### LL(1) GRAMMARS

A context-free grammar whose Predict sets are always disjoint (for the same non-terminal) is said to be *LL(1)*.

LL(1) grammars are ideally suited for top-down parsing because it is always possible to correctly predict the expansion of any non-terminal. No backup is ever needed.

Formally, let  $\begin{aligned} &\text{First}(X_1...X_n) = \\ &\{a \text{ in } V_t \mid A \rightarrow X_1...X_n \Rightarrow^* a...\} \end{aligned}$   $\begin{aligned} &\text{Follow}(A) = \{a \text{ in } V_t \mid S \Rightarrow^+ ...Aa...\} \end{aligned}$ 

 $\begin{aligned} & \text{Predict}(A \rightarrow X_1 ... X_n) = \\ & \text{If } X_1 ... X_n \Rightarrow^* \lambda \\ & \text{Then First}(X_1 ... X_n) \text{ U Follow}(A) \\ & \text{Else First}(X_1 ... X_n) \end{aligned}$ 

If some CFG, G, has the property that for all pairs of distinct productions with the same lefthand side,  $A \rightarrow X_1 ... X_n$  and  $A \rightarrow Y_1 ... Y_n$ 

 $A \rightarrow X_1...X_n$  and  $A \rightarrow Y_1...Y_m$  it is the case that

Predict(A  $\rightarrow$  X<sub>1</sub>...X<sub>n</sub>)  $\cap$ 

 $Predict(A \rightarrow Y_1...Y_m) = \phi$ 

then G is LL(1).

LL(1) grammars are easy to parse in a top-down manner since predictions are always correct.

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### Example

Production	Predict Set
$S \rightarrow A a$	{b,d,a}
$A \rightarrow B D$	{b, d, a}
$B \to b$	{ b }
$B \rightarrow \lambda$	{d, a}
$D\tod$	{ d }
$D \rightarrow \lambda$	{ a }

Since the predict sets of both B productions and both D productions are disjoint, this grammar is LL(1).

### RECURSIVE DESCENT PARSERS

An early implementation of topdown (LL(1)) parsing was recursive descent.

A parser was organized as a set of parsing procedures, one for each non-terminal. Each parsing procedure was responsible for parsing a sequence of tokens derivable from its non-terminal.

For example, a parsing procedure, A, when called, would call the scanner and match a token sequence derivable from A.

Starting with the start symbol's parsing procedure, we would then match the entire input, which must be derivable from the start symbol.

This approach is called recursive descent because the parsing procedures were typically recursive, and they descended down the input's parse tree (as top-down parsers always do).

## Building A Recursive Descent Parser

We start with a procedure **Match**, that matches the current input token against a predicted token:

void Match(Terminal a) {
 if (a == currentToken)
 currentToken = Scanner();
 else SyntaxErrror();}

To build a parsing procedure for a non-terminal A, we look at all productions with A on the lefthand side:

$$A \rightarrow X_1...X_n \mid A \rightarrow Y_1...Y_m \mid ...$$

We use predict sets to decide which production to match (LL(1) grammars always have disjoint predict sets).

We match a production's righthand side by calling Match to

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match terminals, and calling parsing procedures to match non-terminals.

The general form of a parsing procedure for

$$\begin{array}{c|c} A \to X_1...X_n & A \to Y_1...Y_m & ... & is \\ \text{void A() } \{\\ \text{if } (\text{currentToken in } \text{Predict}(A \to X_1...X_n)) \\ \text{for}(\text{i=1}; \text{i<=n}; \text{i++}) \\ \text{if } (X[\text{i] is a terminal}) \\ \text{Match}(X[\text{i]}); \\ \text{else } X[\text{i]()}; \\ \text{else} \\ \text{if } (\text{currentToken in } \text{Predict}(A \to Y_1...Y_m)) \\ \text{for}(\text{i=1}; \text{i<=m}; \text{i++}) \\ \text{if } (Y[\text{i] is a terminal}) \\ \text{Match}(Y[\text{i]}); \\ \text{else } Y[\text{i]()}; \\ \text{else} \\ \text{// } \text{Handle other } A \to ... \text{ productions} \\ \text{else } \text{// } \text{No production } \text{predicted} \\ \text{SyntaxError()}; \\ \} \end{array}$$

Usually this general form isn't used.

Instead, each production is "macro-expanded" into a sequence of **Match** and parsing procedure calls.

### Example: CSX-Lite

Production	Predict Set
Prog → { Stmts } Eof	{
Stmts → Stmt Stmts	id if
Stmts $\rightarrow \lambda$	}
$Stmt \to id = Expr \; ;$	id
Stmt  o if (Expr)Stmt	if
Expr → id Etail	id
Etail → + Expr	+
Etail → - Expr	-
Etail $\rightarrow \lambda$	) ;

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```
CSX-Lite Parsing Procedures
```

```
void Prog() {
   Match("{");
   Stmts();
  Match("}");
  Match (Eof);
void Stmts() {
 if (currentToken == id ||
currentToken == if) {
       Stmt();
      Stmts();
 } else {
       /* null */
}}
void Stmt() {
  if (currentToken == id) {
      Match(id);
Match("=");
      Expr();
Match(";");
 } else {
      Match(if);
      Match("(");
      Expr();
      Match(")");
      Stmt();
}}
```

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```
void Expr() {
   Match(id);
   Etail();
}

void Etail() {
   if (currentToken == "+") {
        Match("+");
        Expr();
} else if (currentToken == "-") {
        Match("-");
        Expr();
} else {
        /* null */
}}
```

Let's use recursive descent to parse { a = b + c; } Eof
We start by calling Prog() since this represents the start symbol.

Calls Pending	Remaining Input
Prog()	{ a = b + c; } Eof
<pre>Match("{"); Stmts(); Match("}"); Match(Eof);</pre>	{ a = b + c; } Eof
Stmts(); Match("}"); Match(Eof);	a = b + c; } Eof
<pre>Stmt(); Stmts(); Match("}"); Match(Eof);</pre>	a = b + c; } Eof
<pre>Match(id); Match("="); Expr(); Match(";"); Stmts(); Match("}"); Match(Eof);</pre>	a = b + c; } Eof

<b>Calls Pending</b>	Remaining Input			
Match("=");	= b + c; } Eof			
<pre>Expr();</pre>				
Match(";");				
Stmts();				
Match("}");				
<pre>Match(Eof);</pre>				
Expr();	b + c; } Eof			
<pre>Match(";");</pre>				
Stmts();				
<pre>Match("}");</pre>				
<pre>Match(Eof);</pre>				
Match(id);	b + c; } Eof			
<pre>Etail();</pre>				
<pre>Match(";");</pre>				
Stmts();				
<pre>Match("}");</pre>				
<pre>Match(Eof);</pre>				
Etail();	+ c; } Eof			
Match(";");				
Stmts();				
Match("}");				
<pre>Match(Eof);</pre>				

Calls Pending	Remaining Input			
Match("+");	+ c; } Eof			
<pre>Expr();</pre>				
<pre>Match(";");</pre>				
Stmts();				
<pre>Match("}");</pre>				
<pre>Match(Eof);</pre>				
Expr();	c; } Eof			
<pre>Match(";");</pre>				
Stmts();				
<pre>Match("}");</pre>				
<pre>Match(Eof);</pre>				
Match(id);	c; } Eof			
<pre>Etail();</pre>				
<pre>Match(";");</pre>				
Stmts();				
<pre>Match("}");</pre>				
<pre>Match(Eof);</pre>				
Etail();	; } Eof			
<pre>Match(";");</pre>				
Stmts();				
<pre>Match("}");</pre>				
<pre>Match(Eof);</pre>				
/* null */	; } Eof			
Match(";");				
Stmts();				
Match("}");				
Match(Eof);				

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Calls Pending	Remaining Input
<pre>Match(";"); Stmts(); Match("}"); Match(Eof);</pre>	; } Eof
Stmts(); Match("}"); Match(Eof);	} Eof
/* null */ Match("}"); Match(Eof);	} Eof
<pre>Match("}"); Match(Eof);</pre>	} Eof
Match(Eof);	Eof
Done!	All input matched

# Syntax Errors in Recursive Descent Parsing

In recursive descent parsing, syntax errors are automatically detected. In fact, they are detected as soon as possible (as soon as the first illegal token is seen).

How? When an illegal token is seen by the parser, either it fails to predict any valid production or it fails to match an expected token in a call to Match.

Let's see how the following illegal CSX-lite program is parsed:

{ b + c = a; } Eof (Where should the first syntax error be detected?)

Calls Pending	Remaining Input
Prog()	{ b + c = a; } Eof
<pre>Match("{"); Stmts(); Match("}"); Match(Eof);</pre>	{ b + c = a; } Eof
Stmts(); Match("}"); Match(Eof);	b + c = a; } Eof
<pre>Stmt(); Stmts(); Match("}"); Match(Eof);</pre>	b + c = a; } Eof
<pre>Match(id); Match("="); Expr(); Match(";"); Stmts(); Match("}"); Match(Eof);</pre>	b + c = a; } Eof

Calls Pending	Remaining Input
<pre>Match("="); Expr(); Match(";"); Stmts(); Match("}"); Match(Eof);</pre>	+ c = a; } Eof
Call to Match fails!	+ c = a; } Eof

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### Table-Driven Top-Down Parsers

Recursive descent parsers have many attractive features. They are actual pieces of code that can be read by programmers and extended.

This makes it fairly easy to understand how parsing is done.

Parsing procedures are also convenient places to add code to build ASTs, or to do type-checking, or to generate code.

A major drawback of recursive descent is that it is quite inconvenient to change the grammar being parsed. Any change, even a minor one, may force parsing procedures to be

reprogrammed, as productions and predict sets are modified.

To a less extent, recursive descent parsing is less efficient than it might be, since subprograms are called just to match a single token or to recognize a righthand side.

An alternative to parsing procedures is to encode all prediction in a parsing table. A pre-programed driver program can use a parse table (and list of productions) to parse any LL(1) grammar.

If a grammar is changed, the parse table and list of productions will change, but the driver need not be changed.

#### LL(1) Parse Tables

An LL(1) parse table, T, is a twodimensional array. Entries in T are production numbers or blank (error) entries.

T is indexed by:

- A, a non-terminal. A is the non-terminal we want to expand.
- CT, the current token that is to be matched.
- $T[A][CT] = A \rightarrow X_1...X_n$ if CT is in Predict( $A \rightarrow X_1...X_n$ ) T[A][CT] = errorif CT predicts no production with A as its lefthand side

### CSX-lite Example

	Production	Predict Set
1	Prog → { Stmts } Eof	{
2	Stmts → Stmt Stmts	id if
3	Stmts $\rightarrow \lambda$	}
4	$Stmt \to id = Expr \; ;$	id
5	$\mathbf{Stmt} \rightarrow \mathbf{if}  \mathbf{(Expr)}  \mathbf{Stmt}$	if
6	Expr → id Etail	id
7	Etail → + Expr	+
8	Etail → - Expr	-
9	Etail $\rightarrow \lambda$	) ;

	{	}	if	(	)	id	=	+	-	;	eof
Prog	1										
Stmts		3	2			2					
Stmt			5			4					
Expr						6					
Etail					9			7	8	9	

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### LL(1) Parser Driver

Here is the driver we'll use with the LL(1) parse table. We'll also use a *parse stack* that remembers symbols we have yet to match.

```
void LLDriver(){
   Push(StartSymbol);
   while(! stackEmpty()){
    //Let X=Top symbol on parse stack
   //Let CT = current token to match
    if (isTerminal(X)) {
       match(X); //CT is updated
       pop(); //X is updated
    } else if (T[X][CT] != Error){
       //Let T[X][CT] = X→Y1...Ym
       Replace X with
       Y1...Ym on parse stack
    } else SyntaxError(CT);
}
```

### Example of LL(1) Parsing

We'll again parse { a = b + c; } Eof
We start by placing Prog (the start symbol) on the parse stack.

Parse Stack	Remaining Input
Prog	{ a = b + c; } Eof
{ Stmts } Eof	{ a = b + c; } Eof
Stmts } Eof	a = b + c; } Eof
Stmt Stmts } Eof	a = b + c; } Eof

Parse Stack	Remaining Input
id = Expr ; Stmts } Eof	a = b + c; } Eof
= Expr ; Stmts } Eof	= b + c; } Eof
Expr; Stmts Eof	b + c; } Eof
id Etail ; Stmts } Eof	b + c; } Eof

Parse Stack	Remaining Input
Etail	+ c; } Eof
; Stmts	
}	
Eof	
+	+ c; } Eof
Expr	
<i>;</i>	
Stmts	
} Eof	
FOI	
Expr	c; } Eof
;	
Stmts	
} Eof	
FOI	
id	c; } Eof
Etail	
;	
Stmts	
} Eof	
EOI	

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**Remaining Input** 

All input matched

1 4120 24441	
Etail; Stmts } Eof	; } Eof
; Stmts } Eof	; } Eof
Stmts } Eof	} Eof
} Eof	} Eof
Eof	Eof

Parse Stack

Done!

### Syntax Errors in LL(1)

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**Parsing** 

In LL(1) parsing, syntax errors are automatically detected as soon as the first illegal token is seen.

How? When an illegal token is seen by the parser, either it fetches an error entry from the LL(1) parse table *or* it fails to match an expected token.

Let's see how the following illegal CSX-lite program is parsed:

 ${ b + c = a; } Eof$ 

(Where should the first syntax error be detected?)

Parse Stack	Remaining Input
Prog	$\{ b + c = a; \} Eof$
{ Stmts } Eof	{ b + c = a; } Eof
Stmts } Eof	b + c = a; } Eof
Stmt Stmts } Eof	b + c = a; } Eof
id = Expr ; Stmts } Eof	b + c = a; } Eof

Parse Stack	Remaining Input
= Expr ; Stmts } Eof	+ c = a; } Eof
Current token (+) fails to match expected token (=)!	+ c = a; } Eof

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