

- I keep working w/ David Puelly (will be avail Spr + Summer)
- Good Sm2 final project.
- David = great resource for time series modeling.
- Possible grant app due in Feb.
- Begin w/ off-the-shelf basic model, expand from there.
- ERCOT = Electrical Power Grid council for TX.  
"Electric Reliability Council of TX"

## Two Goals:

### 1) Optimization Problem:

- want to model grid load for several (3-4) days into the future.
- want to satisfy demand at cheapest cost possible.
- many sources can be used to power grid (supply load), ea. with different load times, load costs + generation costs.
- Demand depends on a few covariates - weather (temp), season, time of day.  
Covariates may be highly corr. (Possible non-linear model)
- Will be vectorized - there are 8 regions to model + predict.
- Bayesian approach → simulate data from posterior.
- Worse to project too low than too high; asymmetric loss fun.

### 2) Demand Response Model:

- All sorts of weird contractual stuff where companies can lower their peak day rates by bidding to send electricity back to the grid. Or can commit to limit use in some way.
- A smoothing problem - want to decrease peaks on high demand days.
- Want some model for response (chg in bkr) due to this demand response process.

⊗ Bayes DLM (dynamic linear model) or AR (autoregression), vectorized.

⊗ Weather is a complication! See next pg.

## Basic Model

$y_t$  = demand on day  $t$

$x_t$  = temp on day  $t$  (most obv. predictor - can also add others)

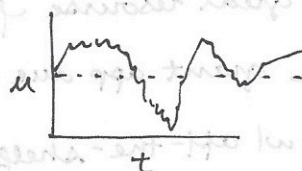
(time of day, season, etc can also be added)

$$y_t = \alpha + \mu_t + \beta_1 x_t + \epsilon_t$$

grand mean  $\alpha$       stationary (chg in mean over time) AR term  $\mu_t$

weather effect (doesn't chg over time)

$$\mu_t = \phi \mu_{t-1} + \delta_t$$



Then what is  $y_{t+1}$ ?

$$y_{t+1} = \alpha + \mu_{t+1} + \beta_1 x_{t+1} + \epsilon_{t+1} \quad \text{where } \mu_{t+1} = \phi \mu_t + \delta_{t+1}$$

$$\epsilon_t \sim N(0, \sigma^2)$$

$$\delta_t \sim N(0, \tau^2)$$

• For Bayesian setting, have posteriors.

↳ So for  $\mu, \phi, \beta, \alpha$  we can predict values by drawing from posterior.

• Catch: we don't know  $x_{t+1}$ . Can forecast  $x_{t+1}$  using a surrogate model for temp.

## Surrogate Model for Temp ( $x_{t+1}$ )

$$x_{t+1} = \hat{x}_{t+1} + \eta_{t+1}$$

↑                      ↑                      ↑

tomorrow    tomorrow    error

actual        forecast    in

temp        temp        forecast

• Time-varying estimates of temp.

• Need diff btwn forecast + real temp to get error.

• Todd @ ARL scraping this data.

• So can simulate  $x_{t+1}$  + pop into above model.

• This model can be completely diff type than above model.

## Approach

• This type of model is type of FFBS; "Full Filter Backward Sampler" - Mike West

• Begin w/ Basic, add Surrogate temp model afterwards. (Basic by mid/late Feb?)

Vectorizing

- Model will be vectorised; have 8 regions.
- Will have 2 models:
  - 1)  $\vec{y} | \vec{x}$  (main model; DLM)
  - 2)  $\vec{x}$  (surrogate model)
- Since  $P(\vec{y} | \vec{x}) P(\vec{x}) = P(\vec{y}, \vec{x})$  will have joint model also

DLM Terminology Note

- Technically, a DLM model has covariates which change over time:

$$y_t = \alpha_t + \beta_{1t} x_t + \epsilon_t$$

$\uparrow$   
 $\beta_1$  varies over time

- Our basic model has  $\beta_1$  fixed, with a time-varying intercept, so is a special case of DLM.

Next Steps

- 1) David to send Jenn chapters in West book to review, + Carlos site/time series notes.
- 2) Jenn to read chapters, articles.
- 3) Jenn to implement toy ffsb model in R.
- 4) D/S meet next week to review code.
- 5) James to send D/S file access.