

```

In[*]:= dim14last6 = { (-7 + x)^2 (-5 + x)^10 (5 + x)^15 (16 - 11 x + x^2),
  (-7 + x)^2 (-5 + x)^9 (-3 + x) (5 + x)^15 (32 - 13 x + x^2),
  (-7 + x) (-5 + x)^10 (5 + x)^15 (-128 + 93 x - 18 x^2 + x^3),
  (-5 + x)^11 (-3 + x) (5 + x)^15 (68 - 17 x + x^2), (-7 + x)^2 (-5 + x)^8 (-3 + x)^2
  (5 + x)^15 (52 - 15 x + x^2), (-9 + x)^2 (-5 + x)^10 (-4 + x) (-3 + x) (5 + x)^15};

```

```

In[*]:= chi = (-7 + x)^2 (-5 + x)^10 (5 + x)^15 (16 - 11 x + x^2)

```

```

Out[*]:= (-7 + x)^2 (-5 + x)^10 (5 + x)^15 (16 - 11 x + x^2)

```

```

CoefficientList[feasibleinterlacingpolylist[chi], x]

```

```

{{-225, -110, 96, -18, 1}, {-209, -110, 96, -18, 1},
 {-193, -110, 96, -18, 1}, {-177, -110, 96, -18, 1},
 {-161, -110, 96, -18, 1}, {-217, -102, 96, -18, 1}, {-345, -86, 96, -18, 1},
 {-329, -86, 96, -18, 1}, {-265, -102, 96, -18, 1}, {-249, -102, 96, -18, 1},
 {-233, -102, 96, -18, 1}, {31, -142, 96, -18, 1}, {-41, -134, 96, -18, 1},
 {-25, -134, 96, -18, 1}, {-9, -134, 96, -18, 1}, {7, -134, 96, -18, 1},
 {-113, -126, 96, -18, 1}, {-97, -126, 96, -18, 1}, {-81, -126, 96, -18, 1},
 {-65, -126, 96, -18, 1}, {-49, -126, 96, -18, 1}, {-185, -118, 96, -18, 1},
 {-169, -118, 96, -18, 1}, {-153, -118, 96, -18, 1}, {-137, -118, 96, -18, 1},
 {-121, -118, 96, -18, 1}, {-105, -118, 96, -18, 1}, {-305, -94, 96, -18, 1},
 {-289, -94, 96, -18, 1}, {-273, -94, 96, -18, 1}, {-385, -78, 96, -18, 1}}

```

```

A = {{31, -142, 96, -18, 1}, {-41, -134, 96, -18, 1},
 {-25, -134, 96, -18, 1}, {-9, -134, 96, -18, 1}, {7, -134, 96, -18, 1},
 {-113, -126, 96, -18, 1}, {-97, -126, 96, -18, 1}, {-81, -126, 96, -18, 1},
 {-65, -126, 96, -18, 1}, {-49, -126, 96, -18, 1}, {-185, -118, 96, -18, 1},
 {-169, -118, 96, -18, 1}, {-153, -118, 96, -18, 1},
 {-137, -118, 96, -18, 1}, {-121, -118, 96, -18, 1}, {-105, -118, 96, -18, 1},
 {-225, -110, 96, -18, 1}, {-209, -110, 96, -18, 1}, {-193, -110, 96, -18, 1},
 {-177, -110, 96, -18, 1}, {-161, -110, 96, -18, 1}, {-265, -102, 96, -18, 1},
 {-249, -102, 96, -18, 1}, {-233, -102, 96, -18, 1}, {-217, -102, 96, -18, 1},
 {-305, -94, 96, -18, 1}, {-289, -94, 96, -18, 1}, {-273, -94, 96, -18, 1},
 {-345, -86, 96, -18, 1}, {-329, -86, 96, -18, 1}, {-385, -78, 96, -18, 1}};

```

A // MatrixForm

$$\begin{pmatrix} 31 & -142 & 96 & -18 & 1 \\ -41 & -134 & 96 & -18 & 1 \\ -25 & -134 & 96 & -18 & 1 \\ -9 & -134 & 96 & -18 & 1 \\ 7 & -134 & 96 & -18 & 1 \\ -113 & -126 & 96 & -18 & 1 \\ -97 & -126 & 96 & -18 & 1 \\ -81 & -126 & 96 & -18 & 1 \\ -65 & -126 & 96 & -18 & 1 \\ -49 & -126 & 96 & -18 & 1 \\ -185 & -118 & 96 & -18 & 1 \\ -169 & -118 & 96 & -18 & 1 \\ -153 & -118 & 96 & -18 & 1 \\ -137 & -118 & 96 & -18 & 1 \\ -121 & -118 & 96 & -18 & 1 \\ -105 & -118 & 96 & -18 & 1 \\ -225 & -110 & 96 & -18 & 1 \\ -209 & -110 & 96 & -18 & 1 \\ -193 & -110 & 96 & -18 & 1 \\ -177 & -110 & 96 & -18 & 1 \\ -161 & -110 & 96 & -18 & 1 \\ -265 & -102 & 96 & -18 & 1 \\ -249 & -102 & 96 & -18 & 1 \\ -233 & -102 & 96 & -18 & 1 \\ -217 & -102 & 96 & -18 & 1 \\ -305 & -94 & 96 & -18 & 1 \\ -289 & -94 & 96 & -18 & 1 \\ -273 & -94 & 96 & -18 & 1 \\ -345 & -86 & 96 & -18 & 1 \\ -329 & -86 & 96 & -18 & 1 \\ -385 & -78 & 96 & -18 & 1 \end{pmatrix}$$

g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]

{75, -3950, 2784, -522, 29}

FindInstance[n[1] ≥ 0 && n[2] ≥ 0 && n[3] ≥ 0 && n[4] ≥ 0 && n[5] ≥ 0 &&

n[6] ≥ 0 && n[7] ≥ 0 && n[8] ≥ 0 && n[9] ≥ 0 && n[10] ≥ 0 && n[11] ≥ 0 &&

n[12] ≥ 0 && n[13] ≥ 0 && n[14] ≥ 0 && n[15] ≥ 0 && n[16] ≥ 0 && n[17] ≥ 0 &&

n[18] ≥ 0 && n[19] ≥ 0 && n[20] ≥ 0 && n[21] ≥ 0 && n[22] ≥ 0 && n[23] ≥ 0 &&

n[24] ≥ 0 && n[25] ≥ 0 && n[26] ≥ 0 && n[27] ≥ 0 && n[28] ≥ 0 && n[29] ≥ 0 &&

n[30] ≥ 0 && n[31] ≥ 0 && Array[n, 31].A == g, Array[n, 31], Integers]

{{n[1] → 18, n[2] → 0, n[3] → 0, n[4] → 0, n[5] → 9, n[6] → 0,

n[7] → 0, n[8] → 0, n[9] → 0, n[10] → 0, n[11] → 0, n[12] → 0, n[13] → 0,

n[14] → 0, n[15] → 0, n[16] → 0, n[17] → 0, n[18] → 0, n[19] → 0,

n[20] → 0, n[21] → 0, n[22] → 0, n[23] → 0, n[24] → 0, n[25] → 0,

n[26] → 0, n[27] → 0, n[28] → 2, n[29] → 0, n[30] → 0, n[31] → 0}}

Array[c, 5].Transpose[A]

```
{ 31 c[1] - 142 c[2] + 96 c[3] - 18 c[4] + c[5],
  -41 c[1] - 134 c[2] + 96 c[3] - 18 c[4] + c[5],
  -25 c[1] - 134 c[2] + 96 c[3] - 18 c[4] + c[5],
  -9 c[1] - 134 c[2] + 96 c[3] - 18 c[4] + c[5], 7 c[1] - 134 c[2] + 96 c[3] - 18 c[4] + c[5],
  -113 c[1] - 126 c[2] + 96 c[3] - 18 c[4] + c[5],
  -97 c[1] - 126 c[2] + 96 c[3] - 18 c[4] + c[5],
  -81 c[1] - 126 c[2] + 96 c[3] - 18 c[4] + c[5],
  -65 c[1] - 126 c[2] + 96 c[3] - 18 c[4] + c[5],
  -49 c[1] - 126 c[2] + 96 c[3] - 18 c[4] + c[5],
  -185 c[1] - 118 c[2] + 96 c[3] - 18 c[4] + c[5],
  -169 c[1] - 118 c[2] + 96 c[3] - 18 c[4] + c[5],
  -153 c[1] - 118 c[2] + 96 c[3] - 18 c[4] + c[5],
  -137 c[1] - 118 c[2] + 96 c[3] - 18 c[4] + c[5],
  -121 c[1] - 118 c[2] + 96 c[3] - 18 c[4] + c[5],
  -105 c[1] - 118 c[2] + 96 c[3] - 18 c[4] + c[5],
  -225 c[1] - 110 c[2] + 96 c[3] - 18 c[4] + c[5],
  -209 c[1] - 110 c[2] + 96 c[3] - 18 c[4] + c[5],
  -193 c[1] - 110 c[2] + 96 c[3] - 18 c[4] + c[5],
  -177 c[1] - 110 c[2] + 96 c[3] - 18 c[4] + c[5],
  -161 c[1] - 110 c[2] + 96 c[3] - 18 c[4] + c[5],
  -265 c[1] - 102 c[2] + 96 c[3] - 18 c[4] + c[5],
  -249 c[1] - 102 c[2] + 96 c[3] - 18 c[4] + c[5],
  -233 c[1] - 102 c[2] + 96 c[3] - 18 c[4] + c[5],
  -217 c[1] - 102 c[2] + 96 c[3] - 18 c[4] + c[5],
  -305 c[1] - 94 c[2] + 96 c[3] - 18 c[4] + c[5],
  -289 c[1] - 94 c[2] + 96 c[3] - 18 c[4] + c[5],
  -273 c[1] - 94 c[2] + 96 c[3] - 18 c[4] + c[5],
  -345 c[1] - 86 c[2] + 96 c[3] - 18 c[4] + c[5],
  -329 c[1] - 86 c[2] + 96 c[3] - 18 c[4] + c[5],
  -385 c[1] - 78 c[2] + 96 c[3] - 18 c[4] + c[5]}
```

Array[c, 5].g

```
75 c[1] - 3950 c[2] + 2784 c[3] - 522 c[4] + 29 c[5]
```

```

warrant1 = Flatten[
  Array[c, 5] /. FindInstance[75 c[1] - 3950 c[2] + 2784 c[3] - 522 c[4] + 29 c[5] < 0 &&
    31 c[1] - 142 c[2] + 96 c[3] - 18 c[4] + c[5] < 0 &&
    -41 c[1] - 134 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -25 c[1] - 134 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -9 c[1] - 134 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    7 c[1] - 134 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -113 c[1] - 126 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -97 c[1] - 126 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -81 c[1] - 126 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -65 c[1] - 126 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -49 c[1] - 126 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -185 c[1] - 118 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -169 c[1] - 118 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -153 c[1] - 118 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -137 c[1] - 118 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -121 c[1] - 118 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -105 c[1] - 118 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -225 c[1] - 110 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -209 c[1] - 110 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -193 c[1] - 110 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -177 c[1] - 110 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -161 c[1] - 110 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -265 c[1] - 102 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -249 c[1] - 102 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -233 c[1] - 102 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -217 c[1] - 102 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -305 c[1] - 94 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -289 c[1] - 94 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -273 c[1] - 94 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -345 c[1] - 86 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -329 c[1] - 86 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -385 c[1] - 78 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0, Array[c, 5], Integers]]
{0, 116, 0, 0, 15744}

GCD[0, 116, 0, 0, 15744]
4

warrant1 = warrant1 / 4
{0, 29, 0, 0, 3936}

Reverse[warrant1]
{3936, 0, 0, 29, 0}

warrant1.g
-406

```

```
warrant1.Transpose[A]
```

```
{-182, 50, 50, 50, 50, 282, 282, 282, 282, 282, 514, 514, 514, 514, 514, 514, 746,  
746, 746, 746, 978, 978, 978, 978, 1210, 1210, 1210, 1442, 1442, 1674}
```

```
warrant2 = Flatten[
```

```
Array[c, 5] /. FindInstance[75 c[1] - 3950 c[2] + 2784 c[3] - 522 c[4] + 29 c[5] < 0 &&  
31 c[1] - 142 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-41 c[1] - 134 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-25 c[1] - 134 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-9 c[1] - 134 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
7 c[1] - 134 c[2] + 96 c[3] - 18 c[4] + c[5] < 0 &&  
-113 c[1] - 126 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-97 c[1] - 126 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-81 c[1] - 126 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-65 c[1] - 126 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-49 c[1] - 126 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-185 c[1] - 118 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-169 c[1] - 118 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-153 c[1] - 118 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-137 c[1] - 118 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-121 c[1] - 118 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-105 c[1] - 118 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-225 c[1] - 110 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-209 c[1] - 110 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-193 c[1] - 110 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-177 c[1] - 110 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-161 c[1] - 110 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-265 c[1] - 102 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-249 c[1] - 102 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-233 c[1] - 102 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-217 c[1] - 102 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-305 c[1] - 94 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-289 c[1] - 94 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-273 c[1] - 94 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-345 c[1] - 86 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-329 c[1] - 86 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0 &&  
-385 c[1] - 78 c[2] + 96 c[3] - 18 c[4] + c[5] ≥ 0, Array[c, 5], Integers]]
```

```
{-492, -2459, 0, 0, -333 696}
```

```
GCD[-492, -2459, 0, 0, -333 696]
```

```
1
```

```
Reverse[warrant2]
```

```
{-333 696, 0, 0, -2459, -492}
```

warrant2.g

-1034

warrant2.Transpose[A]

{230, 15982, 8110, 238, -7634, 31734, 23862, 15990, 8118, 246, 47486,
39614, 31742, 23870, 15998, 8126, 47494, 39622, 31750, 23878, 16006,
47502, 39630, 31758, 23886, 47510, 39638, 31766, 47518, 39646, 47526}

feasibleinterlacingpolylist[chi]

{(-9+x)(-5+x)²(1+x), -209-110x+96x²-18x³+x⁴,
-193-110x+96x²-18x³+x⁴, -177-110x+96x²-18x³+x⁴,
(-7+x)(23+19x-11x²+x³), (-7+x)(1+x)(31-12x+x²),
(-5+x)(69+31x-13x²+x³), (-7+x)(47+19x-11x²+x³),
(-5+x)(53+31x-13x²+x³), -249-102x+96x²-18x³+x⁴,
-233-102x+96x²-18x³+x⁴, 31-142x+96x²-18x³+x⁴,
-41-134x+96x²-18x³+x⁴, -25-134x+96x²-18x³+x⁴, (-9+x)(1+15x-9x²+x³),
(-7+x)(-1+19x-11x²+x³), -113-126x+96x²-18x³+x⁴,
-97-126x+96x²-18x³+x⁴, (-9+x)(-3+x)(-3-6x+x²),
-65-126x+96x²-18x³+x⁴, (-7+x)(7+19x-11x²+x³),
(-5+x)(37+31x-13x²+x³), -169-118x+96x²-18x³+x⁴,
(-9+x)(17+15x-9x²+x³), -137-118x+96x²-18x³+x⁴,
-121-118x+96x²-18x³+x⁴, (-7+x)(-3+x)(-5-8x+x²),
(-5+x)(61+31x-13x²+x³), -289-94x+96x²-18x³+x⁴,
(-7+x)(39+19x-11x²+x³), (-7+x)(-5+x)(-11-6x+x²)}

In[]:= list = {(-9+x)(-5+x)²(1+x),
-209-110x+96x²-18x³+x⁴, -193-110x+96x²-18x³+x⁴,
-177-110x+96x²-18x³+x⁴, (-7+x)(23+19x-11x²+x³),
(-7+x)(1+x)(31-12x+x²), (-5+x)(69+31x-13x²+x³),
(-7+x)(47+19x-11x²+x³), (-5+x)(53+31x-13x²+x³),
-249-102x+96x²-18x³+x⁴, -233-102x+96x²-18x³+x⁴,
31-142x+96x²-18x³+x⁴, -41-134x+96x²-18x³+x⁴,
-25-134x+96x²-18x³+x⁴, (-9+x)(1+15x-9x²+x³),
(-7+x)(-1+19x-11x²+x³), -113-126x+96x²-18x³+x⁴,
-97-126x+96x²-18x³+x⁴, (-9+x)(-3+x)(-3-6x+x²),
-65-126x+96x²-18x³+x⁴, (-7+x)(7+19x-11x²+x³),
(-5+x)(37+31x-13x²+x³), -169-118x+96x²-18x³+x⁴,
(-9+x)(17+15x-9x²+x³), -137-118x+96x²-18x³+x⁴,
-121-118x+96x²-18x³+x⁴, (-7+x)(-3+x)(-5-8x+x²),
(-5+x)(61+31x-13x²+x³), -289-94x+96x²-18x³+x⁴,
(-7+x)(39+19x-11x²+x³), (-7+x)(-5+x)(-11-6x+x²)};

```
In[*]:= warrantpoly = {31 - 142 x + 96 x^2 - 18 x^3 + x^4, (-7 + x) (-1 + 19 x - 11 x^2 + x^3)}
```

```
Out[*]:= {31 - 142 x + 96 x^2 - 18 x^3 + x^4, (-7 + x) (-1 + 19 x - 11 x^2 + x^3)}
```

```
In[*]:= anglesquared = anglesquaredmat[chi, list] // FullSimplify;
```

```
In[*]:= anglesquared // MatrixForm
```

```
Out[*] // MatrixForm =
```

$$\begin{pmatrix} \frac{35}{72} & \frac{7(57+5\sqrt{57})}{2736} & 0 & \frac{2}{9} & \frac{7}{48} - \frac{35}{48\sqrt{57}} \\ \frac{39}{80} & \frac{97}{672} + \frac{45\sqrt{\frac{3}{19}}}{224} & \frac{2}{35} & \frac{1}{6} & \frac{97}{672} - \frac{45\sqrt{\frac{3}{19}}}{224} \\ \frac{22}{45} & \frac{1}{7} + \frac{10}{21\sqrt{57}} & \frac{4}{35} & \frac{1}{9} & \frac{1}{7} - \frac{10}{21\sqrt{57}} \\ \frac{353}{720} & \frac{5(1083+47\sqrt{57})}{38304} & \frac{6}{35} & \frac{1}{18} & \frac{95}{672} - \frac{235}{672\sqrt{57}} \\ \frac{59}{120} & \frac{893+25\sqrt{57}}{6384} & \frac{8}{35} & 0 & \frac{893-25\sqrt{57}}{6384} \\ \frac{29}{60} & \frac{1}{168}(29+\sqrt{57}) & \frac{6}{35} & 0 & \frac{1}{168}(29-\sqrt{57}) \\ \frac{67}{144} & \frac{23}{96} + \frac{67}{96\sqrt{57}} & 0 & \frac{1}{18} & \frac{23}{96} - \frac{67}{96\sqrt{57}} \\ \frac{7}{15} & \frac{5}{21} + \frac{4}{7\sqrt{57}} & \frac{2}{35} & 0 & \frac{5}{21} - \frac{4}{7\sqrt{57}} \\ \frac{23}{48} & \frac{17}{96} + \frac{23}{32\sqrt{57}} & 0 & \frac{1}{6} & \frac{17}{96} - \frac{23}{32\sqrt{57}} \\ \frac{173}{360} & \frac{59}{336} + \frac{199}{336\sqrt{57}} & \frac{2}{35} & \frac{1}{9} & \frac{59}{336} - \frac{199}{336\sqrt{57}} \\ \frac{347}{720} & \frac{39}{224} + \frac{313}{672\sqrt{57}} & \frac{4}{35} & \frac{1}{18} & \frac{39}{224} - \frac{313}{672\sqrt{57}} \\ \frac{47}{90} & \frac{57+\sqrt{57}}{4788} & \frac{12}{35} & \frac{1}{9} & \frac{1}{84} - \frac{1}{84\sqrt{57}} \\ \frac{41}{80} & \frac{1}{672}(31+3\sqrt{57}) & \frac{8}{35} & \frac{1}{6} & \frac{1}{672}(31-3\sqrt{57}) \\ \frac{37}{72} & \frac{5}{112} + \frac{43}{336\sqrt{57}} & \frac{2}{7} & \frac{1}{9} & \frac{5}{112} - \frac{43}{336\sqrt{57}} \\ \frac{371}{720} & \frac{1653+\sqrt{57}}{38304} & \frac{12}{35} & \frac{1}{18} & \frac{29}{672} - \frac{1}{672\sqrt{57}} \\ \frac{31}{60} & \frac{1}{24} - \frac{1}{8\sqrt{57}} & \frac{2}{5} & 0 & \frac{1}{456}(19+\sqrt{57}) \\ \frac{181}{360} & \frac{9}{112} + \frac{167}{336\sqrt{57}} & \frac{4}{35} & \frac{2}{9} & \frac{9}{112} - \frac{167}{336\sqrt{57}} \\ \frac{121}{240} & \frac{53}{672} + \frac{83}{224\sqrt{57}} & \frac{6}{35} & \frac{1}{6} & \frac{53}{672} - \frac{83}{224\sqrt{57}} \\ \frac{91}{180} & \frac{741+41\sqrt{57}}{9576} & \frac{8}{35} & \frac{1}{9} & \frac{741-41\sqrt{57}}{9576} \\ \frac{73}{144} & \frac{17}{224} + \frac{79}{672\sqrt{57}} & \frac{2}{7} & \frac{1}{18} & \frac{17}{224} - \frac{79}{672\sqrt{57}} \\ \frac{61}{120} & \frac{475-\sqrt{57}}{6384} & \frac{12}{35} & 0 & \frac{475+\sqrt{57}}{6384} \\ \frac{71}{144} & \frac{11}{96} + \frac{71}{96\sqrt{57}} & 0 & \frac{5}{18} & \frac{11}{96} - \frac{71}{96\sqrt{57}} \\ \frac{89}{180} & \frac{1083+103\sqrt{57}}{9576} & \frac{2}{35} & \frac{2}{9} & \frac{1083-103\sqrt{57}}{9576} \\ \frac{119}{240} & \frac{25}{224} + \frac{109}{224\sqrt{57}} & \frac{4}{35} & \frac{1}{6} & \frac{25}{224} - \frac{109}{224\sqrt{57}} \\ \frac{179}{360} & \frac{37}{336} + \frac{121}{336\sqrt{57}} & \frac{6}{35} & \frac{1}{9} & \frac{37}{336} - \frac{121}{336\sqrt{57}} \\ \frac{359}{720} & \frac{73}{672} + \frac{157}{672\sqrt{57}} & \frac{8}{35} & \frac{1}{18} & \frac{73}{672} - \frac{157}{672\sqrt{57}} \\ \frac{1}{2} & \frac{1}{532}(57+\sqrt{57}) & \frac{2}{7} & 0 & \frac{1}{532}(57-\sqrt{57}) \\ \frac{17}{36} & \frac{5}{24} + \frac{17}{24\sqrt{57}} & 0 & \frac{1}{9} & \frac{5}{24} - \frac{17}{24\sqrt{57}} \\ \frac{341}{720} & \frac{7923+391\sqrt{57}}{38304} & \frac{2}{35} & \frac{1}{18} & \frac{7923-391\sqrt{57}}{38304} \\ \frac{19}{40} & \frac{437+17\sqrt{57}}{2128} & \frac{4}{35} & 0 & \frac{437-17\sqrt{57}}{2128} \\ \frac{11}{24} & \frac{1}{912}(247+11\sqrt{57}) & 0 & 0 & \frac{1}{912}(247-11\sqrt{57}) \end{pmatrix}$$

```
In[*]:= anglemat = Sqrt[anglesquared] // FullSimplify;
```


In[]:= anglemat // MatrixForm

Out[]:= MatrixForm=

$\frac{\sqrt{\frac{35}{2}}}{6}$	$\sqrt{\frac{7}{48} + \frac{35}{48\sqrt{57}}}$	0	$\frac{\sqrt{2}}{3}$	$\sqrt{\frac{7}{48} - \frac{35}{48\sqrt{57}}}$
$\frac{\sqrt{\frac{39}{5}}}{4}$	$\sqrt{\frac{97}{672} + \frac{45\sqrt{\frac{3}{19}}}{224}}$	$\sqrt{\frac{2}{35}}$	$\frac{1}{\sqrt{6}}$	$\sqrt{\frac{97}{672} - \frac{45\sqrt{\frac{3}{19}}}{224}}$
$\frac{\sqrt{\frac{22}{5}}}{3}$	$\sqrt{\frac{1}{7} + \frac{10}{21\sqrt{57}}}$	$\frac{2}{\sqrt{35}}$	$\frac{1}{3}$	$\sqrt{\frac{1}{7} - \frac{10}{21\sqrt{57}}}$
$\frac{\sqrt{\frac{353}{5}}}{12}$	$\sqrt{\frac{95}{672} + \frac{235}{672\sqrt{57}}}$	$\sqrt{\frac{6}{35}}$	$\frac{1}{3\sqrt{2}}$	$\sqrt{\frac{95}{672} - \frac{235}{672\sqrt{57}}}$
$\frac{\sqrt{\frac{59}{30}}}{2}$	$\sqrt{\frac{47}{336} + \frac{25}{112\sqrt{57}}}$	$2\sqrt{\frac{2}{35}}$	0	$\sqrt{0.332...}$
$\frac{\sqrt{\frac{29}{15}}}{2}$	$\sqrt{0.466...}$	$\sqrt{\frac{6}{35}}$	0	$\sqrt{0.357...}$
$\frac{\sqrt{\frac{67}{12}}}{12}$	$\sqrt{\frac{23}{96} + \frac{67}{96\sqrt{57}}}$	0	$\frac{1}{3\sqrt{2}}$	$\sqrt{\frac{23}{96} - \frac{67}{96\sqrt{57}}}$
$\sqrt{\frac{7}{15}}$	$\sqrt{\frac{5}{21} + \frac{4}{7\sqrt{57}}}$	$\sqrt{\frac{2}{35}}$	0	$\sqrt{\frac{5}{21} - \frac{4}{7\sqrt{57}}}$
$\frac{\sqrt{\frac{23}{3}}}{4}$	$\sqrt{\frac{17}{96} + \frac{23}{32\sqrt{57}}}$	0	$\frac{1}{\sqrt{6}}$	$\sqrt{\frac{17}{96} - \frac{23}{32\sqrt{57}}}$
$\frac{\sqrt{\frac{173}{10}}}{6}$	$\sqrt{\frac{59}{336} + \frac{199}{336\sqrt{57}}}$	$\sqrt{\frac{2}{35}}$	$\frac{1}{3}$	$\sqrt{\frac{59}{336} - \frac{199}{336\sqrt{57}}}$
$\frac{\sqrt{\frac{347}{5}}}{12}$	$\sqrt{\frac{39}{224} + \frac{313}{672\sqrt{57}}}$	$\frac{2}{\sqrt{35}}$	$\frac{1}{3\sqrt{2}}$	$\sqrt{\frac{39}{224} - \frac{313}{672\sqrt{57}}}$
$\frac{\sqrt{\frac{47}{10}}}{3}$	$\frac{1}{6}\sqrt{\frac{1}{133}(57 + \sqrt{57})}$	$2\sqrt{\frac{3}{35}}$	$\frac{1}{3}$	$\sqrt{\frac{1}{84} - \frac{1}{84\sqrt{57}}}$
$\frac{\sqrt{\frac{41}{5}}}{4}$	$\sqrt{0.283...}$	$2\sqrt{\frac{2}{35}}$	$\frac{1}{\sqrt{6}}$	$\sqrt{0.111...}$
$\frac{\sqrt{\frac{37}{2}}}{6}$	$\sqrt{\frac{5}{112} + \frac{43}{336\sqrt{57}}}$	$\sqrt{\frac{2}{7}}$	$\frac{1}{3}$	$\sqrt{\frac{5}{112} - \frac{43}{336\sqrt{57}}}$
$\frac{\sqrt{\frac{371}{5}}}{12}$	$\frac{1}{12}\sqrt{\frac{1}{266}(1653 + \sqrt{57})}$	$2\sqrt{\frac{3}{35}}$	$\frac{1}{3\sqrt{2}}$	$\sqrt{\frac{29}{672} - \frac{1}{672\sqrt{57}}}$
$\frac{\sqrt{\frac{31}{15}}}{2}$	$\sqrt{\frac{1}{24} - \frac{1}{8\sqrt{57}}}$	$\sqrt{\frac{2}{5}}$	0	$\sqrt{0.241...}$
$\frac{\sqrt{\frac{181}{10}}}{6}$	$\sqrt{\frac{9}{112} + \frac{167}{336\sqrt{57}}}$	$\frac{2}{\sqrt{35}}$	$\frac{\sqrt{2}}{3}$	$\sqrt{\frac{9}{112} - \frac{167}{336\sqrt{57}}}$
$\frac{11}{4\sqrt{15}}$	$\sqrt{\frac{53}{672} + \frac{83}{224\sqrt{57}}}$	$\sqrt{\frac{6}{35}}$	$\frac{1}{\sqrt{6}}$	$\sqrt{\frac{53}{672} - \frac{83}{224\sqrt{57}}}$
$\frac{\sqrt{\frac{91}{5}}}{6}$	$\sqrt{\frac{13}{168} + \frac{41}{168\sqrt{57}}}$	$2\sqrt{\frac{2}{35}}$	$\frac{1}{3}$	$\sqrt{0.212...}$
$\frac{\sqrt{73}}{12}$	$\sqrt{\frac{17}{224} + \frac{79}{672\sqrt{57}}}$	$\sqrt{\frac{2}{7}}$	$\frac{1}{3\sqrt{2}}$	$\sqrt{\frac{17}{224} - \frac{79}{672\sqrt{57}}}$
$\frac{\sqrt{\frac{61}{30}}}{2}$	$\sqrt{0.271...}$	$2\sqrt{\frac{3}{35}}$	0	$\frac{1}{4}\sqrt{\frac{1}{399}(475 + \sqrt{57})}$
$\frac{\sqrt{71}}{12}$	$\sqrt{\frac{11}{96} + \frac{71}{96\sqrt{57}}}$	0	$\frac{\sqrt{\frac{5}{2}}}{3}$	$\sqrt{\frac{11}{96} - \frac{71}{96\sqrt{57}}}$
$\frac{\sqrt{\frac{89}{5}}}{6}$	$\sqrt{\frac{19}{168} + \frac{103}{168\sqrt{57}}}$	$\sqrt{\frac{2}{35}}$	$\frac{\sqrt{2}}{3}$	$\sqrt{0.179...}$
$\frac{\sqrt{\frac{119}{15}}}{4}$	$\sqrt{0.420...}$	$\frac{2}{\sqrt{35}}$	$\frac{1}{\sqrt{6}}$	$\sqrt{0.217...}$

$\frac{\sqrt{\frac{179}{10}}}{6}$	$\sqrt{\frac{37}{336} + \frac{121}{336\sqrt{57}}}$	$\sqrt{\frac{6}{35}}$	$\frac{1}{3}$	$\sqrt{\frac{37}{336} - \frac{121}{336\sqrt{57}}}$
$\frac{\sqrt{\frac{359}{5}}}{12}$	$\sqrt{\frac{73}{672} + \frac{157}{672\sqrt{57}}}$	$2\sqrt{\frac{2}{35}}$	$\frac{1}{3\sqrt{2}}$	$\sqrt{\frac{73}{672} - \frac{157}{672\sqrt{57}}}$
$\frac{1}{\sqrt{2}}$	$\sqrt{0.348...}$	$\sqrt{\frac{2}{7}}$	0	$\sqrt{0.305...}$
$\frac{\sqrt{17}}{6}$	$\sqrt{\frac{5}{24} + \frac{17}{24\sqrt{57}}}$	0	$\frac{1}{3}$	$\sqrt{\frac{5}{24} - \frac{17}{24\sqrt{57}}}$
$\frac{\sqrt{\frac{341}{5}}}{12}$	$\sqrt{\frac{139}{672} + \frac{391}{672\sqrt{57}}}$	$\sqrt{\frac{2}{35}}$	$\frac{1}{3\sqrt{2}}$	$\sqrt{0.360...}$
$\frac{\sqrt{\frac{19}{10}}}{2}$	$\sqrt{0.515...}$	$\frac{2}{\sqrt{35}}$	0	$\sqrt{0.381...}$
$\frac{\sqrt{\frac{11}{6}}}{2}$	$\sqrt{\frac{13}{48} + \frac{11}{16\sqrt{57}}}$	0	0	$\frac{1}{4}\sqrt{\frac{13}{3} - \frac{11}{\sqrt{57}}}$

In[]:= **chi**

Out[]:= $(-7 + x)^2 (-5 + x)^{10} (5 + x)^{15} (16 - 11x + x^2)$

In[]:= **coeff[chi, (x + 5) (x - 5) (x - 7)] // FullSimplify**

Out[]:= $\left\{-\frac{3}{2}(-85 + \sqrt{57}), \frac{3}{2}(85 + \sqrt{57})\right\}$

In[]:= **combinationangle** $\left[\left\{-\frac{3}{2}(-85 + \sqrt{57}), \frac{3}{2}(85 + \sqrt{57})\right\}, \{12, 16\}, \{2, 5\}, \text{anglemat}\right] // \text{FullSimplify}$

Out[]:= $\left\{\sqrt{\frac{1}{57}(921 + 128\sqrt{42})}, \sqrt{-1.27...}\right\}$

In[]:= **RootReduce** $\left[\sqrt{\frac{1}{57}(921 + 128\sqrt{42})}\right]$

Out[]:= $\sqrt{5.54...}$

combinations[chi, (x + 5) (x - 5) (x - 7), warrantpoly[[1], warrantpoly[[2], list, anglesquared] // FullSimplify

$\left\{\sqrt{\frac{1}{57}(921 + 128\sqrt{42})}, \text{Root}[2809 - 1842\sqrt{1^2} + 57\sqrt{1^4} \&, 2]\right\}$

compatible[combinations[chi, (x + 5) (x - 5) (x - 7), warrantpoly[[1], warrantpoly[[2], list, anglesquared] // FullSimplify]

0

In[*]:= **chi** = $(-7 + x)^2 (-5 + x)^9 (-3 + x) (5 + x)^{15} (32 - 13x + x^2)$

Out[*]:= $(-7 + x)^2 (-5 + x)^9 (-3 + x) (5 + x)^{15} (32 - 13x + x^2)$

CoefficientList[feasibleinterlacingpolylist[chi], x]

```
{{-219, 853, -638, 186, -23, 1},
 {-3, 757, -630, 186, -23, 1}, {-51, 773, -630, 186, -23, 1},
 {-99, 789, -630, 186, -23, 1}, {-147, 805, -630, 186, -23, 1},
 {165, 677, -622, 186, -23, 1}, {117, 693, -622, 186, -23, 1},
 {69, 709, -622, 186, -23, 1}, {21, 725, -622, 186, -23, 1},
 {365, 597, -614, 186, -23, 1}, {285, 613, -614, 186, -23, 1},
 {237, 629, -614, 186, -23, 1}, {189, 645, -614, 186, -23, 1},
 {485, 533, -606, 186, -23, 1}, {405, 549, -606, 186, -23, 1},
 {437, 549, -606, 186, -23, 1}, {357, 565, -606, 186, -23, 1},
 {605, 469, -598, 186, -23, 1}, {525, 485, -598, 186, -23, 1}}
```

```
A = {{-219, 853, -638, 186, -23, 1},
 {-3, 757, -630, 186, -23, 1}, {-51, 773, -630, 186, -23, 1},
 {-99, 789, -630, 186, -23, 1}, {-147, 805, -630, 186, -23, 1},
 {165, 677, -622, 186, -23, 1}, {117, 693, -622, 186, -23, 1},
 {69, 709, -622, 186, -23, 1}, {21, 725, -622, 186, -23, 1},
 {365, 597, -614, 186, -23, 1}, {285, 613, -614, 186, -23, 1},
 {237, 629, -614, 186, -23, 1}, {189, 645, -614, 186, -23, 1},
 {485, 533, -606, 186, -23, 1}, {405, 549, -606, 186, -23, 1},
 {437, 549, -606, 186, -23, 1}, {357, 565, -606, 186, -23, 1},
 {605, 469, -598, 186, -23, 1}, {525, 485, -598, 186, -23, 1}};
```

A // MatrixForm

```
( -219 853 -638 186 -23 1
  -3  757 -630 186 -23 1
  -51 773 -630 186 -23 1
  -99 789 -630 186 -23 1
 -147 805 -630 186 -23 1
  165 677 -622 186 -23 1
  117 693 -622 186 -23 1
   69 709 -622 186 -23 1
   21 725 -622 186 -23 1
  365 597 -614 186 -23 1
  285 613 -614 186 -23 1
  237 629 -614 186 -23 1
  189 645 -614 186 -23 1
  485 533 -606 186 -23 1
  405 549 -606 186 -23 1
  437 549 -606 186 -23 1
  357 565 -606 186 -23 1
  605 469 -598 186 -23 1
  525 485 -598 186 -23 1)
```

g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]

```
{-2935, 22993, -18286, 5394, -667, 29}
```

```

FindInstance[n[1] ≥ 0 && n[2] ≥ 0 && n[3] ≥ 0 && n[4] ≥ 0 && n[5] ≥ 0 &&
  n[6] ≥ 0 && n[7] ≥ 0 && n[8] ≥ 0 && n[9] ≥ 0 && n[10] ≥ 0 && n[11] ≥ 0 &&
  n[12] ≥ 0 && n[13] ≥ 0 && n[14] ≥ 0 && n[15] ≥ 0 && n[16] ≥ 0 && n[17] ≥ 0 &&
  n[18] ≥ 0 && n[19] ≥ 0 && Array[n, 19].A == g, Array[n, 19], Integers]
{{n[1] → 14, n[2] → 0, n[3] → 0, n[4] → 0, n[5] → 11, n[6] → 0,
  n[7] → 0, n[8] → 0, n[9] → 0, n[10] → 0, n[11] → 0, n[12] → 0, n[13] → 0,
  n[14] → 0, n[15] → 0, n[16] → 4, n[17] → 0, n[18] → 0, n[19] → 0}}

```

Array[c, 6].Transpose[A]

```

{-219 c[1] + 853 c[2] - 638 c[3] + 186 c[4] - 23 c[5] + c[6],
 -3 c[1] + 757 c[2] - 630 c[3] + 186 c[4] - 23 c[5] + c[6],
 -51 c[1] + 773 c[2] - 630 c[3] + 186 c[4] - 23 c[5] + c[6],
 -99 c[1] + 789 c[2] - 630 c[3] + 186 c[4] - 23 c[5] + c[6],
 -147 c[1] + 805 c[2] - 630 c[3] + 186 c[4] - 23 c[5] + c[6],
 165 c[1] + 677 c[2] - 622 c[3] + 186 c[4] - 23 c[5] + c[6],
 117 c[1] + 693 c[2] - 622 c[3] + 186 c[4] - 23 c[5] + c[6],
 69 c[1] + 709 c[2] - 622 c[3] + 186 c[4] - 23 c[5] + c[6],
 21 c[1] + 725 c[2] - 622 c[3] + 186 c[4] - 23 c[5] + c[6],
 365 c[1] + 597 c[2] - 614 c[3] + 186 c[4] - 23 c[5] + c[6],
 285 c[1] + 613 c[2] - 614 c[3] + 186 c[4] - 23 c[5] + c[6],
 237 c[1] + 629 c[2] - 614 c[3] + 186 c[4] - 23 c[5] + c[6],
 189 c[1] + 645 c[2] - 614 c[3] + 186 c[4] - 23 c[5] + c[6],
 485 c[1] + 533 c[2] - 606 c[3] + 186 c[4] - 23 c[5] + c[6],
 405 c[1] + 549 c[2] - 606 c[3] + 186 c[4] - 23 c[5] + c[6],
 437 c[1] + 549 c[2] - 606 c[3] + 186 c[4] - 23 c[5] + c[6],
 357 c[1] + 565 c[2] - 606 c[3] + 186 c[4] - 23 c[5] + c[6],
 605 c[1] + 469 c[2] - 598 c[3] + 186 c[4] - 23 c[5] + c[6],
 525 c[1] + 485 c[2] - 598 c[3] + 186 c[4] - 23 c[5] + c[6]}

```

Array[c, 6].g

```

-2935 c[1] + 22993 c[2] - 18286 c[3] + 5394 c[4] - 667 c[5] + 29 c[6]

```

```

warrant1 = Flatten[Array[c, 6] /. FindInstance[
  -2935 c[1] + 22993 c[2] - 18286 c[3] + 5394 c[4] - 667 c[5] + 29 c[6] < 0 &&
  -219 c[1] + 853 c[2] - 638 c[3] + 186 c[4] - 23 c[5] + c[6] < 0 &&
  -3 c[1] + 757 c[2] - 630 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  -51 c[1] + 773 c[2] - 630 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  -99 c[1] + 789 c[2] - 630 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  -147 c[1] + 805 c[2] - 630 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  165 c[1] + 677 c[2] - 622 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  117 c[1] + 693 c[2] - 622 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  69 c[1] + 709 c[2] - 622 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  21 c[1] + 725 c[2] - 622 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  365 c[1] + 597 c[2] - 614 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  285 c[1] + 613 c[2] - 614 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  237 c[1] + 629 c[2] - 614 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  189 c[1] + 645 c[2] - 614 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  485 c[1] + 533 c[2] - 606 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  405 c[1] + 549 c[2] - 606 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  437 c[1] + 549 c[2] - 606 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  357 c[1] + 565 c[2] - 606 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  605 c[1] + 469 c[2] - 598 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 && 525 c[1] +
    485 c[2] - 598 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0, Array[c, 6], Integers]]
{-235, -703, -845, 0, 0, 0}

GCD[-235, -703, -845, 0, 0, 0]
1

Reverse[warrant1]
{0, 0, 0, -845, -703, -235}

warrant1.g
-22684

warrant1.Transpose[A]
{-9084, 884, 916, 948, 980, 10884, 10916, 10948, 10980, 13364,
  20916, 20948, 20980, 23396, 30948, 23428, 30980, 33428, 40980}

```

```

warrant2 = Flatten[Array[c, 6] /. FindInstance[
  -2935 c[1] + 22993 c[2] - 18286 c[3] + 5394 c[4] - 667 c[5] + 29 c[6] < 0 &&
  -219 c[1] + 853 c[2] - 638 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  -3 c[1] + 757 c[2] - 630 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  -51 c[1] + 773 c[2] - 630 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  -99 c[1] + 789 c[2] - 630 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  -147 c[1] + 805 c[2] - 630 c[3] + 186 c[4] - 23 c[5] + c[6] < 0 &&
  165 c[1] + 677 c[2] - 622 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  117 c[1] + 693 c[2] - 622 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  69 c[1] + 709 c[2] - 622 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  21 c[1] + 725 c[2] - 622 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  365 c[1] + 597 c[2] - 614 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  285 c[1] + 613 c[2] - 614 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  237 c[1] + 629 c[2] - 614 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  189 c[1] + 645 c[2] - 614 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  485 c[1] + 533 c[2] - 606 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  405 c[1] + 549 c[2] - 606 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  437 c[1] + 549 c[2] - 606 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  357 c[1] + 565 c[2] - 606 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  605 c[1] + 469 c[2] - 598 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 && 525 c[1] +
    485 c[2] - 598 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0, Array[c, 6], Integers]]
{-433, -1593, -6261, 0, 0, -2729736}

GCD[-433, -1593, -6261, 0, 0, -2729736]
1

Reverse[warrant2]
{-2729736, 0, 0, -6261, -1593, -433}

warrant2.g
-30692

warrant2.Transpose[A]
{780, 10092, 5388, 684, -4020, 14700, 9996, 5292, 588,
  5452, 14604, 9900, 5196, 5356, 14508, 652, 9804, 5260, 14412}

```

```
feasibleinterlacingpolylist[chi]
```

```
{ (-3 + x) (73 - 260 x + 126 x^2 - 20 x^3 + x^4),  
  (-3 + x) (1 - 252 x + 126 x^2 - 20 x^3 + x^4), (-3 + x) (17 - 252 x + 126 x^2 - 20 x^3 + x^4),  
  (-3 + x) (33 - 252 x + 126 x^2 - 20 x^3 + x^4), (-7 + x) (-3 + x) (-7 + 35 x - 13 x^2 + x^3),  
  (-5 + x) (-3 + x) (11 + 51 x - 15 x^2 + x^3), (-3 + x) (-39 - 244 x + 126 x^2 - 20 x^3 + x^4),  
  (-3 + x) (-23 - 244 x + 126 x^2 - 20 x^3 + x^4), (-7 + x) (-3 + x) (1 + 35 x - 13 x^2 + x^3),  
  (-5 + x) (-73 - 134 x + 96 x^2 - 18 x^3 + x^4), (-5 + x) (-3 + x) (19 + 51 x - 15 x^2 + x^3),  
  (-3 + x) (-79 - 236 x + 126 x^2 - 20 x^3 + x^4), (-9 + x) (-7 + x) (-3 + x) (-1 - 4 x + x^2),  
  (-5 + x) (-97 - 126 x + 96 x^2 - 18 x^3 + x^4), (-9 + x) (-5 + x) (-3 + x) (-3 - 6 x + x^2),  
  437 + 549 x - 606 x^2 + 186 x^3 - 23 x^4 + x^5, (-7 + x) (-3 + x) (17 + 35 x - 13 x^2 + x^3),  
  (-5 + x) (-121 - 118 x + 96 x^2 - 18 x^3 + x^4), (-7 + x) (-5 + x) (-3 + x) (-5 - 8 x + x^2) }
```

```
list = { (-3 + x) (73 - 260 x + 126 x^2 - 20 x^3 + x^4),  
  (-3 + x) (1 - 252 x + 126 x^2 - 20 x^3 + x^4), (-3 + x) (17 - 252 x + 126 x^2 - 20 x^3 + x^4),  
  (-3 + x) (33 - 252 x + 126 x^2 - 20 x^3 + x^4), (-7 + x) (-3 + x) (-7 + 35 x - 13 x^2 + x^3),  
  (-5 + x) (-3 + x) (11 + 51 x - 15 x^2 + x^3), (-3 + x) (-39 - 244 x + 126 x^2 - 20 x^3 + x^4),  
  (-3 + x) (-23 - 244 x + 126 x^2 - 20 x^3 + x^4), (-7 + x) (-3 + x) (1 + 35 x - 13 x^2 + x^3),  
  (-5 + x) (-73 - 134 x + 96 x^2 - 18 x^3 + x^4), (-5 + x) (-3 + x) (19 + 51 x - 15 x^2 + x^3),  
  (-3 + x) (-79 - 236 x + 126 x^2 - 20 x^3 + x^4), (-9 + x) (-7 + x) (-3 + x) (-1 - 4 x + x^2),  
  (-5 + x) (-97 - 126 x + 96 x^2 - 18 x^3 + x^4), (-9 + x) (-5 + x) (-3 + x) (-3 - 6 x + x^2),  
  437 + 549 x - 606 x^2 + 186 x^3 - 23 x^4 + x^5, (-7 + x) (-3 + x) (17 + 35 x - 13 x^2 + x^3),  
  (-5 + x) (-121 - 118 x + 96 x^2 - 18 x^3 + x^4), (-7 + x) (-5 + x) (-3 + x) (-5 - 8 x + x^2) };
```

```
warrantpoly =
```

```
{ (-3 + x) (73 - 260 x + 126 x^2 - 20 x^3 + x^4), (-7 + x) (-3 + x) (-7 + 35 x - 13 x^2 + x^3) }  
{ (-3 + x) (73 - 260 x + 126 x^2 - 20 x^3 + x^4), (-7 + x) (-3 + x) (-7 + 35 x - 13 x^2 + x^3) }
```

```
anglesquared = anglesquaredmat[chi, list] // FullSimplify;
```

anglesquared // MatrixForm

$$\left(\begin{array}{cc} \frac{478}{915} & 0 \\ \frac{157}{305} & 0 \\ \frac{472}{915} & 0 \\ \frac{473}{915} & 0 \\ \frac{158}{305} & 0 \\ \frac{31}{61} & 0 \\ \frac{466}{915} & 0 \\ \frac{467}{915} & 0 \\ \frac{156}{305} & 0 \\ \frac{367}{732} & \frac{1}{4} \\ \frac{92}{183} & 0 \\ \frac{461}{915} & 0 \\ \frac{154}{305} & 0 \\ \frac{121}{244} & \frac{1}{4} \\ \frac{91}{183} & 0 \\ \frac{1819}{3660} & \frac{1}{4} \\ \frac{152}{305} & 0 \\ \frac{359}{732} & \frac{1}{4} \\ \frac{30}{61} & 0 \end{array} \begin{array}{c} \frac{1107+133\sqrt{41}}{50020} \\ \frac{4633+647\sqrt{41}}{50020} \\ \frac{943+102\sqrt{41}}{12505} \\ \frac{2911+169\sqrt{41}}{50020} \\ \frac{205-7\sqrt{41}}{5002} \\ \frac{89}{610} + \frac{461}{610\sqrt{41}} \\ \frac{6437+683\sqrt{41}}{50020} \\ \frac{34}{305} + \frac{111}{305\sqrt{41}} \\ \frac{1}{244} (23 + \sqrt{41}) \\ \frac{205-7\sqrt{41}}{5002} \\ \frac{4551+479\sqrt{41}}{25010} \\ \frac{8241+719\sqrt{41}}{50020} \\ \frac{9}{61} + \frac{24}{61\sqrt{41}} \\ \frac{47}{610} - \frac{17}{610\sqrt{41}} \\ \frac{7(779+71\sqrt{41})}{25010} \\ \frac{2993-273\sqrt{41}}{50020} \\ \frac{49}{244} + \frac{151}{244\sqrt{41}} \\ \frac{2829+\sqrt{41}}{25010} \\ \frac{1271+103\sqrt{41}}{5002} \end{array} \begin{array}{cc} \frac{3}{10} & \frac{2}{15} \\ \frac{1}{10} & \frac{1}{5} \\ \frac{1}{10} & \frac{2}{15} \\ \frac{3}{10} & \frac{1}{15} \\ \frac{2}{10} & 0 \\ 0 & \frac{1}{5} \\ \frac{1}{10} & \frac{2}{15} \\ \frac{1}{5} & \frac{1}{15} \\ \frac{3}{10} & 0 \\ 0 & \frac{1}{6} \\ 0 & \frac{2}{15} \\ \frac{1}{10} & \frac{1}{15} \\ \frac{1}{5} & 0 \\ 0 & \frac{1}{10} \\ 0 & \frac{1}{15} \\ \frac{1}{10} & \frac{1}{30} \\ \frac{1}{10} & 0 \\ 0 & \frac{1}{30} \\ 0 & 0 \end{array} \begin{array}{c} \frac{1107-133\sqrt{41}}{50020} \\ \frac{4633-647\sqrt{41}}{50020} \\ \frac{943-102\sqrt{41}}{12505} \\ \frac{2911-169\sqrt{41}}{50020} \\ \frac{205+7\sqrt{41}}{5002} \\ \frac{89}{610} - \frac{461}{610\sqrt{41}} \\ \frac{6437-683\sqrt{41}}{50020} \\ \frac{34}{305} - \frac{111}{305\sqrt{41}} \\ \frac{1}{244} (23 - \sqrt{41}) \\ \frac{205+7\sqrt{41}}{5002} \\ \frac{4551-479\sqrt{41}}{25010} \\ \frac{8241-719\sqrt{41}}{50020} \\ \frac{9}{61} - \frac{24}{61\sqrt{41}} \\ \frac{47}{610} + \frac{17}{610\sqrt{41}} \\ \frac{7(-779+71\sqrt{41})}{25010} \\ \frac{2993+273\sqrt{41}}{50020} \\ \frac{49}{244} - \frac{151}{244\sqrt{41}} \\ \frac{69}{610} - \frac{1}{610\sqrt{41}} \\ \frac{1271-103\sqrt{41}}{5002} \end{array} \right)$$

combinations[chi, (x + 5) (x - 5) (x - 7), warrantpoly[[1],
warrantpoly[[2]], list, anglesquared] // FullSimplify

$$\left\{ \sqrt{\frac{5}{41}} (101 + 64\sqrt{2}), -\sqrt{\frac{5}{41}} (101 - 64\sqrt{2}), \right. \\ \left. \sqrt{\frac{5}{41}} (101 - 64\sqrt{2}), -\sqrt{\frac{5}{41}} (101 + 64\sqrt{2}) \right\}$$

compatible[combinations[chi, (x + 5) (x - 5) (x - 7),
warrantpoly[[1], warrantpoly[[2]], list, anglesquared] // FullSimplify]

0

$$\text{chi} = (-7 + x) (-5 + x)^{10} (5 + x)^{15} (-128 + 93x - 18x^2 + x^3) \\ (-7 + x) (-5 + x)^{10} (5 + x)^{15} (-128 + 93x - 18x^2 + x^3)$$

`CoefficientList[feasibleinterlacingpolylist[chi], x]`

```
{ {1575, 545, -782, 222, -25, 1},
  {-137, 1121, -830, 222, -25, 1}, {-105, 1121, -830, 222, -25, 1},
  {-249, 1137, -830, 222, -25, 1}, {-217, 1137, -830, 222, -25, 1},
  {-329, 1153, -830, 222, -25, 1}, {223, 1009, -822, 222, -25, 1},
  {255, 1009, -822, 222, -25, 1}, {143, 1025, -822, 222, -25, 1},
  {175, 1025, -822, 222, -25, 1}, {31, 1041, -822, 222, -25, 1},
  {63, 1041, -822, 222, -25, 1}, {-49, 1057, -822, 222, -25, 1},
  {-161, 1073, -822, 222, -25, 1}, {695, 881, -814, 222, -25, 1},
  {615, 897, -814, 222, -25, 1}, {503, 913, -814, 222, -25, 1},
  {535, 913, -814, 222, -25, 1}, {423, 929, -814, 222, -25, 1},
  {455, 929, -814, 222, -25, 1}, {343, 945, -814, 222, -25, 1},
  {231, 961, -814, 222, -25, 1}, {975, 785, -806, 222, -25, 1},
  {895, 801, -806, 222, -25, 1}, {815, 817, -806, 222, -25, 1},
  {703, 833, -806, 222, -25, 1}, {735, 833, -806, 222, -25, 1},
  {623, 849, -806, 222, -25, 1}, {511, 865, -806, 222, -25, 1},
  {1175, 705, -798, 222, -25, 1}, {1095, 721, -798, 222, -25, 1},
  {983, 737, -798, 222, -25, 1}, {1015, 737, -798, 222, -25, 1},
  {903, 753, -798, 222, -25, 1}, {1375, 625, -790, 222, -25, 1},
  {1295, 641, -790, 222, -25, 1}, {1183, 657, -790, 222, -25, 1},
  {1655, 529, -782, 222, -25, 1}, {1463, 561, -782, 222, -25, 1},
  {1855, 449, -774, 222, -25, 1}, {2135, 353, -766, 222, -25, 1}}
```

```
A = { {-137, 1121, -830, 222, -25, 1},
  {-105, 1121, -830, 222, -25, 1}, {-249, 1137, -830, 222, -25, 1},
  {-217, 1137, -830, 222, -25, 1}, {-329, 1153, -830, 222, -25, 1},
  {223, 1009, -822, 222, -25, 1}, {255, 1009, -822, 222, -25, 1},
  {143, 1025, -822, 222, -25, 1}, {175, 1025, -822, 222, -25, 1},
  {31, 1041, -822, 222, -25, 1}, {63, 1041, -822, 222, -25, 1},
  {-49, 1057, -822, 222, -25, 1}, {-161, 1073, -822, 222, -25, 1},
  {695, 881, -814, 222, -25, 1}, {615, 897, -814, 222, -25, 1},
  {503, 913, -814, 222, -25, 1}, {535, 913, -814, 222, -25, 1},
  {423, 929, -814, 222, -25, 1}, {455, 929, -814, 222, -25, 1},
  {343, 945, -814, 222, -25, 1}, {231, 961, -814, 222, -25, 1},
  {975, 785, -806, 222, -25, 1}, {895, 801, -806, 222, -25, 1},
  {815, 817, -806, 222, -25, 1}, {703, 833, -806, 222, -25, 1},
  {735, 833, -806, 222, -25, 1}, {623, 849, -806, 222, -25, 1},
  {511, 865, -806, 222, -25, 1}, {1175, 705, -798, 222, -25, 1},
  {1095, 721, -798, 222, -25, 1}, {983, 737, -798, 222, -25, 1},
  {1015, 737, -798, 222, -25, 1}, {903, 753, -798, 222, -25, 1},
  {1375, 625, -790, 222, -25, 1}, {1295, 641, -790, 222, -25, 1},
  {1183, 657, -790, 222, -25, 1}, {1655, 529, -782, 222, -25, 1},
  {1575, 545, -782, 222, -25, 1}, {1463, 561, -782, 222, -25, 1},
  {1855, 449, -774, 222, -25, 1}, {2135, 353, -766, 222, -25, 1}};
```

A // MatrixForm

```
( -137 1121 -830 222 -25 1 )
( -105 1121 -830 222 -25 1 )
( -249 1137 -830 222 -25 1 )
( -217 1137 -830 222 -25 1 )
( -329 1153 -830 222 -25 1 )
( 223 1009 -822 222 -25 1 )
( 255 1009 -822 222 -25 1 )
( 143 1025 -822 222 -25 1 )
( 175 1025 -822 222 -25 1 )
( 31 1041 -822 222 -25 1 )
( 63 1041 -822 222 -25 1 )
( -49 1057 -822 222 -25 1 )
( -161 1073 -822 222 -25 1 )
( 695 881 -814 222 -25 1 )
( 615 897 -814 222 -25 1 )
( 503 913 -814 222 -25 1 )
( 535 913 -814 222 -25 1 )
( 423 929 -814 222 -25 1 )
( 455 929 -814 222 -25 1 )
( 343 945 -814 222 -25 1 )
( 231 961 -814 222 -25 1 )
( 975 785 -806 222 -25 1 )
( 895 801 -806 222 -25 1 )
( 815 817 -806 222 -25 1 )
( 703 833 -806 222 -25 1 )
( 735 833 -806 222 -25 1 )
( 623 849 -806 222 -25 1 )
( 511 865 -806 222 -25 1 )
( 1175 705 -798 222 -25 1 )
( 1095 721 -798 222 -25 1 )
( 983 737 -798 222 -25 1 )
( 1015 737 -798 222 -25 1 )
( 903 753 -798 222 -25 1 )
( 1375 625 -790 222 -25 1 )
( 1295 641 -790 222 -25 1 )
( 1183 657 -790 222 -25 1 )
( 1655 529 -782 222 -25 1 )
( 1575 545 -782 222 -25 1 )
( 1463 561 -782 222 -25 1 )
( 1855 449 -774 222 -25 1 )
( 2135 353 -766 222 -25 1 )
```

g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]

```
{-2925, 30925, -23854, 6438, -725, 29}
```

```

FindInstance[n[1] ≥ 0 && n[2] ≥ 0 && n[3] ≥ 0 && n[4] ≥ 0 && n[5] ≥ 0 && n[6] ≥ 0 &&
  n[7] ≥ 0 && n[8] ≥ 0 && n[9] ≥ 0 && n[10] ≥ 0 && n[11] ≥ 0 && n[12] ≥ 0 && n[13] ≥ 0 &&
  n[14] ≥ 0 && n[15] ≥ 0 && n[16] ≥ 0 && n[17] ≥ 0 && n[18] ≥ 0 && n[19] ≥ 0 && n[20] ≥ 0 &&
  n[21] ≥ 0 && n[22] ≥ 0 && n[23] ≥ 0 && n[24] ≥ 0 && n[25] ≥ 0 && n[26] ≥ 0 &&
  n[27] ≥ 0 && n[28] ≥ 0 && n[29] ≥ 0 && n[30] ≥ 0 && n[31] ≥ 0 && n[32] ≥ 0 &&
  n[33] ≥ 0 && n[34] ≥ 0 && n[35] ≥ 0 && n[36] ≥ 0 && n[37] ≥ 0 && n[38] ≥ 0 &&
  n[39] ≥ 0 && n[40] ≥ 0 && n[41] ≥ 0 && Array[n, 41].A == g, Array[n, 41], Integers]

{ {n[1] → 0, n[2] → 0, n[3] → 6, n[4] → 0, n[5] → 0, n[6] → 0, n[7] → 0,
  n[8] → 0, n[9] → 0, n[10] → 0, n[11] → 0, n[12] → 0, n[13] → 21, n[14] → 0,
  n[15] → 0, n[16] → 0, n[17] → 0, n[18] → 0, n[19] → 0, n[20] → 0, n[21] → 0,
  n[22] → 2, n[23] → 0, n[24] → 0, n[25] → 0, n[26] → 0, n[27] → 0, n[28] → 0,
  n[29] → 0, n[30] → 0, n[31] → 0, n[32] → 0, n[33] → 0, n[34] → 0, n[35] → 0,
  n[36] → 0, n[37] → 0, n[38] → 0, n[39] → 0, n[40] → 0, n[41] → 0} }

```

Array[c, 6].Transpose[A]

```
{ -137 c[1] + 1121 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6],
  -105 c[1] + 1121 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6],
  -249 c[1] + 1137 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6],
  -217 c[1] + 1137 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6],
  -329 c[1] + 1153 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6],
  223 c[1] + 1009 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6],
  255 c[1] + 1009 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6],
  143 c[1] + 1025 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6],
  175 c[1] + 1025 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6],
  31 c[1] + 1041 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6],
  63 c[1] + 1041 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6],
  -49 c[1] + 1057 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6],
  -161 c[1] + 1073 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6],
  695 c[1] + 881 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6],
  615 c[1] + 897 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6],
  503 c[1] + 913 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6],
  535 c[1] + 913 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6],
  423 c[1] + 929 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6],
  455 c[1] + 929 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6],
  343 c[1] + 945 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6],
  231 c[1] + 961 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6],
  975 c[1] + 785 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6],
  895 c[1] + 801 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6],
  815 c[1] + 817 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6],
  703 c[1] + 833 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6],
  735 c[1] + 833 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6],
  623 c[1] + 849 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6],
  511 c[1] + 865 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6],
  1175 c[1] + 705 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6],
  1095 c[1] + 721 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6],
  983 c[1] + 737 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6],
  1015 c[1] + 737 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6],
  903 c[1] + 753 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6],
  1375 c[1] + 625 c[2] - 790 c[3] + 222 c[4] - 25 c[5] + c[6],
  1295 c[1] + 641 c[2] - 790 c[3] + 222 c[4] - 25 c[5] + c[6],
  1183 c[1] + 657 c[2] - 790 c[3] + 222 c[4] - 25 c[5] + c[6],
  1655 c[1] + 529 c[2] - 782 c[3] + 222 c[4] - 25 c[5] + c[6],
  1575 c[1] + 545 c[2] - 782 c[3] + 222 c[4] - 25 c[5] + c[6],
  1463 c[1] + 561 c[2] - 782 c[3] + 222 c[4] - 25 c[5] + c[6],
  1855 c[1] + 449 c[2] - 774 c[3] + 222 c[4] - 25 c[5] + c[6],
  2135 c[1] + 353 c[2] - 766 c[3] + 222 c[4] - 25 c[5] + c[6] }
```

Array[c, 6].g

```
-2925 c[1] + 30925 c[2] - 23854 c[3] + 6438 c[4] - 725 c[5] + 29 c[6]
```

```

warrant1 = Flatten[Array[c, 6] /. FindInstance[
  -2925 c[1] + 30925 c[2] - 23854 c[3] + 6438 c[4] - 725 c[5] + 29 c[6] < 0 &&
  -137 c[1] + 1121 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  -105 c[1] + 1121 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  -249 c[1] + 1137 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6] < 0 &&
  -217 c[1] + 1137 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  -329 c[1] + 1153 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  223 c[1] + 1009 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  255 c[1] + 1009 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  143 c[1] + 1025 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  175 c[1] + 1025 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  31 c[1] + 1041 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  63 c[1] + 1041 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  -49 c[1] + 1057 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  -161 c[1] + 1073 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  695 c[1] + 881 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  615 c[1] + 897 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  503 c[1] + 913 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  535 c[1] + 913 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  423 c[1] + 929 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  455 c[1] + 929 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  343 c[1] + 945 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  231 c[1] + 961 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  975 c[1] + 785 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  895 c[1] + 801 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  815 c[1] + 817 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  703 c[1] + 833 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  735 c[1] + 833 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  623 c[1] + 849 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  511 c[1] + 865 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1175 c[1] + 705 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1095 c[1] + 721 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  983 c[1] + 737 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1015 c[1] + 737 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  903 c[1] + 753 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1375 c[1] + 625 c[2] - 790 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1295 c[1] + 641 c[2] - 790 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1183 c[1] + 657 c[2] - 790 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1655 c[1] + 529 c[2] - 782 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1575 c[1] + 545 c[2] - 782 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1463 c[1] + 561 c[2] - 782 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1855 c[1] + 449 c[2] - 774 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 && 2135 c[1] +
    353 c[2] - 766 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0, Array[c, 6], Integers]]
{2066, 12395, 80553, 0, 0, 53248032}

```

GCD[2066, 12 395, 80 553, 0, 0, 53 248 032]

1

Reverse[warrant1]

{53 248 032, 0, 0, 80 553, 12 395, 2066}

warrant1.g

–46 009

warrant1.Transpose[A]

{795, 66 907, –32 277, 33 835, 763, 739, 66 851, 33 779, 99 891, 707, 66 819, 33 747, 675,
33 755, 66 795, 33 723, 99 835, 66 763, 132 875, 99 803, 66 731, 66 739, 99 779,
132 819, 99 747, 165 859, 132 787, 99 715, 132 763, 165 803, 132 731, 198 843,
165 771, 198 787, 231 827, 198 755, 231 771, 264 811, 231 739, 297 795, 330 779}

```

warrant2 = Flatten[Array[c, 6] /. FindInstance[
  -2925 c[1] + 30925 c[2] - 23854 c[3] + 6438 c[4] - 725 c[5] + 29 c[6] < 0 &&
  -137 c[1] + 1121 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  -105 c[1] + 1121 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  -249 c[1] + 1137 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  -217 c[1] + 1137 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  -329 c[1] + 1153 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  223 c[1] + 1009 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  255 c[1] + 1009 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  143 c[1] + 1025 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  175 c[1] + 1025 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  31 c[1] + 1041 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  63 c[1] + 1041 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  -49 c[1] + 1057 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  -161 c[1] + 1073 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6] < 0 &&
  695 c[1] + 881 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  615 c[1] + 897 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  503 c[1] + 913 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  535 c[1] + 913 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  423 c[1] + 929 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  455 c[1] + 929 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  343 c[1] + 945 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  231 c[1] + 961 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  975 c[1] + 785 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  895 c[1] + 801 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  815 c[1] + 817 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  703 c[1] + 833 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  735 c[1] + 833 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  623 c[1] + 849 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  511 c[1] + 865 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1175 c[1] + 705 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1095 c[1] + 721 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  983 c[1] + 737 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1015 c[1] + 737 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  903 c[1] + 753 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1375 c[1] + 625 c[2] - 790 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1295 c[1] + 641 c[2] - 790 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1183 c[1] + 657 c[2] - 790 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1655 c[1] + 529 c[2] - 782 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1575 c[1] + 545 c[2] - 782 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1463 c[1] + 561 c[2] - 782 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1855 c[1] + 449 c[2] - 774 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 && 2135 c[1] +
    353 c[2] - 766 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0, Array[c, 6], Integers]]
{101, 329, 416, 0, 0, 0}

```

GCD[101, 329, 416, 0, 0, 0]

1

Reverse[warrant2]

{0, 0, 0, 416, 329, 101}

warrant2.g

-44 364

warrant2.Transpose[A]

{9692, 12 924, 3644, 6876, 828, 12 532, 15 764, 9716, 12 948, 3668,
6900, 852, -5196, 21 420, 18 604, 12 556, 15 788, 9740, 12 972, 6924, 876,
21 444, 18 628, 15 812, 9764, 12 996, 6948, 900, 18 652, 15 836, 9788,
13 020, 6972, 15 860, 13 044, 6996, 15 884, 13 068, 7020, 13 092, 13 116}

feasibleinterlacingpolylist[chi]

{(-9 + x) (-7 + x) (-5 + x)² (1 + x),
-137 + 1121 x - 830 x² + 222 x³ - 25 x⁴ + x⁵, (-7 + x) (-5 + x) (-3 + x) (1 - 10 x + x²),
-249 + 1137 x - 830 x² + 222 x³ - 25 x⁴ + x⁵, (-7 + x) (31 - 158 x + 96 x² - 18 x³ + x⁴),
(-7 + x) (47 - 158 x + 96 x² - 18 x³ + x⁴), 223 + 1009 x - 822 x² + 222 x³ - 25 x⁴ + x⁵,
(-5 + x) (-51 - 212 x + 122 x² - 20 x³ + x⁴), 143 + 1025 x - 822 x² + 222 x³ - 25 x⁴ + x⁵,
(-7 + x) (-5 + x) (5 + 31 x - 13 x² + x³), 31 + 1041 x - 822 x² + 222 x³ - 25 x⁴ + x⁵,
(-7 + x) (-3 + x) (3 + 51 x - 15 x² + x³), (-7 + x) (7 - 150 x + 96 x² - 18 x³ + x⁴),
(-7 + x) (23 - 12 x + x²) (1 - 6 x + x²), (-5 + x) (-139 - 204 x + 122 x² - 20 x³ + x⁴),
(-5 + x) (41 - 14 x + x²) (-3 - 6 x + x²), 503 + 913 x - 814 x² + 222 x³ - 25 x⁴ + x⁵,
(-5 + x) (-107 - 204 x + 122 x² - 20 x³ + x⁴), 423 + 929 x - 814 x² + 222 x³ - 25 x⁴ + x⁵,
(-7 + x) (-5 + x) (13 + 31 x - 13 x² + x³), (-7 + x) (-49 - 142 x + 96 x² - 18 x³ + x⁴),
(-7 + x) (-3 + x) (11 + 51 x - 15 x² + x³), (-5 + x)² (39 + 47 x - 15 x² + x³),
(-5 + x) (-179 - 196 x + 122 x² - 20 x³ + x⁴), (-5 + x) (-163 - 196 x + 122 x² - 20 x³ + x⁴),
703 + 833 x - 806 x² + 222 x³ - 25 x⁴ + x⁵, (-7 + x) (-5 + x) (21 + 31 x - 13 x² + x³),
(-7 + x) (-89 - 134 x + 96 x² - 18 x³ + x⁴), (-7 + x) (-73 - 134 x + 96 x² - 18 x³ + x⁴),
(-5 + x)² (47 + 47 x - 15 x² + x³), (-5 + x) (-219 - 188 x + 122 x² - 20 x³ + x⁴),
983 + 737 x - 798 x² + 222 x³ - 25 x⁴ + x⁵, (-7 + x) (-5 + x) (29 + 31 x - 13 x² + x³),
(-7 + x) (-129 - 126 x + 96 x² - 18 x³ + x⁴), (-5 + x)² (55 + 47 x - 15 x² + x³),
(-7 + x) (-5 + x) (37 + 31 x - 13 x² + x³), (-7 + x) (-169 - 118 x + 96 x² - 18 x³ + x⁴),
(-5 + x) (-331 - 172 x + 122 x² - 20 x³ + x⁴), (-7 + x) (-209 - 110 x + 96 x² - 18 x³ + x⁴),
(-7 + x) (-5 + x) (53 + 31 x - 13 x² + x³), (-7 + x) (-5 + x) (61 + 31 x - 13 x² + x³) }


```
list = {(-9 + x) (-7 + x) (-5 + x)^2 (1 + x),
  -137 + 1121 x - 830 x^2 + 222 x^3 - 25 x^4 + x^5, (-7 + x) (-5 + x) (-3 + x) (1 - 10 x + x^2),
  -249 + 1137 x - 830 x^2 + 222 x^3 - 25 x^4 + x^5, (-7 + x) (31 - 158 x + 96 x^2 - 18 x^3 + x^4),
  (-7 + x) (47 - 158 x + 96 x^2 - 18 x^3 + x^4), 223 + 1009 x - 822 x^2 + 222 x^3 - 25 x^4 + x^5,
  (-5 + x) (-51 - 212 x + 122 x^2 - 20 x^3 + x^4), 143 + 1025 x - 822 x^2 + 222 x^3 - 25 x^4 + x^5,
  (-7 + x) (-5 + x) (5 + 31 x - 13 x^2 + x^3), 31 + 1041 x - 822 x^2 + 222 x^3 - 25 x^4 + x^5,
  (-7 + x) (-3 + x) (3 + 51 x - 15 x^2 + x^3), (-7 + x) (7 - 150 x + 96 x^2 - 18 x^3 + x^4),
  (-7 + x) (23 - 12 x + x^2) (1 - 6 x + x^2), (-5 + x) (-139 - 204 x + 122 x^2 - 20 x^3 + x^4),
  (-5 + x) (41 - 14 x + x^2) (-3 - 6 x + x^2), 503 + 913 x - 814 x^2 + 222 x^3 - 25 x^4 + x^5,
  (-5 + x) (-107 - 204 x + 122 x^2 - 20 x^3 + x^4), 423 + 929 x - 814 x^2 + 222 x^3 - 25 x^4 + x^5,
  (-7 + x) (-5 + x) (13 + 31 x - 13 x^2 + x^3), (-7 + x) (-49 - 142 x + 96 x^2 - 18 x^3 + x^4),
  (-7 + x) (-3 + x) (11 + 51 x - 15 x^2 + x^3), (-5 + x)^2 (39 + 47 x - 15 x^2 + x^3),
  (-5 + x) (-179 - 196 x + 122 x^2 - 20 x^3 + x^4), (-5 + x) (-163 - 196 x + 122 x^2 - 20 x^3 + x^4),
  703 + 833 x - 806 x^2 + 222 x^3 - 25 x^4 + x^5, (-7 + x) (-5 + x) (21 + 31 x - 13 x^2 + x^3),
  (-7 + x) (-89 - 134 x + 96 x^2 - 18 x^3 + x^4), (-7 + x) (-73 - 134 x + 96 x^2 - 18 x^3 + x^4),
  (-5 + x)^2 (47 + 47 x - 15 x^2 + x^3), (-5 + x) (-219 - 188 x + 122 x^2 - 20 x^3 + x^4),
  983 + 737 x - 798 x^2 + 222 x^3 - 25 x^4 + x^5, (-7 + x) (-5 + x) (29 + 31 x - 13 x^2 + x^3),
  (-7 + x) (-129 - 126 x + 96 x^2 - 18 x^3 + x^4), (-5 + x)^2 (55 + 47 x - 15 x^2 + x^3),
  (-7 + x) (-5 + x) (37 + 31 x - 13 x^2 + x^3), (-7 + x) (-169 - 118 x + 96 x^2 - 18 x^3 + x^4),
  (-5 + x) (-331 - 172 x + 122 x^2 - 20 x^3 + x^4), (-7 + x) (-209 - 110 x + 96 x^2 - 18 x^3 + x^4),
  (-7 + x) (-5 + x) (53 + 31 x - 13 x^2 + x^3), (-7 + x) (-5 + x) (61 + 31 x - 13 x^2 + x^3)};
```

```
warrantpoly =
```

```
{-249 + 1137 x - 830 x^2 + 222 x^3 - 25 x^4 + x^5, (-7 + x) (23 - 12 x + x^2) (1 - 6 x + x^2)}
{-249 + 1137 x - 830 x^2 + 222 x^3 - 25 x^4 + x^5, (-7 + x) (23 - 12 x + x^2) (1 - 6 x + x^2)}
```

```
anglesquared = anglesquaredmat[chi, list] // FullSimplify;
```

```
anglesquared // MatrixForm
```

$\frac{35}{73}$	$\text{Root}[-25 + 534 \#1 - 3534 \#1^2 + 6789 \#1^3 \&, 3]$	0	$\text{Root}[-25 + 534 \#1 -$
$\frac{2281}{4380}$	$\text{Root}[-1 + 1053 \#1 - 24840 \#1^2 + 94608 \#1^3 \&, 2]$	$\frac{2}{15}$	$\text{Root}[-1 + 1053 \#1 - 2$
$\frac{38}{73}$	$\text{Root}[-1 + 195 \#1 - 3255 \#1^2 + 6789 \#1^3 \&, 2]$	0	$\text{Root}[-1 + 195 \#1 -$
$\frac{2287}{4380}$	$\text{Root}[-53 + 9513 \#1 - 374976 \#1^2 + 2932848 \#1^3 \&, 2]$	$\frac{4}{15}$	$\text{Root}[-53 + 9513 \#1 - 37$
$\frac{381}{730}$	$\text{Root}[-97 + 10791 \#1 - 252774 \#1^2 + 733212 \#1^3 \&, 2]$	$\frac{2}{15}$	$\text{Root}[-97 + 10791 \#1 - 1$
$\frac{191}{365}$	$\text{Root}[-5 + 936 \#1 - 38502 \#1^2 + 183303 \#1^3 \&, 1]$	$\frac{4}{15}$	$\text{Root}[-5 + 936 \#1 - 38$
$\frac{1123}{2190}$	$\text{Root}[-37 + 6633 \#1 - 137268 \#1^2 + 733212 \#1^3 \&, 3]$	$\frac{2}{15}$	$\text{Root}[-37 + 6633 \#1 - 1$
$\frac{449}{876}$	$\text{Root}[-353 + 36117 \#1 - 395064 \#1^2 + 977616 \#1^3 \&, 2]$	0	$\text{Root}[-353 + 36117 \#1 -$
$\frac{2251}{4380}$	$\text{Root}[-769 + 56061 \#1 - 790128 \#1^2 + 2932848 \#1^3 \&, 2]$	$\frac{2}{15}$	$\text{Root}[-769 + 56061 \#1 - 7$
$\frac{75}{146}$	$\text{Root}[-205 + 11619 \#1 - 118854 \#1^2 + 244404 \#1^3 \&, 2]$	0	$\text{Root}[-205 + 11619 \#1 -$
$\frac{2257}{4380}$	$\text{Root}[-215 + 16659 \#1 - 395064 \#1^2 + 2932848 \#1^3 \&, 3]$	$\frac{4}{15}$	$\text{Root}[-215 + 16659 \#1 - 3$
$\frac{188}{365}$	$\text{Root}[-100 + 5130 \#1 - 64449 \#1^2 + 183303 \#1^3 \&, 2]$	$\frac{2}{15}$	$\text{Root}[-100 + 5130 \#1 -$
$\frac{377}{730}$	$\text{Root}[-167 + 9405 \#1 - 159030 \#1^2 + 733212 \#1^3 \&, 2]$	$\frac{4}{15}$	$\text{Root}[-167 + 9405 \#1 - 1$

$\frac{189}{365}$	$\text{Root}[-1 + 126 \#1 - 5022 \#1^2 + 61101 \#1^3 \&, 1]$	$\frac{2}{5}$	$\text{Root}[-1 + 126 \#1 - 5022 \#1^2 + 61101 \#1^3 \&, 1]$
$\frac{147}{292}$	$\text{Root}[-47 + 10683 \#1 - 241056 \#1^2 + 977616 \#1^3 \&, 3]$	0	$\text{Root}[-47 + 10683 \#1 - 241056 \#1^2 + 977616 \#1^3 \&, 3]$
$\frac{221}{438}$	$\text{Root}[-97 + 7137 \#1 - 80352 \#1^2 + 244404 \#1^3 \&, 3]$	0	$\text{Root}[-97 + 7137 \#1 - 80352 \#1^2 + 244404 \#1^3 \&, 3]$
$\frac{554}{1095}$	$\text{Root}[-61 + 5535 \#1 - 142290 \#1^2 + 733212 \#1^3 \&, 3]$	$\frac{2}{15}$	$\text{Root}[-61 + 5535 \#1 - 142290 \#1^2 + 733212 \#1^3 \&, 3]$
$\frac{443}{876}$	$\text{Root}[-325 + 15081 \#1 - 133920 \#1^2 + 325872 \#1^3 \&, 2]$	0	$\text{Root}[-325 + 15081 \#1 - 133920 \#1^2 + 325872 \#1^3 \&, 2]$
$\frac{2221}{4380}$	$\text{Root}[-1483 + 67167 \#1 - 810216 \#1^2 + 2932848 \#1^3 \&, 3]$	$\frac{2}{15}$	$\text{Root}[-1483 + 67167 \#1 - 810216 \#1^2 + 2932848 \#1^3 \&, 3]$
$\frac{37}{73}$	$\text{Root}[-107 + 3798 \#1 - 30132 \#1^2 + 61101 \#1^3 \&, 2]$	0	$\text{Root}[-107 + 3798 \#1 - 30132 \#1^2 + 61101 \#1^3 \&, 2]$
$\frac{371}{730}$	$\text{Root}[-769 + 27171 \#1 - 262818 \#1^2 + 733212 \#1^3 \&, 2]$	$\frac{2}{15}$	$\text{Root}[-769 + 27171 \#1 - 262818 \#1^2 + 733212 \#1^3 \&, 2]$
$\frac{186}{365}$	$\text{Root}[-71 + 2997 \#1 - 41013 \#1^2 + 183303 \#1^3 \&, 3]$	$\frac{4}{15}$	$\text{Root}[-71 + 2997 \#1 - 41013 \#1^2 + 183303 \#1^3 \&, 3]$
$\frac{145}{292}$	$\text{Root}[-1 + 597 \#1 - 27528 \#1^2 + 108624 \#1^3 \&, 3]$	0	$\text{Root}[-1 + 597 \#1 - 27528 \#1^2 + 108624 \#1^3 \&, 3]$
$\frac{109}{219}$	$\text{Root}[-155 + 7101 \#1 - 82026 \#1^2 + 244404 \#1^3 \&, 3]$	0	$\text{Root}[-155 + 7101 \#1 - 82026 \#1^2 + 244404 \#1^3 \&, 3]$
$\frac{437}{876}$	$\text{Root}[-1525 + 50265 \#1 - 408456 \#1^2 + 977616 \#1^3 \&, 3]$	0	$\text{Root}[-1525 + 50265 \#1 - 408456 \#1^2 + 977616 \#1^3 \&, 3]$
$\frac{2191}{4380}$	$\text{Root}[-1597 + 65961 \#1 - 830304 \#1^2 + 2932848 \#1^3 \&, 3]$	$\frac{2}{15}$	$\text{Root}[-1597 + 65961 \#1 - 830304 \#1^2 + 2932848 \#1^3 \&, 3]$
$\frac{1}{2}$	$\text{Root}[-1 + 27 \#1 - 186 \#1^2 + 372 \#1^3 \&, 2]$	0	$\text{Root}[-1 + 27 \#1 - 186 \#1^2 + 372 \#1^3 \&, 2]$
$\frac{183}{365}$	$\text{Root}[-265 + 7686 \#1 - 66960 \#1^2 + 183303 \#1^3 \&, 3]$	$\frac{2}{15}$	$\text{Root}[-265 + 7686 \#1 - 66960 \#1^2 + 183303 \#1^3 \&, 3]$
$\frac{367}{730}$	$\text{Root}[-227 + 11493 \#1 - 169074 \#1^2 + 733212 \#1^3 \&, 3]$	$\frac{4}{15}$	$\text{Root}[-227 + 11493 \#1 - 169074 \#1^2 + 733212 \#1^3 \&, 3]$
$\frac{215}{438}$	$\text{Root}[-41 + 2013 \#1 - 27900 \#1^2 + 81468 \#1^3 \&, 3]$	0	$\text{Root}[-41 + 2013 \#1 - 27900 \#1^2 + 81468 \#1^3 \&, 3]$
$\frac{431}{876}$	$\text{Root}[-1811 + 51183 \#1 - 415152 \#1^2 + 977616 \#1^3 \&, 3]$	0	$\text{Root}[-1811 + 51183 \#1 - 415152 \#1^2 + 977616 \#1^3 \&, 3]$
$\frac{2161}{4380}$	$\text{Root}[-535 + 52443 \#1 - 850392 \#1^2 + 2932848 \#1^3 \&, 3]$	$\frac{2}{15}$	$\text{Root}[-535 + 52443 \#1 - 850392 \#1^2 + 2932848 \#1^3 \&, 3]$
$\frac{36}{73}$	$\text{Root}[-211 + 4815 \#1 - 30969 \#1^2 + 61101 \#1^3 \&, 3]$	0	$\text{Root}[-211 + 4815 \#1 - 30969 \#1^2 + 61101 \#1^3 \&, 3]$
$\frac{361}{730}$	$\text{Root}[-1129 + 31239 \#1 - 272862 \#1^2 + 733212 \#1^3 \&, 3]$	$\frac{2}{15}$	$\text{Root}[-1129 + 31239 \#1 - 272862 \#1^2 + 733212 \#1^3 \&, 3]$
$\frac{425}{876}$	$\text{Root}[-547 + 15999 \#1 - 140616 \#1^2 + 325872 \#1^3 \&, 3]$	0	$\text{Root}[-547 + 15999 \#1 - 140616 \#1^2 + 325872 \#1^3 \&, 3]$
$\frac{71}{146}$	$\text{Root}[-941 + 19755 \#1 - 125550 \#1^2 + 244404 \#1^3 \&, 3]$	0	$\text{Root}[-941 + 19755 \#1 - 125550 \#1^2 + 244404 \#1^3 \&, 3]$
$\frac{178}{365}$	$\text{Root}[-208 + 7164 \#1 - 69471 \#1^2 + 183303 \#1^3 \&, 3]$	$\frac{2}{15}$	$\text{Root}[-208 + 7164 \#1 - 69471 \#1^2 + 183303 \#1^3 \&, 3]$
$\frac{419}{876}$	$\text{Root}[-823 + 40707 \#1 - 428544 \#1^2 + 977616 \#1^3 \&, 3]$	0	$\text{Root}[-823 + 40707 \#1 - 428544 \#1^2 + 977616 \#1^3 \&, 3]$
$\frac{351}{730}$	$\text{Root}[-25 + 22995 \#1 - 282906 \#1^2 + 733212 \#1^3 \&, 3]$	$\frac{2}{15}$	$\text{Root}[-25 + 22995 \#1 - 282906 \#1^2 + 733212 \#1^3 \&, 3]$
$\frac{69}{146}$	$\text{Root}[-673 + 17667 \#1 - 128898 \#1^2 + 244404 \#1^3 \&, 3]$	0	$\text{Root}[-673 + 17667 \#1 - 128898 \#1^2 + 244404 \#1^3 \&, 3]$
$\frac{34}{73}$	$\text{Root}[-53 + 3771 \#1 - 32643 \#1^2 + 61101 \#1^3 \&, 3]$	0	$\text{Root}[-53 + 3771 \#1 - 32643 \#1^2 + 61101 \#1^3 \&, 3]$

```

combinations[chi, (x + 5) (x - 5), warrantpoly[[1],
warrantpoly[[2]], list, anglesquared] // FullSimplify

```

```
{Root[3 115 225 - 15 630 756 #1^2 + 16 570 710 #1^4 - 6 177 060 #1^6 + 700 569 #1^8 &, 6],
Root[3 115 225 - 15 630 756 #1^2 + 16 570 710 #1^4 - 6 177 060 #1^6 + 700 569 #1^8 &, 2],
Root[3 115 225 - 15 630 756 #1^2 + 16 570 710 #1^4 - 6 177 060 #1^6 + 700 569 #1^8 &, 6],
Root[3 115 225 - 15 630 756 #1^2 + 16 570 710 #1^4 - 6 177 060 #1^6 + 700 569 #1^8 &, 2],
Root[3 115 225 - 15 630 756 #1^2 + 16 570 710 #1^4 - 6 177 060 #1^6 + 700 569 #1^8 &, 5],
Root[3 115 225 - 15 630 756 #1^2 + 16 570 710 #1^4 - 6 177 060 #1^6 + 700 569 #1^8 &, 1],
Root[3 115 225 - 15 630 756 #1^2 + 16 570 710 #1^4 - 6 177 060 #1^6 + 700 569 #1^8 &, 5],
Root[3 115 225 - 15 630 756 #1^2 + 16 570 710 #1^4 - 6 177 060 #1^6 + 700 569 #1^8 &, 1]}
```

```
compatible[combinations[chi, (x + 5) (x - 5),
warrantpoly[[1]], warrantpoly[[2]], list, anglesquared] // FullSimplify]
```

```
0
```

```
In[*]:= chi = (-5 + x)^11 (-3 + x) (5 + x)^15 (68 - 17 x + x^2)
```

```
Out[*]:= (-5 + x)^11 (-3 + x) (5 + x)^15 (68 - 17 x + x^2)
```

```
CoefficientList[feasibleinterlacingpolylist[chi], x]
```

```
{{-75, -220, 122, -20, 1}, {-59, -220, 122, -20, 1},
{-43, -220, 122, -20, 1}, {-27, -220, 122, -20, 1}, {93, -244, 122, -20, 1},
{5, -236, 122, -20, 1}, {21, -236, 122, -20, 1}, {37, -236, 122, -20, 1},
{53, -236, 122, -20, 1}, {69, -236, 122, -20, 1}, {-35, -228, 122, -20, 1},
{-19, -228, 122, -20, 1}, {-3, -228, 122, -20, 1}, {13, -228, 122, -20, 1},
{29, -228, 122, -20, 1}, {-115, -212, 122, -20, 1}, {-99, -212, 122, -20, 1},
{-83, -212, 122, -20, 1}, {-155, -204, 122, -20, 1}, {-139, -204, 122, -20, 1},
{-195, -196, 122, -20, 1}, {-179, -196, 122, -20, 1}, {-235, -188, 122, -20, 1}}
```

```
A = {{93, -244, 122, -20, 1}, {5, -236, 122, -20, 1}, {21, -236, 122, -20, 1},
{37, -236, 122, -20, 1}, {53, -236, 122, -20, 1}, {69, -236, 122, -20, 1},
{-35, -228, 122, -20, 1}, {-19, -228, 122, -20, 1}, {-3, -228, 122, -20, 1},
{13, -228, 122, -20, 1}, {29, -228, 122, -20, 1}, {-75, -220, 122, -20, 1},
{-59, -220, 122, -20, 1}, {-43, -220, 122, -20, 1}, {-27, -220, 122, -20, 1},
{-115, -212, 122, -20, 1}, {-99, -212, 122, -20, 1}, {-83, -212, 122, -20, 1},
{-155, -204, 122, -20, 1}, {-139, -204, 122, -20, 1}, {-195, -196, 122, -20, 1},
{-179, -196, 122, -20, 1}, {-235, -188, 122, -20, 1}};
```

A // MatrixForm

$$\begin{pmatrix} 93 & -244 & 122 & -20 & 1 \\ 5 & -236 & 122 & -20 & 1 \\ 21 & -236 & 122 & -20 & 1 \\ 37 & -236 & 122 & -20 & 1 \\ 53 & -236 & 122 & -20 & 1 \\ 69 & -236 & 122 & -20 & 1 \\ -35 & -228 & 122 & -20 & 1 \\ -19 & -228 & 122 & -20 & 1 \\ -3 & -228 & 122 & -20 & 1 \\ 13 & -228 & 122 & -20 & 1 \\ 29 & -228 & 122 & -20 & 1 \\ -75 & -220 & 122 & -20 & 1 \\ -59 & -220 & 122 & -20 & 1 \\ -43 & -220 & 122 & -20 & 1 \\ -27 & -220 & 122 & -20 & 1 \\ -115 & -212 & 122 & -20 & 1 \\ -99 & -212 & 122 & -20 & 1 \\ -83 & -212 & 122 & -20 & 1 \\ -155 & -204 & 122 & -20 & 1 \\ -139 & -204 & 122 & -20 & 1 \\ -195 & -196 & 122 & -20 & 1 \\ -179 & -196 & 122 & -20 & 1 \\ -235 & -188 & 122 & -20 & 1 \end{pmatrix}$$

g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]

{1105, -6684, 3538, -580, 29}

FindInstance[n[1] ≥ 0 && n[2] ≥ 0 && n[3] ≥ 0 && n[4] ≥ 0 && n[5] ≥ 0 && n[6] ≥ 0 &&

n[7] ≥ 0 && n[8] ≥ 0 && n[9] ≥ 0 && n[10] ≥ 0 && n[11] ≥ 0 && n[12] ≥ 0 && n[13] ≥ 0 &&

n[14] ≥ 0 && n[15] ≥ 0 && n[16] ≥ 0 && n[17] ≥ 0 && n[18] ≥ 0 && n[19] ≥ 0 && n[20] ≥ 0 &&

n[21] ≥ 0 && n[22] ≥ 0 && n[23] ≥ 0 && Array[n, 23].A == g, Array[n, 23], Integers]

**{{n[1] → 0, n[2] → 0, n[3] → 0, n[4] → 0, n[5] → 0, n[6] → 14, n[7] → 0, n[8] → 0,
n[9] → 0, n[10] → 1, n[11] → 9, n[12] → 0, n[13] → 0, n[14] → 0, n[15] → 5, n[16] → 0,
n[17] → 0, n[18] → 0, n[19] → 0, n[20] → 0, n[21] → 0, n[22] → 0, n[23] → 0}}}**

Array[c, 5].Transpose[A]

```
{ 93 c[1] - 244 c[2] + 122 c[3] - 20 c[4] + c[5],
  5 c[1] - 236 c[2] + 122 c[3] - 20 c[4] + c[5],
  21 c[1] - 236 c[2] + 122 c[3] - 20 c[4] + c[5],
  37 c[1] - 236 c[2] + 122 c[3] - 20 c[4] + c[5],
  53 c[1] - 236 c[2] + 122 c[3] - 20 c[4] + c[5],
  69 c[1] - 236 c[2] + 122 c[3] - 20 c[4] + c[5],
 -35 c[1] - 228 c[2] + 122 c[3] - 20 c[4] + c[5],
 -19 c[1] - 228 c[2] + 122 c[3] - 20 c[4] + c[5],
 -3 c[1] - 228 c[2] + 122 c[3] - 20 c[4] + c[5],
 13 c[1] - 228 c[2] + 122 c[3] - 20 c[4] + c[5],
 29 c[1] - 228 c[2] + 122 c[3] - 20 c[4] + c[5],
 -75 c[1] - 220 c[2] + 122 c[3] - 20 c[4] + c[5],
 -59 c[1] - 220 c[2] + 122 c[3] - 20 c[4] + c[5],
 -43 c[1] - 220 c[2] + 122 c[3] - 20 c[4] + c[5],
 -27 c[1] - 220 c[2] + 122 c[3] - 20 c[4] + c[5],
 -115 c[1] - 212 c[2] + 122 c[3] - 20 c[4] + c[5],
 -99 c[1] - 212 c[2] + 122 c[3] - 20 c[4] + c[5],
 -83 c[1] - 212 c[2] + 122 c[3] - 20 c[4] + c[5],
 -155 c[1] - 204 c[2] + 122 c[3] - 20 c[4] + c[5],
 -139 c[1] - 204 c[2] + 122 c[3] - 20 c[4] + c[5],
 -195 c[1] - 196 c[2] + 122 c[3] - 20 c[4] + c[5],
 -179 c[1] - 196 c[2] + 122 c[3] - 20 c[4] + c[5],
 -235 c[1] - 188 c[2] + 122 c[3] - 20 c[4] + c[5]}
```

Array[c, 5].g

```
1105 c[1] - 6684 c[2] + 3538 c[3] - 580 c[4] + 29 c[5]
```

```

warrant = Flatten[Array[c, 5] /.
  FindInstance[1105 c[1] - 6684 c[2] + 3538 c[3] - 580 c[4] + 29 c[5] < 0 &&
    93 c[1] - 244 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    5 c[1] - 236 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    21 c[1] - 236 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    37 c[1] - 236 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    53 c[1] - 236 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    69 c[1] - 236 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -35 c[1] - 228 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -19 c[1] - 228 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -3 c[1] - 228 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    13 c[1] - 228 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    29 c[1] - 228 c[2] + 122 c[3] - 20 c[4] + c[5] < 0 &&
    -75 c[1] - 220 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -59 c[1] - 220 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -43 c[1] - 220 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -27 c[1] - 220 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -115 c[1] - 212 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -99 c[1] - 212 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -83 c[1] - 212 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -155 c[1] - 204 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -139 c[1] - 204 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -195 c[1] - 196 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -179 c[1] - 196 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -235 c[1] - 188 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0, Array[c, 5], Integers]]
{-190, -1143, 0, 0, -256444}

GCD[-190, -1143, 0, 0, -256444]
1

Reverse[warrant]
{-256444, 0, 0, -1143, -190}

warrant.g
-7014

warrant.Transpose[A]
{4778, 12354, 9314, 6274, 3234, 194, 10810, 7770, 4730, 1690, -1350,
  9266, 6226, 3186, 146, 7722, 4682, 1642, 6178, 3138, 4634, 1594, 3090}

```

feasibleinterlacingpolylist[chi]

$$\begin{aligned} & \{ (-5+x)^2 (-3-10x+x^2), (59-16x+x^2) (-1-4x+x^2), \\ & -43-220x+122x^2-20x^3+x^4, -27-220x+122x^2-20x^3+x^4, \\ & (-3+x) (-31+71x-17x^2+x^3), (-5+x) (-1+47x-15x^2+x^3), \\ & 21-236x+122x^2-20x^3+x^4, (37-14x+x^2) (1-6x+x^2), 53-236x+122x^2-20x^3+x^4, \\ & (-3+x) (-23+71x-17x^2+x^3), (-5+x) (7+47x-15x^2+x^3), \\ & -19-228x+122x^2-20x^3+x^4, -3-228x+122x^2-20x^3+x^4, \\ & 13-228x+122x^2-20x^3+x^4, 29-228x+122x^2-20x^3+x^4, \\ & (-5+x) (23+47x-15x^2+x^3), -99-212x+122x^2-20x^3+x^4, \\ & -83-212x+122x^2-20x^3+x^4, (-5+x) (31+47x-15x^2+x^3), \\ & -139-204x+122x^2-20x^3+x^4, (-5+x) (39+47x-15x^2+x^3), \\ & -179-196x+122x^2-20x^3+x^4, (-5+x) (47+47x-15x^2+x^3) \} \end{aligned}$$

In[]:= **list =**

$$\begin{aligned} & \{ (-5+x)^2 (-3-10x+x^2), (59-16x+x^2) (-1-4x+x^2), -43-220x+122x^2-20x^3+x^4, \\ & -27-220x+122x^2-20x^3+x^4, (-3+x) (-31+71x-17x^2+x^3), \\ & (-5+x) (-1+47x-15x^2+x^3), 21-236x+122x^2-20x^3+x^4, \\ & (37-14x+x^2) (1-6x+x^2), 53-236x+122x^2-20x^3+x^4, \\ & (-3+x) (-23+71x-17x^2+x^3), (-5+x) (7+47x-15x^2+x^3), \\ & -19-228x+122x^2-20x^3+x^4, -3-228x+122x^2-20x^3+x^4, \\ & 13-228x+122x^2-20x^3+x^4, 29-228x+122x^2-20x^3+x^4, \\ & (-5+x) (23+47x-15x^2+x^3), -99-212x+122x^2-20x^3+x^4, \\ & -83-212x+122x^2-20x^3+x^4, (-5+x) (31+47x-15x^2+x^3), \\ & -139-204x+122x^2-20x^3+x^4, (-5+x) (39+47x-15x^2+x^3), \\ & -179-196x+122x^2-20x^3+x^4, (-5+x) (47+47x-15x^2+x^3) \}; \end{aligned}$$

warrantpoly = 29 - 228 x + 122 x² - 20 x³ + x⁴

29 - 228 x + 122 x² - 20 x³ + x⁴

In[]:= **chi**

Out[]:= $(-5+x)^{11} (-3+x) (5+x)^{15} (68-17x+x^2)$

In[]:= **orderedroots[minipoly[chi]]**

Out[]:= $\left\{ -5, 3, 5, \frac{1}{2} (17 - \sqrt{17}), \frac{1}{2} (17 + \sqrt{17}) \right\}$

{2}

{4, 5}

{2, 4, 5}

In[]:= **anglesquared = anglesquaredmat[chi, list] // FullSimplify;**

```
In[*]:= anglesquared // MatrixForm
```

```
Out[*] // MatrixForm =
```

$$\begin{pmatrix} \frac{45}{89} \frac{3}{13} & 0 & \frac{5185+937 \sqrt{17}}{39338} & \frac{5185-937 \sqrt{17}}{39338} \\ \frac{451}{890} \frac{5}{26} \frac{1}{10} & \frac{7905+1163 \sqrt{17}}{78676} & \frac{7905-1163 \sqrt{17}}{78676} \\ \frac{226}{445} \frac{2}{13} \frac{1}{5} & \frac{1360+113 \sqrt{17}}{19669} & \frac{1360-113 \sqrt{17}}{19669} \\ \frac{453}{890} \frac{3}{26} \frac{3}{10} & -\frac{7(-425+37 \sqrt{17})}{78676} & \frac{7(425+37 \sqrt{17})}{78676} \\ \frac{234}{445} 0 \frac{3}{10} & \frac{527+125 \sqrt{17}}{6052} & \frac{527-125 \sqrt{17}}{6052} \\ \frac{46}{89} \frac{2}{13} 0 & \frac{6477+1565 \sqrt{17}}{39338} & \frac{6477-1565 \sqrt{17}}{39338} \\ \frac{461}{890} \frac{3}{26} \frac{1}{10} & \frac{10489+2419 \sqrt{17}}{78676} & \frac{10489-2419 \sqrt{17}}{78676} \\ \frac{231}{445} \frac{1}{13} \frac{1}{5} & \frac{2006+427 \sqrt{17}}{19669} & \frac{2006-427 \sqrt{17}}{19669} \\ \frac{463}{890} \frac{1}{26} \frac{3}{10} & \frac{5559+997 \sqrt{17}}{78676} & \frac{5559-997 \sqrt{17}}{78676} \\ \frac{232}{445} 0 \frac{2}{5} & \frac{119+11 \sqrt{17}}{3026} & \frac{119-11 \sqrt{17}}{3026} \\ \frac{91}{178} \frac{5}{26} 0 & \frac{5831+1251 \sqrt{17}}{39338} & \frac{5831-1251 \sqrt{17}}{39338} \\ \frac{228}{445} \frac{2}{13} \frac{1}{10} & \frac{9197+1791 \sqrt{17}}{78676} & \frac{9197-1791 \sqrt{17}}{78676} \\ \frac{457}{890} \frac{3}{26} \frac{1}{5} & \frac{9(187+30 \sqrt{17})}{19669} & -\frac{9(-187+30 \sqrt{17})}{19669} \\ \frac{229}{445} \frac{1}{13} \frac{3}{10} & \frac{4267+369 \sqrt{17}}{78676} & \frac{4267-369 \sqrt{17}}{78676} \\ \frac{459}{890} \frac{1}{26} \frac{2}{5} & \frac{901-171 \sqrt{17}}{39338} & \frac{901+171 \sqrt{17}}{39338} \\ \frac{1}{2} \frac{7}{26} 0 & \frac{1}{442} (51+7 \sqrt{17}) & \frac{1}{442} (51-7 \sqrt{17}) \\ \frac{223}{445} \frac{3}{13} \frac{1}{10} & \frac{6613+535 \sqrt{17}}{78676} & \frac{6613-535 \sqrt{17}}{78676} \\ \frac{447}{890} \frac{5}{26} \frac{1}{5} & \frac{1037-44 \sqrt{17}}{19669} & \frac{1037+44 \sqrt{17}}{19669} \\ \frac{44}{89} \frac{4}{13} 0 & \frac{3893+309 \sqrt{17}}{39338} & \frac{3893-309 \sqrt{17}}{39338} \\ \frac{441}{890} \frac{7}{26} \frac{1}{10} & \frac{5321-93 \sqrt{17}}{78676} & \frac{5321+93 \sqrt{17}}{78676} \\ \frac{87}{178} \frac{9}{26} 0 & \frac{3247-5 \sqrt{17}}{39338} & \frac{3247+5 \sqrt{17}}{39338} \\ \frac{218}{445} \frac{4}{13} \frac{1}{10} & \frac{4029-721 \sqrt{17}}{78676} & \frac{4029+721 \sqrt{17}}{78676} \\ \frac{43}{89} \frac{5}{13} 0 & \frac{2601-319 \sqrt{17}}{39338} & \frac{2601+319 \sqrt{17}}{39338} \end{pmatrix}$$

```
In[*]:= anglemat = Sqrt[anglesquared] // FullSimplify;
```


In[*]:= **anglemat** // MatrixForm

Out[*]//MatrixForm=

$3 \sqrt{\frac{5}{89}}$	$\sqrt{\frac{3}{13}}$	0	$\sqrt{\frac{5185+937 \sqrt{17}}{39338}}$	<input type="button" value="0.183..."/>
$\sqrt{\frac{451}{890}}$	$\sqrt{\frac{5}{26}}$	$\frac{1}{\sqrt{10}}$	<input type="button" value="0.402..."/>	<input type="button" value="0.199..."/>
$\sqrt{\frac{226}{445}}$	$\sqrt{\frac{2}{13}}$	$\frac{1}{\sqrt{5}}$	<input type="button" value="0.305..."/>	<input type="button" value="0.213..."/>
$\sqrt{\frac{453}{890}}$	$\sqrt{\frac{3}{26}}$	$\sqrt{\frac{3}{10}}$	<input type="button" value="0.156..."/>	<input type="button" value="0.227..."/>
$3 \sqrt{\frac{26}{445}}$	0	$\sqrt{\frac{3}{10}}$	<input type="button" value="0.415..."/>	<input type="button" value="0.0438..."/>
$\sqrt{\frac{46}{89}}$	$\sqrt{\frac{2}{13}}$	0	<input type="button" value="0.573..."/>	<input type="button" value="0.0249..."/>
$\sqrt{\frac{461}{890}}$	$\sqrt{\frac{3}{26}}$	$\frac{1}{\sqrt{10}}$	<input type="button" value="0.510..."/>	<input type="button" value="0.0809..."/>
$\sqrt{\frac{231}{445}}$	$\frac{1}{\sqrt{13}}$	$\frac{1}{\sqrt{5}}$	<input type="button" value="0.438..."/>	<input type="button" value="0.112..."/>
$\sqrt{\frac{463}{890}}$	$\frac{1}{\sqrt{26}}$	$\sqrt{\frac{3}{10}}$	<input type="button" value="0.351..."/>	<input type="button" value="0.136..."/>
$2 \sqrt{\frac{58}{445}}$	0	$\sqrt{\frac{2}{5}}$	<input type="button" value="0.233..."/>	<input type="button" value="0.156..."/>
$\sqrt{\frac{91}{178}}$	$\sqrt{\frac{5}{26}}$	0	<input type="button" value="0.529..."/>	<input type="button" value="0.131..."/>
$2 \sqrt{\frac{57}{445}}$	$\sqrt{\frac{2}{13}}$	$\frac{1}{\sqrt{10}}$	<input type="button" value="0.459..."/>	<input type="button" value="0.152..."/>
$\sqrt{\frac{457}{890}}$	$\sqrt{\frac{3}{26}}$	$\frac{1}{\sqrt{5}}$	<input type="button" value="0.377..."/>	<input type="button" value="0.170..."/>
$\sqrt{\frac{229}{445}}$	$\frac{1}{\sqrt{13}}$	$\sqrt{\frac{3}{10}}$	<input type="button" value="0.271..."/>	<input type="button" value="0.187..."/>
$3 \sqrt{\frac{51}{890}}$	$\frac{1}{\sqrt{26}}$	$\sqrt{\frac{2}{5}}$	<input type="button" value="0.0706..."/>	<input type="button" value="0.202..."/>
$\frac{1}{\sqrt{2}}$	$\sqrt{\frac{7}{26}}$	0	$\sqrt{\frac{1}{442} (51 + 7 \sqrt{17})}$	<input type="button" value="0.224..."/>
$\sqrt{\frac{223}{445}}$	$\sqrt{\frac{3}{13}}$	$\frac{1}{\sqrt{10}}$	<input type="button" value="0.335..."/>	<input type="button" value="0.237..."/>
$\sqrt{\frac{447}{890}}$	$\sqrt{\frac{5}{26}}$	$\frac{1}{\sqrt{5}}$	<input type="button" value="0.209..."/>	$\sqrt{\frac{1037+44 \sqrt{17}}{19669}}$
$2 \sqrt{\frac{11}{89}}$	$\frac{2}{\sqrt{13}}$	0	$\sqrt{\frac{3893+309 \sqrt{17}}{39338}}$	<input type="button" value="0.258..."/>
$\frac{21}{\sqrt{890}}$	$\sqrt{\frac{7}{26}}$	$\frac{1}{\sqrt{10}}$	<input type="button" value="0.251..."/>	<input type="button" value="0.269..."/>
$\sqrt{\frac{87}{178}}$	$\frac{3}{\sqrt{26}}$	0	$\sqrt{\frac{3247-5 \sqrt{17}}{39338}}$	$\sqrt{\frac{3247+5 \sqrt{17}}{39338}}$
$\sqrt{\frac{218}{445}}$	$\frac{2}{\sqrt{13}}$	$\frac{1}{\sqrt{10}}$	<input type="button" value="0.116..."/>	<input type="button" value="0.298..."/>
$\sqrt{\frac{43}{89}}$	$\sqrt{\frac{5}{13}}$	0	<input type="button" value="0.181..."/>	<input type="button" value="0.316..."/>

In[*]:= **chi**

Out[*]= $(-5 + x)^{11} (-3 + x) (5 + x)^{15} (68 - 17x + x^2)$

In[*]:= **coeff**[chi, (x + 5) (x - 5) (68 - 17x + x²)] // FullSimplify

Out[*]= {-416}

```
In[*]:= coeff[chi, (x + 5) (x - 5) (x - 3)] // FullSimplify
```

```
Out[*]:=  $\left\{ \frac{1}{2} (711 - 145 \sqrt{17}), \frac{1}{2} (711 + 145 \sqrt{17}) \right\}$ 
```

```
In[*]:= coeff[chi, (x + 5) (x - 5)] // FullSimplify
```

```
Out[*]:=  $\left\{ -16, \frac{1}{2} (103 - 17 \sqrt{17}), \frac{1}{2} (103 + 17 \sqrt{17}) \right\}$ 
```

```
In[*]:= For[i = 1, i ≤ Length[list], i++,
```

```
    If[compatible[combinationangle[{-416}, {15, i}, {2}, anglemat]] == 1, Print[i]]
```

```
]
```

```
3
```

```
5
```

```
6
```

```
9
```

```
10
```

```
12
```

```
15
```

```
21
```

```
In[*]:= For[i = 1, i ≤ Length[list], i++,
```

```
    If[compatiblefrminipoly[MinimalPolynomial[
```

```
        combinationangle[{-416}, {15, i}, {2}, anglemat], x]] == 1, Print[i]]
```

```
]
```

```
3
```

```
5
```

```
6
```

```
9
```

```
10
```

```
12
```

```
15
```

```
21
```

```
In[*]:= MinimalPolynomial[combinationangle[
```

```
     $\left\{ \frac{1}{2} (711 - 145 \sqrt{17}), \frac{1}{2} (711 + 145 \sqrt{17}) \right\}, \{15, 5\}, \{4, 5\}, \text{anglemat}], x]$ 
```

```
Out[*]:=  $\{ 16\,129 - 1234\,x^2 + 17\,x^4, 16\,129 - 1234\,x^2 + 17\,x^4 \}$ 
```

```

In[*]:= For[i = 1, i ≤ Length[list], i++,
  If[compatiblefrminipoly[
    MinimalPolynomial[combinationangle[ $\left\{\frac{1}{2} (711 - 145 \sqrt{17}), \frac{1}{2} (711 + 145 \sqrt{17})\right\}$ ,
    {15, i}, {4, 5}, anglemat], x]] == 1, Print[i]
  ]
]
6
13
15
23

```

```

In[*]:= For[i = 1, i ≤ Length[list], i++,
  If[compatiblefrminipoly[MinimalPolynomial[
    combinationangle[ $\left\{-16, \frac{1}{2} (103 - 17 \sqrt{17}), \frac{1}{2} (103 + 17 \sqrt{17})\right\}$ ,
    {15, i}, {2, 4, 5}, anglemat], x]] == 1, Print[i]
  ]
]
6
15

refinedlist = {};

For[i = 1, i ≤ Length[list], i++,
  If[compatible[combinations[chi, (x + 5) (x - 5), warrantpoly, list[[i]], list,
    anglesquared] // FullSimplify] == 1, AppendTo[refinedlist, list[[i]]]
]

refinedlist
{(-5 + x) (-1 + 47 x - 15 x2 + x3), 29 - 228 x + 122 x2 - 20 x3 + x4}

refinedA = CoefficientList[refinedlist, x]
{{5, -236, 122, -20, 1}, {29, -228, 122, -20, 1}}

refinedA // MatrixForm

$$\begin{pmatrix} 5 & -236 & 122 & -20 & 1 \\ 29 & -228 & 122 & -20 & 1 \end{pmatrix}$$


Array[c, 5].Transpose[refinedA]
{5 c[1] - 236 c[2] + 122 c[3] - 20 c[4] + c[5],
 29 c[1] - 228 c[2] + 122 c[3] - 20 c[4] + c[5]}

Array[c, 5].g
1105 c[1] - 6684 c[2] + 3538 c[3] - 580 c[4] + 29 c[5]

```

```

cert = Flatten[Array[c, 5] /.
  FindInstance[1105 c[1] - 6684 c[2] + 3538 c[3] - 580 c[4] + 29 c[5] < 0 &&
    5 c[1] - 236 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    29 c[1] - 228 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0, Array[c, 5], Integers]]
{-46, -7, 0, 0, 0}

GCD[-46, -7, 0, 0, 0]
1

Reverse[cert]
{0, 0, 0, -7, -46}

cert.g
-4042

cert.Transpose[refinedA]
{1422, 262}

```

$$\text{chi} = (-7 + x)^2 (-5 + x)^8 (-3 + x)^2 (5 + x)^{15} (52 - 15x + x^2)$$

$$(-7 + x)^2 (-5 + x)^8 (-3 + x)^2 (5 + x)^{15} (52 - 15x + x^2)$$

```

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{-525, 1405, -890, 226, -25, 1}, {-85, 1277, -882, 226, -25, 1},
{-165, 1293, -882, 226, -25, 1}, {-245, 1309, -882, 226, -25, 1},
{-357, 1325, -882, 226, -25, 1}, {275, 1165, -874, 226, -25, 1},
{195, 1181, -874, 226, -25, 1}, {115, 1197, -874, 226, -25, 1},
{35, 1213, -874, 226, -25, 1}, {475, 1085, -866, 226, -25, 1},
{395, 1101, -866, 226, -25, 1}, {315, 1117, -866, 226, -25, 1},
{675, 1005, -858, 226, -25, 1}, {595, 1021, -858, 226, -25, 1},
{875, 925, -850, 226, -25, 1}, {1155, 829, -842, 226, -25, 1}}

A = {{-525, 1405, -890, 226, -25, 1}, {-85, 1277, -882, 226, -25, 1},
{-165, 1293, -882, 226, -25, 1}, {-245, 1309, -882, 226, -25, 1},
{-357, 1325, -882, 226, -25, 1}, {275, 1165, -874, 226, -25, 1},
{195, 1181, -874, 226, -25, 1}, {115, 1197, -874, 226, -25, 1},
{35, 1213, -874, 226, -25, 1}, {475, 1085, -866, 226, -25, 1},
{395, 1101, -866, 226, -25, 1}, {315, 1117, -866, 226, -25, 1},
{675, 1005, -858, 226, -25, 1}, {595, 1021, -858, 226, -25, 1},
{875, 925, -850, 226, -25, 1}, {1155, 829, -842, 226, -25, 1}};

```

A // MatrixForm

$$\begin{pmatrix} -525 & 1405 & -890 & 226 & -25 & 1 \\ -85 & 1277 & -882 & 226 & -25 & 1 \\ -165 & 1293 & -882 & 226 & -25 & 1 \\ -245 & 1309 & -882 & 226 & -25 & 1 \\ -357 & 1325 & -882 & 226 & -25 & 1 \\ 275 & 1165 & -874 & 226 & -25 & 1 \\ 195 & 1181 & -874 & 226 & -25 & 1 \\ 115 & 1197 & -874 & 226 & -25 & 1 \\ 35 & 1213 & -874 & 226 & -25 & 1 \\ 475 & 1085 & -866 & 226 & -25 & 1 \\ 395 & 1101 & -866 & 226 & -25 & 1 \\ 315 & 1117 & -866 & 226 & -25 & 1 \\ 675 & 1005 & -858 & 226 & -25 & 1 \\ 595 & 1021 & -858 & 226 & -25 & 1 \\ 875 & 925 & -850 & 226 & -25 & 1 \\ 1155 & 829 & -842 & 226 & -25 & 1 \end{pmatrix}$$

g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]

{-4345, 36841, -25490, 6554, -725, 29}

Solve[n[1] ≥ 0 && n[2] ≥ 0 && n[3] ≥ 0 && n[4] ≥ 0 && n[5] ≥ 0 && n[6] ≥ 0 && n[7] ≥ 0 &&
n[8] ≥ 0 && n[9] ≥ 0 && n[10] ≥ 0 && n[11] ≥ 0 && n[12] ≥ 0 && n[13] ≥ 0 &&
n[14] ≥ 0 && n[15] ≥ 0 && n[16] ≥ 0 && Array[n, 16].A == g, Array[n, 16], Integers]

{{n[1] → 0, n[2] → 0, n[3] → 0, n[4] → 0,
n[5] → 20, n[6] → 6, n[7] → 1, n[8] → 0, n[9] → 0, n[10] → 2,
n[11] → 0, n[12] → 0, n[13] → 0, n[14] → 0, n[15] → 0, n[16] → 0},
{n[1] → 0, n[2] → 0, n[3] → 0, n[4] → 0, n[5] → 20, n[6] → 7, n[7] → 0,
n[8] → 0, n[9] → 0, n[10] → 1, n[11] → 1, n[12] → 0, n[13] → 0,
n[14] → 0, n[15] → 0, n[16] → 0}, {n[1] → 0, n[2] → 0, n[3] → 0,
n[4] → 0, n[5] → 20, n[6] → 7, n[7] → 1, n[8] → 0, n[9] → 0, n[10] → 0,
n[11] → 0, n[12] → 0, n[13] → 1, n[14] → 0, n[15] → 0, n[16] → 0},
{n[1] → 0, n[2] → 0, n[3] → 0, n[4] → 0, n[5] → 20, n[6] → 8,
n[7] → 0, n[8] → 0, n[9] → 0, n[10] → 0, n[11] → 0,
n[12] → 0, n[13] → 0, n[14] → 1, n[15] → 0, n[16] → 0}}

Array[c, 6].Transpose[A]

```
{ -525 c[1] + 1405 c[2] - 890 c[3] + 226 c[4] - 25 c[5] + c[6] ,
  -85 c[1] + 1277 c[2] - 882 c[3] + 226 c[4] - 25 c[5] + c[6] ,
  -165 c[1] + 1293 c[2] - 882 c[3] + 226 c[4] - 25 c[5] + c[6] ,
  -245 c[1] + 1309 c[2] - 882 c[3] + 226 c[4] - 25 c[5] + c[6] ,
  -357 c[1] + 1325 c[2] - 882 c[3] + 226 c[4] - 25 c[5] + c[6] ,
  275 c[1] + 1165 c[2] - 874 c[3] + 226 c[4] - 25 c[5] + c[6] ,
  195 c[1] + 1181 c[2] - 874 c[3] + 226 c[4] - 25 c[5] + c[6] ,
  115 c[1] + 1197 c[2] - 874 c[3] + 226 c[4] - 25 c[5] + c[6] ,
  35 c[1] + 1213 c[2] - 874 c[3] + 226 c[4] - 25 c[5] + c[6] ,
  475 c[1] + 1085 c[2] - 866 c[3] + 226 c[4] - 25 c[5] + c[6] ,
  395 c[1] + 1101 c[2] - 866 c[3] + 226 c[4] - 25 c[5] + c[6] ,
  315 c[1] + 1117 c[2] - 866 c[3] + 226 c[4] - 25 c[5] + c[6] ,
  675 c[1] + 1005 c[2] - 858 c[3] + 226 c[4] - 25 c[5] + c[6] ,
  595 c[1] + 1021 c[2] - 858 c[3] + 226 c[4] - 25 c[5] + c[6] ,
  875 c[1] + 925 c[2] - 850 c[3] + 226 c[4] - 25 c[5] + c[6] ,
  1155 c[1] + 829 c[2] - 842 c[3] + 226 c[4] - 25 c[5] + c[6] }
```

Array[c, 6].g

```
-4345 c[1] + 36841 c[2] - 25490 c[3] + 6554 c[4] - 725 c[5] + 29 c[6]
```

warrant1 = Flatten[Array[c, 6] /. FindInstance[

```
-4345 c[1] + 36841 c[2] - 25490 c[3] + 6554 c[4] - 725 c[5] + 29 c[6] < 0 &&
-525 c[1] + 1405 c[2] - 890 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
-85 c[1] + 1277 c[2] - 882 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
-165 c[1] + 1293 c[2] - 882 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
-245 c[1] + 1309 c[2] - 882 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
-357 c[1] + 1325 c[2] - 882 c[3] + 226 c[4] - 25 c[5] + c[6] < 0 &&
275 c[1] + 1165 c[2] - 874 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
195 c[1] + 1181 c[2] - 874 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
115 c[1] + 1197 c[2] - 874 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
35 c[1] + 1213 c[2] - 874 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
475 c[1] + 1085 c[2] - 866 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
395 c[1] + 1101 c[2] - 866 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
315 c[1] + 1117 c[2] - 866 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
675 c[1] + 1005 c[2] - 858 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
595 c[1] + 1021 c[2] - 858 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
875 c[1] + 925 c[2] - 850 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 && 1155 c[1] +
829 c[2] - 842 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0, Array[c, 6], Integers]]
```

```
{154, 507, 708, 0, 0, 0}
```

GCD[154, 507, 708, 0, 0, 0]

```
1
```

Reverse[warrant1]

```
{0, 0, 0, 708, 507, 154}
```

warrant1.g

-37 663

warrant1.Transpose[A]

{1365, 9893, 5685, 1477, -7659, 14 213, 10 005,
5797, 1589, 10 117, 5909, 1701, 6021, 1813, 1925, 2037}

warrant2 = Flatten[Array[c, 6] /. FindInstance[

-4345 c[1] + 36 841 c[2] - 25 490 c[3] + 6554 c[4] - 725 c[5] + 29 c[6] < 0 &&
-525 c[1] + 1405 c[2] - 890 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
-85 c[1] + 1277 c[2] - 882 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
-165 c[1] + 1293 c[2] - 882 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
-245 c[1] + 1309 c[2] - 882 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
-357 c[1] + 1325 c[2] - 882 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
275 c[1] + 1165 c[2] - 874 c[3] + 226 c[4] - 25 c[5] + c[6] < 0 &&
195 c[1] + 1181 c[2] - 874 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
115 c[1] + 1197 c[2] - 874 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
35 c[1] + 1213 c[2] - 874 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
475 c[1] + 1085 c[2] - 866 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
395 c[1] + 1101 c[2] - 866 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
315 c[1] + 1117 c[2] - 866 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
675 c[1] + 1005 c[2] - 858 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
595 c[1] + 1021 c[2] - 858 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 &&
875 c[1] + 925 c[2] - 850 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0 && 1155 c[1] +
829 c[2] - 842 c[3] + 226 c[4] - 25 c[5] + c[6] ≥ 0, Array[c, 6], Integers]]

{1196, 6783, 39 525, 0, 0, 26 302 558}

GCD[1196, 6783, 39 525, 0, 0, 26 302 558]

1

Reverse[warrant2]

{26 302 558, 0, 0, 39 525, 6783, 1196}

warrant2.g

-22 185

warrant2.Transpose[A]

{27 523, 1739, 14 587, 27 435, 2011, -11 197, 1651,
14 499, 27 347, 1563, 14 411, 27 259, 14 323, 27 171, 27 083, 26 995}

```
feasibleinterlacingpolylist[chi]
```

```
{ (-7 + x) (-5 + x) (-3 + x) (5 - 10 x + x^2), (-5 + x) (17 - 252 x + 126 x^2 - 20 x^3 + x^4),  
  (-5 + x) (33 - 252 x + 126 x^2 - 20 x^3 + x^4), (-7 + x) (-5 + x) (-7 + 35 x - 13 x^2 + x^3),  
  (-7 + x) (-3 + x) (-17 + 55 x - 15 x^2 + x^3), (-5 + x)^2 (11 + 51 x - 15 x^2 + x^3),  
  (-5 + x) (-39 - 244 x + 126 x^2 - 20 x^3 + x^4), (-5 + x) (-23 - 244 x + 126 x^2 - 20 x^3 + x^4),  
  (-7 + x) (-5 + x) (1 + 35 x - 13 x^2 + x^3), (-5 + x)^2 (19 + 51 x - 15 x^2 + x^3),  
  (-5 + x) (-79 - 236 x + 126 x^2 - 20 x^3 + x^4), (-9 + x) (-7 + x) (-5 + x) (-1 - 4 x + x^2),  
  (-9 + x) (-5 + x)^2 (-3 - 6 x + x^2), (-7 + x) (-5 + x) (17 + 35 x - 13 x^2 + x^3),  
  (-7 + x) (-5 + x)^2 (-5 - 8 x + x^2), (-7 + x) (-5 + x) (33 + 35 x - 13 x^2 + x^3) }
```

```
list = { (-7 + x) (-5 + x) (-3 + x) (5 - 10 x + x^2), (-5 + x) (17 - 252 x + 126 x^2 - 20 x^3 + x^4),  
  (-5 + x) (33 - 252 x + 126 x^2 - 20 x^3 + x^4), (-7 + x) (-5 + x) (-7 + 35 x - 13 x^2 + x^3),  
  (-7 + x) (-3 + x) (-17 + 55 x - 15 x^2 + x^3), (-5 + x)^2 (11 + 51 x - 15 x^2 + x^3),  
  (-5 + x) (-39 - 244 x + 126 x^2 - 20 x^3 + x^4), (-5 + x) (-23 - 244 x + 126 x^2 - 20 x^3 + x^4),  
  (-7 + x) (-5 + x) (1 + 35 x - 13 x^2 + x^3), (-5 + x)^2 (19 + 51 x - 15 x^2 + x^3),  
  (-5 + x) (-79 - 236 x + 126 x^2 - 20 x^3 + x^4), (-9 + x) (-7 + x) (-5 + x) (-1 - 4 x + x^2),  
  (-9 + x) (-5 + x)^2 (-3 - 6 x + x^2), (-7 + x) (-5 + x) (17 + 35 x - 13 x^2 + x^3),  
  (-7 + x) (-5 + x)^2 (-5 - 8 x + x^2), (-7 + x) (-5 + x) (33 + 35 x - 13 x^2 + x^3) };
```

```
warrantpoly = { (-7 + x) (-3 + x) (-17 + 55 x - 15 x^2 + x^3), (-5 + x)^2 (11 + 51 x - 15 x^2 + x^3) }  
{ (-7 + x) (-3 + x) (-17 + 55 x - 15 x^2 + x^3), (-5 + x)^2 (11 + 51 x - 15 x^2 + x^3) }
```

```
anglesquared = anglesquaredmat[chi, list] // FullSimplify;
```


anglesquared // MatrixForm

$$\begin{pmatrix} \frac{10}{19} & 0 & 0 & \frac{9}{38} + \frac{35}{38\sqrt{17}} & 0 & \frac{9}{38} - \frac{35}{38\sqrt{17}} \\ \frac{59}{114} & \frac{1}{8} & 0 & \frac{493+117\sqrt{17}}{5168} & \frac{1}{6} & \frac{493-117\sqrt{17}}{5168} \\ \frac{473}{912} & \frac{3}{32} & 0 & \frac{3145+673\sqrt{17}}{20672} & \frac{1}{12} & \frac{3145-673\sqrt{17}}{20672} \\ \frac{79}{152} & \frac{1}{16} & 0 & \frac{2159+439\sqrt{17}}{10336} & 0 & \frac{2159-439\sqrt{17}}{10336} \\ \frac{99}{190} & 0 & \frac{2}{5} & \frac{3}{76} - \frac{1}{76\sqrt{17}} & 0 & \frac{51+\sqrt{17}}{1292} \\ \frac{155}{304} & \frac{7}{32} & 0 & \frac{221+21\sqrt{17}}{20672} & \frac{1}{4} & \frac{221-21\sqrt{17}}{20672} \\ \frac{233}{456} & \frac{3}{16} & 0 & \frac{697+113\sqrt{17}}{10336} & \frac{1}{6} & \frac{697-113\sqrt{17}}{10336} \\ \frac{467}{912} & \frac{5}{32} & 0 & \frac{2567+431\sqrt{17}}{20672} & \frac{1}{12} & \frac{2567-431\sqrt{17}}{20672} \\ \frac{39}{76} & \frac{1}{8} & 0 & \frac{935+159\sqrt{17}}{5168} & 0 & \frac{935-159\sqrt{17}}{5168} \\ \frac{115}{228} & \frac{1}{4} & 0 & \frac{3}{76} - \frac{1}{76\sqrt{17}} & \frac{1}{6} & \frac{51+\sqrt{17}}{1292} \\ \frac{461}{912} & \frac{7}{32} & 0 & \frac{9(221+21\sqrt{17})}{20672} & \frac{1}{12} & -\frac{9(-221+21\sqrt{17})}{20672} \\ \frac{77}{152} & \frac{3}{16} & 0 & \frac{93}{608} + \frac{197}{608\sqrt{17}} & 0 & \frac{93}{608} - \frac{197}{608\sqrt{17}} \\ \frac{455}{912} & \frac{9}{32} & 0 & \frac{1411-53\sqrt{17}}{20672} & \frac{1}{12} & \frac{1411+53\sqrt{17}}{20672} \\ \frac{1}{2} & \frac{1}{4} & 0 & \frac{1}{136} (17 + \sqrt{17}) & 0 & \frac{1}{8} - \frac{1}{8\sqrt{17}} \\ \frac{75}{152} & \frac{5}{16} & 0 & \frac{59}{608} - \frac{45}{608\sqrt{17}} & 0 & \frac{59}{608} + \frac{45}{608\sqrt{17}} \\ \frac{37}{76} & \frac{3}{8} & 0 & \frac{357-83\sqrt{17}}{5168} & 0 & \frac{357+83\sqrt{17}}{5168} \end{pmatrix}$$

refinedlist = {};

For[i = 1, i ≤ Length[list], i++,

 If[compatible[

 combinations[chi, (x + 5) (x - 5) (x - 3) (x - 7), warrantpoly[[1], list[[i]], list,
 anglesquared] // FullSimplify] == 1, AppendTo[refinedlist, list[[i]]]

]

refinedlist

{ (-7 + x) (-5 + x) (-3 + x) (5 - 10 x + x²),
 (-5 + x) (17 - 252 x + 126 x² - 20 x³ + x⁴), (-7 + x) (-3 + x) (-17 + 55 x - 15 x² + x³),
 (-5 + x)² (11 + 51 x - 15 x² + x³), (-5 + x)² (19 + 51 x - 15 x² + x³),
 (-5 + x) (-79 - 236 x + 126 x² - 20 x³ + x⁴), (-7 + x) (-5 + x) (33 + 35 x - 13 x² + x³) }

refinedlist = { (-7 + x) (-3 + x) (-17 + 55 x - 15 x² + x³),
 (-5 + x)² (11 + 51 x - 15 x² + x³), (-5 + x)² (19 + 51 x - 15 x² + x³),
 (-5 + x) (-79 - 236 x + 126 x² - 20 x³ + x⁴), (-7 + x) (-5 + x) (-3 + x) (5 - 10 x + x²),
 (-5 + x) (17 - 252 x + 126 x² - 20 x³ + x⁴), (-7 + x) (-5 + x) (33 + 35 x - 13 x² + x³) };

refinedA = CoefficientList[refinedlist, x];

```
refinedA // MatrixForm
```

$$\begin{pmatrix} -357 & 1325 & -882 & 226 & -25 & 1 \\ 275 & 1165 & -874 & 226 & -25 & 1 \\ 475 & 1085 & -866 & 226 & -25 & 1 \\ 395 & 1101 & -866 & 226 & -25 & 1 \\ -525 & 1405 & -890 & 226 & -25 & 1 \\ -85 & 1277 & -882 & 226 & -25 & 1 \\ 1155 & 829 & -842 & 226 & -25 & 1 \end{pmatrix}$$

```
Solve[n[1] ≥ 0 && n[2] ≥ 0 && n[3] ≥ 0 && n[4] ≥ 0 && n[5] ≥ 0 &&
  n[6] ≥ 0 && n[7] ≥ 0 && Array[n, 7].refinedA == g, Array[n, 7], Integers]
{{n[1] → 20, n[2] → 7, n[3] → 1, n[4] → 1, n[5] → 0, n[6] → 0, n[7] → 0}}
```

```
uniquesoln =
```

```
Flatten[Array[n, 7] /. Solve[n[1] ≥ 0 && n[2] ≥ 0 && n[3] ≥ 0 && n[4] ≥ 0 && n[5] ≥ 0 &&
  n[6] ≥ 0 && n[7] ≥ 0 && Array[n, 7].refinedA == g, Array[n, 7], Integers]]
{20, 7, 1, 1, 0, 0, 0}
```

```
refinedanglesquared = anglesquaredmat[chi, refinedlist] // FullSimplify;
```

```
refinedanglesquared // MatrixForm
```

$$\begin{pmatrix} \frac{99}{190} & 0 & \frac{2}{5} & \frac{3}{76} - \frac{1}{76\sqrt{17}} & 0 & \frac{51+\sqrt{17}}{1292} \\ \frac{155}{304} & \frac{7}{32} & 0 & \frac{221+21\sqrt{17}}{20672} & \frac{1}{4} & \frac{221-21\sqrt{17}}{20672} \\ \frac{115}{228} & \frac{1}{4} & 0 & \frac{3}{76} - \frac{1}{76\sqrt{17}} & \frac{1}{6} & \frac{51+\sqrt{17}}{1292} \\ \frac{461}{912} & \frac{7}{32} & 0 & \frac{9(221+21\sqrt{17})}{20672} & \frac{1}{12} & -\frac{9(-221+21\sqrt{17})}{20672} \\ \frac{10}{19} & 0 & 0 & \frac{9}{38} + \frac{35}{38\sqrt{17}} & 0 & \frac{9}{38} - \frac{35}{38\sqrt{17}} \\ \frac{59}{114} & \frac{1}{8} & 0 & \frac{493+117\sqrt{17}}{5168} & \frac{1}{6} & \frac{493-117\sqrt{17}}{5168} \\ \frac{37}{76} & \frac{3}{8} & 0 & \frac{357-83\sqrt{17}}{5168} & 0 & \frac{357+83\sqrt{17}}{5168} \end{pmatrix}$$

$$\text{beta} = \text{Sqrt}\left[\frac{3}{76} - \frac{1}{76\sqrt{17}}\right];$$

$$\text{beta} * (\text{Sqrt}[17] + 1) / 8 - \text{Sqrt}\left[\frac{221 + 21\sqrt{17}}{20672}\right] // \text{FullSimplify}$$

```
0
```

$$\text{betabar} = \text{Sqrt}\left[\frac{51 + \sqrt{17}}{1292}\right];$$

$$\text{betabar} * (\text{Sqrt}[17] - 1) / 8 - \text{Sqrt}\left[\frac{221 - 21\sqrt{17}}{20672}\right] // \text{FullSimplify}$$

```
0
```

```

u = {beta, beta, beta, beta, beta, beta, beta, beta,
     beta, beta, beta, beta, beta, beta, beta, beta, beta, beta,
     beta, beta, beta * (Sqrt[17] + 1) / 8, beta * (Sqrt[17] + 1) / 8,
     beta * (Sqrt[17] + 1) / 8, beta * (Sqrt[17] + 1) / 8, beta * (Sqrt[17] + 1) / 8,
     beta * (Sqrt[17] + 1) / 8, beta * (Sqrt[17] + 1) / 8, 3 * beta * (Sqrt[17] + 1) / 8};

```

```

combinations[chi, (x + 5) (x - 5) (x - 3) (x - 7), refinedlist[[1]],
  refinedlist[[2]], refinedlist, refinedanglesquared] // FullSimplify

```

$$\left\{ \frac{75}{\sqrt{17}}, -19 \right\}$$

```

v = {betabar, betabar, betabar, betabar, betabar, betabar,
     betabar, betabar, betabar, betabar, betabar, betabar, betabar,
     betabar, betabar, betabar, betabar, betabar, betabar, betabar,
     betabar, -betabar * (Sqrt[17] - 1) / 8, -betabar * (Sqrt[17] - 1) / 8,
     -betabar * (Sqrt[17] - 1) / 8, -betabar * (Sqrt[17] - 1) / 8,
     -betabar * (Sqrt[17] - 1) / 8, -betabar * (Sqrt[17] - 1) / 8,
     -betabar * (Sqrt[17] - 1) / 8, -3 * betabar * (Sqrt[17] - 1) / 8};

```

```
Total[u * v] // FullSimplify
```

$$\sqrt{\frac{17}{38}}$$

```

v = {-betabar, -betabar, -betabar, -betabar, -betabar, -betabar,
     -betabar, -betabar, -betabar, -betabar, -betabar, -betabar, -betabar,
     -betabar, -betabar, -betabar, -betabar, -betabar, -betabar, -betabar,
     -betabar, betabar * (Sqrt[17] - 1) / 8, betabar * (Sqrt[17] - 1) / 8,
     betabar * (Sqrt[17] - 1) / 8, betabar * (Sqrt[17] - 1) / 8,
     betabar * (Sqrt[17] - 1) / 8, betabar * (Sqrt[17] - 1) / 8,
     betabar * (Sqrt[17] - 1) / 8, 3 * betabar * (Sqrt[17] - 1) / 8};

```

```
Total[u * v] // FullSimplify
```

$$-\sqrt{\frac{17}{38}}$$

```
In[ ]:= chisub = (-9 + x) (-5 + x)^9 (5 + x)^14 (31 - 12 x + x^2) (-1 - 4 x + x^2)
```

```
Out[ ]:= (-9 + x) (-5 + x)^9 (5 + x)^14 (31 - 12 x + x^2) (-1 - 4 x + x^2)
```

```
list = feasibleinterlacingpolylist[chisub]
```

```

{(-5 + x) (150 - 141 x - 210 x^2 + 124 x^3 - 20 x^4 + x^5),
 -718 + 855 x + 909 x^2 - 830 x^3 + 224 x^4 - 25 x^5 + x^6,
 -686 + 855 x + 909 x^2 - 830 x^3 + 224 x^4 - 25 x^5 + x^6,

```

$$\begin{aligned}
& -654 + 855x + 909x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-1+x)(1+x)(38-13x+x^2)(31-12x+x^2), \\
& (-5+x)(1+x)(31-12x+x^2)(6-9x+x^2), \\
& (1+x)(31-12x+x^2)(-34+51x-14x^2+x^3), \\
& (-9+x)(-5+x)(1+x)(-22+37x-12x^2+x^3), \\
& (-9+x)(-5+x)(1+x)(-18+37x-12x^2+x^3), \\
& (-5+x)(1+x)(170-351x+145x^2-21x^3+x^4), \\
& (-5+x)(1+x)(178-351x+145x^2-21x^3+x^4), \\
& (-5+x)(1+x)(150-347x+145x^2-21x^3+x^4), \\
& (1+x)(-974+1973x-1080x^2+250x^3-26x^4+x^5), \\
& (1+x)(-1014+1981x-1080x^2+250x^3-26x^4+x^5), \\
& -1042 + 859x + 945x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -1010 + 859x + 945x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& (31-12x+x^2)(-22+13x+37x^2-13x^3+x^4), \\
& (-5+x)(218-237x-198x^2+124x^3-20x^4+x^5), \\
& (-5+x)(114-157x-206x^2+124x^3-20x^4+x^5), \\
& (-5+x)(-6-7x+x^2)(-11+39x-13x^2+x^3), \\
& -298 + 851x + 873x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x)(154-165x-206x^2+124x^3-20x^4+x^5), \\
& -738 + 979x + 865x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -706 + 979x + 865x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -922 + 795x + 953x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -890 + 795x + 953x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x)(3-8x+x^2)(30+25x-12x^2+x^3), \\
& -418 + 915x + 865x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -798 + 623x + 1005x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x)(194-173x-206x^2+124x^3-20x^4+x^5), \\
& -938 + 1059x + 857x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -906 + 1059x + 857x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -958 + 983x + 893x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -926 + 983x + 893x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x)(138-181x-206x^2+124x^3-20x^4+x^5), \\
& -6446 + 4087x + 333x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x)(1194-565x-174x^2+124x^3-20x^4+x^5), \\
& (-9+x)(-5+x)(-14+15x+25x^2-11x^3+x^4), \\
& -598 + 871x + 901x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (31-12x+x^2)(-26+17x+37x^2-13x^3+x^4), \\
& -1050 + 827x + 953x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -1018 + 827x + 953x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -998 + 951x + 901x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -966 + 951x + 901x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -934 + 951x + 901x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -974 + 919x + 909x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -942 + 919x + 909x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -818 + 1075x + 849x^2 - 826x^3 + 224x^4 - 25x^5 + x^6,
\end{aligned}$$

$$\begin{aligned}
& -858 + 1043x + 857x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -826 + 1043x + 857x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -726 + 575x + 1013x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -794 + 763x + 953x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -762 + 763x + 953x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -722 + 715x + 961x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& (-23 + 43x - 13x^2 + x^3)(30 + 25x - 12x^2 + x^3), \\
& (-5 + x)(158 - 149x - 210x^2 + 124x^3 - 20x^4 + x^5), \\
& -758 + 903x + 901x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -726 + 903x + 901x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -678 + 807x + 917x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -646 + 807x + 917x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -614 + 807x + 917x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(130 - 173x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& -618 + 995x + 857x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(122 - 165x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& -578 + 947x + 865x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(94 - 189x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -1246 + 799x + 989x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -802 + 731x + 961x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -770 + 731x + 961x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(174 - 149x - 210x^2 + 124x^3 - 20x^4 + x^5), \\
& -838 + 919x + 901x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -806 + 919x + 901x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -598 + 791x + 917x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -566 + 791x + 917x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -534 + 791x + 917x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -478 + 727x + 925x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -446 + 727x + 925x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(114 - 173x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(42 - 149x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& -178 + 787x + 881x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-9 + x)(-1 - 4x + x^2)(-6 + 33x - 12x^2 + x^3), (31 - 12x + x^2)(2 - 9x + x^2)(-1 - 4x + x^2), \\
& (-9 + x)(42 - 33x - 122x^2 + 80x^3 - 16x^4 + x^5), \\
& -426 + 355x + 1065x^2 - 842x^3 + 224x^4 - 25x^5 + x^6, \\
& -554 + 387x + 1065x^2 - 842x^3 + 224x^4 - 25x^5 + x^6, \\
& (-9 + x)(-1 - 4x + x^2)(-2 + 33x - 12x^2 + x^3), \\
& -130 + 243x + 1073x^2 - 842x^3 + 224x^4 - 25x^5 + x^6, \\
& -98 + 243x + 1073x^2 - 842x^3 + 224x^4 - 25x^5 + x^6, \\
& -178 + 259x + 1073x^2 - 842x^3 + 224x^4 - 25x^5 + x^6, \\
& -226 + 275x + 1073x^2 - 842x^3 + 224x^4 - 25x^5 + x^6, \\
& -306 + 291x + 1073x^2 - 842x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2)(-14 + 5x + 37x^2 - 13x^3 + x^4), \\
& -58 + 195x + 1081x^2 - 842x^3 + 224x^4 - 25x^5 + x^6, \\
& (-1 - 4x + x^2)(26 - 299x + 141x^2 - 21x^3 + x^4), \\
& -106 + 211x + 1081x^2 - 842x^3 + 224x^4 - 25x^5 + x^6,
\end{aligned}$$

$$\begin{aligned}
& (31 - 12x + x^2) (-6 + 5x + 37x^2 - 13x^3 + x^4), \\
& (-9 + x) (102 - 65x - 118x^2 + 80x^3 - 16x^4 + x^5), \\
& -998 + 703x + 997x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -1046 + 719x + 997x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -670 + 591x + 1005x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -750 + 607x + 1005x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -718 + 607x + 1005x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -926 + 655x + 1005x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& (-1 + x) (31 - 12x + x^2) (34 + 25x - 12x^2 + x^3), \\
& (-9 + x) (2 - 5x + x^2) (19 + 23x - 11x^2 + x^3), \\
& -422 + 495x + 1013x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -390 + 495x + 1013x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -502 + 511x + 1013x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -470 + 511x + 1013x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -550 + 527x + 1013x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -518 + 527x + 1013x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& (-23 + 43x - 13x^2 + x^3) (26 + 25x - 12x^2 + x^3), \\
& -678 + 559x + 1013x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-26 + 9x + 37x^2 - 13x^3 + x^4), (-9 + x) (-1 - 4x + x^2) (2 + 33x - 12x^2 + x^3), \\
& (-9 + x) (14 - 41x - 118x^2 + 80x^3 - 16x^4 + x^5), \\
& -94 + 383x + 1021x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -62 + 383x + 1021x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -174 + 399x + 1021x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -142 + 399x + 1021x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -254 + 415x + 1021x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -222 + 415x + 1021x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -190 + 415x + 1021x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -302 + 431x + 1021x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -270 + 431x + 1021x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -350 + 447x + 1021x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -430 + 463x + 1021x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -398 + 463x + 1021x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -478 + 479x + 1021x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-18 + 9x + 37x^2 - 13x^3 + x^4), \\
& -6 + 319x + 1029x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -54 + 335x + 1029x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -22 + 335x + 1029x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& (-1 - 4x + x^2) (-10 - 295x + 141x^2 - 21x^3 + x^4), \\
& (17 + 35x - 13x^2 + x^3) (-6 + 33x - 12x^2 + x^3), \\
& -70 + 351x + 1029x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -182 + 367x + 1029x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -150 + 367x + 1029x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& -230 + 383x + 1029x^2 - 838x^3 + 224x^4 - 25x^5 + x^6, \\
& (-11 + 39x - 13x^2 + x^3) (18 + 29x - 12x^2 + x^3), \\
& (31 - 12x + x^2) (-5 - 8x + x^2) (2 - 5x + x^2), (31 - 12x + x^2) (-2 + 9x + 37x^2 - 13x^3 + x^4), \\
& -1866 + 1163x + 921x^2 - 834x^3 + 224x^4 - 25x^5 + x^6,
\end{aligned}$$

$$\begin{aligned}
& -1538 + 1051x + 929x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -1618 + 1067x + 929x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& (-9 + x)(-1 + x)(-138 - 49x + 65x^2 - 15x^3 + x^4), \\
& -1210 + 939x + 937x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -1290 + 955x + 937x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -1370 + 971x + 937x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -1338 + 971x + 937x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -1418 + 987x + 937x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -1546 + 1019x + 937x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& (-9 + x)(98 - 81x - 114x^2 + 80x^3 - 16x^4 + x^5), \\
& -994 + 843x + 945x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -962 + 843x + 945x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -1122 + 875x + 945x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -1090 + 875x + 945x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -1170 + 891x + 945x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& (-1 + x)(1218 + 311x - 634x^2 + 200x^3 - 24x^4 + x^5), \\
& -1298 + 923x + 945x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -1346 + 939x + 945x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2)(-46 + 13x + 37x^2 - 13x^3 + x^4), \\
& (-9 + x)(74 - 73x - 114x^2 + 80x^3 - 16x^4 + x^5), \\
& -634 + 731x + 953x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -746 + 747x + 953x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -714 + 747x + 953x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -682 + 747x + 953x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -874 + 779x + 953x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -842 + 779x + 953x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -970 + 811x + 953x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -1098 + 843x + 953x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& (-9 + x)(34 - 65x - 114x^2 + 80x^3 - 16x^4 + x^5), \\
& -418 + 635x + 961x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -386 + 635x + 961x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& (3 - 8x + x^2)(-118 - 103x + 85x^2 - 17x^3 + x^4), \\
& -498 + 651x + 961x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -466 + 651x + 961x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -434 + 651x + 961x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -546 + 667x + 961x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -514 + 667x + 961x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -482 + 667x + 961x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -626 + 683x + 961x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -594 + 683x + 961x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -562 + 683x + 961x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -674 + 699x + 961x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -642 + 699x + 961x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -850 + 747x + 961x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2)(-30 + 13x + 37x^2 - 13x^3 + x^4), \\
& (-9 + x)(-1 - 4x + x^2)(6 + 33x - 12x^2 + x^3),
\end{aligned}$$

$$\begin{aligned}
& (-9 + x) (-5 + x) (-2 + 11x + 25x^2 - 11x^3 + x^4), \\
& -58 + 523x + 969x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -26 + 523x + 969x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (34 - 101x - 214x^2 + 124x^3 - 20x^4 + x^5), \\
& -138 + 539x + 969x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -106 + 539x + 969x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (50 - 101x - 214x^2 + 124x^3 - 20x^4 + x^5), \\
& -218 + 555x + 969x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -186 + 555x + 969x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -154 + 555x + 969x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -298 + 571x + 969x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& (-14 + 47x - 14x^2 + x^3) (19 + 23x - 11x^2 + x^3), \\
& -234 + 571x + 969x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -378 + 587x + 969x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -346 + 587x + 969x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -314 + 587x + 969x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -426 + 603x + 969x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -394 + 603x + 969x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -362 + 603x + 969x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -474 + 619x + 969x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -442 + 619x + 969x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -554 + 635x + 969x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -522 + 635x + 969x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -490 + 635x + 969x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -602 + 651x + 969x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& (38 - 13x + x^2) (-15 + 12x + 30x^2 - 12x^3 + x^4), \\
& (-5 + x) (-6 - 93x - 214x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (10 - 93x - 214x^2 + 124x^3 - 20x^4 + x^5), \\
& -18 + 475x + 977x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& 14 + 475x + 977x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& (-1 - 4x + x^2) (-46 - 291x + 141x^2 - 21x^3 + x^4), \\
& (-5 + x) (26 - 93x - 214x^2 + 124x^3 - 20x^4 + x^5), \\
& -98 + 491x + 977x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -66 + 491x + 977x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& (17 + 35x - 13x^2 + x^3) (-2 + 33x - 12x^2 + x^3), \\
& -178 + 507x + 977x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -146 + 507x + 977x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -114 + 507x + 977x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -226 + 523x + 977x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -194 + 523x + 977x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -162 + 523x + 977x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -306 + 539x + 977x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -274 + 539x + 977x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& (-11 + 39x - 13x^2 + x^3) (22 + 29x - 12x^2 + x^3), \\
& -354 + 555x + 977x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -322 + 555x + 977x^2 - 834x^3 + 224x^4 - 25x^5 + x^6,
\end{aligned}$$

$$\begin{aligned}
& (31 - 12x + x^2) (-14 + 13x + 37x^2 - 13x^3 + x^4), \\
& 22 + 427x + 985x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -58 + 443x + 985x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -26 + 443x + 985x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& 6 + 443x + 985x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, (38 - 13x + x^2) (-1 - 8x + x^2) (-1 - 4x + x^2), \\
& -106 + 459x + 985x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& -74 + 459x + 985x^2 - 834x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-6 + 13x + 37x^2 - 13x^3 + x^4), \\
& (-9 + x) (262 - 137x - 110x^2 + 80x^3 - 16x^4 + x^5), \\
& -2110 + 1399x + 861x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -2238 + 1431x + 861x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-9 + x) (198 - 121x - 110x^2 + 80x^3 - 16x^4 + x^5), \\
& -1862 + 1303x + 869x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1830 + 1303x + 869x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (10 - 9x + x^2) (-191 - 40x + 70x^2 - 16x^3 + x^4), \\
& -1990 + 1335x + 869x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -2038 + 1351x + 869x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1534 + 1191x + 877x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1502 + 1191x + 877x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1614 + 1207x + 877x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1582 + 1207x + 877x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1662 + 1223x + 877x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1742 + 1239x + 877x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1710 + 1239x + 877x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1790 + 1255x + 877x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1838 + 1271x + 877x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1918 + 1287x + 877x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-66 + 17x + 37x^2 - 13x^3 + x^4), \\
& (-9 + x) (134 - 105x - 110x^2 + 80x^3 - 16x^4 + x^5), \\
& -1174 + 1079x + 885x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1286 + 1095x + 885x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1254 + 1095x + 885x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-1 + x) (1366 + 255x - 630x^2 + 200x^3 - 24x^4 + x^5), \\
& -1334 + 1111x + 885x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1302 + 1111x + 885x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1414 + 1127x + 885x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-1 + x) (1382 + 255x - 630x^2 + 200x^3 - 24x^4 + x^5), \\
& -1494 + 1143x + 885x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1462 + 1143x + 885x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1542 + 1159x + 885x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1510 + 1159x + 885x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1590 + 1175x + 885x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1670 + 1191x + 885x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1718 + 1207x + 885x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-58 + 17x + 37x^2 - 13x^3 + x^4), \\
& (-9 + x) (94 - 97x - 110x^2 + 80x^3 - 16x^4 + x^5),
\end{aligned}$$

$$\begin{aligned}
& -1038 + 999x + 893x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1006 + 999x + 893x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1118 + 1015x + 893x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1086 + 1015x + 893x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1054 + 1015x + 893x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1166 + 1031x + 893x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1134 + 1031x + 893x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1246 + 1047x + 893x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1214 + 1047x + 893x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1182 + 1047x + 893x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1294 + 1063x + 893x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1262 + 1063x + 893x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-1+x) (1342 + 263x - 630x^2 + 200x^3 - 24x^4 + x^5), \\
& -1310 + 1079x + 893x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1422 + 1095x + 893x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1390 + 1095x + 893x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1470 + 1111x + 893x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-50 + 17x + 37x^2 - 13x^3 + x^4), \\
& (-5+x) (142 - 149x - 210x^2 + 124x^3 - 20x^4 + x^5), \\
& -678 + 887x + 901x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -646 + 887x + 901x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -918 + 935x + 901x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -886 + 935x + 901x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -854 + 935x + 901x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1046 + 967x + 901x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -982 + 967x + 901x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1094 + 983x + 901x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1062 + 983x + 901x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1174 + 999x + 901x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1142 + 999x + 901x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1222 + 1015x + 901x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -1190 + 1015x + 901x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-1+x) (31 - 12x + x^2) (42 + 25x - 12x^2 + x^3), \\
& (-9+x) (-5+x) (-6 + 15x + 25x^2 - 11x^3 + x^4), \\
& (-5+x) (70 - 141x - 210x^2 + 124x^3 - 20x^4 + x^5), \\
& -318 + 775x + 909x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (86 - 141x - 210x^2 + 124x^3 - 20x^4 + x^5), \\
& -398 + 791x + 909x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (102 - 141x - 210x^2 + 124x^3 - 20x^4 + x^5), \\
& -478 + 807x + 909x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -446 + 807x + 909x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (118 - 141x - 210x^2 + 124x^3 - 20x^4 + x^5), \\
& -558 + 823x + 909x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -526 + 823x + 909x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (134 - 141x - 210x^2 + 124x^3 - 20x^4 + x^5), \\
& -638 + 839x + 909x^2 - 830x^3 + 224x^4 - 25x^5 + x^6,
\end{aligned}$$

$$\begin{aligned}
& -606 + 839x + 909x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -798 + 871x + 909x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -766 + 871x + 909x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -734 + 871x + 909x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -846 + 887x + 909x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -814 + 887x + 909x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -926 + 903x + 909x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -894 + 903x + 909x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -862 + 903x + 909x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-9 + x)(-5 + x)(-2 - 7x + x^2)(-1 - 4x + x^2), \\
& (-5 + x)(-2 - 133x - 210x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(14 - 133x - 210x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(30 - 133x - 210x^2 + 124x^3 - 20x^4 + x^5), \\
& -118 + 695x + 917x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(46 - 133x - 210x^2 + 124x^3 - 20x^4 + x^5), \\
& -198 + 711x + 917x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(62 - 133x - 210x^2 + 124x^3 - 20x^4 + x^5), \\
& -278 + 727x + 917x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(3 - 8x + x^2)(26 + 25x - 12x^2 + x^3), \\
& -358 + 743x + 917x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -326 + 743x + 917x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(94 - 133x - 210x^2 + 124x^3 - 20x^4 + x^5), \\
& -438 + 759x + 917x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -406 + 759x + 917x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(110 - 133x - 210x^2 + 124x^3 - 20x^4 + x^5), \\
& -518 + 775x + 917x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -486 + 775x + 917x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (2 - 5x + x^2)(-227 - 180x + 122x^2 - 20x^3 + x^4), \\
& -726 + 823x + 917x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -694 + 823x + 917x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(-10 - 125x - 210x^2 + 124x^3 - 20x^4 + x^5), \\
& (-1 - 4x + x^2)(-82 - 287x + 141x^2 - 21x^3 + x^4), \\
& (-5 + x)(6 - 125x - 210x^2 + 124x^3 - 20x^4 + x^5), \\
& 2 + 631x + 925x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(22 - 125x - 210x^2 + 124x^3 - 20x^4 + x^5), \\
& -78 + 647x + 925x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(2 - 9x + x^2)(19 + 23x - 11x^2 + x^3), \\
& -158 + 663x + 925x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -126 + 663x + 925x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(54 - 125x - 210x^2 + 124x^3 - 20x^4 + x^5), \\
& -238 + 679x + 925x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& -206 + 679x + 925x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(70 - 125x - 210x^2 + 124x^3 - 20x^4 + x^5), \\
& -318 + 695x + 925x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
& (-11 + 39x - 13x^2 + x^3)(26 + 29x - 12x^2 + x^3),
\end{aligned}$$

$$\begin{aligned}
& (-5+x) (86-125x-210x^2+124x^3-20x^4+x^5), \\
& -398+711x+925x^2-830x^3+224x^4-25x^5+x^6, \\
& -366+711x+925x^2-830x^3+224x^4-25x^5+x^6, \\
& -334+711x+925x^2-830x^3+224x^4-25x^5+x^6, \\
& (31-12x+x^2) (-18+17x+37x^2-13x^3+x^4), \\
& (-5+x) (-2-117x-210x^2+124x^3-20x^4+x^5), \\
& 42+583x+933x^2-830x^3+224x^4-25x^5+x^6, \\
& (-1-4x+x^2) (-74-287x+141x^2-21x^3+x^4), \\
& (-5+x) (14-117x-210x^2+124x^3-20x^4+x^5), \\
& -38+599x+933x^2-830x^3+224x^4-25x^5+x^6, \\
& -6+599x+933x^2-830x^3+224x^4-25x^5+x^6, \\
& (-5+x) (-5-8x+x^2) (-6+33x-12x^2+x^3), \\
& -118+615x+933x^2-830x^3+224x^4-25x^5+x^6, \\
& -86+615x+933x^2-830x^3+224x^4-25x^5+x^6, \\
& (-5+x) (46-117x-210x^2+124x^3-20x^4+x^5), \\
& -198+631x+933x^2-830x^3+224x^4-25x^5+x^6, \\
& (-5+x) (31-12x+x^2) (2-3x-8x^2+x^3), (-5+x) (-1-8x+x^2) (10+29x-12x^2+x^3), \\
& -2650+1747x+793x^2-826x^3+224x^4-25x^5+x^6, \\
& -2730+1763x+793x^2-826x^3+224x^4-25x^5+x^6, \\
& -2858+1795x+793x^2-826x^3+224x^4-25x^5+x^6, \\
& (-9+x) (-6-3x+x^2) (-43+47x-13x^2+x^3), \\
& -2402+1651x+801x^2-826x^3+224x^4-25x^5+x^6, \\
& -2482+1667x+801x^2-826x^3+224x^4-25x^5+x^6, \\
& -2530+1683x+801x^2-826x^3+224x^4-25x^5+x^6, \\
& -2610+1699x+801x^2-826x^3+224x^4-25x^5+x^6, \\
& -2658+1715x+801x^2-826x^3+224x^4-25x^5+x^6, \\
& (-9+x) (234-145x-106x^2+80x^3-16x^4+x^5), \\
& -2074+1539x+809x^2-826x^3+224x^4-25x^5+x^6, \\
& -2154+1555x+809x^2-826x^3+224x^4-25x^5+x^6, \\
& -2234+1571x+809x^2-826x^3+224x^4-25x^5+x^6, \\
& -2202+1571x+809x^2-826x^3+224x^4-25x^5+x^6, \\
& -2282+1587x+809x^2-826x^3+224x^4-25x^5+x^6, \\
& -2362+1603x+809x^2-826x^3+224x^4-25x^5+x^6, \\
& -2330+1603x+809x^2-826x^3+224x^4-25x^5+x^6, \\
& -2410+1619x+809x^2-826x^3+224x^4-25x^5+x^6, \\
& -2538+1651x+809x^2-826x^3+224x^4-25x^5+x^6, \\
& (31-12x+x^2) (-86+21x+37x^2-13x^3+x^4), \\
& (-9+x) (194-137x-106x^2+80x^3-16x^4+x^5), \\
& -1858+1443x+817x^2-826x^3+224x^4-25x^5+x^6, \\
& -1826+1443x+817x^2-826x^3+224x^4-25x^5+x^6, \\
& -1794+1443x+817x^2-826x^3+224x^4-25x^5+x^6, \\
& -1906+1459x+817x^2-826x^3+224x^4-25x^5+x^6, \\
& -1874+1459x+817x^2-826x^3+224x^4-25x^5+x^6, \\
& -1986+1475x+817x^2-826x^3+224x^4-25x^5+x^6, \\
& -1954+1475x+817x^2-826x^3+224x^4-25x^5+x^6, \\
& -2034+1491x+817x^2-826x^3+224x^4-25x^5+x^6,
\end{aligned}$$

$$\begin{aligned}
& -2002 + 1491x + 817x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -2114 + 1507x + 817x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -2082 + 1507x + 817x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-46 + 51x - 14x^2 + x^3)(47 + 19x - 11x^2 + x^3), \\
& -2210 + 1539x + 817x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -2290 + 1555x + 817x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -2338 + 1571x + 817x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2)(13 - 10x + x^2)(-6 - 3x + x^2), \\
& (-9 + x)(-5 + x)(-1 + x)(34 + 15x - 10x^2 + x^3), \\
& -1498 + 1331x + 825x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1466 + 1331x + 825x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(322 - 205x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& -1578 + 1347x + 825x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-1 + x)(1546 + 199x - 626x^2 + 200x^3 - 24x^4 + x^5), \\
& -1658 + 1363x + 825x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1626 + 1363x + 825x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1738 + 1379x + 825x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1706 + 1379x + 825x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1674 + 1379x + 825x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1786 + 1395x + 825x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1754 + 1395x + 825x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1866 + 1411x + 825x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1834 + 1411x + 825x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1802 + 1411x + 825x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1914 + 1427x + 825x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1882 + 1427x + 825x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1962 + 1443x + 825x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -2042 + 1459x + 825x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -2010 + 1459x + 825x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (38 - 13x + x^2)(-55 + 20x + 30x^2 - 12x^3 + x^4), \\
& (31 - 12x + x^2)(-70 + 21x + 37x^2 - 13x^3 + x^4), \\
& (-9 + x)(-5 + x)(-26 + 19x + 25x^2 - 11x^3 + x^4), \\
& -1138 + 1219x + 833x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(250 - 197x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& -1218 + 1235x + 833x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(266 - 197x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& -1298 + 1251x + 833x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1266 + 1251x + 833x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(282 - 197x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& -1378 + 1267x + 833x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1346 + 1267x + 833x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(-1 + x)(-298 - 101x + 105x^2 - 19x^3 + x^4), \\
& -1458 + 1283x + 833x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1426 + 1283x + 833x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1538 + 1299x + 833x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-1 + x)(1506 + 207x - 626x^2 + 200x^3 - 24x^4 + x^5),
\end{aligned}$$

$$\begin{aligned}
& -1474 + 1299x + 833x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1618 + 1315x + 833x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1586 + 1315x + 833x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1554 + 1315x + 833x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1666 + 1331x + 833x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1634 + 1331x + 833x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1714 + 1347x + 833x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1682 + 1347x + 833x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1794 + 1363x + 833x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1762 + 1363x + 833x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1842 + 1379x + 833x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1810 + 1379x + 833x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-62 + 21x + 37x^2 - 13x^3 + x^4), \\
& (-5 + x) (178 - 189x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (194 - 189x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& -938 + 1139x + 841x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (210 - 189x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& -1018 + 1155x + 841x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (226 - 189x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& -1098 + 1171x + 841x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (242 - 189x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& -1178 + 1187x + 841x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1146 + 1187x + 841x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (258 - 189x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& -1258 + 1203x + 841x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1226 + 1203x + 841x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (274 - 189x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& -1338 + 1219x + 841x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1306 + 1219x + 841x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1274 + 1219x + 841x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1418 + 1235x + 841x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1386 + 1235x + 841x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1354 + 1235x + 841x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-1 + x) (1466 + 215x - 626x^2 + 200x^3 - 24x^4 + x^5), \\
& -1434 + 1251x + 841x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1546 + 1267x + 841x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1514 + 1267x + 841x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-1 + x) (38 - 13x + x^2) (39 + 19x - 11x^2 + x^3), \\
& -1594 + 1283x + 841x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1562 + 1283x + 841x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-54 + 21x + 37x^2 - 13x^3 + x^4), \\
& (-5 + x) (122 - 181x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (154 - 181x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (186 - 181x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& -898 + 1091x + 849x^2 - 826x^3 + 224x^4 - 25x^5 + x^6,
\end{aligned}$$

$$\begin{aligned}
& (-5+x) (202 - 181x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& -978 + 1107x + 849x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -946 + 1107x + 849x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (218 - 181x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& -1058 + 1123x + 849x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1026 + 1123x + 849x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (234 - 181x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& -1138 + 1139x + 849x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1106 + 1139x + 849x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1218 + 1155x + 849x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1186 + 1155x + 849x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1154 + 1155x + 849x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1298 + 1171x + 849x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1266 + 1171x + 849x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1234 + 1171x + 849x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1346 + 1187x + 849x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1314 + 1187x + 849x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-1+x) (31 - 12x + x^2) (46 + 25x - 12x^2 + x^3), \\
& (-5+x) (82 - 173x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (98 - 173x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (146 - 173x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& -698 + 1011x + 857x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (162 - 173x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& -778 + 1027x + 857x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (210 - 173x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& -1018 + 1075x + 857x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -986 + 1075x + 857x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -954 + 1075x + 857x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1098 + 1091x + 857x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -1066 + 1091x + 857x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-38 + 21x + 37x^2 - 13x^3 + x^4), \\
& (-5+x) (58 - 165x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (74 - 165x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (106 - 165x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& -498 + 931x + 865x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (138 - 165x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& -658 + 963x + 865x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& -626 + 963x + 865x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (170 - 165x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& -818 + 995x + 865x^2 - 826x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (18 - 157x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (34 - 157x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (50 - 157x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (82 - 157x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& -378 + 867x + 873x^2 - 826x^3 + 224x^4 - 25x^5 + x^6,
\end{aligned}$$

$$\begin{aligned}
& (-5+x) (98-157x-206x^2+124x^3-20x^4+x^5), \\
& -458+883x+873x^2-826x^3+224x^4-25x^5+x^6, \\
& -426+883x+873x^2-826x^3+224x^4-25x^5+x^6, \\
& (-5+x) (-1-4x+x^2) (22+61x-16x^2+x^3), \\
& (-5+x) (-6-149x-206x^2+124x^3-20x^4+x^5), \\
& (-5+x) (-5-8x+x^2) (-2+33x-12x^2+x^3), \\
& (-5+x) (26-149x-206x^2+124x^3-20x^4+x^5), \\
& -98+771x+881x^2-826x^3+224x^4-25x^5+x^6, \\
& (-5+x) (-1-8x+x^2) (14+29x-12x^2+x^3), \\
& (-9+x) (358-193x-102x^2+80x^3-16x^4+x^5), \\
& -3350+2127x+725x^2-822x^3+224x^4-25x^5+x^6, \\
& -3478+2159x+725x^2-822x^3+224x^4-25x^5+x^6, \\
& -2974+1999x+733x^2-822x^3+224x^4-25x^5+x^6, \\
& -3022+2015x+733x^2-822x^3+224x^4-25x^5+x^6, \\
& -3102+2031x+733x^2-822x^3+224x^4-25x^5+x^6, \\
& -3150+2047x+733x^2-822x^3+224x^4-25x^5+x^6, \\
& -3230+2063x+733x^2-822x^3+224x^4-25x^5+x^6, \\
& (-9+x) (294-177x-102x^2+80x^3-16x^4+x^5), \\
& -2614+1887x+741x^2-822x^3+224x^4-25x^5+x^6, \\
& -2726+1903x+741x^2-822x^3+224x^4-25x^5+x^6, \\
& -2694+1903x+741x^2-822x^3+224x^4-25x^5+x^6, \\
& -2774+1919x+741x^2-822x^3+224x^4-25x^5+x^6, \\
& -2854+1935x+741x^2-822x^3+224x^4-25x^5+x^6, \\
& -2822+1935x+741x^2-822x^3+224x^4-25x^5+x^6, \\
& -2902+1951x+741x^2-822x^3+224x^4-25x^5+x^6, \\
& -2982+1967x+741x^2-822x^3+224x^4-25x^5+x^6, \\
& -3030+1983x+741x^2-822x^3+224x^4-25x^5+x^6, \\
& -3158+2015x+741x^2-822x^3+224x^4-25x^5+x^6, \\
& (-9+x) (254-169x-102x^2+80x^3-16x^4+x^5), \\
& (-9+x) (-5+x) (-54+23x+25x^2-11x^3+x^4), \\
& -2398+1791x+749x^2-822x^3+224x^4-25x^5+x^6, \\
& -2366+1791x+749x^2-822x^3+224x^4-25x^5+x^6, \\
& -2478+1807x+749x^2-822x^3+224x^4-25x^5+x^6, \\
& -2446+1807x+749x^2-822x^3+224x^4-25x^5+x^6, \\
& -2526+1823x+749x^2-822x^3+224x^4-25x^5+x^6, \\
& (-43+47x-13x^2+x^3) (58+21x-12x^2+x^3), \\
& -2606+1839x+749x^2-822x^3+224x^4-25x^5+x^6, \\
& -2574+1839x+749x^2-822x^3+224x^4-25x^5+x^6, \\
& -2654+1855x+749x^2-822x^3+224x^4-25x^5+x^6, \\
& -2622+1855x+749x^2-822x^3+224x^4-25x^5+x^6, \\
& -2734+1871x+749x^2-822x^3+224x^4-25x^5+x^6, \\
& -2702+1871x+749x^2-822x^3+224x^4-25x^5+x^6, \\
& -2782+1887x+749x^2-822x^3+224x^4-25x^5+x^6, \\
& -2830+1903x+749x^2-822x^3+224x^4-25x^5+x^6, \\
& -2910+1919x+749x^2-822x^3+224x^4-25x^5+x^6, \\
& (31-12x+x^2) (-98+25x+37x^2-13x^3+x^4),
\end{aligned}$$

$$\begin{aligned}
& (-9 + x) (-5 + x) (-46 + 23x + 25x^2 - 11x^3 + x^4), \\
& -2038 + 1679x + 757x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (430 - 253x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -2118 + 1695x + 757x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (446 - 253x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -2198 + 1711x + 757x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2166 + 1711x + 757x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2278 + 1727x + 757x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2246 + 1727x + 757x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2358 + 1743x + 757x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2326 + 1743x + 757x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2294 + 1743x + 757x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2406 + 1759x + 757x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2374 + 1759x + 757x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2486 + 1775x + 757x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2454 + 1775x + 757x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2534 + 1791x + 757x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2502 + 1791x + 757x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2582 + 1807x + 757x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2662 + 1823x + 757x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2630 + 1823x + 757x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2710 + 1839x + 757x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-90 + 25x + 37x^2 - 13x^3 + x^4), \\
& (-9 + x) (-5 + x) (-1 + x) (38 + 15x - 10x^2 + x^3), \\
& (-5 + x) (358 - 245x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -1758 + 1583x + 765x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (374 - 245x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -1838 + 1599x + 765x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (390 - 245x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -1918 + 1615x + 765x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (406 - 245x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -1998 + 1631x + 765x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -1966 + 1631x + 765x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (422 - 245x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -2078 + 1647x + 765x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2046 + 1647x + 765x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2158 + 1663x + 765x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2126 + 1663x + 765x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2238 + 1679x + 765x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2206 + 1679x + 765x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2174 + 1679x + 765x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2286 + 1695x + 765x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2254 + 1695x + 765x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2334 + 1711x + 765x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2302 + 1711x + 765x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2414 + 1727x + 765x^2 - 822x^3 + 224x^4 - 25x^5 + x^6,
\end{aligned}$$

$$\begin{aligned}
& -2382 + 1727x + 765x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2462 + 1743x + 765x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2)(-82 + 25x + 37x^2 - 13x^3 + x^4), \\
& (-5 + x)(286 - 237x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(302 - 237x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(318 - 237x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(-1 + x)(-334 - 97x + 105x^2 - 19x^3 + x^4), \\
& -1638 + 1519x + 773x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(350 - 237x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -1718 + 1535x + 773x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(366 - 237x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -1798 + 1551x + 773x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -1766 + 1551x + 773x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(382 - 237x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -1878 + 1567x + 773x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -1846 + 1567x + 773x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(398 - 237x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -1958 + 1583x + 773x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -1926 + 1583x + 773x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2038 + 1599x + 773x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2006 + 1599x + 773x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-42 + 51x - 14x^2 + x^3)(47 + 19x - 11x^2 + x^3), \\
& -2086 + 1615x + 773x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2054 + 1615x + 773x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2166 + 1631x + 773x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2134 + 1631x + 773x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2214 + 1647x + 773x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -2182 + 1647x + 773x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2)(-74 + 25x + 37x^2 - 13x^3 + x^4), \\
& (-5 + x)(246 - 229x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(262 - 229x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(278 - 229x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(294 - 229x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -1438 + 1439x + 781x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(310 - 229x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -1518 + 1455x + 781x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(-1 + x)(-326 - 97x + 105x^2 - 19x^3 + x^4), \\
& -1598 + 1471x + 781x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(342 - 229x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -1678 + 1487x + 781x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-1 + x)(1646 + 159x - 622x^2 + 200x^3 - 24x^4 + x^5), \\
& (-5 + x)(358 - 229x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -1758 + 1503x + 781x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -1726 + 1503x + 781x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -1838 + 1519x + 781x^2 - 822x^3 + 224x^4 - 25x^5 + x^6,
\end{aligned}$$

$$\begin{aligned}
& -1806 + 1519x + 781x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -1774 + 1519x + 781x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -1918 + 1535x + 781x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -1886 + 1535x + 781x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -1854 + 1535x + 781x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -1966 + 1551x + 781x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -1934 + 1551x + 781x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-66 + 25x + 37x^2 - 13x^3 + x^4), \\
& (-5 + x) (222 - 221x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (238 - 221x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (254 - 221x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -1238 + 1359x + 789x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (270 - 221x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -1318 + 1375x + 789x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (286 - 221x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -1398 + 1391x + 789x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (302 - 221x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -1478 + 1407x + 789x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -1446 + 1407x + 789x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (-1 + x) (-318 - 97x + 105x^2 - 19x^3 + x^4), \\
& -1558 + 1423x + 789x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -1526 + 1423x + 789x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (334 - 221x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -1638 + 1439x + 789x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-1 + x) (1606 + 167x - 622x^2 + 200x^3 - 24x^4 + x^5), \\
& -1718 + 1455x + 789x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -1686 + 1455x + 789x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-58 + 25x + 37x^2 - 13x^3 + x^4), \\
& (-5 + x) (182 - 213x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (198 - 213x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (214 - 213x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (230 - 213x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -1118 + 1295x + 797x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (246 - 213x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -1198 + 1311x + 797x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (262 - 213x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -1278 + 1327x + 797x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -1246 + 1327x + 797x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (278 - 213x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -1358 + 1343x + 797x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-34 + 51x - 14x^2 + x^3) (39 + 19x - 11x^2 + x^3), \\
& (-5 + x) (294 - 213x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -1438 + 1359x + 797x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (-1 + x) (31 - 12x + x^2) (-10 - 7x + x^2), \\
& (-5 + x) (158 - 205x - 202x^2 + 124x^3 - 20x^4 + x^5),
\end{aligned}$$

$$\begin{aligned}
& (-5+x) (174 - 205x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (190 - 205x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -918 + 1215x + 805x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (206 - 205x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -998 + 1231x + 805x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (222 - 205x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -1078 + 1247x + 805x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (238 - 205x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (118 - 197x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (134 - 197x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (166 - 197x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -798 + 1151x + 813x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (78 - 189x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (110 - 189x - 202x^2 + 124x^3 - 20x^4 + x^5), \\
& -3842 + 2459x + 657x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3970 + 2491x + 657x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-9+x) (394 - 217x - 98x^2 + 80x^3 - 16x^4 + x^5), \\
& -3514 + 2347x + 665x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3594 + 2363x + 665x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3642 + 2379x + 665x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3722 + 2395x + 665x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3850 + 2427x + 665x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-9+x) (354 - 209x - 98x^2 + 80x^3 - 16x^4 + x^5), \\
& -3298 + 2251x + 673x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3266 + 2251x + 673x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3346 + 2267x + 673x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3314 + 2267x + 673x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3394 + 2283x + 673x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3474 + 2299x + 673x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3442 + 2299x + 673x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3522 + 2315x + 673x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3602 + 2331x + 673x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-73 + 63x - 15x^2 + x^3) (50 + 11x - 10x^2 + x^3), \\
& (-9+x) (-5+x) (-66 + 27x + 25x^2 - 11x^3 + x^4), \\
& -2938 + 2139x + 681x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (610 - 309x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -3018 + 2155x + 681x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2986 + 2155x + 681x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3098 + 2171x + 681x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3066 + 2171x + 681x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3146 + 2187x + 681x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3114 + 2187x + 681x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3226 + 2203x + 681x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3194 + 2203x + 681x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3274 + 2219x + 681x^2 - 818x^3 + 224x^4 - 25x^5 + x^6,
\end{aligned}$$

$$\begin{aligned}
& -3354 + 2235x + 681x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3322 + 2235x + 681x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3402 + 2251x + 681x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3450 + 2267x + 681x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3530 + 2283x + 681x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-2 + x)(31 - 12x + x^2)(59 + 15x - 11x^2 + x^3), \\
& (-9 + x)(-5 + x)(-58 + 27x + 25x^2 - 11x^3 + x^4), \\
& -2578 + 2027x + 689x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(538 - 301x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -2658 + 2043x + 689x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(554 - 301x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -2738 + 2059x + 689x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(570 - 301x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -2818 + 2075x + 689x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2786 + 2075x + 689x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2898 + 2091x + 689x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2866 + 2091x + 689x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2978 + 2107x + 689x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2946 + 2107x + 689x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3026 + 2123x + 689x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2994 + 2123x + 689x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3106 + 2139x + 689x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3074 + 2139x + 689x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3154 + 2155x + 689x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3122 + 2155x + 689x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3202 + 2171x + 689x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3282 + 2187x + 689x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3330 + 2203x + 689x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2)(-110 + 29x + 37x^2 - 13x^3 + x^4), \\
& (-9 + x)(-5 + x)(-50 + 27x + 25x^2 - 11x^3 + x^4), \\
& (-5 + x)(466 - 293x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(482 - 293x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(498 - 293x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -2458 + 1963x + 697x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(514 - 293x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -2538 + 1979x + 697x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(530 - 293x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -2618 + 1995x + 697x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2586 + 1995x + 697x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(546 - 293x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -2698 + 2011x + 697x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-43 + 47x - 13x^2 + x^3)(62 + 21x - 12x^2 + x^3), \\
& -2778 + 2027x + 697x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2746 + 2027x + 697x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2858 + 2043x + 697x^2 - 818x^3 + 224x^4 - 25x^5 + x^6,
\end{aligned}$$

$$\begin{aligned}
& -2826 + 2043x + 697x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2794 + 2043x + 697x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2906 + 2059x + 697x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2874 + 2059x + 697x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2954 + 2075x + 697x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3034 + 2091x + 697x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (38 - 13x + x^2)(-79 + 28x + 30x^2 - 12x^3 + x^4), \\
& -3082 + 2107x + 697x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2)(-102 + 29x + 37x^2 - 13x^3 + x^4), \\
& (-5 + x)(426 - 285x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(442 - 285x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(458 - 285x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -2258 + 1883x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(474 - 285x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -2338 + 1899x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(490 - 285x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -2418 + 1915x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(-11 - 6x + x^2)(-46 + 51x - 14x^2 + x^3), \\
& -2498 + 1931x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2466 + 1931x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(522 - 285x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -2578 + 1947x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2546 + 1947x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2658 + 1963x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2626 + 1963x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2594 + 1963x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2706 + 1979x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2674 + 1979x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2786 + 1995x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-54 + 55x - 14x^2 + x^3)(51 + 15x - 11x^2 + x^3), \\
& (13 - 10x + x^2)(-218 - 13x + 61x^2 - 15x^3 + x^4), \\
& -2802 + 2011x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2)(-94 + 29x + 37x^2 - 13x^3 + x^4), \\
& (-5 + x)(386 - 277x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(402 - 277x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(418 - 277x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(434 - 277x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -2138 + 1819x + 713x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(450 - 277x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -2218 + 1835x + 713x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(466 - 277x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -2298 + 1851x + 713x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2266 + 1851x + 713x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(482 - 277x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -2378 + 1867x + 713x^2 - 818x^3 + 224x^4 - 25x^5 + x^6,
\end{aligned}$$

$$\begin{aligned}
& -2346 + 1867x + 713x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2458 + 1883x + 713x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2426 + 1883x + 713x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2538 + 1899x + 713x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2506 + 1899x + 713x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2474 + 1899x + 713x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2586 + 1915x + 713x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2554 + 1915x + 713x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2)(-86 + 29x + 37x^2 - 13x^3 + x^4), \\
& (-5 + x)(346 - 269x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(-1 + x)(-362 - 93x + 105x^2 - 19x^3 + x^4), \\
& (-5 + x)(378 - 269x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(394 - 269x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -1938 + 1739x + 721x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(410 - 269x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -2018 + 1755x + 721x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(426 - 269x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -2098 + 1771x + 721x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(442 - 269x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -2178 + 1787x + 721x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2146 + 1787x + 721x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(458 - 269x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -2258 + 1803x + 721x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2226 + 1803x + 721x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2338 + 1819x + 721x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2306 + 1819x + 721x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2)(-78 + 29x + 37x^2 - 13x^3 + x^4), \\
& (-5 + x)(322 - 261x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(338 - 261x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(-1 + x)(-354 - 93x + 105x^2 - 19x^3 + x^4), \\
& -1738 + 1659x + 729x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(370 - 261x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -1818 + 1675x + 729x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(386 - 261x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -1898 + 1691x + 729x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(402 - 261x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -1978 + 1707x + 729x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -1946 + 1707x + 729x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(418 - 261x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -2058 + 1723x + 729x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(31 - 12x + x^2)(14 - 3x - 8x^2 + x^3), \\
& (-5 + x)(282 - 253x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(298 - 253x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(314 - 253x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(330 - 253x - 198x^2 + 124x^3 - 20x^4 + x^5),
\end{aligned}$$

$$\begin{aligned}
& -1618 + 1595x + 737x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x)(-1+x)(-346 - 93x + 105x^2 - 19x^3 + x^4), \\
& -1698 + 1611x + 737x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x)(362 - 253x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)(242 - 245x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)(258 - 245x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)(274 - 245x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)(290 - 245x - 198x^2 + 124x^3 - 20x^4 + x^5), \\
& -1418 + 1515x + 745x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x)(6 - 9x + x^2)(39 + 19x - 11x^2 + x^3), \\
& (-9+x)(-7 - 2x + x^2)(-74 + 59x - 14x^2 + x^3), \\
& -4414 + 2807x + 589x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -4462 + 2823x + 589x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-9+x)(454 - 249x - 94x^2 + 80x^3 - 16x^4 + x^5), \\
& -4166 + 2711x + 597x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -4134 + 2711x + 597x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -4214 + 2727x + 597x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -4342 + 2759x + 597x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -4470 + 2791x + 597x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3838 + 2599x + 605x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3806 + 2599x + 605x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3918 + 2615x + 605x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3886 + 2615x + 605x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3966 + 2631x + 605x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3934 + 2631x + 605x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -4014 + 2647x + 605x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -4094 + 2663x + 605x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -4142 + 2679x + 605x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -4222 + 2695x + 605x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-9+x)(-5+x)(-78 + 31x + 25x^2 - 11x^3 + x^4), \\
& -3478 + 2487x + 613x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x)(718 - 357x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -3558 + 2503x + 613x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x)(734 - 357x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -3638 + 2519x + 613x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3606 + 2519x + 613x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3718 + 2535x + 613x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3686 + 2535x + 613x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3766 + 2551x + 613x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3846 + 2567x + 613x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3814 + 2567x + 613x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3894 + 2583x + 613x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3974 + 2599x + 613x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-73 + 63x - 15x^2 + x^3)(54 + 11x - 10x^2 + x^3), \\
& -4022 + 2615x + 613x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -4150 + 2647x + 613x^2 - 814x^3 + 224x^4 - 25x^5 + x^6,
\end{aligned}$$

$$\begin{aligned}
& (-9 + x) (-7 + x) (-5 + x) (10 - 3x - 4x^2 + x^3), \\
& (-5 + x) (646 - 349x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (662 - 349x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -3278 + 2407x + 621x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (678 - 349x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -3358 + 2423x + 621x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (694 - 349x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -3438 + 2439x + 621x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3406 + 2439x + 621x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3518 + 2455x + 621x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3486 + 2455x + 621x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3598 + 2471x + 621x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3566 + 2471x + 621x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3646 + 2487x + 621x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3614 + 2487x + 621x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3726 + 2503x + 621x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3694 + 2503x + 621x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3774 + 2519x + 621x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3822 + 2535x + 621x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3902 + 2551x + 621x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3950 + 2567x + 621x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-130 + 33x + 37x^2 - 13x^3 + x^4), \\
& (-5 + x) (590 - 341x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (606 - 341x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (622 - 341x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -3078 + 2327x + 629x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (638 - 341x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -3158 + 2343x + 629x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (654 - 341x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -3238 + 2359x + 629x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (670 - 341x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -3318 + 2375x + 629x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3286 + 2375x + 629x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3398 + 2391x + 629x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3366 + 2391x + 629x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3478 + 2407x + 629x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3446 + 2407x + 629x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3414 + 2407x + 629x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3526 + 2423x + 629x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3494 + 2423x + 629x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3574 + 2439x + 629x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3654 + 2455x + 629x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3622 + 2455x + 629x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3702 + 2471x + 629x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-122 + 33x + 37x^2 - 13x^3 + x^4),
\end{aligned}$$

$$\begin{aligned}
& (-5+x) (550 - 333x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (566 - 333x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (582 - 333x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (598 - 333x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -2958 + 2263x + 637x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (614 - 333x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -3038 + 2279x + 637x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (630 - 333x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -3118 + 2295x + 637x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3086 + 2295x + 637x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (646 - 333x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -3198 + 2311x + 637x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3166 + 2311x + 637x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3278 + 2327x + 637x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3246 + 2327x + 637x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3326 + 2343x + 637x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3294 + 2343x + 637x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3406 + 2359x + 637x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3374 + 2359x + 637x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3454 + 2375x + 637x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-58 + 55x - 14x^2 + x^3) (59 + 15x - 11x^2 + x^3), \\
& (31 - 12x + x^2) (-114 + 33x + 37x^2 - 13x^3 + x^4), \\
& (-5+x) (510 - 325x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (526 - 325x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (542 - 325x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (558 - 325x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -2758 + 2183x + 645x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (574 - 325x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-43 + 47x - 13x^2 + x^3) (66 + 21x - 12x^2 + x^3), \\
& (-5+x) (590 - 325x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -2918 + 2215x + 645x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (606 - 325x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -2998 + 2231x + 645x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -2966 + 2231x + 645x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3078 + 2247x + 645x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3046 + 2247x + 645x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3158 + 2263x + 645x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3126 + 2263x + 645x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (13 - 10x + x^2) (-238 - 9x + 61x^2 - 15x^3 + x^4), \\
& -3206 + 2279x + 645x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3174 + 2279x + 645x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-106 + 33x + 37x^2 - 13x^3 + x^4), \\
& (-5+x) (486 - 317x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (502 - 317x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (518 - 317x - 194x^2 + 124x^3 - 20x^4 + x^5),
\end{aligned}$$

$$\begin{aligned}
& -2558 + 2103x + 653x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(534 - 317x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -2638 + 2119x + 653x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(550 - 317x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -2718 + 2135x + 653x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(566 - 317x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -2798 + 2151x + 653x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -2766 + 2151x + 653x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(582 - 317x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -2878 + 2167x + 653x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -2846 + 2167x + 653x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -2958 + 2183x + 653x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -2926 + 2183x + 653x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2)(-98 + 33x + 37x^2 - 13x^3 + x^4), \\
& (-5 + x)(446 - 309x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(-11 - 6x + x^2)(-42 + 51x - 14x^2 + x^3), \\
& (-5 + x)(478 - 309x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(494 - 309x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -2438 + 2039x + 661x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(10 - 9x + x^2)(51 + 15x - 11x^2 + x^3), \\
& -2518 + 2055x + 661x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(526 - 309x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -2598 + 2071x + 661x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -2566 + 2071x + 661x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(542 - 309x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -2678 + 2087x + 661x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(31 - 12x + x^2)(18 - 3x - 8x^2 + x^3), \\
& (-5 + x)(422 - 301x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(438 - 301x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(454 - 301x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -2238 + 1959x + 669x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(470 - 301x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -2318 + 1975x + 669x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(486 - 301x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(-1 + x)(-382 - 89x + 105x^2 - 19x^3 + x^4), \\
& (-5 + x)(398 - 293x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(414 - 293x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(342 - 285x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(358 - 285x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -5282 + 3267x + 513x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4954 + 3155x + 521x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -5034 + 3171x + 521x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& (-9 + x)(514 - 281x - 90x^2 + 80x^3 - 16x^4 + x^5), \\
& -4706 + 3059x + 529x^2 - 810x^3 + 224x^4 - 25x^5 + x^6,
\end{aligned}$$

$$\begin{aligned}
& -4786 + 3075x + 529x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4754 + 3075x + 529x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4834 + 3091x + 529x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4962 + 3123x + 529x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& (-9 + x)(-7 + x)(-5 + x)(-2 + x)(-7 - 2x + x^2), \\
& -4378 + 2947x + 537x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4458 + 2963x + 537x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4426 + 2963x + 537x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4538 + 2979x + 537x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4506 + 2979x + 537x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4586 + 2995x + 537x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4634 + 3011x + 537x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4714 + 3027x + 537x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4762 + 3043x + 537x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4842 + 3059x + 537x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& (-9 + x)(-5 + x)(-90 + 35x + 25x^2 - 11x^3 + x^4), \\
& (-7 + x)(-5 + x)(-118 + 41x + 33x^2 - 13x^3 + x^4), \\
& -4098 + 2851x + 545x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(842 - 405x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& -4178 + 2867x + 545x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(858 - 405x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& -4258 + 2883x + 545x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4338 + 2899x + 545x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4306 + 2899x + 545x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4386 + 2915x + 545x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& (-7 - 2x + x^2)(638 - 601x + 185x^2 - 23x^3 + x^4), \\
& -4434 + 2931x + 545x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4514 + 2947x + 545x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4594 + 2963x + 545x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4642 + 2979x + 545x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4770 + 3011x + 545x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(754 - 397x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& (-7 + x)(-5 + x)(-110 + 41x + 33x^2 - 13x^3 + x^4), \\
& (-5 + x)(786 - 397x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& -3898 + 2771x + 553x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(802 - 397x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& -3978 + 2787x + 553x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(818 - 397x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& -4058 + 2803x + 553x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4138 + 2819x + 553x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4106 + 2819x + 553x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4218 + 2835x + 553x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4186 + 2835x + 553x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4266 + 2851x + 553x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4346 + 2867x + 553x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& (-2 + x)(2157 - 355x - 454x^2 + 178x^3 - 23x^4 + x^5),
\end{aligned}$$

$$\begin{aligned}
& -4394 + 2883x + 553x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4442 + 2899x + 553x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& (38 - 13x + x^2)(17 - 10x + x^2)(-7 - 2x + x^2), \\
& (31 - 12x + x^2)(-150 + 37x + 37x^2 - 13x^3 + x^4), \\
& (-7 + x)(-5 + x)(-102 + 41x + 33x^2 - 13x^3 + x^4), \\
& (-5 + x)(730 - 389x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(746 - 389x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(762 - 389x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& -3778 + 2707x + 561x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(778 - 389x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& -3858 + 2723x + 561x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(794 - 389x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& -3938 + 2739x + 561x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -3906 + 2739x + 561x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4018 + 2755x + 561x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -3986 + 2755x + 561x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4098 + 2771x + 561x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4066 + 2771x + 561x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4146 + 2787x + 561x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4114 + 2787x + 561x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4194 + 2803x + 561x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4274 + 2819x + 561x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4322 + 2835x + 561x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2)(-142 + 37x + 37x^2 - 13x^3 + x^4), \\
& (-5 + x)(674 - 381x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(690 - 381x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(706 - 381x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(722 - 381x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& -3578 + 2627x + 569x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(738 - 381x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& -3658 + 2643x + 569x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(754 - 381x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& -3738 + 2659x + 569x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(770 - 381x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& -3818 + 2675x + 569x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -3786 + 2675x + 569x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -3898 + 2691x + 569x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -3866 + 2691x + 569x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -3946 + 2707x + 569x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& (38 - 13x + x^2)(-103 + 36x + 30x^2 - 12x^3 + x^4), \\
& -4026 + 2723x + 569x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -3994 + 2723x + 569x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4074 + 2739x + 569x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& (-2 + x)(31 - 12x + x^2)(67 + 15x - 11x^2 + x^3), \\
& (-5 + x)(650 - 373x - 190x^2 + 124x^3 - 20x^4 + x^5),
\end{aligned}$$

$$\begin{aligned}
& (-5+x) (666-373x-190x^2+124x^3-20x^4+x^5), \\
& (-5+x) (682-373x-190x^2+124x^3-20x^4+x^5), \\
& -3378+2547x+577x^2-810x^3+224x^4-25x^5+x^6, \\
& (-5+x) (698-373x-190x^2+124x^3-20x^4+x^5), \\
& -3458+2563x+577x^2-810x^3+224x^4-25x^5+x^6, \\
& (-5+x) (714-373x-190x^2+124x^3-20x^4+x^5), \\
& -3538+2579x+577x^2-810x^3+224x^4-25x^5+x^6, \\
& (-5+x) (730-373x-190x^2+124x^3-20x^4+x^5), \\
& -3618+2595x+577x^2-810x^3+224x^4-25x^5+x^6, \\
& -3586+2595x+577x^2-810x^3+224x^4-25x^5+x^6, \\
& -3698+2611x+577x^2-810x^3+224x^4-25x^5+x^6, \\
& -3666+2611x+577x^2-810x^3+224x^4-25x^5+x^6, \\
& -3778+2627x+577x^2-810x^3+224x^4-25x^5+x^6, \\
& -3746+2627x+577x^2-810x^3+224x^4-25x^5+x^6, \\
& -3826+2643x+577x^2-810x^3+224x^4-25x^5+x^6, \\
& -3794+2643x+577x^2-810x^3+224x^4-25x^5+x^6, \\
& (31-12x+x^2) (-126+37x+37x^2-13x^3+x^4), \\
& (-5+x) (610-365x-190x^2+124x^3-20x^4+x^5), \\
& (-5+x) (626-365x-190x^2+124x^3-20x^4+x^5), \\
& (-5+x) (642-365x-190x^2+124x^3-20x^4+x^5), \\
& (-5+x) (658-365x-190x^2+124x^3-20x^4+x^5), \\
& -3258+2483x+585x^2-810x^3+224x^4-25x^5+x^6, \\
& (-5+x) (674-365x-190x^2+124x^3-20x^4+x^5), \\
& -3338+2499x+585x^2-810x^3+224x^4-25x^5+x^6, \\
& (-5+x) (690-365x-190x^2+124x^3-20x^4+x^5), \\
& -3418+2515x+585x^2-810x^3+224x^4-25x^5+x^6, \\
& -3386+2515x+585x^2-810x^3+224x^4-25x^5+x^6, \\
& (-5+x) (706-365x-190x^2+124x^3-20x^4+x^5), \\
& -3498+2531x+585x^2-810x^3+224x^4-25x^5+x^6, \\
& -3466+2531x+585x^2-810x^3+224x^4-25x^5+x^6, \\
& -3578+2547x+585x^2-810x^3+224x^4-25x^5+x^6, \\
& -3546+2547x+585x^2-810x^3+224x^4-25x^5+x^6, \\
& (31-12x+x^2) (-118+37x+37x^2-13x^3+x^4), \\
& (-5+x) (586-357x-190x^2+124x^3-20x^4+x^5), \\
& (-5+x) (-14-7x+x^2) (-43+47x-13x^2+x^3), \\
& (-5+x) (618-357x-190x^2+124x^3-20x^4+x^5), \\
& -3058+2403x+593x^2-810x^3+224x^4-25x^5+x^6, \\
& (-5+x) (634-357x-190x^2+124x^3-20x^4+x^5), \\
& -3138+2419x+593x^2-810x^3+224x^4-25x^5+x^6, \\
& (-5+x) (13-10x+x^2) (50+11x-10x^2+x^3), \\
& -3218+2435x+593x^2-810x^3+224x^4-25x^5+x^6, \\
& (-5+x) (666-357x-190x^2+124x^3-20x^4+x^5), \\
& -3298+2451x+593x^2-810x^3+224x^4-25x^5+x^6, \\
& (-5+x) (31-12x+x^2) (22-3x-8x^2+x^3), \\
& (-5+x) (546-349x-190x^2+124x^3-20x^4+x^5),
\end{aligned}$$

$$\begin{aligned}
& (-5+x) (562-349x-190x^2+124x^3-20x^4+x^5), \\
& (-5+x) (578-349x-190x^2+124x^3-20x^4+x^5), \\
& (-5+x) (594-349x-190x^2+124x^3-20x^4+x^5), \\
& -2938+2339x+601x^2-810x^3+224x^4-25x^5+x^6, \\
& (-5+x) (610-349x-190x^2+124x^3-20x^4+x^5), \\
& (-5+x) (506-341x-190x^2+124x^3-20x^4+x^5), \\
& (-5+x) (522-341x-190x^2+124x^3-20x^4+x^5), \\
& (-5+x) (538-341x-190x^2+124x^3-20x^4+x^5), \\
& (-5+x) (482-333x-190x^2+124x^3-20x^4+x^5), \\
& (-9+x) (614-321x-86x^2+80x^3-16x^4+x^5), \\
& -5654+3535x+453x^2-806x^3+224x^4-25x^5+x^6, \\
& (-7+x) (754-379x-120x^2+98x^3-18x^4+x^5), \\
& -5246+3407x+461x^2-806x^3+224x^4-25x^5+x^6, \\
& -5326+3423x+461x^2-806x^3+224x^4-25x^5+x^6, \\
& -5406+3439x+461x^2-806x^3+224x^4-25x^5+x^6, \\
& -5454+3455x+461x^2-806x^3+224x^4-25x^5+x^6, \\
& (-9+x) (-5+x) (-110+39x+25x^2-11x^3+x^4), \\
& -4918+3295x+469x^2-806x^3+224x^4-25x^5+x^6, \\
& (-5+x) (1006-461x-186x^2+124x^3-20x^4+x^5), \\
& (-7+x) (714-371x-120x^2+98x^3-18x^4+x^5), \\
& -5078+3327x+469x^2-806x^3+224x^4-25x^5+x^6, \\
& -5158+3343x+469x^2-806x^3+224x^4-25x^5+x^6, \\
& -5126+3343x+469x^2-806x^3+224x^4-25x^5+x^6, \\
& -5206+3359x+469x^2-806x^3+224x^4-25x^5+x^6, \\
& (-74+59x-14x^2+x^3) (71+11x-11x^2+x^3), \\
& -5334+3391x+469x^2-806x^3+224x^4-25x^5+x^6, \\
& -5462+3423x+469x^2-806x^3+224x^4-25x^5+x^6, \\
& (-9+x) (-5+x) (-102+39x+25x^2-11x^3+x^4), \\
& (-5+x) (934-453x-186x^2+124x^3-20x^4+x^5), \\
& (-5+x) (950-453x-186x^2+124x^3-20x^4+x^5), \\
& (-7+x) (674-363x-120x^2+98x^3-18x^4+x^5), \\
& (-7+x) (-5+x) (-138+45x+33x^2-13x^3+x^4), \\
& -4798+3231x+477x^2-806x^3+224x^4-25x^5+x^6, \\
& (-5+x) (982-453x-186x^2+124x^3-20x^4+x^5), \\
& -4878+3247x+477x^2-806x^3+224x^4-25x^5+x^6, \\
& -4958+3263x+477x^2-806x^3+224x^4-25x^5+x^6, \\
& -4926+3263x+477x^2-806x^3+224x^4-25x^5+x^6, \\
& -5006+3279x+477x^2-806x^3+224x^4-25x^5+x^6, \\
& -5086+3295x+477x^2-806x^3+224x^4-25x^5+x^6, \\
& -5134+3311x+477x^2-806x^3+224x^4-25x^5+x^6, \\
& -5214+3327x+477x^2-806x^3+224x^4-25x^5+x^6, \\
& -5262+3343x+477x^2-806x^3+224x^4-25x^5+x^6, \\
& (-5+x) (878-445x-186x^2+124x^3-20x^4+x^5), \\
& (-5+x) (894-445x-186x^2+124x^3-20x^4+x^5),
\end{aligned}$$

$$\begin{aligned}
& (-7+x)(-5+x)(-130+45x+33x^2-13x^3+x^4), \\
& (-5+x)(926-445x-186x^2+124x^3-20x^4+x^5), \\
& -4598+3151x+485x^2-806x^3+224x^4-25x^5+x^6, \\
& (-5+x)(942-445x-186x^2+124x^3-20x^4+x^5), \\
& -4678+3167x+485x^2-806x^3+224x^4-25x^5+x^6, \\
& -4758+3183x+485x^2-806x^3+224x^4-25x^5+x^6, \\
& -4726+3183x+485x^2-806x^3+224x^4-25x^5+x^6, \\
& -4838+3199x+485x^2-806x^3+224x^4-25x^5+x^6, \\
& -4806+3199x+485x^2-806x^3+224x^4-25x^5+x^6, \\
& -4886+3215x+485x^2-806x^3+224x^4-25x^5+x^6, \\
& -4966+3231x+485x^2-806x^3+224x^4-25x^5+x^6, \\
& -4934+3231x+485x^2-806x^3+224x^4-25x^5+x^6, \\
& -5014+3247x+485x^2-806x^3+224x^4-25x^5+x^6, \\
& -5142+3279x+485x^2-806x^3+224x^4-25x^5+x^6, \\
& (31-12x+x^2)(-170+41x+37x^2-13x^3+x^4), \\
& (-7+x)(-5+x)(-122+45x+33x^2-13x^3+x^4), \\
& (-5+x)(870-437x-186x^2+124x^3-20x^4+x^5), \\
& (-5+x)(886-437x-186x^2+124x^3-20x^4+x^5), \\
& -4398+3071x+493x^2-806x^3+224x^4-25x^5+x^6, \\
& (-5+x)(902-437x-186x^2+124x^3-20x^4+x^5), \\
& -4478+3087x+493x^2-806x^3+224x^4-25x^5+x^6, \\
& (-5+x)(918-437x-186x^2+124x^3-20x^4+x^5), \\
& -4558+3103x+493x^2-806x^3+224x^4-25x^5+x^6, \\
& -4638+3119x+493x^2-806x^3+224x^4-25x^5+x^6, \\
& -4606+3119x+493x^2-806x^3+224x^4-25x^5+x^6, \\
& -4718+3135x+493x^2-806x^3+224x^4-25x^5+x^6, \\
& -4686+3135x+493x^2-806x^3+224x^4-25x^5+x^6, \\
& -4766+3151x+493x^2-806x^3+224x^4-25x^5+x^6, \\
& -4734+3151x+493x^2-806x^3+224x^4-25x^5+x^6, \\
& -4814+3167x+493x^2-806x^3+224x^4-25x^5+x^6, \\
& -4894+3183x+493x^2-806x^3+224x^4-25x^5+x^6, \\
& -4942+3199x+493x^2-806x^3+224x^4-25x^5+x^6, \\
& (31-12x+x^2)(-162+41x+37x^2-13x^3+x^4), \\
& (-5+x)(814-429x-186x^2+124x^3-20x^4+x^5), \\
& (-5+x)(830-429x-186x^2+124x^3-20x^4+x^5), \\
& (-5+x)(846-429x-186x^2+124x^3-20x^4+x^5), \\
& (-5+x)(862-429x-186x^2+124x^3-20x^4+x^5), \\
& -4278+3007x+501x^2-806x^3+224x^4-25x^5+x^6, \\
& (-5+x)(878-429x-186x^2+124x^3-20x^4+x^5), \\
& -4358+3023x+501x^2-806x^3+224x^4-25x^5+x^6, \\
& (-5+x)(894-429x-186x^2+124x^3-20x^4+x^5), \\
& -4438+3039x+501x^2-806x^3+224x^4-25x^5+x^6, \\
& -4406+3039x+501x^2-806x^3+224x^4-25x^5+x^6, \\
& -4518+3055x+501x^2-806x^3+224x^4-25x^5+x^6, \\
& -4486+3055x+501x^2-806x^3+224x^4-25x^5+x^6,
\end{aligned}$$

$$\begin{aligned}
& -4566 + 3071x + 501x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& -4646 + 3087x + 501x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& -4614 + 3087x + 501x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& -4694 + 3103x + 501x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-154 + 41x + 37x^2 - 13x^3 + x^4), \\
& (-5 + x) (774 - 421x - 186x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (790 - 421x - 186x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (806 - 421x - 186x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (822 - 421x - 186x^2 + 124x^3 - 20x^4 + x^5), \\
& -4078 + 2927x + 509x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (838 - 421x - 186x^2 + 124x^3 - 20x^4 + x^5), \\
& -4158 + 2943x + 509x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (-7 - 2x + x^2) (-122 + 95x - 18x^2 + x^3), \\
& -4238 + 2959x + 509x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& -4318 + 2975x + 509x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& -4286 + 2975x + 509x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& -4398 + 2991x + 509x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& -4366 + 2991x + 509x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& -4446 + 3007x + 509x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& -4414 + 3007x + 509x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-146 + 41x + 37x^2 - 13x^3 + x^4), \\
& (-5 + x) (750 - 413x - 186x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (766 - 413x - 186x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (782 - 413x - 186x^2 + 124x^3 - 20x^4 + x^5), \\
& -3878 + 2847x + 517x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (798 - 413x - 186x^2 + 124x^3 - 20x^4 + x^5), \\
& -3958 + 2863x + 517x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (814 - 413x - 186x^2 + 124x^3 - 20x^4 + x^5), \\
& -4038 + 2879x + 517x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (830 - 413x - 186x^2 + 124x^3 - 20x^4 + x^5), \\
& -4118 + 2895x + 517x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& -4086 + 2895x + 517x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& -4198 + 2911x + 517x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& -4166 + 2911x + 517x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-138 + 41x + 37x^2 - 13x^3 + x^4), \\
& (-5 + x) (710 - 405x - 186x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (726 - 405x - 186x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (742 - 405x - 186x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (758 - 405x - 186x^2 + 124x^3 - 20x^4 + x^5), \\
& -3758 + 2783x + 525x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (774 - 405x - 186x^2 + 124x^3 - 20x^4 + x^5), \\
& -3838 + 2799x + 525x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (790 - 405x - 186x^2 + 124x^3 - 20x^4 + x^5), \\
& -3918 + 2815x + 525x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (31 - 12x + x^2) (26 - 3x - 8x^2 + x^3),
\end{aligned}$$

$$\begin{aligned}
& (-5+x) (670-397x-186x^2+124x^3-20x^4+x^5), \\
& (-5+x) (686-397x-186x^2+124x^3-20x^4+x^5), \\
& (-5+x) (13-10x+x^2) (54+11x-10x^2+x^3), \\
& (-5+x) (718-397x-186x^2+124x^3-20x^4+x^5), \\
& -3558+2703x+533x^2-806x^3+224x^4-25x^5+x^6, \\
& (-5+x) (734-397x-186x^2+124x^3-20x^4+x^5), \\
& (-5+x) (646-389x-186x^2+124x^3-20x^4+x^5), \\
& (-5+x) (662-389x-186x^2+124x^3-20x^4+x^5), \\
& (-5+x) (606-381x-186x^2+124x^3-20x^4+x^5), \\
& (-9+x) (674-353x-82x^2+80x^3-16x^4+x^5), \\
& (-7+x) (878-427x-116x^2+98x^3-18x^4+x^5), \\
& -6274+3899x+385x^2-802x^3+224x^4-25x^5+x^6, \\
& (-9+x) (-5+x) (-130+43x+25x^2-11x^3+x^4), \\
& -5818+3755x+393x^2-802x^3+224x^4-25x^5+x^6, \\
& -5898+3771x+393x^2-802x^3+224x^4-25x^5+x^6, \\
& -5946+3787x+393x^2-802x^3+224x^4-25x^5+x^6, \\
& -6026+3803x+393x^2-802x^3+224x^4-25x^5+x^6, \\
& -6074+3819x+393x^2-802x^3+224x^4-25x^5+x^6, \\
& (-9+x) (-5+x) (-122+43x+25x^2-11x^3+x^4), \\
& (-5+x) (1114-509x-182x^2+124x^3-20x^4+x^5), \\
& (-5+x) (1130-509x-182x^2+124x^3-20x^4+x^5), \\
& -5618+3675x+401x^2-802x^3+224x^4-25x^5+x^6, \\
& (-7+x) (814-411x-116x^2+98x^3-18x^4+x^5), \\
& -5778+3707x+401x^2-802x^3+224x^4-25x^5+x^6, \\
& -5746+3707x+401x^2-802x^3+224x^4-25x^5+x^6, \\
& -5826+3723x+401x^2-802x^3+224x^4-25x^5+x^6, \\
& -5954+3755x+401x^2-802x^3+224x^4-25x^5+x^6, \\
& -6082+3787x+401x^2-802x^3+224x^4-25x^5+x^6, \\
& (-5+x) (1042-501x-182x^2+124x^3-20x^4+x^5), \\
& (-5+x) (1058-501x-182x^2+124x^3-20x^4+x^5), \\
& (-5+x) (1074-501x-182x^2+124x^3-20x^4+x^5), \\
& (-5+x) (1090-501x-182x^2+124x^3-20x^4+x^5), \\
& (-7+x) (774-403x-116x^2+98x^3-18x^4+x^5), \\
& (-7+x) (-5+x) (-158+49x+33x^2-13x^3+x^4), \\
& -5498+3611x+409x^2-802x^3+224x^4-25x^5+x^6, \\
& -5578+3627x+409x^2-802x^3+224x^4-25x^5+x^6, \\
& -5626+3643x+409x^2-802x^3+224x^4-25x^5+x^6, \\
& -5706+3659x+409x^2-802x^3+224x^4-25x^5+x^6, \\
& -5754+3675x+409x^2-802x^3+224x^4-25x^5+x^6, \\
& -5834+3691x+409x^2-802x^3+224x^4-25x^5+x^6, \\
& (-5+x) (1018-493x-182x^2+124x^3-20x^4+x^5), \\
& (-5+x) (1034-493x-182x^2+124x^3-20x^4+x^5), \\
& (-7+x) (-5+x) (-150+49x+33x^2-13x^3+x^4), \\
& -5218+3515x+417x^2-802x^3+224x^4-25x^5+x^6,
\end{aligned}$$

$$\begin{aligned}
& (-5 + x) (1066 - 493x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& -5298 + 3531x + 417x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -5378 + 3547x + 417x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -5458 + 3563x + 417x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -5426 + 3563x + 417x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -5506 + 3579x + 417x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -5586 + 3595x + 417x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -5634 + 3611x + 417x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -5762 + 3643x + 417x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (978 - 485x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& (-7 + x) (-5 + x) (-2 + x) (71 + 11x - 11x^2 + x^3), \\
& (-5 + x) (1010 - 485x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (1026 - 485x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& -5098 + 3451x + 425x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (1042 - 485x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& -5178 + 3467x + 425x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -5258 + 3483x + 425x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -5226 + 3483x + 425x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -5338 + 3499x + 425x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -5306 + 3499x + 425x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -5386 + 3515x + 425x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& (38 - 13x + x^2) (-143 + 44x + 30x^2 - 12x^3 + x^4), \\
& -5514 + 3547x + 425x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-182 + 45x + 37x^2 - 13x^3 + x^4), \\
& (-7 + x) (-5 + x) (-134 + 49x + 33x^2 - 13x^3 + x^4), \\
& (-5 + x) (954 - 477x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (970 - 477x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (986 - 477x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& -4898 + 3371x + 433x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (1002 - 477x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& -4978 + 3387x + 433x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (1018 - 477x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& -5058 + 3403x + 433x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -5138 + 3419x + 433x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -5106 + 3419x + 433x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -5186 + 3435x + 433x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -5266 + 3451x + 433x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -5234 + 3451x + 433x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -5314 + 3467x + 433x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-174 + 45x + 37x^2 - 13x^3 + x^4), \\
& (-5 + x) (914 - 469x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (930 - 469x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (946 - 469x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& -4698 + 3291x + 441x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (-2 + x) (-481 - 6x + 88x^2 - 18x^3 + x^4),
\end{aligned}$$

$$\begin{aligned}
& -4778 + 3307x + 441x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (978 - 469x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& -4858 + 3323x + 441x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -4938 + 3339x + 441x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -4906 + 3339x + 441x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -5018 + 3355x + 441x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -4986 + 3355x + 441x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& (17 - 10x + x^2) (-298 + 23x + 57x^2 - 15x^3 + x^4), \\
& (31 - 12x + x^2) (-166 + 45x + 37x^2 - 13x^3 + x^4), \\
& (-5 + x) (874 - 461x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (890 - 461x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (906 - 461x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (922 - 461x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& -4578 + 3227x + 449x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (938 - 461x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& -4658 + 3243x + 449x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (954 - 461x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& -4738 + 3259x + 449x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -4706 + 3259x + 449x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -4818 + 3275x + 449x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -4786 + 3275x + 449x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-158 + 45x + 37x^2 - 13x^3 + x^4), \\
& (-5 + x) (850 - 453x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (866 - 453x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (882 - 453x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& -4378 + 3147x + 457x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (898 - 453x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& -4458 + 3163x + 457x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (914 - 453x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& -4538 + 3179x + 457x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (-2 + x) (31 - 12x + x^2) (-15 - 6x + x^2), \\
& (-5 + x) (810 - 445x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (826 - 445x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (842 - 445x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (858 - 445x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (770 - 437x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (786 - 437x - 182x^2 + 124x^3 - 20x^4 + x^5), \\
& (-9 + x) (-3 + x) (-258 + 45x + 41x^2 - 13x^3 + x^4), \\
& -6718 + 4215x + 317x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& -6766 + 4231x + 317x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& (-3 + x) (2298 - 655x - 324x^2 + 158x^3 - 22x^4 + x^5), \\
& (-9 + x) (-5 + x) (-142 + 47x + 25x^2 - 11x^3 + x^4), \\
& (-5 + x) (1294 - 565x - 178x^2 + 124x^3 - 20x^4 + x^5), \\
& -6438 + 4119x + 325x^2 - 798x^3 + 224x^4 - 25x^5 + x^6,
\end{aligned}$$

$$\begin{aligned}
& -6518 + 4135x + 325x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& (-7+x)(938 - 459x - 112x^2 + 98x^3 - 18x^4 + x^5), \\
& -6646 + 4167x + 325x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& (-9+x)(-5+x)(-134 + 47x + 25x^2 - 11x^3 + x^4), \\
& (-5+x)(1222 - 557x - 178x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)(1238 - 557x - 178x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)(1254 - 557x - 178x^2 + 124x^3 - 20x^4 + x^5), \\
& -6238 + 4039x + 333x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& -6318 + 4055x + 333x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& (-7+x)(914 - 451x - 112x^2 + 98x^3 - 18x^4 + x^5), \\
& -6574 + 4119x + 333x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x)(1182 - 549x - 178x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)(1198 - 549x - 178x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)(1214 - 549x - 178x^2 + 124x^3 - 20x^4 + x^5), \\
& -6038 + 3959x + 341x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x)(1230 - 549x - 178x^2 + 124x^3 - 20x^4 + x^5), \\
& (-7+x)(874 - 443x - 112x^2 + 98x^3 - 18x^4 + x^5), \\
& -6198 + 3991x + 341x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& -6246 + 4007x + 341x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& -6326 + 4023x + 341x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& -6454 + 4055x + 341x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x)(1142 - 541x - 178x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)(1158 - 541x - 178x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)(1174 - 541x - 178x^2 + 124x^3 - 20x^4 + x^5), \\
& (-7+x)(-5+x)(-170 + 53x + 33x^2 - 13x^3 + x^4), \\
& -5918 + 3895x + 349x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& -5998 + 3911x + 349x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& -6078 + 3927x + 349x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& -6046 + 3927x + 349x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& -6126 + 3943x + 349x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& -6206 + 3959x + 349x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& -6254 + 3975x + 349x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x)(1118 - 533x - 178x^2 + 124x^3 - 20x^4 + x^5), \\
& (-7+x)(-5+x)(-162 + 53x + 33x^2 - 13x^3 + x^4), \\
& (-5+x)(1150 - 533x - 178x^2 + 124x^3 - 20x^4 + x^5), \\
& -5718 + 3815x + 357x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x)(1166 - 533x - 178x^2 + 124x^3 - 20x^4 + x^5), \\
& -5798 + 3831x + 357x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& -5878 + 3847x + 357x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& -5958 + 3863x + 357x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& -5926 + 3863x + 357x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& -6006 + 3879x + 357x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& -6054 + 3895x + 357x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& -6134 + 3911x + 357x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2)(-202 + 49x + 37x^2 - 13x^3 + x^4),
\end{aligned}$$

$$\begin{aligned}
& (-7+x)(-5+x)(-154+53x+33x^2-13x^3+x^4), \\
& (-5+x)(1094-525x-178x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1110-525x-178x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1126-525x-178x^2+124x^3-20x^4+x^5), \\
& -5598+3751x+365x^2-798x^3+224x^4-25x^5+x^6, \\
& (-5+x)(1142-525x-178x^2+124x^3-20x^4+x^5), \\
& -5678+3767x+365x^2-798x^3+224x^4-25x^5+x^6, \\
& -5758+3783x+365x^2-798x^3+224x^4-25x^5+x^6, \\
& -5726+3783x+365x^2-798x^3+224x^4-25x^5+x^6, \\
& -5806+3799x+365x^2-798x^3+224x^4-25x^5+x^6, \\
& -5886+3815x+365x^2-798x^3+224x^4-25x^5+x^6, \\
& -5934+3831x+365x^2-798x^3+224x^4-25x^5+x^6, \\
& (31-12x+x^2)(-194+49x+37x^2-13x^3+x^4), \\
& (-5+x)(1038-517x-178x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1054-517x-178x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1070-517x-178x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1086-517x-178x^2+124x^3-20x^4+x^5), \\
& -5398+3671x+373x^2-798x^3+224x^4-25x^5+x^6, \\
& (-5+x)(1102-517x-178x^2+124x^3-20x^4+x^5), \\
& -5478+3687x+373x^2-798x^3+224x^4-25x^5+x^6, \\
& -5558+3703x+373x^2-798x^3+224x^4-25x^5+x^6, \\
& -5638+3719x+373x^2-798x^3+224x^4-25x^5+x^6, \\
& -5606+3719x+373x^2-798x^3+224x^4-25x^5+x^6, \\
& -5686+3735x+373x^2-798x^3+224x^4-25x^5+x^6, \\
& (31-12x+x^2)(-186+49x+37x^2-13x^3+x^4), \\
& (-5+x)(1014-509x-178x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1030-509x-178x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1046-509x-178x^2+124x^3-20x^4+x^5), \\
& -5198+3591x+381x^2-798x^3+224x^4-25x^5+x^6, \\
& (-5+x)(1062-509x-178x^2+124x^3-20x^4+x^5), \\
& -5278+3607x+381x^2-798x^3+224x^4-25x^5+x^6, \\
& (-5+x)(1078-509x-178x^2+124x^3-20x^4+x^5), \\
& -5358+3623x+381x^2-798x^3+224x^4-25x^5+x^6, \\
& -5438+3639x+381x^2-798x^3+224x^4-25x^5+x^6, \\
& (17-10x+x^2)(-318+27x+57x^2-15x^3+x^4), \\
& (31-12x+x^2)(-178+49x+37x^2-13x^3+x^4), \\
& (-5+x)(974-501x-178x^2+124x^3-20x^4+x^5), \\
& (-5+x)(990-501x-178x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1006-501x-178x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1022-501x-178x^2+124x^3-20x^4+x^5), \\
& -5078+3527x+389x^2-798x^3+224x^4-25x^5+x^6, \\
& (-5+x)(1038-501x-178x^2+124x^3-20x^4+x^5), \\
& -5158+3543x+389x^2-798x^3+224x^4-25x^5+x^6, \\
& (-5+x)(2+x)(31-12x+x^2)(17-10x+x^2),
\end{aligned}$$

$$\begin{aligned}
& (-5+x) (934 - 493x - 178x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (950 - 493x - 178x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (966 - 493x - 178x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (982 - 493x - 178x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (910 - 485x - 178x^2 + 124x^3 - 20x^4 + x^5), \\
& -7586 + 4675x + 241x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -7258 + 4563x + 249x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& (-3+x) (2446 - 711x - 320x^2 + 158x^3 - 22x^4 + x^5), \\
& (-3+x) (2462 - 711x - 320x^2 + 158x^3 - 22x^4 + x^5), \\
& (-9+x) (-5+x) (-154 + 51x + 25x^2 - 11x^3 + x^4), \\
& (-5+x) (1402 - 613x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1418 - 613x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& -7058 + 4483x + 257x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -7138 + 4499x + 257x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& (-7+x) (-3+x) (-346 + 51x + 53x^2 - 15x^3 + x^4), \\
& (-5+x) (1346 - 605x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1362 - 605x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1378 - 605x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& -6858 + 4403x + 265x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -6938 + 4419x + 265x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -7018 + 4435x + 265x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -7066 + 4451x + 265x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (1306 - 597x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1322 - 597x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1338 - 597x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1354 - 597x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& -6738 + 4339x + 273x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& (-7+x) (974 - 483x - 108x^2 + 98x^3 - 18x^4 + x^5), \\
& -6866 + 4371x + 273x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -6946 + 4387x + 273x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& (-3+x) (2358 - 687x - 320x^2 + 158x^3 - 22x^4 + x^5), \\
& (-5+x) (1282 - 589x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1298 - 589x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1314 - 589x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& (-7+x) (934 - 475x - 108x^2 + 98x^3 - 18x^4 + x^5), \\
& -6618 + 4275x + 281x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -6698 + 4291x + 281x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -6746 + 4307x + 281x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -6826 + 4323x + 281x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -6874 + 4339x + 281x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (1242 - 581x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1258 - 581x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& (-7+x) (-5+x) (-182 + 57x + 33x^2 - 13x^3 + x^4), \\
& (-5+x) (1290 - 581x - 174x^2 + 124x^3 - 20x^4 + x^5),
\end{aligned}$$

$$\begin{aligned}
& -6418 + 4195x + 289x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -6498 + 4211x + 289x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -6578 + 4227x + 289x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -6546 + 4227x + 289x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -6626 + 4243x + 289x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -6754 + 4275x + 289x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& (-3 + x)(31 - 12x + x^2)(74 + 7x - 10x^2 + x^3), \\
& (-5 + x)(1202 - 573x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& (-7 + x)(-5 + x)(-174 + 57x + 33x^2 - 13x^3 + x^4), \\
& (-5 + x)(1234 - 573x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(1250 - 573x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& -6218 + 4115x + 297x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(1266 - 573x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& -6298 + 4131x + 297x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -6378 + 4147x + 297x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -6426 + 4163x + 297x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -6506 + 4179x + 297x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -6554 + 4195x + 297x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2)(-214 + 53x + 37x^2 - 13x^3 + x^4), \\
& (-5 + x)(1178 - 565x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(1210 - 565x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& -6018 + 4035x + 305x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(1226 - 565x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& -6098 + 4051x + 305x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -6178 + 4067x + 305x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -6258 + 4083x + 305x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -6226 + 4083x + 305x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -6306 + 4099x + 305x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2)(-206 + 53x + 37x^2 - 13x^3 + x^4), \\
& (-5 + x)(1138 - 557x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(1154 - 557x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(1170 - 557x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(1186 - 557x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& -5898 + 3971x + 313x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(1202 - 557x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& -5978 + 3987x + 313x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -6058 + 4003x + 313x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& -6026 + 4003x + 313x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2)(-198 + 53x + 37x^2 - 13x^3 + x^4), \\
& (-5 + x)(1114 - 549x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(1130 - 549x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(1146 - 549x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& -5698 + 3891x + 321x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(1162 - 549x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& -5778 + 3907x + 321x^2 - 794x^3 + 224x^4 - 25x^5 + x^6,
\end{aligned}$$

$$\begin{aligned}
& (-5+x) (31-12x+x^2) (38-3x-8x^2+x^3), \\
& (-5+x) (-2+x) (-537+2x+88x^2-18x^3+x^4), \\
& (-5+x) (1090-541x-174x^2+124x^3-20x^4+x^5), \\
& (-5+x) (1106-541x-174x^2+124x^3-20x^4+x^5), \\
& (-5+x) (1034-533x-174x^2+124x^3-20x^4+x^5), \\
& -8206+5039x+173x^2-790x^3+224x^4-25x^5+x^6, \\
& (-9+x) (-5+x) (-3+x) (58+x-8x^2+x^3), \\
& (-3+x) (2626-767x-316x^2+158x^3-22x^4+x^5), \\
& -7958+4943x+181x^2-790x^3+224x^4-25x^5+x^6, \\
& (-5+x) (1510-661x-170x^2+124x^3-20x^4+x^5), \\
& (-5+x) (1526-661x-170x^2+124x^3-20x^4+x^5), \\
& (-5+x) (-3+x) (-514+49x+73x^2-17x^3+x^4), \\
& (-3+x) (2586-759x-316x^2+158x^3-22x^4+x^5), \\
& -7886+4895x+189x^2-790x^3+224x^4-25x^5+x^6, \\
& (-5+x) (1470-653x-170x^2+124x^3-20x^4+x^5), \\
& (-5+x) (1486-653x-170x^2+124x^3-20x^4+x^5), \\
& (-5+x) (1502-653x-170x^2+124x^3-20x^4+x^5), \\
& -7558+4783x+197x^2-790x^3+224x^4-25x^5+x^6, \\
& (-3+x) (2546-751x-316x^2+158x^3-22x^4+x^5), \\
& (-5+x) (1446-645x-170x^2+124x^3-20x^4+x^5), \\
& (-5+x) (1462-645x-170x^2+124x^3-20x^4+x^5), \\
& (-5+x) (1478-645x-170x^2+124x^3-20x^4+x^5), \\
& -7358+4703x+205x^2-790x^3+224x^4-25x^5+x^6, \\
& -7438+4719x+205x^2-790x^3+224x^4-25x^5+x^6, \\
& (-3+x) (2522-743x-316x^2+158x^3-22x^4+x^5), \\
& (-5+x) (1406-637x-170x^2+124x^3-20x^4+x^5), \\
& (-5+x) (1422-637x-170x^2+124x^3-20x^4+x^5), \\
& (-5+x) (1438-637x-170x^2+124x^3-20x^4+x^5), \\
& (-7+x) (1034-515x-104x^2+98x^3-18x^4+x^5), \\
& -7318+4655x+213x^2-790x^3+224x^4-25x^5+x^6, \\
& -7366+4671x+213x^2-790x^3+224x^4-25x^5+x^6, \\
& (-3+x) (2482-735x-316x^2+158x^3-22x^4+x^5), \\
& (-5+x) (1366-629x-170x^2+124x^3-20x^4+x^5), \\
& (-5+x) (1382-629x-170x^2+124x^3-20x^4+x^5), \\
& (-5+x) (1398-629x-170x^2+124x^3-20x^4+x^5), \\
& (-7+x) (-5+x) (-202+61x+33x^2-13x^3+x^4), \\
& -7038+4559x+221x^2-790x^3+224x^4-25x^5+x^6, \\
& -7118+4575x+221x^2-790x^3+224x^4-25x^5+x^6, \\
& -7198+4591x+221x^2-790x^3+224x^4-25x^5+x^6, \\
& -7246+4607x+221x^2-790x^3+224x^4-25x^5+x^6, \\
& (-3+x) (2458-727x-316x^2+158x^3-22x^4+x^5), \\
& (-5+x) (1342-621x-170x^2+124x^3-20x^4+x^5), \\
& (-7+x) (-5+x) (-194+61x+33x^2-13x^3+x^4),
\end{aligned}$$

$$\begin{aligned}
& (-5+x) (1374 - 621x - 170x^2 + 124x^3 - 20x^4 + x^5), \\
& -6838 + 4479x + 229x^2 - 790x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (1390 - 621x - 170x^2 + 124x^3 - 20x^4 + x^5), \\
& -6918 + 4495x + 229x^2 - 790x^3 + 224x^4 - 25x^5 + x^6, \\
& -6998 + 4511x + 229x^2 - 790x^3 + 224x^4 - 25x^5 + x^6, \\
& -7046 + 4527x + 229x^2 - 790x^3 + 224x^4 - 25x^5 + x^6, \\
& -7126 + 4543x + 229x^2 - 790x^3 + 224x^4 - 25x^5 + x^6, \\
& (-3+x) (31 - 12x + x^2) (78 + 7x - 10x^2 + x^3), \\
& (-7+x) (-5+x) (-186 + 61x + 33x^2 - 13x^3 + x^4), \\
& (-5+x) (1318 - 613x - 170x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1334 - 613x - 170x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1350 - 613x - 170x^2 + 124x^3 - 20x^4 + x^5), \\
& -6718 + 4415x + 237x^2 - 790x^3 + 224x^4 - 25x^5 + x^6, \\
& -6798 + 4431x + 237x^2 - 790x^3 + 224x^4 - 25x^5 + x^6, \\
& -6878 + 4447x + 237x^2 - 790x^3 + 224x^4 - 25x^5 + x^6, \\
& -6846 + 4447x + 237x^2 - 790x^3 + 224x^4 - 25x^5 + x^6, \\
& -6926 + 4463x + 237x^2 - 790x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-226 + 57x + 37x^2 - 13x^3 + x^4), \\
& (-5+x) (1278 - 605x - 170x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1294 - 605x - 170x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1310 - 605x - 170x^2 + 124x^3 - 20x^4 + x^5), \\
& -6518 + 4335x + 245x^2 - 790x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (1326 - 605x - 170x^2 + 124x^3 - 20x^4 + x^5), \\
& -6598 + 4351x + 245x^2 - 790x^3 + 224x^4 - 25x^5 + x^6, \\
& -6678 + 4367x + 245x^2 - 790x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-218 + 57x + 37x^2 - 13x^3 + x^4), \\
& (-5+x) (1238 - 597x - 170x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1254 - 597x - 170x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1270 - 597x - 170x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1286 - 597x - 170x^2 + 124x^3 - 20x^4 + x^5), \\
& -6398 + 4271x + 253x^2 - 790x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (31 - 12x + x^2) (42 - 3x - 8x^2 + x^3), \\
& (-5+x) (1198 - 589x - 170x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1214 - 589x - 170x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1230 - 589x - 170x^2 + 124x^3 - 20x^4 + x^5), \\
& -8698 + 5371x + 105x^2 - 786x^3 + 224x^4 - 25x^5 + x^6, \\
& (-9+x) (-5+x) (-3+x) (62 + x - 8x^2 + x^3), \\
& (-5+x) (1690 - 717x - 166x^2 + 124x^3 - 20x^4 + x^5), \\
& -8578 + 5307x + 113x^2 - 786x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (1634 - 709x - 166x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (-3+x) (-550 + 53x + 73x^2 - 17x^3 + x^4), \\
& (-5+x) (1666 - 709x - 166x^2 + 124x^3 - 20x^4 + x^5), \\
& -8378 + 5227x + 121x^2 - 786x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (1610 - 701x - 166x^2 + 124x^3 - 20x^4 + x^5),
\end{aligned}$$

$$\begin{aligned}
& (-5+x)(-3+x)(-542+53x+73x^2-17x^3+x^4), \\
& (-3+x)(2726-807x-312x^2+158x^3-22x^4+x^5), \\
& -8258+5163x+129x^2-786x^3+224x^4-25x^5+x^6, \\
& (-5+x)(1570-693x-166x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1586-693x-166x^2+124x^3-20x^4+x^5), \\
& (-5+x)(-3+x)(-534+53x+73x^2-17x^3+x^4), \\
& (-3+x)(2686-799x-312x^2+158x^3-22x^4+x^5), \\
& -8186+5115x+137x^2-786x^3+224x^4-25x^5+x^6, \\
& (-5+x)(1546-685x-166x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1562-685x-166x^2+124x^3-20x^4+x^5), \\
& -7858+5003x+145x^2-786x^3+224x^4-25x^5+x^6, \\
& (-7+x)(-3+x)(-378+59x+53x^2-15x^3+x^4), \\
& -8066+5051x+145x^2-786x^3+224x^4-25x^5+x^6, \\
& (-5+x)(1506-677x-166x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1522-677x-166x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1538-677x-166x^2+124x^3-20x^4+x^5), \\
& -7738+4939x+153x^2-786x^3+224x^4-25x^5+x^6, \\
& (-3+x)(2606-783x-312x^2+158x^3-22x^4+x^5), \\
& (-3+x)(38-13x+x^2)(69+3x-9x^2+x^3), \\
& (-5+x)(1466-669x-166x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1482-669x-166x^2+124x^3-20x^4+x^5), \\
& (-7+x)(-5+x)(-214+65x+33x^2-13x^3+x^4), \\
& (-5+x)(1514-669x-166x^2+124x^3-20x^4+x^5), \\
& -7538+4859x+161x^2-786x^3+224x^4-25x^5+x^6, \\
& -7618+4875x+161x^2-786x^3+224x^4-25x^5+x^6, \\
& (-3+x)(2582-775x-312x^2+158x^3-22x^4+x^5), \\
& (31-12x+x^2)(-254+61x+37x^2-13x^3+x^4), \\
& (-7+x)(-5+x)(-206+65x+33x^2-13x^3+x^4), \\
& (-5+x)(1458-661x-166x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1474-661x-166x^2+124x^3-20x^4+x^5), \\
& -7338+4779x+169x^2-786x^3+224x^4-25x^5+x^6, \\
& -7418+4795x+169x^2-786x^3+224x^4-25x^5+x^6, \\
& -7498+4811x+169x^2-786x^3+224x^4-25x^5+x^6, \\
& -7546+4827x+169x^2-786x^3+224x^4-25x^5+x^6, \\
& (-3+x)(31-12x+x^2)(82+7x-10x^2+x^3), \\
& (-5+x)(1402-653x-166x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1418-653x-166x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1434-653x-166x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1450-653x-166x^2+124x^3-20x^4+x^5), \\
& -7218+4715x+177x^2-786x^3+224x^4-25x^5+x^6, \\
& -7298+4731x+177x^2-786x^3+224x^4-25x^5+x^6, \\
& (31-12x+x^2)(-238+61x+37x^2-13x^3+x^4), \\
& (-5+x)(1362-645x-166x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1378-645x-166x^2+124x^3-20x^4+x^5),
\end{aligned}$$

$$\begin{aligned}
& (-5+x) (1394 - 645x - 166x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1410 - 645x - 166x^2 + 124x^3 - 20x^4 + x^5), \\
& -7018 + 4635x + 185x^2 - 786x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (31 - 12x + x^2) (46 - 3x - 8x^2 + x^3), \\
& (-5+x) (1338 - 637x - 166x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1354 - 637x - 166x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1798 - 765x - 162x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1814 - 765x - 162x^2 + 124x^3 - 20x^4 + x^5), \\
& -9198 + 5671x + 45x^2 - 782x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (1774 - 757x - 162x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1790 - 757x - 162x^2 + 124x^3 - 20x^4 + x^5), \\
& (-11 - 2x + x^2) (818 - 657x + 189x^2 - 23x^3 + x^4), \\
& (-5+x) (-3+x) (-578 + 57x + 73x^2 - 17x^3 + x^4), \\
& (-5+x) (1750 - 749x - 162x^2 + 124x^3 - 20x^4 + x^5), \\
& -8878 + 5527x + 61x^2 - 782x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (-3+x) (-570 + 57x + 73x^2 - 17x^3 + x^4), \\
& (-5+x) (1726 - 741x - 162x^2 + 124x^3 - 20x^4 + x^5), \\
& -8678 + 5447x + 69x^2 - 782x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (1670 - 733x - 162x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (-3+x) (-562 + 57x + 73x^2 - 17x^3 + x^4), \\
& -8558 + 5383x + 77x^2 - 782x^3 + 224x^4 - 25x^5 + x^6, \\
& -8686 + 5415x + 77x^2 - 782x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (1630 - 725x - 162x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1646 - 725x - 162x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (-3+x) (-554 + 57x + 73x^2 - 17x^3 + x^4), \\
& (-7+x) (-3+x) (-398 + 63x + 53x^2 - 15x^3 + x^4), \\
& -8438 + 5319x + 85x^2 - 782x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (1606 - 717x - 162x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1622 - 717x - 162x^2 + 124x^3 - 20x^4 + x^5), \\
& (-7+x) (-5+x) (-3+x) (78 + 3x - 10x^2 + x^3), \\
& -8158 + 5223x + 93x^2 - 782x^3 + 224x^4 - 25x^5 + x^6, \\
& (-3+x) (2746 - 831x - 308x^2 + 158x^3 - 22x^4 + x^5), \\
& -8366 + 5271x + 93x^2 - 782x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (1566 - 709x - 162x^2 + 124x^3 - 20x^4 + x^5), \\
& (-7+x) (-5+x) (-226 + 69x + 33x^2 - 13x^3 + x^4), \\
& (-5+x) (1598 - 709x - 162x^2 + 124x^3 - 20x^4 + x^5), \\
& -8038 + 5159x + 101x^2 - 782x^3 + 224x^4 - 25x^5 + x^6, \\
& (-3+x) (2706 - 823x - 308x^2 + 158x^3 - 22x^4 + x^5), \\
& (-3+x) (2722 - 823x - 308x^2 + 158x^3 - 22x^4 + x^5), \\
& (31 - 12x + x^2) (-266 + 65x + 37x^2 - 13x^3 + x^4), \\
& (-5+x) (1542 - 701x - 162x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1558 - 701x - 162x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1574 - 701x - 162x^2 + 124x^3 - 20x^4 + x^5),
\end{aligned}$$

$$\begin{aligned}
& -7838 + 5079x + 109x^2 - 782x^3 + 224x^4 - 25x^5 + x^6, \\
& -7918 + 5095x + 109x^2 - 782x^3 + 224x^4 - 25x^5 + x^6, \\
& (-3+x)(31-12x+x^2)(86+7x-10x^2+x^3), \\
& (-5+x)(1502-693x-162x^2+124x^3-20x^4+x^5), \\
& (-5+x)(22-11x+x^2)(69+3x-9x^2+x^3), \\
& (-5+x)(1534-693x-162x^2+124x^3-20x^4+x^5), \\
& (-5+x)(31-12x+x^2)(50-3x-8x^2+x^3), \\
& (-5+x)(1462-685x-162x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1478-685x-162x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1938-813x-158x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1898-805x-158x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1914-805x-158x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1874-797x-158x^2+124x^3-20x^4+x^5), \\
& -9498 + 5891x - 7x^2 - 778x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x)(1834-789x-158x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1850-789x-158x^2+124x^3-20x^4+x^5), \\
& (-5+x)(-3+x)(-598+61x+73x^2-17x^3+x^4), \\
& (-5+x)(1810-781x-158x^2+124x^3-20x^4+x^5), \\
& -9178 + 5747x + 9x^2 - 778x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x)(-3+x)(-590+61x+73x^2-17x^3+x^4), \\
& (-5+x)(1786-773x-158x^2+124x^3-20x^4+x^5), \\
& -8978 + 5667x + 17x^2 - 778x^3 + 224x^4 - 25x^5 + x^6, \\
& (-7+x)(1294-627x-92x^2+98x^3-18x^4+x^5), \\
& (-5+x)(1730-765x-158x^2+124x^3-20x^4+x^5), \\
& (-5+x)(-3+x)(-582+61x+73x^2-17x^3+x^4), \\
& (-5+x)(1762-765x-158x^2+124x^3-20x^4+x^5), \\
& -8858 + 5603x + 25x^2 - 778x^3 + 224x^4 - 25x^5 + x^6, \\
& -8986 + 5635x + 25x^2 - 778x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x)(1706-757x-158x^2+124x^3-20x^4+x^5), \\
& (-7+x)(-5+x)(-3+x)(82+3x-10x^2+x^3), \\
& (-3+x)(2886-879x-304x^2+158x^3-22x^4+x^5), \\
& -8738 + 5539x + 33x^2 - 778x^3 + 224x^4 - 25x^5 + x^6, \\
& (31-12x+x^2)(26-11x+x^2)(-11-2x+x^2), \\
& (-7+x)(-5+x)(-238+73x+33x^2-13x^3+x^4), \\
& (-5+x)(1682-749x-158x^2+124x^3-20x^4+x^5), \\
& (-5+x)(-3+x)(-566+61x+73x^2-17x^3+x^4), \\
& (-3+x)(2846-871x-304x^2+158x^3-22x^4+x^5), \\
& (31-12x+x^2)(-278+69x+37x^2-13x^3+x^4), \\
& (-5+x)(1626-741x-158x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1642-741x-158x^2+124x^3-20x^4+x^5), \\
& (-5+x)(1658-741x-158x^2+124x^3-20x^4+x^5), \\
& (-5+x)(-3+x)(31-12x+x^2)(-18-5x+x^2), \\
& (-5+x)(1602-733x-158x^2+124x^3-20x^4+x^5),
\end{aligned}$$

$$\begin{aligned}
& (-5+x) (2062 - 861x - 154x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (2038 - 853x - 154x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1998 - 845x - 154x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1974 - 837x - 154x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1934 - 829x - 154x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1894 - 821x - 154x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1910 - 821x - 154x^2 + 124x^3 - 20x^4 + x^5), \\
& -9678 + 6047x - 51x^2 - 774x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (1870 - 813x - 154x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1886 - 813x - 154x^2 + 124x^3 - 20x^4 + x^5), \\
& (-7+x) (1354 - 659x - 88x^2 + 98x^3 - 18x^4 + x^5), \\
& (-5+x) (-3+x) (-610 + 65x + 73x^2 - 17x^3 + x^4), \\
& (-5+x) (1846 - 805x - 154x^2 + 124x^3 - 20x^4 + x^5), \\
& -9358 + 5903x - 35x^2 - 774x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-306 + 73x + 37x^2 - 13x^3 + x^4), \\
& (-5+x) (1790 - 797x - 154x^2 + 124x^3 - 20x^4 + x^5), \\
& (-7+x) (-5+x) (-3+x) (86 + 3x - 10x^2 + x^3), \\
& (-5+x) (1822 - 797x - 154x^2 + 124x^3 - 20x^4 + x^5), \\
& -9158 + 5823x - 27x^2 - 774x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-298 + 73x + 37x^2 - 13x^3 + x^4), \\
& (-5+x) (1766 - 789x - 154x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (-3+x) (-594 + 65x + 73x^2 - 17x^3 + x^4), \\
& (-5+x) (31 - 12x + x^2) (58 - 3x - 8x^2 + x^3), \\
& (-5+x) (1726 - 781x - 154x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (2162 - 901x - 150x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (2098 - 885x - 150x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (2058 - 877x - 150x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (2034 - 869x - 150x^2 + 124x^3 - 20x^4 + x^5), \\
& (38 - 13x + x^2) (-271 + 76x + 30x^2 - 12x^3 + x^4), \\
& (-5+x) (1994 - 861x - 150x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (2010 - 861x - 150x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (1970 - 853x - 150x^2 + 124x^3 - 20x^4 + x^5), \\
& -9978 + 6267x - 103x^2 - 770x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5+x) (1930 - 845x - 150x^2 + 124x^3 - 20x^4 + x^5), \\
& (-7+x) (-5+x) (-278 + 81x + 33x^2 - 13x^3 + x^4), \\
& (31 - 12x + x^2) (-318 + 77x + 37x^2 - 13x^3 + x^4), \\
& (-7+x) (-5+x) (-3+x) (90 + 3x - 10x^2 + x^3), \\
& (-5+x) (1906 - 837x - 150x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (31 - 12x + x^2) (62 - 3x - 8x^2 + x^3), \\
& (-5+x) (2158 - 917x - 146x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (2134 - 909x - 146x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (2094 - 901x - 146x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x) (2054 - 893x - 146x^2 + 124x^3 - 20x^4 + x^5),
\end{aligned}$$

$$\begin{aligned}
&(-5+x)(2070-893x-146x^2+124x^3-20x^4+x^5), \\
&(31-12x+x^2)(-338+81x+37x^2-13x^3+x^4), \\
&(-7+x)(-5+x)(-290+85x+33x^2-13x^3+x^4), \\
&(-5+x)(31-12x+x^2)(66-3x-8x^2+x^3), \\
&(-5+x)(2258-957x-142x^2+124x^3-20x^4+x^5), \\
&(-5+x)(2194-941x-142x^2+124x^3-20x^4+x^5), \\
&(-5+x)(2154-933x-142x^2+124x^3-20x^4+x^5), \\
&(-7+x)(-5+x)(31-12x+x^2)(-10-x+x^2), \\
&(-5+x)(2318-989x-138x^2+124x^3-20x^4+x^5), \\
&(-5+x)(31-12x+x^2)(74-3x-8x^2+x^3), (-5+x)(31-12x+x^2)(78-3x-8x^2+x^3) \}
\end{aligned}$$

Length[list]

1950

listmod128 = modfilter[list*mu[chisub] // Factor, chiSmod128n27, 128]

$$\begin{aligned}
&\{(-5+x)^9(5+x)^{13}(150-141x-210x^2+124x^3-20x^4+x^5), \\
&(-5+x)^8(5+x)^{13}(-686+855x+909x^2-830x^3+224x^4-25x^5+x^6), \\
&(-5+x)^9(1+x)(5+x)^{13}(178-351x+145x^2-21x^3+x^4), \\
&(-5+x)^8(5+x)^{13}(-6446+4087x+333x^2-798x^3+224x^4-25x^5+x^6), \\
&(-5+x)^8(5+x)^{13}(-942+919x+909x^2-830x^3+224x^4-25x^5+x^6), \\
&(-5+x)^8(5+x)^{13}(-826+1043x+857x^2-826x^3+224x^4-25x^5+x^6), \\
&(-5+x)^9(5+x)^{13}(114-173x-206x^2+124x^3-20x^4+x^5), \\
&(-5+x)^8(5+x)^{13}(-554+387x+1065x^2-842x^3+224x^4-25x^5+x^6), \\
&(-5+x)^8(5+x)^{13}(-390+495x+1013x^2-838x^3+224x^4-25x^5+x^6), \\
&(-5+x)^8(5+x)^{13}(-550+527x+1013x^2-838x^3+224x^4-25x^5+x^6), \\
&(-5+x)^8(5+x)^{13}(31-12x+x^2)(-26+9x+37x^2-13x^3+x^4), \\
&(-5+x)^8(5+x)^{13}(-994+843x+945x^2-834x^3+224x^4-25x^5+x^6), \\
&(-5+x)^8(5+x)^{13}(-1090+875x+945x^2-834x^3+224x^4-25x^5+x^6), \\
&(-5+x)^8(5+x)^{13}(-1346+939x+945x^2-834x^3+224x^4-25x^5+x^6), \\
&(-5+x)^8(5+x)^{13}(-98+491x+977x^2-834x^3+224x^4-25x^5+x^6), \\
&(-5+x)^8(5+x)^{13}(17+35x-13x^2+x^3)(-2+33x-12x^2+x^3), \\
&(-5+x)^8(5+x)^{13}(-194+523x+977x^2-834x^3+224x^4-25x^5+x^6), \\
&(-5+x)^8(5+x)^{13}(-354+555x+977x^2-834x^3+224x^4-25x^5+x^6), \\
&(-5+x)^8(5+x)^{13}(-1582+1207x+877x^2-830x^3+224x^4-25x^5+x^6), \\
&(-5+x)^8(5+x)^{13}(-1742+1239x+877x^2-830x^3+224x^4-25x^5+x^6), \\
&(-5+x)^8(5+x)^{13}(-1838+1271x+877x^2-830x^3+224x^4-25x^5+x^6), \\
&(-9+x)(-5+x)^9(5+x)^{13}(-6+15x+25x^2-11x^3+x^4), \\
&(-5+x)^9(5+x)^{13}(86-141x-210x^2+124x^3-20x^4+x^5), \\
&(-5+x)^9(5+x)^{13}(118-141x-210x^2+124x^3-20x^4+x^5), \\
&(-5+x)^8(5+x)^{13}(-526+823x+909x^2-830x^3+224x^4-25x^5+x^6), \\
&(-5+x)^8(5+x)^{13}(-846+887x+909x^2-830x^3+224x^4-25x^5+x^6), \\
&(-5+x)^9(5+x)^{13}(-1-8x+x^2)(10+29x-12x^2+x^3), \\
&(-9+x)(-5+x)^9(-1+x)(5+x)^{13}(34+15x-10x^2+x^3),
\end{aligned}$$

$$\begin{aligned}
& (-5+x)^8 (5+x)^{13} (-1466 + 1331x + 825x^2 - 826x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-1626 + 1363x + 825x^2 - 826x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-1786 + 1395x + 825x^2 - 826x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-1882 + 1427x + 825x^2 - 826x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-2042 + 1459x + 825x^2 - 826x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^9 (5+x)^{13} (82 - 173x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)^9 (5+x)^{13} (146 - 173x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)^9 (5+x)^{13} (210 - 173x - 206x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)^8 (5+x)^{13} (-986 + 1075x + 857x^2 - 826x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^9 (5+x)^{13} (-1 - 8x + x^2) (14 + 29x - 12x^2 + x^3), \\
& (-5+x)^8 (5+x)^{13} (-2614 + 1887x + 741x^2 - 822x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-2774 + 1919x + 741x^2 - 822x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-3030 + 1983x + 741x^2 - 822x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-1718 + 1535x + 773x^2 - 822x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-1878 + 1567x + 773x^2 - 822x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-2038 + 1599x + 773x^2 - 822x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-42 + 51x - 14x^2 + x^3) (47 + 19x - 11x^2 + x^3), \\
& (-5+x)^8 (5+x)^{13} (-2134 + 1631x + 773x^2 - 822x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (31 - 12x + x^2) (-74 + 25x + 37x^2 - 13x^3 + x^4), \\
& (-5+x)^8 (5+x)^{13} (-918 + 1215x + 805x^2 - 822x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-1078 + 1247x + 805x^2 - 822x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-3314 + 2267x + 673x^2 - 818x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-3474 + 2299x + 673x^2 - 818x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-2258 + 1883x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-2418 + 1915x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-2578 + 1947x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-2674 + 1979x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (13 - 10x + x^2) (-218 - 13x + 61x^2 - 15x^3 + x^4), \\
& (-5+x)^8 (5+x)^{13} (-1618 + 1595x + 737x^2 - 818x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-3806 + 2599x + 605x^2 - 814x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-3966 + 2631x + 605x^2 - 814x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-4222 + 2695x + 605x^2 - 814x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^9 (5+x)^{13} (550 - 333x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)^9 (5+x)^{13} (582 - 333x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)^9 (5+x)^{13} (614 - 333x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)^9 (5+x)^{13} (646 - 333x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)^8 (5+x)^{13} (-3166 + 2311x + 637x^2 - 814x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-3326 + 2343x + 637x^2 - 814x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-58 + 55x - 14x^2 + x^3) (59 + 15x - 11x^2 + x^3), \\
& (-5+x)^9 (5+x)^{13} (422 - 301x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)^9 (5+x)^{13} (454 - 301x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)^9 (5+x)^{13} (486 - 301x - 194x^2 + 124x^3 - 20x^4 + x^5),
\end{aligned}$$

$$\begin{aligned}
& (-7+x)(-5+x)^9(5+x)^{13}(-110+41x+33x^2-13x^3+x^4), \\
& (-5+x)^9(5+x)^{13}(802-397x-190x^2+124x^3-20x^4+x^5), \\
& (-5+x)^8(5+x)^{13}(-4106+2819x+553x^2-810x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8(5+x)^{13}(-4266+2851x+553x^2-810x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8(5+x)^{13}(38-13x+x^2)(17-10x+x^2)(-7-2x+x^2), \\
& (-5+x)^9(5+x)^{13}(610-365x-190x^2+124x^3-20x^4+x^5), \\
& (-5+x)^9(5+x)^{13}(642-365x-190x^2+124x^3-20x^4+x^5), \\
& (-5+x)^9(5+x)^{13}(674-365x-190x^2+124x^3-20x^4+x^5), \\
& (-5+x)^9(5+x)^{13}(706-365x-190x^2+124x^3-20x^4+x^5), \\
& (-5+x)^8(5+x)^{13}(-3466+2531x+585x^2-810x^3+224x^4-25x^5+x^6), \\
& (-5+x)^9(5+x)^{13}(482-333x-190x^2+124x^3-20x^4+x^5), \\
& (-7+x)(-5+x)^8(5+x)^{13}(714-371x-120x^2+98x^3-18x^4+x^5), \\
& (-5+x)^8(5+x)^{13}(-5158+3343x+469x^2-806x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8(5+x)^{13}(-74+59x-14x^2+x^3)(71+11x-11x^2+x^3), \\
& (-5+x)^8(5+x)^{13}(-4358+3023x+501x^2-806x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8(5+x)^{13}(-4518+3055x+501x^2-806x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8(5+x)^{13}(-4614+3087x+501x^2-806x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8(5+x)^{13}(31-12x+x^2)(-154+41x+37x^2-13x^3+x^4), \\
& (-5+x)^8(5+x)^{13}(-3558+2703x+533x^2-806x^3+224x^4-25x^5+x^6), \\
& (-7+x)(-5+x)^8(5+x)^{13}(814-411x-116x^2+98x^3-18x^4+x^5), \\
& (-5+x)^8(5+x)^{13}(-5954+3755x+401x^2-802x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8(5+x)^{13}(-4898+3371x+433x^2-802x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8(5+x)^{13}(-5058+3403x+433x^2-802x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8(5+x)^{13}(-5314+3467x+433x^2-802x^3+224x^4-25x^5+x^6), \\
& (-9+x)(-5+x)^9(5+x)^{13}(-134+47x+25x^2-11x^3+x^4), \\
& (-5+x)^9(5+x)^{13}(1238-557x-178x^2+124x^3-20x^4+x^5), \\
& (-7+x)(-5+x)^9(5+x)^{13}(-154+53x+33x^2-13x^3+x^4), \\
& (-5+x)^9(5+x)^{13}(1110-525x-178x^2+124x^3-20x^4+x^5), \\
& (-5+x)^9(5+x)^{13}(1142-525x-178x^2+124x^3-20x^4+x^5), \\
& (-5+x)^8(5+x)^{13}(-5806+3799x+365x^2-798x^3+224x^4-25x^5+x^6), \\
& (-5+x)^9(5+x)^{13}(950-493x-178x^2+124x^3-20x^4+x^5), \\
& (-5+x)^9(5+x)^{13}(982-493x-178x^2+124x^3-20x^4+x^5), \\
& (-5+x)^8(-3+x)(5+x)^{13}(2462-711x-320x^2+158x^3-22x^4+x^5), \\
& (-5+x)^9(5+x)^{13}(1298-589x-174x^2+124x^3-20x^4+x^5), \\
& (-5+x)^8(5+x)^{13}(-6746+4307x+281x^2-794x^3+224x^4-25x^5+x^6), \\
& (-5+x)^9(5+x)^{13}(1138-557x-174x^2+124x^3-20x^4+x^5), \\
& (-5+x)^9(5+x)^{13}(1170-557x-174x^2+124x^3-20x^4+x^5), \\
& (-5+x)^9(5+x)^{13}(1202-557x-174x^2+124x^3-20x^4+x^5), \\
& (-5+x)^8(-3+x)(5+x)^{13}(2546-751x-316x^2+158x^3-22x^4+x^5), \\
& (-5+x)^8(5+x)^{13}(-6838+4479x+229x^2-790x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8(5+x)^{13}(-6998+4511x+229x^2-790x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8(-3+x)(5+x)^{13}(31-12x+x^2)(78+7x-10x^2+x^3),
\end{aligned}$$

$$\begin{aligned}
& (-5+x)^8 (-3+x) (5+x)^{13} (2726 - 807x - 312x^2 + 158x^3 - 22x^4 + x^5), \\
& (-5+x)^8 (5+x)^{13} (-7538 + 4859x + 161x^2 - 786x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^9 (-3+x) (5+x)^{13} (-578 + 57x + 73x^2 - 17x^3 + x^4), \\
& (-5+x)^9 (5+x)^{13} (1606 - 717x - 162x^2 + 124x^3 - 20x^4 + x^5), \\
& (-7+x) (-5+x)^9 (-3+x) (5+x)^{13} (78 + 3x - 10x^2 + x^3), \\
& (-5+x)^9 (5+x)^{13} (1478 - 685x - 162x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)^9 (-3+x) (5+x)^{13} (-598 + 61x + 73x^2 - 17x^3 + x^4), \\
& (-7+x) (-5+x)^9 (5+x)^{13} (-238 + 73x + 33x^2 - 13x^3 + x^4), \\
& (-5+x)^9 (-3+x) (5+x)^{13} (-566 + 61x + 73x^2 - 17x^3 + x^4), \\
& (-7+x) (-5+x)^8 (5+x)^{13} (1354 - 659x - 88x^2 + 98x^3 - 18x^4 + x^5), \\
& (-5+x)^9 (5+x)^{13} (2134 - 909x - 146x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)^9 (5+x)^{13} (2194 - 941x - 142x^2 + 124x^3 - 20x^4 + x^5) \}
\end{aligned}$$

Length[listmod128]

124

CoefficientList[listmod128 / mu[chisub] // Factor, x]

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{-194, 523, 977, -834, 224, -25, 1}, {-354, 555, 977, -834, 224, -25, 1},
{-1582, 1207, 877, -830, 224, -25, 1}, {-1742, 1239, 877, -830, 224, -25, 1},
{-1838, 1271, 877, -830, 224, -25, 1}, {-270, 759, 909, -830, 224, -25, 1},
{-430, 791, 909, -830, 224, -25, 1}, {-590, 823, 909, -830, 224, -25, 1},
{-526, 823, 909, -830, 224, -25, 1}, {-750, 855, 909, -830, 224, -25, 1},
{-686, 855, 909, -830, 224, -25, 1}, {-846, 887, 909, -830, 224, -25, 1},
{-942, 919, 909, -830, 224, -25, 1}, {50, 535, 941, -830, 224, -25, 1},
{-1530, 1331, 825, -826, 224, -25, 1}, {-1466, 1331, 825, -826, 224, -25, 1},

```

```

{-1626, 1363, 825, -826, 224, -25, 1}, {-1786, 1395, 825, -826, 224, -25, 1},
{-1882, 1427, 825, -826, 224, -25, 1}, {-2042, 1459, 825, -826, 224, -25, 1},
{-410, 947, 857, -826, 224, -25, 1}, {-570, 979, 857, -826, 224, -25, 1},
{-730, 1011, 857, -826, 224, -25, 1}, {-890, 1043, 857, -826, 224, -25, 1},
{-826, 1043, 857, -826, 224, -25, 1}, {-1050, 1075, 857, -826, 224, -25, 1},
{-986, 1075, 857, -826, 224, -25, 1}, {70, 691, 889, -826, 224, -25, 1},
{-2614, 1887, 741, -822, 224, -25, 1}, {-2774, 1919, 741, -822, 224, -25, 1},
{-3030, 1983, 741, -822, 224, -25, 1}, {-1718, 1535, 773, -822, 224, -25, 1},
{-1878, 1567, 773, -822, 224, -25, 1}, {-2038, 1599, 773, -822, 224, -25, 1},
{-1974, 1599, 773, -822, 224, -25, 1}, {-2134, 1631, 773, -822, 224, -25, 1},
{-2294, 1663, 773, -822, 224, -25, 1}, {-918, 1215, 805, -822, 224, -25, 1},
{-1078, 1247, 805, -822, 224, -25, 1}, {-3314, 2267, 673, -818, 224, -25, 1},
{-3474, 2299, 673, -818, 224, -25, 1}, {-2258, 1883, 705, -818, 224, -25, 1},
{-2418, 1915, 705, -818, 224, -25, 1}, {-2578, 1947, 705, -818, 224, -25, 1},
{-2674, 1979, 705, -818, 224, -25, 1}, {-2834, 2011, 705, -818, 224, -25, 1},
{-1618, 1595, 737, -818, 224, -25, 1}, {-3806, 2599, 605, -814, 224, -25, 1},
{-3966, 2631, 605, -814, 224, -25, 1}, {-4222, 2695, 605, -814, 224, -25, 1},
{-2750, 2215, 637, -814, 224, -25, 1}, {-2910, 2247, 637, -814, 224, -25, 1},
{-3070, 2279, 637, -814, 224, -25, 1}, {-3230, 2311, 637, -814, 224, -25, 1},
{-3166, 2311, 637, -814, 224, -25, 1}, {-3326, 2343, 637, -814, 224, -25, 1},
{-3422, 2375, 637, -814, 224, -25, 1}, {-2110, 1927, 669, -814, 224, -25, 1},
{-2270, 1959, 669, -814, 224, -25, 1}, {-2430, 1991, 669, -814, 224, -25, 1},
{-3850, 2755, 553, -810, 224, -25, 1}, {-4010, 2787, 553, -810, 224, -25, 1},
{-4106, 2819, 553, -810, 224, -25, 1}, {-4266, 2851, 553, -810, 224, -25, 1},
{-4522, 2915, 553, -810, 224, -25, 1}, {-3050, 2435, 585, -810, 224, -25, 1},
{-3210, 2467, 585, -810, 224, -25, 1}, {-3370, 2499, 585, -810, 224, -25, 1},
{-3530, 2531, 585, -810, 224, -25, 1}, {-3466, 2531, 585, -810, 224, -25, 1},
{-2410, 2147, 617, -810, 224, -25, 1}, {-4998, 3311, 469, -806, 224, -25, 1},
{-5158, 3343, 469, -806, 224, -25, 1}, {-5254, 3375, 469, -806, 224, -25, 1},
{-4358, 3023, 501, -806, 224, -25, 1}, {-4518, 3055, 501, -806, 224, -25, 1},
{-4614, 3087, 501, -806, 224, -25, 1}, {-4774, 3119, 501, -806, 224, -25, 1},
{-3558, 2703, 533, -806, 224, -25, 1}, {-5698, 3691, 401, -802, 224, -25, 1},
{-5954, 3755, 401, -802, 224, -25, 1}, {-4898, 3371, 433, -802, 224, -25, 1},
{-5058, 3403, 433, -802, 224, -25, 1}, {-5314, 3467, 433, -802, 224, -25, 1},
{-6030, 3991, 333, -798, 224, -25, 1}, {-6190, 4023, 333, -798, 224, -25, 1},
{-6446, 4087, 333, -798, 224, -25, 1}, {-5390, 3703, 365, -798, 224, -25, 1},
{-5550, 3735, 365, -798, 224, -25, 1}, {-5710, 3767, 365, -798, 224, -25, 1},
{-5806, 3799, 365, -798, 224, -25, 1}, {-4750, 3415, 397, -798, 224, -25, 1},
{-4910, 3447, 397, -798, 224, -25, 1}, {-7386, 4595, 249, -794, 224, -25, 1},
{-6490, 4243, 281, -794, 224, -25, 1}, {-6746, 4307, 281, -794, 224, -25, 1},
{-5690, 3923, 313, -794, 224, -25, 1}, {-5850, 3955, 313, -794, 224, -25, 1},
{-6010, 3987, 313, -794, 224, -25, 1}, {-7638, 4799, 197, -790, 224, -25, 1},
{-6838, 4479, 229, -790, 224, -25, 1}, {-6998, 4511, 229, -790, 224, -25, 1},
{-7254, 4575, 229, -790, 224, -25, 1}, {-8178, 5147, 129, -786, 224, -25, 1},
{-7538, 4859, 161, -786, 224, -25, 1}, {-8670, 5479, 61, -782, 224, -25, 1},
{-8030, 5191, 93, -782, 224, -25, 1}, {-8190, 5223, 93, -782, 224, -25, 1},
{-7390, 4903, 125, -782, 224, -25, 1}, {-8970, 5699, 9, -778, 224, -25, 1},

```

```
{-8330, 5411, 41, -778, 224, -25, 1}, {-8490, 5443, 41, -778, 224, -25, 1},
{-9478, 5967, -43, -774, 224, -25, 1}, {-10670, 6679, -179, -766, 224, -25, 1},
{-10970, 6899, -231, -762, 224, -25, 1}};
```

```
Asub // MatrixForm
```

```
(-554 387 1065 -842 224 -25 1)
(-390 495 1013 -838 224 -25 1)
(-550 527 1013 -838 224 -25 1)
(-806 591 1013 -838 224 -25 1)
(-994 843 945 -834 224 -25 1)
(-1090 875 945 -834 224 -25 1)
(-1346 939 945 -834 224 -25 1)
(-98 491 977 -834 224 -25 1)
(-34 491 977 -834 224 -25 1)
(-194 523 977 -834 224 -25 1)
(-354 555 977 -834 224 -25 1)
(-1582 1207 877 -830 224 -25 1)
(-1742 1239 877 -830 224 -25 1)
(-1838 1271 877 -830 224 -25 1)
(-270 759 909 -830 224 -25 1)
(-430 791 909 -830 224 -25 1)
(-590 823 909 -830 224 -25 1)
(-526 823 909 -830 224 -25 1)
(-750 855 909 -830 224 -25 1)
(-686 855 909 -830 224 -25 1)
(-846 887 909 -830 224 -25 1)
(-942 919 909 -830 224 -25 1)
(50 535 941 -830 224 -25 1)
(-1530 1331 825 -826 224 -25 1)
(-1466 1331 825 -826 224 -25 1)
(-1626 1363 825 -826 224 -25 1)
(-1786 1395 825 -826 224 -25 1)
(-1882 1427 825 -826 224 -25 1)
(-2042 1459 825 -826 224 -25 1)
(-410 947 857 -826 224 -25 1)
(-570 979 857 -826 224 -25 1)
(-730 1011 857 -826 224 -25 1)
(-890 1043 857 -826 224 -25 1)
(-826 1043 857 -826 224 -25 1)
(-1050 1075 857 -826 224 -25 1)
(-986 1075 857 -826 224 -25 1)
(70 691 889 -826 224 -25 1)
(-2614 1887 741 -822 224 -25 1)
(-2774 1919 741 -822 224 -25 1)
(-3030 1983 741 -822 224 -25 1)
(-1718 1535 773 -822 224 -25 1)
(-1878 1567 773 -822 224 -25 1)
(-2038 1599 773 -822 224 -25 1)
(-1974 1599 773 -822 224 -25 1)
(-2134 1631 773 -822 224 -25 1)
(-2294 1663 773 -822 224 -25 1)
(-918 1215 805 -822 224 -25 1)
(-1078 1247 805 -822 224 -25 1)
(-3314 2267 673 -818 224 -25 1)
(-2474 2200 673 -818 224 -25 1)
```

-3414	2299	815	-818	224	-25	1
-2258	1883	705	-818	224	-25	1
-2418	1915	705	-818	224	-25	1
-2578	1947	705	-818	224	-25	1
-2674	1979	705	-818	224	-25	1
-2834	2011	705	-818	224	-25	1
-1618	1595	737	-818	224	-25	1
-3806	2599	605	-814	224	-25	1
-3966	2631	605	-814	224	-25	1
-4222	2695	605	-814	224	-25	1
-2750	2215	637	-814	224	-25	1
-2910	2247	637	-814	224	-25	1
-3070	2279	637	-814	224	-25	1
-3230	2311	637	-814	224	-25	1
-3166	2311	637	-814	224	-25	1
-3326	2343	637	-814	224	-25	1
-3422	2375	637	-814	224	-25	1
-2110	1927	669	-814	224	-25	1
-2270	1959	669	-814	224	-25	1
-2430	1991	669	-814	224	-25	1
-3850	2755	553	-810	224	-25	1
-4010	2787	553	-810	224	-25	1
-4106	2819	553	-810	224	-25	1
-4266	2851	553	-810	224	-25	1
-4522	2915	553	-810	224	-25	1
-3050	2435	585	-810	224	-25	1
-3210	2467	585	-810	224	-25	1
-3370	2499	585	-810	224	-25	1
-3530	2531	585	-810	224	-25	1
-3466	2531	585	-810	224	-25	1
-2410	2147	617	-810	224	-25	1
-4998	3311	469	-806	224	-25	1
-5158	3343	469	-806	224	-25	1
-5254	3375	469	-806	224	-25	1
-4358	3023	501	-806	224	-25	1
-4518	3055	501	-806	224	-25	1
-4614	3087	501	-806	224	-25	1
-4774	3119	501	-806	224	-25	1
-3558	2703	533	-806	224	-25	1
-5698	3691	401	-802	224	-25	1
-5954	3755	401	-802	224	-25	1
-4898	3371	433	-802	224	-25	1
-5058	3403	433	-802	224	-25	1
-5314	3467	433	-802	224	-25	1
-6030	3991	333	-798	224	-25	1
-6190	4023	333	-798	224	-25	1
-6446	4087	333	-798	224	-25	1
-5390	3703	365	-798	224	-25	1
-5550	3735	365	-798	224	-25	1
-5710	3767	365	-798	224	-25	1
-5806	3799	365	-798	224	-25	1
-4750	3415	397	-798	224	-25	1
-4910	3447	397	-798	224	-25	1
-7386	4595	249	-794	224	-25	1
-6490	4243	281	-794	224	-25	1

-6746	4307	281	-794	224	-25	1
-5690	3923	313	-794	224	-25	1
-5850	3955	313	-794	224	-25	1
-6010	3987	313	-794	224	-25	1
-7638	4799	197	-790	224	-25	1
-6838	4479	229	-790	224	-25	1
-6998	4511	229	-790	224	-25	1
-7254	4575	229	-790	224	-25	1
-8178	5147	129	-786	224	-25	1
-7538	4859	161	-786	224	-25	1
-8670	5479	61	-782	224	-25	1
-8030	5191	93	-782	224	-25	1
-8190	5223	93	-782	224	-25	1
-7390	4903	125	-782	224	-25	1
-8970	5699	9	-778	224	-25	1
-8330	5411	41	-778	224	-25	1
-8490	5443	41	-778	224	-25	1
-9478	5967	-43	-774	224	-25	1
-10670	6679	-179	-766	224	-25	1
-10970	6899	-231	-762	224	-25	1

```
gsub = CoefficientList[D[chisub, x] / mu[chisub] // Factor, x]
```

```
{-31400, 22692, 27148, -23400, 6272, -700, 28}
```

```

FindInstance[n[1] ≥ 0 && n[2] ≥ 0 && n[3] ≥ 0 && n[4] ≥ 0 && n[5] ≥ 0 && n[6] ≥ 0 &&
  n[7] ≥ 0 && n[8] ≥ 0 && n[9] ≥ 0 && n[10] ≥ 0 && n[11] ≥ 0 && n[12] ≥ 0 && n[13] ≥ 0 &&
  n[14] ≥ 0 && n[15] ≥ 0 && n[16] ≥ 0 && n[17] ≥ 0 && n[18] ≥ 0 && n[19] ≥ 0 && n[20] ≥ 0 &&
  n[21] ≥ 0 && n[22] ≥ 0 && n[23] ≥ 0 && n[24] ≥ 0 && n[25] ≥ 0 && n[26] ≥ 0 &&
  n[27] ≥ 0 && n[28] ≥ 0 && n[29] ≥ 0 && n[30] ≥ 0 && n[31] ≥ 0 && n[32] ≥ 0 &&
  n[33] ≥ 0 && n[34] ≥ 0 && n[35] ≥ 0 && n[36] ≥ 0 && n[37] ≥ 0 && n[38] ≥ 0 &&
  n[39] ≥ 0 && n[40] ≥ 0 && n[41] ≥ 0 && n[42] ≥ 0 && n[43] ≥ 0 && n[44] ≥ 0 &&
  n[45] ≥ 0 && n[46] ≥ 0 && n[47] ≥ 0 && n[48] ≥ 0 && n[49] ≥ 0 && n[50] ≥ 0 &&
  n[51] ≥ 0 && n[52] ≥ 0 && n[53] ≥ 0 && n[54] ≥ 0 && n[55] ≥ 0 && n[56] ≥ 0 &&
  n[57] ≥ 0 && n[58] ≥ 0 && n[59] ≥ 0 && n[60] ≥ 0 && n[61] ≥ 0 && n[62] ≥ 0 &&
  n[63] ≥ 0 && n[64] ≥ 0 && n[65] ≥ 0 && n[66] ≥ 0 && n[67] ≥ 0 && n[68] ≥ 0 &&
  n[69] ≥ 0 && n[70] ≥ 0 && n[71] ≥ 0 && n[72] ≥ 0 && n[73] ≥ 0 && n[74] ≥ 0 &&
  n[75] ≥ 0 && n[76] ≥ 0 && n[77] ≥ 0 && n[78] ≥ 0 && n[79] ≥ 0 && n[80] ≥ 0 &&
  n[81] ≥ 0 && n[82] ≥ 0 && n[83] ≥ 0 && n[84] ≥ 0 && n[85] ≥ 0 && n[86] ≥ 0 &&
  n[87] ≥ 0 && n[88] ≥ 0 && n[89] ≥ 0 && n[90] ≥ 0 && n[91] ≥ 0 && n[92] ≥ 0 &&
  n[93] ≥ 0 && n[94] ≥ 0 && n[95] ≥ 0 && n[96] ≥ 0 && n[97] ≥ 0 && n[98] ≥ 0 &&
  n[99] ≥ 0 && n[100] ≥ 0 && n[101] ≥ 0 && n[102] ≥ 0 && n[103] ≥ 0 && n[104] ≥ 0 &&
  n[105] ≥ 0 && n[106] ≥ 0 && n[107] ≥ 0 && n[108] ≥ 0 && n[109] ≥ 0 && n[110] ≥ 0 &&
  n[111] ≥ 0 && n[112] ≥ 0 && n[113] ≥ 0 && n[114] ≥ 0 && n[115] ≥ 0 && n[116] ≥ 0 &&
  n[117] ≥ 0 && n[118] ≥ 0 && n[119] ≥ 0 && n[120] ≥ 0 && n[121] ≥ 0 && n[122] ≥ 0 &&
  n[123] ≥ 0 && n[124] ≥ 0 && Array[n, 124].Asub == gsub, Array[n, 124], Integers]

{{n[1] → 10, n[2] → 0, n[3] → 4, n[4] → 2, n[5] → 0, n[6] → 0, n[7] → 2, n[8] → 0,
  n[9] → 0, n[10] → 0, n[11] → 0, n[12] → 0, n[13] → 1, n[14] → 7, n[15] → 0,
  n[16] → 0, n[17] → 0, n[18] → 0, n[19] → 0, n[20] → 0, n[21] → 0, n[22] → 0,
  n[23] → 0, n[24] → 0, n[25] → 0, n[26] → 0, n[27] → 0, n[28] → 0, n[29] → 0,
  n[30] → 0, n[31] → 0, n[32] → 0, n[33] → 0, n[34] → 0, n[35] → 0, n[36] → 0,
  n[37] → 0, n[38] → 0, n[39] → 0, n[40] → 1, n[41] → 1, n[42] → 0, n[43] → 0,
  n[44] → 0, n[45] → 0, n[46] → 0, n[47] → 0, n[48] → 0, n[49] → 0, n[50] → 0,
  n[51] → 0, n[52] → 0, n[53] → 0, n[54] → 0, n[55] → 0, n[56] → 0, n[57] → 0,
  n[58] → 0, n[59] → 0, n[60] → 0, n[61] → 0, n[62] → 0, n[63] → 0, n[64] → 0,
  n[65] → 0, n[66] → 0, n[67] → 0, n[68] → 0, n[69] → 0, n[70] → 0, n[71] → 0,
  n[72] → 0, n[73] → 0, n[74] → 0, n[75] → 0, n[76] → 0, n[77] → 0, n[78] → 0,
  n[79] → 0, n[80] → 0, n[81] → 0, n[82] → 0, n[83] → 0, n[84] → 0, n[85] → 0,
  n[86] → 0, n[87] → 0, n[88] → 0, n[89] → 0, n[90] → 0, n[91] → 0, n[92] → 0,
  n[93] → 0, n[94] → 0, n[95] → 0, n[96] → 0, n[97] → 0, n[98] → 0, n[99] → 0,
  n[100] → 0, n[101] → 0, n[102] → 0, n[103] → 0, n[104] → 0, n[105] → 0, n[106] → 0,
  n[107] → 0, n[108] → 0, n[109] → 0, n[110] → 0, n[111] → 0, n[112] → 0,
  n[113] → 0, n[114] → 0, n[115] → 0, n[116] → 0, n[117] → 0, n[118] → 0,
  n[119] → 0, n[120] → 0, n[121] → 0, n[122] → 0, n[123] → 0, n[124] → 0}}

```

Array[c, 7].Transpose[Asub]

```

{-554 c[1] + 387 c[2] + 1065 c[3] - 842 c[4] + 224 c[5] - 25 c[6] + c[7],
 -390 c[1] + 495 c[2] + 1013 c[3] - 838 c[4] + 224 c[5] - 25 c[6] + c[7],
 -550 c[1] + 527 c[2] + 1013 c[3] - 838 c[4] + 224 c[5] - 25 c[6] + c[7],
 -806 c[1] + 591 c[2] + 1013 c[3] - 838 c[4] + 224 c[5] - 25 c[6] + c[7],
 -994 c[1] + 843 c[2] + 945 c[3] - 834 c[4] + 224 c[5] - 25 c[6] + c[7],
 -1090 c[1] + 875 c[2] + 945 c[3] - 834 c[4] + 224 c[5] - 25 c[6] + c[7],

```


$-1346\,c[1] + 939\,c[2] + 945\,c[3] - 834\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-98\,c[1] + 491\,c[2] + 977\,c[3] - 834\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-34\,c[1] + 491\,c[2] + 977\,c[3] - 834\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-194\,c[1] + 523\,c[2] + 977\,c[3] - 834\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-354\,c[1] + 555\,c[2] + 977\,c[3] - 834\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-1582\,c[1] + 1207\,c[2] + 877\,c[3] - 830\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-1742\,c[1] + 1239\,c[2] + 877\,c[3] - 830\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-1838\,c[1] + 1271\,c[2] + 877\,c[3] - 830\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-270\,c[1] + 759\,c[2] + 909\,c[3] - 830\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-430\,c[1] + 791\,c[2] + 909\,c[3] - 830\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-590\,c[1] + 823\,c[2] + 909\,c[3] - 830\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-526\,c[1] + 823\,c[2] + 909\,c[3] - 830\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-750\,c[1] + 855\,c[2] + 909\,c[3] - 830\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-686\,c[1] + 855\,c[2] + 909\,c[3] - 830\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-846\,c[1] + 887\,c[2] + 909\,c[3] - 830\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-942\,c[1] + 919\,c[2] + 909\,c[3] - 830\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $50\,c[1] + 535\,c[2] + 941\,c[3] - 830\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-1530\,c[1] + 1331\,c[2] + 825\,c[3] - 826\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-1466\,c[1] + 1331\,c[2] + 825\,c[3] - 826\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-1626\,c[1] + 1363\,c[2] + 825\,c[3] - 826\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-1786\,c[1] + 1395\,c[2] + 825\,c[3] - 826\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-1882\,c[1] + 1427\,c[2] + 825\,c[3] - 826\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-2042\,c[1] + 1459\,c[2] + 825\,c[3] - 826\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-410\,c[1] + 947\,c[2] + 857\,c[3] - 826\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-570\,c[1] + 979\,c[2] + 857\,c[3] - 826\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-730\,c[1] + 1011\,c[2] + 857\,c[3] - 826\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-890\,c[1] + 1043\,c[2] + 857\,c[3] - 826\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-826\,c[1] + 1043\,c[2] + 857\,c[3] - 826\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-1050\,c[1] + 1075\,c[2] + 857\,c[3] - 826\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-986\,c[1] + 1075\,c[2] + 857\,c[3] - 826\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $70\,c[1] + 691\,c[2] + 889\,c[3] - 826\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-2614\,c[1] + 1887\,c[2] + 741\,c[3] - 822\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-2774\,c[1] + 1919\,c[2] + 741\,c[3] - 822\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-3030\,c[1] + 1983\,c[2] + 741\,c[3] - 822\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-1718\,c[1] + 1535\,c[2] + 773\,c[3] - 822\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-1878\,c[1] + 1567\,c[2] + 773\,c[3] - 822\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-2038\,c[1] + 1599\,c[2] + 773\,c[3] - 822\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-1974\,c[1] + 1599\,c[2] + 773\,c[3] - 822\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-2134\,c[1] + 1631\,c[2] + 773\,c[3] - 822\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-2294\,c[1] + 1663\,c[2] + 773\,c[3] - 822\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-918\,c[1] + 1215\,c[2] + 805\,c[3] - 822\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-1078\,c[1] + 1247\,c[2] + 805\,c[3] - 822\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-3314\,c[1] + 2267\,c[2] + 673\,c[3] - 818\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-3474\,c[1] + 2299\,c[2] + 673\,c[3] - 818\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-2258\,c[1] + 1883\,c[2] + 705\,c[3] - 818\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-2418\,c[1] + 1915\,c[2] + 705\,c[3] - 818\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$
 $-2578\,c[1] + 1947\,c[2] + 705\,c[3] - 818\,c[4] + 224\,c[5] - 25\,c[6] + c[7],$

$-2674 c[1] + 1979 c[2] + 705 c[3] - 818 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-2834 c[1] + 2011 c[2] + 705 c[3] - 818 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-1618 c[1] + 1595 c[2] + 737 c[3] - 818 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-3806 c[1] + 2599 c[2] + 605 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-3966 c[1] + 2631 c[2] + 605 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-4222 c[1] + 2695 c[2] + 605 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-2750 c[1] + 2215 c[2] + 637 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-2910 c[1] + 2247 c[2] + 637 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-3070 c[1] + 2279 c[2] + 637 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-3230 c[1] + 2311 c[2] + 637 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-3166 c[1] + 2311 c[2] + 637 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-3326 c[1] + 2343 c[2] + 637 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-3422 c[1] + 2375 c[2] + 637 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-2110 c[1] + 1927 c[2] + 669 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-2270 c[1] + 1959 c[2] + 669 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-2430 c[1] + 1991 c[2] + 669 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-3850 c[1] + 2755 c[2] + 553 c[3] - 810 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-4010 c[1] + 2787 c[2] + 553 c[3] - 810 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-4106 c[1] + 2819 c[2] + 553 c[3] - 810 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-4266 c[1] + 2851 c[2] + 553 c[3] - 810 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-4522 c[1] + 2915 c[2] + 553 c[3] - 810 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-3050 c[1] + 2435 c[2] + 585 c[3] - 810 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-3210 c[1] + 2467 c[2] + 585 c[3] - 810 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-3370 c[1] + 2499 c[2] + 585 c[3] - 810 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-3530 c[1] + 2531 c[2] + 585 c[3] - 810 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-3466 c[1] + 2531 c[2] + 585 c[3] - 810 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-2410 c[1] + 2147 c[2] + 617 c[3] - 810 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-4998 c[1] + 3311 c[2] + 469 c[3] - 806 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-5158 c[1] + 3343 c[2] + 469 c[3] - 806 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-5254 c[1] + 3375 c[2] + 469 c[3] - 806 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-4358 c[1] + 3023 c[2] + 501 c[3] - 806 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-4518 c[1] + 3055 c[2] + 501 c[3] - 806 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-4614 c[1] + 3087 c[2] + 501 c[3] - 806 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-4774 c[1] + 3119 c[2] + 501 c[3] - 806 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-3558 c[1] + 2703 c[2] + 533 c[3] - 806 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-5698 c[1] + 3691 c[2] + 401 c[3] - 802 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-5954 c[1] + 3755 c[2] + 401 c[3] - 802 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-4898 c[1] + 3371 c[2] + 433 c[3] - 802 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-5058 c[1] + 3403 c[2] + 433 c[3] - 802 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-5314 c[1] + 3467 c[2] + 433 c[3] - 802 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-6030 c[1] + 3991 c[2] + 333 c[3] - 798 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-6190 c[1] + 4023 c[2] + 333 c[3] - 798 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-6446 c[1] + 4087 c[2] + 333 c[3] - 798 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-5390 c[1] + 3703 c[2] + 365 c[3] - 798 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-5550 c[1] + 3735 c[2] + 365 c[3] - 798 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-5710 c[1] + 3767 c[2] + 365 c[3] - 798 c[4] + 224 c[5] - 25 c[6] + c[7],$
 $-5806 c[1] + 3799 c[2] + 365 c[3] - 798 c[4] + 224 c[5] - 25 c[6] + c[7],$

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-4750 c[1] + 3415 c[2] + 397 c[3] - 798 c[4] + 224 c[5] - 25 c[6] + c[7],
-4910 c[1] + 3447 c[2] + 397 c[3] - 798 c[4] + 224 c[5] - 25 c[6] + c[7],
-7386 c[1] + 4595 c[2] + 249 c[3] - 794 c[4] + 224 c[5] - 25 c[6] + c[7],
-6490 c[1] + 4243 c[2] + 281 c[3] - 794 c[4] + 224 c[5] - 25 c[6] + c[7],
-6746 c[1] + 4307 c[2] + 281 c[3] - 794 c[4] + 224 c[5] - 25 c[6] + c[7],
-5690 c[1] + 3923 c[2] + 313 c[3] - 794 c[4] + 224 c[5] - 25 c[6] + c[7],
-5850 c[1] + 3955 c[2] + 313 c[3] - 794 c[4] + 224 c[5] - 25 c[6] + c[7],
-6010 c[1] + 3987 c[2] + 313 c[3] - 794 c[4] + 224 c[5] - 25 c[6] + c[7],
-7638 c[1] + 4799 c[2] + 197 c[3] - 790 c[4] + 224 c[5] - 25 c[6] + c[7],
-6838 c[1] + 4479 c[2] + 229 c[3] - 790 c[4] + 224 c[5] - 25 c[6] + c[7],
-6998 c[1] + 4511 c[2] + 229 c[3] - 790 c[4] + 224 c[5] - 25 c[6] + c[7],
-7254 c[1] + 4575 c[2] + 229 c[3] - 790 c[4] + 224 c[5] - 25 c[6] + c[7],
-8178 c[1] + 5147 c[2] + 129 c[3] - 786 c[4] + 224 c[5] - 25 c[6] + c[7],
-7538 c[1] + 4859 c[2] + 161 c[3] - 786 c[4] + 224 c[5] - 25 c[6] + c[7],
-8670 c[1] + 5479 c[2] + 61 c[3] - 782 c[4] + 224 c[5] - 25 c[6] + c[7],
-8030 c[1] + 5191 c[2] + 93 c[3] - 782 c[4] + 224 c[5] - 25 c[6] + c[7],
-8190 c[1] + 5223 c[2] + 93 c[3] - 782 c[4] + 224 c[5] - 25 c[6] + c[7],
-7390 c[1] + 4903 c[2] + 125 c[3] - 782 c[4] + 224 c[5] - 25 c[6] + c[7],
-8970 c[1] + 5699 c[2] + 9 c[3] - 778 c[4] + 224 c[5] - 25 c[6] + c[7],
-8330 c[1] + 5411 c[2] + 41 c[3] - 778 c[4] + 224 c[5] - 25 c[6] + c[7],
-8490 c[1] + 5443 c[2] + 41 c[3] - 778 c[4] + 224 c[5] - 25 c[6] + c[7],
-9478 c[1] + 5967 c[2] - 43 c[3] - 774 c[4] + 224 c[5] - 25 c[6] + c[7],
-10670 c[1] + 6679 c[2] - 179 c[3] - 766 c[4] + 224 c[5] - 25 c[6] + c[7],
-10970 c[1] + 6899 c[2] - 231 c[3] - 762 c[4] + 224 c[5] - 25 c[6] + c[7] }

```

Array[c, 7].gsub

```
-31400 c[1] + 22692 c[2] + 27148 c[3] - 23400 c[4] + 6272 c[5] - 700 c[6] + 28 c[7]
```

warrantsub = Flatten[Array[c, 7] /. FindInstance[

```

-31400 c[1] + 22692 c[2] + 27148 c[3] - 23400 c[4] + 6272 c[5] - 700 c[6] + 28 c[7] <
0 && -554 c[1] + 387 c[2] + 1065 c[3] - 842 c[4] + 224 c[5] - 25 c[6] + c[7] < 0 &&
-390 c[1] + 495 c[2] + 1013 c[3] - 838 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-550 c[1] + 527 c[2] + 1013 c[3] - 838 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-806 c[1] + 591 c[2] + 1013 c[3] - 838 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-994 c[1] + 843 c[2] + 945 c[3] - 834 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-1090 c[1] + 875 c[2] + 945 c[3] - 834 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-1346 c[1] + 939 c[2] + 945 c[3] - 834 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-98 c[1] + 491 c[2] + 977 c[3] - 834 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-34 c[1] + 491 c[2] + 977 c[3] - 834 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-194 c[1] + 523 c[2] + 977 c[3] - 834 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-354 c[1] + 555 c[2] + 977 c[3] - 834 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-1582 c[1] + 1207 c[2] + 877 c[3] - 830 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-1742 c[1] + 1239 c[2] + 877 c[3] - 830 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-1838 c[1] + 1271 c[2] + 877 c[3] - 830 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-270 c[1] + 759 c[2] + 909 c[3] - 830 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-430 c[1] + 791 c[2] + 909 c[3] - 830 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-590 c[1] + 823 c[2] + 909 c[3] - 830 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&

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-526 c[1] + 823 c[2] + 909 c[3] - 830 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-750 c[1] + 855 c[2] + 909 c[3] - 830 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-686 c[1] + 855 c[2] + 909 c[3] - 830 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-846 c[1] + 887 c[2] + 909 c[3] - 830 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-942 c[1] + 919 c[2] + 909 c[3] - 830 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
50 c[1] + 535 c[2] + 941 c[3] - 830 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-1530 c[1] + 1331 c[2] + 825 c[3] - 826 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-1466 c[1] + 1331 c[2] + 825 c[3] - 826 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-1626 c[1] + 1363 c[2] + 825 c[3] - 826 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-1786 c[1] + 1395 c[2] + 825 c[3] - 826 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-1882 c[1] + 1427 c[2] + 825 c[3] - 826 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-2042 c[1] + 1459 c[2] + 825 c[3] - 826 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-410 c[1] + 947 c[2] + 857 c[3] - 826 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-570 c[1] + 979 c[2] + 857 c[3] - 826 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-730 c[1] + 1011 c[2] + 857 c[3] - 826 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-890 c[1] + 1043 c[2] + 857 c[3] - 826 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-826 c[1] + 1043 c[2] + 857 c[3] - 826 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-1050 c[1] + 1075 c[2] + 857 c[3] - 826 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-986 c[1] + 1075 c[2] + 857 c[3] - 826 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
70 c[1] + 691 c[2] + 889 c[3] - 826 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-2614 c[1] + 1887 c[2] + 741 c[3] - 822 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-2774 c[1] + 1919 c[2] + 741 c[3] - 822 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-3030 c[1] + 1983 c[2] + 741 c[3] - 822 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-1718 c[1] + 1535 c[2] + 773 c[3] - 822 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-1878 c[1] + 1567 c[2] + 773 c[3] - 822 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-2038 c[1] + 1599 c[2] + 773 c[3] - 822 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-1974 c[1] + 1599 c[2] + 773 c[3] - 822 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-2134 c[1] + 1631 c[2] + 773 c[3] - 822 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-2294 c[1] + 1663 c[2] + 773 c[3] - 822 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-918 c[1] + 1215 c[2] + 805 c[3] - 822 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-1078 c[1] + 1247 c[2] + 805 c[3] - 822 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-3314 c[1] + 2267 c[2] + 673 c[3] - 818 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-3474 c[1] + 2299 c[2] + 673 c[3] - 818 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-2258 c[1] + 1883 c[2] + 705 c[3] - 818 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-2418 c[1] + 1915 c[2] + 705 c[3] - 818 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-2578 c[1] + 1947 c[2] + 705 c[3] - 818 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-2674 c[1] + 1979 c[2] + 705 c[3] - 818 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-2834 c[1] + 2011 c[2] + 705 c[3] - 818 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-1618 c[1] + 1595 c[2] + 737 c[3] - 818 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-3806 c[1] + 2599 c[2] + 605 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-3966 c[1] + 2631 c[2] + 605 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-4222 c[1] + 2695 c[2] + 605 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-2750 c[1] + 2215 c[2] + 637 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-2910 c[1] + 2247 c[2] + 637 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-3070 c[1] + 2279 c[2] + 637 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-3230 c[1] + 2311 c[2] + 637 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
-3166 c[1] + 2311 c[2] + 637 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&

$$\begin{aligned}
& -3326 c[1] + 2343 c[2] + 637 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -3422 c[1] + 2375 c[2] + 637 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -2110 c[1] + 1927 c[2] + 669 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -2270 c[1] + 1959 c[2] + 669 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -2430 c[1] + 1991 c[2] + 669 c[3] - 814 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -3850 c[1] + 2755 c[2] + 553 c[3] - 810 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -4010 c[1] + 2787 c[2] + 553 c[3] - 810 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -4106 c[1] + 2819 c[2] + 553 c[3] - 810 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -4266 c[1] + 2851 c[2] + 553 c[3] - 810 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -4522 c[1] + 2915 c[2] + 553 c[3] - 810 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -3050 c[1] + 2435 c[2] + 585 c[3] - 810 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -3210 c[1] + 2467 c[2] + 585 c[3] - 810 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -3370 c[1] + 2499 c[2] + 585 c[3] - 810 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -3530 c[1] + 2531 c[2] + 585 c[3] - 810 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -3466 c[1] + 2531 c[2] + 585 c[3] - 810 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -2410 c[1] + 2147 c[2] + 617 c[3] - 810 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -4998 c[1] + 3311 c[2] + 469 c[3] - 806 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -5158 c[1] + 3343 c[2] + 469 c[3] - 806 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -5254 c[1] + 3375 c[2] + 469 c[3] - 806 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -4358 c[1] + 3023 c[2] + 501 c[3] - 806 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -4518 c[1] + 3055 c[2] + 501 c[3] - 806 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -4614 c[1] + 3087 c[2] + 501 c[3] - 806 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -4774 c[1] + 3119 c[2] + 501 c[3] - 806 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -3558 c[1] + 2703 c[2] + 533 c[3] - 806 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -5698 c[1] + 3691 c[2] + 401 c[3] - 802 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -5954 c[1] + 3755 c[2] + 401 c[3] - 802 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -4898 c[1] + 3371 c[2] + 433 c[3] - 802 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -5058 c[1] + 3403 c[2] + 433 c[3] - 802 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -5314 c[1] + 3467 c[2] + 433 c[3] - 802 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -6030 c[1] + 3991 c[2] + 333 c[3] - 798 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -6190 c[1] + 4023 c[2] + 333 c[3] - 798 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -6446 c[1] + 4087 c[2] + 333 c[3] - 798 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -5390 c[1] + 3703 c[2] + 365 c[3] - 798 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -5550 c[1] + 3735 c[2] + 365 c[3] - 798 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -5710 c[1] + 3767 c[2] + 365 c[3] - 798 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -5806 c[1] + 3799 c[2] + 365 c[3] - 798 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -4750 c[1] + 3415 c[2] + 397 c[3] - 798 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -4910 c[1] + 3447 c[2] + 397 c[3] - 798 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -7386 c[1] + 4595 c[2] + 249 c[3] - 794 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -6490 c[1] + 4243 c[2] + 281 c[3] - 794 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -6746 c[1] + 4307 c[2] + 281 c[3] - 794 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -5690 c[1] + 3923 c[2] + 313 c[3] - 794 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -5850 c[1] + 3955 c[2] + 313 c[3] - 794 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -6010 c[1] + 3987 c[2] + 313 c[3] - 794 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -7638 c[1] + 4799 c[2] + 197 c[3] - 790 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -6838 c[1] + 4479 c[2] + 229 c[3] - 790 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\& \\
& -6998 c[1] + 4511 c[2] + 229 c[3] - 790 c[4] + 224 c[5] - 25 c[6] + c[7] \geq 0 \&\&
\end{aligned}$$

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- 7254 c[1] + 4575 c[2] + 229 c[3] - 790 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
- 8178 c[1] + 5147 c[2] + 129 c[3] - 786 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
- 7538 c[1] + 4859 c[2] + 161 c[3] - 786 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
- 8670 c[1] + 5479 c[2] + 61 c[3] - 782 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
- 8030 c[1] + 5191 c[2] + 93 c[3] - 782 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
- 8190 c[1] + 5223 c[2] + 93 c[3] - 782 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
- 7390 c[1] + 4903 c[2] + 125 c[3] - 782 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
- 8970 c[1] + 5699 c[2] + 9 c[3] - 778 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
- 8330 c[1] + 5411 c[2] + 41 c[3] - 778 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
- 8490 c[1] + 5443 c[2] + 41 c[3] - 778 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
- 9478 c[1] + 5967 c[2] - 43 c[3] - 774 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
- 10 670 c[1] + 6679 c[2] - 179 c[3] - 766 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0 &&
- 10 970 c[1] + 6899 c[2] - 231 c[3] - 762 c[4] + 224 c[5] - 25 c[6] + c[7] ≥ 0,
Array[c, 7], Integers]]

{-344, -1486, -5303, -7130, 0, 0, 0}

GCD[-344, -1486, -5303, -7130, 0, 0, 0]

1

Reverse[warrantsub]

{0, 0, 0, -7130, -5303, -1486, -344}

warrantsub.gsub

-42 556

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warrantsub.Transpose[Asub]

{-28 741, 1591, 9079, 2039, 24 323, 9795, 2755, 69 475, 47 459, 54 947, 62 435,
17 775, 25 263, 10 735, 62 479, 69 967, 77 455, 55 439, 84 943, 62 927, 70 415,
55 887, 115 567, 62 859, 40 843, 48 331, 55 819, 41 291, 48 779, 78 507, 85 995,
93 483, 100 971, 78 955, 108 459, 86 443, 124 107, 26 471, 33 959, 26 919,
71 623, 79 111, 86 599, 64 583, 72 071, 79 559, 102 247, 109 735, 34 675, 42 163,
72 339, 79 827, 87 315, 72 787, 80 275, 110 451, 42 655, 50 143, 43 103, 80 319,
87 807, 95 295, 102 783, 80 767, 88 255, 73 727, 118 431, 125 919, 133 407,
73 211, 80 699, 66 171, 73 659, 66 619, 103 835, 111 323, 118 811, 126 299,
104 283, 141 947, 58 839, 66 327, 51 799, 96 951, 104 439, 89 911, 97 399,
127 575, 67 043, 60 003, 97 667, 105 155, 98 115, 67 535, 75 023, 67 983, 105 647,
113 135, 120 623, 106 095, 143 759, 151 247, 53 387, 98 539, 91 499, 129 163,
136 651, 144 139, 84 167, 114 791, 122 279, 115 239, 84 883, 122 995, 92 863,
130 975, 138 463, 169 087, 116 379, 154 491, 161 979, 140 119, 156 303, 179 819}

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In[ ]:= listmod128 = { (-5 + x)^9 (5 + x)^13 (150 - 141 x - 210 x^2 + 124 x^3 - 20 x^4 + x^5),
(-5 + x)^8 (5 + x)^13 (-686 + 855 x + 909 x^2 - 830 x^3 + 224 x^4 - 25 x^5 + x^6),
(-5 + x)^9 (1 + x) (5 + x)^13 (178 - 351 x + 145 x^2 - 21 x^3 + x^4),
(-5 + x)^8 (5 + x)^13 (-6446 + 4087 x + 333 x^2 - 798 x^3 + 224 x^4 - 25 x^5 + x^6),
(-5 + x)^8 (5 + x)^13 (-942 + 919 x + 909 x^2 - 830 x^3 + 224 x^4 - 25 x^5 + x^6),

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$$\begin{aligned}
& (-5+x)^8 (5+x)^{13} (-826+1043x+857x^2-826x^3+224x^4-25x^5+x^6), \\
& (-5+x)^9 (5+x)^{13} (114-173x-206x^2+124x^3-20x^4+x^5), \\
& (-5+x)^8 (5+x)^{13} (-554+387x+1065x^2-842x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8 (5+x)^{13} (-390+495x+1013x^2-838x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8 (5+x)^{13} (-550+527x+1013x^2-838x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8 (5+x)^{13} (31-12x+x^2) (-26+9x+37x^2-13x^3+x^4), \\
& (-5+x)^8 (5+x)^{13} (-994+843x+945x^2-834x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8 (5+x)^{13} (-1090+875x+945x^2-834x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8 (5+x)^{13} (-1346+939x+945x^2-834x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8 (5+x)^{13} (-98+491x+977x^2-834x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8 (5+x)^{13} (17+35x-13x^2+x^3) (-2+33x-12x^2+x^3), \\
& (-5+x)^8 (5+x)^{13} (-194+523x+977x^2-834x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8 (5+x)^{13} (-354+555x+977x^2-834x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8 (5+x)^{13} (-1582+1207x+877x^2-830x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8 (5+x)^{13} (-1742+1239x+877x^2-830x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8 (5+x)^{13} (-1838+1271x+877x^2-830x^3+224x^4-25x^5+x^6), \\
& (-9+x) (-5+x)^9 (5+x)^{13} (-6+15x+25x^2-11x^3+x^4), \\
& (-5+x)^9 (5+x)^{13} (86-141x-210x^2+124x^3-20x^4+x^5), \\
& (-5+x)^9 (5+x)^{13} (118-141x-210x^2+124x^3-20x^4+x^5), \\
& (-5+x)^8 (5+x)^{13} (-526+823x+909x^2-830x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8 (5+x)^{13} (-846+887x+909x^2-830x^3+224x^4-25x^5+x^6), \\
& (-5+x)^9 (5+x)^{13} (-1-8x+x^2) (10+29x-12x^2+x^3), \\
& (-9+x) (-5+x)^9 (-1+x) (5+x)^{13} (34+15x-10x^2+x^3), \\
& (-5+x)^8 (5+x)^{13} (-1466+1331x+825x^2-826x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8 (5+x)^{13} (-1626+1363x+825x^2-826x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8 (5+x)^{13} (-1786+1395x+825x^2-826x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8 (5+x)^{13} (-1882+1427x+825x^2-826x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8 (5+x)^{13} (-2042+1459x+825x^2-826x^3+224x^4-25x^5+x^6), \\
& (-5+x)^9 (5+x)^{13} (82-173x-206x^2+124x^3-20x^4+x^5), \\
& (-5+x)^9 (5+x)^{13} (146-173x-206x^2+124x^3-20x^4+x^5), \\
& (-5+x)^9 (5+x)^{13} (210-173x-206x^2+124x^3-20x^4+x^5), \\
& (-5+x)^8 (5+x)^{13} (-986+1075x+857x^2-826x^3+224x^4-25x^5+x^6), \\
& (-5+x)^9 (5+x)^{13} (-1-8x+x^2) (14+29x-12x^2+x^3), \\
& (-5+x)^8 (5+x)^{13} (-2614+1887x+741x^2-822x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8 (5+x)^{13} (-2774+1919x+741x^2-822x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8 (5+x)^{13} (-3030+1983x+741x^2-822x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8 (5+x)^{13} (-1718+1535x+773x^2-822x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8 (5+x)^{13} (-1878+1567x+773x^2-822x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8 (5+x)^{13} (-2038+1599x+773x^2-822x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8 (5+x)^{13} (-42+51x-14x^2+x^3) (47+19x-11x^2+x^3), \\
& (-5+x)^8 (5+x)^{13} (-2134+1631x+773x^2-822x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8 (5+x)^{13} (31-12x+x^2) (-74+25x+37x^2-13x^3+x^4),
\end{aligned}$$

$$\begin{aligned}
& (-5+x)^8 (5+x)^{13} (-918 + 1215x + 805x^2 - 822x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-1078 + 1247x + 805x^2 - 822x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-3314 + 2267x + 673x^2 - 818x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-3474 + 2299x + 673x^2 - 818x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-2258 + 1883x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-2418 + 1915x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-2578 + 1947x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-2674 + 1979x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (13 - 10x + x^2) (-218 - 13x + 61x^2 - 15x^3 + x^4), \\
& (-5+x)^8 (5+x)^{13} (-1618 + 1595x + 737x^2 - 818x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-3806 + 2599x + 605x^2 - 814x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-3966 + 2631x + 605x^2 - 814x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-4222 + 2695x + 605x^2 - 814x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^9 (5+x)^{13} (550 - 333x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)^9 (5+x)^{13} (582 - 333x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)^9 (5+x)^{13} (614 - 333x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)^9 (5+x)^{13} (646 - 333x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)^8 (5+x)^{13} (-3166 + 2311x + 637x^2 - 814x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-3326 + 2343x + 637x^2 - 814x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-58 + 55x - 14x^2 + x^3) (59 + 15x - 11x^2 + x^3), \\
& (-5+x)^9 (5+x)^{13} (422 - 301x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)^9 (5+x)^{13} (454 - 301x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)^9 (5+x)^{13} (486 - 301x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-7+x) (-5+x)^9 (5+x)^{13} (-110 + 41x + 33x^2 - 13x^3 + x^4), \\
& (-5+x)^9 (5+x)^{13} (802 - 397x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)^8 (5+x)^{13} (-4106 + 2819x + 553x^2 - 810x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-4266 + 2851x + 553x^2 - 810x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (38 - 13x + x^2) (17 - 10x + x^2) (-7 - 2x + x^2), \\
& (-5+x)^9 (5+x)^{13} (610 - 365x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)^9 (5+x)^{13} (642 - 365x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)^9 (5+x)^{13} (674 - 365x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)^9 (5+x)^{13} (706 - 365x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5+x)^8 (5+x)^{13} (-3466 + 2531x + 585x^2 - 810x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^9 (5+x)^{13} (482 - 333x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& (-7+x) (-5+x)^8 (5+x)^{13} (714 - 371x - 120x^2 + 98x^3 - 18x^4 + x^5), \\
& (-5+x)^8 (5+x)^{13} (-5158 + 3343x + 469x^2 - 806x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-74 + 59x - 14x^2 + x^3) (71 + 11x - 11x^2 + x^3), \\
& (-5+x)^8 (5+x)^{13} (-4358 + 3023x + 501x^2 - 806x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-4518 + 3055x + 501x^2 - 806x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (-4614 + 3087x + 501x^2 - 806x^3 + 224x^4 - 25x^5 + x^6), \\
& (-5+x)^8 (5+x)^{13} (31 - 12x + x^2) (-154 + 41x + 37x^2 - 13x^3 + x^4), \\
& (-5+x)^8 (5+x)^{13} (-3558 + 2703x + 533x^2 - 806x^3 + 224x^4 - 25x^5 + x^6),
\end{aligned}$$

$$\begin{aligned}
& (-7+x)(-5+x)^8(5+x)^{13}(814-411x-116x^2+98x^3-18x^4+x^5), \\
& (-5+x)^8(5+x)^{13}(-5954+3755x+401x^2-802x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8(5+x)^{13}(-4898+3371x+433x^2-802x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8(5+x)^{13}(-5058+3403x+433x^2-802x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8(5+x)^{13}(-5314+3467x+433x^2-802x^3+224x^4-25x^5+x^6), \\
& (-9+x)(-5+x)^9(5+x)^{13}(-134+47x+25x^2-11x^3+x^4), \\
& (-5+x)^9(5+x)^{13}(1238-557x-178x^2+124x^3-20x^4+x^5), \\
& (-7+x)(-5+x)^9(5+x)^{13}(-154+53x+33x^2-13x^3+x^4), \\
& (-5+x)^9(5+x)^{13}(1110-525x-178x^2+124x^3-20x^4+x^5), \\
& (-5+x)^9(5+x)^{13}(1142-525x-178x^2+124x^3-20x^4+x^5), \\
& (-5+x)^8(5+x)^{13}(-5806+3799x+365x^2-798x^3+224x^4-25x^5+x^6), \\
& (-5+x)^9(5+x)^{13}(950-493x-178x^2+124x^3-20x^4+x^5), \\
& (-5+x)^9(5+x)^{13}(982-493x-178x^2+124x^3-20x^4+x^5), \\
& (-5+x)^8(-3+x)(5+x)^{13}(2462-711x-320x^2+158x^3-22x^4+x^5), \\
& (-5+x)^9(5+x)^{13}(1298-589x-174x^2+124x^3-20x^4+x^5), \\
& (-5+x)^8(5+x)^{13}(-6746+4307x+281x^2-794x^3+224x^4-25x^5+x^6), \\
& (-5+x)^9(5+x)^{13}(1138-557x-174x^2+124x^3-20x^4+x^5), \\
& (-5+x)^9(5+x)^{13}(1170-557x-174x^2+124x^3-20x^4+x^5), \\
& (-5+x)^9(5+x)^{13}(1202-557x-174x^2+124x^3-20x^4+x^5), \\
& (-5+x)^8(-3+x)(5+x)^{13}(2546-751x-316x^2+158x^3-22x^4+x^5), \\
& (-5+x)^8(5+x)^{13}(-6838+4479x+229x^2-790x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8(5+x)^{13}(-6998+4511x+229x^2-790x^3+224x^4-25x^5+x^6), \\
& (-5+x)^8(-3+x)(5+x)^{13}(31-12x+x^2)(78+7x-10x^2+x^3), \\
& (-5+x)^8(-3+x)(5+x)^{13}(2726-807x-312x^2+158x^3-22x^4+x^5), \\
& (-5+x)^8(5+x)^{13}(-7538+4859x+161x^2-786x^3+224x^4-25x^5+x^6), \\
& (-5+x)^9(-3+x)(5+x)^{13}(-578+57x+73x^2-17x^3+x^4), \\
& (-5+x)^9(5+x)^{13}(1606-717x-162x^2+124x^3-20x^4+x^5), \\
& (-7+x)(-5+x)^9(-3+x)(5+x)^{13}(78+3x-10x^2+x^3), \\
& (-5+x)^9(5+x)^{13}(1478-685x-162x^2+124x^3-20x^4+x^5), \\
& (-5+x)^9(-3+x)(5+x)^{13}(-598+61x+73x^2-17x^3+x^4), \\
& (-7+x)(-5+x)^9(5+x)^{13}(-238+73x+33x^2-13x^3+x^4), \\
& (-5+x)^9(-3+x)(5+x)^{13}(-566+61x+73x^2-17x^3+x^4), \\
& (-7+x)(-5+x)^8(5+x)^{13}(1354-659x-88x^2+98x^3-18x^4+x^5), \\
& (-5+x)^9(5+x)^{13}(2134-909x-146x^2+124x^3-20x^4+x^5), \\
& (-5+x)^9(5+x)^{13}(2194-941x-142x^2+124x^3-20x^4+x^5)\};
\end{aligned}$$

In[*]:= Length[listmod128]

Out[*]= 124

In[*]:= listmod128[[8]]

Out[*]= $(-5+x)^8(5+x)^{13}(-554+387x+1065x^2-842x^3+224x^4-25x^5+x^6)$

In[*]:= listmod128 = listmod128 / mu[chisub] // Factor

Out[*]= $\{(-5+x)(150-141x-210x^2+124x^3-20x^4+x^5),$
 $-686+855x+909x^2-830x^3+224x^4-25x^5+x^6,$

$$\begin{aligned}
& (-5+x)(1+x)(178-351x+145x^2-21x^3+x^4), \\
& -6446+4087x+333x^2-798x^3+224x^4-25x^5+x^6, \\
& -942+919x+909x^2-830x^3+224x^4-25x^5+x^6, \\
& -826+1043x+857x^2-826x^3+224x^4-25x^5+x^6, \\
& (-5+x)(114-173x-206x^2+124x^3-20x^4+x^5), \\
& -554+387x+1065x^2-842x^3+224x^4-25x^5+x^6, \\
& -390+495x+1013x^2-838x^3+224x^4-25x^5+x^6, \\
& -550+527x+1013x^2-838x^3+224x^4-25x^5+x^6, \\
& (31-12x+x^2)(-26+9x+37x^2-13x^3+x^4), \\
& -994+843x+945x^2-834x^3+224x^4-25x^5+x^6, \\
& -1090+875x+945x^2-834x^3+224x^4-25x^5+x^6, \\
& -1346+939x+945x^2-834x^3+224x^4-25x^5+x^6, \\
& -98+491x+977x^2-834x^3+224x^4-25x^5+x^6, \\
& (17+35x-13x^2+x^3)(-2+33x-12x^2+x^3), \\
& -194+523x+977x^2-834x^3+224x^4-25x^5+x^6, \\
& -354+555x+977x^2-834x^3+224x^4-25x^5+x^6, \\
& -1582+1207x+877x^2-830x^3+224x^4-25x^5+x^6, \\
& -1742+1239x+877x^2-830x^3+224x^4-25x^5+x^6, \\
& -1838+1271x+877x^2-830x^3+224x^4-25x^5+x^6, \\
& (-9+x)(-5+x)(-6+15x+25x^2-11x^3+x^4), \\
& (-5+x)(86-141x-210x^2+124x^3-20x^4+x^5), \\
& (-5+x)(118-141x-210x^2+124x^3-20x^4+x^5), \\
& -526+823x+909x^2-830x^3+224x^4-25x^5+x^6, \\
& -846+887x+909x^2-830x^3+224x^4-25x^5+x^6, \\
& (-5+x)(-1-8x+x^2)(10+29x-12x^2+x^3), \\
& (-9+x)(-5+x)(-1+x)(34+15x-10x^2+x^3), \\
& -1466+1331x+825x^2-826x^3+224x^4-25x^5+x^6, \\
& -1626+1363x+825x^2-826x^3+224x^4-25x^5+x^6, \\
& -1786+1395x+825x^2-826x^3+224x^4-25x^5+x^6, \\
& -1882+1427x+825x^2-826x^3+224x^4-25x^5+x^6, \\
& -2042+1459x+825x^2-826x^3+224x^4-25x^5+x^6, \\
& (-5+x)(82-173x-206x^2+124x^3-20x^4+x^5), \\
& (-5+x)(146-173x-206x^2+124x^3-20x^4+x^5), \\
& (-5+x)(210-173x-206x^2+124x^3-20x^4+x^5), \\
& -986+1075x+857x^2-826x^3+224x^4-25x^5+x^6, \\
& (-5+x)(-1-8x+x^2)(14+29x-12x^2+x^3), \\
& -2614+1887x+741x^2-822x^3+224x^4-25x^5+x^6, \\
& -2774+1919x+741x^2-822x^3+224x^4-25x^5+x^6, \\
& -3030+1983x+741x^2-822x^3+224x^4-25x^5+x^6, \\
& -1718+1535x+773x^2-822x^3+224x^4-25x^5+x^6, \\
& -1878+1567x+773x^2-822x^3+224x^4-25x^5+x^6, \\
& -2038+1599x+773x^2-822x^3+224x^4-25x^5+x^6, \\
& (-42+51x-14x^2+x^3)(47+19x-11x^2+x^3), \\
& -2134+1631x+773x^2-822x^3+224x^4-25x^5+x^6, \\
& (31-12x+x^2)(-74+25x+37x^2-13x^3+x^4),
\end{aligned}$$

$$\begin{aligned}
& -918 + 1215x + 805x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -1078 + 1247x + 805x^2 - 822x^3 + 224x^4 - 25x^5 + x^6, \\
& -3314 + 2267x + 673x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3474 + 2299x + 673x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2258 + 1883x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2418 + 1915x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2578 + 1947x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -2674 + 1979x + 705x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& (13 - 10x + x^2) (-218 - 13x + 61x^2 - 15x^3 + x^4), \\
& -1618 + 1595x + 737x^2 - 818x^3 + 224x^4 - 25x^5 + x^6, \\
& -3806 + 2599x + 605x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3966 + 2631x + 605x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -4222 + 2695x + 605x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (550 - 333x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (582 - 333x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (614 - 333x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (646 - 333x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& -3166 + 2311x + 637x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& -3326 + 2343x + 637x^2 - 814x^3 + 224x^4 - 25x^5 + x^6, \\
& (-58 + 55x - 14x^2 + x^3) (59 + 15x - 11x^2 + x^3), \\
& (-5 + x) (422 - 301x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (454 - 301x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (486 - 301x - 194x^2 + 124x^3 - 20x^4 + x^5), \\
& (-7 + x) (-5 + x) (-110 + 41x + 33x^2 - 13x^3 + x^4), \\
& (-5 + x) (802 - 397x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& -4106 + 2819x + 553x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& -4266 + 2851x + 553x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& (38 - 13x + x^2) (17 - 10x + x^2) (-7 - 2x + x^2), \\
& (-5 + x) (610 - 365x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (642 - 365x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (674 - 365x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x) (706 - 365x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& -3466 + 2531x + 585x^2 - 810x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x) (482 - 333x - 190x^2 + 124x^3 - 20x^4 + x^5), \\
& (-7 + x) (714 - 371x - 120x^2 + 98x^3 - 18x^4 + x^5), \\
& -5158 + 3343x + 469x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& (-74 + 59x - 14x^2 + x^3) (71 + 11x - 11x^2 + x^3), \\
& -4358 + 3023x + 501x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& -4518 + 3055x + 501x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& -4614 + 3087x + 501x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& (31 - 12x + x^2) (-154 + 41x + 37x^2 - 13x^3 + x^4), \\
& -3558 + 2703x + 533x^2 - 806x^3 + 224x^4 - 25x^5 + x^6, \\
& (-7 + x) (814 - 411x - 116x^2 + 98x^3 - 18x^4 + x^5), \\
& -5954 + 3755x + 401x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -4898 + 3371x + 433x^2 - 802x^3 + 224x^4 - 25x^5 + x^6,
\end{aligned}$$

$$\begin{aligned}
& -5058 + 3403x + 433x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& -5314 + 3467x + 433x^2 - 802x^3 + 224x^4 - 25x^5 + x^6, \\
& (-9 + x)(-5 + x)(-134 + 47x + 25x^2 - 11x^3 + x^4), \\
& (-5 + x)(1238 - 557x - 178x^2 + 124x^3 - 20x^4 + x^5), \\
& (-7 + x)(-5 + x)(-154 + 53x + 33x^2 - 13x^3 + x^4), \\
& (-5 + x)(1110 - 525x - 178x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(1142 - 525x - 178x^2 + 124x^3 - 20x^4 + x^5), \\
& -5806 + 3799x + 365x^2 - 798x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(950 - 493x - 178x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(982 - 493x - 178x^2 + 124x^3 - 20x^4 + x^5), \\
& (-3 + x)(2462 - 711x - 320x^2 + 158x^3 - 22x^4 + x^5), \\
& (-5 + x)(1298 - 589x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& -6746 + 4307x + 281x^2 - 794x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(1138 - 557x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(1170 - 557x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(1202 - 557x - 174x^2 + 124x^3 - 20x^4 + x^5), \\
& (-3 + x)(2546 - 751x - 316x^2 + 158x^3 - 22x^4 + x^5), \\
& -6838 + 4479x + 229x^2 - 790x^3 + 224x^4 - 25x^5 + x^6, \\
& -6998 + 4511x + 229x^2 - 790x^3 + 224x^4 - 25x^5 + x^6, \\
& (-3 + x)(31 - 12x + x^2)(78 + 7x - 10x^2 + x^3), \\
& (-3 + x)(2726 - 807x - 312x^2 + 158x^3 - 22x^4 + x^5), \\
& -7538 + 4859x + 161x^2 - 786x^3 + 224x^4 - 25x^5 + x^6, \\
& (-5 + x)(-3 + x)(-578 + 57x + 73x^2 - 17x^3 + x^4), \\
& (-5 + x)(1606 - 717x - 162x^2 + 124x^3 - 20x^4 + x^5), \\
& (-7 + x)(-5 + x)(-3 + x)(78 + 3x - 10x^2 + x^3), \\
& (-5 + x)(1478 - 685x - 162x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(-3 + x)(-598 + 61x + 73x^2 - 17x^3 + x^4), \\
& (-7 + x)(-5 + x)(-238 + 73x + 33x^2 - 13x^3 + x^4), \\
& (-5 + x)(-3 + x)(-566 + 61x + 73x^2 - 17x^3 + x^4), \\
& (-7 + x)(1354 - 659x - 88x^2 + 98x^3 - 18x^4 + x^5), \\
& (-5 + x)(2134 - 909x - 146x^2 + 124x^3 - 20x^4 + x^5), \\
& (-5 + x)(2194 - 941x - 142x^2 + 124x^3 - 20x^4 + x^5) \}
\end{aligned}$$

$$\begin{aligned}
\text{warrantpolysub} &= -826 + 1043x + 857x^2 - 826x^3 + 224x^4 - 25x^5 + x^6 \\
&-826 + 1043x + 857x^2 - 826x^3 + 224x^4 - 25x^5 + x^6
\end{aligned}$$

In[]:= listmod128[{8, 20, 28, 38, 67}]

$$\begin{aligned}
\text{Out[]} &= \{-554 + 387x + 1065x^2 - 842x^3 + 224x^4 - 25x^5 + x^6, \\
&-1742 + 1239x + 877x^2 - 830x^3 + 224x^4 - 25x^5 + x^6, \\
&(-9 + x)(-5 + x)(-1 + x)(34 + 15x - 10x^2 + x^3), \\
&(-5 + x)(-1 - 8x + x^2)(14 + 29x - 12x^2 + x^3), \\
&(-58 + 55x - 14x^2 + x^3)(59 + 15x - 11x^2 + x^3)\}
\end{aligned}$$

In[]:= anglesquaredsubcheckcompatible = anglesquaredsub[{8, 20, 28, 38, 67}];

```
In[*]:= anglesquaredsubcheckcompatible // MatrixForm
```

```
Out[*] // MatrixForm =
```

$$\begin{pmatrix} \frac{5674}{11165} & \frac{1}{440} (5 + \sqrt{5}) & \frac{25-3\sqrt{5}}{1160} & \frac{1}{440} (5 - \sqrt{5}) & \frac{2}{5} & \frac{25+3\sqrt{5}}{1160} & \frac{2}{77} \\ \frac{5492}{11165} & -\frac{9}{440} (-5 + \sqrt{5}) & \frac{45-17\sqrt{5}}{1160} & \frac{9}{440} (5 + \sqrt{5}) & \frac{1}{5} & \frac{45+17\sqrt{5}}{1160} & \frac{2}{77} \\ \frac{156}{319} & \frac{1}{440} (65 - 19\sqrt{5}) & \frac{1}{232} (25 - 3\sqrt{5}) & \frac{1}{440} (65 + 19\sqrt{5}) & 0 & \frac{1}{232} (25 + 3\sqrt{5}) & 0 \\ \frac{1112}{2233} & \frac{5}{88} - \frac{1}{8\sqrt{5}} & \frac{165+73\sqrt{5}}{1160} & \frac{5}{88} + \frac{1}{8\sqrt{5}} & 0 & \frac{165-73\sqrt{5}}{1160} & \frac{8}{77} \\ \frac{5252}{11165} & \frac{5}{88} + \frac{1}{8\sqrt{5}} & \frac{65+27\sqrt{5}}{1160} & \frac{5}{88} - \frac{1}{8\sqrt{5}} & \frac{1}{5} & \frac{65-27\sqrt{5}}{1160} & \frac{8}{77} \end{pmatrix}$$

```
In[*]:= anglesubcheckcompatible = Sqrt[anglesquaredsubcheckcompatible] // FullSimplify;
```

```
In[*]:= anglesubcheckcompatible // MatrixForm
```

```
Out[*] // MatrixForm =
```

$$\begin{pmatrix} \sqrt{\frac{5674}{11165}} & \frac{1}{2} \sqrt{\frac{1}{110} (5 + \sqrt{5})} & \sqrt{0.126...} & \sqrt{0.0793...} & \sqrt{\frac{2}{5}} & \sqrt{\frac{5}{232} + \frac{3}{232\sqrt{5}}} & \sqrt{\frac{2}{77}} \\ 2 \sqrt{\frac{1373}{11165}} & \frac{3}{2} \sqrt{\frac{1}{110} (5 - \sqrt{5})} & \sqrt{0.0776...} & \frac{3}{2} \sqrt{\frac{1}{110} (5 + \sqrt{5})} & \frac{1}{\sqrt{5}} & \sqrt{\frac{9}{232} + \frac{17}{232\sqrt{5}}} & \sqrt{\frac{2}{77}} \\ 2 \sqrt{\frac{39}{319}} & \sqrt{0.226...} & \sqrt{0.281...} & \sqrt{\frac{13}{88} + \frac{19}{88\sqrt{5}}} & 0 & \sqrt{\frac{25}{232} + \frac{3\sqrt{5}}{232}} & 0 \\ 2 \sqrt{\frac{278}{2233}} & \sqrt{\frac{5}{88} - \frac{1}{8\sqrt{5}}} & \sqrt{0.532...} & \sqrt{\frac{5}{88} + \frac{1}{8\sqrt{5}}} & 0 & \sqrt{0.0390...} & 2 \sqrt{\frac{2}{77}} \\ 2 \sqrt{\frac{1313}{11165}} & \sqrt{\frac{5}{88} + \frac{1}{8\sqrt{5}}} & \sqrt{0.329...} & \sqrt{\frac{5}{88} - \frac{1}{8\sqrt{5}}} & \frac{1}{\sqrt{5}} & \sqrt{0.0632...} & 2 \sqrt{\frac{2}{77}} \end{pmatrix}$$

```
In[*]:= chisub
```

```
orderedroots[minipoly[chisub]]
```

$$\text{Out[*]} = (-9 + x) (-5 + x)^9 (5 + x)^{14} (31 - 12x + x^2) (-1 - 4x + x^2)$$

$$\text{Out[*]} = \{-5, 2 - \sqrt{5}, 6 - \sqrt{5}, 2 + \sqrt{5}, 5, 6 + \sqrt{5}, 9\}$$

```
{7}, {2, 4}, {3, 6}, {2, 4, 7}, {3, 6, 7}, {2, 3, 4, 6}, {2, 3, 4, 6, 7}
```

```
In[*]:= coeff[chisub, (x + 5) (x - 5) (x^2 - 4 x - 1) (x^2 - 12 x + 31)] // FullSimplify
```

$$\text{Out[*]} = \{9856\}$$

```
In[*]:= For[i = 1, i ≤ 5, i++,
```

```
Print[compatiblefrminipoly[MinimalPolynomial[
combinationangle[{9856}, {1, i}, {7}, anglesubcheckcompatible], x]]]
```

```
]
```

```
1
```

```
1
```

```
1
```

```
1
```

```
1
```

```
In[*]:= coeff[chisub, (x + 5) (x - 5) (x - 9) (x^2 - 12 x + 31)] // FullSimplify
```

$$\text{Out[*]} = \{352 (11 + 5\sqrt{5}), 352 (11 - 5\sqrt{5})\}$$

```

In[*]:= For[i = 1, i ≤ 5, i++,
  Print[compatiblefrminipoly[
    MinimalPolynomial[combinationangle[{352 (11 + 5 √5), 352 (11 - 5 √5)},
      {1, i}, {2, 4}, anglesubcheckcompatible], x]]]
]
1
1
1
1
1
1

In[*]:= coeff[chisub, (x + 5) (x - 5) (x - 9) (x^2 - 4 x - 1)] // FullSimplify
Out[*]:= {32 (-19 + 7 √5), -32 (19 + 7 √5)}

In[*]:= For[i = 1, i ≤ 5, i++,
  Print[compatiblefrminipoly[
    MinimalPolynomial[combinationangle[{32 (-19 + 7 √5), -32 (19 + 7 √5)},
      {1, i}, {3, 6}, anglesubcheckcompatible], x]]]
]
1
1
1
1
1
1

In[*]:= coeff[chisub, (x + 5) (x - 5) (x^2 - 12 x + 31)] // FullSimplify
Out[*]:= {-32 (13 + 6 √5), 32 (-13 + 6 √5), 224}

In[*]:= For[i = 1, i ≤ 5, i++,
  Print[compatiblefrminipoly[
    MinimalPolynomial[combinationangle[{-32 (13 + 6 √5), 32 (-13 + 6 √5), 224},
      {1, i}, {2, 4, 7}, anglesubcheckcompatible], x]]]
]
1
1
1
1
1
1

```

```
In[*]:= coeff[chisub, (x + 5) (x - 5) (x^2 - 4 x - 1)] // FullSimplify
```

```
Out[*]:= {736 - 320  $\sqrt{5}$ , 736 + 320  $\sqrt{5}$ , 2464}
```

```
In[*]:= For[i = 1, i ≤ 5, i++,
  Print[compatiblefrminipoly[
    MinimalPolynomial[combinationangle[{736 - 320  $\sqrt{5}$ , 736 + 320  $\sqrt{5}$ , 2464},
      {1, i}, {3, 6, 7}, anglesubcheckcompatible], x]]]
  ]
1
1
1
1
1
1
```

```
In[*]:= coeff[chisub, (x + 5) (x - 5) (x - 9)] // FullSimplify
```

```
Out[*]:= {44 (3 +  $\sqrt{5}$ ), 4 (3 + 5  $\sqrt{5}$ ), -44 (-3 +  $\sqrt{5}$ ), 12 - 20  $\sqrt{5}$ }
```

```
In[*]:= For[i = 1, i ≤ 5, i++,
  Print[compatiblefrminipoly[MinimalPolynomial[
    combinationangle[{44 (3 +  $\sqrt{5}$ ), 4 (3 + 5  $\sqrt{5}$ ), -44 (-3 +  $\sqrt{5}$ ), 12 - 20  $\sqrt{5}$ },
      {1, i}, {2, 3, 4, 6}, anglesubcheckcompatible], x]]]
  ]
1
1
1
1
1
1
```

```
In[*]:= coeff[chisub, (x + 5) (x - 5)] // FullSimplify
```

```
Out[*]:= {-4 (4 +  $\sqrt{5}$ ), 16 - 12  $\sqrt{5}$ , 4 (-4 +  $\sqrt{5}$ ), 4 (4 + 3  $\sqrt{5}$ ), 56}
```

```
In[*]:= For[i = 1, i ≤ 5, i++,
  Print[compatiblefrminipoly[MinimalPolynomial[
    combinationangle[{-4 (4 +  $\sqrt{5}$ ), 16 - 12  $\sqrt{5}$ , 4 (-4 +  $\sqrt{5}$ ), 4 (4 + 3  $\sqrt{5}$ ), 56},
      {1, i}, {2, 3, 4, 6, 7}, anglesubcheckcompatible], x]]]
  ]
```

1

1

1

1

1

```
In[*]:= anglesquaredsub = anglesquaredmat[chisub, listmod128] // FullSimplify;
```

```
In[*]:= anglesquaredsub // MatrixForm
```

```
Out[*] // MatrixForm=
```

$\frac{1110}{2233}$	$\frac{17}{88} - \frac{3}{8\sqrt{5}}$	$\frac{45-17\sqrt{5}}{1160}$	$\frac{17}{88} + \frac{3}{8\sqrt{5}}$	0	$\frac{45+17\sqrt{5}}{1160}$	$\frac{3}{77}$
$\frac{793}{1595}$	$\frac{7}{88} - \frac{1}{8\sqrt{5}}$	$\frac{115+21\sqrt{5}}{1160}$	$\frac{7}{88} + \frac{1}{8\sqrt{5}}$	$\frac{1}{10}$	$\frac{115-21\sqrt{5}}{1160}$	$\frac{1}{22}$
$\frac{1101}{2233}$	$\frac{1}{440} (65 - 23\sqrt{5})$	$\frac{85+13\sqrt{5}}{1160}$	$\frac{1}{440} (65 + 23\sqrt{5})$	0	$\frac{85-13\sqrt{5}}{1160}$	$\frac{5}{77}$
$\frac{703}{1595}$	$\frac{1}{8} + \frac{17}{88\sqrt{5}}$	$\frac{95-23\sqrt{5}}{1160}$	$\frac{1}{8} - \frac{17}{88\sqrt{5}}$	$\frac{1}{10}$	$\frac{95+23\sqrt{5}}{1160}$	$\frac{1}{22}$
$\frac{5542}{11165}$	$\frac{1}{88} (5 - \sqrt{5})$	$\frac{65+27\sqrt{5}}{1160}$	$\frac{1}{88} (5 + \sqrt{5})$	$\frac{1}{5}$	$\frac{65-27\sqrt{5}}{1160}$	$\frac{6}{77}$
$\frac{5506}{11165}$	$\frac{1}{440} (15 - \sqrt{5})$	$\frac{155+51\sqrt{5}}{1160}$	$\frac{1}{440} (15 + \sqrt{5})$	$\frac{1}{10}$	$\frac{155-51\sqrt{5}}{1160}$	$\frac{1}{14}$
$\frac{1103}{2233}$	$\frac{1}{440} (25 - 7\sqrt{5})$	$\frac{1}{232} (41 + 9\sqrt{5})$	$\frac{1}{440} (25 + 7\sqrt{5})$	0	$\frac{1}{232} (41 - 9\sqrt{5})$	$\frac{3}{77}$
$\frac{5674}{11165}$	$\frac{1}{440} (5 + \sqrt{5})$	$\frac{25-3\sqrt{5}}{1160}$	$\frac{1}{440} (5 - \sqrt{5})$	$\frac{2}{5}$	$\frac{25+3\sqrt{5}}{1160}$	$\frac{2}{77}$
$\frac{1128}{2233}$	$\frac{1}{220} (5 - \sqrt{5})$	$\frac{1}{116} (11 + \sqrt{5})$	$\frac{1}{220} (5 + \sqrt{5})$	$\frac{1}{4}$	$\frac{1}{116} (11 - \sqrt{5})$	$\frac{3}{308}$
$\frac{161}{319}$	$\frac{1}{44} (3 - \sqrt{5})$	$\frac{1}{580} (25 - 3\sqrt{5})$	$\frac{1}{44} (3 + \sqrt{5})$	$\frac{1}{4}$	$\frac{1}{580} (25 + 3\sqrt{5})$	$\frac{1}{44}$
$\frac{194}{385}$	$\frac{1}{110} (5 - \sqrt{5})$	0	$\frac{1}{110} (5 + \sqrt{5})$	$\frac{7}{20}$	0	$\frac{17}{308}$
$\frac{5569}{11165}$	$\frac{1}{220} (25 - 8\sqrt{5})$	$\frac{1}{116} (7 - 2\sqrt{5})$	$\frac{1}{220} (25 + 8\sqrt{5})$	$\frac{3}{20}$	$\frac{1}{116} (7 + 2\sqrt{5})$	$\frac{1}{308}$
$\frac{159}{319}$	$\frac{1}{220} (10 - \sqrt{5})$	$\frac{1}{580} (40 + \sqrt{5})$	$\frac{1}{220} (10 + \sqrt{5})$	$\frac{1}{4}$	$\frac{1}{580} (40 - \sqrt{5})$	$\frac{1}{44}$
$\frac{5556}{11165}$	$\frac{1}{220} (5 + 2\sqrt{5})$	$\frac{1}{580} (15 + 4\sqrt{5})$	$\frac{1}{220} (5 - 2\sqrt{5})$	$\frac{7}{20}$	$\frac{1}{580} (15 - 4\sqrt{5})$	$\frac{17}{308}$
$\frac{5623}{11165}$	$\frac{1}{220} (30 - 13\sqrt{5})$	$\frac{1}{580} (40 + \sqrt{5})$	$\frac{1}{220} (30 + 13\sqrt{5})$	$\frac{1}{20}$	$\frac{1}{580} (40 - \sqrt{5})$	$\frac{1}{28}$
$\frac{5624}{11165}$	$\frac{1}{220} (5 - 2\sqrt{5})$	$\frac{1}{116} (15 + 4\sqrt{5})$	$\frac{1}{220} (5 + 2\sqrt{5})$	$\frac{3}{20}$	$\frac{1}{116} (15 - 4\sqrt{5})$	$\frac{13}{308}$
$\frac{5619}{11165}$	$\frac{3}{220} (5 - 2\sqrt{5})$	$\frac{3}{580} (15 + 4\sqrt{5})$	$\frac{3}{220} (5 + 2\sqrt{5})$	$\frac{3}{20}$	$\frac{3}{580} (15 - 4\sqrt{5})$	$\frac{17}{308}$
$\frac{802}{1595}$	$\frac{1}{44} (5 - 2\sqrt{5})$	$\frac{1}{580} (15 + 4\sqrt{5})$	$\frac{1}{44} (5 + 2\sqrt{5})$	$\frac{3}{20}$	$\frac{1}{580} (15 - 4\sqrt{5})$	$\frac{3}{44}$
$\frac{5497}{11165}$	$\frac{1}{440} (25 - \sqrt{5})$	$\frac{105-\sqrt{5}}{1160}$	$\frac{1}{440} (25 + \sqrt{5})$	$\frac{1}{5}$	$\frac{105+\sqrt{5}}{1160}$	$\frac{1}{77}$
$\frac{5492}{11165}$	$-\frac{9}{440} (-5 + \sqrt{5})$	$\frac{45-17\sqrt{5}}{1160}$	$\frac{9}{440} (5 + \sqrt{5})$	$\frac{1}{5}$	$\frac{45+17\sqrt{5}}{1160}$	$\frac{2}{77}$
$\frac{784}{1595}$	$\frac{1}{88} (3 + \sqrt{5})$	$\frac{1}{232} (11 + \sqrt{5})$	$\frac{1}{88} (3 - \sqrt{5})$	$\frac{3}{10}$	$\frac{1}{232} (11 - \sqrt{5})$	$\frac{1}{22}$
$\frac{159}{319}$	$\frac{1}{440} (25 - 9\sqrt{5})$	$\frac{225+31\sqrt{5}}{1160}$	$\frac{1}{440} (25 + 9\sqrt{5})$	0	$\frac{225-31\sqrt{5}}{1160}$	0
$\frac{1112}{2233}$	$\frac{1}{440} (45 - 17\sqrt{5})$	$\frac{3}{232} (11 + \sqrt{5})$	$\frac{1}{440} (45 + 17\sqrt{5})$	0	$-\frac{3}{232} (-11 + \sqrt{5})$	$\frac{1}{77}$
$\frac{101}{203}$	$\frac{1}{88} (13 - 5\sqrt{5})$	$\frac{105-\sqrt{5}}{1160}$	$\frac{1}{88} (13 + 5\sqrt{5})$	0	$\frac{105+\sqrt{5}}{1160}$	$\frac{2}{77}$
$\frac{5556}{11165}$	$-\frac{3}{440} (-5 + \sqrt{5})$	$\frac{175+37\sqrt{5}}{1160}$	$\frac{3}{440} (5 + \sqrt{5})$	$\frac{1}{10}$	$\frac{175-37\sqrt{5}}{1160}$	$\frac{5}{154}$
$\frac{5546}{11165}$	$\frac{1}{8} - \frac{19}{88\sqrt{5}}$	$\frac{1}{232} (11 + \sqrt{5})$	$\frac{1}{8} + \frac{19}{88\sqrt{5}}$	$\frac{1}{10}$	$\frac{1}{232} (11 - \sqrt{5})$	$\frac{9}{154}$
$\frac{160}{319}$	$\frac{1}{440} (65 - 29\sqrt{5})$	$\frac{65+27\sqrt{5}}{1160}$	$\frac{1}{440} (65 + 29\sqrt{5})$	0	$\frac{65-27\sqrt{5}}{1160}$	$\frac{1}{11}$
$\frac{156}{319}$	$\frac{1}{440} (65 - 19\sqrt{5})$	$\frac{1}{232} (25 - 3\sqrt{5})$	$\frac{1}{440} (65 + 19\sqrt{5})$	0	$\frac{1}{232} (25 + 3\sqrt{5})$	0
$\frac{5461}{\dots}$	$\frac{3}{\dots} (5 + \sqrt{5})$	$\frac{195+23\sqrt{5}}{\dots}$	$-\frac{3}{\dots} (-5 + \sqrt{5})$	$\frac{1}{\dots}$	$\frac{195-23\sqrt{5}}{\dots}$	$\frac{1}{\dots}$

11 165	$\frac{496}{1015}$	$\frac{1}{88} (7 - \sqrt{5})$	$\frac{1160}{1160}$	$\frac{135+7\sqrt{5}}{1160}$	$\frac{440}{88} (7 + \sqrt{5})$	$\frac{1}{88}$	$\frac{1160}{1160}$	$\frac{135-7\sqrt{5}}{1160}$	154
5451	$\frac{1}{8} - \frac{13}{88\sqrt{5}}$		$\frac{75-9\sqrt{5}}{1160}$		$\frac{1}{8} + \frac{13}{88\sqrt{5}}$	$\frac{1}{10}$	$\frac{3(25+3\sqrt{5})}{1160}$	$\frac{5}{154}$	154
5447	$\frac{1}{440} (25 + \sqrt{5})$		$\frac{85+13\sqrt{5}}{1160}$		$\frac{1}{440} (25 - \sqrt{5})$	$\frac{1}{5}$	$\frac{85-13\sqrt{5}}{1160}$	$\frac{4}{77}$	
5442	$\frac{1}{440} (45 - 7\sqrt{5})$		$\frac{25-3\sqrt{5}}{1160}$		$\frac{1}{440} (45 + 7\sqrt{5})$	$\frac{1}{5}$	$\frac{25+3\sqrt{5}}{1160}$	$\frac{5}{77}$	
1104	$\frac{1}{440} (5 + \sqrt{5})$		$\frac{265+61\sqrt{5}}{1160}$		$\frac{1}{440} (5 - \sqrt{5})$	0	$\frac{265-61\sqrt{5}}{1160}$	$\frac{2}{77}$	
38	$-\frac{3}{88} (-3 + \sqrt{5})$		$\frac{1}{40} (5 + \sqrt{5})$		$\frac{3}{88} (3 + \sqrt{5})$	0	$\frac{1}{40} (5 - \sqrt{5})$	$\frac{4}{77}$	
100	$\frac{1}{440} (85 - 31\sqrt{5})$		$\frac{25-3\sqrt{5}}{1160}$		$\frac{1}{440} (85 + 31\sqrt{5})$	0	$\frac{25+3\sqrt{5}}{1160}$	$\frac{6}{77}$	
5501	$\frac{1}{440} (35 - 9\sqrt{5})$	$\frac{1}{232} (19 + 7\sqrt{5})$			$\frac{1}{440} (35 + 9\sqrt{5})$	$\frac{1}{10}$	$\frac{1}{232} (19 - 7\sqrt{5})$	$\frac{13}{154}$	
1112	$\frac{5}{88} - \frac{1}{8\sqrt{5}}$		$\frac{165+73\sqrt{5}}{1160}$		$\frac{5}{88} + \frac{1}{8\sqrt{5}}$	0	$\frac{165-73\sqrt{5}}{1160}$	$\frac{8}{77}$	
5359	$\frac{1}{110} (5 + 2\sqrt{5})$	$\frac{1}{290} (40 + \sqrt{5})$			$\frac{1}{110} (5 - 2\sqrt{5})$	$\frac{3}{20}$	$\frac{1}{290} (40 - \sqrt{5})$	$\frac{1}{308}$	
5354	$\frac{1}{11}$	$\frac{1}{290} (25 - 3\sqrt{5})$			$\frac{1}{11}$	$\frac{3}{20}$	$\frac{1}{290} (25 + 3\sqrt{5})$	$\frac{5}{308}$	
1069	$\frac{3}{220} (5 + \sqrt{5})$	$\frac{1}{580} (25 - 3\sqrt{5})$			$-\frac{3}{220} (-5 + \sqrt{5})$	$\frac{1}{4}$	$\frac{1}{580} (25 + 3\sqrt{5})$	$\frac{15}{308}$	
5413	$\frac{1}{220} (15 - \sqrt{5})$	$\frac{1}{580} (85 + 13\sqrt{5})$			$\frac{1}{220} (15 + \sqrt{5})$	$\frac{1}{20}$	$\frac{1}{580} (85 - 13\sqrt{5})$	$\frac{1}{28}$	
5408	$\frac{1}{44} (5 - \sqrt{5})$	$\frac{1}{116} (11 + \sqrt{5})$			$\frac{1}{44} (5 + \sqrt{5})$	$\frac{1}{20}$	$\frac{1}{116} (11 - \sqrt{5})$	$\frac{15}{308}$	
5403	$\frac{1}{220} (35 - 9\sqrt{5})$	$\frac{1}{580} (25 - 3\sqrt{5})$			$\frac{1}{220} (35 + 9\sqrt{5})$	$\frac{1}{20}$	$\frac{1}{580} (25 + 3\sqrt{5})$	$\frac{19}{308}$	
772	$\frac{1}{110} (5 + \sqrt{5})$	$\frac{1}{145} (15 + 4\sqrt{5})$			$\frac{1}{110} (5 - \sqrt{5})$	$\frac{3}{20}$	$\frac{1}{145} (15 - 4\sqrt{5})$	$\frac{3}{44}$	
5399	$\frac{1}{110} (10 - \sqrt{5})$	$\frac{1}{290} (15 + 4\sqrt{5})$			$\frac{1}{110} (10 + \sqrt{5})$	$\frac{3}{20}$	$\frac{1}{290} (15 - 4\sqrt{5})$	$\frac{25}{308}$	
186	$-\frac{3}{110} (-5 + \sqrt{5})$	0			$\frac{3}{110} (5 + \sqrt{5})$	$\frac{3}{20}$	0	$\frac{29}{308}$	
5463	$\frac{1}{220} (5 + \sqrt{5})$	$\frac{1}{116} (19 + 7\sqrt{5})$			$\frac{1}{220} (5 - \sqrt{5})$	$\frac{1}{20}$	$\frac{1}{116} (19 - 7\sqrt{5})$	$\frac{27}{308}$	
5458	$-\frac{3}{220} (-5 + \sqrt{5})$	$\frac{1}{580} (65 + 27\sqrt{5})$			$\frac{3}{220} (5 + \sqrt{5})$	$\frac{1}{20}$	$\frac{1}{580} (65 - 27\sqrt{5})$	$\frac{31}{308}$	
5284	$\frac{1}{220} (15 + 4\sqrt{5})$	$\frac{1}{580} (65 - 2\sqrt{5})$			$\frac{1}{220} (15 - 4\sqrt{5})$	$\frac{3}{20}$	$\frac{1}{580} (65 + 2\sqrt{5})$	$\frac{5}{308}$	
5279	$\frac{5}{44}$	$\frac{1}{116} (7 - 2\sqrt{5})$			$\frac{5}{44}$	$\frac{3}{20}$	$\frac{1}{116} (7 + 2\sqrt{5})$	$\frac{9}{308}$	
5343	$\frac{1}{220} (10 + 3\sqrt{5})$	$\frac{1}{580} (100 + 17\sqrt{5})$			$\frac{1}{220} (10 - 3\sqrt{5})$	$\frac{1}{20}$	$\frac{1}{580} (100 - 17\sqrt{5})$	$\frac{1}{28}$	
5338	$\frac{1}{220} (20 - \sqrt{5})$	$\frac{1}{580} (70 + 9\sqrt{5})$			$\frac{1}{220} (20 + \sqrt{5})$	$\frac{1}{20}$	$\frac{1}{580} (70 - 9\sqrt{5})$	$\frac{15}{308}$	
5333	$\frac{1}{44} (6 - \sqrt{5})$	$\frac{1}{580} (40 + \sqrt{5})$			$\frac{1}{44} (6 + \sqrt{5})$	$\frac{1}{20}$	$\frac{1}{580} (40 - \sqrt{5})$	$\frac{19}{308}$	
5329	$\frac{1}{220} (15 + 2\sqrt{5})$	$\frac{3}{580} (15 + 4\sqrt{5})$			$\frac{1}{220} (15 - 2\sqrt{5})$	$\frac{3}{20}$	$\frac{3}{580} (15 - 4\sqrt{5})$	$\frac{25}{308}$	
484	$\frac{1}{220} (25 - 2\sqrt{5})$	$\frac{1}{580} (15 + 4\sqrt{5})$			$\frac{1}{220} (25 + 2\sqrt{5})$	$\frac{3}{20}$	$\frac{1}{580} (15 - 4\sqrt{5})$	$\frac{29}{308}$	
5388	$\frac{1}{220} (10 + \sqrt{5})$	$\frac{1}{580} (80 + 31\sqrt{5})$			$\frac{1}{220} (10 - \sqrt{5})$	$\frac{1}{20}$	$\frac{1}{580} (80 - 31\sqrt{5})$	$\frac{31}{308}$	
5216	$\frac{1}{440} (35 + 9\sqrt{5})$	$\frac{155-7\sqrt{5}}{1160}$			$\frac{1}{440} (35 - 9\sqrt{5})$	$\frac{1}{10}$	$\frac{155+7\sqrt{5}}{1160}$	$\frac{1}{154}$	
5211	$\frac{1}{440} (55 + \sqrt{5})$	$\frac{95-23\sqrt{5}}{1160}$			$\frac{1}{8} - \frac{1}{88\sqrt{5}}$	$\frac{1}{10}$	$\frac{95+23\sqrt{5}}{1160}$	$\frac{3}{154}$	
5202	$\frac{1}{440} (45 + 7\sqrt{5})$	$\frac{45-17\sqrt{5}}{1160}$			$\frac{1}{440} (45 - 7\sqrt{5})$	$\frac{1}{5}$	$\frac{45+17\sqrt{5}}{1160}$	$\frac{4}{77}$	
1055	$\frac{1}{440} (25 + 7\sqrt{5})$	$\frac{225+31\sqrt{5}}{1160}$			$\frac{1}{440} (25 - 7\sqrt{5})$	0	$\frac{225-31\sqrt{5}}{1160}$	$\frac{2}{77}$	
1054	$\frac{1}{440} (45 - \sqrt{5})$	$\frac{3}{232} (11 + \sqrt{5})$			$\frac{1}{440} (45 + \sqrt{5})$	0	$-\frac{3}{232} (-11 + \sqrt{5})$	$\frac{3}{77}$	
1053	$\frac{1}{440} (65 - 9\sqrt{5})$	$\frac{105-\sqrt{5}}{1160}$			$\frac{1}{440} (65 + 9\sqrt{5})$	0	$\frac{105+\sqrt{5}}{1160}$	$\frac{4}{77}$	
1052	$-\frac{17}{440} (-5 + \sqrt{5})$	$\frac{45-17\sqrt{5}}{1160}$			$\frac{17}{440} (5 + \sqrt{5})$	0	$\frac{45+17\sqrt{5}}{1160}$	$\frac{5}{77}$	
5261	$\frac{1}{88} (7 + \sqrt{5})$	$\frac{115+21\sqrt{5}}{1160}$			$\frac{1}{88} (7 - \sqrt{5})$	$\frac{1}{10}$	$\frac{115-21\sqrt{5}}{1160}$	$\frac{1}{154}$	

$\frac{5256}{11165}$	$\frac{1}{8} - \frac{3}{88\sqrt{5}}$	$\frac{1}{232} (11 + \sqrt{5})$	$\frac{1}{8} + \frac{3}{88\sqrt{5}}$	$\frac{1}{10}$	$\frac{1}{232} (11 - \sqrt{5})$	$\frac{13}{154}$
$\frac{5252}{11165}$	$\frac{5}{88} + \frac{1}{8\sqrt{5}}$	$\frac{65+27\sqrt{5}}{1160}$	$\frac{5}{88} - \frac{1}{8\sqrt{5}}$	$\frac{1}{5}$	$\frac{65-27\sqrt{5}}{1160}$	$\frac{8}{77}$
$\frac{152}{319}$	$\frac{1}{440} (25 + 3\sqrt{5})$	$\frac{185+59\sqrt{5}}{1160}$	$\frac{1}{440} (25 - 3\sqrt{5})$	0	$\frac{185-59\sqrt{5}}{1160}$	$\frac{1}{11}$
$\frac{1063}{2233}$	$\frac{1}{88} (9 - \sqrt{5})$	$\frac{125+43\sqrt{5}}{1160}$	$\frac{1}{88} (9 + \sqrt{5})$	0	$\frac{125-43\sqrt{5}}{1160}$	$\frac{8}{77}$
$\frac{1062}{2233}$	$-\frac{13}{440} (-5 + \sqrt{5})$	$\frac{65+27\sqrt{5}}{1160}$	$\frac{13}{440} (5 + \sqrt{5})$	0	$\frac{65-27\sqrt{5}}{1160}$	$\frac{9}{77}$
$\frac{1035}{2233}$	$\frac{1}{88} (9 + \sqrt{5})$	$\frac{185+\sqrt{5}}{1160}$	$\frac{1}{88} (9 - \sqrt{5})$	0	$\frac{185-\sqrt{5}}{1160}$	$\frac{1}{77}$
$\frac{94}{203}$	$\frac{1}{440} (65 - 3\sqrt{5})$	$\frac{1}{232} (25 - 3\sqrt{5})$	$\frac{1}{440} (65 + 3\sqrt{5})$	0	$\frac{1}{232} (25 + 3\sqrt{5})$	$\frac{2}{77}$
$\frac{738}{1595}$	$\frac{7}{88} + \frac{1}{8\sqrt{5}}$	$\frac{135+7\sqrt{5}}{1160}$	$\frac{7}{88} - \frac{1}{8\sqrt{5}}$	$\frac{1}{10}$	$\frac{135-7\sqrt{5}}{1160}$	$\frac{1}{22}$
$\frac{5161}{11165}$	$\frac{1}{8} + \frac{3}{88\sqrt{5}}$	$\frac{75-9\sqrt{5}}{1160}$	$\frac{1}{8} - \frac{3}{88\sqrt{5}}$	$\frac{1}{10}$	$\frac{3(25+3\sqrt{5})}{1160}$	$\frac{9}{154}$
$\frac{736}{1595}$	$\frac{9}{440} (5 + \sqrt{5})$	$\frac{25-3\sqrt{5}}{1160}$	$-\frac{9}{440} (-5 + \sqrt{5})$	$\frac{1}{5}$	$\frac{25+3\sqrt{5}}{1160}$	$\frac{1}{11}$
$\frac{95}{203}$	$\frac{1}{440} (25 + 9\sqrt{5})$	$\frac{1}{232} (41 + 9\sqrt{5})$	$\frac{1}{440} (25 - 9\sqrt{5})$	0	$\frac{1}{232} (41 - 9\sqrt{5})$	$\frac{5}{77}$
$\frac{36}{77}$	$\frac{1}{440} (45 + \sqrt{5})$	$\frac{1}{40} (5 + \sqrt{5})$	$\frac{1}{440} (45 - \sqrt{5})$	0	$\frac{1}{40} (5 - \sqrt{5})$	$\frac{6}{77}$
$\frac{149}{319}$	$\frac{1}{440} (65 - 7\sqrt{5})$	$\frac{85+13\sqrt{5}}{1160}$	$\frac{1}{440} (65 + 7\sqrt{5})$	0	$\frac{85-13\sqrt{5}}{1160}$	$\frac{1}{11}$
$\frac{1042}{2233}$	$\frac{1}{88} (17 - 3\sqrt{5})$	$\frac{25-3\sqrt{5}}{1160}$	$\frac{1}{88} (17 + 3\sqrt{5})$	0	$\frac{25+3\sqrt{5}}{1160}$	$\frac{8}{77}$
$\frac{5211}{11165}$	$\frac{7}{440} (5 + \sqrt{5})$	$\frac{1}{232} (19 + 7\sqrt{5})$	$-\frac{7}{440} (-5 + \sqrt{5})$	$\frac{1}{10}$	$\frac{1}{232} (19 - 7\sqrt{5})$	$\frac{17}{154}$
$\frac{1054}{2233}$	$\frac{1}{88} (5 + \sqrt{5})$	$\frac{165+73\sqrt{5}}{1160}$	$\frac{1}{88} (5 - \sqrt{5})$	0	$\frac{165-73\sqrt{5}}{1160}$	$\frac{10}{77}$
$\frac{5073}{11165}$	$\frac{1}{44} (5 + \sqrt{5})$	$\frac{1}{580} (75 - 9\sqrt{5})$	$\frac{1}{44} (5 - \sqrt{5})$	$\frac{1}{20}$	$\frac{3}{580} (25 + 3\sqrt{5})$	$\frac{3}{308}$
$\frac{724}{1595}$	$\frac{1}{220} (35 + \sqrt{5})$	$\frac{1}{580} (45 - 17\sqrt{5})$	$\frac{1}{220} (35 - \sqrt{5})$	$\frac{1}{20}$	$\frac{1}{580} (45 + 17\sqrt{5})$	$\frac{1}{44}$
$\frac{5064}{11165}$	$\frac{1}{55} (5 + 2\sqrt{5})$	$\frac{1}{290} (25 - 3\sqrt{5})$	$\frac{1}{55} (5 - 2\sqrt{5})$	$\frac{3}{20}$	$\frac{1}{290} (25 + 3\sqrt{5})$	$\frac{13}{308}$
$\frac{5118}{11165}$	$\frac{1}{220} (25 + 3\sqrt{5})$	$\frac{1}{116} (11 + \sqrt{5})$	$\frac{1}{220} (25 - 3\sqrt{5})$	$\frac{1}{20}$	$\frac{1}{116} (11 - \sqrt{5})$	$\frac{23}{308}$
$\frac{5113}{11165}$	$\frac{1}{220} (35 - \sqrt{5})$	$\frac{1}{580} (25 - 3\sqrt{5})$	$\frac{1}{220} (35 + \sqrt{5})$	$\frac{1}{20}$	$\frac{1}{580} (25 + 3\sqrt{5})$	$\frac{27}{308}$
$\frac{5109}{11165}$	$\frac{1}{110} (10 + 3\sqrt{5})$	$\frac{1}{290} (15 + 4\sqrt{5})$	$\frac{1}{110} (10 - 3\sqrt{5})$	$\frac{3}{20}$	$\frac{1}{290} (15 - 4\sqrt{5})$	$\frac{3}{28}$
$\frac{16}{35}$	$\frac{1}{110} (15 + \sqrt{5})$	0	$\frac{1}{110} (15 - \sqrt{5})$	$\frac{3}{20}$	0	$\frac{37}{308}$
$\frac{5168}{11165}$	$\frac{1}{44} (3 + \sqrt{5})$	$\frac{1}{580} (65 + 27\sqrt{5})$	$\frac{1}{44} (3 - \sqrt{5})$	$\frac{1}{20}$	$\frac{1}{580} (65 - 27\sqrt{5})$	$\frac{39}{308}$
$\frac{714}{1595}$	$\frac{1}{44} (6 + \sqrt{5})$	$\frac{1}{580} (60 - 13\sqrt{5})$	$\frac{1}{44} (6 - \sqrt{5})$	$\frac{1}{20}$	$\frac{1}{580} (60 + 13\sqrt{5})$	$\frac{1}{44}$
$\frac{4989}{11165}$	$\frac{1}{220} (25 + 8\sqrt{5})$	$\frac{1}{116} (7 - 2\sqrt{5})$	$\frac{1}{220} (25 - 8\sqrt{5})$	$\frac{3}{20}$	$\frac{1}{116} (7 + 2\sqrt{5})$	$\frac{17}{308}$
$\frac{5048}{11165}$	$\frac{1}{220} (20 + 7\sqrt{5})$	$\frac{1}{580} (70 + 9\sqrt{5})$	$\frac{1}{220} (20 - 7\sqrt{5})$	$\frac{1}{20}$	$\frac{1}{580} (70 - 9\sqrt{5})$	$\frac{23}{308}$
$\frac{5043}{11165}$	$\frac{3}{220} (10 + \sqrt{5})$	$\frac{1}{580} (40 + \sqrt{5})$	$-\frac{3}{220} (-10 + \sqrt{5})$	$\frac{1}{20}$	$\frac{1}{580} (40 - \sqrt{5})$	$\frac{27}{308}$
$\frac{5034}{11165}$	$\frac{1}{220} (25 + 6\sqrt{5})$	$\frac{1}{580} (15 + 4\sqrt{5})$	$\frac{1}{220} (25 - 6\sqrt{5})$	$\frac{3}{20}$	$\frac{1}{580} (15 - 4\sqrt{5})$	$\frac{37}{308}$
$\frac{141}{319}$	$\frac{1}{440} (45 + 19\sqrt{5})$	$\frac{205-13\sqrt{5}}{1160}$	$\frac{1}{440} (45 - 19\sqrt{5})$	0	$\frac{205+13\sqrt{5}}{1160}$	0
$\frac{34}{77}$	$\frac{13}{88} + \frac{1}{8\sqrt{5}}$	$\frac{1}{40} (5 - \sqrt{5})$	$\frac{13}{88} - \frac{1}{8\sqrt{5}}$	0	$\frac{1}{40} (5 + \sqrt{5})$	$\frac{1}{77}$
$\frac{996}{2233}$	$\frac{3}{88} (3 + \sqrt{5})$	$\frac{3}{232} (11 + \sqrt{5})$	$-\frac{3}{88} (-3 + \sqrt{5})$	0	$-\frac{3}{232} (-11 + \sqrt{5})$	$\frac{5}{77}$
$\frac{995}{2233}$	$\frac{1}{440} (65 + 7\sqrt{5})$	$\frac{105+\sqrt{5}}{1160}$	$\frac{1}{440} (65 - 7\sqrt{5})$	0	$\frac{105-\sqrt{5}}{1160}$	$\frac{6}{77}$
$\frac{142}{319}$	$\frac{1}{440} (85 - \sqrt{5})$	$\frac{45-17\sqrt{5}}{1160}$	$\frac{1}{440} (85 + \sqrt{5})$	0	$\frac{45+17\sqrt{5}}{1160}$	$\frac{1}{11}$
$\frac{4966}{11165}$	$\frac{1}{8} + \frac{13}{88\sqrt{5}}$	$\frac{1}{232} (11 + \sqrt{5})$	$\frac{1}{8} - \frac{13}{88\sqrt{5}}$	$\frac{1}{10}$	$\frac{1}{232} (11 - \sqrt{5})$	$\frac{17}{154}$
1005	9 . 1	125+43 $\sqrt{5}$	9 1	∞	125-43 $\sqrt{5}$	10

$\frac{2233}{1004}$	$\frac{1}{440} (65 + 3\sqrt{5})$	$\frac{1160}{65+27\sqrt{5}}$	$\frac{1}{440} (65 - 3\sqrt{5})$	0	$\frac{1160}{65-27\sqrt{5}}$	$\frac{1}{7}$
$\frac{4826}{11165}$	$\frac{1}{8} + \frac{23}{88\sqrt{5}}$	$\frac{115-37\sqrt{5}}{1160}$	$\frac{1}{8} - \frac{23}{88\sqrt{5}}$	$\frac{1}{10}$	$\frac{115+37\sqrt{5}}{1160}$	$\frac{3}{154}$
$\frac{976}{2233}$	$\frac{13}{440} (5 + \sqrt{5})$	$\frac{1}{232} (25 - 3\sqrt{5})$	$-\frac{13}{440} (-5 + \sqrt{5})$	0	$\frac{1}{232} (25 + 3\sqrt{5})$	$\frac{4}{77}$
$\frac{4871}{11165}$	$\frac{1}{8} + \frac{19}{88\sqrt{5}}$	$\frac{75-9\sqrt{5}}{1160}$	$\frac{1}{8} - \frac{19}{88\sqrt{5}}$	$\frac{1}{10}$	$\frac{3(25+3\sqrt{5})}{1160}$	$\frac{13}{154}$
$\frac{34}{77}$	$\frac{1}{440} (45 + 17\sqrt{5})$	$\frac{1}{40} (5 + \sqrt{5})$	$\frac{1}{440} (45 - 17\sqrt{5})$	0	$\frac{1}{40} (5 - \sqrt{5})$	$\frac{8}{77}$
$\frac{985}{2233}$	$\frac{1}{440} (65 + 9\sqrt{5})$	$\frac{85+13\sqrt{5}}{1160}$	$\frac{1}{440} (65 - 9\sqrt{5})$	0	$\frac{85-13\sqrt{5}}{1160}$	$\frac{9}{77}$
$\frac{984}{2233}$	$\frac{1}{440} (85 + \sqrt{5})$	$\frac{25-3\sqrt{5}}{1160}$	$\frac{1}{440} (85 - \sqrt{5})$	0	$\frac{25+3\sqrt{5}}{1160}$	$\frac{10}{77}$
$\frac{4778}{11165}$	$\frac{1}{220} (35 + 9\sqrt{5})$	$\frac{1}{580} (45 - 17\sqrt{5})$	$\frac{1}{220} (35 - 9\sqrt{5})$	$\frac{1}{20}$	$\frac{1}{580} (45 + 17\sqrt{5})$	$\frac{15}{308}$
$\frac{4828}{11165}$	$\frac{5}{44} + \frac{1}{4\sqrt{5}}$	$\frac{1}{116} (11 + \sqrt{5})$	$\frac{5}{44} - \frac{1}{4\sqrt{5}}$	$\frac{1}{20}$	$\frac{1}{116} (11 - \sqrt{5})$	$\frac{31}{308}$
$\frac{689}{1595}$	$\frac{7}{220} (5 + \sqrt{5})$	$\frac{1}{580} (25 - 3\sqrt{5})$	$-\frac{7}{220} (-5 + \sqrt{5})$	$\frac{1}{20}$	$\frac{1}{580} (25 + 3\sqrt{5})$	$\frac{5}{44}$
$\frac{166}{385}$	$\frac{1}{22} (3 + \sqrt{5})$	0	$\frac{1}{22} (3 - \sqrt{5})$	$\frac{3}{20}$	0	$\frac{45}{308}$
$\frac{428}{1015}$	$\frac{1}{220} (30 + 13\sqrt{5})$	$\frac{1}{580} (60 - 13\sqrt{5})$	$\frac{1}{220} (30 - 13\sqrt{5})$	$\frac{1}{20}$	$\frac{1}{580} (60 + 13\sqrt{5})$	$\frac{15}{308}$
$\frac{679}{1595}$	$\frac{3}{22} + \frac{1}{4\sqrt{5}}$	$\frac{1}{580} (40 + \sqrt{5})$	$\frac{3}{22} - \frac{1}{4\sqrt{5}}$	$\frac{1}{20}$	$\frac{1}{580} (40 - \sqrt{5})$	$\frac{5}{44}$
$\frac{32}{77}$	$\frac{1}{440} (65 + 27\sqrt{5})$	$\frac{1}{40} (5 - \sqrt{5})$	$\frac{1}{440} (65 - 27\sqrt{5})$	0	$\frac{1}{40} (5 + \sqrt{5})$	$\frac{3}{77}$
$\frac{937}{2233}$	$\frac{1}{440} (65 + 23\sqrt{5})$	$\frac{105-\sqrt{5}}{1160}$	$\frac{1}{440} (65 - 23\sqrt{5})$	0	$\frac{105+\sqrt{5}}{1160}$	$\frac{8}{77}$
$\frac{936}{2233}$	$\frac{1}{88} (17 + 3\sqrt{5})$	$\frac{45-17\sqrt{5}}{1160}$	$\frac{1}{88} (17 - 3\sqrt{5})$	0	$\frac{45+17\sqrt{5}}{1160}$	$\frac{9}{77}$
$\frac{86}{203}$	$\frac{1}{440} (65 + 19\sqrt{5})$	$\frac{65+27\sqrt{5}}{1160}$	$\frac{1}{440} (65 - 19\sqrt{5})$	0	$\frac{65-27\sqrt{5}}{1160}$	$\frac{13}{77}$
$\frac{918}{2233}$	$\frac{1}{440} (65 + 29\sqrt{5})$	$\frac{1}{232} (25 - 3\sqrt{5})$	$\frac{1}{440} (65 - 29\sqrt{5})$	0	$\frac{1}{232} (25 + 3\sqrt{5})$	$\frac{6}{77}$
$\frac{927}{2233}$	$\frac{1}{88} (13 + 5\sqrt{5})$	$\frac{85+13\sqrt{5}}{1160}$	$\frac{1}{88} (13 - 5\sqrt{5})$	0	$\frac{85-13\sqrt{5}}{1160}$	$\frac{1}{7}$
$\frac{926}{2233}$	$\frac{17}{440} (5 + \sqrt{5})$	$\frac{25-3\sqrt{5}}{1160}$	$-\frac{17}{440} (-5 + \sqrt{5})$	0	$\frac{25+3\sqrt{5}}{1160}$	$\frac{12}{77}$
$\frac{4533}{11165}$	$\frac{1}{44} (7 + 3\sqrt{5})$	$\frac{1}{580} (25 - 3\sqrt{5})$	$\frac{1}{44} (7 - 3\sqrt{5})$	$\frac{1}{20}$	$\frac{1}{580} (25 + 3\sqrt{5})$	$\frac{43}{308}$
$\frac{878}{2233}$	$\frac{1}{440} (85 + 31\sqrt{5})$	$\frac{45-17\sqrt{5}}{1160}$	$\frac{1}{440} (85 - 31\sqrt{5})$	0	$\frac{45+17\sqrt{5}}{1160}$	$\frac{1}{7}$
$\frac{124}{319}$	$\frac{17}{88} + \frac{3}{8\sqrt{5}}$	$\frac{25-3\sqrt{5}}{1160}$	$\frac{17}{88} - \frac{3}{8\sqrt{5}}$	0	$\frac{25+3\sqrt{5}}{1160}$	$\frac{2}{11}$

orderedroots[minipoly[chisub]]

$\{-5, 2 - \sqrt{5}, 6 - \sqrt{5}, 2 + \sqrt{5}, 5, 6 + \sqrt{5}, 9\}$

orderedroots[(x - 9) (x^2 - 4 x - 1) (x^2 - 12 x + 31)]

$\{2 - \sqrt{5}, 6 - \sqrt{5}, 2 + \sqrt{5}, 6 + \sqrt{5}, 9\}$

combinationsminipoly = {};

```

For[i = 1, i ≤ Length[listmod128], i++,
  AppendTo[combinationsminpoly, MinimalPolynomial[
    -4 (4 + √5) * Sqrt[anglesquaredsub[[8, 2]] * Sqrt[anglesquaredsub[[i, 2]] +
    4 (4 - 3 √5) * Sqrt[anglesquaredsub[[8, 3]] * Sqrt[anglesquaredsub[[i, 3]] +
    4 (4 - √5) * Sqrt[anglesquaredsub[[8, 4]] * Sqrt[anglesquaredsub[[i, 4]] +
    4 (4 + 3 √5) * Sqrt[anglesquaredsub[[8, 6]] * Sqrt[anglesquaredsub[[i, 6]] +
    56 * Sqrt[anglesquaredsub[[8, 7]] * Sqrt[anglesquaredsub[[i, 7]], x]]
  ]
]

For[i = 1, i ≤ Length[listmod128], i++,
  AppendTo[combinationsminpoly, MinimalPolynomial[
    -4 (4 + √5) * Sqrt[anglesquaredsub[[8, 2]] * Sqrt[anglesquaredsub[[i, 2]] +
    4 (4 - 3 √5) * Sqrt[anglesquaredsub[[8, 3]] * Sqrt[anglesquaredsub[[i, 3]] +
    4 (4 - √5) * Sqrt[anglesquaredsub[[8, 4]] * Sqrt[anglesquaredsub[[i, 4]] +
    4 (4 + 3 √5) * Sqrt[anglesquaredsub[[8, 6]] * Sqrt[anglesquaredsub[[i, 6]] -
    56 * Sqrt[anglesquaredsub[[8, 7]] * Sqrt[anglesquaredsub[[i, 7]], x]]
  ]
]

For[i = 1, i ≤ Length[listmod128], i++,
  AppendTo[combinationsminpoly, MinimalPolynomial[
    -4 (4 + √5) * Sqrt[anglesquaredsub[[8, 2]] * Sqrt[anglesquaredsub[[i, 2]] +
    4 (4 - 3 √5) * Sqrt[anglesquaredsub[[8, 3]] * Sqrt[anglesquaredsub[[i, 3]] +
    4 (4 - √5) * Sqrt[anglesquaredsub[[8, 4]] * Sqrt[anglesquaredsub[[i, 4]] -
    4 (4 + 3 √5) * Sqrt[anglesquaredsub[[8, 6]] * Sqrt[anglesquaredsub[[i, 6]] +
    56 * Sqrt[anglesquaredsub[[8, 7]] * Sqrt[anglesquaredsub[[i, 7]], x]]
  ]
]

For[i = 1, i ≤ Length[listmod128], i++,
  AppendTo[combinationsminpoly, MinimalPolynomial[
    -4 (4 + √5) * Sqrt[anglesquaredsub[[8, 2]] * Sqrt[anglesquaredsub[[i, 2]] +
    4 (4 - 3 √5) * Sqrt[anglesquaredsub[[8, 3]] * Sqrt[anglesquaredsub[[i, 3]] +
    4 (4 - √5) * Sqrt[anglesquaredsub[[8, 4]] * Sqrt[anglesquaredsub[[i, 4]] -
    4 (4 + 3 √5) * Sqrt[anglesquaredsub[[8, 6]] * Sqrt[anglesquaredsub[[i, 6]] -
    56 * Sqrt[anglesquaredsub[[8, 7]] * Sqrt[anglesquaredsub[[i, 7]], x]]
  ]
]

```

```

For[i = 1, i ≤ Length[listmod128], i++,
  AppendTo[combinationsminpoly, MinimalPolynomial[
    -4 (4 + √5) * Sqrt[anglesquaredsub[[8, 2]]] * Sqrt[anglesquaredsub[[i, 2]]] +
    4 (4 - 3 √5) * Sqrt[anglesquaredsub[[8, 3]]] * Sqrt[anglesquaredsub[[i, 3]]] -
    4 (4 - √5) * Sqrt[anglesquaredsub[[8, 4]]] * Sqrt[anglesquaredsub[[i, 4]]] +
    4 (4 + 3 √5) * Sqrt[anglesquaredsub[[8, 6]]] * Sqrt[anglesquaredsub[[i, 6]]] +
    56 * Sqrt[anglesquaredsub[[8, 7]]] * Sqrt[anglesquaredsub[[i, 7]]], x]]
]

For[i = 1, i ≤ Length[listmod128], i++,
  AppendTo[combinationsminpoly, MinimalPolynomial[
    -4 (4 + √5) * Sqrt[anglesquaredsub[[8, 2]]] * Sqrt[anglesquaredsub[[i, 2]]] +
    4 (4 - 3 √5) * Sqrt[anglesquaredsub[[8, 3]]] * Sqrt[anglesquaredsub[[i, 3]]] -
    4 (4 - √5) * Sqrt[anglesquaredsub[[8, 4]]] * Sqrt[anglesquaredsub[[i, 4]]] +
    4 (4 + 3 √5) * Sqrt[anglesquaredsub[[8, 6]]] * Sqrt[anglesquaredsub[[i, 6]]] -
    56 * Sqrt[anglesquaredsub[[8, 7]]] * Sqrt[anglesquaredsub[[i, 7]]], x]]
]

For[i = 1, i ≤ Length[listmod128], i++,
  AppendTo[combinationsminpoly, MinimalPolynomial[
    -4 (4 + √5) * Sqrt[anglesquaredsub[[8, 2]]] * Sqrt[anglesquaredsub[[i, 2]]] +
    4 (4 - 3 √5) * Sqrt[anglesquaredsub[[8, 3]]] * Sqrt[anglesquaredsub[[i, 3]]] -
    4 (4 - √5) * Sqrt[anglesquaredsub[[8, 4]]] * Sqrt[anglesquaredsub[[i, 4]]] -
    4 (4 + 3 √5) * Sqrt[anglesquaredsub[[8, 6]]] * Sqrt[anglesquaredsub[[i, 6]]] +
    56 * Sqrt[anglesquaredsub[[8, 7]]] * Sqrt[anglesquaredsub[[i, 7]]], x]]
]

For[i = 1, i ≤ Length[listmod128], i++,
  AppendTo[combinationsminpoly, MinimalPolynomial[
    -4 (4 + √5) * Sqrt[anglesquaredsub[[8, 2]]] * Sqrt[anglesquaredsub[[i, 2]]] +
    4 (4 - 3 √5) * Sqrt[anglesquaredsub[[8, 3]]] * Sqrt[anglesquaredsub[[i, 3]]] -
    4 (4 - √5) * Sqrt[anglesquaredsub[[8, 4]]] * Sqrt[anglesquaredsub[[i, 4]]] -
    4 (4 + 3 √5) * Sqrt[anglesquaredsub[[8, 6]]] * Sqrt[anglesquaredsub[[i, 6]]] -
    56 * Sqrt[anglesquaredsub[[8, 7]]] * Sqrt[anglesquaredsub[[i, 7]]], x]]
]

```

```

For[i = 1, i ≤ Length[listmod128], i++,
  AppendTo[combinationsminpoly, MinimalPolynomial[
    -4 (4 + √5) * Sqrt[anglesquaredsub[[8, 2]]] * Sqrt[anglesquaredsub[[i, 2]]] -
    4 (4 - 3 √5) * Sqrt[anglesquaredsub[[8, 3]]] * Sqrt[anglesquaredsub[[i, 3]]] +
    4 (4 - √5) * Sqrt[anglesquaredsub[[8, 4]]] * Sqrt[anglesquaredsub[[i, 4]]] +
    4 (4 + 3 √5) * Sqrt[anglesquaredsub[[8, 6]]] * Sqrt[anglesquaredsub[[i, 6]]] +
    56 * Sqrt[anglesquaredsub[[8, 7]]] * Sqrt[anglesquaredsub[[i, 7]]], x]]
]

For[i = 1, i ≤ Length[listmod128], i++,
  AppendTo[combinationsminpoly, MinimalPolynomial[
    -4 (4 + √5) * Sqrt[anglesquaredsub[[8, 2]]] * Sqrt[anglesquaredsub[[i, 2]]] -
    4 (4 - 3 √5) * Sqrt[anglesquaredsub[[8, 3]]] * Sqrt[anglesquaredsub[[i, 3]]] +
    4 (4 - √5) * Sqrt[anglesquaredsub[[8, 4]]] * Sqrt[anglesquaredsub[[i, 4]]] +
    4 (4 + 3 √5) * Sqrt[anglesquaredsub[[8, 6]]] * Sqrt[anglesquaredsub[[i, 6]]] -
    56 * Sqrt[anglesquaredsub[[8, 7]]] * Sqrt[anglesquaredsub[[i, 7]]], x]]
]

For[i = 1, i ≤ Length[listmod128], i++,
  AppendTo[combinationsminpoly, MinimalPolynomial[
    -4 (4 + √5) * Sqrt[anglesquaredsub[[8, 2]]] * Sqrt[anglesquaredsub[[i, 2]]] -
    4 (4 - 3 √5) * Sqrt[anglesquaredsub[[8, 3]]] * Sqrt[anglesquaredsub[[i, 3]]] +
    4 (4 - √5) * Sqrt[anglesquaredsub[[8, 4]]] * Sqrt[anglesquaredsub[[i, 4]]] -
    4 (4 + 3 √5) * Sqrt[anglesquaredsub[[8, 6]]] * Sqrt[anglesquaredsub[[i, 6]]] +
    56 * Sqrt[anglesquaredsub[[8, 7]]] * Sqrt[anglesquaredsub[[i, 7]]], x]]
]

For[i = 1, i ≤ Length[listmod128], i++,
  AppendTo[combinationsminpoly, MinimalPolynomial[
    -4 (4 + √5) * Sqrt[anglesquaredsub[[8, 2]]] * Sqrt[anglesquaredsub[[i, 2]]] -
    4 (4 - 3 √5) * Sqrt[anglesquaredsub[[8, 3]]] * Sqrt[anglesquaredsub[[i, 3]]] +
    4 (4 - √5) * Sqrt[anglesquaredsub[[8, 4]]] * Sqrt[anglesquaredsub[[i, 4]]] -
    4 (4 + 3 √5) * Sqrt[anglesquaredsub[[8, 6]]] * Sqrt[anglesquaredsub[[i, 6]]] -
    56 * Sqrt[anglesquaredsub[[8, 7]]] * Sqrt[anglesquaredsub[[i, 7]]], x]]
]

```

```

For[i = 1, i ≤ Length[listmod128], i++,
  AppendTo[combinationsminpoly, MinimalPolynomial[
    -4 (4 + √5) * Sqrt[anglesquaredsub[[8, 2]] * Sqrt[anglesquaredsub[[i, 2]] -
    4 (4 - 3 √5) * Sqrt[anglesquaredsub[[8, 3]] * Sqrt[anglesquaredsub[[i, 3]] -
    4 (4 - √5) * Sqrt[anglesquaredsub[[8, 4]] * Sqrt[anglesquaredsub[[i, 4]] +
    4 (4 + 3 √5) * Sqrt[anglesquaredsub[[8, 6]] * Sqrt[anglesquaredsub[[i, 6]] +
    56 * Sqrt[anglesquaredsub[[8, 7]] * Sqrt[anglesquaredsub[[i, 7]], x]]
  ]
]

For[i = 1, i ≤ Length[listmod128], i++,
  AppendTo[combinationsminpoly, MinimalPolynomial[
    -4 (4 + √5) * Sqrt[anglesquaredsub[[8, 2]] * Sqrt[anglesquaredsub[[i, 2]] -
    4 (4 - 3 √5) * Sqrt[anglesquaredsub[[8, 3]] * Sqrt[anglesquaredsub[[i, 3]] -
    4 (4 - √5) * Sqrt[anglesquaredsub[[8, 4]] * Sqrt[anglesquaredsub[[i, 4]] +
    4 (4 + 3 √5) * Sqrt[anglesquaredsub[[8, 6]] * Sqrt[anglesquaredsub[[i, 6]] -
    56 * Sqrt[anglesquaredsub[[8, 7]] * Sqrt[anglesquaredsub[[i, 7]], x]]
  ]
]

For[i = 1, i ≤ Length[listmod128], i++,
  AppendTo[combinationsminpoly, MinimalPolynomial[
    -4 (4 + √5) * Sqrt[anglesquaredsub[[8, 2]] * Sqrt[anglesquaredsub[[i, 2]] -
    4 (4 - 3 √5) * Sqrt[anglesquaredsub[[8, 3]] * Sqrt[anglesquaredsub[[i, 3]] -
    4 (4 - √5) * Sqrt[anglesquaredsub[[8, 4]] * Sqrt[anglesquaredsub[[i, 4]] -
    4 (4 + 3 √5) * Sqrt[anglesquaredsub[[8, 6]] * Sqrt[anglesquaredsub[[i, 6]] +
    56 * Sqrt[anglesquaredsub[[8, 7]] * Sqrt[anglesquaredsub[[i, 7]], x]]
  ]
]

For[i = 1, i ≤ Length[listmod128], i++,
  AppendTo[combinationsminpoly, MinimalPolynomial[
    -4 (4 + √5) * Sqrt[anglesquaredsub[[8, 2]] * Sqrt[anglesquaredsub[[i, 2]] -
    4 (4 - 3 √5) * Sqrt[anglesquaredsub[[8, 3]] * Sqrt[anglesquaredsub[[i, 3]] -
    4 (4 - √5) * Sqrt[anglesquaredsub[[8, 4]] * Sqrt[anglesquaredsub[[i, 4]] -
    4 (4 + 3 √5) * Sqrt[anglesquaredsub[[8, 6]] * Sqrt[anglesquaredsub[[i, 6]] -
    56 * Sqrt[anglesquaredsub[[8, 7]] * Sqrt[anglesquaredsub[[i, 7]], x]]
  ]
]

```

```

Length[combinationsminpoly]
1984

integercombination = {};

For[i = 1, i ≤ Length[combinationsminpoly], i++,
  If[combinationsminpoly[[i]] - x ∈ Integers, AppendTo[integercombination, i]]]

integercombination
{286, 392, 504, 687, 772, 896, 1030, 1136, 1516, 1640, 1744, 1927}

Mod[integercombination, 124]
{38, 20, 8, 67, 28, 28, 38, 20, 28, 28, 8, 67}

integercombination = Sort[DeleteDuplicates[Mod[integercombination, 124]]]
{8, 20, 28, 38, 67}

refinedlistsub = listmod128[[integercombination]]
{-554 + 387 x + 1065 x2 - 842 x3 + 224 x4 - 25 x5 + x6,
 -1742 + 1239 x + 877 x2 - 830 x3 + 224 x4 - 25 x5 + x6,
 (-9 + x) (-5 + x) (-1 + x) (34 + 15 x - 10 x2 + x3),
 (-5 + x) (-1 - 8 x + x2) (14 + 29 x - 12 x2 + x3),
 (-58 + 55 x - 14 x2 + x3) (59 + 15 x - 11 x2 + x3) }

refinedlistsub * mu[chisub] // Factor
{(-5 + x)8 (5 + x)13 (-554 + 387 x + 1065 x2 - 842 x3 + 224 x4 - 25 x5 + x6),
 (-5 + x)8 (5 + x)13 (-1742 + 1239 x + 877 x2 - 830 x3 + 224 x4 - 25 x5 + x6),
 (-9 + x) (-5 + x)9 (-1 + x) (5 + x)13 (34 + 15 x - 10 x2 + x3),
 (-5 + x)9 (5 + x)13 (-1 - 8 x + x2) (14 + 29 x - 12 x2 + x3),
 (-5 + x)8 (5 + x)13 (-58 + 55 x - 14 x2 + x3) (59 + 15 x - 11 x2 + x3) }

refinedAsub = CoefficientList[refinedlistsub, x]
{{-554, 387, 1065, -842, 224, -25, 1},
 {-1742, 1239, 877, -830, 224, -25, 1}, {-1530, 1331, 825, -826, 224, -25, 1},
 {70, 691, 889, -826, 224, -25, 1}, {-3422, 2375, 637, -814, 224, -25, 1}}

refinedAsub // MatrixForm

$$\begin{pmatrix} -554 & 387 & 1065 & -842 & 224 & -25 & 1 \\ -1742 & 1239 & 877 & -830 & 224 & -25 & 1 \\ -1530 & 1331 & 825 & -826 & 224 & -25 & 1 \\ 70 & 691 & 889 & -826 & 224 & -25 & 1 \\ -3422 & 2375 & 637 & -814 & 224 & -25 & 1 \end{pmatrix}$$


Solve[Array[n, 5].refinedAsub == gsub, Array[n, 5]]

$$\left\{ \left\{ n[1] \rightarrow \frac{39}{2}, n[2] \rightarrow 2, n[3] \rightarrow \frac{9}{4}, n[4] \rightarrow \frac{1}{4}, n[5] \rightarrow 4 \right\} \right\}$$


```


$$\text{chi} = (-9 + x)^2 (-5 + x)^{10} (-4 + x) (-3 + x) (5 + x)^{15}$$

$$(-9 + x)^2 (-5 + x)^{10} (-4 + x) (-3 + x) (5 + x)^{15}$$

feasibleinterlacingpolylist[chi]

$$\left\{ (31 - 12x + x^2) (-1 - 4x + x^2), (-5 + x) (-3 + x) (-1 - 8x + x^2), \right.$$

$$(-3 + x) (-11 + 39x - 13x^2 + x^3), (-3 + x) (-3 + 39x - 13x^2 + x^3),$$

$$\left. (-5 + x) (11 + 23x - 11x^2 + x^3), (-5 + x) (19 + 23x - 11x^2 + x^3) \right\}$$

$$\text{reducedlist} = \left\{ (-5 + x) (-3 + x) (-1 - 8x + x^2), \right.$$

$$(-3 + x) (-11 + 39x - 13x^2 + x^3), (-3 + x) (-3 + 39x - 13x^2 + x^3),$$

$$\left. (-5 + x) (11 + 23x - 11x^2 + x^3), (-5 + x) (19 + 23x - 11x^2 + x^3) \right\}$$

$$\left\{ (-5 + x) (-3 + x) (-1 - 8x + x^2), \right.$$

$$(-3 + x) (-11 + 39x - 13x^2 + x^3), (-3 + x) (-3 + 39x - 13x^2 + x^3),$$

$$\left. (-5 + x) (11 + 23x - 11x^2 + x^3), (-5 + x) (19 + 23x - 11x^2 + x^3) \right\}$$

reducedA = CoefficientList[reducedlist, x]

$$\{\{-15, -112, 78, -16, 1\}, \{33, -128, 78, -16, 1\},$$

$$\{9, -120, 78, -16, 1\}, \{-55, -104, 78, -16, 1\}, \{-95, -96, 78, -16, 1\}\}$$

g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]

$$\{525, -3600, 2262, -464, 29\}$$

allsoln = Array[n, 5] /. Solve[n[1] ≥ 0 && n[2] ≥ 0 && n[3] ≥ 0 &&

n[4] ≥ 0 && n[5] ≥ 0 && Array[n, 5].reducedA == g, Array[n, 5], Integers]

$$\{\{0, 24, 2, 0, 3\}, \{0, 25, 0, 2, 2\}, \{1, 25, 0, 0, 3\}\}$$

anglesquared = anglesquaredmat[chi, reducedlist] // FullSimplify;

anglesquared // MatrixForm

$$\begin{pmatrix} \frac{32}{63} & 0 & \frac{17}{45} & 0 & \frac{4}{35} \\ \frac{164}{315} & 0 & \frac{1}{45} & \frac{2}{5} & \frac{2}{35} \\ \frac{18}{35} & 0 & \frac{1}{5} & \frac{1}{5} & \frac{3}{35} \\ \frac{1}{2} & \frac{1}{6} & \frac{1}{5} & 0 & \frac{2}{15} \\ \frac{31}{63} & \frac{1}{3} & \frac{1}{45} & 0 & \frac{16}{105} \end{pmatrix}$$

chi

$$(-9 + x)^2 (-5 + x)^{10} (-4 + x) (-3 + x) (5 + x)^{15}$$

$$(-9 + x) (-5 + x) (5 + x) /. x \rightarrow 3$$

$$(-9 + x) \quad (-5 + x) \quad (5 + x) \quad / \cdot \quad x \rightarrow 4$$

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$$v = \begin{pmatrix} \text{Sqrt}\left[\frac{1}{45}\right] \\ \text{Sqrt}\left[\frac{1}{5}\right] \\ \text{Sqrt}\left[\frac{1}{5}\right] \\ \text{Sqrt}\left[\frac{1}{45}\right] \\ \text{Sqrt}\left[\frac{1}{45}\right] \\ \text{Sqrt}\left[\frac{1}{45}\right] \end{pmatrix}; u = \begin{pmatrix} 0 \\ -\text{Sqrt}\left[\frac{1}{3}\right] \\ -\text{Sqrt}\left[\frac{1}{3}\right] \\ \text{Sqrt}\left[\frac{1}{3}\right] \end{pmatrix}$$

Total[u * u]

 $\{\mathbf{1}\}$

Total[v * v]

{1}

Total[u * v]

$\left\{-\frac{1}{3\sqrt{15}}\right\}$

[illegible]

Total[u * u]

 $\{\mathbf{1}\}$

Total[v * v]

 $\{\mathbf{1}\}$

Total[u * u]

 $\{1\}$

Total[v * v]

$$\{1\}$$

Total[u * v]

 $\{0\}$

```
96 u.Transpose[u] + 45 v.Transpose[v] // MatrixForm
```

[illegible]

Total[u * v]

 $\{0\}$

```
96 u.Transpose[u] + 45 v.Transpose[v] // MatrixForm
```

[illegible]