

```

feasiblecharpolylist[95, (x + 5) ^ 75 (x - 19) ^ 13]
{ (-19 + x) (-18 + x) (-17 + x)^3 (395 - 40 x + x^2) ,
  (-22 + x) (-19 + x)^2 (-17 + x)^4 , (-19 + x)^2 (-18 + x) (-17 + x)^2 (353 - 38 x + x^2) ,
  (-19 + x) (-17 + x)^3 (-7102 + 1115 x - 58 x^2 + x^3) , (-21 + x)^2 (-18 + x) (-17 + x)^4 ,
  (-19 + x)^2 (-17 + x)^2 (-6350 + 1037 x - 56 x^2 + x^3) ,
  (-19 + x) (-17 + x)^2 (120658 - 26053 x + 2101 x^2 - 75 x^3 + x^4) ,
  (-21 + x) (-19 + x) (-17 + x)^3 (338 - 37 x + x^2) ,
  (-19 + x)^2 (-18 + x) (-17 + x) (-5993 + 999 x - 55 x^2 + x^3) ,
  (-19 + x)^3 (-17 + x)^2 (334 - 37 x + x^2) ,
  (-21 + x) (-19 + x) (-18 + x) (-17 + x)^2 (319 - 36 x + x^2) ,
  (-19 + x)^3 (-17 + x) (-5674 + 963 x - 54 x^2 + x^3) ,
  (-21 + x) (-19 + x)^2 (-17 + x)^2 (302 - 35 x + x^2) ,
  (-19 + x)^2 (-17 + x) (338 - 37 x + x^2) (319 - 36 x + x^2) ,
  (-21 + x) (-19 + x)^3 (-18 + x) (-17 + x) (-15 + x) ,
  (-19 + x)^3 (96398 - 22041 x + 1881 x^2 - 71 x^3 + x^4) ,
  (-19 + x)^2 (-17 + x) (107738 - 23967 x + 1989 x^2 - 73 x^3 + x^4) ,
  (-19 + x)^2 (-18 + x) (319 - 36 x + x^2)^2 , (-19 + x)^3 (-17 + x) (-5666 + 963 x - 54 x^2 + x^3) ,
  (-19 + x)^4 (-15 + x) (338 - 37 x + x^2) , (-19 + x)^3 (319 - 36 x + x^2) (302 - 35 x + x^2) ,
  (-19 + x)^3 (-18 + x) (-5347 + 927 x - 53 x^2 + x^3) ,
  (-19 + x)^4 (-17 + x) (298 - 35 x + x^2) , (-19 + x)^4 (-5062 + 893 x - 52 x^2 + x^3) ,
  (-19 + x)^4 (-18 + x) (281 - 34 x + x^2) , (-19 + x)^6 (-14 + x) }

```

```

dim20list = {(-19 + x)^14 (-18 + x) (-17 + x)^3 (5 + x)^75 (395 - 40 x + x^2),
  (-22 + x) (-19 + x)^15 (-17 + x)^4 (5 + x)^75, (-19 + x)^15 (-18 + x) (-17 + x)^2 (5 + x)^75
  (353 - 38 x + x^2), (-19 + x)^14 (-17 + x)^3 (5 + x)^75 (-7102 + 1115 x - 58 x^2 + x^3),
  (-21 + x)^2 (-19 + x)^13 (-18 + x) (-17 + x)^4 (5 + x)^75,
  (-19 + x)^15 (-17 + x)^2 (5 + x)^75 (-6350 + 1037 x - 56 x^2 + x^3),
  (-19 + x)^14 (-17 + x)^2 (5 + x)^75 (120658 - 26053 x + 2101 x^2 - 75 x^3 + x^4),
  (-21 + x) (-19 + x)^14 (-17 + x)^3 (5 + x)^75 (338 - 37 x + x^2),
  (-19 + x)^15 (-18 + x) (-17 + x) (5 + x)^75 (-5993 + 999 x - 55 x^2 + x^3),
  (-19 + x)^16 (-17 + x)^2 (5 + x)^75 (334 - 37 x + x^2),
  (-21 + x) (-19 + x)^14 (-18 + x) (-17 + x)^2 (5 + x)^75 (319 - 36 x + x^2),
  (-19 + x)^16 (-17 + x) (5 + x)^75 (-5674 + 963 x - 54 x^2 + x^3),
  (-21 + x) (-19 + x)^15 (-17 + x)^2 (5 + x)^75 (302 - 35 x + x^2),
  (-19 + x)^15 (-17 + x) (5 + x)^75 (338 - 37 x + x^2) (319 - 36 x + x^2),
  (-21 + x) (-19 + x)^16 (-18 + x) (-17 + x) (-15 + x) (5 + x)^75,
  (-19 + x)^16 (5 + x)^75 (96398 - 22041 x + 1881 x^2 - 71 x^3 + x^4),
  (-19 + x)^15 (-17 + x) (5 + x)^75 (107738 - 23967 x + 1989 x^2 - 73 x^3 + x^4),
  (-19 + x)^15 (-18 + x) (5 + x)^75 (319 - 36 x + x^2)^2,
  (-19 + x)^16 (-17 + x) (5 + x)^75 (-5666 + 963 x - 54 x^2 + x^3),
  (-19 + x)^17 (-15 + x) (5 + x)^75 (338 - 37 x + x^2),
  (-19 + x)^16 (5 + x)^75 (319 - 36 x + x^2) (302 - 35 x + x^2),
  (-19 + x)^16 (-18 + x) (5 + x)^75 (-5347 + 927 x - 53 x^2 + x^3),
  (-19 + x)^17 (-17 + x) (5 + x)^75 (298 - 35 x + x^2),
  (-19 + x)^17 (5 + x)^75 (-5062 + 893 x - 52 x^2 + x^3),
  (-19 + x)^17 (-18 + x) (5 + x)^75 (281 - 34 x + x^2), (-19 + x)^19 (-14 + x) (5 + x)^75}};

Length[dim20list]

```

26

```

modfilter[dim20list, chiSmod32n95, 32]
{(-22 + x) (-19 + x)^15 (-17 + x)^4 (5 + x)^75,
  (-21 + x)^2 (-19 + x)^13 (-18 + x) (-17 + x)^4 (5 + x)^75,
  (-19 + x)^16 (-17 + x)^2 (5 + x)^75 (334 - 37 x + x^2),
  (-21 + x) (-19 + x)^15 (-17 + x)^2 (5 + x)^75 (302 - 35 x + x^2),
  (-19 + x)^15 (-18 + x) (5 + x)^75 (319 - 36 x + x^2)^2,
  (-19 + x)^17 (-15 + x) (5 + x)^75 (338 - 37 x + x^2),
  (-19 + x)^17 (-17 + x) (5 + x)^75 (298 - 35 x + x^2), (-19 + x)^19 (-14 + x) (5 + x)^75}

dim20listmod32 = {(-22 + x) (-19 + x)^15 (-17 + x)^4 (5 + x)^75, (-21 + x)^2 (-19 + x)^13
  (-18 + x) (-17 + x)^4 (5 + x)^75, (-19 + x)^16 (-17 + x)^2 (5 + x)^75 (334 - 37 x + x^2),
  (-21 + x) (-19 + x)^15 (-17 + x)^2 (5 + x)^75 (302 - 35 x + x^2), (-19 + x)^15 (-18 + x)
  (5 + x)^75 (319 - 36 x + x^2)^2, (-19 + x)^17 (-15 + x) (5 + x)^75 (338 - 37 x + x^2),
  (-19 + x)^17 (-17 + x) (5 + x)^75 (298 - 35 x + x^2), (-19 + x)^19 (-14 + x) (5 + x)^75};

```

```

Length[dim20listmod32]
8

chi = (-21 + x)2 (-19 + x)13 (-18 + x) (-17 + x)4 (5 + x)75
(-21 + x)2 (-19 + x)13 (-18 + x) (-17 + x)4 (5 + x)75

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{89607, -20962, 1824, -70, 1},
 {89471, -20954, 1824, -70, 1}, {89319, -20946, 1824, -70, 1} }

A = {{89607, -20962, 1824, -70, 1},
      {89471, -20954, 1824, -70, 1}, {89319, -20946, 1824, -70, 1}};

A // MatrixForm
{{89607, -20962, 1824, -70, 1},
 {89471, -20954, 1824, -70, 1},
 {89319, -20946, 1824, -70, 1} }

g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{8503665, -1990902, 173280, -6650, 95}

Array[c, 5].Transpose[A]
{89607 c[1] - 20962 c[2] + 1824 c[3] - 70 c[4] + c[5],
 89471 c[1] - 20954 c[2] + 1824 c[3] - 70 c[4] + c[5],
 89319 c[1] - 20946 c[2] + 1824 c[3] - 70 c[4] + c[5]}

Array[c, 5].g
8503665 c[1] - 1990902 c[2] + 173280 c[3] - 6650 c[4] + 95 c[5]

cert = Flatten[Array[c, 5] /.
  FindInstance[8503665 c[1] - 1990902 c[2] + 173280 c[3] - 6650 c[4] + 95 c[5] < 0 &&
    89607 c[1] - 20962 c[2] + 1824 c[3] - 70 c[4] + c[5] ≥ 0 &&
    89471 c[1] - 20954 c[2] + 1824 c[3] - 70 c[4] + c[5] ≥ 0 &&
    89319 c[1] - 20946 c[2] + 1824 c[3] - 70 c[4] + c[5] ≥ 0, Array[c, 5], Integers]]
{49420, 889549, 0, 0, 14218410144}

GCD[49420, 889549, 0, 0, 14218410144]
1

Reverse[cert]
{14218410144, 0, 0, 889549, 49420}

```

```

cert.g
-4 795 218

cert.Transpose[A]
{61946, 457218, 61770}

chi = (-19 + x)^15 (-18 + x) (5 + x)^75 (319 - 36 x + x^2)^2
(-19 + x)^15 (-18 + x) (5 + x)^75 (319 - 36 x + x^2)^2

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{80 069, -19 244, 1722, -68, 1},
 {79 933, -19 236, 1722, -68, 1}, {79 781, -19 228, 1722, -68, 1} }

A = {{80 069, -19 244, 1722, -68, 1},
{79 933, -19 236, 1722, -68, 1}, {79 781, -19 228, 1722, -68, 1}};

A // MatrixForm

$$\begin{pmatrix} 80\ 069 & -19\ 244 & 1722 & -68 & 1 \\ 79\ 933 & -19\ 236 & 1722 & -68 & 1 \\ 79\ 781 & -19\ 228 & 1722 & -68 & 1 \end{pmatrix}$$


g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{7 598 275, -1 827 740, 163 590, -6460, 95}

Array[c, 5].Transpose[A]
{80 069 c[1] - 19 244 c[2] + 1722 c[3] - 68 c[4] + c[5],
 79 933 c[1] - 19 236 c[2] + 1722 c[3] - 68 c[4] + c[5],
 79 781 c[1] - 19 228 c[2] + 1722 c[3] - 68 c[4] + c[5]}

Array[c, 5].g
7 598 275 c[1] - 1 827 740 c[2] + 163 590 c[3] - 6460 c[4] + 95 c[5]

cert = Flatten[Array[c, 5] /.
FindInstance[7 598 275 c[1] - 1 827 740 c[2] + 163 590 c[3] - 6460 c[4] + 95 c[5] < 0 &&
80 069 c[1] - 19 244 c[2] + 1722 c[3] - 68 c[4] + c[5] ≥ 0 &&
79 933 c[1] - 19 236 c[2] + 1722 c[3] - 68 c[4] + c[5] ≥ 0 &&
79 781 c[1] - 19 228 c[2] + 1722 c[3] - 68 c[4] + c[5] ≥ 0, Array[c, 5], Integers]]
{26 657, 479 808, 0, 0, 7 099 110 312}

GCD[26 657, 479 808, 0, 0, 7 099 110 312]
1

```

```

Reverse[cert]
{7 099 110 312, 0, 0, 479 808, 26 657}

cert.g
-1 577 605

cert.Transpose[A]
{84 493, 297 605, 84 205}

chi = (-19 + x)^16 (-17 + x)^2 (5 + x)^75 (334 - 37 x + x^2)
(-19 + x)^16 (-17 + x)^2 (5 + x)^75 (334 - 37 x + x^2)

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{78 897, -19 108, 1718, -68, 1},
 {78 913, -19 108, 1718, -68, 1}, {79 033, -19 116, 1718, -68, 1},
 {78 761, -19 100, 1718, -68, 1}, {78 777, -19 100, 1718, -68, 1},
 {78 793, -19 100, 1718, -68, 1}, {78 625, -19 092, 1718, -68, 1},
 {78 641, -19 092, 1718, -68, 1}, {78 489, -19 084, 1718, -68, 1} }

A = {{79 033, -19 116, 1718, -68, 1},
      {78 897, -19 108, 1718, -68, 1}, {78 913, -19 108, 1718, -68, 1},
      {78 761, -19 100, 1718, -68, 1}, {78 777, -19 100, 1718, -68, 1},
      {78 793, -19 100, 1718, -68, 1}, {78 625, -19 092, 1718, -68, 1},
      {78 641, -19 092, 1718, -68, 1}, {78 489, -19 084, 1718, -68, 1}};

A // MatrixForm

$$\begin{pmatrix} 79\ 033 & -19\ 116 & 1718 & -68 & 1 \\ 78\ 897 & -19\ 108 & 1718 & -68 & 1 \\ 78\ 913 & -19\ 108 & 1718 & -68 & 1 \\ 78\ 761 & -19\ 100 & 1718 & -68 & 1 \\ 78\ 777 & -19\ 100 & 1718 & -68 & 1 \\ 78\ 793 & -19\ 100 & 1718 & -68 & 1 \\ 78\ 625 & -19\ 092 & 1718 & -68 & 1 \\ 78\ 641 & -19\ 092 & 1718 & -68 & 1 \\ 78\ 489 & -19\ 084 & 1718 & -68 & 1 \end{pmatrix}$$


g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{7 513 695, -1 816 316, 163 210, -6460, 95}

```

```

Array[c, 5].Transpose[A]
{79 033 c[1] - 19 116 c[2] + 1718 c[3] - 68 c[4] + c[5], 
 78 897 c[1] - 19 108 c[2] + 1718 c[3] - 68 c[4] + c[5], 
 78 913 c[1] - 19 108 c[2] + 1718 c[3] - 68 c[4] + c[5], 
 78 761 c[1] - 19 100 c[2] + 1718 c[3] - 68 c[4] + c[5], 
 78 777 c[1] - 19 100 c[2] + 1718 c[3] - 68 c[4] + c[5], 
 78 793 c[1] - 19 100 c[2] + 1718 c[3] - 68 c[4] + c[5], 
 78 625 c[1] - 19 092 c[2] + 1718 c[3] - 68 c[4] + c[5], 
 78 641 c[1] - 19 092 c[2] + 1718 c[3] - 68 c[4] + c[5], 
 78 489 c[1] - 19 084 c[2] + 1718 c[3] - 68 c[4] + c[5]}

Array[c, 5].g
7513 695 c[1] - 1816 316 c[2] + 163 210 c[3] - 6460 c[4] + 95 c[5]

cert = Flatten[Array[c, 5] /.
  FindInstance[7513 695 c[1] - 1816 316 c[2] + 163 210 c[3] - 6460 c[4] + 95 c[5] < 0 &&
    79 033 c[1] - 19 116 c[2] + 1718 c[3] - 68 c[4] + c[5] ≥ 0 &&
    78 897 c[1] - 19 108 c[2] + 1718 c[3] - 68 c[4] + c[5] ≥ 0 &&
    78 913 c[1] - 19 108 c[2] + 1718 c[3] - 68 c[4] + c[5] ≥ 0 &&
    78 761 c[1] - 19 100 c[2] + 1718 c[3] - 68 c[4] + c[5] ≥ 0 &&
    78 777 c[1] - 19 100 c[2] + 1718 c[3] - 68 c[4] + c[5] ≥ 0 &&
    78 793 c[1] - 19 100 c[2] + 1718 c[3] - 68 c[4] + c[5] ≥ 0 &&
    78 625 c[1] - 19 092 c[2] + 1718 c[3] - 68 c[4] + c[5] ≥ 0 &&
    78 641 c[1] - 19 092 c[2] + 1718 c[3] - 68 c[4] + c[5] ≥ 0 &&
    78 489 c[1] - 19 084 c[2] + 1718 c[3] - 68 c[4] + c[5] ≥ 0, Array[c, 5], Integers]]
{-2190, -9058, 0, 0, 0}

GCD[-2190, -9058, 0, 0, 0]
2

cert = cert / 2
{-1095, -4529, 0, 0, 0}

Reverse[cert]
{0, 0, 0, -4529, -1095}

cert.g
-1 400 861

cert.Transpose[A]
{35 229, 147 917, 130 397, 260 605, 243 085, 225 565, 373 293, 355 773, 485 981}

```

```

chi = (-21 + x) (-19 + x)15 (-17 + x)2 (5 + x)75 (302 - 35 x + x2)
(-21 + x) (-19 + x)15 (-17 + x)2 (5 + x)75 (302 - 35 x + x2)

CoefficientList[feasibleinterlacingpolylist[chi], x]

{{-1501899, 442253, -51758, 3010, -87, 1},
 {-1499043, 441949, -51750, 3010, -87, 1},
 {-1499347, 441965, -51750, 3010, -87, 1},
 {-1499651, 441981, -51750, 3010, -87, 1},
 {-1496459, 441661, -51742, 3010, -87, 1},
 {-1496763, 441677, -51742, 3010, -87, 1},
 {-1497067, 441693, -51742, 3010, -87, 1},
 {-1493875, 441373, -51734, 3010, -87, 1},
 {-1494179, 441389, -51734, 3010, -87, 1},
 {-1491291, 441085, -51726, 3010, -87, 1} }

A = {{-1501899, 442253, -51758, 3010, -87, 1},
 {-1499043, 441949, -51750, 3010, -87, 1}, {-1499347, 441965,
 -51750, 3010, -87, 1}, {-1499651, 441981, -51750, 3010, -87, 1},
 {-1496459, 441661, -51742, 3010, -87, 1}, {-1496763, 441677,
 -51742, 3010, -87, 1}, {-1497067, 441693, -51742, 3010, -87, 1},
 {-1493875, 441373, -51734, 3010, -87, 1}, {-1494179, 441389,
 -51734, 3010, -87, 1}, {-1491291, 441085, -51726, 3010, -87, 1}};

A // MatrixForm

{{-1501899, 442253, -51758, 3010, -87, 1},
 {-1499043, 441949, -51750, 3010, -87, 1},
 {-1499347, 441965, -51750, 3010, -87, 1},
 {-1499651, 441981, -51750, 3010, -87, 1},
 {-1496459, 441661, -51742, 3010, -87, 1},
 {-1496763, 441677, -51742, 3010, -87, 1},
 {-1497067, 441693, -51742, 3010, -87, 1},
 {-1493875, 441373, -51734, 3010, -87, 1},
 {-1494179, 441389, -51734, 3010, -87, 1},
 {-1491291, 441085, -51726, 3010, -87, 1} }

g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{-142669165, 42012067, -4916938, 285950, -8265, 95}

```

```

Array[c, 6].Transpose[A]
{-1501899 c[1] + 442253 c[2] - 51758 c[3] + 3010 c[4] - 87 c[5] + c[6],
 -1499043 c[1] + 441949 c[2] - 51750 c[3] + 3010 c[4] - 87 c[5] + c[6],
 -1499347 c[1] + 441965 c[2] - 51750 c[3] + 3010 c[4] - 87 c[5] + c[6],
 -1499651 c[1] + 441981 c[2] - 51750 c[3] + 3010 c[4] - 87 c[5] + c[6],
 -1496459 c[1] + 441661 c[2] - 51742 c[3] + 3010 c[4] - 87 c[5] + c[6],
 -1496763 c[1] + 441677 c[2] - 51742 c[3] + 3010 c[4] - 87 c[5] + c[6],
 -1497067 c[1] + 441693 c[2] - 51742 c[3] + 3010 c[4] - 87 c[5] + c[6],
 -1493875 c[1] + 441373 c[2] - 51734 c[3] + 3010 c[4] - 87 c[5] + c[6],
 -1494179 c[1] + 441389 c[2] - 51734 c[3] + 3010 c[4] - 87 c[5] + c[6],
 -1491291 c[1] + 441085 c[2] - 51726 c[3] + 3010 c[4] - 87 c[5] + c[6]}

Array[c, 6].g
-142669165 c[1] + 42012067 c[2] - 4916938 c[3] + 285950 c[4] - 8265 c[5] + 95 c[6]

cert = Flatten[
Array[c, 6] /. FindInstance[-142669165 c[1] + 42012067 c[2] - 4916938 c[3] +
285950 c[4] - 8265 c[5] + 95 c[6] < 0 &&
-1501899 c[1] + 442253 c[2] - 51758 c[3] + 3010 c[4] - 87 c[5] + c[6] ≥ 0 &&
-1499043 c[1] + 441949 c[2] - 51750 c[3] + 3010 c[4] - 87 c[5] + c[6] ≥ 0 &&
-1499347 c[1] + 441965 c[2] - 51750 c[3] + 3010 c[4] - 87 c[5] + c[6] ≥ 0 &&
-1499651 c[1] + 441981 c[2] - 51750 c[3] + 3010 c[4] - 87 c[5] + c[6] ≥ 0 &&
-1496459 c[1] + 441661 c[2] - 51742 c[3] + 3010 c[4] - 87 c[5] + c[6] ≥ 0 &&
-1496763 c[1] + 441677 c[2] - 51742 c[3] + 3010 c[4] - 87 c[5] + c[6] ≥ 0 &&
-1497067 c[1] + 441693 c[2] - 51742 c[3] + 3010 c[4] - 87 c[5] + c[6] ≥ 0 &&
-1493875 c[1] + 441373 c[2] - 51734 c[3] + 3010 c[4] - 87 c[5] + c[6] ≥ 0 &&
-1494179 c[1] + 441389 c[2] - 51734 c[3] + 3010 c[4] - 87 c[5] + c[6] ≥ 0 &&
-1491291 c[1] + 441085 c[2] - 51726 c[3] + 3010 c[4] - 87 c[5] + c[6] ≥ 0,
Array[c, 6], Integers]]
{44780, 443285, 2488265, 0, 0, 0}

GCD[44780, 443285, 2488265, 0, 0, 0]
5

cert = cert / 5
{8956, 88657, 497653, 0, 0, 0}

Reverse[cert]
{0, 0, 0, 497653, 88657, 8956}

cert.g
-10164235

cert.Transpose[A]
{292803, 2900635, 1596523, 292411, 4490947,
 3186835, 1882723, 6081259, 4777147, 7671571}

```

```

chi = (-19 + x)17 (-15 + x) (5 + x)75 (338 - 37 x + x2)
(-19 + x)17 (-15 + x) (5 + x)75 (338 - 37 x + x2)

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{70635, -17534, 1620, -66, 1},
 {70499, -17526, 1620, -66, 1}, {70515, -17526, 1620, -66, 1},
 {70363, -17518, 1620, -66, 1}, {70379, -17518, 1620, -66, 1},
 {70395, -17518, 1620, -66, 1}, {70243, -17510, 1620, -66, 1}};

A = {{70635, -17534, 1620, -66, 1},
 {70499, -17526, 1620, -66, 1}, {70515, -17526, 1620, -66, 1},
 {70363, -17518, 1620, -66, 1}, {70379, -17518, 1620, -66, 1},
 {70395, -17518, 1620, -66, 1}, {70243, -17510, 1620, -66, 1}};

A // MatrixForm
( 70635 -17534 1620 -66 1
 70499 -17526 1620 -66 1
 70515 -17526 1620 -66 1
 70363 -17518 1620 -66 1
 70379 -17518 1620 -66 1
 70395 -17518 1620 -66 1
 70243 -17510 1620 -66 1)

g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{6708965, -1665682, 153900, -6270, 95}

Array[c, 5].Transpose[A]
{70635 c[1] - 17534 c[2] + 1620 c[3] - 66 c[4] + c[5],
 70499 c[1] - 17526 c[2] + 1620 c[3] - 66 c[4] + c[5],
 70515 c[1] - 17526 c[2] + 1620 c[3] - 66 c[4] + c[5],
 70363 c[1] - 17518 c[2] + 1620 c[3] - 66 c[4] + c[5],
 70379 c[1] - 17518 c[2] + 1620 c[3] - 66 c[4] + c[5],
 70395 c[1] - 17518 c[2] + 1620 c[3] - 66 c[4] + c[5],
 70243 c[1] - 17510 c[2] + 1620 c[3] - 66 c[4] + c[5]}

Array[c, 5].g
6708965 c[1] - 1665682 c[2] + 153900 c[3] - 6270 c[4] + 95 c[5]

```

```

cert = Flatten[Array[c, 5] /.
  FindInstance[6 708 965 c[1] - 1 665 682 c[2] + 153 900 c[3] - 6270 c[4] + 95 c[5] < 0 &&
  70 635 c[1] - 17 534 c[2] + 1620 c[3] - 66 c[4] + c[5] ≥ 0 &&
  70 499 c[1] - 17 526 c[2] + 1620 c[3] - 66 c[4] + c[5] ≥ 0 &&
  70 515 c[1] - 17 526 c[2] + 1620 c[3] - 66 c[4] + c[5] ≥ 0 &&
  70 363 c[1] - 17 518 c[2] + 1620 c[3] - 66 c[4] + c[5] ≥ 0 &&
  70 379 c[1] - 17 518 c[2] + 1620 c[3] - 66 c[4] + c[5] ≥ 0 &&
  70 395 c[1] - 17 518 c[2] + 1620 c[3] - 66 c[4] + c[5] ≥ 0 &&
  70 243 c[1] - 17 510 c[2] + 1620 c[3] - 66 c[4] + c[5] ≥ 0, Array[c, 5], Integers]]
{15 690, 266 716, 0, 0, 3 568 395 060}

GCD[15 690, 266 716, 0, 0, 3 568 395 060]
2

cert = cert / 2
{7845, 133 358, 0, 0, 1 784 197 530}

Reverse[cert]
{1 784 197 530, 0, 0, 133 358, 7845}

cert.g
-1 424 381

cert.Transpose[A]
{29 933, 29 877, 155 397, 29 821, 155 341, 280 861, 155 285}

```

$$\chi_i = (-19 + x)^{17} (-17 + x) (5 + x)^{75} (298 - 35 x + x^2)$$

$$(-19 + x)^{17} (-17 + x) (5 + x)^{75} (298 - 35 x + x^2)$$

```

CoefficientList[feasibleinterlacingpolylis[chi], x]
{{70 499, -17 526, 1620, -66, 1}, {70 515, -17 526, 1620, -66, 1},
 {70 363, -17 518, 1620, -66, 1}, {70 379, -17 518, 1620, -66, 1},
 {70 395, -17 518, 1620, -66, 1}, {70 227, -17 510, 1620, -66, 1},
 {70 243, -17 510, 1620, -66, 1}, {70 091, -17 502, 1620, -66, 1}};

A = {{70 499, -17 526, 1620, -66, 1}, {70 515, -17 526, 1620, -66, 1},
 {70 363, -17 518, 1620, -66, 1}, {70 379, -17 518, 1620, -66, 1},
 {70 395, -17 518, 1620, -66, 1}, {70 227, -17 510, 1620, -66, 1},
 {70 243, -17 510, 1620, -66, 1}, {70 091, -17 502, 1620, -66, 1}};

```

```

A // MatrixForm

$$\begin{pmatrix} 70499 & -17526 & 1620 & -66 & 1 \\ 70515 & -17526 & 1620 & -66 & 1 \\ 70363 & -17518 & 1620 & -66 & 1 \\ 70379 & -17518 & 1620 & -66 & 1 \\ 70395 & -17518 & 1620 & -66 & 1 \\ 70227 & -17510 & 1620 & -66 & 1 \\ 70243 & -17510 & 1620 & -66 & 1 \\ 70091 & -17502 & 1620 & -66 & 1 \end{pmatrix}$$


g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{6703605, -1665314, 153900, -6270, 95}

Array[c, 5].Transpose[A]
{70499 c[1] - 17526 c[2] + 1620 c[3] - 66 c[4] + c[5],
 70515 c[1] - 17526 c[2] + 1620 c[3] - 66 c[4] + c[5],
 70363 c[1] - 17518 c[2] + 1620 c[3] - 66 c[4] + c[5],
 70379 c[1] - 17518 c[2] + 1620 c[3] - 66 c[4] + c[5],
 70395 c[1] - 17518 c[2] + 1620 c[3] - 66 c[4] + c[5],
 70227 c[1] - 17510 c[2] + 1620 c[3] - 66 c[4] + c[5],
 70243 c[1] - 17510 c[2] + 1620 c[3] - 66 c[4] + c[5],
 70091 c[1] - 17502 c[2] + 1620 c[3] - 66 c[4] + c[5]}

Array[c, 5].g
6703605 c[1] - 1665314 c[2] + 153900 c[3] - 6270 c[4] + 95 c[5]

cert = Flatten[Array[c, 5] /.
  FindInstance[6703605 c[1] - 1665314 c[2] + 153900 c[3] - 6270 c[4] + 95 c[5] < 0 &&
    70499 c[1] - 17526 c[2] + 1620 c[3] - 66 c[4] + c[5] ≥ 0 &&
    70515 c[1] - 17526 c[2] + 1620 c[3] - 66 c[4] + c[5] ≥ 0 &&
    70363 c[1] - 17518 c[2] + 1620 c[3] - 66 c[4] + c[5] ≥ 0 &&
    70379 c[1] - 17518 c[2] + 1620 c[3] - 66 c[4] + c[5] ≥ 0 &&
    70395 c[1] - 17518 c[2] + 1620 c[3] - 66 c[4] + c[5] ≥ 0 &&
    70227 c[1] - 17510 c[2] + 1620 c[3] - 66 c[4] + c[5] ≥ 0 &&
    70243 c[1] - 17510 c[2] + 1620 c[3] - 66 c[4] + c[5] ≥ 0 &&
    70091 c[1] - 17502 c[2] + 1620 c[3] - 66 c[4] + c[5] ≥ 0, Array[c, 5], Integers]]
{-2587, -10412, 0, 0, 0}

GCD[-2587, -10412, 0, 0, 0]
1

Reverse[cert]
{0, 0, 0, -10412, -2587}

cert.g
-2976767

cert.Transpose[A]
{99799, 58407, 368335, 326943, 285551, 636871, 595479, 905407}

```

```

chi = (-22 + x) (-19 + x)15 (-17 + x)4 (5 + x)75
(-22 + x) (-19 + x)15 (-17 + x)4 (5 + x)75

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{{-5187, 919, -53, 1}, {-5195, 919, -53, 1},
  {-5203, 919, -53, 1}, {-5211, 919, -53, 1}}}

A = {{-5211, 919, -53, 1}, {-5203, 919, -53, 1},
      {-5195, 919, -53, 1}, {-5187, 919, -53, 1}};

A // MatrixForm

$$\begin{pmatrix} -5211 & 919 & -53 & 1 \\ -5203 & 919 & -53 & 1 \\ -5195 & 919 & -53 & 1 \\ -5187 & 919 & -53 & 1 \end{pmatrix}$$


g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{-494925, 87305, -5035, 95}

FindInstance[n[1] ≥ 0 && n[2] ≥ 0 && n[3] ≥ 0 && n[4] ≥ 0 && Array[n, 4].A == g,
  Array[n, 4], Integers]
{{n[1] → 88, n[2] → 0, n[3] → 6, n[4] → 1} }

Array[c, 4].Transpose[A]
{-5211 c[1] + 919 c[2] - 53 c[3] + c[4], -5203 c[1] + 919 c[2] - 53 c[3] + c[4],
 -5195 c[1] + 919 c[2] - 53 c[3] + c[4], -5187 c[1] + 919 c[2] - 53 c[3] + c[4]}

Array[c, 4].g
-494925 c[1] + 87305 c[2] - 5035 c[3] + 95 c[4]

warrant = Flatten[
  Array[c, 4] /. FindInstance[-494925 c[1] + 87305 c[2] - 5035 c[3] + 95 c[4] < 0 &&
    -5211 c[1] + 919 c[2] - 53 c[3] + c[4] < 0 && -5203 c[1] + 919 c[2] - 53 c[3] + c[4] ≥
    0 && -5195 c[1] + 919 c[2] - 53 c[3] + c[4] ≥ 0 &&
    -5187 c[1] + 919 c[2] - 53 c[3] + c[4] ≥ 0, Array[c, 4], Integers]]
{917, 0, 0, 4776043}

GCD[917, 0, 0, 4776043]
1

Reverse[warrant]
{4776043, 0, 0, 917}

```

```
warrant.g
```

```
- 122 140
```

```
warrant.Transpose[A]
```

```
{ - 2444, 4892, 12 228, 19 564 }
```

$$\text{chiwarrant} = (-19 + x)^{14} (-17 + x)^3 (5 + x)^{74} (-5211 + 919 x - 53 x^2 + x^3) \\ (-19 + x)^{14} (-17 + x)^3 (5 + x)^{74} (-5211 + 919 x - 53 x^2 + x^3)$$

```
list = feasibleinterlacingpolylist[chiwarrant]
```

$$\begin{aligned} & \{ (236 - 31 x + x^2) (-5211 + 919 x - 53 x^2 + x^3), \\ & (-17 + x) (72 340 - 18 005 x + 1659 x^2 - 67 x^3 + x^4), \\ & (-17 + x) (72 256 - 18 001 x + 1659 x^2 - 67 x^3 + x^4), \\ & (-17 + x) (72 264 - 18 001 x + 1659 x^2 - 67 x^3 + x^4), \\ & - 1228 640 + 378 289 x - 46 204 x^2 + 2798 x^3 - 84 x^4 + x^5, \\ & (-17 + x) (72 272 - 18 001 x + 1659 x^2 - 67 x^3 + x^4), \\ & - 1228 776 + 378 297 x - 46 204 x^2 + 2798 x^3 - 84 x^4 + x^5, \\ & (-17 + x) (-13 + x) (-5560 + 957 x - 54 x^2 + x^3), (-17 + x) (288 - 35 x + x^2) (251 - 32 x + x^2), \\ & (-17 + x) (72 172 - 17 997 x + 1659 x^2 - 67 x^3 + x^4), \\ & (-17 + x) (-15 + x) (-4812 + 879 x - 52 x^2 + x^3), \\ & (-17 + x) (72 188 - 17 997 x + 1659 x^2 - 67 x^3 + x^4), \\ & (-17 + x) (72 196 - 17 997 x + 1659 x^2 - 67 x^3 + x^4), \\ & - 1227 484 + 378 153 x - 46 200 x^2 + 2798 x^3 - 84 x^4 + x^5, \\ & (-17 + x) (72 204 - 17 997 x + 1659 x^2 - 67 x^3 + x^4), \\ & - 1227 620 + 378 161 x - 46 200 x^2 + 2798 x^3 - 84 x^4 + x^5, \\ & (-17 + x) (72 212 - 17 997 x + 1659 x^2 - 67 x^3 + x^4), \\ & - 1227 756 + 378 169 x - 46 200 x^2 + 2798 x^3 - 84 x^4 + x^5, \\ & (-17 + x) (72 220 - 17 997 x + 1659 x^2 - 67 x^3 + x^4), \\ & (251 - 32 x + x^2) (-4892 + 883 x - 52 x^2 + x^3), \\ & (-17 + x) (-13 + x) (-5556 + 957 x - 54 x^2 + x^3), \\ & (-17 + x) (72 104 - 17 993 x + 1659 x^2 - 67 x^3 + x^4), \\ & (-17 + x) (72 112 - 17 993 x + 1659 x^2 - 67 x^3 + x^4), \\ & (-17 + x) (-15 + x) (-4808 + 879 x - 52 x^2 + x^3), \\ & (-17 + x) (72 128 - 17 993 x + 1659 x^2 - 67 x^3 + x^4), \\ & - 1226 328 + 378 017 x - 46 196 x^2 + 2798 x^3 - 84 x^4 + x^5, \\ & (-17 + x) (72 136 - 17 993 x + 1659 x^2 - 67 x^3 + x^4), \\ & - 1226 464 + 378 025 x - 46 196 x^2 + 2798 x^3 - 84 x^4 + x^5, \\ & (-17 + x) (72 144 - 17 993 x + 1659 x^2 - 67 x^3 + x^4), \\ & - 1226 600 + 378 033 x - 46 196 x^2 + 2798 x^3 - 84 x^4 + x^5, \\ & (-17 + x) (311 - 36 x + x^2) (232 - 31 x + x^2), \\ & - 1226 736 + 378 041 x - 46 196 x^2 + 2798 x^3 - 84 x^4 + x^5, \end{aligned}$$

$$\begin{aligned}
& (-17 + x) (72160 - 17993x + 1659x^2 - 67x^3 + x^4), \\
& (-13 + x) (376 - 39x + x^2) (251 - 32x + x^2), \\
& -1226872 + 378049x - 46196x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17 + x) (72168 - 17993x + 1659x^2 - 67x^3 + x^4), \\
& -1227008 + 378057x - 46196x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17 + x) (-13 + x) (-5552 + 957x - 54x^2 + x^3), \\
& (-17 + x) (72028 - 17989x + 1659x^2 - 67x^3 + x^4), \\
& (-17 + x) (72036 - 17989x + 1659x^2 - 67x^3 + x^4), \\
& (-17 + x) (332 - 37x + x^2) (217 - 30x + x^2), \\
& (-17 + x) (72052 - 17989x + 1659x^2 - 67x^3 + x^4), \\
& (-17 + x) (-15 + x) (-4804 + 879x - 52x^2 + x^3), \\
& -1225172 + 377881x - 46192x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17 + x) (72068 - 17989x + 1659x^2 - 67x^3 + x^4), \\
& -1225308 + 377889x - 46192x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17 + x) (72076 - 17989x + 1659x^2 - 67x^3 + x^4), \\
& -1225444 + 377897x - 46192x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17 + x) (72084 - 17989x + 1659x^2 - 67x^3 + x^4), \\
& -1225580 + 377905x - 46192x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17 + x) (269 - 34x + x^2) (268 - 33x + x^2), \\
& -1225732 + 377913x - 46192x^2 + 2798x^3 - 84x^4 + x^5, \\
& -1225716 + 377913x - 46192x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17 + x) (72100 - 17989x + 1659x^2 - 67x^3 + x^4), \\
& -1225868 + 377921x - 46192x^2 + 2798x^3 - 84x^4 + x^5, \\
& -1225852 + 377921x - 46192x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17 + x) (72108 - 17989x + 1659x^2 - 67x^3 + x^4), \\
& (-13 + x) (94308 - 21817x + 1875x^2 - 71x^3 + x^4), \\
& -1225988 + 377929x - 46192x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17 + x) (72116 - 17989x + 1659x^2 - 67x^3 + x^4), \\
& (-19 + x) (-17 + x) (-13 + x) (292 - 35x + x^2), \\
& (-17 + x) (71960 - 17985x + 1659x^2 - 67x^3 + x^4), \\
& (-17 + x) (71968 - 17985x + 1659x^2 - 67x^3 + x^4), \\
& (-17 + x) (71976 - 17985x + 1659x^2 - 67x^3 + x^4), \\
& (-17 + x) (71984 - 17985x + 1659x^2 - 67x^3 + x^4), \\
& (-15 + x) (376 - 39x + x^2) (217 - 30x + x^2), \\
& (-17 + x) (71992 - 17985x + 1659x^2 - 67x^3 + x^4), \\
& -1224016 + 377745x - 46188x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17 + x) (-15 + x) (-4800 + 879x - 52x^2 + x^3), \\
& -1224152 + 377753x - 46188x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17 + x) (72008 - 17985x + 1659x^2 - 67x^3 + x^4), \\
& -1224288 + 377761x - 46188x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17 + x) (72016 - 17985x + 1659x^2 - 67x^3 + x^4), \\
& -1224440 + 377769x - 46188x^2 + 2798x^3 - 84x^4 + x^5, \\
& -1224424 + 377769x - 46188x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17 + x) (72024 - 17985x + 1659x^2 - 67x^3 + x^4),
\end{aligned}$$

$$\begin{aligned}
& -1224576 + 377777x - 46188x^2 + 2798x^3 - 84x^4 + x^5, \\
& -1224560 + 377777x - 46188x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17+x) (72032 - 17985x + 1659x^2 - 67x^3 + x^4), \\
& -1224712 + 377785x - 46188x^2 + 2798x^3 - 84x^4 + x^5, \\
& -1224696 + 377785x - 46188x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17+x) (72040 - 17985x + 1659x^2 - 67x^3 + x^4), \\
& -1224848 + 377793x - 46188x^2 + 2798x^3 - 84x^4 + x^5, \\
& -1224832 + 377793x - 46188x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-19+x) (-17+x) (-3792 + 747x - 48x^2 + x^3), \\
& -1224984 + 377801x - 46188x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-19+x) (64472 - 16491x + 1563x^2 - 65x^3 + x^4), \\
& (-17+x) (71892 - 17981x + 1659x^2 - 67x^3 + x^4), \\
& (-17+x) (71900 - 17981x + 1659x^2 - 67x^3 + x^4), \\
& (-17+x) (71908 - 17981x + 1659x^2 - 67x^3 + x^4), \\
& (-17+x) (-12+x) (-5993 + 999x - 55x^2 + x^3), \\
& -1222724 + 377601x - 46184x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17+x) (71924 - 17981x + 1659x^2 - 67x^3 + x^4), \\
& (-15+x) (81524 - 19739x + 1763x^2 - 69x^3 + x^4), \\
& (-17+x) (71932 - 17981x + 1659x^2 - 67x^3 + x^4), \\
& -1222996 + 377617x - 46184x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17+x) (-15+x) (-4796 + 879x - 52x^2 + x^3), \\
& -1223132 + 377625x - 46184x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17+x) (71948 - 17981x + 1659x^2 - 67x^3 + x^4), \\
& -1223284 + 377633x - 46184x^2 + 2798x^3 - 84x^4 + x^5, \\
& -1223268 + 377633x - 46184x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17+x) (71956 - 17981x + 1659x^2 - 67x^3 + x^4), \\
& (268 - 33x + x^2) (-4565 + 847x - 51x^2 + x^3), \\
& -1223404 + 377641x - 46184x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17+x) (71964 - 17981x + 1659x^2 - 67x^3 + x^4), \\
& -1223556 + 377649x - 46184x^2 + 2798x^3 - 84x^4 + x^5, \\
& -1223540 + 377649x - 46184x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-19+x) (-17+x) (-3788 + 747x - 48x^2 + x^3), \\
& -1223692 + 377657x - 46184x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-19+x) (64404 - 16487x + 1563x^2 - 65x^3 + x^4), \\
& -1223844 + 377665x - 46184x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-19+x) (64412 - 16487x + 1563x^2 - 65x^3 + x^4), \\
& (-19+x) (64420 - 16487x + 1563x^2 - 65x^3 + x^4), \\
& (-17+x) (-16+x) (-4489 + 843x - 51x^2 + x^3), \\
& (-17+x) (71832 - 17977x + 1659x^2 - 67x^3 + x^4), \\
& (-17+x) (71840 - 17977x + 1659x^2 - 67x^3 + x^4), \\
& (-17+x) (71848 - 17977x + 1659x^2 - 67x^3 + x^4), \\
& -1221568 + 377465x - 46180x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17+x) (71856 - 17977x + 1659x^2 - 67x^3 + x^4), \\
& -1221704 + 377473x - 46180x^2 + 2798x^3 - 84x^4 + x^5,
\end{aligned}$$

$$\begin{aligned}
& (-17 + x) (71864 - 17977x + 1659x^2 - 67x^3 + x^4), \\
& (-15 + x) (81456 - 19735x + 1763x^2 - 69x^3 + x^4), \\
& (-17 + x) (71872 - 17977x + 1659x^2 - 67x^3 + x^4), \\
& -1221976 + 377489x - 46180x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17 + x) (-15 + x) (-4792 + 879x - 52x^2 + x^3), \\
& -1222128 + 377497x - 46180x^2 + 2798x^3 - 84x^4 + x^5, \\
& -1222112 + 377497x - 46180x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17 + x) (71888 - 17977x + 1659x^2 - 67x^3 + x^4), \\
& -1222264 + 377505x - 46180x^2 + 2798x^3 - 84x^4 + x^5, \\
& -1222248 + 377505x - 46180x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-19 + x) (-17 + x) (-3784 + 747x - 48x^2 + x^3), \\
& -1222400 + 377513x - 46180x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-19 + x) (64336 - 16483x + 1563x^2 - 65x^3 + x^4), \\
& (-21 + x) (-19 + x) (-3064 + 639x - 44x^2 + x^3), \\
& (-19 + x) (64352 - 16483x + 1563x^2 - 65x^3 + x^4), \\
& (-17 + x) (71748 - 17973x + 1659x^2 - 67x^3 + x^4), \\
& (-17 + x) (71756 - 17973x + 1659x^2 - 67x^3 + x^4), \\
& (-17 + x) (71764 - 17973x + 1659x^2 - 67x^3 + x^4), \\
& (-17 + x) (71772 - 17973x + 1659x^2 - 67x^3 + x^4), \\
& (-17 + x) (71780 - 17973x + 1659x^2 - 67x^3 + x^4), \\
& -1220412 + 377329x - 46176x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17 + x) (71788 - 17973x + 1659x^2 - 67x^3 + x^4), \\
& -1220548 + 377337x - 46176x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17 + x) (71796 - 17973x + 1659x^2 - 67x^3 + x^4), \\
& -1220684 + 377345x - 46176x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17 + x) (71804 - 17973x + 1659x^2 - 67x^3 + x^4), \\
& (-15 + x) (81388 - 19731x + 1763x^2 - 69x^3 + x^4), \\
& (-17 + x) (71812 - 17973x + 1659x^2 - 67x^3 + x^4), \\
& -1220972 + 377361x - 46176x^2 + 2798x^3 - 84x^4 + x^5, \\
& -1220956 + 377361x - 46176x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-21 + x) (-19 + x) (-17 + x) (-15 + x) (-12 + x), \\
& (-21 + x) (58148 - 15201x + 1475x^2 - 63x^3 + x^4), \\
& (-19 + x) (64268 - 16479x + 1563x^2 - 65x^3 + x^4), \\
& (-19 + x) (64276 - 16479x + 1563x^2 - 65x^3 + x^4), \\
& (-17 + x) (71680 - 17969x + 1659x^2 - 67x^3 + x^4), \\
& (-17 + x) (71688 - 17969x + 1659x^2 - 67x^3 + x^4), \\
& (-17 + x) (-16 + x) (-4481 + 843x - 51x^2 + x^3), \\
& (-17 + x) (71704 - 17969x + 1659x^2 - 67x^3 + x^4), \\
& -1219120 + 377185x - 46172x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17 + x) (71712 - 17969x + 1659x^2 - 67x^3 + x^4), \\
& -1219256 + 377193x - 46172x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17 + x) (71720 - 17969x + 1659x^2 - 67x^3 + x^4), \\
& -1219392 + 377201x - 46172x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17 + x) (71728 - 17969x + 1659x^2 - 67x^3 + x^4),
\end{aligned}$$

$$\begin{aligned}
& -1219528 + 377209x - 46172x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-21+x)(-17+x)(-3416+693x-46x^2+x^3), \\
& -1219664 + 377217x - 46172x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-19+x)(-17+x)(-3776+747x-48x^2+x^3), \\
& -1219816 + 377225x - 46172x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-19+x)(-15+x)(-4280+813x-50x^2+x^3), \\
& (-19+x)(64208-16475x+1563x^2-65x^3+x^4), \\
& (-17+x)(71612-17965x+1659x^2-67x^3+x^4), \\
& (-17+x)(71620-17965x+1659x^2-67x^3+x^4), \\
& (-17+x)(71628-17965x+1659x^2-67x^3+x^4), \\
& (-17+x)(71636-17965x+1659x^2-67x^3+x^4), \\
& -1217964 + 377049x - 46168x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17+x)(71644-17965x+1659x^2-67x^3+x^4), \\
& -1218100 + 377057x - 46168x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-21+x)(-17+x)(-3412+693x-46x^2+x^3), \\
& -1218236 + 377065x - 46168x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17+x)(71660-17965x+1659x^2-67x^3+x^4), \\
& -1218372 + 377073x - 46168x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-19+x)(-17+x)(-3772+747x-48x^2+x^3), \\
& -1218524 + 377081x - 46168x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-19+x)(64132-16471x+1563x^2-65x^3+x^4), \\
& (-19+x)(-15+x)(-4276+813x-50x^2+x^3), \\
& (-17+x)(71544-17961x+1659x^2-67x^3+x^4), \\
& (-17+x)(71552-17961x+1659x^2-67x^3+x^4), \\
& (-17+x)(71560-17961x+1659x^2-67x^3+x^4), \\
& (-21+x)(-17+x)(-16+x)(213-30x+x^2), \\
& -1216808 + 376913x - 46164x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17+x)(71576-17961x+1659x^2-67x^3+x^4), \\
& -1216944 + 376921x - 46164x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17+x)(71584-17961x+1659x^2-67x^3+x^4), \\
& -1217080 + 376929x - 46164x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-19+x)(-17+x)(-3768+747x-48x^2+x^3), \\
& (-19+x)(64064-16467x+1563x^2-65x^3+x^4), \\
& (-19+x)(64072-16467x+1563x^2-65x^3+x^4), \\
& (-17+x)^2(-4204+809x-50x^2+x^3), (-17+x)(71476-17957x+1659x^2-67x^3+x^4), \\
& (-21+x)(-17+x)(-3404+693x-46x^2+x^3), \\
& (-17+x)(71492-17957x+1659x^2-67x^3+x^4), \\
& (-17+x)(71500-17957x+1659x^2-67x^3+x^4), \\
& -1215652 + 376777x - 46160x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17+x)(71508-17957x+1659x^2-67x^3+x^4), \\
& -1215788 + 376785x - 46160x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-19+x)(-17+x)(-3764+747x-48x^2+x^3), \\
& (-19+x)(63996-16463x+1563x^2-65x^3+x^4), \\
& (-21+x)(-17+x)^2(200-29x+x^2), (-17+x)(71408-17953x+1659x^2-67x^3+x^4),
\end{aligned}$$

$$\begin{aligned}
& (-17+x) (71416 - 17953x + 1659x^2 - 67x^3 + x^4), \\
& (-17+x) (71424 - 17953x + 1659x^2 - 67x^3 + x^4), \\
& -1214360 + 376633x - 46156x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-17+x) (71432 - 17953x + 1659x^2 - 67x^3 + x^4), \\
& -1214496 + 376641x - 46156x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-19+x) (-17+x) (-16+x) (235 - 32x + x^2), \\
& (-19+x) (63928 - 16459x + 1563x^2 - 65x^3 + x^4), \\
& (-17+x)^2 (-4196 + 809x - 50x^2 + x^3), (-17+x) (71340 - 17949x + 1659x^2 - 67x^3 + x^4), \\
& (-17+x) (71348 - 17949x + 1659x^2 - 67x^3 + x^4), \\
& (-17+x) (71356 - 17949x + 1659x^2 - 67x^3 + x^4), \\
& -1213204 + 376497x - 46152x^2 + 2798x^3 - 84x^4 + x^5, \\
& (-19+x) (-17+x) (-3756 + 747x - 48x^2 + x^3), \\
& (-19+x) (63860 - 16455x + 1563x^2 - 65x^3 + x^4), \\
& (-17+x)^2 (-4192 + 809x - 50x^2 + x^3), (-17+x) (71272 - 17945x + 1659x^2 - 67x^3 + x^4), \\
& (-17+x) (71280 - 17945x + 1659x^2 - 67x^3 + x^4), \\
& (-19+x) (-17+x) (-3752 + 747x - 48x^2 + x^3), \\
& (-19+x) (-16+x) (-3987 + 779x - 49x^2 + x^3), \\
& (-17+x) (71188 - 17941x + 1659x^2 - 67x^3 + x^4), \\
& (-17+x)^2 (-4188 + 809x - 50x^2 + x^3), (-17+x) (71204 - 17941x + 1659x^2 - 67x^3 + x^4), \\
& (-19+x) (-17+x) (-3748 + 747x - 48x^2 + x^3), \\
& (-17+x) (71120 - 17937x + 1659x^2 - 67x^3 + x^4), \\
& (-17+x)^2 (-4184 + 809x - 50x^2 + x^3), (-19+x) (-17+x) (-3744 + 747x - 48x^2 + x^3), \\
& (-17+x) (71052 - 17933x + 1659x^2 - 67x^3 + x^4), \\
& (-20+x) (-19+x) (-17+x)^2 (-11+x), (-19+x) (-17+x) (-3736 + 747x - 48x^2 + x^3) \}
\end{aligned}$$

Length[list]

239

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listmod32 = modfilter[list * mu[chiwarrant] // Factor, chiSmod32n93, 32]
{(-19+x)^13 (-17+x)^3 (5+x)^73 (72264 - 18001x + 1659x^2 - 67x^3 + x^4),
 (-19+x)^13 (-17+x)^3 (-13+x) (5+x)^73 (-5560 + 957x - 54x^2 + x^3),
 (-19+x)^13 (-17+x)^3 (-15+x) (5+x)^73 (-4812 + 879x - 52x^2 + x^3),
 (-19+x)^13 (-17+x)^3 (5+x)^73 (72196 - 17997x + 1659x^2 - 67x^3 + x^4),
 (-19+x)^13 (-17+x)^3 (5+x)^73 (72212 - 17997x + 1659x^2 - 67x^3 + x^4),
 (-19+x)^13 (-17+x)^3 (-13+x) (5+x)^73 (-5556 + 957x - 54x^2 + x^3),
 (-19+x)^13 (-17+x)^2 (5+x)^73 (-1226464 + 378025x - 46196x^2 + 2798x^3 - 84x^4 + x^5),
 (-19+x)^13 (-17+x)^2 (5+x)^73 (-1226736 + 378041x - 46196x^2 + 2798x^3 - 84x^4 + x^5),
 (-19+x)^13 (-17+x)^2 (5+x)^73 (-1227008 + 378057x - 46196x^2 + 2798x^3 - 84x^4 + x^5),
 (-19+x)^13 (-17+x)^2 (5+x)^73 (-1225308 + 377889x - 46192x^2 + 2798x^3 - 84x^4 + x^5),
 (-19+x)^13 (-17+x)^2 (5+x)^73 (-1225580 + 377905x - 46192x^2 + 2798x^3 - 84x^4 + x^5),
 (-19+x)^13 (-17+x)^2 (5+x)^73 (-1225852 + 377921x - 46192x^2 + 2798x^3 - 84x^4 + x^5),
 (-19+x)^13 (-17+x)^3 (5+x)^73 (71960 - 17985x + 1659x^2 - 67x^3 + x^4),
 (-19+x)^13 (-17+x)^3 (5+x)^73 (71976 - 17985x + 1659x^2 - 67x^3 + x^4),

```

$$\begin{aligned}
& (-19+x)^{13} (-17+x)^3 (5+x)^{73} (71992 - 17985x + 1659x^2 - 67x^3 + x^4), \\
& (-19+x)^{13} (-17+x)^3 (5+x)^{73} (72008 - 17985x + 1659x^2 - 67x^3 + x^4), \\
& (-19+x)^{13} (-17+x)^2 (5+x)^{73} (-1224440 + 377769x - 46188x^2 + 2798x^3 - 84x^4 + x^5), \\
& (-19+x)^{13} (-17+x)^3 (5+x)^{73} (72024 - 17985x + 1659x^2 - 67x^3 + x^4), \\
& (-19+x)^{13} (-17+x)^2 (5+x)^{73} (-1224712 + 377785x - 46188x^2 + 2798x^3 - 84x^4 + x^5), \\
& (-19+x)^{13} (-17+x)^3 (5+x)^{73} (72040 - 17985x + 1659x^2 - 67x^3 + x^4), \\
& (-19+x)^{13} (-17+x)^2 (5+x)^{73} (-1224984 + 377801x - 46188x^2 + 2798x^3 - 84x^4 + x^5), \\
& (-19+x)^{13} (-17+x)^3 (5+x)^{73} (71892 - 17981x + 1659x^2 - 67x^3 + x^4), \\
& (-19+x)^{13} (-17+x)^3 (5+x)^{73} (71908 - 17981x + 1659x^2 - 67x^3 + x^4), \\
& (-19+x)^{13} (-17+x)^3 (5+x)^{73} (71924 - 17981x + 1659x^2 - 67x^3 + x^4), \\
& (-19+x)^{13} (-17+x)^3 (-15+x) (5+x)^{73} (-4796 + 879x - 52x^2 + x^3), \\
& (-19+x)^{13} (-17+x)^2 (5+x)^{73} (-1223284 + 377633x - 46184x^2 + 2798x^3 - 84x^4 + x^5), \\
& (-19+x)^{13} (-17+x)^3 (5+x)^{73} (71956 - 17981x + 1659x^2 - 67x^3 + x^4), \\
& (-19+x)^{13} (-17+x)^2 (5+x)^{73} (-1223556 + 377649x - 46184x^2 + 2798x^3 - 84x^4 + x^5), \\
& (-19+x)^{14} (-17+x)^3 (5+x)^{73} (-3788 + 747x - 48x^2 + x^3), \\
& (-19+x)^{14} (-17+x)^2 (5+x)^{73} (64412 - 16487x + 1563x^2 - 65x^3 + x^4), \\
& (-19+x)^{13} (-17+x)^2 (5+x)^{73} (-1221568 + 377465x - 46180x^2 + 2798x^3 - 84x^4 + x^5), \\
& (-19+x)^{13} (-17+x)^2 (-15+x) (5+x)^{73} (81456 - 19735x + 1763x^2 - 69x^3 + x^4), \\
& (-19+x)^{13} (-17+x)^2 (5+x)^{73} (-1222112 + 377497x - 46180x^2 + 2798x^3 - 84x^4 + x^5), \\
& (-19+x)^{14} (-17+x)^2 (5+x)^{73} (64336 - 16483x + 1563x^2 - 65x^3 + x^4), \\
& (-19+x)^{14} (-17+x)^2 (5+x)^{73} (64352 - 16483x + 1563x^2 - 65x^3 + x^4), \\
& (-19+x)^{13} (-17+x)^2 (5+x)^{73} (-1220412 + 377329x - 46176x^2 + 2798x^3 - 84x^4 + x^5), \\
& (-19+x)^{13} (-17+x)^2 (5+x)^{73} (-1220684 + 377345x - 46176x^2 + 2798x^3 - 84x^4 + x^5), \\
& (-19+x)^{13} (-17+x)^2 (5+x)^{73} (-1220956 + 377361x - 46176x^2 + 2798x^3 - 84x^4 + x^5), \\
& (-19+x)^{13} (-17+x)^3 (5+x)^{73} (71688 - 17969x + 1659x^2 - 67x^3 + x^4), \\
& (-19+x)^{13} (-17+x)^3 (5+x)^{73} (71704 - 17969x + 1659x^2 - 67x^3 + x^4), \\
& (-19+x)^{13} (-17+x)^3 (5+x)^{73} (71720 - 17969x + 1659x^2 - 67x^3 + x^4), \\
& (-21+x) (-19+x)^{13} (-17+x)^3 (5+x)^{73} (-3416 + 693x - 46x^2 + x^3), \\
& (-19+x)^{13} (-17+x)^2 (5+x)^{73} (-1219816 + 377225x - 46172x^2 + 2798x^3 - 84x^4 + x^5), \\
& (-19+x)^{13} (-17+x)^3 (5+x)^{73} (71620 - 17965x + 1659x^2 - 67x^3 + x^4), \\
& (-19+x)^{13} (-17+x)^3 (5+x)^{73} (71636 - 17965x + 1659x^2 - 67x^3 + x^4), \\
& (-21+x) (-19+x)^{13} (-17+x)^3 (5+x)^{73} (-3412 + 693x - 46x^2 + x^3), \\
& (-19+x)^{14} (-17+x)^3 (5+x)^{73} (-3772 + 747x - 48x^2 + x^3), \\
& (-19+x)^{14} (-17+x)^2 (-15+x) (5+x)^{73} (-4276 + 813x - 50x^2 + x^3), \\
& (-19+x)^{13} (-17+x)^2 (5+x)^{73} (-1216944 + 376921x - 46164x^2 + 2798x^3 - 84x^4 + x^5), \\
& (-19+x)^{14} (-17+x)^2 (5+x)^{73} (64064 - 16467x + 1563x^2 - 65x^3 + x^4), \\
& (-19+x)^{13} (-17+x)^2 (5+x)^{73} (-1215788 + 376785x - 46160x^2 + 2798x^3 - 84x^4 + x^5), \\
& (-21+x) (-19+x)^{13} (-17+x)^4 (5+x)^{73} (200 - 29x + x^2), \\
& (-19+x)^{13} (-17+x)^3 (5+x)^{73} (71416 - 17953x + 1659x^2 - 67x^3 + x^4), \\
& (-19+x)^{13} (-17+x)^3 (5+x)^{73} (71432 - 17953x + 1659x^2 - 67x^3 + x^4), \\
& (-19+x)^{13} (-17+x)^4 (5+x)^{73} (-4196 + 809x - 50x^2 + x^3), \\
& (-19+x)^{13} (-17+x)^3 (5+x)^{73} (71348 - 17949x + 1659x^2 - 67x^3 + x^4),
\end{aligned}$$

$$\begin{aligned} & (-19+x)^{14} (-17+x)^3 (5+x)^{73} (-3756 + 747x - 48x^2 + x^3), \\ & (-19+x)^{14} (-17+x)^2 (-16+x) (5+x)^{73} (-3987 + 779x - 49x^2 + x^3), \\ & (-19+x)^{13} (-17+x)^4 (5+x)^{73} (-4184 + 809x - 50x^2 + x^3), \\ & (-20+x) (-19+x)^{14} (-17+x)^4 (-11+x) (5+x)^{73} \} \end{aligned}$$

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Length[listmod32]
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60
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CoefficientList[listmod32 / mu[chiwarrant] // Factor, x]
{{-1228488, 378281, -46204, 2798, -84, 1},
 {-1228760, 378297, -46204, 2798, -84, 1},
 {-1227060, 378129, -46200, 2798, -84, 1},
 {-1227332, 378145, -46200, 2798, -84, 1},
 {-1227604, 378161, -46200, 2798, -84, 1},
 {-1227876, 378177, -46200, 2798, -84, 1},
 {-1226464, 378025, -46196, 2798, -84, 1},
 {-1226736, 378041, -46196, 2798, -84, 1},
 {-1227008, 378057, -46196, 2798, -84, 1},
 {-1225308, 377889, -46192, 2798, -84, 1},
 {-1225580, 377905, -46192, 2798, -84, 1},
 {-1225852, 377921, -46192, 2798, -84, 1},
 {-1223320, 377705, -46188, 2798, -84, 1},
 {-1223592, 377721, -46188, 2798, -84, 1},
 {-1223864, 377737, -46188, 2798, -84, 1},
 {-1224136, 377753, -46188, 2798, -84, 1},
 {-1224440, 377769, -46188, 2798, -84, 1},
 {-1224408, 377769, -46188, 2798, -84, 1},
 {-1224712, 377785, -46188, 2798, -84, 1},
 {-1224680, 377785, -46188, 2798, -84, 1},
 {-1224984, 377801, -46188, 2798, -84, 1},
 {-1222164, 377569, -46184, 2798, -84, 1},
 {-1222436, 377585, -46184, 2798, -84, 1},
 {-1222708, 377601, -46184, 2798, -84, 1},
 {-1222980, 377617, -46184, 2798, -84, 1},
 {-1223284, 377633, -46184, 2798, -84, 1},
 {-1223252, 377633, -46184, 2798, -84, 1},
 {-1223556, 377649, -46184, 2798, -84, 1},
 {-1223524, 377649, -46184, 2798, -84, 1},
 {-1223828, 377665, -46184, 2798, -84, 1},
 {-1221568, 377465, -46180, 2798, -84, 1},
 {-1221840, 377481, -46180, 2798, -84, 1},
 {-1222112, 377497, -46180, 2798, -84, 1},
 {-1222384, 377513, -46180, 2798, -84, 1},
 {-1222688, 377529, -46180, 2798, -84, 1},
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 {-1220684, 377345, -46176, 2798, -84, 1},
 {-1220956, 377361, -46176, 2798, -84, 1},
```

```
{-1218696, 377161, -46172, 2798, -84, 1},  
{-1218968, 377177, -46172, 2798, -84, 1},  
{-1219240, 377193, -46172, 2798, -84, 1},  
{-1219512, 377209, -46172, 2798, -84, 1},  
{-1219816, 377225, -46172, 2798, -84, 1},  
{-1217540, 377025, -46168, 2798, -84, 1},  
{-1217812, 377041, -46168, 2798, -84, 1},  
{-1218084, 377057, -46168, 2798, -84, 1},  
{-1218356, 377073, -46168, 2798, -84, 1},  
{-1218660, 377089, -46168, 2798, -84, 1},  
{-1216944, 376921, -46164, 2798, -84, 1},  
{-1217216, 376937, -46164, 2798, -84, 1},  
{-1215788, 376785, -46160, 2798, -84, 1},  
{-1213800, 376601, -46156, 2798, -84, 1},  
{-1214072, 376617, -46156, 2798, -84, 1},  
{-1214344, 376633, -46156, 2798, -84, 1},  
{-1212644, 376465, -46152, 2798, -84, 1},  
{-1212916, 376481, -46152, 2798, -84, 1},  
{-1213188, 376497, -46152, 2798, -84, 1},  
{-1212048, 376361, -46148, 2798, -84, 1},  
{-1209176, 376057, -46140, 2798, -84, 1},  
{-1208020, 375921, -46136, 2798, -84, 1} }
```

```

A1 = {{-1228488, 378281, -46204, 2798, -84, 1},
      {-1228760, 378297, -46204, 2798, -84, 1},
      {-1227060, 378129, -46200, 2798, -84, 1}, {-1227332, 378145,
         -46200, 2798, -84, 1}, {-1227604, 378161, -46200, 2798, -84, 1},
      {-1227876, 378177, -46200, 2798, -84, 1}, {-1226464, 378025,
         -46196, 2798, -84, 1}, {-1226736, 378041, -46196, 2798, -84, 1},
      {-1227008, 378057, -46196, 2798, -84, 1}, {-1225308, 377889,
         -46192, 2798, -84, 1}, {-1225580, 377905, -46192, 2798, -84, 1},
      {-1225852, 377921, -46192, 2798, -84, 1}, {-1223320, 377705,
         -46188, 2798, -84, 1}, {-1223592, 377721, -46188, 2798, -84, 1},
      {-1223864, 377737, -46188, 2798, -84, 1}, {-1224136, 377753,
         -46188, 2798, -84, 1}, {-1224440, 377769, -46188, 2798, -84, 1},
      {-1224408, 377769, -46188, 2798, -84, 1}, {-1224712, 377785,
         -46188, 2798, -84, 1}, {-1224680, 377785, -46188, 2798, -84, 1},
      {-1224984, 377801, -46188, 2798, -84, 1}, {-1222164, 377569,
         -46184, 2798, -84, 1}, {-1222436, 377585, -46184, 2798, -84, 1},
      {-1222708, 377601, -46184, 2798, -84, 1}, {-1222980, 377617,
         -46184, 2798, -84, 1}, {-1223284, 377633, -46184, 2798, -84, 1},
      {-1223252, 377633, -46184, 2798, -84, 1}, {-1223556, 377649,
         -46184, 2798, -84, 1}, {-1223828, 377665, -46184, 2798, -84, 1},
      {-1221568, 377465, -46180, 2798, -84, 1}, {-1221840, 377481, -46180, 2798, -84, 1},
      {-1222112, 377497, -46180, 2798, -84, 1}, {-1222384, 377513,
         -46180, 2798, -84, 1}, {-1222688, 377529, -46180, 2798, -84, 1},
      {-1220412, 377329, -46176, 2798, -84, 1}, {-1220684, 377345,
         -46176, 2798, -84, 1}, {-1218696, 377161, -46172, 2798, -84, 1},
      {-1218968, 377177, -46172, 2798, -84, 1}, {-1219240, 377193, -46172, 2798, -84, 1},
      {-1219512, 377209, -46172, 2798, -84, 1}, {-1219816, 377225,
         -46172, 2798, -84, 1}, {-1217540, 377025, -46168, 2798, -84, 1},
      {-1217812, 377041, -46168, 2798, -84, 1}, {-1218084, 377057,
         -46168, 2798, -84, 1}, {-1218356, 377073, -46168, 2798, -84, 1},
      {-1218660, 377089, -46168, 2798, -84, 1}, {-1216944, 376921,
         -46164, 2798, -84, 1}, {-1217216, 376937, -46164, 2798, -84, 1},
      {-1215788, 376785, -46160, 2798, -84, 1}, {-1213800, 376601,
         -46156, 2798, -84, 1}, {-1214072, 376617, -46156, 2798, -84, 1},
      {-1214344, 376633, -46156, 2798, -84, 1}, {-1212644, 376465,
         -46152, 2798, -84, 1}, {-1212916, 376481, -46152, 2798, -84, 1},
      {-1213188, 376497, -46152, 2798, -84, 1}, {-1212048, 376361,
         -46148, 2798, -84, 1}, {-1209176, 376057, -46140, 2798, -84, 1},
      {-1208020, 375921, -46136, 2798, -84, 1}};

A1 // MatrixForm

```

$$\left(\begin{array}{cccccc} -1228488 & 378281 & -46204 & 2798 & -84 & 1 \\ -1228760 & 378297 & -46204 & 2798 & -84 & 1 \\ -1227060 & 378129 & -46200 & 2798 & -84 & 1 \\ -1227332 & 378145 & -46200 & 2798 & -84 & 1 \\ -1227604 & 378161 & -46200 & 2798 & -84 & 1 \end{array} \right)$$

-1 227 876	378 177	-46 200	2798	-84	1
-1 226 464	378 025	-46 196	2798	-84	1
-1 226 736	378 041	-46 196	2798	-84	1
-1 227 008	378 057	-46 196	2798	-84	1
-1 225 308	377 889	-46 192	2798	-84	1
-1 225 580	377 905	-46 192	2798	-84	1
-1 225 852	377 921	-46 192	2798	-84	1
-1 223 320	377 705	-46 188	2798	-84	1
-1 223 592	377 721	-46 188	2798	-84	1
-1 223 864	377 737	-46 188	2798	-84	1
-1 224 136	377 753	-46 188	2798	-84	1
-1 224 440	377 769	-46 188	2798	-84	1
-1 224 408	377 769	-46 188	2798	-84	1
-1 224 712	377 785	-46 188	2798	-84	1
-1 224 680	377 785	-46 188	2798	-84	1
-1 224 984	377 801	-46 188	2798	-84	1
-1 222 164	377 569	-46 184	2798	-84	1
-1 222 436	377 585	-46 184	2798	-84	1
-1 222 708	377 601	-46 184	2798	-84	1
-1 222 980	377 617	-46 184	2798	-84	1
-1 223 284	377 633	-46 184	2798	-84	1
-1 223 252	377 633	-46 184	2798	-84	1
-1 223 556	377 649	-46 184	2798	-84	1
-1 223 524	377 649	-46 184	2798	-84	1
-1 223 828	377 665	-46 184	2798	-84	1
-1 221 568	377 465	-46 180	2798	-84	1
-1 221 840	377 481	-46 180	2798	-84	1
-1 222 112	377 497	-46 180	2798	-84	1
-1 222 384	377 513	-46 180	2798	-84	1
-1 222 688	377 529	-46 180	2798	-84	1
-1 220 412	377 329	-46 176	2798	-84	1
-1 220 684	377 345	-46 176	2798	-84	1
-1 220 956	377 361	-46 176	2798	-84	1
-1 218 696	377 161	-46 172	2798	-84	1
-1 218 968	377 177	-46 172	2798	-84	1
-1 219 240	377 193	-46 172	2798	-84	1
-1 219 512	377 209	-46 172	2798	-84	1
-1 219 816	377 225	-46 172	2798	-84	1
-1 217 540	377 025	-46 168	2798	-84	1
-1 217 812	377 041	-46 168	2798	-84	1
-1 218 084	377 057	-46 168	2798	-84	1
-1 218 356	377 073	-46 168	2798	-84	1
-1 218 660	377 089	-46 168	2798	-84	1
-1 216 944	376 921	-46 164	2798	-84	1
-1 217 216	376 937	-46 164	2798	-84	1
-1 215 788	376 785	-46 160	2798	-84	1
-1 213 800	376 601	-46 156	2798	-84	1
-1 214 072	376 617	-46 156	2798	-84	1
-1 214 344	376 633	-46 156	2798	-84	1
-1 212 644	376 465	-46 152	2798	-84	1
-1 212 916	376 481	-46 152	2798	-84	1
-1 213 188	376 497	-46 152	2798	-84	1
-1 212 048	376 361	-46 148	2798	-84	1
-1 209 176	376 057	-46 140	2798	-84	1
-1 208 020	375 921	-46 136	2798	-84	1

```

g1 = CoefficientList[D[chiwarrant, x] / mu[chiwarrant] // Factor, x]
{-115 382 912, 35 547 054, -4 342 840, 263 012, -7896, 94}

Array[c, 6].Transpose[A1]

{-1 228 488 c[1] + 378 281 c[2] - 46 204 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 228 760 c[1] + 378 297 c[2] - 46 204 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 227 060 c[1] + 378 129 c[2] - 46 200 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 227 332 c[1] + 378 145 c[2] - 46 200 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 227 604 c[1] + 378 161 c[2] - 46 200 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 227 876 c[1] + 378 177 c[2] - 46 200 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 226 464 c[1] + 378 025 c[2] - 46 196 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 226 736 c[1] + 378 041 c[2] - 46 196 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 227 008 c[1] + 378 057 c[2] - 46 196 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 225 308 c[1] + 377 889 c[2] - 46 192 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 225 580 c[1] + 377 905 c[2] - 46 192 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 225 852 c[1] + 377 921 c[2] - 46 192 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 223 320 c[1] + 377 705 c[2] - 46 188 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 223 592 c[1] + 377 721 c[2] - 46 188 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 223 864 c[1] + 377 737 c[2] - 46 188 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 224 136 c[1] + 377 753 c[2] - 46 188 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 224 440 c[1] + 377 769 c[2] - 46 188 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 224 408 c[1] + 377 769 c[2] - 46 188 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 224 712 c[1] + 377 785 c[2] - 46 188 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 224 680 c[1] + 377 785 c[2] - 46 188 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 224 984 c[1] + 377 801 c[2] - 46 188 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 222 164 c[1] + 377 569 c[2] - 46 184 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 222 436 c[1] + 377 585 c[2] - 46 184 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 222 708 c[1] + 377 601 c[2] - 46 184 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 222 980 c[1] + 377 617 c[2] - 46 184 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 223 284 c[1] + 377 633 c[2] - 46 184 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 223 252 c[1] + 377 633 c[2] - 46 184 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 223 556 c[1] + 377 649 c[2] - 46 184 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 223 524 c[1] + 377 649 c[2] - 46 184 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 223 828 c[1] + 377 665 c[2] - 46 184 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 221 568 c[1] + 377 465 c[2] - 46 180 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 221 840 c[1] + 377 481 c[2] - 46 180 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 222 112 c[1] + 377 497 c[2] - 46 180 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 222 384 c[1] + 377 513 c[2] - 46 180 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 222 688 c[1] + 377 529 c[2] - 46 180 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 220 412 c[1] + 377 329 c[2] - 46 176 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 220 684 c[1] + 377 345 c[2] - 46 176 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 220 956 c[1] + 377 361 c[2] - 46 176 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 218 696 c[1] + 377 161 c[2] - 46 172 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 218 968 c[1] + 377 177 c[2] - 46 172 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 219 240 c[1] + 377 193 c[2] - 46 172 c[3] + 2798 c[4] - 84 c[5] + c[6],
 -1 219 512 c[1] + 377 209 c[2] - 46 172 c[3] + 2798 c[4] - 84 c[5] + c[6],

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- 1219 816 c[1] + 377 225 c[2] - 46 172 c[3] + 2798 c[4] - 84 c[5] + c[6] ,
- 1217 540 c[1] + 377 025 c[2] - 46 168 c[3] + 2798 c[4] - 84 c[5] + c[6] ,
- 1217 812 c[1] + 377 041 c[2] - 46 168 c[3] + 2798 c[4] - 84 c[5] + c[6] ,
- 1218 084 c[1] + 377 057 c[2] - 46 168 c[3] + 2798 c[4] - 84 c[5] + c[6] ,
- 1218 356 c[1] + 377 073 c[2] - 46 168 c[3] + 2798 c[4] - 84 c[5] + c[6] ,
- 1218 660 c[1] + 377 089 c[2] - 46 168 c[3] + 2798 c[4] - 84 c[5] + c[6] ,
- 1216 944 c[1] + 376 921 c[2] - 46 164 c[3] + 2798 c[4] - 84 c[5] + c[6] ,
- 1217 216 c[1] + 376 937 c[2] - 46 164 c[3] + 2798 c[4] - 84 c[5] + c[6] ,
- 1215 788 c[1] + 376 785 c[2] - 46 160 c[3] + 2798 c[4] - 84 c[5] + c[6] ,
- 1213 800 c[1] + 376 601 c[2] - 46 156 c[3] + 2798 c[4] - 84 c[5] + c[6] ,
- 1214 072 c[1] + 376 617 c[2] - 46 156 c[3] + 2798 c[4] - 84 c[5] + c[6] ,
- 1214 344 c[1] + 376 633 c[2] - 46 156 c[3] + 2798 c[4] - 84 c[5] + c[6] ,
- 1212 644 c[1] + 376 465 c[2] - 46 152 c[3] + 2798 c[4] - 84 c[5] + c[6] ,
- 1212 916 c[1] + 376 481 c[2] - 46 152 c[3] + 2798 c[4] - 84 c[5] + c[6] ,
- 1213 188 c[1] + 376 497 c[2] - 46 152 c[3] + 2798 c[4] - 84 c[5] + c[6] ,
- 1212 048 c[1] + 376 361 c[2] - 46 148 c[3] + 2798 c[4] - 84 c[5] + c[6] ,
- 1209 176 c[1] + 376 057 c[2] - 46 140 c[3] + 2798 c[4] - 84 c[5] + c[6] ,
- 1208 020 c[1] + 375 921 c[2] - 46 136 c[3] + 2798 c[4] - 84 c[5] + c[6] }

```

Array[c, 6].g1

```
- 115 382 912 c[1] + 35 547 054 c[2] - 4 342 840 c[3] + 263 012 c[4] - 7896 c[5] + 94 c[6]
```

cert1 = Flatten[

```

  Array[c, 6] /. FindInstance[- 115 382 912 c[1] + 35 547 054 c[2] - 4 342 840 c[3] +
    263 012 c[4] - 7896 c[5] + 94 c[6] < 0 &&
- 1228 488 c[1] + 378 281 c[2] - 46 204 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
- 1228 760 c[1] + 378 297 c[2] - 46 204 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
- 1227 060 c[1] + 378 129 c[2] - 46 200 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
- 1227 332 c[1] + 378 145 c[2] - 46 200 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
- 1227 604 c[1] + 378 161 c[2] - 46 200 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
- 1227 876 c[1] + 378 177 c[2] - 46 200 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
- 1226 464 c[1] + 378 025 c[2] - 46 196 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
- 1226 736 c[1] + 378 041 c[2] - 46 196 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
- 1227 008 c[1] + 378 057 c[2] - 46 196 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
- 1225 308 c[1] + 377 889 c[2] - 46 192 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
- 1225 580 c[1] + 377 905 c[2] - 46 192 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
- 1225 852 c[1] + 377 921 c[2] - 46 192 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
- 1223 320 c[1] + 377 705 c[2] - 46 188 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
- 1223 592 c[1] + 377 721 c[2] - 46 188 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
- 1223 864 c[1] + 377 737 c[2] - 46 188 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
- 1224 136 c[1] + 377 753 c[2] - 46 188 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
- 1224 440 c[1] + 377 769 c[2] - 46 188 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
- 1224 408 c[1] + 377 769 c[2] - 46 188 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
- 1224 712 c[1] + 377 785 c[2] - 46 188 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
- 1224 680 c[1] + 377 785 c[2] - 46 188 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
- 1224 984 c[1] + 377 801 c[2] - 46 188 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
- 1222 164 c[1] + 377 569 c[2] - 46 184 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
```

```

-1 222 436 c[1] + 377 585 c[2] - 46 184 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 222 708 c[1] + 377 601 c[2] - 46 184 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 222 980 c[1] + 377 617 c[2] - 46 184 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 223 284 c[1] + 377 633 c[2] - 46 184 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 223 252 c[1] + 377 633 c[2] - 46 184 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 223 556 c[1] + 377 649 c[2] - 46 184 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 223 524 c[1] + 377 649 c[2] - 46 184 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 223 828 c[1] + 377 665 c[2] - 46 184 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 221 568 c[1] + 377 465 c[2] - 46 180 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 221 840 c[1] + 377 481 c[2] - 46 180 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 222 112 c[1] + 377 497 c[2] - 46 180 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 222 384 c[1] + 377 513 c[2] - 46 180 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 222 688 c[1] + 377 529 c[2] - 46 180 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 220 412 c[1] + 377 329 c[2] - 46 176 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 220 684 c[1] + 377 345 c[2] - 46 176 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 220 956 c[1] + 377 361 c[2] - 46 176 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 218 696 c[1] + 377 161 c[2] - 46 172 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 218 968 c[1] + 377 177 c[2] - 46 172 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 219 240 c[1] + 377 193 c[2] - 46 172 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 219 512 c[1] + 377 209 c[2] - 46 172 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 219 816 c[1] + 377 225 c[2] - 46 172 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 217 540 c[1] + 377 025 c[2] - 46 168 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 217 812 c[1] + 377 041 c[2] - 46 168 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 218 084 c[1] + 377 057 c[2] - 46 168 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 218 356 c[1] + 377 073 c[2] - 46 168 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 218 660 c[1] + 377 089 c[2] - 46 168 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 216 944 c[1] + 376 921 c[2] - 46 164 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 217 216 c[1] + 376 937 c[2] - 46 164 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 215 788 c[1] + 376 785 c[2] - 46 160 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 213 800 c[1] + 376 601 c[2] - 46 156 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 214 072 c[1] + 376 617 c[2] - 46 156 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 214 344 c[1] + 376 633 c[2] - 46 156 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 212 644 c[1] + 376 465 c[2] - 46 152 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 212 916 c[1] + 376 481 c[2] - 46 152 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 213 188 c[1] + 376 497 c[2] - 46 152 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 212 048 c[1] + 376 361 c[2] - 46 148 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 209 176 c[1] + 376 057 c[2] - 46 140 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0 &&
-1 208 020 c[1] + 375 921 c[2] - 46 136 c[3] + 2798 c[4] - 84 c[5] + c[6] ≥ 0,
Array[c, 6], Integers]]
{265 131, 4 595 613, 79 981 334, 0, 0, 2 282 735 504 746}

GCD[265 131, 4 595 613, 79 981 334, 0, 0, 2 282 735 504 746]
1

Reverse[cert1]
{2 282 735 504 746, 0, 0, 79 981 334, 4 595 613, 265 131}

```

cert1.g1

- 82 469 806

cert1.Transpose[A1]

```
{777935, 2192111, 777163, 2191339, 3605515, 5019691, 776823, 2190999,  
3605175, 2190227, 3604403, 5018579, 3603199, 5017375, 6431551, 7845727,  
775711, 9259903, 2189887, 10674079, 3604063, 5016603, 6430779, 7844955,  
9259131, 2189115, 10673307, 3603291, 12087483, 5017467, 5016263,  
6430439, 7844615, 9258791, 2188775, 6429667, 7843843, 9258019, 9256815,  
10670991, 12085167, 13499343, 6429327, 10670219, 12084395, 13498571,  
14912747, 7842731, 10669879, 12084055, 12083283, 13496255, 14910431,  
16324607, 14909659, 16323835, 17738011, 14909319, 19149871, 20563275}
```