

# Compulsory exercise 1: Group 12

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## Problem 1

a)

Quantative: Time, income earned, horsepower of a car.

Qvalitative: Marital status, origin, Gender.

b)

KNN, LDA, QDA can be used for multi-class classifications

c)

i)

The three components is called bias, variance and irreducible error.

$(E[f(X) - \hat{f}(X)])^2$  represents the bias. It is the squared expectation between our model and the true data. A high bias indicates that our model is too simple and does not capture the complexities in our data(underfitting).

$Var(\hat{f}(X))$  is the variance of our model. A high variance means our model is following our training data quite tight. It could mean our model too complex, it might follow our training data quite good, but fail on test data(overfitting).

$var(\epsilon)$  is the irreducible error. This error we have no control over. It is the inherit noise of the data, the randomness and natural variability of the true data.

ii)

Often by increasing the bias, we will reduce the variance, and vice verca. High variance could lead to higher score on training data, but if increased too much it would also decrease the score on the test data(overfitting). A high bias could make our model more interpretative and give us somehow good score on test data, but if too low it could make our model miss relevant relations between predictors and response(Underfitting). This is why we have a bias-variance trade off.

d)

The nereast neighbour for  $k=1$  is a blue dot, so our classification is blue.

For  $K=3$ , two of the nearest neighbors are red and 1 blue. This gives  $2/3$  red, so it is red.

For  $K=5$  we have  $3/5$  red, so it is red.

e)

i)

```
data(Boston)
data = Boston
model = lm(medv ~ rm + age, data=data)
summary(model)
```

```
##
## Call:
## lm(formula = medv ~ rm + age, data = data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -20.555  -2.882  -0.274   2.293  40.799
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -25.27740     2.85676  -8.848  < 2e-16 ***
## rm           8.40158     0.41208  20.388  < 2e-16 ***
## age        -0.07278     0.01029   -7.075 5.02e-12 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 6.316 on 503 degrees of freedom
## Multiple R-squared:  0.5303, Adjusted R-squared:  0.5284
## F-statistic: 283.9 on 2 and 503 DF,  p-value: < 2.2e-16
```

ii)

```
cor_matrix = cor(data.frame(data$medv, data$rm, data$age))
print(cor_matrix)
```

```
##           data.medv  data.rm  data.age
## data.medv 1.0000000  0.6953599 -0.3769546
## data.rm   0.6953599  1.0000000 -0.2402649
## data.age  -0.3769546 -0.2402649  1.0000000
```

iii)

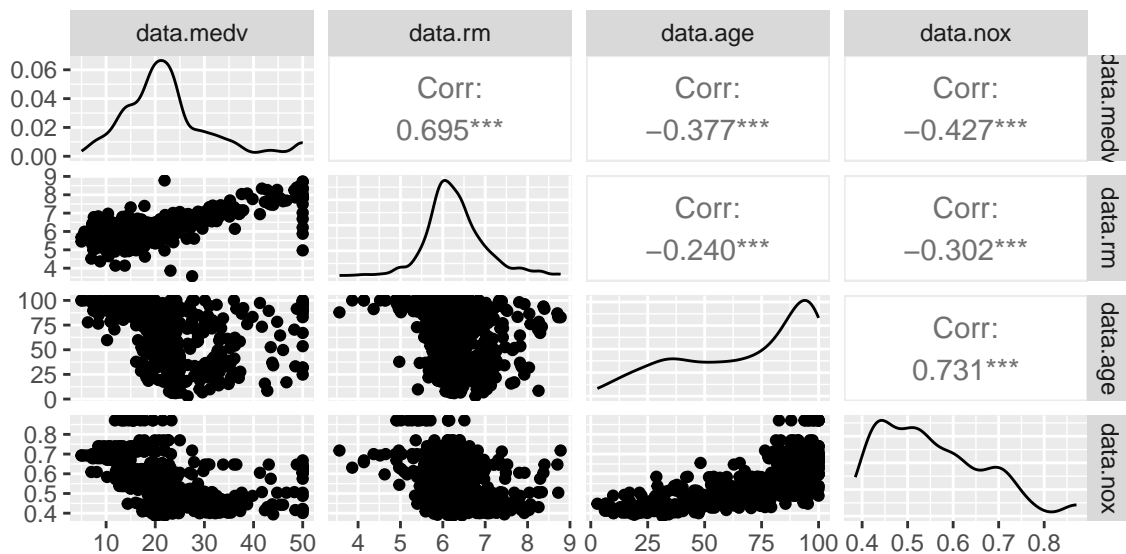
```
model2 = lm(medv ~ rm + age + nox, data=data)
summary(model2)
```

```
##
## Call:
## lm(formula = medv ~ rm + age + nox, data = data)
##
```

```
## Residuals:
##      Min       1Q   Median       3Q      Max
## -18.343  -3.168  -0.539   2.221  40.260
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -19.08308    3.33919  -5.715 1.88e-08 ***
## rm           8.12542    0.41525  19.568 < 2e-16 ***
## age        -0.03686    0.01449  -2.544 0.011269 *
## nox        -12.47877    3.58434  -3.481 0.000542 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 6.247 on 502 degrees of freedom
## Multiple R-squared:  0.5413, Adjusted R-squared:  0.5386
## F-statistic: 197.5 on 3 and 502 DF,  p-value: < 2.2e-16
```

iv)

```
ggpairs(data.frame(data$medv, data$rm, data$age, data$nox))
```



Looking at the correlation between Age and NOX, it is 0.731, which is quite high which suggests it has multicollinearity, which means they give some of the same information for the model.

## Problem 2

a)

```
model3 = lm(medv ~ poly(rm, 2) + I(age*crim) + age + crim, data=data)
summary(model3)
```

```
##
## Call:
## lm(formula = medv ~ poly(rm, 2) + I(age * crim) + age + crim,
##     data = data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -34.314  -2.602  -0.369   2.136  35.081
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   28.096141   0.666283  42.169 < 2e-16 ***
## poly(rm, 2)1  123.366564   5.600727  22.027 < 2e-16 ***
## poly(rm, 2)2   64.836354   5.479728  11.832 < 2e-16 ***
## I(age * crim)   0.005792   0.003553   1.630  0.1037
## age          -0.067283   0.009342  -7.202 2.19e-12 ***
## crim          -0.796544   0.338946  -2.350  0.0192 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 5.369 on 500 degrees of freedom
## Multiple R-squared:  0.6626, Adjusted R-squared:  0.6592
## F-statistic: 196.3 on 5 and 500 DF, p-value: < 2.2e-16
```

```
valuechanged = (-10*(-0.796544)+60*(-0.067283)+0.005792 * (-10 + 60))*1000
```

If the crime is reduced by 10 and age is 60, and then considering all other factor are kept equal our median value of the property is changed by 4218.06.

b)

First thing we could do is to plot all our data with say ggpairs from GGally. We can then look how the data is spread and correlated. We want to carefully identify if we have any outliers. If most our points follow a specific pattern, but then one point stick out, we could carefully consider to remove it. One approach could be to look at the mean and std of a given data columns and if some point lie 2 standard deviations away from the mean we could remove them.

c)

```
model4 <- lm(medv ~ crim + age + rm, data = Boston)
summary(model4)
```

```
##
## Call:
## lm(formula = medv ~ crim + age + rm, data = Boston)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -19.959  -3.143  -0.633   2.150  39.940
##
```

```
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept) -23.60556    2.76938  -8.524 < 2e-16 ***
## crim        -0.21102    0.03407  -6.195 1.22e-09 ***
## age         -0.05224    0.01046  -4.993 8.21e-07 ***
## rm          8.03284    0.40201  19.982 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 6.094 on 502 degrees of freedom
## Multiple R-squared:  0.5636, Adjusted R-squared:  0.561
## F-statistic: 216.1 on 3 and 502 DF,  p-value: < 2.2e-16
```

i)

A t-value is calculated with the follow formula:  $t = \frac{\text{Coefficient Estimate}}{\text{Standard Error}} = \frac{10}{-0.052}$

The t-value for rm if the estimated coefficient was 10, but with the same standard error is 24.89.

A higher coefficient with standard error kept the same gives us a higher t value and higher t values makes our estimate for statistically significant, as the p value drops. The t distribution is like a normal distribution but with a estimated variance from the sample. With a low amount of sample the t distributions curve has fatter tails and lower around the mean, as sample increases it converges to a normal distribution. So a higher absolute t value puts our score further towards the tails, strengthening our result.

When the coefficient estimate is increased, taking it further away from zero, it increases the t-value, making it more statistically significant.

ii)

```
f_test <-anova(model4)
print(f_test)
```

```
## Analysis of Variance Table
##
## Response: medv
##           Df Sum Sq Mean Sq F value    Pr(>F)
## crim        1  6440.8   6440.8  173.458 < 2.2e-16 ***
## age         1  2809.8   2809.8   75.671 < 2.2e-16 ***
## rm          1 14825.7  14825.7  399.275 < 2.2e-16 ***
## Residuals 502 18640.0     37.1
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

An F-test was utilized to decide if at least one of the predictors is useful in predicting the response.

In this case, all three predictors has a p-value associated with the F-statisic that is  $< 2.2^{-16}$ . Since the p-value is essentially zero, we have strong evidence to reject the null hypothesis, which would be that none of the predictors were useful in predicting the response variable. Thus, at least one of the predictors is useful in predicting the response.

iii)

```
model5 <- lm(medv ~ crim + age, data = Boston)
f_test_2 <- anova(model5)
print(f_test_2)
```

```
## Analysis of Variance Table
##
## Response: medv
##           Df Sum Sq Mean Sq F value    Pr(>F)
## crim       1   6441  6440.8   96.807 < 2.2e-16 ***
## age        1   2810  2809.8   42.232 1.954e-10 ***
## Residuals 503   33466    66.5
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

The p-value associated with F values, though increased for age in this model without the predictor rm, are still significantly lower than the typical significance level of 0.05. Thus the null hypothesis can be rejected for both predictors. We conclude that the model is still useful.

```
new_data <- data.frame(crim = 10, age = 90, rm = 5)
# Predict the response variable using the model for the confidence interval
prediction_c <- predict(model4, newdata = new_data, interval = "confidence", level = 0.99)

# Extract lower and upper bounds from the confidence interval prediction
lower_bound_c <- prediction_c[1]
upper_bound_c <- prediction_c[2]

# Print the results for the confidence interval
cat("Lower bound of 99% confidence interval:", lower_bound_c, "\n")
```

```
## Lower bound of 99% confidence interval: 9.746544
```

```
cat("Upper bound of 99% confidence interval:", upper_bound_c, "\n\n")
```

```
## Upper bound of 99% confidence interval: 8.25632
```

```
# Predict the response variable using the model for the prediction interval
prediction_p <- predict(model4, newdata = new_data, interval = "prediction", level = 0.99)

# Extract lower and upper bounds from the prediction interval prediction
lower_bound_p <- prediction_p[1]
upper_bound_p <- prediction_p[2]

# Print the results for the prediction interval
cat("Lower bound of 99% prediction interval:", lower_bound_p, "\n")
```

```
## Lower bound of 99% prediction interval: 9.746544
```

```
cat("Upper bound of 99% prediction interval:", upper_bound_p, "\n")
```

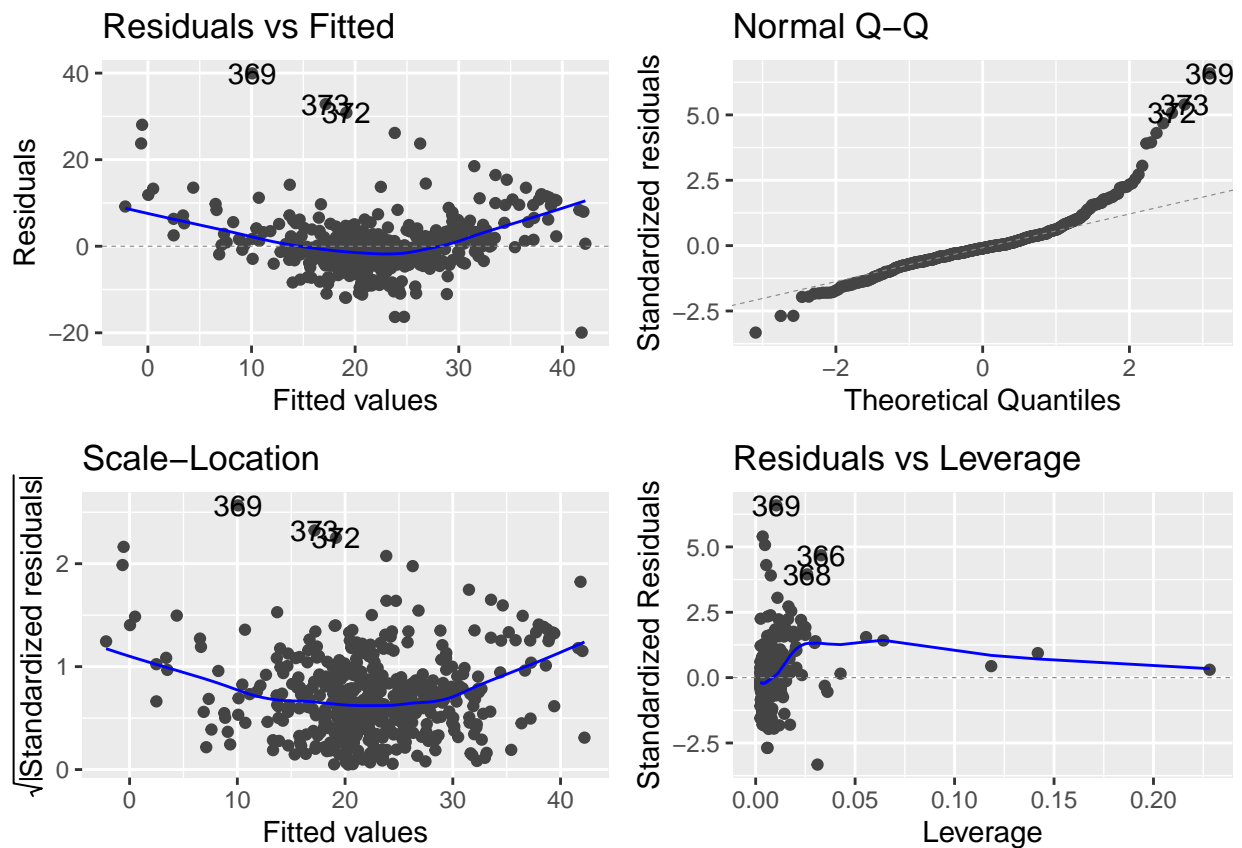
```
## Upper bound of 99% prediction interval: -6.079652
```

iii)

The difference between confidence interval and prediction interval is that the confidence interval estimates the range in which the population mean response most likely will lie, and the prediction interval estimates the range in which a future individual observation most likely will fall within.

iv)

```
# Create diagnostic plots
autoplot(model14, which = c(1, 2, 3, 5))
```



```
## e)
```

i)

The gender is a binary qualitative variable. The student has used two binary variables to describe what only needs one. If two binary qualitative variables were used, it would in fact allow for four different cases:

Case 1: Male and Female	$x_{male} = 1$ and $x_{female} = 1$
Case 2: Male and Not Female	$x_{male} = 1$ and $x_{female} = 0$
Case 3: Not Male and Female	$x_{male} = 0$ and $x_{female} = 1$
Case 4: Not Male and Not Female	$x_{male} = 0$ and $x_{female} = 0$

In reality, there are only two cases:

Case 1: Male (and Not Female)	$x_{gender} = 1$
Case 2: Female (and Not Male)	$x_{gender} = 0$

ii)

The formula should only have one binary quantitative variable to describe the gender.

$$y = \beta_0 + \beta_1 x_{gender} + \varepsilon$$

where

$$x_{gender} = \begin{cases} 1 & \text{if male} \\ 0 & \text{if female} \end{cases}$$

\*\*iii) A formula for a linear model that predicts income based on the predictor education degree with three categories {Bachelor, Master, PhD} is:

$$y = \beta_0 + \beta_1 x_{education} + \varepsilon$$

where

$$x_{education} = \begin{cases} 2 & \text{if PhD} \\ 1 & \text{if Master} \\ 0 & \text{if Bachelor} \end{cases}$$

f)

i) True

ii) False

iii) True

iv) False

### Problem 3

a)

i)



```

data("titanic_train")
vars_to_be_removed <- c("PassengerId", "Name", "Ticket", "Cabin", "Embarked")
titanic_train <- titanic_train[, -which(names(titanic_train) %in% vars_to_be_removed)]
titanic_train$Pclass <- as.factor(titanic_train$Pclass)
train_idx <- sample(1:nrow(titanic_train), 0.8 * nrow(titanic_train))
titanic_test <- titanic_train[-train_idx, ]
titanic_train <- titanic_train[train_idx, ]
titanic_train <- na.omit(titanic_train)
titanic_test <- na.omit(titanic_test)
logReg = glm(Survived ~ Pclass + Sex + Age + SibSp + Parch + Fare, data = titanic_train, family = "binomial")
predicted_probabilities <- predict(logReg, newdata = titanic_test, type = "response")
predicted_labels <- ifelse(predicted_probabilities > 0.5, 1, 0)
actual_labels <- titanic_test$Survived
misclassification_error <- mean(predicted_labels != actual_labels)
accuracy <- 1 - misclassification_error
print(round(accuracy,2))

```

```
## [1] 0.79
```

ii)

```

chitest = anova(logReg,test="Chisq")
chitest

```

```

## Analysis of Deviance Table
##
## Model: binomial, link: logit
##
## Response: Survived
##
## Terms added sequentially (first to last)
##
##
##          Df Deviance Resid. Df Resid. Dev  Pr(>Chi)
## NULL                564      763.63
## Pclass    2    69.483      562    694.15 8.163e-16 ***
## Sex       1   156.007      561    538.14 < 2.2e-16 ***
## Age       1    17.682      560    520.46 2.611e-05 ***
## SibSp     1    10.866      559    509.59 0.0009795 ***
## Parch     1     0.289      558    509.30 0.5911460
## Fare      1     1.074      557    508.23 0.3001461
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

Given that the p value is less than  $2.2 \cdot 10^{-16}$  suggest passenger class is really relevant predictor. In fact it is our strongest predictor.  $H_0$  is that our predictor could just as well be 0, a low p value would break this hypothesis.

iii)

```
newdata = data.frame(Pclass=as.factor(c(1,3)),Sex=c("female","female"),Age=c(40,40),SibSp=c(1,1),Parch=
casepredict = predict(logReg,newdata = newdata,type="response")
casepredict
```

```
##          1          2
## 0.9217204 0.4136693
```

Comparing the a woman with the all the same factors, except for class and fare price, the higher class woman has a 0.92 chance of survival, while the lower class woman has a 0.41 chance of survival.

iv)

```
ldamodel = lda(Survived ~ ., data = titanic_train)
print(ldamodel)
```

```
## Call:
## lda(Survived ~ ., data = titanic_train)
##
## Prior probabilities of groups:
##          0          1
## 0.5929204 0.4070796
##
## Group means:
##      Pclass2  Pclass3  Sexmale      Age      SibSp      Parch      Fare
## 0 0.2119403 0.6238806 0.8417910 30.74328 0.5432836 0.3820896 23.76219
## 1 0.2695652 0.2956522 0.3173913 28.71413 0.5000000 0.5217391 53.21353
##
## Coefficients of linear discriminants:
##              LD1
## Pclass2 -0.789073856
## Pclass3 -1.504574355
## Sexmale -2.068582677
## Age     -0.026553115
## SibSp   -0.251774569
## Parch   -0.086165420
## Fare     0.001778469
```

```
predicted <- predict(ldamodel, newdata = titanic_test)
predicted_labels <- predicted$class
actual_labels <- titanic_test$Survived
misclassification_error = mean(predicted_labels != actual_labels)
accuracy <- 1 - misclassification_error
print(accuracy)
```

```
## [1] 0.7919463
```

v)

```
qdamodel = qda(Survived ~ ., data = titanic_train)
print(qdamodel)
```

```
## Call:
## qda(Survived ~ ., data = titanic_train)
##
## Prior probabilities of groups:
##      0      1
## 0.5929204 0.4070796
##
## Group means:
##      Pclass2  Pclass3  Sexmale      Age      SibSp      Parch      Fare
## 0 0.2119403 0.6238806 0.8417910 30.74328 0.5432836 0.3820896 23.76219
## 1 0.2695652 0.2956522 0.3173913 28.71413 0.5000000 0.5217391 53.21353
```

```
predicted <- predict(qdamodel, newdata = titanic_test)
predicted_labels <- predicted$class
actual_labels <- titanic_test$Survived
misclassification_error = mean(predicted_labels != actual_labels)
accuracy <- 1 - misclassification_error
print(accuracy)
```

```
## [1] 0.7986577
```

vi)

```
logreg_probs <- predict(logReg, newdata = titanic_test, type = "response")
lda_probs <- predict(ldamodel, newdata = titanic_test)$posterior[,2]
qda_probs <- predict(qdamodel, newdata = titanic_test)$posterior[,2]
actual_outcomes <- titanic_test$Survived
```

```
# ROC for Logistic Regression
roc_logreg <- roc(actual_outcomes, logreg_probs)
```

```
## Setting levels: control = 0, case = 1
```

```
## Setting direction: controls < cases
```

```
# ROC for LDA
roc_lda <- roc(actual_outcomes, lda_probs)
```

```
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
```

```

# ROC for QDA
roc_qda <- roc(actual_outcomes, qda_probs)

## Setting levels: control = 0, case = 1
## Setting direction: controls < cases

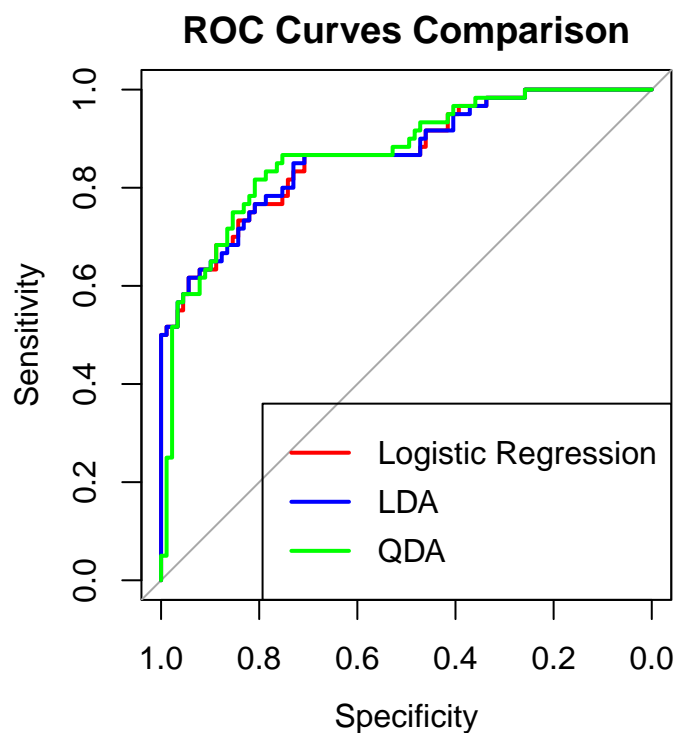
# Plot ROC curve for Logistic Regression
plot(roc_logreg, main="ROC Curves Comparison", col="red", xlim=c(1, 0), ylim=c(0, 1))

# Add ROC curve for LDA
lines(roc_lda, col="blue")

# Add ROC curve for QDA
lines(roc_qda, col="green")

# Add legend
legend("bottomright", legend=c("Logistic Regression", "LDA", "QDA"),
      col=c("red", "blue", "green"), lwd=2)

```



```

# AUC for Logistic Regression
auc_logreg <- roc_logreg$auc

# AUC for LDA
auc_lda <- roc_lda$auc

# AUC for QDA
auc_qda <- roc_qda$auc

```

```
# Print AUC values
cat("AUC for Logistic Regression:", auc_logreg, "\n")
```

```
## AUC for Logistic Regression: 0.8677903
```

```
cat("AUC for LDA:", auc_lda, "\n")
```

```
## AUC for LDA: 0.867603
```

```
cat("AUC for QDA:", auc_qda, "\n")
```

```
## AUC for QDA: 0.8702247
```

AUC over 0.8 is generally considered good. QDA performs slightly better than LDA and Logistic Regression. However Logistic regression is almost as accurate, but more interpretable, for one it gives clearer relationships between the predictors and they are linear.

b)

Diagnostic Paradigm:

The diagnostic paradigm in classification focuses on directly modeling the relationship between the predictors and the outcome (class labels). The primary goal is to diagnose the class of an observation based on its features. Models under this paradigm typically estimate the probability that an observation belongs to a certain class given its features. This approach is more deterministic, where the decision rule is often based on the estimated probabilities and predefined thresholds. Sampling Paradigm:

The sampling paradigm, on the other hand, is based on modeling the distribution of features for each class. It involves estimating how the data is generated or sampled for each class and then uses this information to classify new observations. This approach is more generative, as it tries to understand the underlying data generation process for each class and uses this generative model to make classification decisions.

Key Differences:

**Modeling Focus:** The diagnostic paradigm focuses on the direct relationship between features and classes, often modeling the conditional probability of a class given the features. The sampling paradigm focuses on modeling the distribution of features for each class, effectively capturing how data for each class is generated. **Approach:** Diagnostic models are more discriminative, directly seeking a decision boundary between classes. Sampling models are generative, aiming to understand the data generation process for each class. **Decision Rule:** In the diagnostic paradigm, classification decisions are often made based on estimated probabilities and thresholds. In the sampling paradigm, decisions are made based on likelihoods derived from the modeled distributions of features for each class.

ii)

Classification Models and Their Paradigms

**Logistic Regression:** Belongs to the diagnostic paradigm. It models the probability of a class given the features directly using the logistic function.

**KNN (K-Nearest Neighbors):** Can be seen as part of the sampling paradigm. It classifies an observation based on the majority class among its K nearest neighbors, effectively using the local distribution of the data around an observation to make a classification decision.

Naive Bayes Classifier: Fits within the sampling paradigm. It is a generative model that assumes independence among features given the class and estimates the distribution of each feature within each class to compute the posterior probability of the class given an observation.

LDA (Linear Discriminant Analysis): Primarily fits within the sampling paradigm. LDA models the distribution of features in each class (assuming a Gaussian distribution with a common covariance matrix across classes) and uses this to classify new observations by finding the class that maximizes the posterior probability.

QDA (Quadratic Discriminant Analysis): Also belongs to the sampling paradigm. Similar to LDA, QDA models the distribution of features for each class, but it allows for class-specific covariance matrices, leading to quadratic decision boundaries. Like LDA, it uses the estimated distributions to compute class probabilities for classification.

c)

i)

The decision boundary is given by setting by taking the log of each pdf and adding the log of the prior probability equal each other.

$$\begin{aligned}
 X|Y=1 &\sim N(-2, 1.5^2) \\
 X|Y=2 &\sim N(2, 1.5^2) \\
 \pi_1 &= 0.3 \\
 \pi_2 &= 0.7
 \end{aligned}$$

$$\begin{aligned}
 g_1(x|\pi_1) &= g_2(x|\pi_2) \\
 \log\left(\frac{1}{\sqrt{2\pi}\sigma_1} + e^{-\frac{(x-\mu_1)^2}{2\sigma_1^2}}\right) + \log(\pi_1) &= \log\left(\frac{1}{\sqrt{2\pi}\sigma_2} + e^{-\frac{(x-\mu_2)^2}{2\sigma_2^2}}\right) + \log(\pi_2) \\
 \log\left(\frac{1}{\sqrt{2\pi}1.5} + e^{-\frac{(x+2)^2}{2 \cdot 1.5^2}}\right) + \log(0.3) &= \log\left(\frac{1}{\sqrt{2\pi}1.5} + e^{-\frac{(x-2)^2}{2 \cdot 1.5^2}}\right) + \log(0.7) \\
 \frac{(x-2)^2 - (x+2)^2}{4.5} + \log(0.3) - \log(0.7) &= 0 \\
 \frac{x^2 - 4x + 4 - x^2 - 4x - 4}{4.5} + \log\left(\frac{0.3}{0.7}\right) &= 0 \\
 \frac{-8x}{4.5} - 0.847 &= 0 \\
 x &= -0.477
 \end{aligned}$$

For  $x=-0.47$  is the point where the graphs cross, at this point a model would change its decision of which class our point belongs to.

```

# generate data for the two normal distributions
n_samples_class1 <- 3000
n_samples_class2 <- 7000
x1 <- rnorm(n_samples_class1, mean = -2, sd = 1.5)
x2 <- rnorm(n_samples_class2, mean = 2, sd = 1.5)
# create a data frame with the generated data
df <- data.frame(X1 = c(x1, x2), class = c(rep(1, n_samples_class1), rep(2, n_samples_class2)))

```

## Problem 4

a)

iv)

True

b)

i)

Corrected three mistakes:

- Corrected the number of folds from 4 to 5.
- 
- Corrected the RMSE formula.

```
# Import the Boston housing price dataset
data(Boston)
# select specific variables
selected_vars <- c("crim", "rm", "age", "medv")
boston_selected <- Boston[, selected_vars]

# manually perform the 5-fold cross-validation
folds <- createFolds(boston_selected$medv, k = 5) # CORRECTED to 5
rmse_list <- list()
for (i in 1:length(folds)) {
  # get the training and validation sets
  train <- boston_selected[-folds[[i]], ] # CORRECTED
  val <- boston_selected[folds[[i]], ]
  # fit a linear regression model
  model <- lm(medv ~ ., data = train)
  # compute RMSE on the validation set
  pred <- predict(model, val)
  rmse <- sqrt(mean((pred - val$medv)^2)) # CORRECTED squared error (RSME)
  rmse <- rmse[1] # take out the value
  # store rmse in rmse_list
  rmse_list[[i]] <- rmse
}
# compute mean of rmse_list
rmse_mean <- mean(as.numeric(rmse_list))
cat("rmse_mean:", rmse_mean, "\n")
```

```
## rmse_mean: 6.058381
```

ii)

Changed: `folds <- createFolds(boston_selected$medv, k = 5)` to: `folds <- createFolds(boston_selected$medv, k = nrow(boston_selected))`