## **Parameters & Notation**

Let

 $y_t = \text{load at time } t$  n = 1 (One observation at each time point) m = Number of covariates at each time point  $D_t = \{y_t, \dots, y_0, D_0, F_t, G\}$  (leaving  $V, W_t$  out for notational clarity)  $G = I_m$   $F_t = \begin{bmatrix} 1 & temp_t & temp_t^2 & bushr_t & y_{t-1} & hr.1_t & \dots & hr.23_t \end{bmatrix}$ 

Where

 $bushr_t$  = Indicator for business operating hour; 1 = business hour, 0 = not business hour  $hr.1_t$  = Indicator for time-point t being during hour 1 of the day

### Model

$$(y_t|\theta_t, D_t, v, W_t) \sim N_1(F_t'\theta_t, v)$$
  
$$(\theta_t|\theta_{t-1}, D_t, W_t) \sim N_m(G\theta_{t-1}, W_t) = N(\theta_{t-1}, W_t)$$

Model assumes v scalar and constant in time, and  $W_t$  is an (mxm) covariance matrix which varies in time. We assume  $W_t$  is diagonal.

### Prior for v

$$v|D_{t-1} \sim IG\left(\frac{n_{t-1}}{2}, \frac{n_{t-1}S_{t-1}}{2}\right)$$
  
 $v|D_t \sim IG\left(\frac{n_t}{2}, \frac{n_tS_t}{2}\right)$ 

where

 $S_0$  = hyperparameter; point estimate for observational variance v at time 0

### **Prior for** $W_t$

Assume  $W_t$  diagonal, so  $W_t = diag(w_{1t}, ..., w_{mt})$ .

$$w_{jt}|D_{t-1} \sim IG\left(\frac{n_{t-1}}{2}, \frac{n_{t-1}T_{j,t-1}}{2}\right)$$

$$v|D_t \sim IG\left(\frac{n_t}{2}, \frac{n_tT_{j,t}}{2}\right)$$

where

 $T_{j,0} = \text{hyperparameter}$ ; point estimate for system variance  $w_j$  at time 0

# **Initial Information**

$$\theta_0|D_0, v) \sim N(m_0, VC_0^*)$$

$$(v|D_0) \sim IG(\frac{n_0}{2}, \frac{n_0S_0}{2})$$

$$w_{j0} \sim IG(\frac{n_0}{2}, \frac{n_0T_{j0}}{2}) \text{ for } j = \{1 \dots m\}$$

Quantities which must be specified:

$$m_0, C_0^*, n_0, S_0, T_{10}, \ldots, T_{m0}$$

### **Inverse Gamma Parameterization**

IG indicates the inverse-gamma, s.t.

$$x \sim IG(a,b) \rightarrow p(x|a,b) = \frac{b^a}{\gamma a} x^{-a-1} \exp\left[-\frac{b}{x}\right]$$