lty = "dashed")
  acf(residuals,na.action = na.pass)
}
```



```
#Model 7, hypothesis 3 (trib vs. trib)
mod7.params
```

```
##
## MARSS fit is
## Estimation method: kem
## Convergence test: conv.test.slope.tol = 0.5, abstol = 0.001
## Estimation converged in 3245 iterations.
## Log-likelihood: -1790.67
## AIC: 3635.341   AICc: 3635.519
##
##
```

	ML.Est	Std.Err	low.CI	up.CI
## R.diag	0.08268	0.001304	0.080121	0.08523
## Q.(1,1)	0.00989	0.001390	0.007160	0.01261
## Q.(2,1)	0.00883	0.001253	0.006374	0.01128
## Q.(3,1)	0.00281	0.000467	0.001896	0.00372
## Q.(4,1)	0.00986	0.001349	0.007212	0.01250
## Q.(2,2)	0.01087	0.001611	0.007714	0.01403
## Q.(3,2)	0.00306	0.000502	0.002082	0.00405
## Q.(4,2)	0.01160	0.001577	0.008509	0.01469
## Q.(3,3)	0.00117	0.000232	0.000712	0.00162
## Q.(4,3)	0.00345	0.000549	0.002378	0.00453
## Q.(4,4)	0.01251	0.001777	0.009031	0.01600
## x0.X1	1.05597	0.320861	0.427090	1.68484
## x0.X2	1.18240	0.327436	0.540634	1.82416

```
## x0.X3      0.78272 0.109468 0.568165 0.99727
## x0.X4      1.17979 0.345826 0.501981 1.85759
## C.(X1,cos.t) -0.00858 0.015715 -0.039381 0.02222
## C.(X2,cos.t) -0.01866 0.016721 -0.051431 0.01412
## C.(X3,cos.t) 0.01416 0.005922 0.002556 0.02577
## C.(X4,cos.t) -0.01592 0.017692 -0.050597 0.01876
## C.(X1,sin.t) -0.02797 0.009499 -0.046582 -0.00935
## C.(X2,sin.t) -0.03301 0.010034 -0.052673 -0.01334
## C.(X3,sin.t) -0.01549 0.003431 -0.022210 -0.00876
## C.(X4,sin.t) -0.03196 0.010695 -0.052923 -0.01100
## C.(X1,airtemp) 0.01313 0.012137 -0.010659 0.03692
## C.(X2,airtemp) 0.02633 0.012964 0.000922 0.05174
## C.(X3,airtemp) 0.00376 0.004686 -0.005427 0.01294
## C.(X4,airtemp) 0.02383 0.013676 -0.002969 0.05064
## Initial states (x0) defined at t=0
##
## CIs calculated at alpha = 0.05 via method=hessian
```

```
par(mfrow=c(5,2), mai=c(0.1,0.5,0.2,0.1), omi=c(0.5,0,0,0))
for (j in 1:5) {
  plot.ts(residuals<-MARSSresiduals(mod7.fit, type = "tt1")$model.residuals[j, ],
          ylab = "Residual")
  abline(h = 0, lty = "dashed")
  acf(residuals,na.action = na.pass)
}
```

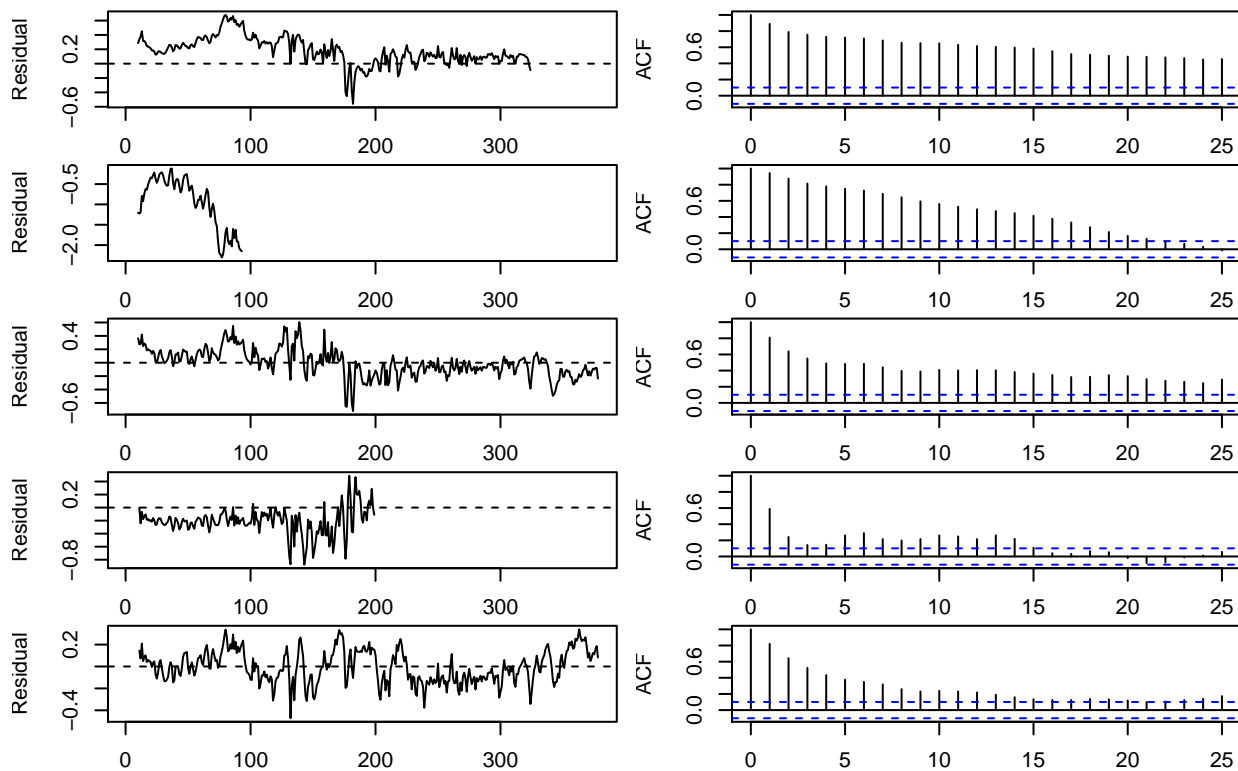
```
## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.
```

```
## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.
```

```
## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.
```

```
## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.
```

```
## MARSSresiduals.tt1 reported warnings. See msg element of returned residuals object.
```

```
#Model 8, hypothesis 4 (all same)
mod8.params
```

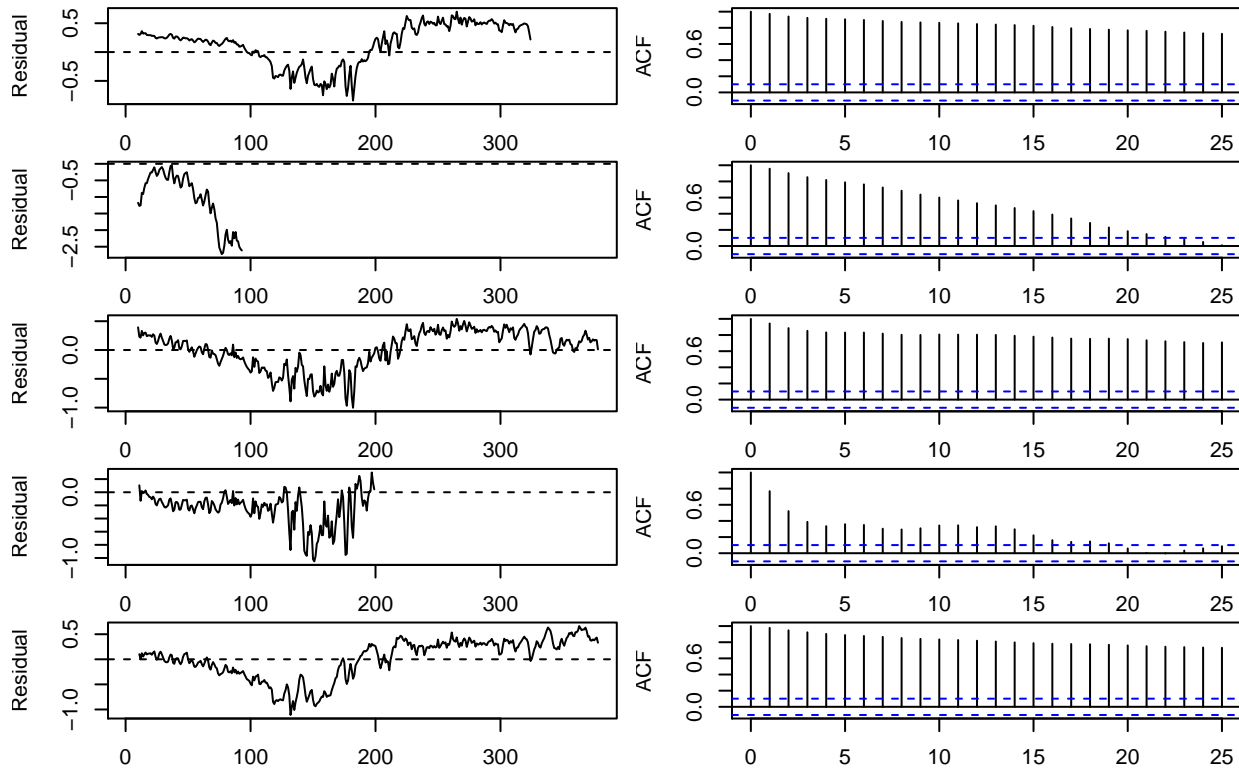
```
##
## MARSS fit is
## Estimation method: kem
## Convergence test: conv.test.slope.tol = 0.5, abstol = 0.001
## Estimation converged in 39 iterations.
## Log-likelihood: -5020.639
## AIC: 10053.28   AICc: 10053.29
##
##           ML.Est  Std.Err  low.CI  up.CI
## R.diag      0.18437 0.002857 0.178767 0.18997
## Q.Q          0.00358 0.000631 0.002345 0.00482
## x0.x0        0.94813 0.193187 0.569495 1.32677
## C.(X1,cos.t) -0.00513 0.010009 -0.024749 0.01449
## C.(X1,sin.t) -0.02543 0.005889 -0.036968 -0.01389
## C.(X1,airtemp) 0.01621 0.007838 0.000849 0.03157
## Initial states (x0) defined at t=0
##
## CIs calculated at alpha = 0.05 via method=hessian
```

```
par(mfrow=c(5,2), mai=c(0.1,0.5,0.2,0.1), omi=c(0.5,0,0,0))
for (j in 1:5) {
  plot.ts(residuals<-MARSSresiduals(mod8.fit, type = "tt1")$model.residuals[j, ],
```

```

      ylab = "Residual")
    abline(h = 0, lty = "dashed")
    acf(residuals, na.action = na.pass)
  }

```



#...these models are not good

Comparing corrected AICc values

```

data.frame(Model=c("Model15", "Model16", "Model17", "Model18"),
  AICc=round(c(mod5.fit$AICc,
    mod6.fit$AICc,
    mod7.fit$AICc,
    mod8.fit$AICc),1))

```

```

##   Model   AICc
## 1 Model5 -548.2
## 2 Model6 9767.9
## 3 Model7 3635.5
## 4 Model8 10053.3

```