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feasiblecharpolylist[29, (x + 5)^15 (x - 5)^4]

{ (-11 + x) (-5 + x)^8 (-4 + x), (-5 + x)^7 (-216 + 119 x - 20 x^2 + x^3),
  (-5 + x)^7 (-212 + 119 x - 20 x^2 + x^3), (-5 + x)^6 (-4 + x) (-267 + 135 x - 21 x^2 + x^3),
  (-5 + x)^7 (-208 + 119 x - 20 x^2 + x^3), (-5 + x)^6 (1048 - 803 x + 219 x^2 - 25 x^3 + x^4),
  (-5 + x)^7 (-3 + x) (68 - 17 x + x^2), (-5 + x)^6 (1028 - 799 x + 219 x^2 - 25 x^3 + x^4),
  (-7 + x) (-5 + x)^6 (-4 + x) (37 - 14 x + x^2),
  (-5 + x)^6 (992 - 795 x + 219 x^2 - 25 x^3 + x^4), (-5 + x)^7 (-200 + 119 x - 20 x^2 + x^3),
  (-5 + x)^5 (-5056 + 4983 x - 1890 x^2 + 344 x^3 - 30 x^4 + x^5),
  (-7 + x) (-5 + x)^6 (-3 + x) (48 - 15 x + x^2), (-5 + x)^6 (1016 - 795 x + 219 x^2 - 25 x^3 + x^4),
  (-5 + x)^6 (972 - 791 x + 219 x^2 - 25 x^3 + x^4),
  (-5 + x)^5 (-4916 + 4935 x - 1886 x^2 + 344 x^3 - 30 x^4 + x^5),
  (-7 + x) (-5 + x)^7 (28 - 13 x + x^2), (-7 + x) (-5 + x)^5 (-4 + x) (-3 + x) (59 - 16 x + x^2),
  (-5 + x)^6 (988 - 791 x + 219 x^2 - 25 x^3 + x^4),
  (-5 + x)^5 (-4996 + 4951 x - 1886 x^2 + 344 x^3 - 30 x^4 + x^5),
  (-5 + x)^6 (-3 + x) (-332 + 153 x - 22 x^2 + x^3), (-5 + x)^6 (-4 + x) (-251 + 135 x - 21 x^2 + x^3),
  (-5 + x)^5 (-4 + x) (41 - 14 x + x^2) (31 - 12 x + x^2),
  (-5 + x)^6 (59 - 16 x + x^2) (16 - 9 x + x^2), (-7 + x) (-5 + x)^6 (-136 + 93 x - 18 x^2 + x^3),
  (-7 + x) (-5 + x)^5 (688 - 601 x + 183 x^2 - 23 x^3 + x^4), (-5 + x)^7 (-192 + 119 x - 20 x^2 + x^3),
  (-7 + x) (-5 + x)^5 (-3 + x) (-232 + 123 x - 20 x^2 + x^3),
  (-5 + x)^5 (-4856 + 4903 x - 1882 x^2 + 344 x^3 - 30 x^4 + x^5),
  (-5 + x)^6 (968 - 787 x + 219 x^2 - 25 x^3 + x^4),
  (-5 + x)^5 (-3 + x) (1632 - 1093 x + 263 x^2 - 27 x^3 + x^4),
  (-5 + x)^6 (976 - 787 x + 219 x^2 - 25 x^3 + x^4), (-8 + x) (-5 + x)^6 (-3 + x) (41 - 14 x + x^2),
  (-5 + x)^6 (32 - 13 x + x^2) (31 - 12 x + x^2), (-7 + x) (-5 + x)^6 (-132 + 93 x - 18 x^2 + x^3),
  (-7 + x) (-5 + x)^5 (668 - 597 x + 183 x^2 - 23 x^3 + x^4),
  (-5 + x)^6 (932 - 783 x + 219 x^2 - 25 x^3 + x^4),
  (-7 + x) (-5 + x)^5 (-4 + x) (-169 + 107 x - 19 x^2 + x^3),
  (-5 + x)^5 (-4716 + 4855 x - 1878 x^2 + 344 x^3 - 30 x^4 + x^5),
  (-5 + x)^7 (-188 + 119 x - 20 x^2 + x^3), (-7 + x) (-5 + x)^5 (-3 + x) (-228 + 123 x - 20 x^2 + x^3),
  (-5 + x)^5 (-4772 + 4863 x - 1878 x^2 + 344 x^3 - 30 x^4 + x^5),
  (-5 + x)^5 (41 - 14 x + x^2) (-116 + 79 x - 16 x^2 + x^3),
  (-5 + x)^6 (948 - 783 x + 219 x^2 - 25 x^3 + x^4),
  (-7 + x)^2 (-5 + x)^4 (-4 + x) (-3 + x) (41 - 14 x + x^2),
  (-5 + x)^5 (-3 + x) (1604 - 1089 x + 263 x^2 - 27 x^3 + x^4),
  (-5 + x)^5 (-4 + x) (1199 - 918 x + 240 x^2 - 26 x^3 + x^4),
  (-5 + x)^6 (956 - 783 x + 219 x^2 - 25 x^3 + x^4),
  (-5 + x)^5 (-3 + x) (52 - 15 x + x^2) (31 - 12 x + x^2),
  (-5 + x)^6 (964 - 783 x + 219 x^2 - 25 x^3 + x^4),
  (-5 + x)^4 (-4 + x) (31 - 12 x + x^2) (-197 + 111 x - 19 x^2 + x^3),
  (-9 + x)^2 (-5 + x)^6 (-4 + x) (-3 + x), (-7 + x) (-5 + x)^6 (-128 + 93 x - 18 x^2 + x^3),
  (-7 + x) (-5 + x)^5 (648 - 593 x + 183 x^2 - 23 x^3 + x^4),
  (-5 + x)^6 (904 - 779 x + 219 x^2 - 25 x^3 + x^4),

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$$\begin{aligned}
& (-7 + x) (-5 + x)^5 (41 - 14x + x^2) (16 - 9x + x^2), \\
& (-5 + x)^5 (-4576 + 4807x - 1874x^2 + 344x^3 - 30x^4 + x^5), \\
& (-5 + x)^6 (912 - 779x + 219x^2 - 25x^3 + x^4), \\
& (-7 + x) (-5 + x)^4 (-3 + x) (1112 - 839x + 223x^2 - 25x^3 + x^4), \\
& (-7 + x) (-5 + x)^5 (664 - 593x + 183x^2 - 23x^3 + x^4), \\
& (-5 + x)^5 (-4632 + 4815x - 1874x^2 + 344x^3 - 30x^4 + x^5), \\
& (-5 + x)^5 (-4616 + 4815x - 1874x^2 + 344x^3 - 30x^4 + x^5), \\
& (-8 + x) (-5 + x)^7 (23 - 12x + x^2), \quad (-7 + x)^2 (-5 + x)^5 (-3 + x) (32 - 13x + x^2), \\
& (-5 + x)^5 (-4688 + 4823x - 1874x^2 + 344x^3 - 30x^4 + x^5), \\
& (-5 + x)^5 (-4672 + 4823x - 1874x^2 + 344x^3 - 30x^4 + x^5), \\
& (-5 + x)^5 (-4656 + 4823x - 1874x^2 + 344x^3 - 30x^4 + x^5), \\
& (-5 + x)^6 (928 - 779x + 219x^2 - 25x^3 + x^4), \\
& (-7 + x) (-5 + x)^4 (-3 + x) (1128 - 839x + 223x^2 - 25x^3 + x^4), \\
& (-8 + x) (-5 + x)^5 (-3 + x) (-197 + 111x - 19x^2 + x^3), \\
& (-5 + x)^5 (31 - 12x + x^2) (-152 + 97x - 18x^2 + x^3), \\
& (-5 + x)^5 (-4696 + 4831x - 1874x^2 + 344x^3 - 30x^4 + x^5), \\
& (-9 + x) (-5 + x)^6 (-104 + 75x - 16x^2 + x^3), \\
& (-5 + x)^4 (-3 + x) (31 - 12x + x^2) (-256 + 127x - 20x^2 + x^3), \\
& (-9 + x) (-5 + x)^5 (-3 + x) (-176 + 101x - 18x^2 + x^3), \\
& (-7 + x) (-5 + x)^6 (-124 + 93x - 18x^2 + x^3), \\
& (-7 + x) (-5 + x)^5 (628 - 589x + 183x^2 - 23x^3 + x^4), \\
& (-5 + x)^6 (876 - 775x + 219x^2 - 25x^3 + x^4), \\
& (-7 + x) (-5 + x)^4 (-3196 + 3581x - 1504x^2 + 298x^3 - 28x^4 + x^5), \\
& (-7 + x) (-5 + x)^5 (636 - 589x + 183x^2 - 23x^3 + x^4), \\
& (-5 + x)^5 (-4436 + 4759x - 1870x^2 + 344x^3 - 30x^4 + x^5), \\
& (-5 + x)^6 (52 - 15x + x^2) (17 - 10x + x^2), \\
& (-7 + x) (-5 + x)^4 (-3236 + 3589x - 1504x^2 + 298x^3 - 28x^4 + x^5), \\
& (-7 + x)^2 (-5 + x)^5 (-4 + x) (23 - 12x + x^2), \\
& (-5 + x)^5 (-4492 + 4767x - 1870x^2 + 344x^3 - 30x^4 + x^5), \\
& (-5 + x)^5 (-4476 + 4767x - 1870x^2 + 344x^3 - 30x^4 + x^5), \\
& (-5 + x)^6 (892 - 775x + 219x^2 - 25x^3 + x^4), \quad (-7 + x)^2 (-5 + x)^4 (-3 + x)^2 (52 - 15x + x^2), \\
& (-7 + x) (-5 + x)^5 (652 - 589x + 183x^2 - 23x^3 + x^4), \\
& (-5 + x)^4 (-197 + 111x - 19x^2 + x^3) (-116 + 79x - 16x^2 + x^3), \\
& (-5 + x)^5 (-4548 + 4775x - 1870x^2 + 344x^3 - 30x^4 + x^5), \\
& (-5 + x)^5 (-4532 + 4775x - 1870x^2 + 344x^3 - 30x^4 + x^5), \\
& (-5 + x)^5 (-4516 + 4775x - 1870x^2 + 344x^3 - 30x^4 + x^5), \quad (-9 + x) (-5 + x)^7 (20 - 11x + x^2), \\
& (-7 + x)^2 (-5 + x)^3 (-4 + x) (-3 + x) (-197 + 111x - 19x^2 + x^3), \\
& (-7 + x) (-5 + x)^5 (-3 + x) (-220 + 123x - 20x^2 + x^3), \\
& (-7 + x) (-5 + x)^4 (-4 + x) (821 - 696x + 202x^2 - 24x^3 + x^4), \\
& (-5 + x)^5 (-4604 + 4783x - 1870x^2 + 344x^3 - 30x^4 + x^5), \\
& (-5 + x)^5 (31 - 12x + x^2) (-148 + 97x - 18x^2 + x^3), \\
& (-9 + x) (-5 + x)^5 (-4 + x) (-127 + 87x - 17x^2 + x^3),
\end{aligned}$$

$$\begin{aligned}
& (-7+x) (-5+x)^4 (-3+x) (1108 - 835x + 223x^2 - 25x^3 + x^4), \\
& (-5+x)^4 (31 - 12x + x^2) (748 - 633x + 187x^2 - 23x^3 + x^4), \\
& (-9+x) (-5+x)^5 (-3+x) (-172 + 101x - 18x^2 + x^3), \\
& (-9+x) (-7+x) (-5+x)^4 (-4+x) (-3+x) (31 - 12x + x^2), \\
& (-5+x)^3 (-4+x) (31 - 12x + x^2)^3, (-7+x) (-5+x)^6 (-120 + 93x - 18x^2 + x^3), \\
& (-7+x) (-5+x)^5 (608 - 585x + 183x^2 - 23x^3 + x^4), \\
& (-5+x)^6 (848 - 771x + 219x^2 - 25x^3 + x^4), \\
& (-7+x) (-5+x)^4 (-3096 + 3541x - 1500x^2 + 298x^3 - 28x^4 + x^5), \\
& (-7+x)^2 (-5+x)^5 (-88 + 71x - 16x^2 + x^3), \\
& (-5+x)^5 (-4296 + 4711x - 1866x^2 + 344x^3 - 30x^4 + x^5), \\
& (-8+x) (-5+x)^6 (-107 + 83x - 17x^2 + x^3), \\
& (-7+x) (-5+x)^4 (16 - 9x + x^2) (-197 + 111x - 19x^2 + x^3), \\
& (-7+x)^2 (-5+x)^4 (448 - 443x + 151x^2 - 21x^3 + x^4), \\
& (-7+x) (-5+x)^5 (624 - 585x + 183x^2 - 23x^3 + x^4), \\
& (-5+x)^5 (17 - 10x + x^2) (-256 + 127x - 20x^2 + x^3), \\
& (-5+x)^5 (-4336 + 4719x - 1866x^2 + 344x^3 - 30x^4 + x^5), \\
& (-9+x) (-5+x)^6 (-96 + 75x - 16x^2 + x^3), \\
& (-7+x)^2 (-5+x)^4 (-3+x) (-152 + 97x - 18x^2 + x^3), \\
& (-7+x) (-5+x)^4 (-3176 + 3557x - 1500x^2 + 298x^3 - 28x^4 + x^5), \\
& (-7+x) (-5+x)^5 (632 - 585x + 183x^2 - 23x^3 + x^4), \\
& (-5+x)^4 (22152 - 28059x + 14057x^2 - 3586x^3 + 494x^4 - 35x^5 + x^6), \\
& (-8+x) (-5+x)^5 (551 - 522x + 168x^2 - 22x^3 + x^4), \\
& (-9+x) (-5+x)^5 (488 - 471x + 155x^2 - 21x^3 + x^4), \\
& (-7+x)^2 (-5+x)^3 (-3+x)^2 (-256 + 127x - 20x^2 + x^3), \\
& (-7+x) (-5+x)^4 (-3+x) (1072 - 831x + 223x^2 - 25x^3 + x^4), \\
& (-7+x) (-5+x)^5 (640 - 585x + 183x^2 - 23x^3 + x^4), \\
& (-5+x)^4 (22432 - 28155x + 14065x^2 - 3586x^3 + 494x^4 - 35x^5 + x^6), \\
& (-9+x) (-5+x)^5 (31 - 12x + x^2) (16 - 9x + x^2), \\
& (-5+x)^4 (-176 + 101x - 18x^2 + x^3) (-127 + 87x - 17x^2 + x^3), \\
& (-7+x) (-5+x)^3 (-3+x) (-5416 + 5235x - 1946x^2 + 348x^3 - 30x^4 + x^5), \\
& (-9+x) (-8+x) (-7+x) (-5+x)^5 (-3+x)^2, \\
& (-7+x) (-5+x)^4 (31 - 12x + x^2) (-104 + 75x - 16x^2 + x^3), \\
& (-7+x) (-5+x)^3 (-3+x) (31 - 12x + x^2) (-176 + 101x - 18x^2 + x^3), \\
& (-5+x)^4 (31 - 12x + x^2) (736 - 629x + 187x^2 - 23x^3 + x^4), \\
& (-8+x) (-5+x)^4 (-3+x) (31 - 12x + x^2)^2, \\
& (-7+x) (-5+x)^5 (52 - 15x + x^2) (11 - 8x + x^2), \\
& (-7+x) (-5+x)^6 (-116 + 93x - 18x^2 + x^3), \\
& (-7+x) (-5+x)^4 (-2956 + 3493x - 1496x^2 + 298x^3 - 28x^4 + x^5), \\
& (-7+x)^2 (-5+x)^5 (-84 + 71x - 16x^2 + x^3), (-5+x)^6 (820 - 767x + 219x^2 - 25x^3 + x^4), \\
& (-7+x)^2 (-5+x)^4 (-4+x) (-107 + 83x - 17x^2 + x^3), \\
& (-7+x) (-5+x)^5 (596 - 581x + 183x^2 - 23x^3 + x^4), \\
& (-5+x)^5 (-4156 + 4663x - 1862x^2 + 344x^3 - 30x^4 + x^5),
\end{aligned}$$

$$\begin{aligned}
& (-9 + x) (-5 + x)^6 (-92 + 75 x - 16 x^2 + x^3), \\
& (-7 + x)^2 (-5 + x)^4 (436 - 439 x + 151 x^2 - 21 x^3 + x^4), \\
& (-7 + x) (-5 + x)^4 (-3036 + 3509 x - 1496 x^2 + 298 x^3 - 28 x^4 + x^5), \\
& (-7 + x) (-5 + x)^5 (604 - 581 x + 183 x^2 - 23 x^3 + x^4), \\
& (-5 + x)^4 (21172 - 27583 x + 13981 x^2 - 3582 x^3 + 494 x^4 - 35 x^5 + x^6), \\
& (-9 + x) (-5 + x)^5 (468 - 467 x + 155 x^2 - 21 x^3 + x^4), \\
& (-7 + x)^2 (-5 + x)^4 (-3 + x) (-148 + 97 x - 18 x^2 + x^3), \\
& (-7 + x)^2 (-5 + x)^3 (-4 + x) (551 - 522 x + 168 x^2 - 22 x^3 + x^4), \\
& (-7 + x) (-5 + x)^4 (-3092 + 3517 x - 1496 x^2 + 298 x^3 - 28 x^4 + x^5), \\
& (-7 + x) (-5 + x)^4 (-3076 + 3517 x - 1496 x^2 + 298 x^3 - 28 x^4 + x^5), \\
& (-9 + x) (-7 + x) (-5 + x)^5 (-4 + x) (17 - 10 x + x^2), \\
& (-5 + x)^4 (31 - 12 x + x^2) (692 - 625 x + 187 x^2 - 23 x^3 + x^4), \\
& (-7 + x)^2 (-5 + x)^3 (-3 + x) (748 - 633 x + 187 x^2 - 23 x^3 + x^4), \\
& (-7 + x) (-5 + x)^3 (15628 - 20757 x + 11005 x^2 - 2986 x^3 + 438 x^4 - 33 x^5 + x^6), \\
& (-9 + x) (-7 + x) (-5 + x)^4 (-3 + x) (-116 + 79 x - 16 x^2 + x^3), \\
& (-7 + x) (-5 + x)^4 (-3116 + 3525 x - 1496 x^2 + 298 x^3 - 28 x^4 + x^5), \\
& (-5 + x)^4 (-172 + 101 x - 18 x^2 + x^3) (-127 + 87 x - 17 x^2 + x^3), \\
& (-7 + x) (-5 + x)^5 (31 - 12 x + x^2) (20 - 11 x + x^2), \\
& (-9 + x) (-7 + x)^3 (-5 + x)^3 (-4 + x) (-3 + x)^2, \\
& (-7 + x) (-5 + x)^3 (-3 + x) (-5276 + 5187 x - 1942 x^2 + 348 x^3 - 30 x^4 + x^5), \\
& (-7 + x) (-5 + x)^3 (-4 + x) (31 - 12 x + x^2) (-127 + 87 x - 17 x^2 + x^3), \\
& (-5 + x)^4 (31 - 12 x + x^2) (708 - 625 x + 187 x^2 - 23 x^3 + x^4), \\
& (-7 + x) (-5 + x)^3 (-3 + x) (31 - 12 x + x^2) (-172 + 101 x - 18 x^2 + x^3), \\
& (-5 + x)^3 (31 - 12 x + x^2)^2 (-116 + 79 x - 16 x^2 + x^3), \\
& (-7 + x)^2 (-5 + x)^2 (-4 + x) (-3 + x) (31 - 12 x + x^2)^2, \\
& (-7 + x) (-5 + x)^5 (552 - 577 x + 183 x^2 - 23 x^3 + x^4), \\
& (-7 + x) (-5 + x)^4 (11 - 8 x + x^2) (-256 + 127 x - 20 x^2 + x^3), \\
& (-7 + x)^2 (-5 + x)^6 (16 - 11 x + x^2), (-5 + x)^5 (-3904 + 4599 x - 1858 x^2 + 344 x^3 - 30 x^4 + x^5), \\
& (-7 + x)^2 (-5 + x)^4 (408 - 435 x + 151 x^2 - 21 x^3 + x^4), \\
& (-7 + x) (-5 + x)^5 (568 - 577 x + 183 x^2 - 23 x^3 + x^4), \\
& (-9 + x) (-8 + x) (-5 + x)^6 (11 - 8 x + x^2), \\
& (-7 + x)^2 (-5 + x)^4 (416 - 435 x + 151 x^2 - 21 x^3 + x^4), \\
& (-7 + x) (-5 + x)^4 (-2896 + 3461 x - 1492 x^2 + 298 x^3 - 28 x^4 + x^5), \\
& (-9 + x) (-7 + x) (-5 + x)^5 (-64 + 57 x - 14 x^2 + x^3), \\
& (-5 + x)^5 (-4016 + 4615 x - 1858 x^2 + 344 x^3 - 30 x^4 + x^5), \\
& (-7 + x)^2 (-5 + x)^4 (424 - 435 x + 151 x^2 - 21 x^3 + x^4), \\
& (-9 + x) (-7 + x) (-5 + x)^4 (328 - 349 x + 127 x^2 - 19 x^3 + x^4), \\
& (-7 + x) (-5 + x)^4 (-2936 + 3469 x - 1492 x^2 + 298 x^3 - 28 x^4 + x^5), \\
& (-8 + x) (-7 + x) (-5 + x)^5 (-73 + 63 x - 15 x^2 + x^3), \\
& (-9 + x) (-7 + x)^2 (-5 + x)^4 (-3 + x) (16 - 9 x + x^2), \\
& (-7 + x)^2 (-5 + x)^3 (-2144 + 2607 x - 1190 x^2 + 256 x^3 - 26 x^4 + x^5), \\
& (-7 + x) (-5 + x)^4 (-3008 + 3477 x - 1492 x^2 + 298 x^3 - 28 x^4 + x^5),
\end{aligned}$$

$$\begin{aligned}
& (-7+x) (-5+x)^4 (17-10x+x^2) (-176+101x-18x^2+x^3), \\
& (-7+x) (-5+x)^4 (31-12x+x^2) (-96+75x-16x^2+x^3), \\
& (-7+x)^3 (-5+x)^3 (-3+x) (-104+75x-16x^2+x^3), \\
& (-7+x) (-5+x)^3 (15208-20473x+10945x^2-2982x^3+438x^4-33x^5+x^6), \\
& (-8+x) (-7+x) (-5+x)^4 (-3+x) (-127+87x-17x^2+x^3), \\
& (-7+x) (-5+x)^3 (31-12x+x^2) (488-471x+155x^2-21x^3+x^4), \\
& (-8+x) (-5+x)^5 (31-12x+x^2) (17-10x+x^2), \\
& (-7+x)^3 (-5+x)^2 (-3+x)^2 (-176+101x-18x^2+x^3), \\
& (-7+x)^2 (-5+x)^3 (-3+x) (736-629x+187x^2-23x^3+x^4), \\
& (-7+x) (-5+x)^3 (31-12x+x^2)^2 (16-9x+x^2), \\
& (-8+x) (-7+x)^2 (-5+x)^3 (-3+x)^2 (31-12x+x^2), \\
& (-7+x) (-5+x)^5 (524-573x+183x^2-23x^3+x^4), \\
& (-7+x)^2 (-5+x)^5 (-76+71x-16x^2+x^3), \\
& (-7+x)^2 (-5+x)^4 (388-431x+151x^2-21x^3+x^4), \\
& (-9+x) (-7+x) (-5+x)^6 (12-9x+x^2), \\
& (-5+x)^5 (-3764+4551x-1854x^2+344x^3-30x^4+x^5), \\
& (-9+x) (-7+x)^2 (-5+x)^4 (-4+x) (11-8x+x^2), \\
& (-7+x) (-5+x)^4 (-2756+3413x-1488x^2+298x^3-28x^4+x^5), \\
& (-7+x) (-5+x)^5 (548-573x+183x^2-23x^3+x^4), \\
& (-7+x)^2 (-5+x)^4 (404-431x+151x^2-21x^3+x^4), \\
& (-7+x) (-5+x)^4 (-2812+3421x-1488x^2+298x^3-28x^4+x^5), \\
& (-7+x) (-5+x)^4 (-2796+3421x-1488x^2+298x^3-28x^4+x^5), \\
& (-7+x)^2 (-5+x)^3 (-3+x) (692-625x+187x^2-23x^3+x^4), \\
& (-7+x)^2 (-5+x)^4 (412-431x+151x^2-21x^3+x^4), \\
& (-7+x)^3 (-5+x)^3 (-4+x) (-73+63x-15x^2+x^3), \\
& (-7+x) (-5+x)^4 (-2868+3429x-1488x^2+298x^3-28x^4+x^5), \\
& (-7+x) (-5+x)^4 (31-12x+x^2) (-92+75x-16x^2+x^3), \\
& (-7+x)^3 (-5+x)^4 (-3+x) (20-11x+x^2), \\
& (-7+x) (-5+x)^3 (-127+87x-17x^2+x^3) (-116+79x-16x^2+x^3), \\
& (-7+x)^2 (-5+x)^3 (-2084+2575x-1186x^2+256x^3-26x^4+x^5), \\
& (-7+x) (-5+x)^4 (17-10x+x^2) (-172+101x-18x^2+x^3), \\
& (-7+x) (-5+x)^3 (31-12x+x^2) (468-467x+155x^2-21x^3+x^4), \\
& (-7+x)^3 (-5+x)^2 (-4+x) (-3+x) (-127+87x-17x^2+x^3), \\
& (-7+x)^2 (-5+x)^3 (-3+x) (708-625x+187x^2-23x^3+x^4), \\
& (-7+x)^2 (-5+x)^3 (-4+x) (31-12x+x^2) (17-10x+x^2), \\
& (-7+x)^3 (-5+x)^2 (-3+x)^2 (-172+101x-18x^2+x^3), \\
& (-7+x)^2 (-5+x)^2 (-3+x) (31-12x+x^2) (-116+79x-16x^2+x^3), \\
& (-7+x)^4 (-5+x) (-4+x) (-3+x)^2 (31-12x+x^2), \\
& (-9+x) (-7+x)^2 (-5+x)^5 (8-7x+x^2), \\
& (-7+x)^2 (-5+x)^4 (368-427x+151x^2-21x^3+x^4), \\
& (-7+x) (-5+x)^5 (512-569x+183x^2-23x^3+x^4), \\
& (-7+x)^2 (-5+x)^4 (376-427x+151x^2-21x^3+x^4),
\end{aligned}$$

$$\begin{aligned}
& (-7+x) (-5+x)^4 (-2616 + 3365x - 1484x^2 + 298x^3 - 28x^4 + x^5), \\
& (-8+x) (-7+x) (-5+x)^6 (13 - 10x + x^2), \\
& (-7+x)^2 (-5+x)^3 (11 - 8x + x^2) (-176 + 101x - 18x^2 + x^3), \\
& (-7+x)^2 (-5+x)^4 (384 - 427x + 151x^2 - 21x^3 + x^4), \\
& (-7+x) (-5+x)^4 (-2672 + 3373x - 1484x^2 + 298x^3 - 28x^4 + x^5), \\
& (-7+x)^2 (-5+x)^3 (-1976 + 2527x - 1182x^2 + 256x^3 - 26x^4 + x^5), \\
& (-7+x)^3 (-5+x)^4 (-56 + 53x - 14x^2 + x^3), \\
& (-8+x) (-7+x) (-5+x)^4 (31 - 12x + x^2) (11 - 8x + x^2), \\
& (-7+x)^2 (-5+x)^3 (16 - 9x + x^2) (-127 + 87x - 17x^2 + x^3), \\
& (-7+x)^3 (-5+x)^3 (-3+x) (-96 + 75x - 16x^2 + x^3), \\
& (-7+x)^2 (-5+x)^4 (400 - 427x + 151x^2 - 21x^3 + x^4), \\
& (-7+x)^2 (-5+x)^3 (31 - 12x + x^2) (-64 + 57x - 14x^2 + x^3), \\
& (-7+x)^3 (-5+x)^2 (-3+x) (488 - 471x + 155x^2 - 21x^3 + x^4), \\
& (-7+x)^2 (-5+x)^2 (31 - 12x + x^2) (328 - 349x + 127x^2 - 19x^3 + x^4), \\
& (-8+x) (-7+x)^2 (-5+x)^4 (-3+x) (17 - 10x + x^2), \\
& (-7+x)^3 (-5+x)^2 (-3+x) (31 - 12x + x^2) (16 - 9x + x^2), \\
& (-8+x) (-7+x)^4 (-5+x)^2 (-3+x)^3, (-7+x)^2 (-5+x)^5 (-68 + 71x - 16x^2 + x^3), \\
& (-7+x)^2 (-5+x)^4 (348 - 423x + 151x^2 - 21x^3 + x^4), \\
& (-7+x) (-5+x)^5 (484 - 565x + 183x^2 - 23x^3 + x^4), \\
& (-7+x)^2 (-5+x)^4 (356 - 423x + 151x^2 - 21x^3 + x^4), \\
& (-7+x) (-5+x)^4 (-2476 + 3317x - 1480x^2 + 298x^3 - 28x^4 + x^5), \\
& (-7+x)^2 (-5+x)^3 (-1836 + 2479x - 1178x^2 + 256x^3 - 26x^4 + x^5), \\
& (-7+x)^3 (-5+x)^4 (-4+x) (13 - 10x + x^2), \\
& (-7+x)^2 (-5+x)^3 (11 - 8x + x^2) (-172 + 101x - 18x^2 + x^3), \\
& (-7+x)^3 (-5+x)^3 (268 - 317x + 123x^2 - 19x^3 + x^4), \\
& (-7+x)^2 (-5+x)^4 (31 - 12x + x^2) (12 - 9x + x^2), \\
& (-7+x)^3 (-5+x)^3 (-3+x) (-92 + 75x - 16x^2 + x^3), \\
& (-7+x)^3 (-5+x)^2 (-4+x) (31 - 12x + x^2) (11 - 8x + x^2), \\
& (-7+x)^2 (-5+x)^3 (-1916 + 2495x - 1178x^2 + 256x^3 - 26x^4 + x^5), \\
& (-7+x)^3 (-5+x)^2 (-3+x) (468 - 467x + 155x^2 - 21x^3 + x^4), \\
& (-7+x)^2 (-5+x)^3 (17 - 10x + x^2) (-116 + 79x - 16x^2 + x^3), \\
& (-7+x)^4 (-5+x)^2 (-4+x) (-3+x) (17 - 10x + x^2), \\
& (-7+x)^4 (-5+x) (-3+x)^2 (-116 + 79x - 16x^2 + x^3), \\
& (-7+x)^6 (-4+x) (-3+x)^3, (-7+x)^2 (-5+x)^5 (-64 + 71x - 16x^2 + x^3), \\
& (-7+x)^2 (-5+x)^4 (328 - 419x + 151x^2 - 21x^3 + x^4), \\
& (-8+x) (-7+x) (-5+x)^5 (-57 + 63x - 15x^2 + x^3), \\
& (-7+x)^2 (-5+x)^3 (-1696 + 2431x - 1174x^2 + 256x^3 - 26x^4 + x^5), \\
& (-7+x)^3 (-5+x)^4 (-48 + 53x - 14x^2 + x^3), \\
& (-7+x)^3 (-5+x)^3 (31 - 12x + x^2) (8 - 7x + x^2), \\
& (-8+x) (-7+x)^2 (-5+x)^4 (-43 + 47x - 13x^2 + x^3), \\
& (-7+x)^3 (-5+x)^3 (256 - 313x + 123x^2 - 19x^3 + x^4), \\
& (-8+x) (-7+x)^3 (-5+x)^3 (-3+x) (11 - 8x + x^2),
\end{aligned}$$

$$\begin{aligned}
& (-7+x)^3 (-5+x)^2 (-1304 + 1829x - 928x^2 + 218x^3 - 24x^4 + x^5), \\
& (-7+x)^3 (-5+x)^3 (17 - 10x + x^2) (16 - 9x + x^2), \\
& (-7+x)^4 (-5+x)^2 (-3+x) (-64 + 57x - 14x^2 + x^3), \\
& (-7+x)^4 (-5+x) (-3+x) (328 - 349x + 127x^2 - 19x^3 + x^4), \\
& (-7+x)^5 (-5+x) (-3+x)^2 (16 - 9x + x^2), (-7+x)^2 (-5+x)^5 (-60 + 71x - 16x^2 + x^3), \\
& (-7+x)^3 (-5+x)^4 (-44 + 53x - 14x^2 + x^3), \\
& (-7+x)^3 (-5+x)^3 (-4+x) (-57 + 63x - 15x^2 + x^3), \\
& (-7+x)^3 (-5+x)^3 (236 - 309x + 123x^2 - 19x^3 + x^4), \\
& (-7+x)^3 (-5+x)^3 (244 - 309x + 123x^2 - 19x^3 + x^4), \\
& (-7+x)^4 (-5+x)^2 (-4+x) (-43 + 47x - 13x^2 + x^3), \\
& (-7+x)^3 (-5+x)^2 (11 - 8x + x^2) (-116 + 79x - 16x^2 + x^3), \\
& (-7+x)^4 (-5+x)^3 (-3+x) (12 - 9x + x^2), \\
& (-7+x)^5 (-5+x) (-4+x) (-3+x) (11 - 8x + x^2), \\
& (-7+x)^2 (-5+x)^4 (272 - 411x + 151x^2 - 21x^3 + x^4), \\
& (-8+x) (-7+x)^3 (-5+x)^5 (-1+x), (-7+x)^3 (-5+x)^3 (208 - 305x + 123x^2 - 19x^3 + x^4), \\
& (-7+x)^3 (-5+x)^3 (216 - 305x + 123x^2 - 19x^3 + x^4), \\
& (-7+x)^4 (-5+x)^3 (-32 + 39x - 12x^2 + x^3), (-7+x)^5 (-5+x)^2 (-3+x) (8 - 7x + x^2), \\
& (-7+x)^4 (-5+x)^2 (16 - 9x + x^2) (11 - 8x + x^2), \\
& (-7+x)^3 (-5+x)^4 (-36 + 53x - 14x^2 + x^3), \\
& (-7+x)^3 (-5+x)^3 (188 - 301x + 123x^2 - 19x^3 + x^4), \\
& (-7+x)^5 (-5+x)^3 (-4+x) (-1+x), (-7+x)^4 (-5+x)^2 (148 - 223x + 99x^2 - 17x^3 + x^4), \\
& (-7+x)^3 (-5+x)^4 (-32 + 53x - 14x^2 + x^3), \\
& (-7+x)^4 (-5+x)^3 (-24 + 39x - 12x^2 + x^3), (-7+x)^4 (-5+x)^4 (4 - 7x + x^2) \}
\end{aligned}$$

dim14list =

$$\begin{aligned}
& \left\{ (-11+x) (-5+x)^{12} (-4+x) (5+x)^{15}, (-5+x)^{11} (5+x)^{15} (-216 + 119x - 20x^2 + x^3), \right. \\
& (-5+x)^{11} (5+x)^{15} (-212 + 119x - 20x^2 + x^3), (-5+x)^{10} (-4+x) (5+x)^{15} \\
& (-267 + 135x - 21x^2 + x^3), (-5+x)^{11} (5+x)^{15} (-208 + 119x - 20x^2 + x^3), \\
& (-5+x)^{10} (5+x)^{15} (1048 - 803x + 219x^2 - 25x^3 + x^4), (-5+x)^{11} (-3+x) \\
& (5+x)^{15} (68 - 17x + x^2), (-5+x)^{10} (5+x)^{15} (1028 - 799x + 219x^2 - 25x^3 + x^4), \\
& (-7+x) (-5+x)^{10} (-4+x) (5+x)^{15} (37 - 14x + x^2), (-5+x)^{10} (5+x)^{15} \\
& (992 - 795x + 219x^2 - 25x^3 + x^4), (-5+x)^{11} (5+x)^{15} (-200 + 119x - 20x^2 + x^3), \\
& (-5+x)^9 (5+x)^{15} (-5056 + 4983x - 1890x^2 + 344x^3 - 30x^4 + x^5), \\
& (-7+x) (-5+x)^{10} (-3+x) (5+x)^{15} (48 - 15x + x^2), \\
& (-5+x)^{10} (5+x)^{15} (1016 - 795x + 219x^2 - 25x^3 + x^4), \\
& (-5+x)^{10} (5+x)^{15} (972 - 791x + 219x^2 - 25x^3 + x^4), \\
& (-5+x)^9 (5+x)^{15} (-4916 + 4935x - 1886x^2 + 344x^3 - 30x^4 + x^5), \\
& (-7+x) (-5+x)^{11} (5+x)^{15} (28 - 13x + x^2), \\
& (-7+x) (-5+x)^9 (-4+x) (-3+x) (5+x)^{15} (59 - 16x + x^2), \\
& (-5+x)^{10} (5+x)^{15} (988 - 791x + 219x^2 - 25x^3 + x^4), \\
& (-5+x)^9 (5+x)^{15} (-4996 + 4951x - 1886x^2 + 344x^3 - 30x^4 + x^5), \\
& \left. (-5+x)^{10} (-3+x) (5+x)^{15} (-332 + 153x - 22x^2 + x^3) \right\}
\end{aligned}$$

$$\begin{aligned}
& (-5 + x)^{10} (-4 + x) (5 + x)^{15} (-251 + 135 x - 21 x^2 + x^3), \\
& (-5 + x)^9 (-4 + x) (5 + x)^{15} (41 - 14 x + x^2) (31 - 12 x + x^2), \\
& (-5 + x)^{10} (5 + x)^{15} (59 - 16 x + x^2) (16 - 9 x + x^2), \\
& (-7 + x) (-5 + x)^{10} (5 + x)^{15} (-136 + 93 x - 18 x^2 + x^3), \\
& (-7 + x) (-5 + x)^9 (5 + x)^{15} (688 - 601 x + 183 x^2 - 23 x^3 + x^4), \\
& (-5 + x)^{11} (5 + x)^{15} (-192 + 119 x - 20 x^2 + x^3), \\
& (-7 + x) (-5 + x)^9 (-3 + x) (5 + x)^{15} (-232 + 123 x - 20 x^2 + x^3), \\
& (-5 + x)^9 (5 + x)^{15} (-4856 + 4903 x - 1882 x^2 + 344 x^3 - 30 x^4 + x^5), \\
& (-5 + x)^{10} (5 + x)^{15} (968 - 787 x + 219 x^2 - 25 x^3 + x^4), \\
& (-5 + x)^9 (-3 + x) (5 + x)^{15} (1632 - 1093 x + 263 x^2 - 27 x^3 + x^4), \\
& (-5 + x)^{10} (5 + x)^{15} (976 - 787 x + 219 x^2 - 25 x^3 + x^4), \\
& (-8 + x) (-5 + x)^{10} (-3 + x) (5 + x)^{15} (41 - 14 x + x^2), \\
& (-5 + x)^{10} (5 + x)^{15} (32 - 13 x + x^2) (31 - 12 x + x^2), \\
& (-7 + x) (-5 + x)^{10} (5 + x)^{15} (-132 + 93 x - 18 x^2 + x^3), \\
& (-7 + x) (-5 + x)^9 (5 + x)^{15} (668 - 597 x + 183 x^2 - 23 x^3 + x^4), \\
& (-5 + x)^{10} (5 + x)^{15} (932 - 783 x + 219 x^2 - 25 x^3 + x^4), \\
& (-7 + x) (-5 + x)^9 (-4 + x) (5 + x)^{15} (-169 + 107 x - 19 x^2 + x^3), \\
& (-5 + x)^9 (5 + x)^{15} (-4716 + 4855 x - 1878 x^2 + 344 x^3 - 30 x^4 + x^5), \\
& (-5 + x)^{11} (5 + x)^{15} (-188 + 119 x - 20 x^2 + x^3), \\
& (-7 + x) (-5 + x)^9 (-3 + x) (5 + x)^{15} (-228 + 123 x - 20 x^2 + x^3), \\
& (-5 + x)^9 (5 + x)^{15} (-4772 + 4863 x - 1878 x^2 + 344 x^3 - 30 x^4 + x^5), \\
& (-5 + x)^9 (5 + x)^{15} (41 - 14 x + x^2) (-116 + 79 x - 16 x^2 + x^3), \\
& (-5 + x)^{10} (5 + x)^{15} (948 - 783 x + 219 x^2 - 25 x^3 + x^4), \\
& (-7 + x)^2 (-5 + x)^8 (-4 + x) (-3 + x) (5 + x)^{15} (41 - 14 x + x^2), \\
& (-5 + x)^9 (-3 + x) (5 + x)^{15} (1604 - 1089 x + 263 x^2 - 27 x^3 + x^4), \\
& (-5 + x)^9 (-4 + x) (5 + x)^{15} (1199 - 918 x + 240 x^2 - 26 x^3 + x^4), \\
& (-5 + x)^{10} (5 + x)^{15} (956 - 783 x + 219 x^2 - 25 x^3 + x^4), \\
& (-5 + x)^9 (-3 + x) (5 + x)^{15} (52 - 15 x + x^2) (31 - 12 x + x^2), \\
& (-5 + x)^{10} (5 + x)^{15} (964 - 783 x + 219 x^2 - 25 x^3 + x^4), \\
& (-5 + x)^8 (-4 + x) (5 + x)^{15} (31 - 12 x + x^2) (-197 + 111 x - 19 x^2 + x^3), \\
& (-9 + x)^2 (-5 + x)^{10} (-4 + x) (-3 + x) (5 + x)^{15}, \\
& (-7 + x) (-5 + x)^{10} (5 + x)^{15} (-128 + 93 x - 18 x^2 + x^3), \\
& (-7 + x) (-5 + x)^9 (5 + x)^{15} (648 - 593 x + 183 x^2 - 23 x^3 + x^4), \\
& (-5 + x)^{10} (5 + x)^{15} (904 - 779 x + 219 x^2 - 25 x^3 + x^4), \\
& (-7 + x) (-5 + x)^9 (5 + x)^{15} (41 - 14 x + x^2) (16 - 9 x + x^2), \\
& (-5 + x)^9 (5 + x)^{15} (-4576 + 4807 x - 1874 x^2 + 344 x^3 - 30 x^4 + x^5), \\
& (-5 + x)^{10} (5 + x)^{15} (912 - 779 x + 219 x^2 - 25 x^3 + x^4), \\
& (-7 + x) (-5 + x)^8 (-3 + x) (5 + x)^{15} (1112 - 839 x + 223 x^2 - 25 x^3 + x^4), \\
& (-7 + x) (-5 + x)^9 (5 + x)^{15} (664 - 593 x + 183 x^2 - 23 x^3 + x^4), \\
& (-5 + x)^9 (5 + x)^{15} (-4632 + 4815 x - 1874 x^2 + 344 x^3 - 30 x^4 + x^5), \\
& (-5 + x)^9 (5 + x)^{15} (-4616 + 4815 x - 1874 x^2 + 344 x^3 - 30 x^4 + x^5), \\
& (-8 + x) (-5 + x)^{11} (5 + x)^{15} (23 - 12 x + x^2),
\end{aligned}$$

$$\begin{aligned}
& (-7+x)^2 (-5+x)^9 (-3+x) (5+x)^{15} (32 - 13x + x^2), \\
& (-5+x)^9 (5+x)^{15} (-4688 + 4823x - 1874x^2 + 344x^3 - 30x^4 + x^5), \\
& (-5+x)^9 (5+x)^{15} (-4672 + 4823x - 1874x^2 + 344x^3 - 30x^4 + x^5), \\
& (-5+x)^9 (5+x)^{15} (-4656 + 4823x - 1874x^2 + 344x^3 - 30x^4 + x^5), \\
& (-5+x)^{10} (5+x)^{15} (928 - 779x + 219x^2 - 25x^3 + x^4), \\
& (-7+x) (-5+x)^8 (-3+x) (5+x)^{15} (1128 - 839x + 223x^2 - 25x^3 + x^4), \\
& (-8+x) (-5+x)^9 (-3+x) (5+x)^{15} (-197 + 111x - 19x^2 + x^3), \\
& (-5+x)^9 (5+x)^{15} (31 - 12x + x^2) (-152 + 97x - 18x^2 + x^3), \\
& (-5+x)^9 (5+x)^{15} (-4696 + 4831x - 1874x^2 + 344x^3 - 30x^4 + x^5), \\
& (-9+x) (-5+x)^{10} (5+x)^{15} (-104 + 75x - 16x^2 + x^3), \\
& (-5+x)^8 (-3+x) (5+x)^{15} (31 - 12x + x^2) (-256 + 127x - 20x^2 + x^3), \\
& (-9+x) (-5+x)^9 (-3+x) (5+x)^{15} (-176 + 101x - 18x^2 + x^3), \\
& (-7+x) (-5+x)^{10} (5+x)^{15} (-124 + 93x - 18x^2 + x^3), \\
& (-7+x) (-5+x)^9 (5+x)^{15} (628 - 589x + 183x^2 - 23x^3 + x^4), \\
& (-5+x)^{10} (5+x)^{15} (876 - 775x + 219x^2 - 25x^3 + x^4), \\
& (-7+x) (-5+x)^8 (5+x)^{15} (-3196 + 3581x - 1504x^2 + 298x^3 - 28x^4 + x^5), \\
& (-7+x) (-5+x)^9 (5+x)^{15} (636 - 589x + 183x^2 - 23x^3 + x^4), \\
& (-5+x)^9 (5+x)^{15} (-4436 + 4759x - 1870x^2 + 344x^3 - 30x^4 + x^5), \\
& (-5+x)^{10} (5+x)^{15} (52 - 15x + x^2) (17 - 10x + x^2), \\
& (-7+x) (-5+x)^8 (5+x)^{15} (-3236 + 3589x - 1504x^2 + 298x^3 - 28x^4 + x^5), \\
& (-7+x)^2 (-5+x)^9 (-4+x) (5+x)^{15} (23 - 12x + x^2), \\
& (-5+x)^9 (5+x)^{15} (-4492 + 4767x - 1870x^2 + 344x^3 - 30x^4 + x^5), \\
& (-5+x)^9 (5+x)^{15} (-4476 + 4767x - 1870x^2 + 344x^3 - 30x^4 + x^5), \\
& (-5+x)^{10} (5+x)^{15} (892 - 775x + 219x^2 - 25x^3 + x^4), \\
& (-7+x)^2 (-5+x)^8 (-3+x)^2 (5+x)^{15} (52 - 15x + x^2), \\
& (-7+x) (-5+x)^9 (5+x)^{15} (652 - 589x + 183x^2 - 23x^3 + x^4), \\
& (-5+x)^8 (5+x)^{15} (-197 + 111x - 19x^2 + x^3) (-116 + 79x - 16x^2 + x^3), \\
& (-5+x)^9 (5+x)^{15} (-4548 + 4775x - 1870x^2 + 344x^3 - 30x^4 + x^5), \\
& (-5+x)^9 (5+x)^{15} (-4532 + 4775x - 1870x^2 + 344x^3 - 30x^4 + x^5), \\
& (-5+x)^9 (5+x)^{15} (-4516 + 4775x - 1870x^2 + 344x^3 - 30x^4 + x^5), \\
& (-9+x) (-5+x)^{11} (5+x)^{15} (20 - 11x + x^2), \\
& (-7+x)^2 (-5+x)^7 (-4+x) (-3+x) (5+x)^{15} (-197 + 111x - 19x^2 + x^3), \\
& (-7+x) (-5+x)^9 (-3+x) (5+x)^{15} (-220 + 123x - 20x^2 + x^3), \\
& (-7+x) (-5+x)^8 (-4+x) (5+x)^{15} (821 - 696x + 202x^2 - 24x^3 + x^4), \\
& (-5+x)^9 (5+x)^{15} (-4604 + 4783x - 1870x^2 + 344x^3 - 30x^4 + x^5), \\
& (-5+x)^9 (5+x)^{15} (31 - 12x + x^2) (-148 + 97x - 18x^2 + x^3), \\
& (-9+x) (-5+x)^9 (-4+x) (5+x)^{15} (-127 + 87x - 17x^2 + x^3), \\
& (-7+x) (-5+x)^8 (-3+x) (5+x)^{15} (1108 - 835x + 223x^2 - 25x^3 + x^4), \\
& (-5+x)^8 (5+x)^{15} (31 - 12x + x^2) (748 - 633x + 187x^2 - 23x^3 + x^4), \\
& (-9+x) (-5+x)^9 (-3+x) (5+x)^{15} (-172 + 101x - 18x^2 + x^3), \\
& (-9+x) (-7+x) (-5+x)^8 (-4+x) (-3+x) (5+x)^{15} (31 - 12x + x^2), \\
& (-5+x)^7 (-4+x) (5+x)^{15} (31 - 12x + x^2)^3,
\end{aligned}$$

$$\begin{aligned}
& (-7+x) (-5+x)^{10} (5+x)^{15} (-120 + 93x - 18x^2 + x^3), \\
& (-7+x) (-5+x)^9 (5+x)^{15} (608 - 585x + 183x^2 - 23x^3 + x^4), \\
& (-5+x)^{10} (5+x)^{15} (848 - 771x + 219x^2 - 25x^3 + x^4), \\
& (-7+x) (-5+x)^8 (5+x)^{15} (-3096 + 3541x - 1500x^2 + 298x^3 - 28x^4 + x^5), \\
& (-7+x)^2 (-5+x)^9 (5+x)^{15} (-88 + 71x - 16x^2 + x^3), \\
& (-5+x)^9 (5+x)^{15} (-4296 + 4711x - 1866x^2 + 344x^3 - 30x^4 + x^5), \\
& (-8+x) (-5+x)^{10} (5+x)^{15} (-107 + 83x - 17x^2 + x^3), \\
& (-7+x) (-5+x)^8 (5+x)^{15} (16 - 9x + x^2) (-197 + 111x - 19x^2 + x^3), \\
& (-7+x)^2 (-5+x)^8 (5+x)^{15} (448 - 443x + 151x^2 - 21x^3 + x^4), \\
& (-7+x) (-5+x)^9 (5+x)^{15} (624 - 585x + 183x^2 - 23x^3 + x^4), \\
& (-5+x)^9 (5+x)^{15} (17 - 10x + x^2) (-256 + 127x - 20x^2 + x^3), \\
& (-5+x)^9 (5+x)^{15} (-4336 + 4719x - 1866x^2 + 344x^3 - 30x^4 + x^5), \\
& (-9+x) (-5+x)^{10} (5+x)^{15} (-96 + 75x - 16x^2 + x^3), \\
& (-7+x)^2 (-5+x)^8 (-3+x) (5+x)^{15} (-152 + 97x - 18x^2 + x^3), \\
& (-7+x) (-5+x)^8 (5+x)^{15} (-3176 + 3557x - 1500x^2 + 298x^3 - 28x^4 + x^5), \\
& (-7+x) (-5+x)^9 (5+x)^{15} (632 - 585x + 183x^2 - 23x^3 + x^4), \\
& (-5+x)^8 (5+x)^{15} (22152 - 28059x + 14057x^2 - 3586x^3 + 494x^4 - 35x^5 + x^6), \\
& (-8+x) (-5+x)^9 (5+x)^{15} (551 - 522x + 168x^2 - 22x^3 + x^4), \\
& (-9+x) (-5+x)^9 (5+x)^{15} (488 - 471x + 155x^2 - 21x^3 + x^4), \\
& (-7+x)^2 (-5+x)^7 (-3+x)^2 (5+x)^{15} (-256 + 127x - 20x^2 + x^3), \\
& (-7+x) (-5+x)^8 (-3+x) (5+x)^{15} (1072 - 831x + 223x^2 - 25x^3 + x^4), \\
& (-7+x) (-5+x)^9 (5+x)^{15} (640 - 585x + 183x^2 - 23x^3 + x^4), \\
& (-5+x)^8 (5+x)^{15} (22432 - 28155x + 14065x^2 - 3586x^3 + 494x^4 - 35x^5 + x^6), \\
& (-9+x) (-5+x)^9 (5+x)^{15} (31 - 12x + x^2) (16 - 9x + x^2), \\
& (-5+x)^8 (5+x)^{15} (-176 + 101x - 18x^2 + x^3) (-127 + 87x - 17x^2 + x^3), \\
& (-7+x) (-5+x)^7 (-3+x) (5+x)^{15} (-5416 + 5235x - 1946x^2 + 348x^3 - 30x^4 + x^5), \\
& (-9+x) (-8+x) (-7+x) (-5+x)^9 (-3+x)^2 (5+x)^{15}, \\
& (-7+x) (-5+x)^8 (5+x)^{15} (31 - 12x + x^2) (-104 + 75x - 16x^2 + x^3), \\
& (-7+x) (-5+x)^7 (-3+x) (5+x)^{15} (31 - 12x + x^2) (-176 + 101x - 18x^2 + x^3), \\
& (-5+x)^8 (5+x)^{15} (31 - 12x + x^2) (736 - 629x + 187x^2 - 23x^3 + x^4), \\
& (-8+x) (-5+x)^8 (-3+x) (5+x)^{15} (31 - 12x + x^2)^2, \\
& (-7+x) (-5+x)^9 (5+x)^{15} (52 - 15x + x^2) (11 - 8x + x^2), \\
& (-7+x) (-5+x)^{10} (5+x)^{15} (-116 + 93x - 18x^2 + x^3), \\
& (-7+x) (-5+x)^8 (5+x)^{15} (-2956 + 3493x - 1496x^2 + 298x^3 - 28x^4 + x^5), \\
& (-7+x)^2 (-5+x)^9 (5+x)^{15} (-84 + 71x - 16x^2 + x^3), \\
& (-5+x)^{10} (5+x)^{15} (820 - 767x + 219x^2 - 25x^3 + x^4), \\
& (-7+x)^2 (-5+x)^8 (-4+x) (5+x)^{15} (-107 + 83x - 17x^2 + x^3), \\
& (-7+x) (-5+x)^9 (5+x)^{15} (596 - 581x + 183x^2 - 23x^3 + x^4), \\
& (-5+x)^9 (5+x)^{15} (-4156 + 4663x - 1862x^2 + 344x^3 - 30x^4 + x^5), \\
& (-9+x) (-5+x)^{10} (5+x)^{15} (-92 + 75x - 16x^2 + x^3), \\
& (-7+x)^2 (-5+x)^8 (5+x)^{15} (436 - 439x + 151x^2 - 21x^3 + x^4), \\
& (-7+x) (-5+x)^8 (5+x)^{15} (-3036 + 3509x - 1496x^2 + 298x^3 - 28x^4 + x^5),
\end{aligned}$$

$$\begin{aligned}
& (-7+x) (-5+x)^9 (5+x)^{15} (604 - 581x + 183x^2 - 23x^3 + x^4), \\
& (-5+x)^8 (5+x)^{15} (21172 - 27583x + 13981x^2 - 3582x^3 + 494x^4 - 35x^5 + x^6), \\
& (-9+x) (-5+x)^9 (5+x)^{15} (468 - 467x + 155x^2 - 21x^3 + x^4), \\
& (-7+x)^2 (-5+x)^8 (-3+x) (5+x)^{15} (-148 + 97x - 18x^2 + x^3), \\
& (-7+x)^2 (-5+x)^7 (-4+x) (5+x)^{15} (551 - 522x + 168x^2 - 22x^3 + x^4), \\
& (-7+x) (-5+x)^8 (5+x)^{15} (-3092 + 3517x - 1496x^2 + 298x^3 - 28x^4 + x^5), \\
& (-7+x) (-5+x)^8 (5+x)^{15} (-3076 + 3517x - 1496x^2 + 298x^3 - 28x^4 + x^5), \\
& (-9+x) (-7+x) (-5+x)^9 (-4+x) (5+x)^{15} (17 - 10x + x^2), \\
& (-5+x)^8 (5+x)^{15} (31 - 12x + x^2) (692 - 625x + 187x^2 - 23x^3 + x^4), \\
& (-7+x)^2 (-5+x)^7 (-3+x) (5+x)^{15} (748 - 633x + 187x^2 - 23x^3 + x^4), \\
& (-7+x) (-5+x)^7 (5+x)^{15} (15628 - 20757x + 11005x^2 - 2986x^3 + 438x^4 - 33x^5 + x^6), \\
& (-9+x) (-7+x) (-5+x)^8 (-3+x) (5+x)^{15} (-116 + 79x - 16x^2 + x^3), \\
& (-7+x) (-5+x)^8 (5+x)^{15} (-3116 + 3525x - 1496x^2 + 298x^3 - 28x^4 + x^5), \\
& (-5+x)^8 (5+x)^{15} (-172 + 101x - 18x^2 + x^3) (-127 + 87x - 17x^2 + x^3), \\
& (-7+x) (-5+x)^9 (5+x)^{15} (31 - 12x + x^2) (20 - 11x + x^2), \\
& (-9+x) (-7+x)^3 (-5+x)^7 (-4+x) (-3+x)^2 (5+x)^{15}, \\
& (-7+x) (-5+x)^7 (-3+x) (5+x)^{15} (-5276 + 5187x - 1942x^2 + 348x^3 - 30x^4 + x^5), \\
& (-7+x) (-5+x)^7 (-4+x) (5+x)^{15} (31 - 12x + x^2) (-127 + 87x - 17x^2 + x^3), \\
& (-5+x)^8 (5+x)^{15} (31 - 12x + x^2) (708 - 625x + 187x^2 - 23x^3 + x^4), \\
& (-7+x) (-5+x)^7 (-3+x) (5+x)^{15} (31 - 12x + x^2) (-172 + 101x - 18x^2 + x^3), \\
& (-5+x)^7 (5+x)^{15} (31 - 12x + x^2)^2 (-116 + 79x - 16x^2 + x^3), \\
& (-7+x)^2 (-5+x)^6 (-4+x) (-3+x) (5+x)^{15} (31 - 12x + x^2)^2, \\
& (-7+x) (-5+x)^9 (5+x)^{15} (552 - 577x + 183x^2 - 23x^3 + x^4), \\
& (-7+x) (-5+x)^8 (5+x)^{15} (11 - 8x + x^2) (-256 + 127x - 20x^2 + x^3), \\
& (-7+x)^2 (-5+x)^{10} (5+x)^{15} (16 - 11x + x^2), \\
& (-5+x)^9 (5+x)^{15} (-3904 + 4599x - 1858x^2 + 344x^3 - 30x^4 + x^5), \\
& (-7+x)^2 (-5+x)^8 (5+x)^{15} (408 - 435x + 151x^2 - 21x^3 + x^4), \\
& (-7+x) (-5+x)^9 (5+x)^{15} (568 - 577x + 183x^2 - 23x^3 + x^4), \\
& (-9+x) (-8+x) (-5+x)^{10} (5+x)^{15} (11 - 8x + x^2), \\
& (-7+x)^2 (-5+x)^8 (5+x)^{15} (416 - 435x + 151x^2 - 21x^3 + x^4), \\
& (-7+x) (-5+x)^8 (5+x)^{15} (-2896 + 3461x - 1492x^2 + 298x^3 - 28x^4 + x^5), \\
& (-9+x) (-7+x) (-5+x)^9 (5+x)^{15} (-64 + 57x - 14x^2 + x^3), \\
& (-5+x)^9 (5+x)^{15} (-4016 + 4615x - 1858x^2 + 344x^3 - 30x^4 + x^5), \\
& (-7+x)^2 (-5+x)^8 (5+x)^{15} (424 - 435x + 151x^2 - 21x^3 + x^4), \\
& (-9+x) (-7+x) (-5+x)^8 (5+x)^{15} (328 - 349x + 127x^2 - 19x^3 + x^4), \\
& (-7+x) (-5+x)^8 (5+x)^{15} (-2936 + 3469x - 1492x^2 + 298x^3 - 28x^4 + x^5), \\
& (-8+x) (-7+x) (-5+x)^9 (5+x)^{15} (-73 + 63x - 15x^2 + x^3), \\
& (-9+x) (-7+x)^2 (-5+x)^8 (-3+x) (5+x)^{15} (16 - 9x + x^2), \\
& (-7+x)^2 (-5+x)^7 (5+x)^{15} (-2144 + 2607x - 1190x^2 + 256x^3 - 26x^4 + x^5), \\
& (-7+x) (-5+x)^8 (5+x)^{15} (-3008 + 3477x - 1492x^2 + 298x^3 - 28x^4 + x^5), \\
& (-7+x) (-5+x)^8 (5+x)^{15} (17 - 10x + x^2) (-176 + 101x - 18x^2 + x^3), \\
& (-7+x) (-5+x)^8 (5+x)^{15} (31 - 12x + x^2) (-96 + 75x - 16x^2 + x^3),
\end{aligned}$$

$$\begin{aligned}
& (-7+x)^3 (-5+x)^7 (-3+x) (5+x)^{15} (-104 + 75x - 16x^2 + x^3), \\
& (-7+x) (-5+x)^7 (5+x)^{15} (15208 - 20473x + 10945x^2 - 2982x^3 + 438x^4 - 33x^5 + x^6), \\
& (-8+x) (-7+x) (-5+x)^8 (-3+x) (5+x)^{15} (-127 + 87x - 17x^2 + x^3), \\
& (-7+x) (-5+x)^7 (5+x)^{15} (31 - 12x + x^2) (488 - 471x + 155x^2 - 21x^3 + x^4), \\
& (-8+x) (-5+x)^9 (5+x)^{15} (31 - 12x + x^2) (17 - 10x + x^2), \\
& (-7+x)^3 (-5+x)^6 (-3+x)^2 (5+x)^{15} (-176 + 101x - 18x^2 + x^3), \\
& (-7+x)^2 (-5+x)^7 (-3+x) (5+x)^{15} (736 - 629x + 187x^2 - 23x^3 + x^4), \\
& (-7+x) (-5+x)^7 (5+x)^{15} (31 - 12x + x^2)^2 (16 - 9x + x^2), \\
& (-8+x) (-7+x)^2 (-5+x)^7 (-3+x)^2 (5+x)^{15} (31 - 12x + x^2), \\
& (-7+x) (-5+x)^9 (5+x)^{15} (524 - 573x + 183x^2 - 23x^3 + x^4), \\
& (-7+x)^2 (-5+x)^9 (5+x)^{15} (-76 + 71x - 16x^2 + x^3), \\
& (-7+x)^2 (-5+x)^8 (5+x)^{15} (388 - 431x + 151x^2 - 21x^3 + x^4), \\
& (-9+x) (-7+x) (-5+x)^{10} (5+x)^{15} (12 - 9x + x^2), \\
& (-5+x)^9 (5+x)^{15} (-3764 + 4551x - 1854x^2 + 344x^3 - 30x^4 + x^5), \\
& (-9+x) (-7+x)^2 (-5+x)^8 (-4+x) (5+x)^{15} (11 - 8x + x^2), \\
& (-7+x) (-5+x)^8 (5+x)^{15} (-2756 + 3413x - 1488x^2 + 298x^3 - 28x^4 + x^5), \\
& (-7+x) (-5+x)^9 (5+x)^{15} (548 - 573x + 183x^2 - 23x^3 + x^4), \\
& (-7+x)^2 (-5+x)^8 (5+x)^{15} (404 - 431x + 151x^2 - 21x^3 + x^4), \\
& (-7+x) (-5+x)^8 (5+x)^{15} (-2812 + 3421x - 1488x^2 + 298x^3 - 28x^4 + x^5), \\
& (-7+x) (-5+x)^8 (5+x)^{15} (-2796 + 3421x - 1488x^2 + 298x^3 - 28x^4 + x^5), \\
& (-7+x)^2 (-5+x)^7 (-3+x) (5+x)^{15} (692 - 625x + 187x^2 - 23x^3 + x^4), \\
& (-7+x)^2 (-5+x)^8 (5+x)^{15} (412 - 431x + 151x^2 - 21x^3 + x^4), \\
& (-7+x)^3 (-5+x)^7 (-4+x) (5+x)^{15} (-73 + 63x - 15x^2 + x^3), \\
& (-7+x) (-5+x)^8 (5+x)^{15} (-2868 + 3429x - 1488x^2 + 298x^3 - 28x^4 + x^5), \\
& (-7+x) (-5+x)^8 (5+x)^{15} (31 - 12x + x^2) (-92 + 75x - 16x^2 + x^3), \\
& (-7+x)^3 (-5+x)^8 (-3+x) (5+x)^{15} (20 - 11x + x^2), \\
& (-7+x) (-5+x)^7 (5+x)^{15} (-127 + 87x - 17x^2 + x^3) (-116 + 79x - 16x^2 + x^3), \\
& (-7+x)^2 (-5+x)^7 (5+x)^{15} (-2084 + 2575x - 1186x^2 + 256x^3 - 26x^4 + x^5), \\
& (-7+x) (-5+x)^8 (5+x)^{15} (17 - 10x + x^2) (-172 + 101x - 18x^2 + x^3), \\
& (-7+x) (-5+x)^7 (5+x)^{15} (31 - 12x + x^2) (468 - 467x + 155x^2 - 21x^3 + x^4), \\
& (-7+x)^3 (-5+x)^6 (-4+x) (-3+x) (5+x)^{15} (-127 + 87x - 17x^2 + x^3), \\
& (-7+x)^2 (-5+x)^7 (-3+x) (5+x)^{15} (708 - 625x + 187x^2 - 23x^3 + x^4), \\
& (-7+x)^2 (-5+x)^7 (-4+x) (5+x)^{15} (31 - 12x + x^2) (17 - 10x + x^2), \\
& (-7+x)^3 (-5+x)^6 (-3+x)^2 (5+x)^{15} (-172 + 101x - 18x^2 + x^3), \\
& (-7+x)^2 (-5+x)^6 (-3+x) (5+x)^{15} (31 - 12x + x^2) (-116 + 79x - 16x^2 + x^3), \\
& (-7+x)^4 (-5+x)^5 (-4+x) (-3+x)^2 (5+x)^{15} (31 - 12x + x^2), \\
& (-9+x) (-7+x)^2 (-5+x)^9 (5+x)^{15} (8 - 7x + x^2), \\
& (-7+x)^2 (-5+x)^8 (5+x)^{15} (368 - 427x + 151x^2 - 21x^3 + x^4), \\
& (-7+x) (-5+x)^9 (5+x)^{15} (512 - 569x + 183x^2 - 23x^3 + x^4), \\
& (-7+x)^2 (-5+x)^8 (5+x)^{15} (376 - 427x + 151x^2 - 21x^3 + x^4), \\
& (-7+x) (-5+x)^8 (5+x)^{15} (-2616 + 3365x - 1484x^2 + 298x^3 - 28x^4 + x^5), \\
& (-8+x) (-7+x) (-5+x)^{10} (5+x)^{15} (13 - 10x + x^2),
\end{aligned}$$

$$\begin{aligned}
& (-7+x)^2 (-5+x)^7 (5+x)^{15} (11 - 8x + x^2) (-176 + 101x - 18x^2 + x^3), \\
& (-7+x)^2 (-5+x)^8 (5+x)^{15} (384 - 427x + 151x^2 - 21x^3 + x^4), \\
& (-7+x) (-5+x)^8 (5+x)^{15} (-2672 + 3373x - 1484x^2 + 298x^3 - 28x^4 + x^5), \\
& (-7+x)^2 (-5+x)^7 (5+x)^{15} (-1976 + 2527x - 1182x^2 + 256x^3 - 26x^4 + x^5), \\
& (-7+x)^3 (-5+x)^8 (5+x)^{15} (-56 + 53x - 14x^2 + x^3), \\
& (-8+x) (-7+x) (-5+x)^8 (5+x)^{15} (31 - 12x + x^2) (11 - 8x + x^2), \\
& (-7+x)^2 (-5+x)^7 (5+x)^{15} (16 - 9x + x^2) (-127 + 87x - 17x^2 + x^3), \\
& (-7+x)^3 (-5+x)^7 (-3+x) (5+x)^{15} (-96 + 75x - 16x^2 + x^3), \\
& (-7+x)^2 (-5+x)^8 (5+x)^{15} (400 - 427x + 151x^2 - 21x^3 + x^4), \\
& (-7+x)^2 (-5+x)^7 (5+x)^{15} (31 - 12x + x^2) (-64 + 57x - 14x^2 + x^3), \\
& (-7+x)^3 (-5+x)^6 (-3+x) (5+x)^{15} (488 - 471x + 155x^2 - 21x^3 + x^4), \\
& (-7+x)^2 (-5+x)^6 (5+x)^{15} (31 - 12x + x^2) (328 - 349x + 127x^2 - 19x^3 + x^4), \\
& (-8+x) (-7+x)^2 (-5+x)^8 (-3+x) (5+x)^{15} (17 - 10x + x^2), \\
& (-7+x)^3 (-5+x)^6 (-3+x) (5+x)^{15} (31 - 12x + x^2) (16 - 9x + x^2), \\
& (-8+x) (-7+x)^4 (-5+x)^6 (-3+x)^3 (5+x)^{15}, \\
& (-7+x)^2 (-5+x)^9 (5+x)^{15} (-68 + 71x - 16x^2 + x^3), \\
& (-7+x)^2 (-5+x)^8 (5+x)^{15} (348 - 423x + 151x^2 - 21x^3 + x^4), \\
& (-7+x)^9 (5+x)^{15} (484 - 565x + 183x^2 - 23x^3 + x^4), \\
& (-7+x)^2 (-5+x)^8 (5+x)^{15} (356 - 423x + 151x^2 - 21x^3 + x^4), \\
& (-7+x)^8 (5+x)^{15} (-2476 + 3317x - 1480x^2 + 298x^3 - 28x^4 + x^5), \\
& (-7+x)^2 (-5+x)^7 (5+x)^{15} (-1836 + 2479x - 1178x^2 + 256x^3 - 26x^4 + x^5), \\
& (-7+x)^3 (-5+x)^8 (-4+x) (5+x)^{15} (13 - 10x + x^2), \\
& (-7+x)^2 (-5+x)^7 (5+x)^{15} (11 - 8x + x^2) (-172 + 101x - 18x^2 + x^3), \\
& (-7+x)^3 (-5+x)^7 (5+x)^{15} (268 - 317x + 123x^2 - 19x^3 + x^4), \\
& (-7+x)^2 (-5+x)^8 (5+x)^{15} (31 - 12x + x^2) (12 - 9x + x^2), \\
& (-7+x)^3 (-5+x)^7 (-3+x) (5+x)^{15} (-92 + 75x - 16x^2 + x^3), \\
& (-7+x)^3 (-5+x)^6 (-4+x) (5+x)^{15} (31 - 12x + x^2) (11 - 8x + x^2), \\
& (-7+x)^2 (-5+x)^7 (5+x)^{15} (-1916 + 2495x - 1178x^2 + 256x^3 - 26x^4 + x^5), \\
& (-7+x)^3 (-5+x)^6 (-3+x) (5+x)^{15} (468 - 467x + 155x^2 - 21x^3 + x^4), \\
& (-7+x)^2 (-5+x)^7 (5+x)^{15} (17 - 10x + x^2) (-116 + 79x - 16x^2 + x^3), \\
& (-7+x)^4 (-5+x)^6 (-4+x) (-3+x) (5+x)^{15} (17 - 10x + x^2), \\
& (-7+x)^4 (-5+x)^5 (-3+x)^2 (5+x)^{15} (-116 + 79x - 16x^2 + x^3), \\
& (-7+x)^6 (-5+x)^4 (-4+x) (-3+x)^3 (5+x)^{15}, \\
& (-7+x)^2 (-5+x)^9 (5+x)^{15} (-64 + 71x - 16x^2 + x^3), \\
& (-7+x)^2 (-5+x)^8 (5+x)^{15} (328 - 419x + 151x^2 - 21x^3 + x^4), \\
& (-8+x) (-7+x) (-5+x)^9 (5+x)^{15} (-57 + 63x - 15x^2 + x^3), \\
& (-7+x)^2 (-5+x)^7 (5+x)^{15} (-1696 + 2431x - 1174x^2 + 256x^3 - 26x^4 + x^5), \\
& (-7+x)^3 (-5+x)^8 (5+x)^{15} (-48 + 53x - 14x^2 + x^3), \\
& (-7+x)^3 (-5+x)^7 (5+x)^{15} (31 - 12x + x^2) (8 - 7x + x^2), \\
& (-8+x) (-7+x)^2 (-5+x)^8 (5+x)^{15} (-43 + 47x - 13x^2 + x^3), \\
& (-7+x)^3 (-5+x)^7 (5+x)^{15} (256 - 313x + 123x^2 - 19x^3 + x^4), \\
& (-8+x) (-7+x)^3 (-5+x)^7 (-3+x) (5+x)^{15} (11 - 8x + x^2),
\end{aligned}$$

$$\begin{aligned}
& (-7+x)^3 (-5+x)^6 (5+x)^{15} (-1304 + 1829x - 928x^2 + 218x^3 - 24x^4 + x^5), \\
& (-7+x)^3 (-5+x)^7 (5+x)^{15} (17 - 10x + x^2) (16 - 9x + x^2), \\
& (-7+x)^4 (-5+x)^6 (-3+x) (5+x)^{15} (-64 + 57x - 14x^2 + x^3), \\
& (-7+x)^4 (-5+x)^5 (-3+x) (5+x)^{15} (328 - 349x + 127x^2 - 19x^3 + x^4), \\
& (-7+x)^5 (-5+x)^5 (-3+x)^2 (5+x)^{15} (16 - 9x + x^2), \\
& (-7+x)^2 (-5+x)^9 (5+x)^{15} (-60 + 71x - 16x^2 + x^3), \\
& (-7+x)^3 (-5+x)^8 (5+x)^{15} (-44 + 53x - 14x^2 + x^3), \\
& (-7+x)^3 (-5+x)^7 (-4+x) (5+x)^{15} (-57 + 63x - 15x^2 + x^3), \\
& (-7+x)^3 (-5+x)^7 (5+x)^{15} (236 - 309x + 123x^2 - 19x^3 + x^4), \\
& (-7+x)^3 (-5+x)^7 (5+x)^{15} (244 - 309x + 123x^2 - 19x^3 + x^4), \\
& (-7+x)^4 (-5+x)^6 (-4+x) (5+x)^{15} (-43 + 47x - 13x^2 + x^3), \\
& (-7+x)^3 (-5+x)^6 (5+x)^{15} (11 - 8x + x^2) (-116 + 79x - 16x^2 + x^3), \\
& (-7+x)^4 (-5+x)^7 (-3+x) (5+x)^{15} (12 - 9x + x^2), \\
& (-7+x)^5 (-5+x)^5 (-4+x) (-3+x) (5+x)^{15} (11 - 8x + x^2), \\
& (-7+x)^2 (-5+x)^8 (5+x)^{15} (272 - 411x + 151x^2 - 21x^3 + x^4), \\
& (-8+x) (-7+x)^3 (-5+x)^9 (-1+x) (5+x)^{15}, \\
& (-7+x)^3 (-5+x)^7 (5+x)^{15} (208 - 305x + 123x^2 - 19x^3 + x^4), \\
& (-7+x)^3 (-5+x)^7 (5+x)^{15} (216 - 305x + 123x^2 - 19x^3 + x^4), \\
& (-7+x)^4 (-5+x)^7 (5+x)^{15} (-32 + 39x - 12x^2 + x^3), \\
& (-7+x)^5 (-5+x)^6 (-3+x) (5+x)^{15} (8 - 7x + x^2), \\
& (-7+x)^4 (-5+x)^6 (5+x)^{15} (16 - 9x + x^2) (11 - 8x + x^2), \\
& (-7+x)^3 (-5+x)^8 (5+x)^{15} (-36 + 53x - 14x^2 + x^3), \\
& (-7+x)^3 (-5+x)^7 (5+x)^{15} (188 - 301x + 123x^2 - 19x^3 + x^4), \\
& (-7+x)^5 (-5+x)^7 (-4+x) (-1+x) (5+x)^{15}, \\
& (-7+x)^4 (-5+x)^6 (5+x)^{15} (148 - 223x + 99x^2 - 17x^3 + x^4), \\
& (-7+x)^3 (-5+x)^8 (5+x)^{15} (-32 + 53x - 14x^2 + x^3), (-7+x)^4 (-5+x)^7 \\
& (5+x)^{15} (-24 + 39x - 12x^2 + x^3), (-7+x)^4 (-5+x)^8 (5+x)^{15} (4 - 7x + x^2) \};
\end{aligned}$$

Length[dim14list]

301

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modfilter[dim14list, chiSmod128n29, 128]
```

$$\left\{ \begin{aligned} & (-11 + x) (-5 + x)^{12} (-4 + x) (5 + x)^{15}, (-5 + x)^{11} (-3 + x) (5 + x)^{15} (68 - 17 x + x^2), \\ & (-7 + x) (-5 + x)^{10} (-3 + x) (5 + x)^{15} (48 - 15 x + x^2), \\ & (-7 + x) (-5 + x)^9 (-4 + x) (5 + x)^{15} (-169 + 107 x - 19 x^2 + x^3), \\ & (-5 + x)^{11} (5 + x)^{15} (-188 + 119 x - 20 x^2 + x^3), \\ & (-9 + x)^2 (-5 + x)^{10} (-4 + x) (-3 + x) (5 + x)^{15}, \\ & (-7 + x) (-5 + x)^{10} (5 + x)^{15} (-128 + 93 x - 18 x^2 + x^3), \\ & (-7 + x)^2 (-5 + x)^9 (-3 + x) (5 + x)^{15} (32 - 13 x + x^2), \\ & (-5 + x)^9 (5 + x)^{15} (-4672 + 4823 x - 1874 x^2 + 344 x^3 - 30 x^4 + x^5), \\ & (-5 + x)^{10} (5 + x)^{15} (928 - 779 x + 219 x^2 - 25 x^3 + x^4), \\ & (-7 + x)^2 (-5 + x)^8 (-3 + x)^2 (5 + x)^{15} (52 - 15 x + x^2), \\ & (-7 + x) (-5 + x)^8 (5 + x)^{15} (-3176 + 3557 x - 1500 x^2 + 298 x^3 - 28 x^4 + x^5), \\ & (-8 + x) (-5 + x)^8 (-3 + x) (5 + x)^{15} (31 - 12 x + x^2)^2, \\ & (-7 + x) (-5 + x)^9 (5 + x)^{15} (596 - 581 x + 183 x^2 - 23 x^3 + x^4), \\ & (-9 + x) (-5 + x)^{10} (5 + x)^{15} (-92 + 75 x - 16 x^2 + x^3), \\ & (-7 + x)^2 (-5 + x)^6 (-4 + x) (-3 + x) (5 + x)^{15} (31 - 12 x + x^2)^2, \\ & (-7 + x)^2 (-5 + x)^{10} (5 + x)^{15} (16 - 11 x + x^2), \\ & (-9 + x) (-7 + x)^2 (-5 + x)^8 (-3 + x) (5 + x)^{15} (16 - 9 x + x^2), \\ & (-7 + x) (-5 + x)^8 (5 + x)^{15} (17 - 10 x + x^2) (-176 + 101 x - 18 x^2 + x^3), \\ & (-7 + x)^2 (-5 + x)^8 (5 + x)^{15} (388 - 431 x + 151 x^2 - 21 x^3 + x^4), \\ & (-7 + x)^3 (-5 + x)^8 (-3 + x) (5 + x)^{15} (20 - 11 x + x^2), \\ & (-7 + x) (-5 + x)^8 (5 + x)^{15} (-2616 + 3365 x - 1484 x^2 + 298 x^3 - 28 x^4 + x^5), \\ & (-8 + x) (-7 + x)^4 (-5 + x)^6 (-3 + x)^3 (5 + x)^{15}, \\ & (-7 + x) (-5 + x)^9 (5 + x)^{15} (484 - 565 x + 183 x^2 - 23 x^3 + x^4), \\ & (-7 + x)^6 (-5 + x)^4 (-4 + x) (-3 + x)^3 (5 + x)^{15}, \\ & (-7 + x)^2 (-5 + x)^9 (5 + x)^{15} (-64 + 71 x - 16 x^2 + x^3), \\ & (-7 + x)^3 (-5 + x)^7 (5 + x)^{15} (256 - 313 x + 123 x^2 - 19 x^3 + x^4), \\ & (-7 + x)^3 (-5 + x)^8 (5 + x)^{15} (-44 + 53 x - 14 x^2 + x^3), \\ & (-7 + x)^4 (-5 + x)^7 (-3 + x) (5 + x)^{15} (12 - 9 x + x^2), \\ & (-7 + x)^5 (-5 + x)^6 (-3 + x) (5 + x)^{15} (8 - 7 x + x^2), \\ & (-7 + x)^4 (-5 + x)^8 (5 + x)^{15} (4 - 7 x + x^2) \end{aligned} \right\}$$

```

dim14listmod128 =
{ (-11 + x) (-5 + x)^12 (-4 + x) (5 + x)^15, (-5 + x)^11 (-3 + x) (5 + x)^15 (68 - 17 x + x^2),
  (-7 + x) (-5 + x)^10 (-3 + x) (5 + x)^15 (48 - 15 x + x^2),
  (-7 + x) (-5 + x)^9 (-4 + x) (5 + x)^15 (-169 + 107 x - 19 x^2 + x^3),
  (-5 + x)^11 (5 + x)^15 (-188 + 119 x - 20 x^2 + x^3),
  (-9 + x)^2 (-5 + x)^10 (-4 + x) (-3 + x) (5 + x)^15, (-7 + x) (-5 + x)^10 (5 + x)^15
  (-128 + 93 x - 18 x^2 + x^3), (-7 + x)^2 (-5 + x)^9 (-3 + x) (5 + x)^15 (32 - 13 x + x^2),
  (-5 + x)^9 (5 + x)^15 (-4672 + 4823 x - 1874 x^2 + 344 x^3 - 30 x^4 + x^5),
  (-5 + x)^10 (5 + x)^15 (928 - 779 x + 219 x^2 - 25 x^3 + x^4),
  (-7 + x)^2 (-5 + x)^8 (-3 + x)^2 (5 + x)^15 (52 - 15 x + x^2),
  (-7 + x) (-5 + x)^8 (5 + x)^15 (-3176 + 3557 x - 1500 x^2 + 298 x^3 - 28 x^4 + x^5),
  (-8 + x) (-5 + x)^8 (-3 + x) (5 + x)^15 (31 - 12 x + x^2)^2,
  (-7 + x) (-5 + x)^9 (5 + x)^15 (596 - 581 x + 183 x^2 - 23 x^3 + x^4),
  (-9 + x) (-5 + x)^10 (5 + x)^15 (-92 + 75 x - 16 x^2 + x^3),
  (-7 + x)^2 (-5 + x)^6 (-4 + x) (-3 + x) (5 + x)^15 (31 - 12 x + x^2)^2,
  (-7 + x)^2 (-5 + x)^10 (5 + x)^15 (16 - 11 x + x^2),
  (-9 + x) (-7 + x)^2 (-5 + x)^8 (-3 + x) (5 + x)^15 (16 - 9 x + x^2),
  (-7 + x) (-5 + x)^8 (5 + x)^15 (17 - 10 x + x^2) (-176 + 101 x - 18 x^2 + x^3),
  (-7 + x)^2 (-5 + x)^8 (5 + x)^15 (388 - 431 x + 151 x^2 - 21 x^3 + x^4),
  (-7 + x)^3 (-5 + x)^8 (-3 + x) (5 + x)^15 (20 - 11 x + x^2),
  (-7 + x) (-5 + x)^8 (5 + x)^15 (-2616 + 3365 x - 1484 x^2 + 298 x^3 - 28 x^4 + x^5),
  (-8 + x) (-7 + x)^4 (-5 + x)^6 (-3 + x)^3 (5 + x)^15,
  (-7 + x) (-5 + x)^9 (5 + x)^15 (484 - 565 x + 183 x^2 - 23 x^3 + x^4),
  (-7 + x)^6 (-5 + x)^4 (-4 + x) (-3 + x)^3 (5 + x)^15,
  (-7 + x)^2 (-5 + x)^9 (5 + x)^15 (-64 + 71 x - 16 x^2 + x^3),
  (-7 + x)^3 (-5 + x)^7 (5 + x)^15 (256 - 313 x + 123 x^2 - 19 x^3 + x^4),
  (-7 + x)^3 (-5 + x)^8 (5 + x)^15 (-44 + 53 x - 14 x^2 + x^3),
  (-7 + x)^4 (-5 + x)^7 (-3 + x) (5 + x)^15 (12 - 9 x + x^2), (-7 + x)^5 (-5 + x)^6
  (-3 + x) (5 + x)^15 (8 - 7 x + x^2), (-7 + x)^4 (-5 + x)^8 (5 + x)^15 (4 - 7 x + x^2) };
```

`Length[dim14listmod128]`

31

```

chi = (-11 + x) (-5 + x)^12 (-4 + x) (5 + x)^15
      (-11 + x) (-5 + x)^12 (-4 + x) (5 + x)^15

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{15, 47, -15, 1}, {7, 47, -15, 1}, {-1, 47, -15, 1}, {-9, 47, -15, 1}}
```

```

A = {{-9, 47, -15, 1}, {-1, 47, -15, 1}, {7, 47, -15, 1}, {15, 47, -15, 1}};

A // MatrixForm

$$\begin{pmatrix} -9 & 47 & -15 & 1 \\ -1 & 47 & -15 & 1 \\ 7 & 47 & -15 & 1 \\ 15 & 47 & -15 & 1 \end{pmatrix}$$


g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{-285, 1363, -435, 29}

Array[c, 4].Transpose[A]
{-9 c[1] + 47 c[2] - 15 c[3] + c[4], -c[1] + 47 c[2] - 15 c[3] + c[4],
 7 c[1] + 47 c[2] - 15 c[3] + c[4], 15 c[1] + 47 c[2] - 15 c[3] + c[4]}

Array[c, 4].g
-285 c[1] + 1363 c[2] - 435 c[3] + 29 c[4]

cert =
Flatten[Array[c, 4] /. FindInstance[-285 c[1] + 1363 c[2] - 435 c[3] + 29 c[4] < 0 &&
-9 c[1] + 47 c[2] - 15 c[3] + c[4] ≥ 0 &&
-c[1] + 47 c[2] - 15 c[3] + c[4] ≥ 0 && 7 c[1] + 47 c[2] - 15 c[3] + c[4] ≥ 0 &&
15 c[1] + 47 c[2] - 15 c[3] + c[4] ≥ 0, Array[c, 4], Integers]]
{88, 0, 0, 846}

GCD[88, 0, 0, 846]
2

cert = cert / 2
{44, 0, 0, 423}

Reverse[cert]
{423, 0, 0, 44}

cert.g
-273

cert.Transpose[A]
{27, 379, 731, 1083}

In[6]:= infeasiblecertshortcut[(-11+x) (-5+x)^12 (-4+x) (5+x)^15,
  feasibleinterlacingpolylist[(-11+x) (-5+x)^12 (-4+x) (5+x)^15]]
Out[6]= {423, 0, 0, 44}

```

```

chi = (-7 + x)^4 (-5 + x)^8 (5 + x)^15 (4 - 7 x + x^2)
(-7 + x)^4 (-5 + x)^8 (5 + x)^15 (4 - 7 x + x^2)

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{{-105, -34, 56, -14, 1}, {-89, -34, 56, -14, 1}, {7, -50, 56, -14, 1},
{-49, -42, 56, -14, 1}, {-33, -42, 56, -14, 1}, {-145, -26, 56, -14, 1}}}

A = {{7, -50, 56, -14, 1}, {-49, -42, 56, -14, 1}, {-33, -42, 56, -14, 1},
{-105, -34, 56, -14, 1}, {-89, -34, 56, -14, 1}, {-145, -26, 56, -14, 1}};

A // MatrixForm

$$\begin{pmatrix} 7 & -50 & 56 & -14 & 1 \\ -49 & -42 & 56 & -14 & 1 \\ -33 & -42 & 56 & -14 & 1 \\ -105 & -34 & 56 & -14 & 1 \\ -89 & -34 & 56 & -14 & 1 \\ -145 & -26 & 56 & -14 & 1 \end{pmatrix}$$


g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{-645, -1274, 1624, -406, 29}

Array[c, 5].Transpose[A]
{7 c[1] - 50 c[2] + 56 c[3] - 14 c[4] + c[5],
 -49 c[1] - 42 c[2] + 56 c[3] - 14 c[4] + c[5], -33 c[1] - 42 c[2] + 56 c[3] - 14 c[4] + c[5],
 -105 c[1] - 34 c[2] + 56 c[3] - 14 c[4] + c[5],
 -89 c[1] - 34 c[2] + 56 c[3] - 14 c[4] + c[5],
 -145 c[1] - 26 c[2] + 56 c[3] - 14 c[4] + c[5]}

Array[c, 5].g
-645 c[1] - 1274 c[2] + 1624 c[3] - 406 c[4] + 29 c[5]

cert = Flatten[Array[c, 5] /.
FindInstance[-645 c[1] - 1274 c[2] + 1624 c[3] - 406 c[4] + 29 c[5] < 0 &&
7 c[1] - 50 c[2] + 56 c[3] - 14 c[4] + c[5] ≥ 0 &&
-49 c[1] - 42 c[2] + 56 c[3] - 14 c[4] + c[5] ≥ 0 &&
-33 c[1] - 42 c[2] + 56 c[3] - 14 c[4] + c[5] ≥ 0 &&
-105 c[1] - 34 c[2] + 56 c[3] - 14 c[4] + c[5] ≥ 0 &&
-89 c[1] - 34 c[2] + 56 c[3] - 14 c[4] + c[5] ≥ 0 &&
-145 c[1] - 26 c[2] + 56 c[3] - 14 c[4] + c[5] ≥ 0, Array[c, 5], Integers]]
{-126, -631, 0, 0, -30576}

GCD[-126, -631, 0, 0, -30576]
1

Reverse[cert]
{-30576, 0, 0, -631, -126}

cert.g
-1540

```

```

cert.Transpose[A]
{92, 2100, 84, 4108, 2092, 4100}

In[=] := infeasiblecertshortcut[(-7 + x)4 (-5 + x)8 (5 + x)15 (4 - 7 x + x2),  

feasibleinterlacingpolylist[(-7 + x)4 (-5 + x)8 (5 + x)15 (4 - 7 x + x2)]]
Out[=] = {-30576, 0, 0, -631, -126}

chi = (-7 + x)6 (-5 + x)4 (-4 + x) (-3 + x)3 (5 + x)15  

(-7 + x)6 (-5 + x)4 (-4 + x) (-3 + x)3 (5 + x)15

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{15, -98, 64, -14, 1} }

A = {{15, -98, 64, -14, 1}};
A // MatrixForm
( 15 -98 64 -14 1 )

g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{195, -2826, 1856, -406, 29}

Array[c, 5].Transpose[A]
{15 c[1] - 98 c[2] + 64 c[3] - 14 c[4] + c[5] }

Array[c, 5].g
195 c[1] - 2826 c[2] + 1856 c[3] - 406 c[4] + 29 c[5]

cert = Flatten[
Array[c, 5] /. FindInstance[195 c[1] - 2826 c[2] + 1856 c[3] - 406 c[4] + 29 c[5] < 0 &&
15 c[1] - 98 c[2] + 64 c[3] - 14 c[4] + c[5] ≥ 0, Array[c, 5], Integers]]
{0, -342, 0, 0, -33465}

GCD[0, -342, 0, 0, -33465]
3

cert = cert / 3
{0, -114, 0, 0, -11155}

Reverse[cert]
{-11155, 0, 0, -114, 0}

cert.g
-1331

```

```

cert.Transpose[A]
{17}

chi = (-8 + x) (-7 + x)4 (-5 + x)6 (-3 + x)3 (5 + x)15
(-8 + x) (-7 + x)4 (-5 + x)6 (-3 + x)3 (5 + x)15

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{{-105, -174, 104, -18, 1}, {63, -198, 104, -18, 1}, {-9, -190, 104, -18, 1},
{7, -190, 104, -18, 1}, {-65, -182, 104, -18, 1}, {-49, -182, 104, -18, 1}}}

A = {{63, -198, 104, -18, 1}, {-9, -190, 104, -18, 1}, {7, -190, 104, -18, 1},
{-65, -182, 104, -18, 1}, {-49, -182, 104, -18, 1}, {-105, -174, 104, -18, 1}};

A // MatrixForm

$$\begin{pmatrix} 63 & -198 & 104 & -18 & 1 \\ -9 & -190 & 104 & -18 & 1 \\ 7 & -190 & 104 & -18 & 1 \\ -65 & -182 & 104 & -18 & 1 \\ -49 & -182 & 104 & -18 & 1 \\ -105 & -174 & 104 & -18 & 1 \end{pmatrix}$$


g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{435, -5598, 3016, -522, 29}

Array[c, 5].Transpose[A]
{63 c[1] - 198 c[2] + 104 c[3] - 18 c[4] + c[5],
-9 c[1] - 190 c[2] + 104 c[3] - 18 c[4] + c[5],
7 c[1] - 190 c[2] + 104 c[3] - 18 c[4] + c[5],
-65 c[1] - 182 c[2] + 104 c[3] - 18 c[4] + c[5],
-49 c[1] - 182 c[2] + 104 c[3] - 18 c[4] + c[5],
-105 c[1] - 174 c[2] + 104 c[3] - 18 c[4] + c[5]}

Array[c, 5].g
435 c[1] - 5598 c[2] + 3016 c[3] - 522 c[4] + 29 c[5]

```

```

cert = Flatten[
  Array[c, 5] /. FindInstance[435 c[1] - 5598 c[2] + 3016 c[3] - 522 c[4] + 29 c[5] < 0 &&
    63 c[1] - 198 c[2] + 104 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -9 c[1] - 190 c[2] + 104 c[3] - 18 c[4] + c[5] ≥ 0 &&
    7 c[1] - 190 c[2] + 104 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -65 c[1] - 182 c[2] + 104 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -49 c[1] - 182 c[2] + 104 c[3] - 18 c[4] + c[5] ≥ 0 &&
    -105 c[1] - 174 c[2] + 104 c[3] - 18 c[4] + c[5] ≥ 0, Array[c, 5], Integers]]
{102, 916, 0, 0, 175136}

GCD[102, 916, 0, 0, 175136]
2

cert = cert / 2
{51, 458, 0, 0, 87568}

Reverse[cert]
{87568, 0, 0, 458, 51}

cert.g
-2227

cert.Transpose[A]
{97, 89, 905, 897, 1713, 2521}

```

$$\begin{aligned} \text{chi} = & (-5 + x)^{11} (5 + x)^{15} (-188 + 119x - 20x^2 + x^3) \\ & (-5 + x)^{11} (5 + x)^{15} (-188 + 119x - 20x^2 + x^3) \end{aligned}$$

CoefficientList[feasibleinterlacingpolylist[chi], x]

```

{{-315, -172, 122, -20, 1}, {-299, -172, 122, -20, 1},
 {37, -220, 122, -20, 1}, {53, -220, 122, -20, 1}, {-51, -212, 122, -20, 1},
 {-35, -212, 122, -20, 1}, {-19, -212, 122, -20, 1}, {-3, -212, 122, -20, 1},
 {-123, -204, 122, -20, 1}, {-107, -204, 122, -20, 1}, {-91, -204, 122, -20, 1},
 {-75, -204, 122, -20, 1}, {-59, -204, 122, -20, 1}, {-195, -196, 122, -20, 1},
 {-179, -196, 122, -20, 1}, {-163, -196, 122, -20, 1}, {-147, -196, 122, -20, 1},
 {-131, -196, 122, -20, 1}, {-115, -196, 122, -20, 1}, {-235, -188, 122, -20, 1},
 {-219, -188, 122, -20, 1}, {-203, -188, 122, -20, 1}, {-187, -188, 122, -20, 1},
 {-275, -180, 122, -20, 1}, {-259, -180, 122, -20, 1}, {-243, -180, 122, -20, 1}}

```

```

A = {{37, -220, 122, -20, 1}, {53, -220, 122, -20, 1}, {-51, -212, 122, -20, 1},
{-35, -212, 122, -20, 1}, {-19, -212, 122, -20, 1}, {-3, -212, 122, -20, 1},
{-123, -204, 122, -20, 1}, {-107, -204, 122, -20, 1}, {-91, -204, 122, -20, 1},
{-75, -204, 122, -20, 1}, {-59, -204, 122, -20, 1}, {-195, -196, 122, -20, 1},
{-179, -196, 122, -20, 1}, {-163, -196, 122, -20, 1}, {-147, -196, 122, -20, 1},
{-131, -196, 122, -20, 1}, {-115, -196, 122, -20, 1}, {-235, -188, 122, -20, 1},
{-219, -188, 122, -20, 1}, {-203, -188, 122, -20, 1}, {-187, -188, 122, -20, 1},
{-275, -180, 122, -20, 1}, {-259, -180, 122, -20, 1}, {-243, -180, 122, -20, 1},
{-315, -172, 122, -20, 1}, {-299, -172, 122, -20, 1}};

A // MatrixForm


$$\begin{pmatrix} 37 & -220 & 122 & -20 & 1 \\ 53 & -220 & 122 & -20 & 1 \\ -51 & -212 & 122 & -20 & 1 \\ -35 & -212 & 122 & -20 & 1 \\ -19 & -212 & 122 & -20 & 1 \\ -3 & -212 & 122 & -20 & 1 \\ -123 & -204 & 122 & -20 & 1 \\ -107 & -204 & 122 & -20 & 1 \\ -91 & -204 & 122 & -20 & 1 \\ -75 & -204 & 122 & -20 & 1 \\ -59 & -204 & 122 & -20 & 1 \\ -195 & -196 & 122 & -20 & 1 \\ -179 & -196 & 122 & -20 & 1 \\ -163 & -196 & 122 & -20 & 1 \\ -147 & -196 & 122 & -20 & 1 \\ -131 & -196 & 122 & -20 & 1 \\ -115 & -196 & 122 & -20 & 1 \\ -235 & -188 & 122 & -20 & 1 \\ -219 & -188 & 122 & -20 & 1 \\ -203 & -188 & 122 & -20 & 1 \\ -187 & -188 & 122 & -20 & 1 \\ -275 & -180 & 122 & -20 & 1 \\ -259 & -180 & 122 & -20 & 1 \\ -243 & -180 & 122 & -20 & 1 \\ -315 & -172 & 122 & -20 & 1 \\ -299 & -172 & 122 & -20 & 1 \end{pmatrix}$$


g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{785, -6268, 3538, -580, 29}

```

Array[c, 5].Transpose[A]

```
{37 c[1] - 220 c[2] + 122 c[3] - 20 c[4] + c[5],  
 53 c[1] - 220 c[2] + 122 c[3] - 20 c[4] + c[5],  
 -51 c[1] - 212 c[2] + 122 c[3] - 20 c[4] + c[5],  
 -35 c[1] - 212 c[2] + 122 c[3] - 20 c[4] + c[5],  
 -19 c[1] - 212 c[2] + 122 c[3] - 20 c[4] + c[5],  
 -3 c[1] - 212 c[2] + 122 c[3] - 20 c[4] + c[5],  
 -123 c[1] - 204 c[2] + 122 c[3] - 20 c[4] + c[5],  
 -107 c[1] - 204 c[2] + 122 c[3] - 20 c[4] + c[5],  
 -91 c[1] - 204 c[2] + 122 c[3] - 20 c[4] + c[5],  
 -75 c[1] - 204 c[2] + 122 c[3] - 20 c[4] + c[5],  
 -59 c[1] - 204 c[2] + 122 c[3] - 20 c[4] + c[5],  
 -195 c[1] - 196 c[2] + 122 c[3] - 20 c[4] + c[5],  
 -179 c[1] - 196 c[2] + 122 c[3] - 20 c[4] + c[5],  
 -163 c[1] - 196 c[2] + 122 c[3] - 20 c[4] + c[5],  
 -147 c[1] - 196 c[2] + 122 c[3] - 20 c[4] + c[5],  
 -131 c[1] - 196 c[2] + 122 c[3] - 20 c[4] + c[5],  
 -115 c[1] - 196 c[2] + 122 c[3] - 20 c[4] + c[5],  
 -235 c[1] - 188 c[2] + 122 c[3] - 20 c[4] + c[5],  
 -219 c[1] - 188 c[2] + 122 c[3] - 20 c[4] + c[5],  
 -203 c[1] - 188 c[2] + 122 c[3] - 20 c[4] + c[5],  
 -187 c[1] - 188 c[2] + 122 c[3] - 20 c[4] + c[5],  
 -275 c[1] - 180 c[2] + 122 c[3] - 20 c[4] + c[5],  
 -259 c[1] - 180 c[2] + 122 c[3] - 20 c[4] + c[5],  
 -243 c[1] - 180 c[2] + 122 c[3] - 20 c[4] + c[5],  
 -315 c[1] - 172 c[2] + 122 c[3] - 20 c[4] + c[5],  
 -299 c[1] - 172 c[2] + 122 c[3] - 20 c[4] + c[5]}
```

Array[c, 5].g

```
785 c[1] - 6268 c[2] + 3538 c[3] - 580 c[4] + 29 c[5]
```

```

cert = Flatten[
  Array[c, 5] /. FindInstance[785 c[1] - 6268 c[2] + 3538 c[3] - 580 c[4] + 29 c[5] < 0 &&
    37 c[1] - 220 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    53 c[1] - 220 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -51 c[1] - 212 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -35 c[1] - 212 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -19 c[1] - 212 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -3 c[1] - 212 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -123 c[1] - 204 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -107 c[1] - 204 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -91 c[1] - 204 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -75 c[1] - 204 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -59 c[1] - 204 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -195 c[1] - 196 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -179 c[1] - 196 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -163 c[1] - 196 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -147 c[1] - 196 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -131 c[1] - 196 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -115 c[1] - 196 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -235 c[1] - 188 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -219 c[1] - 188 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -203 c[1] - 188 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -187 c[1] - 188 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -275 c[1] - 180 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -259 c[1] - 180 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -243 c[1] - 180 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -315 c[1] - 172 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0 &&
    -299 c[1] - 172 c[2] + 122 c[3] - 20 c[4] + c[5] ≥ 0, Array[c, 5], Integers]]

{-366, -2563, 0, 0, -544 242}

GCD[-366, -2563, 0, 0, -544 242]
1

Reverse[cert]
{-544 242, 0, 0, -2563, -366}

cert.g
-5444

cert.Transpose[A]
{6076, 220, 17780, 11924, 6068, 212, 23628, 17772,
 11916, 6060, 204, 29476, 23620, 17764, 11908, 6052, 196,
 23612, 17756, 11900, 6044, 17748, 11892, 6036, 11884, 6028}

```

$$\text{chi} = (-7 + x) (-5 + x)^{10} (-3 + x) (5 + x)^{15} (48 - 15 x + x^2)$$

$$(-7 + x) (-5 + x)^{10} (-3 + x) (5 + x)^{15} (48 - 15 x + x^2)$$

```

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{{-345, 1249, -846, 222, -25, 1}, {15, 1137, -838, 222, -25, 1},
  {-65, 1153, -838, 222, -25, 1}, {-145, 1169, -838, 222, -25, 1},
  {-225, 1185, -838, 222, -25, 1}, {-273, 1201, -838, 222, -25, 1},
  {295, 1041, -830, 222, -25, 1}, {215, 1057, -830, 222, -25, 1},
  {135, 1073, -830, 222, -25, 1}, {55, 1089, -830, 222, -25, 1},
  {-25, 1105, -830, 222, -25, 1}, {-105, 1121, -830, 222, -25, 1},
  {495, 961, -822, 222, -25, 1}, {415, 977, -822, 222, -25, 1},
  {335, 993, -822, 222, -25, 1}, {255, 1009, -822, 222, -25, 1},
  {175, 1025, -822, 222, -25, 1}, {695, 881, -814, 222, -25, 1},
  {615, 897, -814, 222, -25, 1}, {535, 913, -814, 222, -25, 1},
  {455, 929, -814, 222, -25, 1}, {895, 801, -806, 222, -25, 1},
  {815, 817, -806, 222, -25, 1}, {735, 833, -806, 222, -25, 1},
  {1095, 721, -798, 222, -25, 1}, {1015, 737, -798, 222, -25, 1}}}

A = {{-345, 1249, -846, 222, -25, 1}, {15, 1137, -838, 222, -25, 1},
  {-65, 1153, -838, 222, -25, 1}, {-145, 1169, -838, 222, -25, 1},
  {-225, 1185, -838, 222, -25, 1}, {-273, 1201, -838, 222, -25, 1},
  {295, 1041, -830, 222, -25, 1}, {215, 1057, -830, 222, -25, 1},
  {135, 1073, -830, 222, -25, 1}, {55, 1089, -830, 222, -25, 1},
  {-25, 1105, -830, 222, -25, 1}, {-105, 1121, -830, 222, -25, 1},
  {495, 961, -822, 222, -25, 1}, {415, 977, -822, 222, -25, 1},
  {335, 993, -822, 222, -25, 1}, {255, 1009, -822, 222, -25, 1},
  {175, 1025, -822, 222, -25, 1}, {695, 881, -814, 222, -25, 1},
  {615, 897, -814, 222, -25, 1}, {535, 913, -814, 222, -25, 1},
  {455, 929, -814, 222, -25, 1}, {895, 801, -806, 222, -25, 1},
  {815, 817, -806, 222, -25, 1}, {735, 833, -806, 222, -25, 1},
  {1095, 721, -798, 222, -25, 1}, {1015, 737, -798, 222, -25, 1}};
```

```
A // MatrixForm
```

$$\begin{pmatrix} -345 & 1249 & -846 & 222 & -25 & 1 \\ 15 & 1137 & -838 & 222 & -25 & 1 \\ -65 & 1153 & -838 & 222 & -25 & 1 \\ -145 & 1169 & -838 & 222 & -25 & 1 \\ -225 & 1185 & -838 & 222 & -25 & 1 \\ -273 & 1201 & -838 & 222 & -25 & 1 \\ 295 & 1041 & -830 & 222 & -25 & 1 \\ 215 & 1057 & -830 & 222 & -25 & 1 \\ 135 & 1073 & -830 & 222 & -25 & 1 \\ 55 & 1089 & -830 & 222 & -25 & 1 \\ -25 & 1105 & -830 & 222 & -25 & 1 \\ -105 & 1121 & -830 & 222 & -25 & 1 \\ 495 & 961 & -822 & 222 & -25 & 1 \\ 415 & 977 & -822 & 222 & -25 & 1 \\ 335 & 993 & -822 & 222 & -25 & 1 \\ 255 & 1009 & -822 & 222 & -25 & 1 \\ 175 & 1025 & -822 & 222 & -25 & 1 \\ 695 & 881 & -814 & 222 & -25 & 1 \\ 615 & 897 & -814 & 222 & -25 & 1 \\ 535 & 913 & -814 & 222 & -25 & 1 \\ 455 & 929 & -814 & 222 & -25 & 1 \\ 895 & 801 & -806 & 222 & -25 & 1 \\ 815 & 817 & -806 & 222 & -25 & 1 \\ 735 & 833 & -806 & 222 & -25 & 1 \\ 1095 & 721 & -798 & 222 & -25 & 1 \\ 1015 & 737 & -798 & 222 & -25 & 1 \end{pmatrix}$$

```
g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{-5325, 34125, -24270, 6438, -725, 29}
```

Array[c, 6].Transpose[A]

```

{-345 c[1] + 1249 c[2] - 846 c[3] + 222 c[4] - 25 c[5] + c[6],
 15 c[1] + 1137 c[2] - 838 c[3] + 222 c[4] - 25 c[5] + c[6],
 -65 c[1] + 1153 c[2] - 838 c[3] + 222 c[4] - 25 c[5] + c[6],
 -145 c[1] + 1169 c[2] - 838 c[3] + 222 c[4] - 25 c[5] + c[6],
 -225 c[1] + 1185 c[2] - 838 c[3] + 222 c[4] - 25 c[5] + c[6],
 -273 c[1] + 1201 c[2] - 838 c[3] + 222 c[4] - 25 c[5] + c[6],
 295 c[1] + 1041 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6],
 215 c[1] + 1057 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6],
 135 c[1] + 1073 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6],
 55 c[1] + 1089 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6],
 -25 c[1] + 1105 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6],
 -105 c[1] + 1121 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6],
 495 c[1] + 961 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6],
 415 c[1] + 977 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6],
 335 c[1] + 993 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6],
 255 c[1] + 1009 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6],
 175 c[1] + 1025 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6],
 695 c[1] + 881 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6],
 615 c[1] + 897 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6],
 535 c[1] + 913 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6],
 455 c[1] + 929 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6],
 895 c[1] + 801 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6],
 815 c[1] + 817 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6],
 735 c[1] + 833 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6],
 1095 c[1] + 721 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6],
 1015 c[1] + 737 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6]}

```

Array[c, 6].g

```
-5325 c[1] + 34 125 c[2] - 24 270 c[3] + 6438 c[4] - 725 c[5] + 29 c[6]
```

```

cert = Flatten[Array[c, 6] /. FindInstance[
  -5325 c[1] + 34125 c[2] - 24270 c[3] + 6438 c[4] - 725 c[5] + 29 c[6] < 0 &&
  -345 c[1] + 1249 c[2] - 846 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  15 c[1] + 1137 c[2] - 838 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  -65 c[1] + 1153 c[2] - 838 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  -145 c[1] + 1169 c[2] - 838 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  -225 c[1] + 1185 c[2] - 838 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  -273 c[1] + 1201 c[2] - 838 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  295 c[1] + 1041 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  215 c[1] + 1057 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  135 c[1] + 1073 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  55 c[1] + 1089 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  -25 c[1] + 1105 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  -105 c[1] + 1121 c[2] - 830 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  495 c[1] + 961 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  415 c[1] + 977 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  335 c[1] + 993 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  255 c[1] + 1009 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  175 c[1] + 1025 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  695 c[1] + 881 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  615 c[1] + 897 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  535 c[1] + 913 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  455 c[1] + 929 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  895 c[1] + 801 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  815 c[1] + 817 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  735 c[1] + 833 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1095 c[1] + 721 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 && 1015 c[1] +
  737 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0, Array[c, 6], Integers]]

{-2820, -12969, -59189, 0, 0, -34793172}

GCD[-2820, -12969, -59189, 0, 0, -34793172]

1

Reverse[cert]

{-34793172, 0, 0, -59189, -12969, -2820}

cert.g

-35583

cert.Transpose[A]

{55341, 19157, 37253, 55349, 73445, 1301, 1069, 19165,
 37261, 55357, 73453, 91549, 1077, 19173, 37269, 55365, 73461,
 1085, 19181, 37277, 55373, 1093, 19189, 37285, 1101, 19197}

```

$$\text{chi} = (-7+x)^3 (-5+x)^8 (-3+x) (5+x)^{15} (20-11x+x^2)$$

$$(-7+x)^3 (-5+x)^8 (-3+x) (5+x)^{15} (20-11x+x^2)$$

```

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{735, 133, -426, 154, -21, 1}, {-9, 501, -466, 154, -21, 1},
{-57, 517, -466, 154, -21, 1}, {-105, 533, -466, 154, -21, 1},
{207, 405, -458, 154, -21, 1}, {127, 421, -458, 154, -21, 1},
{159, 421, -458, 154, -21, 1}, {79, 437, -458, 154, -21, 1},
{111, 437, -458, 154, -21, 1}, {31, 453, -458, 154, -21, 1},
{63, 453, -458, 154, -21, 1}, {375, 325, -450, 154, -21, 1},
{295, 341, -450, 154, -21, 1}, {327, 341, -450, 154, -21, 1},
{215, 357, -450, 154, -21, 1}, {247, 357, -450, 154, -21, 1},
{279, 357, -450, 154, -21, 1}, {199, 373, -450, 154, -21, 1},
{231, 373, -450, 154, -21, 1}, {495, 261, -442, 154, -21, 1},
{415, 277, -442, 154, -21, 1}, {447, 277, -442, 154, -21, 1},
{335, 293, -442, 154, -21, 1}, {367, 293, -442, 154, -21, 1},
{399, 293, -442, 154, -21, 1}, {287, 309, -442, 154, -21, 1},
{615, 197, -434, 154, -21, 1}, {535, 213, -434, 154, -21, 1},
{567, 213, -434, 154, -21, 1}, {455, 229, -434, 154, -21, 1}}
A = {{-9, 501, -466, 154, -21, 1}, {-57, 517, -466, 154, -21, 1},
{-105, 533, -466, 154, -21, 1}, {207, 405, -458, 154, -21, 1},
{127, 421, -458, 154, -21, 1}, {159, 421, -458, 154, -21, 1},
{79, 437, -458, 154, -21, 1}, {111, 437, -458, 154, -21, 1},
{31, 453, -458, 154, -21, 1}, {63, 453, -458, 154, -21, 1},
{375, 325, -450, 154, -21, 1}, {295, 341, -450, 154, -21, 1},
{327, 341, -450, 154, -21, 1}, {215, 357, -450, 154, -21, 1},
{247, 357, -450, 154, -21, 1}, {279, 357, -450, 154, -21, 1},
{199, 373, -450, 154, -21, 1}, {231, 373, -450, 154, -21, 1},
{495, 261, -442, 154, -21, 1}, {415, 277, -442, 154, -21, 1},
{447, 277, -442, 154, -21, 1}, {335, 293, -442, 154, -21, 1},
{367, 293, -442, 154, -21, 1}, {399, 293, -442, 154, -21, 1},
{287, 309, -442, 154, -21, 1}, {615, 197, -434, 154, -21, 1},
{535, 213, -434, 154, -21, 1}, {567, 213, -434, 154, -21, 1},
{455, 229, -434, 154, -21, 1}};

```

```

A // MatrixForm


$$\left( \begin{array}{ccccccc}
-9 & 501 & -466 & 154 & -21 & 1 \\
-57 & 517 & -466 & 154 & -21 & 1 \\
-105 & 533 & -466 & 154 & -21 & 1 \\
207 & 405 & -458 & 154 & -21 & 1 \\
127 & 421 & -458 & 154 & -21 & 1 \\
159 & 421 & -458 & 154 & -21 & 1 \\
79 & 437 & -458 & 154 & -21 & 1 \\
111 & 437 & -458 & 154 & -21 & 1 \\
31 & 453 & -458 & 154 & -21 & 1 \\
63 & 453 & -458 & 154 & -21 & 1 \\
375 & 325 & -450 & 154 & -21 & 1 \\
295 & 341 & -450 & 154 & -21 & 1 \\
327 & 341 & -450 & 154 & -21 & 1 \\
215 & 357 & -450 & 154 & -21 & 1 \\
247 & 357 & -450 & 154 & -21 & 1 \\
279 & 357 & -450 & 154 & -21 & 1 \\
199 & 373 & -450 & 154 & -21 & 1 \\
231 & 373 & -450 & 154 & -21 & 1 \\
495 & 261 & -442 & 154 & -21 & 1 \\
415 & 277 & -442 & 154 & -21 & 1 \\
447 & 277 & -442 & 154 & -21 & 1 \\
335 & 293 & -442 & 154 & -21 & 1 \\
367 & 293 & -442 & 154 & -21 & 1 \\
399 & 293 & -442 & 154 & -21 & 1 \\
287 & 309 & -442 & 154 & -21 & 1 \\
615 & 197 & -434 & 154 & -21 & 1 \\
535 & 213 & -434 & 154 & -21 & 1 \\
567 & 213 & -434 & 154 & -21 & 1 \\
455 & 229 & -434 & 154 & -21 & 1 \\
735 & 133 & -426 & 154 & -21 & 1
\end{array} \right)$$


g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{-925, 14545, -13474, 4466, -609, 29}

```

Array[c, 6].Transpose[A]

```
{-9 c[1] + 501 c[2] - 466 c[3] + 154 c[4] - 21 c[5] + c[6],  

 -57 c[1] + 517 c[2] - 466 c[3] + 154 c[4] - 21 c[5] + c[6],  

 -105 c[1] + 533 c[2] - 466 c[3] + 154 c[4] - 21 c[5] + c[6],  

 207 c[1] + 405 c[2] - 458 c[3] + 154 c[4] - 21 c[5] + c[6],  

 127 c[1] + 421 c[2] - 458 c[3] + 154 c[4] - 21 c[5] + c[6],  

 159 c[1] + 421 c[2] - 458 c[3] + 154 c[4] - 21 c[5] + c[6],  

 79 c[1] + 437 c[2] - 458 c[3] + 154 c[4] - 21 c[5] + c[6],  

 111 c[1] + 437 c[2] - 458 c[3] + 154 c[4] - 21 c[5] + c[6],  

 31 c[1] + 453 c[2] - 458 c[3] + 154 c[4] - 21 c[5] + c[6],  

 63 c[1] + 453 c[2] - 458 c[3] + 154 c[4] - 21 c[5] + c[6],  

 375 c[1] + 325 c[2] - 450 c[3] + 154 c[4] - 21 c[5] + c[6],  

 295 c[1] + 341 c[2] - 450 c[3] + 154 c[4] - 21 c[5] + c[6],  

 327 c[1] + 341 c[2] - 450 c[3] + 154 c[4] - 21 c[5] + c[6],  

 215 c[1] + 357 c[2] - 450 c[3] + 154 c[4] - 21 c[5] + c[6],  

 247 c[1] + 357 c[2] - 450 c[3] + 154 c[4] - 21 c[5] + c[6],  

 279 c[1] + 357 c[2] - 450 c[3] + 154 c[4] - 21 c[5] + c[6],  

 199 c[1] + 373 c[2] - 450 c[3] + 154 c[4] - 21 c[5] + c[6],  

 231 c[1] + 373 c[2] - 450 c[3] + 154 c[4] - 21 c[5] + c[6],  

 495 c[1] + 261 c[2] - 442 c[3] + 154 c[4] - 21 c[5] + c[6],  

 415 c[1] + 277 c[2] - 442 c[3] + 154 c[4] - 21 c[5] + c[6],  

 447 c[1] + 277 c[2] - 442 c[3] + 154 c[4] - 21 c[5] + c[6],  

 335 c[1] + 293 c[2] - 442 c[3] + 154 c[4] - 21 c[5] + c[6],  

 367 c[1] + 293 c[2] - 442 c[3] + 154 c[4] - 21 c[5] + c[6],  

 399 c[1] + 293 c[2] - 442 c[3] + 154 c[4] - 21 c[5] + c[6],  

 287 c[1] + 309 c[2] - 442 c[3] + 154 c[4] - 21 c[5] + c[6],  

 615 c[1] + 197 c[2] - 434 c[3] + 154 c[4] - 21 c[5] + c[6],  

 535 c[1] + 213 c[2] - 434 c[3] + 154 c[4] - 21 c[5] + c[6],  

 567 c[1] + 213 c[2] - 434 c[3] + 154 c[4] - 21 c[5] + c[6],  

 455 c[1] + 229 c[2] - 434 c[3] + 154 c[4] - 21 c[5] + c[6],  

 735 c[1] + 133 c[2] - 426 c[3] + 154 c[4] - 21 c[5] + c[6]}
```

Array[c, 6].g

```
-925 c[1] + 14 545 c[2] - 13 474 c[3] + 4466 c[4] - 609 c[5] + 29 c[6]
```

```

cert = Flatten[Array[c, 6] /. FindInstance[
-925 c[1] + 14545 c[2] - 13474 c[3] + 4466 c[4] - 609 c[5] + 29 c[6] < 0 &&
-9 c[1] + 501 c[2] - 466 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
-57 c[1] + 517 c[2] - 466 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
-105 c[1] + 533 c[2] - 466 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
207 c[1] + 405 c[2] - 458 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
127 c[1] + 421 c[2] - 458 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
159 c[1] + 421 c[2] - 458 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
79 c[1] + 437 c[2] - 458 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
111 c[1] + 437 c[2] - 458 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
31 c[1] + 453 c[2] - 458 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
63 c[1] + 453 c[2] - 458 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
375 c[1] + 325 c[2] - 450 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
295 c[1] + 341 c[2] - 450 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
327 c[1] + 341 c[2] - 450 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
215 c[1] + 357 c[2] - 450 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
247 c[1] + 357 c[2] - 450 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
279 c[1] + 357 c[2] - 450 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
199 c[1] + 373 c[2] - 450 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
231 c[1] + 373 c[2] - 450 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
495 c[1] + 261 c[2] - 442 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
415 c[1] + 277 c[2] - 442 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
447 c[1] + 277 c[2] - 442 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
335 c[1] + 293 c[2] - 442 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
367 c[1] + 293 c[2] - 442 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
399 c[1] + 293 c[2] - 442 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
287 c[1] + 309 c[2] - 442 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
615 c[1] + 197 c[2] - 434 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
535 c[1] + 213 c[2] - 434 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
567 c[1] + 213 c[2] - 434 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
455 c[1] + 229 c[2] - 434 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 && 735 c[1] +
133 c[2] - 426 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0, Array[c, 6], Integers]]
{361, 1084, 4712, 0, 0, 1656424}

GCD[361, 1084, 4712, 0, 0, 1656424]
1

Reverse[cert]
{1656424, 0, 0, 4712, 1084, 361}

cert.g
-20337

cert.Transpose[A]
{467, 483, 499, 12075, 539, 12091, 555, 12107, 571, 12123, 23699,
12163, 23715, 627, 12179, 23731, 12195, 23747, 35339, 23803, 35355,
12267, 23819, 35371, 12283, 46979, 35443, 46995, 23907, 58619}

```

```

chi = (-7 + x)^4 (-5 + x)^7 (-3 + x) (5 + x)^15 (12 - 9 x + x^2)
(-7 + x)^4 (-5 + x)^7 (-3 + x) (5 + x)^15 (12 - 9 x + x^2)

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{525, 65, -314, 126, -19, 1},
 {-11, 305, -338, 126, -19, 1}, {21, 305, -338, 126, -19, 1},
 {157, 225, -330, 126, -19, 1}, {189, 225, -330, 126, -19, 1},
 {77, 241, -330, 126, -19, 1}, {325, 145, -322, 126, -19, 1},
 {357, 145, -322, 126, -19, 1}, {245, 161, -322, 126, -19, 1}};

A = {{-11, 305, -338, 126, -19, 1},
      {21, 305, -338, 126, -19, 1}, {157, 225, -330, 126, -19, 1},
      {189, 225, -330, 126, -19, 1}, {77, 241, -330, 126, -19, 1},
      {325, 145, -322, 126, -19, 1}, {357, 145, -322, 126, -19, 1},
      {245, 161, -322, 126, -19, 1}, {525, 65, -314, 126, -19, 1}};

A // MatrixForm

$$\begin{pmatrix} -11 & 305 & -338 & 126 & -19 & 1 \\ 21 & 305 & -338 & 126 & -19 & 1 \\ 157 & 225 & -330 & 126 & -19 & 1 \\ 189 & 225 & -330 & 126 & -19 & 1 \\ 77 & 241 & -330 & 126 & -19 & 1 \\ 325 & 145 & -322 & 126 & -19 & 1 \\ 357 & 145 & -322 & 126 & -19 & 1 \\ 245 & 161 & -322 & 126 & -19 & 1 \\ 525 & 65 & -314 & 126 & -19 & 1 \end{pmatrix}$$


g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{345, 8829, -9810, 3654, -551, 29}

Array[c, 6].Transpose[A]
{-11 c[1] + 305 c[2] - 338 c[3] + 126 c[4] - 19 c[5] + c[6],
 21 c[1] + 305 c[2] - 338 c[3] + 126 c[4] - 19 c[5] + c[6],
 157 c[1] + 225 c[2] - 330 c[3] + 126 c[4] - 19 c[5] + c[6],
 189 c[1] + 225 c[2] - 330 c[3] + 126 c[4] - 19 c[5] + c[6],
 77 c[1] + 241 c[2] - 330 c[3] + 126 c[4] - 19 c[5] + c[6],
 325 c[1] + 145 c[2] - 322 c[3] + 126 c[4] - 19 c[5] + c[6],
 357 c[1] + 145 c[2] - 322 c[3] + 126 c[4] - 19 c[5] + c[6],
 245 c[1] + 161 c[2] - 322 c[3] + 126 c[4] - 19 c[5] + c[6],
 525 c[1] + 65 c[2] - 314 c[3] + 126 c[4] - 19 c[5] + c[6]}

Array[c, 6].g
345 c[1] + 8829 c[2] - 9810 c[3] + 3654 c[4] - 551 c[5] + 29 c[6]

```

```

cert = Flatten[Array[c, 6] /.
  FindInstance[345 c[1] + 8829 c[2] - 9810 c[3] + 3654 c[4] - 551 c[5] + 29 c[6] < 0 &&
    -11 c[1] + 305 c[2] - 338 c[3] + 126 c[4] - 19 c[5] + c[6] ≥ 0 &&
    21 c[1] + 305 c[2] - 338 c[3] + 126 c[4] - 19 c[5] + c[6] ≥ 0 &&
    157 c[1] + 225 c[2] - 330 c[3] + 126 c[4] - 19 c[5] + c[6] ≥ 0 &&
    189 c[1] + 225 c[2] - 330 c[3] + 126 c[4] - 19 c[5] + c[6] ≥ 0 &&
    77 c[1] + 241 c[2] - 330 c[3] + 126 c[4] - 19 c[5] + c[6] ≥ 0 &&
    325 c[1] + 145 c[2] - 322 c[3] + 126 c[4] - 19 c[5] + c[6] ≥ 0 &&
    357 c[1] + 145 c[2] - 322 c[3] + 126 c[4] - 19 c[5] + c[6] ≥ 0 &&
    245 c[1] + 161 c[2] - 322 c[3] + 126 c[4] - 19 c[5] + c[6] ≥ 0 && 525 c[1] +
    65 c[2] - 314 c[3] + 126 c[4] - 19 c[5] + c[6] ≥ 0, Array[c, 6], Integers]]
{0, 0, 2913, 0, 0, 984942}

GCD[0, 0, 2913, 0, 0, 984942]
3

cert = cert / 3
{0, 0, 971, 0, 0, 328314}

Reverse[cert]
{328314, 0, 0, 971, 0, 0}

cert.g
-4404

cert.Transpose[A]
{116, 116, 7884, 7884, 7884, 15652, 15652, 15652, 23420}

```

$$\chi = (-7+x)^5 (-5+x)^6 (-3+x) (5+x)^{15} (8-7x+x^2)$$

$$(-7+x)^5 (-5+x)^6 (-3+x) (5+x)^{15} (8-7x+x^2)$$

```

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{15, 217, -254, 102, -17, 1}, {135, 153, -246, 102, -17, 1},
 {55, 169, -246, 102, -17, 1}, {255, 89, -238, 102, -17, 1}}

```

```

A = {{15, 217, -254, 102, -17, 1}, {135, 153, -246, 102, -17, 1},
 {55, 169, -246, 102, -17, 1}, {255, 89, -238, 102, -17, 1}};

```

```

A // MatrixForm

$$\begin{pmatrix} 15 & 217 & -254 & 102 & -17 & 1 \\ 135 & 153 & -246 & 102 & -17 & 1 \\ 55 & 169 & -246 & 102 & -17 & 1 \\ 255 & 89 & -238 & 102 & -17 & 1 \end{pmatrix}$$


```

```

g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{515, 5893, -7270, 2958, -493, 29}

Array[c, 6].Transpose[A]
{15 c[1] + 217 c[2] - 254 c[3] + 102 c[4] - 17 c[5] + c[6],
 135 c[1] + 153 c[2] - 246 c[3] + 102 c[4] - 17 c[5] + c[6],
 55 c[1] + 169 c[2] - 246 c[3] + 102 c[4] - 17 c[5] + c[6],
 255 c[1] + 89 c[2] - 238 c[3] + 102 c[4] - 17 c[5] + c[6]}

Array[c, 6].g
515 c[1] + 5893 c[2] - 7270 c[3] + 2958 c[4] - 493 c[5] + 29 c[6]

cert = Flatten[Array[c, 6] /.
  FindInstance[515 c[1] + 5893 c[2] - 7270 c[3] + 2958 c[4] - 493 c[5] + 29 c[6] < 0 &&
    15 c[1] + 217 c[2] - 254 c[3] + 102 c[4] - 17 c[5] + c[6] ≥ 0 &&
    135 c[1] + 153 c[2] - 246 c[3] + 102 c[4] - 17 c[5] + c[6] ≥ 0 &&
    55 c[1] + 169 c[2] - 246 c[3] + 102 c[4] - 17 c[5] + c[6] ≥ 0 && 255 c[1] +
      89 c[2] - 238 c[3] + 102 c[4] - 17 c[5] + c[6] ≥ 0, Array[c, 6], Integers]]
{76, 75, 67, 0, 0, 0}

GCD[76, 75, 67, 0, 0, 0]
1

Reverse[cert]
{0, 0, 0, 67, 75, 76}

cert.g
-5975

cert.Transpose[A]
{397, 5253, 373, 10109}

```

$$\begin{aligned} \text{chi} = & (-9+x) (-5+x)^{10} (5+x)^{15} (-92+75x-16x^2+x^3) \\ & (-9+x) (-5+x)^{10} (5+x)^{15} (-92+75x-16x^2+x^3) \end{aligned}$$

```

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{1575, 545, -782, 222, -25, 1},
 {-369, 1121, -822, 222, -25, 1}, {135, 993, -814, 222, -25, 1},
 {-9, 1009, -814, 222, -25, 1}, {-121, 1025, -814, 222, -25, 1},
 {495, 881, -806, 222, -25, 1}, {351, 897, -806, 222, -25, 1},
 {383, 897, -806, 222, -25, 1}, {239, 913, -806, 222, -25, 1},
 {855, 769, -798, 222, -25, 1}, {711, 785, -798, 222, -25, 1},
 {743, 785, -798, 222, -25, 1}, {775, 785, -798, 222, -25, 1},
 {631, 801, -798, 222, -25, 1}, {1215, 657, -790, 222, -25, 1},
 {1103, 673, -790, 222, -25, 1}, {1135, 673, -790, 222, -25, 1},
 {1023, 689, -790, 222, -25, 1}, {1495, 561, -782, 222, -25, 1},
 {1383, 577, -782, 222, -25, 1}, {1855, 449, -774, 222, -25, 1},
 {1775, 465, -774, 222, -25, 1}, {2135, 353, -766, 222, -25, 1}};

A = {{-369, 1121, -822, 222, -25, 1},
 {135, 993, -814, 222, -25, 1}, {-9, 1009, -814, 222, -25, 1},
 {-121, 1025, -814, 222, -25, 1}, {495, 881, -806, 222, -25, 1},
 {351, 897, -806, 222, -25, 1}, {383, 897, -806, 222, -25, 1},
 {239, 913, -806, 222, -25, 1}, {855, 769, -798, 222, -25, 1},
 {711, 785, -798, 222, -25, 1}, {743, 785, -798, 222, -25, 1},
 {775, 785, -798, 222, -25, 1}, {631, 801, -798, 222, -25, 1},
 {1215, 657, -790, 222, -25, 1}, {1103, 673, -790, 222, -25, 1},
 {1135, 673, -790, 222, -25, 1}, {1023, 689, -790, 222, -25, 1},
 {1575, 545, -782, 222, -25, 1}, {1495, 561, -782, 222, -25, 1},
 {1383, 577, -782, 222, -25, 1}, {1855, 449, -774, 222, -25, 1},
 {1775, 465, -774, 222, -25, 1}, {2135, 353, -766, 222, -25, 1}};

```

```
A // MatrixForm
```

$$\begin{pmatrix} -369 & 1121 & -822 & 222 & -25 & 1 \\ 135 & 993 & -814 & 222 & -25 & 1 \\ -9 & 1009 & -814 & 222 & -25 & 1 \\ -121 & 1025 & -814 & 222 & -25 & 1 \\ 495 & 881 & -806 & 222 & -25 & 1 \\ 351 & 897 & -806 & 222 & -25 & 1 \\ 383 & 897 & -806 & 222 & -25 & 1 \\ 239 & 913 & -806 & 222 & -25 & 1 \\ 855 & 769 & -798 & 222 & -25 & 1 \\ 711 & 785 & -798 & 222 & -25 & 1 \\ 743 & 785 & -798 & 222 & -25 & 1 \\ 775 & 785 & -798 & 222 & -25 & 1 \\ 631 & 801 & -798 & 222 & -25 & 1 \\ 1215 & 657 & -790 & 222 & -25 & 1 \\ 1103 & 673 & -790 & 222 & -25 & 1 \\ 1135 & 673 & -790 & 222 & -25 & 1 \\ 1023 & 689 & -790 & 222 & -25 & 1 \\ 1575 & 545 & -782 & 222 & -25 & 1 \\ 1495 & 561 & -782 & 222 & -25 & 1 \\ 1383 & 577 & -782 & 222 & -25 & 1 \\ 1855 & 449 & -774 & 222 & -25 & 1 \\ 1775 & 465 & -774 & 222 & -25 & 1 \\ 2135 & 353 & -766 & 222 & -25 & 1 \end{pmatrix}$$

```
g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{-1525, 28925, -23542, 6438, -725, 29}
```

Array[c, 6].Transpose[A]

```
{-369 c[1] + 1121 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6],  
135 c[1] + 993 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6],  
-9 c[1] + 1009 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6],  
-121 c[1] + 1025 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6],  
495 c[1] + 881 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6],  
351 c[1] + 897 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6],  
383 c[1] + 897 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6],  
239 c[1] + 913 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6],  
855 c[1] + 769 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6],  
711 c[1] + 785 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6],  
743 c[1] + 785 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6],  
775 c[1] + 785 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6],  
631 c[1] + 801 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6],  
1215 c[1] + 657 c[2] - 790 c[3] + 222 c[4] - 25 c[5] + c[6],  
1103 c[1] + 673 c[2] - 790 c[3] + 222 c[4] - 25 c[5] + c[6],  
1135 c[1] + 673 c[2] - 790 c[3] + 222 c[4] - 25 c[5] + c[6],  
1023 c[1] + 689 c[2] - 790 c[3] + 222 c[4] - 25 c[5] + c[6],  
1575 c[1] + 545 c[2] - 782 c[3] + 222 c[4] - 25 c[5] + c[6],  
1495 c[1] + 561 c[2] - 782 c[3] + 222 c[4] - 25 c[5] + c[6],  
1383 c[1] + 577 c[2] - 782 c[3] + 222 c[4] - 25 c[5] + c[6],  
1855 c[1] + 449 c[2] - 774 c[3] + 222 c[4] - 25 c[5] + c[6],  
1775 c[1] + 465 c[2] - 774 c[3] + 222 c[4] - 25 c[5] + c[6],  
2135 c[1] + 353 c[2] - 766 c[3] + 222 c[4] - 25 c[5] + c[6]}
```

Array[c, 6].g

```
-1525 c[1] + 28925 c[2] - 23542 c[3] + 6438 c[4] - 725 c[5] + 29 c[6]
```

```

cert = Flatten[Array[c, 6] /. FindInstance[
  -1525 c[1] + 28925 c[2] - 23542 c[3] + 6438 c[4] - 725 c[5] + 29 c[6] < 0 &&
  -369 c[1] + 1121 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  135 c[1] + 993 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  -9 c[1] + 1009 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  -121 c[1] + 1025 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  495 c[1] + 881 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  351 c[1] + 897 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  383 c[1] + 897 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  239 c[1] + 913 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  855 c[1] + 769 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  711 c[1] + 785 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  743 c[1] + 785 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  775 c[1] + 785 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  631 c[1] + 801 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1215 c[1] + 657 c[2] - 790 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1103 c[1] + 673 c[2] - 790 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1135 c[1] + 673 c[2] - 790 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1023 c[1] + 689 c[2] - 790 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1575 c[1] + 545 c[2] - 782 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1495 c[1] + 561 c[2] - 782 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1383 c[1] + 577 c[2] - 782 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1855 c[1] + 449 c[2] - 774 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1775 c[1] + 465 c[2] - 774 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 && 2135 c[1] +
  353 c[2] - 766 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0, Array[c, 6], Integers]]
{112, 395, 479, 0, 0, 0}

GCD[112, 395, 479, 0, 0, 0]
1

Reverse[cert]
{0, 0, 0, 479, 395, 112}

cert.g
-22 043

cert.Transpose[A]
{7729, 17449, 7641, 1417, 17361, 7553, 11137, 1329, 17273, 7465, 11049, 14633,
4825, 17185, 10961, 14545, 8321, 17097, 14457, 8233, 14369, 11729, 11641}

```

$$\begin{aligned} \text{chi} = & (-7+x)^2 (-5+x)^9 (5+x)^{15} (-64+71x-16x^2+x^3) \\ & (-7+x)^2 (-5+x)^9 (5+x)^{15} (-64+71x-16x^2+x^3) \end{aligned}$$

```

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{1085, 293, -582, 186, -23, 1}, {1053, 293, -582, 186, -23, 1},
 {-91, 629, -606, 186, -23, 1}, {1365, 197, -574, 186, -23, 1},
 {21, 613, -606, 186, -23, 1}, {525, 485, -598, 186, -23, 1},
 {381, 501, -598, 186, -23, 1}, {413, 501, -598, 186, -23, 1},
 {301, 517, -598, 186, -23, 1}, {189, 533, -598, 186, -23, 1},
 {885, 373, -590, 186, -23, 1}, {773, 389, -590, 186, -23, 1},
 {805, 389, -590, 186, -23, 1}, {693, 405, -590, 186, -23, 1},
 {581, 421, -590, 186, -23, 1}, {469, 437, -590, 186, -23, 1},
 {1165, 277, -582, 186, -23, 1}, {973, 309, -582, 186, -23, 1},
 {861, 325, -582, 186, -23, 1}, {1445, 181, -574, 186, -23, 1},
 {1253, 213, -574, 186, -23, 1}, {1725, 85, -566, 186, -23, 1},
 {1645, 101, -566, 186, -23, 1}, {1533, 117, -566, 186, -23, 1},
 {1925, 5, -558, 186, -23, 1}, {2205, -91, -550, 186, -23, 1}}

```

A = {{21, 613, -606, 186, -23, 1}, {-91, 629, -606, 186, -23, 1},
 {525, 485, -598, 186, -23, 1}, {381, 501, -598, 186, -23, 1},
 {413, 501, -598, 186, -23, 1}, {301, 517, -598, 186, -23, 1},
 {189, 533, -598, 186, -23, 1}, {885, 373, -590, 186, -23, 1},
 {773, 389, -590, 186, -23, 1}, {805, 389, -590, 186, -23, 1},
 {693, 405, -590, 186, -23, 1}, {581, 421, -590, 186, -23, 1},
 {469, 437, -590, 186, -23, 1}, {1165, 277, -582, 186, -23, 1},
 {1053, 293, -582, 186, -23, 1}, {1085, 293, -582, 186, -23, 1},
 {973, 309, -582, 186, -23, 1}, {861, 325, -582, 186, -23, 1},
 {1445, 181, -574, 186, -23, 1}, {1365, 197, -574, 186, -23, 1},
 {1253, 213, -574, 186, -23, 1}, {1725, 85, -566, 186, -23, 1},
 {1645, 101, -566, 186, -23, 1}, {1533, 117, -566, 186, -23, 1},
 {1925, 5, -558, 186, -23, 1}, {2205, -91, -550, 186, -23, 1}};

```
A // MatrixForm
```

$$\left(\begin{array}{ccccccc} 21 & 613 & -606 & 186 & -23 & 1 \\ -91 & 629 & -606 & 186 & -23 & 1 \\ 525 & 485 & -598 & 186 & -23 & 1 \\ 381 & 501 & -598 & 186 & -23 & 1 \\ 413 & 501 & -598 & 186 & -23 & 1 \\ 301 & 517 & -598 & 186 & -23 & 1 \\ 189 & 533 & -598 & 186 & -23 & 1 \\ 885 & 373 & -590 & 186 & -23 & 1 \\ 773 & 389 & -590 & 186 & -23 & 1 \\ 805 & 389 & -590 & 186 & -23 & 1 \\ 693 & 405 & -590 & 186 & -23 & 1 \\ 581 & 421 & -590 & 186 & -23 & 1 \\ 469 & 437 & -590 & 186 & -23 & 1 \\ 1165 & 277 & -582 & 186 & -23 & 1 \\ 1053 & 293 & -582 & 186 & -23 & 1 \\ 1085 & 293 & -582 & 186 & -23 & 1 \\ 973 & 309 & -582 & 186 & -23 & 1 \\ 861 & 325 & -582 & 186 & -23 & 1 \\ 1445 & 181 & -574 & 186 & -23 & 1 \\ 1365 & 197 & -574 & 186 & -23 & 1 \\ 1253 & 213 & -574 & 186 & -23 & 1 \\ 1725 & 85 & -566 & 186 & -23 & 1 \\ 1645 & 101 & -566 & 186 & -23 & 1 \\ 1533 & 117 & -566 & 186 & -23 & 1 \\ 1925 & 5 & -558 & 186 & -23 & 1 \\ 2205 & -91 & -550 & 186 & -23 & 1 \end{array} \right)$$

```
g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{2185, 16657, -17454, 5394, -667, 29}
```

```

Array[c, 6].Transpose[A]
{21 c[1] + 613 c[2] - 606 c[3] + 186 c[4] - 23 c[5] + c[6],
 -91 c[1] + 629 c[2] - 606 c[3] + 186 c[4] - 23 c[5] + c[6],
 525 c[1] + 485 c[2] - 598 c[3] + 186 c[4] - 23 c[5] + c[6],
 381 c[1] + 501 c[2] - 598 c[3] + 186 c[4] - 23 c[5] + c[6],
 413 c[1] + 501 c[2] - 598 c[3] + 186 c[4] - 23 c[5] + c[6],
 301 c[1] + 517 c[2] - 598 c[3] + 186 c[4] - 23 c[5] + c[6],
 189 c[1] + 533 c[2] - 598 c[3] + 186 c[4] - 23 c[5] + c[6],
 885 c[1] + 373 c[2] - 590 c[3] + 186 c[4] - 23 c[5] + c[6],
 773 c[1] + 389 c[2] - 590 c[3] + 186 c[4] - 23 c[5] + c[6],
 805 c[1] + 389 c[2] - 590 c[3] + 186 c[4] - 23 c[5] + c[6],
 693 c[1] + 405 c[2] - 590 c[3] + 186 c[4] - 23 c[5] + c[6],
 581 c[1] + 421 c[2] - 590 c[3] + 186 c[4] - 23 c[5] + c[6],
 469 c[1] + 437 c[2] - 590 c[3] + 186 c[4] - 23 c[5] + c[6],
 1165 c[1] + 277 c[2] - 582 c[3] + 186 c[4] - 23 c[5] + c[6],
 1053 c[1] + 293 c[2] - 582 c[3] + 186 c[4] - 23 c[5] + c[6],
 1085 c[1] + 293 c[2] - 582 c[3] + 186 c[4] - 23 c[5] + c[6],
 973 c[1] + 309 c[2] - 582 c[3] + 186 c[4] - 23 c[5] + c[6],
 861 c[1] + 325 c[2] - 582 c[3] + 186 c[4] - 23 c[5] + c[6],
 1445 c[1] + 181 c[2] - 574 c[3] + 186 c[4] - 23 c[5] + c[6],
 1365 c[1] + 197 c[2] - 574 c[3] + 186 c[4] - 23 c[5] + c[6],
 1253 c[1] + 213 c[2] - 574 c[3] + 186 c[4] - 23 c[5] + c[6],
 1725 c[1] + 85 c[2] - 566 c[3] + 186 c[4] - 23 c[5] + c[6],
 1645 c[1] + 101 c[2] - 566 c[3] + 186 c[4] - 23 c[5] + c[6],
 1533 c[1] + 117 c[2] - 566 c[3] + 186 c[4] - 23 c[5] + c[6],
 1925 c[1] + 5 c[2] - 558 c[3] + 186 c[4] - 23 c[5] + c[6],
 2205 c[1] - 91 c[2] - 550 c[3] + 186 c[4] - 23 c[5] + c[6]}

```

Array[c, 6].g

$$2185 c[1] + 16\,657 c[2] - 17\,454 c[3] + 5394 c[4] - 667 c[5] + 29 c[6]$$

```

cert = Flatten[Array[c, 6] /. FindInstance[
  2185 c[1] + 16657 c[2] - 17454 c[3] + 5394 c[4] - 667 c[5] + 29 c[6] < 0 &&
  21 c[1] + 613 c[2] - 606 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  -91 c[1] + 629 c[2] - 606 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  525 c[1] + 485 c[2] - 598 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  381 c[1] + 501 c[2] - 598 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  413 c[1] + 501 c[2] - 598 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  301 c[1] + 517 c[2] - 598 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  189 c[1] + 533 c[2] - 598 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  885 c[1] + 373 c[2] - 590 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  773 c[1] + 389 c[2] - 590 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  805 c[1] + 389 c[2] - 590 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  693 c[1] + 405 c[2] - 590 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  581 c[1] + 421 c[2] - 590 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  469 c[1] + 437 c[2] - 590 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  1165 c[1] + 277 c[2] - 582 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  1053 c[1] + 293 c[2] - 582 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  1085 c[1] + 293 c[2] - 582 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  973 c[1] + 309 c[2] - 582 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  861 c[1] + 325 c[2] - 582 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  1445 c[1] + 181 c[2] - 574 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  1365 c[1] + 197 c[2] - 574 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  1253 c[1] + 213 c[2] - 574 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  1725 c[1] + 85 c[2] - 566 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  1645 c[1] + 101 c[2] - 566 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  1533 c[1] + 117 c[2] - 566 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 &&
  1925 c[1] + 5 c[2] - 558 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0 && 2205 c[1] -
  91 c[2] - 550 c[3] + 186 c[4] - 23 c[5] + c[6] ≥ 0, Array[c, 6], Integers]]
{184, 1105, 6816, 0, 0, 3452532}

GCD[184, 1105, 6816, 0, 0, 3452532]
1

Reverse[cert]
{3452532, 0, 0, 6816, 1105, 184}

cert.g
-35011

cert.Transpose[A]
{3265, 337, 9089, 273, 6161, 3233, 305, 6097, 3169, 9057, 6129, 3201, 273, 6065,
  3137, 9025, 6097, 3169, 6033, 8993, 6065, 6001, 8961, 6033, 8929, 8897}

```

$$\text{chi} = (-7 + x)^3 (-5 + x)^8 (5 + x)^{15} (-44 + 53x - 14x^2 + x^3)$$

$$(-7 + x)^3 (-5 + x)^8 (5 + x)^{15} (-44 + 53x - 14x^2 + x^3)$$

```

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{735, 133, -426, 154, -21, 1},
 {695, 181, -434, 154, -21, 1}, {55, 389, -450, 154, -21, 1},
 {-25, 405, -450, 154, -21, 1}, {335, 293, -442, 154, -21, 1},
 {255, 309, -442, 154, -21, 1}, {175, 325, -442, 154, -21, 1},
 {615, 197, -434, 154, -21, 1}, {535, 213, -434, 154, -21, 1},
 {455, 229, -434, 154, -21, 1}, {975, 85, -426, 154, -21, 1},
 {895, 101, -426, 154, -21, 1}, {815, 117, -426, 154, -21, 1},
 {1175, 5, -418, 154, -21, 1}, {1095, 21, -418, 154, -21, 1},
 {1015, 37, -418, 154, -21, 1}, {1295, -59, -410, 154, -21, 1}}

```

A = {{55, 389, -450, 154, -21, 1},
 {-25, 405, -450, 154, -21, 1}, {335, 293, -442, 154, -21, 1},
 {255, 309, -442, 154, -21, 1}, {175, 325, -442, 154, -21, 1},
 {695, 181, -434, 154, -21, 1}, {615, 197, -434, 154, -21, 1},
 {535, 213, -434, 154, -21, 1}, {455, 229, -434, 154, -21, 1},
 {975, 85, -426, 154, -21, 1}, {895, 101, -426, 154, -21, 1},
 {815, 117, -426, 154, -21, 1}, {735, 133, -426, 154, -21, 1},
 {1175, 5, -418, 154, -21, 1}, {1095, 21, -418, 154, -21, 1},
 {1015, 37, -418, 154, -21, 1}, {1295, -59, -410, 154, -21, 1}};

A // MatrixForm

55	389	-450	154	-21	1
-25	405	-450	154	-21	1
335	293	-442	154	-21	1
255	309	-442	154	-21	1
175	325	-442	154	-21	1
695	181	-434	154	-21	1
615	197	-434	154	-21	1
535	213	-434	154	-21	1
455	229	-434	154	-21	1
975	85	-426	154	-21	1
895	101	-426	154	-21	1
815	117	-426	154	-21	1
735	133	-426	154	-21	1
1175	5	-418	154	-21	1
1095	21	-418	154	-21	1
1015	37	-418	154	-21	1
1295	-59	-410	154	-21	1

```

g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{1795, 11409, -13058, 4466, -609, 29}

Array[c, 6].Transpose[A]
{55 c[1] + 389 c[2] - 450 c[3] + 154 c[4] - 21 c[5] + c[6],
 -25 c[1] + 405 c[2] - 450 c[3] + 154 c[4] - 21 c[5] + c[6],
 335 c[1] + 293 c[2] - 442 c[3] + 154 c[4] - 21 c[5] + c[6],
 255 c[1] + 309 c[2] - 442 c[3] + 154 c[4] - 21 c[5] + c[6],
 175 c[1] + 325 c[2] - 442 c[3] + 154 c[4] - 21 c[5] + c[6],
 695 c[1] + 181 c[2] - 434 c[3] + 154 c[4] - 21 c[5] + c[6],
 615 c[1] + 197 c[2] - 434 c[3] + 154 c[4] - 21 c[5] + c[6],
 535 c[1] + 213 c[2] - 434 c[3] + 154 c[4] - 21 c[5] + c[6],
 455 c[1] + 229 c[2] - 434 c[3] + 154 c[4] - 21 c[5] + c[6],
 975 c[1] + 85 c[2] - 426 c[3] + 154 c[4] - 21 c[5] + c[6],
 895 c[1] + 101 c[2] - 426 c[3] + 154 c[4] - 21 c[5] + c[6],
 815 c[1] + 117 c[2] - 426 c[3] + 154 c[4] - 21 c[5] + c[6],
 735 c[1] + 133 c[2] - 426 c[3] + 154 c[4] - 21 c[5] + c[6],
 1175 c[1] + 5 c[2] - 418 c[3] + 154 c[4] - 21 c[5] + c[6],
 1095 c[1] + 21 c[2] - 418 c[3] + 154 c[4] - 21 c[5] + c[6],
 1015 c[1] + 37 c[2] - 418 c[3] + 154 c[4] - 21 c[5] + c[6],
 1295 c[1] - 59 c[2] - 410 c[3] + 154 c[4] - 21 c[5] + c[6]}

Array[c, 6].g
1795 c[1] + 11409 c[2] - 13058 c[3] + 4466 c[4] - 609 c[5] + 29 c[6]

cert = Flatten[Array[c, 6] /. FindInstance[
 1795 c[1] + 11409 c[2] - 13058 c[3] + 4466 c[4] - 609 c[5] + 29 c[6] < 0 &&
 55 c[1] + 389 c[2] - 450 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
 -25 c[1] + 405 c[2] - 450 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
 335 c[1] + 293 c[2] - 442 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
 255 c[1] + 309 c[2] - 442 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
 175 c[1] + 325 c[2] - 442 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
 695 c[1] + 181 c[2] - 434 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
 615 c[1] + 197 c[2] - 434 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
 535 c[1] + 213 c[2] - 434 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
 455 c[1] + 229 c[2] - 434 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
 975 c[1] + 85 c[2] - 426 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
 895 c[1] + 101 c[2] - 426 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
 815 c[1] + 117 c[2] - 426 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
 735 c[1] + 133 c[2] - 426 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
 1175 c[1] + 5 c[2] - 418 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
 1095 c[1] + 21 c[2] - 418 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
 1015 c[1] + 37 c[2] - 418 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0 &&
 1295 c[1] - 59 c[2] - 410 c[3] + 154 c[4] - 21 c[5] + c[6] ≥ 0, Array[c, 6], Integers]]
{-52, -173, -157, 0, 0, 0}

```

```

GCD[-52, -173, -157, 0, 0, 0]
1

Reverse[cert]
{0, 0, 0, -157, -173, -52}

cert.g
-16991

cert.Transpose[A]
{493, 1885, 1285, 2677, 4069, 685, 2077, 3469,
 4861, 1477, 2869, 4261, 5653, 3661, 5053, 6445, 7237}

chi = (-8 + x) (-5 + x)^8 (-3 + x) (5 + x)^15 (31 - 12 x + x^2)^2
(-8 + x) (-5 + x)^8 (-3 + x) (5 + x)^15 (31 - 12 x + x^2)^2

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{-279, 945, -674, 190, -23, 1},
 {-31, 849, -666, 190, -23, 1}, {217, 753, -658, 190, -23, 1},
 {105, 769, -658, 190, -23, 1}, {465, 657, -650, 190, -23, 1}};

A = {{-279, 945, -674, 190, -23, 1},
 {-31, 849, -666, 190, -23, 1}, {217, 753, -658, 190, -23, 1},
 {105, 769, -658, 190, -23, 1}, {465, 657, -650, 190, -23, 1}};

A // MatrixForm

$$\begin{pmatrix} -279 & 945 & -674 & 190 & -23 & 1 \\ -31 & 849 & -666 & 190 & -23 & 1 \\ 217 & 753 & -658 & 190 & -23 & 1 \\ 105 & 769 & -658 & 190 & -23 & 1 \\ 465 & 657 & -650 & 190 & -23 & 1 \end{pmatrix}$$


g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{-3115, 25277, -19354, 5510, -667, 29}

Array[c, 6].Transpose[A]
{-279 c[1] + 945 c[2] - 674 c[3] + 190 c[4] - 23 c[5] + c[6],
 -31 c[1] + 849 c[2] - 666 c[3] + 190 c[4] - 23 c[5] + c[6],
 217 c[1] + 753 c[2] - 658 c[3] + 190 c[4] - 23 c[5] + c[6],
 105 c[1] + 769 c[2] - 658 c[3] + 190 c[4] - 23 c[5] + c[6],
 465 c[1] + 657 c[2] - 650 c[3] + 190 c[4] - 23 c[5] + c[6]}

```

```

Array[c, 6].g
-3115 c[1] + 25 277 c[2] - 19 354 c[3] + 5510 c[4] - 667 c[5] + 29 c[6]

cert = Flatten[Array[c, 6] /. FindInstance[
  -3115 c[1] + 25 277 c[2] - 19 354 c[3] + 5510 c[4] - 667 c[5] + 29 c[6] < 0 &&
  -279 c[1] + 945 c[2] - 674 c[3] + 190 c[4] - 23 c[5] + c[6] ≥ 0 &&
  -31 c[1] + 849 c[2] - 666 c[3] + 190 c[4] - 23 c[5] + c[6] ≥ 0 &&
  217 c[1] + 753 c[2] - 658 c[3] + 190 c[4] - 23 c[5] + c[6] ≥ 0 &&
  105 c[1] + 769 c[2] - 658 c[3] + 190 c[4] - 23 c[5] + c[6] ≥ 0 && 465 c[1] +
  657 c[2] - 650 c[3] + 190 c[4] - 23 c[5] + c[6] ≥ 0, Array[c, 6], Integers]]
```

{-217, -1528, -11608, 0, 0, -6439670}

```

GCD[-217, -1528, -11608, 0, 0, -6439670]
1

Reverse[cert]
{-6439670, 0, 0, -11608, -1528, -217}

cert.g
-36499

cert.Transpose[A]
{705, 713, 721, 577, 729}

```

$$\text{chi} = (-5 + x)^{10} (5 + x)^{15} (928 - 779 x + 219 x^2 - 25 x^3 + x^4)$$

$$(-5 + x)^{10} (5 + x)^{15} (928 - 779 x + 219 x^2 - 25 x^3 + x^4)$$

```

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{-145, 1089, -822, 222, -25, 1},
 {295, 961, -814, 222, -25, 1}, {215, 977, -814, 222, -25, 1},
 {135, 993, -814, 222, -25, 1}, {655, 849, -806, 222, -25, 1},
 {575, 865, -806, 222, -25, 1}, {495, 881, -806, 222, -25, 1},
 {1015, 737, -798, 222, -25, 1}, {935, 753, -798, 222, -25, 1},
 {855, 769, -798, 222, -25, 1}, {775, 785, -798, 222, -25, 1},
 {1295, 641, -790, 222, -25, 1}, {1215, 657, -790, 222, -25, 1},
 {1135, 673, -790, 222, -25, 1}, {1495, 561, -782, 222, -25, 1}}

```

```

A = {{-145, 1089, -822, 222, -25, 1},
      {295, 961, -814, 222, -25, 1}, {215, 977, -814, 222, -25, 1},
      {135, 993, -814, 222, -25, 1}, {655, 849, -806, 222, -25, 1},
      {575, 865, -806, 222, -25, 1}, {495, 881, -806, 222, -25, 1},
      {1015, 737, -798, 222, -25, 1}, {935, 753, -798, 222, -25, 1},
      {855, 769, -798, 222, -25, 1}, {775, 785, -798, 222, -25, 1},
      {1295, 641, -790, 222, -25, 1}, {1215, 657, -790, 222, -25, 1},
      {1135, 673, -790, 222, -25, 1}, {1495, 561, -782, 222, -25, 1}};

A // MatrixForm


$$\begin{pmatrix} -145 & 1089 & -822 & 222 & -25 & 1 \\ 295 & 961 & -814 & 222 & -25 & 1 \\ 215 & 977 & -814 & 222 & -25 & 1 \\ 135 & 993 & -814 & 222 & -25 & 1 \\ 655 & 849 & -806 & 222 & -25 & 1 \\ 575 & 865 & -806 & 222 & -25 & 1 \\ 495 & 881 & -806 & 222 & -25 & 1 \\ 1015 & 737 & -798 & 222 & -25 & 1 \\ 935 & 753 & -798 & 222 & -25 & 1 \\ 855 & 769 & -798 & 222 & -25 & 1 \\ 775 & 785 & -798 & 222 & -25 & 1 \\ 1295 & 641 & -790 & 222 & -25 & 1 \\ 1215 & 657 & -790 & 222 & -25 & 1 \\ 1135 & 673 & -790 & 222 & -25 & 1 \\ 1495 & 561 & -782 & 222 & -25 & 1 \end{pmatrix}$$


g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{-3725, 31725, -23854, 6438, -725, 29}

Array[c, 6].Transpose[A]

{-145 c[1] + 1089 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6],
 295 c[1] + 961 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6],
 215 c[1] + 977 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6],
 135 c[1] + 993 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6],
 655 c[1] + 849 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6],
 575 c[1] + 865 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6],
 495 c[1] + 881 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6],
 1015 c[1] + 737 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6],
 935 c[1] + 753 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6],
 855 c[1] + 769 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6],
 775 c[1] + 785 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6],
 1295 c[1] + 641 c[2] - 790 c[3] + 222 c[4] - 25 c[5] + c[6],
 1215 c[1] + 657 c[2] - 790 c[3] + 222 c[4] - 25 c[5] + c[6],
 1135 c[1] + 673 c[2] - 790 c[3] + 222 c[4] - 25 c[5] + c[6],
 1495 c[1] + 561 c[2] - 782 c[3] + 222 c[4] - 25 c[5] + c[6]}

Array[c, 6].g

-3725 c[1] + 31725 c[2] - 23854 c[3] + 6438 c[4] - 725 c[5] + 29 c[6]

```

```

cert = Flatten[Array[c, 6] /. FindInstance[
  -3725 c[1] + 31725 c[2] - 23854 c[3] + 6438 c[4] - 725 c[5] + 29 c[6] < 0 &&
  -145 c[1] + 1089 c[2] - 822 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  295 c[1] + 961 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  215 c[1] + 977 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  135 c[1] + 993 c[2] - 814 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  655 c[1] + 849 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  575 c[1] + 865 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  495 c[1] + 881 c[2] - 806 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1015 c[1] + 737 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  935 c[1] + 753 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  855 c[1] + 769 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  775 c[1] + 785 c[2] - 798 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1295 c[1] + 641 c[2] - 790 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1215 c[1] + 657 c[2] - 790 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1135 c[1] + 673 c[2] - 790 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0 &&
  1495 c[1] + 561 c[2] - 782 c[3] + 222 c[4] - 25 c[5] + c[6] ≥ 0,
  Array[c, 6], Integers]]
{ -71, -265, -339, 0, 0, 0}

GCD[-71, -265, -339, 0, 0, 0]
1

Reverse[cert]
{0, 0, 0, -339, -265, -71}

cert.g
-56144

cert.Transpose[A]
{368, 336, 1776, 3216, 1744, 3184, 4624,
 3152, 4592, 6032, 7472, 6000, 7440, 8880, 10288}

```

$$\begin{aligned}
 \text{chi} = & (-7 + x) (-5 + x)^9 (-4 + x) (5 + x)^{15} (-169 + 107 x - 19 x^2 + x^3) \\
 & (-7 + x) (-5 + x)^9 (-4 + x) (5 + x)^{15} (-169 + 107 x - 19 x^2 + x^3)
 \end{aligned}$$

```

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{461, -5710, 5271, -1940, 347, -30, 1}, {525, -5710, 5271, -1940, 347, -30, 1},
{861, -5870, 5287, -1940, 347, -30, 1}, {-35, -5518, 5255, -1940, 347, -30, 1},
{845, -5774, 5271, -1940, 347, -30, 1}, {685, -5742, 5271, -1940, 347, -30, 1},
{1021, -5902, 5287, -1940, 347, -30, 1}, {-1675, -4630, 5103, -1932, 347, -30, 1},
{-1115, -4822, 5119, -1932, 347, -30, 1},
{-1275, -4790, 5119, -1932, 347, -30, 1},
{-715, -4982, 5135, -1932, 347, -30, 1}, {-875, -4950, 5135, -1932, 347, -30, 1},
{-155, -5174, 5151, -1932, 347, -30, 1}, {-379, -5142, 5151, -1932, 347, -30, 1},
{-315, -5142, 5151, -1932, 347, -30, 1}, {245, -5334, 5167, -1932, 347, -30, 1},
{21, -5302, 5167, -1932, 347, -30, 1}, {-2675, -4030, 4983, -1924, 347, -30, 1},
{-2115, -4222, 4999, -1924, 347, -30, 1},
{-2275, -4190, 4999, -1924, 347, -30, 1},
{-1555, -4414, 5015, -1924, 347, -30, 1},
{-1715, -4382, 5015, -1924, 347, -30, 1},
{-1155, -4574, 5031, -1924, 347, -30, 1},
{-1379, -4542, 5031, -1924, 347, -30, 1}, {-595, -4766, 5047, -1924, 347, -30, 1},
{-819, -4734, 5047, -1924, 347, -30, 1}, {-3515, -3462, 4863, -1916, 347, -30, 1},
{-2955, -3654, 4879, -1916, 347, -30, 1},
{-3115, -3622, 4879, -1916, 347, -30, 1},
{-2555, -3814, 4895, -1916, 347, -30, 1},
{-1995, -4006, 4911, -1916, 347, -30, 1},
{-1435, -4198, 4927, -1916, 347, -30, 1},
{-4915, -2702, 4727, -1908, 347, -30, 1},
{-4515, -2862, 4743, -1908, 347, -30, 1},
{-3955, -3054, 4759, -1908, 347, -30, 1},
{-3395, -3246, 4775, -1908, 347, -30, 1},
{-5355, -2294, 4623, -1900, 347, -30, 1},
{-6755, -1534, 4487, -1892, 347, -30, 1}}

```

```

A = {{-35, -5518, 5255, -1940, 347, -30, 1},
      {845, -5774, 5271, -1940, 347, -30, 1}, {685, -5742, 5271, -1940, 347, -30, 1},
      {461, -5710, 5271, -1940, 347, -30, 1}, {525, -5710, 5271, -1940, 347, -30, 1},
      {1021, -5902, 5287, -1940, 347, -30, 1}, {861, -5870, 5287, -1940, 347, -30, 1},
      {-1675, -4630, 5103, -1932, 347, -30, 1},
      {-1115, -4822, 5119, -1932, 347, -30, 1}, {-1275, -4790, 5119,
      -1932, 347, -30, 1}, {-715, -4982, 5135, -1932, 347, -30, 1},
      {-875, -4950, 5135, -1932, 347, -30, 1}, {-155, -5174, 5151,
      -1932, 347, -30, 1}, {-379, -5142, 5151, -1932, 347, -30, 1},
      {-315, -5142, 5151, -1932, 347, -30, 1}, {245, -5334, 5167, -1932, 347, -30, 1},
      {21, -5302, 5167, -1932, 347, -30, 1}, {-2675, -4030, 4983, -1924, 347, -30, 1},
      {-2115, -4222, 4999, -1924, 347, -30, 1},
      {-2275, -4190, 4999, -1924, 347, -30, 1},
      {-1555, -4414, 5015, -1924, 347, -30, 1}, {-1715, -4382, 5015,
      -1924, 347, -30, 1}, {-1155, -4574, 5031, -1924, 347, -30, 1},
      {-1379, -4542, 5031, -1924, 347, -30, 1}, {-595, -4766, 5047,
      -1924, 347, -30, 1}, {-819, -4734, 5047, -1924, 347, -30, 1},
      {-3515, -3462, 4863, -1916, 347, -30, 1}, {-2955, -3654, 4879,
      -1916, 347, -30, 1}, {-3115, -3622, 4879, -1916, 347, -30, 1},
      {-2555, -3814, 4895, -1916, 347, -30, 1}, {-1995, -4006, 4911,
      -1916, 347, -30, 1}, {-1435, -4198, 4927, -1916, 347, -30, 1},
      {-4915, -2702, 4727, -1908, 347, -30, 1}, {-4515, -2862, 4743,
      -1908, 347, -30, 1}, {-3955, -3054, 4759, -1908, 347, -30, 1},
      {-3395, -3246, 4775, -1908, 347, -30, 1}, {-5355, -2294, 4623,
      -1900, 347, -30, 1}, {-6755, -1534, 4487, -1892, 347, -30, 1}};

```

```
A // MatrixForm
```

$$\left(\begin{array}{ccccccc} -35 & -5518 & 5255 & -1940 & 347 & -30 & 1 \\ 845 & -5774 & 5271 & -1940 & 347 & -30 & 1 \\ 685 & -5742 & 5271 & -1940 & 347 & -30 & 1 \\ 461 & -5710 & 5271 & -1940 & 347 & -30 & 1 \\ 525 & -5710 & 5271 & -1940 & 347 & -30 & 1 \\ 1021 & -5902 & 5287 & -1940 & 347 & -30 & 1 \\ 861 & -5870 & 5287 & -1940 & 347 & -30 & 1 \\ -1675 & -4630 & 5103 & -1932 & 347 & -30 & 1 \\ -1115 & -4822 & 5119 & -1932 & 347 & -30 & 1 \\ -1275 & -4790 & 5119 & -1932 & 347 & -30 & 1 \\ -715 & -4982 & 5135 & -1932 & 347 & -30 & 1 \\ -875 & -4950 & 5135 & -1932 & 347 & -30 & 1 \\ -155 & -5174 & 5151 & -1932 & 347 & -30 & 1 \\ -379 & -5142 & 5151 & -1932 & 347 & -30 & 1 \\ -315 & -5142 & 5151 & -1932 & 347 & -30 & 1 \\ 245 & -5334 & 5167 & -1932 & 347 & -30 & 1 \\ 21 & -5302 & 5167 & -1932 & 347 & -30 & 1 \\ -2675 & -4030 & 4983 & -1924 & 347 & -30 & 1 \\ -2115 & -4222 & 4999 & -1924 & 347 & -30 & 1 \\ -2275 & -4190 & 4999 & -1924 & 347 & -30 & 1 \\ -1555 & -4414 & 5015 & -1924 & 347 & -30 & 1 \\ -1715 & -4382 & 5015 & -1924 & 347 & -30 & 1 \\ -1155 & -4574 & 5031 & -1924 & 347 & -30 & 1 \\ -1379 & -4542 & 5031 & -1924 & 347 & -30 & 1 \\ -595 & -4766 & 5047 & -1924 & 347 & -30 & 1 \\ -819 & -4734 & 5047 & -1924 & 347 & -30 & 1 \\ -3515 & -3462 & 4863 & -1916 & 347 & -30 & 1 \\ -2955 & -3654 & 4879 & -1916 & 347 & -30 & 1 \\ -3115 & -3622 & 4879 & -1916 & 347 & -30 & 1 \\ -2555 & -3814 & 4895 & -1916 & 347 & -30 & 1 \\ -1995 & -4006 & 4911 & -1916 & 347 & -30 & 1 \\ -1435 & -4198 & 4927 & -1916 & 347 & -30 & 1 \\ -4915 & -2702 & 4727 & -1908 & 347 & -30 & 1 \\ -4515 & -2862 & 4743 & -1908 & 347 & -30 & 1 \\ -3955 & -3054 & 4759 & -1908 & 347 & -30 & 1 \\ -3395 & -3246 & 4775 & -1908 & 347 & -30 & 1 \\ -5355 & -2294 & 4623 & -1900 & 347 & -30 & 1 \\ -6755 & -1534 & 4487 & -1892 & 347 & -30 & 1 \end{array} \right)$$

```
g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{20585, -165318, 151915, -56148, 10063, -870, 29}
```

Array[c, 7].Transpose[A]

```
{-35 c[1] - 5518 c[2] + 5255 c[3] - 1940 c[4] + 347 c[5] - 30 c[6] + c[7],  
845 c[1] - 5774 c[2] + 5271 c[3] - 1940 c[4] + 347 c[5] - 30 c[6] + c[7],  
685 c[1] - 5742 c[2] + 5271 c[3] - 1940 c[4] + 347 c[5] - 30 c[6] + c[7],  
461 c[1] - 5710 c[2] + 5271 c[3] - 1940 c[4] + 347 c[5] - 30 c[6] + c[7],  
525 c[1] - 5710 c[2] + 5271 c[3] - 1940 c[4] + 347 c[5] - 30 c[6] + c[7],  
1021 c[1] - 5902 c[2] + 5287 c[3] - 1940 c[4] + 347 c[5] - 30 c[6] + c[7],  
861 c[1] - 5870 c[2] + 5287 c[3] - 1940 c[4] + 347 c[5] - 30 c[6] + c[7],  
-1675 c[1] - 4630 c[2] + 5103 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7],  
-1115 c[1] - 4822 c[2] + 5119 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7],  
-1275 c[1] - 4790 c[2] + 5119 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7],  
-715 c[1] - 4982 c[2] + 5135 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7],  
-875 c[1] - 4950 c[2] + 5135 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7],  
-155 c[1] - 5174 c[2] + 5151 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7],  
-379 c[1] - 5142 c[2] + 5151 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7],  
-315 c[1] - 5142 c[2] + 5151 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7],  
245 c[1] - 5334 c[2] + 5167 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7],  
21 c[1] - 5302 c[2] + 5167 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7],  
-2675 c[1] - 4030 c[2] + 4983 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  
-2115 c[1] - 4222 c[2] + 4999 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  
-2275 c[1] - 4190 c[2] + 4999 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  
-1555 c[1] - 4414 c[2] + 5015 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  
-1715 c[1] - 4382 c[2] + 5015 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  
-1155 c[1] - 4574 c[2] + 5031 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  
-1379 c[1] - 4542 c[2] + 5031 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  
-595 c[1] - 4766 c[2] + 5047 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  
-819 c[1] - 4734 c[2] + 5047 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  
-3515 c[1] - 3462 c[2] + 4863 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  
-2955 c[1] - 3654 c[2] + 4879 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  
-3115 c[1] - 3622 c[2] + 4879 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  
-2555 c[1] - 3814 c[2] + 4895 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  
-1995 c[1] - 4006 c[2] + 4911 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  
-1435 c[1] - 4198 c[2] + 4927 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  
-4915 c[1] - 2702 c[2] + 4727 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7],  
-4515 c[1] - 2862 c[2] + 4743 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7],  
-3955 c[1] - 3054 c[2] + 4759 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7],  
-3395 c[1] - 3246 c[2] + 4775 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7],  
-5355 c[1] - 2294 c[2] + 4623 c[3] - 1900 c[4] + 347 c[5] - 30 c[6] + c[7],  
-6755 c[1] - 1534 c[2] + 4487 c[3] - 1892 c[4] + 347 c[5] - 30 c[6] + c[7]}
```

Array[c, 7].g

```
20 585 c[1] - 165 318 c[2] + 151 915 c[3] - 56 148 c[4] + 10 063 c[5] - 870 c[6] + 29 c[7]
```

```

cert = Flatten[
  Array[c, 7] /. FindInstance[20585 c[1] - 165318 c[2] + 151915 c[3] - 56148 c[4] +
    10063 c[5] - 870 c[6] + 29 c[7] < 0 &&
    -35 c[1] - 5518 c[2] + 5255 c[3] - 1940 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    845 c[1] - 5774 c[2] + 5271 c[3] - 1940 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    685 c[1] - 5742 c[2] + 5271 c[3] - 1940 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    461 c[1] - 5710 c[2] + 5271 c[3] - 1940 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    525 c[1] - 5710 c[2] + 5271 c[3] - 1940 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    1021 c[1] - 5902 c[2] + 5287 c[3] - 1940 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    861 c[1] - 5870 c[2] + 5287 c[3] - 1940 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1675 c[1] - 4630 c[2] + 5103 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1115 c[1] - 4822 c[2] + 5119 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1275 c[1] - 4790 c[2] + 5119 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -715 c[1] - 4982 c[2] + 5135 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -875 c[1] - 4950 c[2] + 5135 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -155 c[1] - 5174 c[2] + 5151 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -379 c[1] - 5142 c[2] + 5151 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -315 c[1] - 5142 c[2] + 5151 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    245 c[1] - 5334 c[2] + 5167 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    21 c[1] - 5302 c[2] + 5167 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -2675 c[1] - 4030 c[2] + 4983 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -2115 c[1] - 4222 c[2] + 4999 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -2275 c[1] - 4190 c[2] + 4999 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1555 c[1] - 4414 c[2] + 5015 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1715 c[1] - 4382 c[2] + 5015 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1155 c[1] - 4574 c[2] + 5031 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1379 c[1] - 4542 c[2] + 5031 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -595 c[1] - 4766 c[2] + 5047 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -819 c[1] - 4734 c[2] + 5047 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -3515 c[1] - 3462 c[2] + 4863 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -2955 c[1] - 3654 c[2] + 4879 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -3115 c[1] - 3622 c[2] + 4879 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -2555 c[1] - 3814 c[2] + 4895 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1995 c[1] - 4006 c[2] + 4911 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1435 c[1] - 4198 c[2] + 4927 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -4915 c[1] - 2702 c[2] + 4727 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -4515 c[1] - 2862 c[2] + 4743 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -3955 c[1] - 3054 c[2] + 4759 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -3395 c[1] - 3246 c[2] + 4775 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -5355 c[1] - 2294 c[2] + 4623 c[3] - 1900 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -6755 c[1] - 1534 c[2] + 4487 c[3] - 1892 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0,
  Array[c, 7], Integers]]
{0, 676, 3743, 8141, 0, 0, 0}
GCD[0, 676, 3743, 8141, 0, 0, 0]
1

```

```

Reverse[cert]
{0, 0, 0, 8141, 3743, 676, 0}

cert.g
-237991

cert.Transpose[A]
{145 757, 32 589, 54 221, 75 853, 75 853, 5949, 27 581, 242 237, 172 333, 193 965,
 124 061, 145 693, 54 157, 75 789, 75 789, 5885, 27 517, 263 805, 193 901, 215 533,
 123 997, 145 629, 75 725, 97 357, 5821, 27 453, 263 741, 193 837, 215 469,
 145 565, 75 661, 5757, 333 581, 285 309, 215 405, 145 501, 285 245, 355 085}

chi = (-9 + x) (-7 + x)^2 (-5 + x)^8 (-3 + x) (5 + x)^15 (16 - 9 x + x^2)
(-9 + x) (-7 + x)^2 (-5 + x)^8 (-3 + x) (5 + x)^15 (16 - 9 x + x^2)

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{{-4305, -764, 3235, -1512, 301, -28, 1}, {567, -3924, 3867, -1552, 301, -28, 1},
  {903, -4084, 3883, -1552, 301, -28, 1}, {-945, -3036, 3715, -1544, 301, -28, 1},
  {-449, -3228, 3731, -1544, 301, -28, 1}, {-385, -3228, 3731, -1544, 301, -28, 1},
  {-609, -3196, 3731, -1544, 301, -28, 1}, {-273, -3356, 3747, -1544, 301, -28, 1},
  {63, -3516, 3763, -1544, 301, -28, 1}, {-1625, -2500, 3595, -1536, 301, -28, 1},
  {-1785, -2468, 3595, -1536, 301, -28, 1},
  {-1225, -2660, 3611, -1536, 301, -28, 1},
  {-1449, -2628, 3611, -1536, 301, -28, 1},
  {-889, -2820, 3627, -1536, 301, -28, 1}, {-1113, -2788, 3627, -1536, 301, -28, 1},
  {-2465, -1932, 3475, -1528, 301, -28, 1},
  {-2625, -1900, 3475, -1528, 301, -28, 1},
  {-2065, -2092, 3491, -1528, 301, -28, 1},
  {-2289, -2060, 3491, -1528, 301, -28, 1},
  {-1729, -2252, 3507, -1528, 301, -28, 1},
  {-1953, -2220, 3507, -1528, 301, -28, 1},
  {-3465, -1332, 3355, -1520, 301, -28, 1},
  {-2905, -1524, 3371, -1520, 301, -28, 1},
  {-3129, -1492, 3371, -1520, 301, -28, 1}, {-3745, -956, 3251, -1512, 301, -28, 1}}

```

```

A = {{567, -3924, 3867, -1552, 301, -28, 1},
{903, -4084, 3883, -1552, 301, -28, 1}, {-945, -3036, 3715, -1544, 301, -28, 1},
{-449, -3228, 3731, -1544, 301, -28, 1}, {-385, -3228, 3731,
-1544, 301, -28, 1}, {-609, -3196, 3731, -1544, 301, -28, 1},
{-273, -3356, 3747, -1544, 301, -28, 1}, {63, -3516, 3763, -1544, 301, -28, 1},
{-1625, -2500, 3595, -1536, 301, -28, 1},
{-1785, -2468, 3595, -1536, 301, -28, 1},
{-1225, -2660, 3611, -1536, 301, -28, 1}, {-1449, -2628, 3611,
-1536, 301, -28, 1}, {-889, -2820, 3627, -1536, 301, -28, 1},
{-1113, -2788, 3627, -1536, 301, -28, 1}, {-2465, -1932, 3475,
-1528, 301, -28, 1}, {-2625, -1900, 3475, -1528, 301, -28, 1},
{-2065, -2092, 3491, -1528, 301, -28, 1}, {-2289, -2060, 3491,
-1528, 301, -28, 1}, {-1729, -2252, 3507, -1528, 301, -28, 1},
{-1953, -2220, 3507, -1528, 301, -28, 1}, {-3465, -1332, 3355,
-1520, 301, -28, 1}, {-2905, -1524, 3371, -1520, 301, -28, 1},
{-3129, -1492, 3371, -1520, 301, -28, 1}, {-4305, -764, 3235,
-1512, 301, -28, 1}, {-3745, -956, 3251, -1512, 301, -28, 1}};

A // MatrixForm


$$\begin{pmatrix} 567 & -3924 & 3867 & -1552 & 301 & -28 & 1 \\ 903 & -4084 & 3883 & -1552 & 301 & -28 & 1 \\ -945 & -3036 & 3715 & -1544 & 301 & -28 & 1 \\ -449 & -3228 & 3731 & -1544 & 301 & -28 & 1 \\ -385 & -3228 & 3731 & -1544 & 301 & -28 & 1 \\ -609 & -3196 & 3731 & -1544 & 301 & -28 & 1 \\ -273 & -3356 & 3747 & -1544 & 301 & -28 & 1 \\ 63 & -3516 & 3763 & -1544 & 301 & -28 & 1 \\ -1625 & -2500 & 3595 & -1536 & 301 & -28 & 1 \\ -1785 & -2468 & 3595 & -1536 & 301 & -28 & 1 \\ -1225 & -2660 & 3611 & -1536 & 301 & -28 & 1 \\ -1449 & -2628 & 3611 & -1536 & 301 & -28 & 1 \\ -889 & -2820 & 3627 & -1536 & 301 & -28 & 1 \\ -1113 & -2788 & 3627 & -1536 & 301 & -28 & 1 \\ -2465 & -1932 & 3475 & -1528 & 301 & -28 & 1 \\ -2625 & -1900 & 3475 & -1528 & 301 & -28 & 1 \\ -2065 & -2092 & 3491 & -1528 & 301 & -28 & 1 \\ -2289 & -2060 & 3491 & -1528 & 301 & -28 & 1 \\ -1729 & -2252 & 3507 & -1528 & 301 & -28 & 1 \\ -1953 & -2220 & 3507 & -1528 & 301 & -28 & 1 \\ -3465 & -1332 & 3355 & -1520 & 301 & -28 & 1 \\ -2905 & -1524 & 3371 & -1520 & 301 & -28 & 1 \\ -3129 & -1492 & 3371 & -1520 & 301 & -28 & 1 \\ -4305 & -764 & 3235 & -1512 & 301 & -28 & 1 \\ -3745 & -956 & 3251 & -1512 & 301 & -28 & 1 \end{pmatrix}$$


g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{8115, -105772, 109975, -44840, 8729, -812, 29}

```

Array[c, 7].Transpose[A]

```
{567 c[1] - 3924 c[2] + 3867 c[3] - 1552 c[4] + 301 c[5] - 28 c[6] + c[7],  
903 c[1] - 4084 c[2] + 3883 c[3] - 1552 c[4] + 301 c[5] - 28 c[6] + c[7],  
-945 c[1] - 3036 c[2] + 3715 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7],  
-449 c[1] - 3228 c[2] + 3731 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7],  
-385 c[1] - 3228 c[2] + 3731 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7],  
-609 c[1] - 3196 c[2] + 3731 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7],  
-273 c[1] - 3356 c[2] + 3747 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7],  
63 c[1] - 3516 c[2] + 3763 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7],  
-1625 c[1] - 2500 c[2] + 3595 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7],  
-1785 c[1] - 2468 c[2] + 3595 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7],  
-1225 c[1] - 2660 c[2] + 3611 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7],  
-1449 c[1] - 2628 c[2] + 3611 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7],  
-889 c[1] - 2820 c[2] + 3627 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7],  
-1113 c[1] - 2788 c[2] + 3627 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7],  
-2465 c[1] - 1932 c[2] + 3475 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7],  
-2625 c[1] - 1900 c[2] + 3475 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7],  
-2065 c[1] - 2092 c[2] + 3491 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7],  
-2289 c[1] - 2060 c[2] + 3491 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7],  
-1729 c[1] - 2252 c[2] + 3507 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7],  
-1953 c[1] - 2220 c[2] + 3507 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7],  
-3465 c[1] - 1332 c[2] + 3355 c[3] - 1520 c[4] + 301 c[5] - 28 c[6] + c[7],  
-2905 c[1] - 1524 c[2] + 3371 c[3] - 1520 c[4] + 301 c[5] - 28 c[6] + c[7],  
-3129 c[1] - 1492 c[2] + 3371 c[3] - 1520 c[4] + 301 c[5] - 28 c[6] + c[7],  
-4305 c[1] - 764 c[2] + 3235 c[3] - 1512 c[4] + 301 c[5] - 28 c[6] + c[7],  
-3745 c[1] - 956 c[2] + 3251 c[3] - 1512 c[4] + 301 c[5] - 28 c[6] + c[7]}
```

Array[c, 7].g

```
8115 c[1] - 105 772 c[2] + 109 975 c[3] - 44 840 c[4] + 8729 c[5] - 812 c[6] + 29 c[7]
```

```

cert = Flatten[Array[c, 7] /. FindInstance[
  8115 c[1] - 105 772 c[2] + 109 975 c[3] - 44 840 c[4] + 8729 c[5] - 812 c[6] + 29 c[7] <
  0 && 567 c[1] - 3924 c[2] + 3867 c[3] - 1552 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  903 c[1] - 4084 c[2] + 3883 c[3] - 1552 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -945 c[1] - 3036 c[2] + 3715 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -449 c[1] - 3228 c[2] + 3731 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -385 c[1] - 3228 c[2] + 3731 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -609 c[1] - 3196 c[2] + 3731 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -273 c[1] - 3356 c[2] + 3747 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  63 c[1] - 3516 c[2] + 3763 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -1625 c[1] - 2500 c[2] + 3595 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -1785 c[1] - 2468 c[2] + 3595 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -1225 c[1] - 2660 c[2] + 3611 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -1449 c[1] - 2628 c[2] + 3611 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -889 c[1] - 2820 c[2] + 3627 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -1113 c[1] - 2788 c[2] + 3627 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -2465 c[1] - 1932 c[2] + 3475 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -2625 c[1] - 1900 c[2] + 3475 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -2065 c[1] - 2092 c[2] + 3491 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -2289 c[1] - 2060 c[2] + 3491 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -1729 c[1] - 2252 c[2] + 3507 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -1953 c[1] - 2220 c[2] + 3507 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -3465 c[1] - 1332 c[2] + 3355 c[3] - 1520 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -2905 c[1] - 1524 c[2] + 3371 c[3] - 1520 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -3129 c[1] - 1492 c[2] + 3371 c[3] - 1520 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -4305 c[1] - 764 c[2] + 3235 c[3] - 1512 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -3745 c[1] - 956 c[2] + 3251 c[3] - 1512 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0,
  Array[c, 7], Integers]]
{-1018, 0, 8413, 20451, 0, 0, 0}
GCD[-1018, 0, 8413, 20451, 0, 0, 0]
1
Reverse[cert]
{0, 0, 0, 20451, 8413, 0, -1018}
cert.g
-64 235
cert.Transpose[A]
{215 913, 8473, 639 961, 269 641, 204 489, 432 521, 225 081, 17 641,
 486 249, 649 129, 213 657, 441 689, 6217, 234 249, 495 417, 658 297, 222 825,
 450 857, 15 385, 243 417, 667 465, 231 993, 460 025, 676 633, 241 161}

```

```

chi = (-7 + x)^2 (-5 + x)^6 (-4 + x) (-3 + x) (5 + x)^15 (31 - 12 x + x^2)^2
      (-7 + x)^2 (-5 + x)^6 (-4 + x) (-3 + x) (5 + x)^15 (31 - 12 x + x^2)^2

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{465, -3218, 3175, -1300, 263, -26, 1} }

A = {{465, -3218, 3175, -1300, 263, -26, 1}};

A // MatrixForm
( 465 -3218 3175 -1300 263 -26 1 )

g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{10205, -91114, 91483, -37636, 7627, -754, 29}

Array[c, 7].Transpose[A]
{465 c[1] - 3218 c[2] + 3175 c[3] - 1300 c[4] + 263 c[5] - 26 c[6] + c[7]}

Array[c, 7].g
10205 c[1] - 91114 c[2] + 91483 c[3] - 37636 c[4] + 7627 c[5] - 754 c[6] + 29 c[7]

cert = Flatten[
  Array[c, 7] /. FindInstance[10205 c[1] - 91114 c[2] + 91483 c[3] - 37636 c[4] +
    7627 c[5] - 754 c[6] + 29 c[7] < 0 && 465 c[1] - 3218 c[2] + 3175 c[3] -
    1300 c[4] + 263 c[5] - 26 c[6] + c[7] ≥ 0, Array[c, 7], Integers]]
{0, 0, 3, -3784, 0, 0, -4921960}

GCD[0, 0, 3, -3784, 0, 0, -4921960]
1

Reverse[cert]
{-4921960, 0, 0, -3784, 3, 0, 0}

cert.g
-47767

cert.Transpose[A]
{6765}

```

$$\begin{aligned} \text{chi} = & (-7 + x) (-5 + x)^9 (5 + x)^{15} (596 - 581x + 183x^2 - 23x^3 + x^4) \\ & (-7 + x) (-5 + x)^9 (5 + x)^{15} (596 - 581x + 183x^2 - 23x^3 + x^4) \end{aligned}$$

```

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{{-7595, -966, 4367, -1884, 347, -30, 1},
{301, -5118, 5079, -1924, 347, -30, 1}, {861, -5310, 5095, -1924, 347, -30, 1},
{1197, -5470, 5111, -1924, 347, -30, 1}, {-1995, -4006, 4911, -1916, 347, -30, 1},
{-1435, -4198, 4927, -1916, 347, -30, 1},
{-1659, -4166, 4927, -1916, 347, -30, 1}, {-875, -4390, 4943, -1916, 347, -30, 1},
{-1099, -4358, 4943, -1916, 347, -30, 1}, {-315, -4582, 4959, -1916, 347, -30, 1},
{-539, -4550, 4959, -1916, 347, -30, 1}, {245, -4774, 4975, -1916, 347, -30, 1},
{21, -4742, 4975, -1916, 347, -30, 1}, {-4515, -2862, 4743, -1908, 347, -30, 1},
{-3955, -3054, 4759, -1908, 347, -30, 1},
{-3395, -3246, 4775, -1908, 347, -30, 1},
{-2835, -3438, 4791, -1908, 347, -30, 1},
{-3059, -3406, 4791, -1908, 347, -30, 1},
{-2275, -3630, 4807, -1908, 347, -30, 1},
{-2499, -3598, 4807, -1908, 347, -30, 1},
{-1715, -3822, 4823, -1908, 347, -30, 1},
{-1939, -3790, 4823, -1908, 347, -30, 1},
{-5915, -2102, 4607, -1900, 347, -30, 1},
{-5355, -2294, 4623, -1900, 347, -30, 1},
{-4795, -2486, 4639, -1900, 347, -30, 1},
{-4235, -2678, 4655, -1900, 347, -30, 1},
{-4459, -2646, 4655, -1900, 347, -30, 1},
{-3675, -2870, 4671, -1900, 347, -30, 1},
{-7315, -1342, 4471, -1892, 347, -30, 1},
{-6755, -1534, 4487, -1892, 347, -30, 1},
{-6195, -1726, 4503, -1892, 347, -30, 1},
{-5635, -1918, 4519, -1892, 347, -30, 1},
{-8715, -582, 4335, -1884, 347, -30, 1}, {-8155, -774, 4351, -1884, 347, -30, 1},
{-10115, 178, 4199, -1876, 347, -30, 1}, {-9555, -14, 4215, -1876, 347, -30, 1}}}

```

```

A = {{301, -5118, 5079, -1924, 347, -30, 1},
{861, -5310, 5095, -1924, 347, -30, 1}, {1197, -5470, 5111, -1924, 347, -30, 1},
{-1995, -4006, 4911, -1916, 347, -30, 1}, {-1435, -4198, 4927,
-1916, 347, -30, 1}, {-1659, -4166, 4927, -1916, 347, -30, 1},
{-875, -4390, 4943, -1916, 347, -30, 1}, {-1099, -4358, 4943,
-1916, 347, -30, 1}, {-315, -4582, 4959, -1916, 347, -30, 1},
{-539, -4550, 4959, -1916, 347, -30, 1}, {245, -4774, 4975, -1916, 347, -30, 1},
{21, -4742, 4975, -1916, 347, -30, 1}, {-4515, -2862, 4743, -1908, 347, -30, 1},
{-3955, -3054, 4759, -1908, 347, -30, 1},
{-3395, -3246, 4775, -1908, 347, -30, 1},
{-2835, -3438, 4791, -1908, 347, -30, 1}, {-3059, -3406, 4791,
-1908, 347, -30, 1}, {-2275, -3630, 4807, -1908, 347, -30, 1},
{-2499, -3598, 4807, -1908, 347, -30, 1}, {-1715, -3822, 4823,
-1908, 347, -30, 1}, {-1939, -3790, 4823, -1908, 347, -30, 1},
{-5915, -2102, 4607, -1900, 347, -30, 1}, {-5355, -2294, 4623,
-1900, 347, -30, 1}, {-4795, -2486, 4639, -1900, 347, -30, 1},
{-4235, -2678, 4655, -1900, 347, -30, 1}, {-4459, -2646, 4655,
-1900, 347, -30, 1}, {-3675, -2870, 4671, -1900, 347, -30, 1},
{-7315, -1342, 4471, -1892, 347, -30, 1}, {-6755, -1534, 4487,
-1892, 347, -30, 1}, {-6195, -1726, 4503, -1892, 347, -30, 1},
{-5635, -1918, 4519, -1892, 347, -30, 1}, {-8715, -582, 4335,
-1884, 347, -30, 1}, {-8155, -774, 4351, -1884, 347, -30, 1},
{-7595, -966, 4367, -1884, 347, -30, 1}, {-10115, 178, 4199,
-1876, 347, -30, 1}, {-9555, -14, 4215, -1876, 347, -30, 1}};

```

```
A // MatrixForm
```

$$\left(\begin{array}{ccccccc} 301 & -5118 & 5079 & -1924 & 347 & -30 & 1 \\ 861 & -5310 & 5095 & -1924 & 347 & -30 & 1 \\ 1197 & -5470 & 5111 & -1924 & 347 & -30 & 1 \\ -1995 & -4006 & 4911 & -1916 & 347 & -30 & 1 \\ -1435 & -4198 & 4927 & -1916 & 347 & -30 & 1 \\ -1659 & -4166 & 4927 & -1916 & 347 & -30 & 1 \\ -875 & -4390 & 4943 & -1916 & 347 & -30 & 1 \\ -1099 & -4358 & 4943 & -1916 & 347 & -30 & 1 \\ -315 & -4582 & 4959 & -1916 & 347 & -30 & 1 \\ -539 & -4550 & 4959 & -1916 & 347 & -30 & 1 \\ 245 & -4774 & 4975 & -1916 & 347 & -30 & 1 \\ 21 & -4742 & 4975 & -1916 & 347 & -30 & 1 \\ -4515 & -2862 & 4743 & -1908 & 347 & -30 & 1 \\ -3955 & -3054 & 4759 & -1908 & 347 & -30 & 1 \\ -3395 & -3246 & 4775 & -1908 & 347 & -30 & 1 \\ -2835 & -3438 & 4791 & -1908 & 347 & -30 & 1 \\ -3059 & -3406 & 4791 & -1908 & 347 & -30 & 1 \\ -2275 & -3630 & 4807 & -1908 & 347 & -30 & 1 \\ -2499 & -3598 & 4807 & -1908 & 347 & -30 & 1 \\ -1715 & -3822 & 4823 & -1908 & 347 & -30 & 1 \\ -1939 & -3790 & 4823 & -1908 & 347 & -30 & 1 \\ -5915 & -2102 & 4607 & -1900 & 347 & -30 & 1 \\ -5355 & -2294 & 4623 & -1900 & 347 & -30 & 1 \\ -4795 & -2486 & 4639 & -1900 & 347 & -30 & 1 \\ -4235 & -2678 & 4655 & -1900 & 347 & -30 & 1 \\ -4459 & -2646 & 4655 & -1900 & 347 & -30 & 1 \\ -3675 & -2870 & 4671 & -1900 & 347 & -30 & 1 \\ -7315 & -1342 & 4471 & -1892 & 347 & -30 & 1 \\ -6755 & -1534 & 4487 & -1892 & 347 & -30 & 1 \\ -6195 & -1726 & 4503 & -1892 & 347 & -30 & 1 \\ -5635 & -1918 & 4519 & -1892 & 347 & -30 & 1 \\ -8715 & -582 & 4335 & -1884 & 347 & -30 & 1 \\ -8155 & -774 & 4351 & -1884 & 347 & -30 & 1 \\ -7595 & -966 & 4367 & -1884 & 347 & -30 & 1 \\ -10115 & 178 & 4199 & -1876 & 347 & -30 & 1 \\ -9555 & -14 & 4215 & -1876 & 347 & -30 & 1 \end{array} \right)$$

```
g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
```

```
{8585, -146918, 146635, -55732, 10063, -870, 29}
```

Array[c, 7].Transpose[A]

```
{301 c[1] - 5118 c[2] + 5079 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  

 861 c[1] - 5310 c[2] + 5095 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  

1197 c[1] - 5470 c[2] + 5111 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  

-1995 c[1] - 4006 c[2] + 4911 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  

-1435 c[1] - 4198 c[2] + 4927 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  

-1659 c[1] - 4166 c[2] + 4927 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  

-875 c[1] - 4390 c[2] + 4943 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  

-1099 c[1] - 4358 c[2] + 4943 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  

-315 c[1] - 4582 c[2] + 4959 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  

-539 c[1] - 4550 c[2] + 4959 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  

245 c[1] - 4774 c[2] + 4975 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  

21 c[1] - 4742 c[2] + 4975 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  

-4515 c[1] - 2862 c[2] + 4743 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7],  

-3955 c[1] - 3054 c[2] + 4759 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7],  

-3395 c[1] - 3246 c[2] + 4775 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7],  

-2835 c[1] - 3438 c[2] + 4791 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7],  

-3059 c[1] - 3406 c[2] + 4791 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7],  

-2275 c[1] - 3630 c[2] + 4807 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7],  

-2499 c[1] - 3598 c[2] + 4807 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7],  

-1715 c[1] - 3822 c[2] + 4823 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7],  

-1939 c[1] - 3790 c[2] + 4823 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7],  

-5915 c[1] - 2102 c[2] + 4607 c[3] - 1900 c[4] + 347 c[5] - 30 c[6] + c[7],  

-5355 c[1] - 2294 c[2] + 4623 c[3] - 1900 c[4] + 347 c[5] - 30 c[6] + c[7],  

-4795 c[1] - 2486 c[2] + 4639 c[3] - 1900 c[4] + 347 c[5] - 30 c[6] + c[7],  

-4235 c[1] - 2678 c[2] + 4655 c[3] - 1900 c[4] + 347 c[5] - 30 c[6] + c[7],  

-4459 c[1] - 2646 c[2] + 4655 c[3] - 1900 c[4] + 347 c[5] - 30 c[6] + c[7],  

-3675 c[1] - 2870 c[2] + 4671 c[3] - 1900 c[4] + 347 c[5] - 30 c[6] + c[7],  

-7315 c[1] - 1342 c[2] + 4471 c[3] - 1892 c[4] + 347 c[5] - 30 c[6] + c[7],  

-6755 c[1] - 1534 c[2] + 4487 c[3] - 1892 c[4] + 347 c[5] - 30 c[6] + c[7],  

-6195 c[1] - 1726 c[2] + 4503 c[3] - 1892 c[4] + 347 c[5] - 30 c[6] + c[7],  

-5635 c[1] - 1918 c[2] + 4519 c[3] - 1892 c[4] + 347 c[5] - 30 c[6] + c[7],  

-8715 c[1] - 582 c[2] + 4335 c[3] - 1884 c[4] + 347 c[5] - 30 c[6] + c[7],  

-8155 c[1] - 774 c[2] + 4351 c[3] - 1884 c[4] + 347 c[5] - 30 c[6] + c[7],  

-7595 c[1] - 966 c[2] + 4367 c[3] - 1884 c[4] + 347 c[5] - 30 c[6] + c[7],  

-10115 c[1] + 178 c[2] + 4199 c[3] - 1876 c[4] + 347 c[5] - 30 c[6] + c[7],  

-9555 c[1] - 14 c[2] + 4215 c[3] - 1876 c[4] + 347 c[5] - 30 c[6] + c[7]}
```

Array[c, 7].g

```
8585 c[1] - 146 918 c[2] + 146 635 c[3] - 55 732 c[4] + 10 063 c[5] - 870 c[6] + 29 c[7]
```

```

cert = Flatten[
  Array[c, 7] /. FindInstance[8585 c[1] - 146 918 c[2] + 146 635 c[3] - 55 732 c[4] +
    10 063 c[5] - 870 c[6] + 29 c[7] < 0 &&
    301 c[1] - 5118 c[2] + 5079 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    861 c[1] - 5310 c[2] + 5095 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    1197 c[1] - 5470 c[2] + 5111 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1995 c[1] - 4006 c[2] + 4911 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1435 c[1] - 4198 c[2] + 4927 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1659 c[1] - 4166 c[2] + 4927 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -875 c[1] - 4390 c[2] + 4943 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1099 c[1] - 4358 c[2] + 4943 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -315 c[1] - 4582 c[2] + 4959 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -539 c[1] - 4550 c[2] + 4959 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    245 c[1] - 4774 c[2] + 4975 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    21 c[1] - 4742 c[2] + 4975 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -4515 c[1] - 2862 c[2] + 4743 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -3955 c[1] - 3054 c[2] + 4759 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -3395 c[1] - 3246 c[2] + 4775 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -2835 c[1] - 3438 c[2] + 4791 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -3059 c[1] - 3406 c[2] + 4791 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -2275 c[1] - 3630 c[2] + 4807 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -2499 c[1] - 3598 c[2] + 4807 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1715 c[1] - 3822 c[2] + 4823 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1939 c[1] - 3790 c[2] + 4823 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -5915 c[1] - 2102 c[2] + 4607 c[3] - 1900 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -5355 c[1] - 2294 c[2] + 4623 c[3] - 1900 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -4795 c[1] - 2486 c[2] + 4639 c[3] - 1900 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -4235 c[1] - 2678 c[2] + 4655 c[3] - 1900 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -4459 c[1] - 2646 c[2] + 4655 c[3] - 1900 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -3675 c[1] - 2870 c[2] + 4671 c[3] - 1900 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -7315 c[1] - 1342 c[2] + 4471 c[3] - 1892 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -6755 c[1] - 1534 c[2] + 4487 c[3] - 1892 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -6195 c[1] - 1726 c[2] + 4503 c[3] - 1892 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -5635 c[1] - 1918 c[2] + 4519 c[3] - 1892 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -8715 c[1] - 582 c[2] + 4335 c[3] - 1884 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -8155 c[1] - 774 c[2] + 4351 c[3] - 1884 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -7595 c[1] - 966 c[2] + 4367 c[3] - 1884 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -10 115 c[1] + 178 c[2] + 4199 c[3] - 1876 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -9555 c[1] - 14 c[2] + 4215 c[3] - 1876 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0,
  Array[c, 7], Integers]]
{ -2015, -14 106, -98 738, -690 887, 0, 0, -899 357 723}

GCD[-2015, -14 106, -98 738, -690 887, 0, 0, -899 357 723]
1

```

```

Reverse[cert]
{-899 357 723, 0, 0, -690 887, -98 738, -14 106, -2015}

cert.g
-179 780

certTranspose[A]
{6556, 6700, 6812, 8012, 8156, 8124, 8300, 8268, 8444, 8412, 8588, 8556, 9436, 9580,
 9724, 9868, 9836, 10 012, 9980, 10 156, 10 124, 11 148, 11 292, 11 436, 11 580,
 11 548, 11 724, 12 860, 13 004, 13 148, 13 292, 14 572, 14 716, 14 860, 16 284, 16 428}

chi = (-7 + x) (-5 + x)9 (5 + x)15 (484 - 565 x + 183 x2 - 23 x3 + x4)
(-7 + x) (-5 + x)9 (5 + x)15 (484 - 565 x + 183 x2 - 23 x3 + x4)

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{-7595, -966, 4367, -1884, 347, -30, 1}, {-1155, -4014, 4839, -1908, 347, -30, 1},
 {-371, -4238, 4855, -1908, 347, -30, 1}, {-2891, -3094, 4687, -1900, 347, -30, 1},
 {-3115, -3062, 4687, -1900, 347, -30, 1},
 {-2331, -3286, 4703, -1900, 347, -30, 1},
 {-5635, -1918, 4519, -1892, 347, -30, 1},
 {-4851, -2142, 4535, -1892, 347, -30, 1},
 {-5075, -2110, 4535, -1892, 347, -30, 1},
 {-8155, -774, 4351, -1884, 347, -30, 1}, {-10 675, 370, 4183, -1876, 347, -30, 1},
 {-10 115, 178, 4199, -1876, 347, -30, 1}, {-9555, -14, 4215, -1876, 347, -30, 1},
 {-12 075, 1130, 4047, -1868, 347, -30, 1}, {-11 515, 938, 4063, -1868, 347, -30, 1}},

A = {{-1155, -4014, 4839, -1908, 347, -30, 1},
{-371, -4238, 4855, -1908, 347, -30, 1},
{-2891, -3094, 4687, -1900, 347, -30, 1}, {-3115, -3062, 4687, -1900,
347, -30, 1}, {-2331, -3286, 4703, -1900, 347, -30, 1}, {-5635, -1918, 4519, -1892, 347, -30, 1}, {-4851, -2142, 4535, -1892, 347, -30, 1}, {-5075, -2110, 4535, -1892, 347, -30, 1}, {-8155, -774, 4351, -1884, 347, -30, 1}, {-7595, -966, 4367, -1884, 347, -30, 1}, {-10 675, 370, 4183, -1876, 347, -30, 1}, {-10 115, 178, 4199, -1876, 347, -30, 1}, {-9555, -14, 4215, -1876, 347, -30, 1}, {-12 075, 1130, 4047, -1868, 347, -30, 1}, {-11 515, 938, 4063, -1868, 347, -30, 1}};
```

A // MatrixForm

$$\left(\begin{array}{ccccccc} -1155 & -4014 & 4839 & -1908 & 347 & -30 & 1 \\ -371 & -4238 & 4855 & -1908 & 347 & -30 & 1 \\ -2891 & -3094 & 4687 & -1900 & 347 & -30 & 1 \\ -3115 & -3062 & 4687 & -1900 & 347 & -30 & 1 \\ -2331 & -3286 & 4703 & -1900 & 347 & -30 & 1 \\ -5635 & -1918 & 4519 & -1892 & 347 & -30 & 1 \\ -4851 & -2142 & 4535 & -1892 & 347 & -30 & 1 \\ -5075 & -2110 & 4535 & -1892 & 347 & -30 & 1 \\ -8155 & -774 & 4351 & -1884 & 347 & -30 & 1 \\ -7595 & -966 & 4367 & -1884 & 347 & -30 & 1 \\ -10675 & 370 & 4183 & -1876 & 347 & -30 & 1 \\ -10115 & 178 & 4199 & -1876 & 347 & -30 & 1 \\ -9555 & -14 & 4215 & -1876 & 347 & -30 & 1 \\ -12075 & 1130 & 4047 & -1868 & 347 & -30 & 1 \\ -11515 & 938 & 4063 & -1868 & 347 & -30 & 1 \end{array} \right)$$

g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]

{-9335, -122182, 140555, -55316, 10063, -870, 29}

Array[c, 7].Transpose[A]

{-1155 c[1] - 4014 c[2] + 4839 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7],
 -371 c[1] - 4238 c[2] + 4855 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7],
 -2891 c[1] - 3094 c[2] + 4687 c[3] - 1900 c[4] + 347 c[5] - 30 c[6] + c[7],
 -3115 c[1] - 3062 c[2] + 4687 c[3] - 1900 c[4] + 347 c[5] - 30 c[6] + c[7],
 -2331 c[1] - 3286 c[2] + 4703 c[3] - 1900 c[4] + 347 c[5] - 30 c[6] + c[7],
 -5635 c[1] - 1918 c[2] + 4519 c[3] - 1892 c[4] + 347 c[5] - 30 c[6] + c[7],
 -4851 c[1] - 2142 c[2] + 4535 c[3] - 1892 c[4] + 347 c[5] - 30 c[6] + c[7],
 -5075 c[1] - 2110 c[2] + 4535 c[3] - 1892 c[4] + 347 c[5] - 30 c[6] + c[7],
 -8155 c[1] - 774 c[2] + 4351 c[3] - 1884 c[4] + 347 c[5] - 30 c[6] + c[7],
 -7595 c[1] - 966 c[2] + 4367 c[3] - 1884 c[4] + 347 c[5] - 30 c[6] + c[7],
 -10675 c[1] + 370 c[2] + 4183 c[3] - 1876 c[4] + 347 c[5] - 30 c[6] + c[7],
 -10115 c[1] + 178 c[2] + 4199 c[3] - 1876 c[4] + 347 c[5] - 30 c[6] + c[7],
 -9555 c[1] - 14 c[2] + 4215 c[3] - 1876 c[4] + 347 c[5] - 30 c[6] + c[7],
 -12075 c[1] + 1130 c[2] + 4047 c[3] - 1868 c[4] + 347 c[5] - 30 c[6] + c[7],
 -11515 c[1] + 938 c[2] + 4063 c[3] - 1868 c[4] + 347 c[5] - 30 c[6] + c[7]}

Array[c, 7].g

-9335 c[1] - 122182 c[2] + 140555 c[3] - 55316 c[4] + 10063 c[5] - 870 c[6] + 29 c[7]

```

cert = Flatten[
  Array[c, 7] /. FindInstance[-9335 c[1] - 122 182 c[2] + 140 555 c[3] - 55 316 c[4] +
    10 063 c[5] - 870 c[6] + 29 c[7] < 0 &&
    -1155 c[1] - 4014 c[2] + 4839 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -371 c[1] - 4238 c[2] + 4855 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -2891 c[1] - 3094 c[2] + 4687 c[3] - 1900 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -3115 c[1] - 3062 c[2] + 4687 c[3] - 1900 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -2331 c[1] - 3286 c[2] + 4703 c[3] - 1900 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -5635 c[1] - 1918 c[2] + 4519 c[3] - 1892 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -4851 c[1] - 2142 c[2] + 4535 c[3] - 1892 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -5075 c[1] - 2110 c[2] + 4535 c[3] - 1892 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -8155 c[1] - 774 c[2] + 4351 c[3] - 1884 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -7595 c[1] - 966 c[2] + 4367 c[3] - 1884 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -10 675 c[1] + 370 c[2] + 4183 c[3] - 1876 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -10 115 c[1] + 178 c[2] + 4199 c[3] - 1876 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -9555 c[1] - 14 c[2] + 4215 c[3] - 1876 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -12 075 c[1] + 1130 c[2] + 4047 c[3] - 1868 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -11 515 c[1] + 938 c[2] + 4063 c[3] - 1868 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0,
  Array[c, 7], Integers]]
{-242, 0, -17, 0, 0, 0, 0}

GCD[-242, 0, -17, 0, 0, 0, 0]
1

Reverse[cert]
{0, 0, 0, 0, -17, 0, -242}

cert.g
-130 365

cert.Transpose[A]
{197 247, 7247, 619 943, 674 151, 484 151, 1 286 847, 1 096 847, 1 151 055,
 1 899 543, 1 763 751, 2 512 239, 2 376 447, 2 240 655, 2 853 351, 2 717 559}

```

$$\begin{aligned}
\text{chi} = & (-7 + x)^2 (-5 + x)^8 (5 + x)^{15} (388 - 431x + 151x^2 - 21x^3 + x^4) \\
& (-7 + x)^2 (-5 + x)^8 (5 + x)^{15} (388 - 431x + 151x^2 - 21x^3 + x^4)
\end{aligned}$$

```

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{{-5425, -380, 3203, -1512, 301, -28, 1}, {-6825, 380, 3067, -1504, 301, -28, 1},
  {-5825, -220, 3187, -1512, 301, -28, 1}, {1015, -3988, 3867, -1552, 301, -28, 1},
  {-785, -3068, 3715, -1544, 301, -28, 1}, {-65, -3292, 3731, -1544, 301, -28, 1},
  {-225, -3260, 3731, -1544, 301, -28, 1}, {-385, -3228, 3731, -1544, 301, -28, 1},
  {495, -3484, 3747, -1544, 301, -28, 1}, {335, -3452, 3747, -1544, 301, -28, 1},
  {175, -3420, 3747, -1544, 301, -28, 1}, {-2025, -2340, 3579, -1536, 301, -28, 1},
  {-2185, -2308, 3579, -1536, 301, -28, 1},
  {-1465, -2532, 3595, -1536, 301, -28, 1},
  {-1625, -2500, 3595, -1536, 301, -28, 1},
  {-1785, -2468, 3595, -1536, 301, -28, 1},
  {-1065, -2692, 3611, -1536, 301, -28, 1},
  {-1225, -2660, 3611, -1536, 301, -28, 1},
  {-505, -2884, 3627, -1536, 301, -28, 1}, {-665, -2852, 3627, -1536, 301, -28, 1},
  {-105, -3044, 3643, -1536, 301, -28, 1}, {-3825, -1420, 3427, -1528, 301, -28, 1},
  {-3425, -1580, 3443, -1528, 301, -28, 1},
  {-2865, -1772, 3459, -1528, 301, -28, 1},
  {-3025, -1740, 3459, -1528, 301, -28, 1},
  {-3185, -1708, 3459, -1528, 301, -28, 1},
  {-2465, -1932, 3475, -1528, 301, -28, 1},
  {-2625, -1900, 3475, -1528, 301, -28, 1},
  {-1905, -2124, 3491, -1528, 301, -28, 1},
  {-2065, -2092, 3491, -1528, 301, -28, 1},
  {-1505, -2284, 3507, -1528, 301, -28, 1}, {-4825, -820, 3307, -1520, 301, -28, 1},
  {-4425, -980, 3323, -1520, 301, -28, 1}, {-3865, -1172, 3339, -1520, 301, -28, 1},
  {-4025, -1140, 3339, -1520, 301, -28, 1},
  {-3465, -1332, 3355, -1520, 301, -28, 1},
  {-2905, -1524, 3371, -1520, 301, -28, 1}, {-6225, -60, 3171, -1512, 301, -28, 1},
  {-5265, -412, 3203, -1512, 301, -28, 1}, {-4865, -572, 3219, -1512, 301, -28, 1},
  {-6265, 188, 3083, -1504, 301, -28, 1}, {-7665, 948, 2947, -1496, 301, -28, 1}}

```

```

A = {{1015, -3988, 3867, -1552, 301, -28, 1},
{-785, -3068, 3715, -1544, 301, -28, 1},
{-65, -3292, 3731, -1544, 301, -28, 1}, {-225, -3260, 3731, -1544, 301, -28, 1},
{-385, -3228, 3731, -1544, 301, -28, 1}, {495, -3484, 3747, -1544, 301, -28, 1},
{335, -3452, 3747, -1544, 301, -28, 1}, {175, -3420, 3747, -1544, 301, -28, 1},
{-2025, -2340, 3579, -1536, 301, -28, 1},
{-2185, -2308, 3579, -1536, 301, -28, 1},
{-1465, -2532, 3595, -1536, 301, -28, 1}, {-1625, -2500, 3595,
-1536, 301, -28, 1}, {-1785, -2468, 3595, -1536, 301, -28, 1},
{-1065, -2692, 3611, -1536, 301, -28, 1}, {-1225, -2660, 3611,
-1536, 301, -28, 1}, {-505, -2884, 3627, -1536, 301, -28, 1},
{-665, -2852, 3627, -1536, 301, -28, 1}, {-105, -3044, 3643,
-1536, 301, -28, 1}, {-3825, -1420, 3427, -1528, 301, -28, 1},
{-3425, -1580, 3443, -1528, 301, -28, 1}, {-2865, -1772, 3459,
-1528, 301, -28, 1}, {-3025, -1740, 3459, -1528, 301, -28, 1},
{-3185, -1708, 3459, -1528, 301, -28, 1}, {-2465, -1932, 3475,
-1528, 301, -28, 1}, {-2625, -1900, 3475, -1528, 301, -28, 1},
{-1905, -2124, 3491, -1528, 301, -28, 1}, {-2065, -2092, 3491,
-1528, 301, -28, 1}, {-1505, -2284, 3507, -1528, 301, -28, 1},
{-4825, -820, 3307, -1520, 301, -28, 1}, {-4425, -980, 3323,
-1520, 301, -28, 1}, {-3865, -1172, 3339, -1520, 301, -28, 1},
{-4025, -1140, 3339, -1520, 301, -28, 1}, {-3465, -1332, 3355,
-1520, 301, -28, 1}, {-2905, -1524, 3371, -1520, 301, -28, 1},
{-6225, -60, 3171, -1512, 301, -28, 1}, {-5825, -220, 3187, -1512, 301, -28, 1},
{-5265, -412, 3203, -1512, 301, -28, 1},
{-5425, -380, 3203, -1512, 301, -28, 1},
{-4865, -572, 3219, -1512, 301, -28, 1}, {-6825, 380, 3067, -1504, 301, -28, 1},
{-6265, 188, 3083, -1504, 301, -28, 1}, {-7665, 948, 2947, -1496, 301, -28, 1}};
```

```
A // MatrixForm
```

$$\left(\begin{array}{ccccccccc} 1015 & -3988 & 3867 & -1552 & 301 & -28 & 1 \\ -785 & -3068 & 3715 & -1544 & 301 & -28 & 1 \\ -65 & -3292 & 3731 & -1544 & 301 & -28 & 1 \\ -225 & -3260 & 3731 & -1544 & 301 & -28 & 1 \\ -385 & -3228 & 3731 & -1544 & 301 & -28 & 1 \\ 495 & -3484 & 3747 & -1544 & 301 & -28 & 1 \\ 335 & -3452 & 3747 & -1544 & 301 & -28 & 1 \\ 175 & -3420 & 3747 & -1544 & 301 & -28 & 1 \\ -2025 & -2340 & 3579 & -1536 & 301 & -28 & 1 \\ -2185 & -2308 & 3579 & -1536 & 301 & -28 & 1 \\ -1465 & -2532 & 3595 & -1536 & 301 & -28 & 1 \\ -1625 & -2500 & 3595 & -1536 & 301 & -28 & 1 \\ -1785 & -2468 & 3595 & -1536 & 301 & -28 & 1 \\ -1065 & -2692 & 3611 & -1536 & 301 & -28 & 1 \\ -1225 & -2660 & 3611 & -1536 & 301 & -28 & 1 \\ -505 & -2884 & 3627 & -1536 & 301 & -28 & 1 \\ -665 & -2852 & 3627 & -1536 & 301 & -28 & 1 \\ -105 & -3044 & 3643 & -1536 & 301 & -28 & 1 \\ -3825 & -1420 & 3427 & -1528 & 301 & -28 & 1 \\ -3425 & -1580 & 3443 & -1528 & 301 & -28 & 1 \\ -2865 & -1772 & 3459 & -1528 & 301 & -28 & 1 \\ -3025 & -1740 & 3459 & -1528 & 301 & -28 & 1 \\ -3185 & -1708 & 3459 & -1528 & 301 & -28 & 1 \\ -2465 & -1932 & 3475 & -1528 & 301 & -28 & 1 \\ -2625 & -1900 & 3475 & -1528 & 301 & -28 & 1 \\ -1905 & -2124 & 3491 & -1528 & 301 & -28 & 1 \\ -2065 & -2092 & 3491 & -1528 & 301 & -28 & 1 \\ -1505 & -2284 & 3507 & -1528 & 301 & -28 & 1 \\ -4825 & -820 & 3307 & -1520 & 301 & -28 & 1 \\ -4425 & -980 & 3323 & -1520 & 301 & -28 & 1 \\ -3865 & -1172 & 3339 & -1520 & 301 & -28 & 1 \\ -4025 & -1140 & 3339 & -1520 & 301 & -28 & 1 \\ -3465 & -1332 & 3355 & -1520 & 301 & -28 & 1 \\ -2905 & -1524 & 3371 & -1520 & 301 & -28 & 1 \\ -6225 & -60 & 3171 & -1512 & 301 & -28 & 1 \\ -5825 & -220 & 3187 & -1512 & 301 & -28 & 1 \\ -5265 & -412 & 3203 & -1512 & 301 & -28 & 1 \\ -5425 & -380 & 3203 & -1512 & 301 & -28 & 1 \\ -4865 & -572 & 3219 & -1512 & 301 & -28 & 1 \\ -6825 & 380 & 3067 & -1504 & 301 & -28 & 1 \\ -6265 & 188 & 3083 & -1504 & 301 & -28 & 1 \\ -7665 & 948 & 2947 & -1496 & 301 & -28 & 1 \end{array} \right)$$

```
g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{235, -96468, 108063, -44736, 8729, -812, 29}
```

Array[c, 7].Transpose[A]

```
{1015 c[1] - 3988 c[2] + 3867 c[3] - 1552 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 785 c[1] - 3068 c[2] + 3715 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 65 c[1] - 3292 c[2] + 3731 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 225 c[1] - 3260 c[2] + 3731 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 385 c[1] - 3228 c[2] + 3731 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7],  
495 c[1] - 3484 c[2] + 3747 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7],  
335 c[1] - 3452 c[2] + 3747 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7],  
175 c[1] - 3420 c[2] + 3747 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 2025 c[1] - 2340 c[2] + 3579 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 2185 c[1] - 2308 c[2] + 3579 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 1465 c[1] - 2532 c[2] + 3595 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 1625 c[1] - 2500 c[2] + 3595 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 1785 c[1] - 2468 c[2] + 3595 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 1065 c[1] - 2692 c[2] + 3611 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 1225 c[1] - 2660 c[2] + 3611 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 505 c[1] - 2884 c[2] + 3627 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 665 c[1] - 2852 c[2] + 3627 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 105 c[1] - 3044 c[2] + 3643 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 3825 c[1] - 1420 c[2] + 3427 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 3425 c[1] - 1580 c[2] + 3443 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 2865 c[1] - 1772 c[2] + 3459 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 3025 c[1] - 1740 c[2] + 3459 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 3185 c[1] - 1708 c[2] + 3459 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 2465 c[1] - 1932 c[2] + 3475 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 2625 c[1] - 1900 c[2] + 3475 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 1905 c[1] - 2124 c[2] + 3491 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 2065 c[1] - 2092 c[2] + 3491 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 1505 c[1] - 2284 c[2] + 3507 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 4825 c[1] - 820 c[2] + 3307 c[3] - 1520 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 4425 c[1] - 980 c[2] + 3323 c[3] - 1520 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 3865 c[1] - 1172 c[2] + 3339 c[3] - 1520 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 4025 c[1] - 1140 c[2] + 3339 c[3] - 1520 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 3465 c[1] - 1332 c[2] + 3355 c[3] - 1520 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 2905 c[1] - 1524 c[2] + 3371 c[3] - 1520 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 6225 c[1] - 60 c[2] + 3171 c[3] - 1512 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 5825 c[1] - 220 c[2] + 3187 c[3] - 1512 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 5265 c[1] - 412 c[2] + 3203 c[3] - 1512 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 5425 c[1] - 380 c[2] + 3203 c[3] - 1512 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 4865 c[1] - 572 c[2] + 3219 c[3] - 1512 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 6825 c[1] + 380 c[2] + 3067 c[3] - 1504 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 6265 c[1] + 188 c[2] + 3083 c[3] - 1504 c[4] + 301 c[5] - 28 c[6] + c[7],  
- 7665 c[1] + 948 c[2] + 2947 c[3] - 1496 c[4] + 301 c[5] - 28 c[6] + c[7]}
```

Array[c, 7].g

```
235 c[1] - 96 468 c[2] + 108 063 c[3] - 44 736 c[4] + 8729 c[5] - 812 c[6] + 29 c[7]
```

```

cert = Flatten[Array[c, 7] /. FindInstance[
  235 c[1] - 96468 c[2] + 108063 c[3] - 44736 c[4] + 8729 c[5] - 812 c[6] + 29 c[7] <
  0 && 1015 c[1] - 3988 c[2] + 3867 c[3] - 1552 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -785 c[1] - 3068 c[2] + 3715 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -65 c[1] - 3292 c[2] + 3731 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -225 c[1] - 3260 c[2] + 3731 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -385 c[1] - 3228 c[2] + 3731 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  495 c[1] - 3484 c[2] + 3747 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  335 c[1] - 3452 c[2] + 3747 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  175 c[1] - 3420 c[2] + 3747 c[3] - 1544 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -2025 c[1] - 2340 c[2] + 3579 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -2185 c[1] - 2308 c[2] + 3579 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -1465 c[1] - 2532 c[2] + 3595 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -1625 c[1] - 2500 c[2] + 3595 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -1785 c[1] - 2468 c[2] + 3595 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -1065 c[1] - 2692 c[2] + 3611 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -1225 c[1] - 2660 c[2] + 3611 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -505 c[1] - 2884 c[2] + 3627 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -665 c[1] - 2852 c[2] + 3627 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -105 c[1] - 3044 c[2] + 3643 c[3] - 1536 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -3825 c[1] - 1420 c[2] + 3427 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -3425 c[1] - 1580 c[2] + 3443 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -2865 c[1] - 1772 c[2] + 3459 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -3025 c[1] - 1740 c[2] + 3459 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -3185 c[1] - 1708 c[2] + 3459 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -2465 c[1] - 1932 c[2] + 3475 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -2625 c[1] - 1900 c[2] + 3475 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -1905 c[1] - 2124 c[2] + 3491 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -2065 c[1] - 2092 c[2] + 3491 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -1505 c[1] - 2284 c[2] + 3507 c[3] - 1528 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -4825 c[1] - 820 c[2] + 3307 c[3] - 1520 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -4425 c[1] - 980 c[2] + 3323 c[3] - 1520 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -3865 c[1] - 1172 c[2] + 3339 c[3] - 1520 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -4025 c[1] - 1140 c[2] + 3339 c[3] - 1520 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -3465 c[1] - 1332 c[2] + 3355 c[3] - 1520 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -2905 c[1] - 1524 c[2] + 3371 c[3] - 1520 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -6225 c[1] - 60 c[2] + 3171 c[3] - 1512 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -5825 c[1] - 220 c[2] + 3187 c[3] - 1512 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -5265 c[1] - 412 c[2] + 3203 c[3] - 1512 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -5425 c[1] - 380 c[2] + 3203 c[3] - 1512 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -4865 c[1] - 572 c[2] + 3219 c[3] - 1512 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -6825 c[1] + 380 c[2] + 3067 c[3] - 1504 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -6265 c[1] + 188 c[2] + 3083 c[3] - 1504 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0 &&
  -7665 c[1] + 948 c[2] + 2947 c[3] - 1496 c[4] + 301 c[5] - 28 c[6] + c[7] ≥ 0,
  Array[c, 7], Integers]]
{238, 978, 3367, 6028, 0, 0, 0}

```

```

GCD[238, 978, 3367, 6028, 0, 0, 0]
1

Reverse[cert]
{0, 0, 0, 6028, 3367, 978, 238}

cert.g
-110261

certTranspose[A]
{6039, 13839, 19999, 13215, 6431, 19375, 12591, 5807, 21015, 14231,
 20391, 13607, 6823, 12983, 6199, 12359, 5575, 4951, 28815, 21407,
 20783, 13999, 7215, 13375, 6591, 12751, 5967, 5343, 21799, 14391, 13767,
 6983, 6359, 5735, 22191, 14783, 14159, 7375, 6751, 7767, 7143, 7535}

```

$$\text{chi} = (-7 + x)^3 (-5 + x)^7 (5 + x)^{15} (256 - 313x + 123x^2 - 19x^3 + x^4) \\ (-7 + x)^3 (-5 + x)^7 (5 + x)^{15} (256 - 313x + 123x^2 - 19x^3 + x^4)$$

```

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{-3675, 70, 2263, -1196, 259, -26, 1},
 {-2235, -938, 2487, -1212, 259, -26, 1}, {-1995, -1066, 2503, -1212, 259, -26, 1},
 {245, -2394, 2759, -1228, 259, -26, 1}, {-995, -1666, 2623, -1220, 259, -26, 1},
 {-1155, -1634, 2623, -1220, 259, -26, 1}, {-275, -1890, 2639, -1220, 259, -26, 1},
 {-435, -1858, 2639, -1220, 259, -26, 1}, {-659, -1826, 2639, -1220, 259, -26, 1},
 {-595, -1826, 2639, -1220, 259, -26, 1}, {-35, -2018, 2655, -1220, 259, -26, 1},
 {-259, -1986, 2655, -1220, 259, -26, 1}, {-1675, -1130, 2503, -1212, 259, -26, 1},
 {-1835, -1098, 2503, -1212, 259, -26, 1},
 {-1275, -1290, 2519, -1212, 259, -26, 1},
 {-1435, -1258, 2519, -1212, 259, -26, 1}, {-715, -1482, 2535, -1212, 259, -26, 1},
 {-875, -1450, 2535, -1212, 259, -26, 1}, {-3075, -370, 2367, -1204, 259, -26, 1},
 {-2675, -530, 2383, -1204, 259, -26, 1}, {-2835, -498, 2383, -1204, 259, -26, 1},
 {-2275, -690, 2399, -1204, 259, -26, 1}, {-1715, -882, 2415, -1204, 259, -26, 1},
 {-4075, 230, 2247, -1196, 259, -26, 1}, {-3115, -122, 2279, -1196, 259, -26, 1}}

```

```

A = {{245, -2394, 2759, -1228, 259, -26, 1}, {-995, -1666, 2623, -1220, 259, -26, 1},
{-1155, -1634, 2623, -1220, 259, -26, 1},
{-275, -1890, 2639, -1220, 259, -26, 1}, {-435, -1858, 2639,
-1220, 259, -26, 1}, {-659, -1826, 2639, -1220, 259, -26, 1},
{-595, -1826, 2639, -1220, 259, -26, 1}, {-35, -2018, 2655, -1220, 259, -26, 1},
{-259, -1986, 2655, -1220, 259, -26, 1},
{-2235, -938, 2487, -1212, 259, -26, 1}, {-1675, -1130, 2503,
-1212, 259, -26, 1}, {-1835, -1098, 2503, -1212, 259, -26, 1},
{-1995, -1066, 2503, -1212, 259, -26, 1}, {-1275, -1290, 2519,
-1212, 259, -26, 1}, {-1435, -1258, 2519, -1212, 259, -26, 1},
{-715, -1482, 2535, -1212, 259, -26, 1}, {-875, -1450, 2535,
-1212, 259, -26, 1}, {-3075, -370, 2367, -1204, 259, -26, 1},
{-2675, -530, 2383, -1204, 259, -26, 1}, {-2835, -498, 2383,
-1204, 259, -26, 1}, {-2275, -690, 2399, -1204, 259, -26, 1},
{-1715, -882, 2415, -1204, 259, -26, 1}, {-4075, 230, 2247, -1196, 259, -26, 1},
{-3675, 70, 2263, -1196, 259, -26, 1}, {-3115, -122, 2279, -1196, 259, -26, 1}};

A // MatrixForm


$$\begin{pmatrix} 245 & -2394 & 2759 & -1228 & 259 & -26 & 1 \\ -995 & -1666 & 2623 & -1220 & 259 & -26 & 1 \\ -1155 & -1634 & 2623 & -1220 & 259 & -26 & 1 \\ -275 & -1890 & 2639 & -1220 & 259 & -26 & 1 \\ -435 & -1858 & 2639 & -1220 & 259 & -26 & 1 \\ -659 & -1826 & 2639 & -1220 & 259 & -26 & 1 \\ -595 & -1826 & 2639 & -1220 & 259 & -26 & 1 \\ -35 & -2018 & 2655 & -1220 & 259 & -26 & 1 \\ -259 & -1986 & 2655 & -1220 & 259 & -26 & 1 \\ -2235 & -938 & 2487 & -1212 & 259 & -26 & 1 \\ -1675 & -1130 & 2503 & -1212 & 259 & -26 & 1 \\ -1835 & -1098 & 2503 & -1212 & 259 & -26 & 1 \\ -1995 & -1066 & 2503 & -1212 & 259 & -26 & 1 \\ -1275 & -1290 & 2519 & -1212 & 259 & -26 & 1 \\ -1435 & -1258 & 2519 & -1212 & 259 & -26 & 1 \\ -715 & -1482 & 2535 & -1212 & 259 & -26 & 1 \\ -875 & -1450 & 2535 & -1212 & 259 & -26 & 1 \\ -3075 & -370 & 2367 & -1204 & 259 & -26 & 1 \\ -2675 & -530 & 2383 & -1204 & 259 & -26 & 1 \\ -2835 & -498 & 2383 & -1204 & 259 & -26 & 1 \\ -2275 & -690 & 2399 & -1204 & 259 & -26 & 1 \\ -1715 & -882 & 2415 & -1204 & 259 & -26 & 1 \\ -4075 & 230 & 2247 & -1196 & 259 & -26 & 1 \\ -3675 & 70 & 2263 & -1196 & 259 & -26 & 1 \\ -3115 & -122 & 2279 & -1196 & 259 & -26 & 1 \end{pmatrix}$$


g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{-2295, -62954, 78403, -35492, 7511, -754, 29}

```

Array[c, 7].Transpose[A]

```
{245 c[1] - 2394 c[2] + 2759 c[3] - 1228 c[4] + 259 c[5] - 26 c[6] + c[7],  

 - 995 c[1] - 1666 c[2] + 2623 c[3] - 1220 c[4] + 259 c[5] - 26 c[6] + c[7],  

 - 1155 c[1] - 1634 c[2] + 2623 c[3] - 1220 c[4] + 259 c[5] - 26 c[6] + c[7],  

 - 275 c[1] - 1890 c[2] + 2639 c[3] - 1220 c[4] + 259 c[5] - 26 c[6] + c[7],  

 - 435 c[1] - 1858 c[2] + 2639 c[3] - 1220 c[4] + 259 c[5] - 26 c[6] + c[7],  

 - 659 c[1] - 1826 c[2] + 2639 c[3] - 1220 c[4] + 259 c[5] - 26 c[6] + c[7],  

 - 595 c[1] - 1826 c[2] + 2639 c[3] - 1220 c[4] + 259 c[5] - 26 c[6] + c[7],  

 - 35 c[1] - 2018 c[2] + 2655 c[3] - 1220 c[4] + 259 c[5] - 26 c[6] + c[7],  

 - 259 c[1] - 1986 c[2] + 2655 c[3] - 1220 c[4] + 259 c[5] - 26 c[6] + c[7],  

 - 2235 c[1] - 938 c[2] + 2487 c[3] - 1212 c[4] + 259 c[5] - 26 c[6] + c[7],  

 - 1675 c[1] - 1130 c[2] + 2503 c[3] - 1212 c[4] + 259 c[5] - 26 c[6] + c[7],  

 - 1835 c[1] - 1098 c[2] + 2503 c[3] - 1212 c[4] + 259 c[5] - 26 c[6] + c[7],  

 - 1995 c[1] - 1066 c[2] + 2503 c[3] - 1212 c[4] + 259 c[5] - 26 c[6] + c[7],  

 - 1275 c[1] - 1290 c[2] + 2519 c[3] - 1212 c[4] + 259 c[5] - 26 c[6] + c[7],  

 - 1435 c[1] - 1258 c[2] + 2519 c[3] - 1212 c[4] + 259 c[5] - 26 c[6] + c[7],  

 - 715 c[1] - 1482 c[2] + 2535 c[3] - 1212 c[4] + 259 c[5] - 26 c[6] + c[7],  

 - 875 c[1] - 1450 c[2] + 2535 c[3] - 1212 c[4] + 259 c[5] - 26 c[6] + c[7],  

 - 3075 c[1] - 370 c[2] + 2367 c[3] - 1204 c[4] + 259 c[5] - 26 c[6] + c[7],  

 - 2675 c[1] - 530 c[2] + 2383 c[3] - 1204 c[4] + 259 c[5] - 26 c[6] + c[7],  

 - 2835 c[1] - 498 c[2] + 2383 c[3] - 1204 c[4] + 259 c[5] - 26 c[6] + c[7],  

 - 2275 c[1] - 690 c[2] + 2399 c[3] - 1204 c[4] + 259 c[5] - 26 c[6] + c[7],  

 - 1715 c[1] - 882 c[2] + 2415 c[3] - 1204 c[4] + 259 c[5] - 26 c[6] + c[7],  

 - 4075 c[1] + 230 c[2] + 2247 c[3] - 1196 c[4] + 259 c[5] - 26 c[6] + c[7],  

 - 3675 c[1] + 70 c[2] + 2263 c[3] - 1196 c[4] + 259 c[5] - 26 c[6] + c[7],  

 - 3115 c[1] - 122 c[2] + 2279 c[3] - 1196 c[4] + 259 c[5] - 26 c[6] + c[7]}
```

Array[c, 7].g

```
- 2295 c[1] - 62954 c[2] + 78403 c[3] - 35492 c[4] + 7511 c[5] - 754 c[6] + 29 c[7]
```

```

cert = Flatten[Array[c, 7] /. FindInstance[
  -2295 c[1] - 62 954 c[2] + 78 403 c[3] - 35 492 c[4] + 7511 c[5] - 754 c[6] + 29 c[7] <
  0 && 245 c[1] - 2394 c[2] + 2759 c[3] - 1228 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0 &&
  -995 c[1] - 1666 c[2] + 2623 c[3] - 1220 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0 &&
  -1155 c[1] - 1634 c[2] + 2623 c[3] - 1220 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0 &&
  -275 c[1] - 1890 c[2] + 2639 c[3] - 1220 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0 &&
  -435 c[1] - 1858 c[2] + 2639 c[3] - 1220 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0 &&
  -659 c[1] - 1826 c[2] + 2639 c[3] - 1220 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0 &&
  -595 c[1] - 1826 c[2] + 2639 c[3] - 1220 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0 &&
  -35 c[1] - 2018 c[2] + 2655 c[3] - 1220 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0 &&
  -259 c[1] - 1986 c[2] + 2655 c[3] - 1220 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0 &&
  -2235 c[1] - 938 c[2] + 2487 c[3] - 1212 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0 &&
  -1675 c[1] - 1130 c[2] + 2503 c[3] - 1212 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0 &&
  -1835 c[1] - 1098 c[2] + 2503 c[3] - 1212 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0 &&
  -1995 c[1] - 1066 c[2] + 2503 c[3] - 1212 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0 &&
  -1275 c[1] - 1290 c[2] + 2519 c[3] - 1212 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0 &&
  -1435 c[1] - 1258 c[2] + 2519 c[3] - 1212 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0 &&
  -715 c[1] - 1482 c[2] + 2535 c[3] - 1212 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0 &&
  -875 c[1] - 1450 c[2] + 2535 c[3] - 1212 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0 &&
  -3075 c[1] - 370 c[2] + 2367 c[3] - 1204 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0 &&
  -2675 c[1] - 530 c[2] + 2383 c[3] - 1204 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0 &&
  -2835 c[1] - 498 c[2] + 2383 c[3] - 1204 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0 &&
  -2275 c[1] - 690 c[2] + 2399 c[3] - 1204 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0 &&
  -1715 c[1] - 882 c[2] + 2415 c[3] - 1204 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0 &&
  -4075 c[1] + 230 c[2] + 2247 c[3] - 1196 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0 &&
  -3675 c[1] + 70 c[2] + 2263 c[3] - 1196 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0 &&
  -3115 c[1] - 122 c[2] + 2279 c[3] - 1196 c[4] + 259 c[5] - 26 c[6] + c[7] ≥ 0,
  Array[c, 7], Integers]]
{174, 616, 1795, 2863, 0, 0, 0}
GCD[174, 616, 1795, 2863, 0, 0, 0]
1
Reverse[cert]
{0, 0, 0, 2863, 1795, 616, 174}
cert.g
-59 205
cert.Transpose[A]
{4567, 16 039, 7911, 32 055, 23 927, 4663, 15 799, 23 687,
 4423, 27 511, 35 399, 27 271, 19 143, 35 159, 27 031, 43 047, 34 919,
 38 743, 38 503, 30 375, 38 263, 46 151, 41 847, 41 607, 49 495}

```

$$\begin{aligned} \text{chi} = & (-5 + x)^9 (5 + x)^{15} (-4672 + 4823 x - 1874 x^2 + 344 x^3 - 30 x^4 + x^5) \\ & (-5 + x)^9 (5 + x)^{15} (-4672 + 4823 x - 1874 x^2 + 344 x^3 - 30 x^4 + x^5) \end{aligned}$$

```
CoefficientList[feasibleinterlacingpolylist[chi], x]
```

```
{ {845, -5934, 5303, -1940, 347, -30, 1},  
  {1501, -6158, 5319, -1940, 347, -30, 1}, {-75, -5270, 5167, -1932, 347, -30, 1},  
  {-235, -5238, 5167, -1932, 347, -30, 1}, {-395, -5206, 5167, -1932, 347, -30, 1},  
  {421, -5462, 5183, -1932, 347, -30, 1}, {485, -5462, 5183, -1932, 347, -30, 1},  
  {261, -5430, 5183, -1932, 347, -30, 1}, {325, -5430, 5183, -1932, 347, -30, 1},  
  {101, -5398, 5183, -1932, 347, -30, 1}, {165, -5398, 5183, -1932, 347, -30, 1},  
  {661, -5590, 5199, -1932, 347, -30, 1}, {-1875, -4350, 5015, -1924, 347, -30, 1},  
  {-2035, -4318, 5015, -1924, 347, -30, 1},  
  {-1155, -4574, 5031, -1924, 347, -30, 1},  
  {-1315, -4542, 5031, -1924, 347, -30, 1},  
  {-1475, -4510, 5031, -1924, 347, -30, 1},  
  {-1635, -4478, 5031, -1924, 347, -30, 1},  
  {-595, -4766, 5047, -1924, 347, -30, 1}, {-755, -4734, 5047, -1924, 347, -30, 1},  
  {-915, -4702, 5047, -1924, 347, -30, 1}, {-1139, -4670, 5047, -1924, 347, -30, 1},  
  {-1075, -4670, 5047, -1924, 347, -30, 1},  
  {-355, -4894, 5063, -1924, 347, -30, 1}, {-579, -4862, 5063, -1924, 347, -30, 1},  
  {-515, -4862, 5063, -1924, 347, -30, 1}, {-3515, -3462, 4863, -1916, 347, -30, 1},  
  {-3115, -3622, 4879, -1916, 347, -30, 1},  
  {-3275, -3590, 4879, -1916, 347, -30, 1},  
  {-2555, -3814, 4895, -1916, 347, -30, 1},  
  {-2715, -3782, 4895, -1916, 347, -30, 1},  
  {-2875, -3750, 4895, -1916, 347, -30, 1},  
  {-2155, -3974, 4911, -1916, 347, -30, 1},  
  {-2315, -3942, 4911, -1916, 347, -30, 1},  
  {-1595, -4166, 4927, -1916, 347, -30, 1},  
  {-1755, -4134, 4927, -1916, 347, -30, 1},  
  {-1979, -4102, 4927, -1916, 347, -30, 1},  
  {-4515, -2862, 4743, -1908, 347, -30, 1},  
  {-3955, -3054, 4759, -1908, 347, -30, 1},  
  {-4115, -3022, 4759, -1908, 347, -30, 1},  
  {-3555, -3214, 4775, -1908, 347, -30, 1},  
  {-3715, -3182, 4775, -1908, 347, -30, 1},  
  {-2995, -3406, 4791, -1908, 347, -30, 1},  
  {-5515, -2262, 4623, -1900, 347, -30, 1},  
  {-4955, -2454, 4639, -1900, 347, -30, 1}}}
```

```
A = {{845, -5934, 5303, -1940, 347, -30, 1}, {1501, -6158, 5319, -1940, 347, -30, 1}, {-75, -5270, 5167, -1932, 347, -30, 1}, {-235, -5238, 5167, -1932, 347, -30, 1}, {-395, -5206, 5167, -1932, 347, -30, 1}, {421, -5462, 5183, -1932, 347, -30, 1}, {485, -5462, 5183, -1932, 347, -30, 1}, {261, -5430, 5183, -1932, 347, -30, 1}, {325, -5430, 5183, -1932, 347, -30, 1}, {101, -5398, 5183, -1932, 347, -30, 1}, {165, -5398, 5183, -1932, 347, -30, 1}, {661, -5590, 5199, -1932, 347, -30, 1}, {-1875, -4350, 5015, -1924, 347, -30, 1}, {-2035, -4318, 5015, -1924, 347, -30, 1}, {-1155, -4574, 5031, -1924, 347, -30, 1}, {-1315, -4542, 5031, -1924, 347, -30, 1}, {-1475, -4510, 5031, -1924, 347, -30, 1}, {-1635, -4478, 5031, -1924, 347, -30, 1}, {-595, -4766, 5047, -1924, 347, -30, 1}, {-755, -4734, 5047, -1924, 347, -30, 1}, {-915, -4702, 5047, -1924, 347, -30, 1}, {-1139, -4670, 5047, -1924, 347, -30, 1}, {-1075, -4670, 5047, -1924, 347, -30, 1}, {-355, -4894, 5063, -1924, 347, -30, 1}, {-579, -4862, 5063, -1924, 347, -30, 1}, {-515, -4862, 5063, -1924, 347, -30, 1}, {-3515, -3462, 4863, -1916, 347, -30, 1}, {-3115, -3622, 4879, -1916, 347, -30, 1}, {-3275, -3590, 4879, -1916, 347, -30, 1}, {-2715, -3782, 4895, -1916, 347, -30, 1}, {-2875, -3750, 4895, -1916, 347, -30, 1}, {-2155, -3974, 4911, -1916, 347, -30, 1}, {-2315, -3942, 4911, -1916, 347, -30, 1}, {-1595, -4166, 4927, -1916, 347, -30, 1}, {-1755, -4134, 4927, -1916, 347, -30, 1}, {-1979, -4102, 4927, -1916, 347, -30, 1}, {-4515, -2862, 4743, -1908, 347, -30, 1}, {-4115, -3022, 4759, -1908, 347, -30, 1}, {-3555, -3214, 4775, -1908, 347, -30, 1}, {-3715, -3182, 4775, -1908, 347, -30, 1}, {-2995, -3406, 4791, -1908, 347, -30, 1}, {-5515, -2262, 4623, -1900, 347, -30, 1}, {-1900, 347, -30, 1}, {-4955, -2454, 4639, -1900, 347, -30, 1}};
```

```
A // MatrixForm
```

$$\left(\begin{array}{ccccccc} 845 & -5934 & 5303 & -1940 & 347 & -30 & 1 \\ 1501 & -6158 & 5319 & -1940 & 347 & -30 & 1 \\ -75 & -5270 & 5167 & -1932 & 347 & -30 & 1 \\ -235 & -5238 & 5167 & -1932 & 347 & -30 & 1 \\ -395 & -5206 & 5167 & -1932 & 347 & -30 & 1 \\ 421 & -5462 & 5183 & -1932 & 347 & -30 & 1 \\ 485 & -5462 & 5183 & -1932 & 347 & -30 & 1 \\ 261 & -5430 & 5183 & -1932 & 347 & -30 & 1 \\ 325 & -5430 & 5183 & -1932 & 347 & -30 & 1 \\ 101 & -5398 & 5183 & -1932 & 347 & -30 & 1 \\ 165 & -5398 & 5183 & -1932 & 347 & -30 & 1 \\ 661 & -5590 & 5199 & -1932 & 347 & -30 & 1 \\ -1875 & -4350 & 5015 & -1924 & 347 & -30 & 1 \\ -2035 & -4318 & 5015 & -1924 & 347 & -30 & 1 \\ -1155 & -4574 & 5031 & -1924 & 347 & -30 & 1 \\ -1315 & -4542 & 5031 & -1924 & 347 & -30 & 1 \\ -1475 & -4510 & 5031 & -1924 & 347 & -30 & 1 \\ -1635 & -4478 & 5031 & -1924 & 347 & -30 & 1 \\ -595 & -4766 & 5047 & -1924 & 347 & -30 & 1 \\ -755 & -4734 & 5047 & -1924 & 347 & -30 & 1 \\ -915 & -4702 & 5047 & -1924 & 347 & -30 & 1 \\ -1139 & -4670 & 5047 & -1924 & 347 & -30 & 1 \\ -1075 & -4670 & 5047 & -1924 & 347 & -30 & 1 \\ -355 & -4894 & 5063 & -1924 & 347 & -30 & 1 \\ -579 & -4862 & 5063 & -1924 & 347 & -30 & 1 \\ -515 & -4862 & 5063 & -1924 & 347 & -30 & 1 \\ -3515 & -3462 & 4863 & -1916 & 347 & -30 & 1 \\ -3115 & -3622 & 4879 & -1916 & 347 & -30 & 1 \\ -3275 & -3590 & 4879 & -1916 & 347 & -30 & 1 \\ -2555 & -3814 & 4895 & -1916 & 347 & -30 & 1 \\ -2715 & -3782 & 4895 & -1916 & 347 & -30 & 1 \\ -2875 & -3750 & 4895 & -1916 & 347 & -30 & 1 \\ -2155 & -3974 & 4911 & -1916 & 347 & -30 & 1 \\ -2315 & -3942 & 4911 & -1916 & 347 & -30 & 1 \\ -1595 & -4166 & 4927 & -1916 & 347 & -30 & 1 \\ -1755 & -4134 & 4927 & -1916 & 347 & -30 & 1 \\ -1979 & -4102 & 4927 & -1916 & 347 & -30 & 1 \\ -4515 & -2862 & 4743 & -1908 & 347 & -30 & 1 \\ -3955 & -3054 & 4759 & -1908 & 347 & -30 & 1 \\ -4115 & -3022 & 4759 & -1908 & 347 & -30 & 1 \\ -3555 & -3214 & 4775 & -1908 & 347 & -30 & 1 \\ -3715 & -3182 & 4775 & -1908 & 347 & -30 & 1 \\ -2995 & -3406 & 4791 & -1908 & 347 & -30 & 1 \\ -5515 & -2262 & 4623 & -1900 & 347 & -30 & 1 \\ -4955 & -2454 & 4639 & -1900 & 347 & -30 & 1 \end{array} \right)$$

```
g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{19 585, -163 118, 150 995, -56 044, 10 063, -870, 29}
```

```
Array[c, 7].Transpose[A]
```

```
{845 c[1] - 5934 c[2] + 5303 c[3] - 1940 c[4] + 347 c[5] - 30 c[6] + c[7],  

 1501 c[1] - 6158 c[2] + 5319 c[3] - 1940 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -75 c[1] - 5270 c[2] + 5167 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -235 c[1] - 5238 c[2] + 5167 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -395 c[1] - 5206 c[2] + 5167 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7],  

 421 c[1] - 5462 c[2] + 5183 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7],  

 485 c[1] - 5462 c[2] + 5183 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7],  

 261 c[1] - 5430 c[2] + 5183 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7],  

 325 c[1] - 5430 c[2] + 5183 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7],  

 101 c[1] - 5398 c[2] + 5183 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7],  

 165 c[1] - 5398 c[2] + 5183 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7],  

 661 c[1] - 5590 c[2] + 5199 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -1875 c[1] - 4350 c[2] + 5015 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -2035 c[1] - 4318 c[2] + 5015 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -1155 c[1] - 4574 c[2] + 5031 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -1315 c[1] - 4542 c[2] + 5031 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -1475 c[1] - 4510 c[2] + 5031 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -1635 c[1] - 4478 c[2] + 5031 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -595 c[1] - 4766 c[2] + 5047 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -755 c[1] - 4734 c[2] + 5047 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -915 c[1] - 4702 c[2] + 5047 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -1139 c[1] - 4670 c[2] + 5047 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -1075 c[1] - 4670 c[2] + 5047 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -355 c[1] - 4894 c[2] + 5063 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -579 c[1] - 4862 c[2] + 5063 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -515 c[1] - 4862 c[2] + 5063 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -3515 c[1] - 3462 c[2] + 4863 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -3115 c[1] - 3622 c[2] + 4879 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -3275 c[1] - 3590 c[2] + 4879 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -2555 c[1] - 3814 c[2] + 4895 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -2715 c[1] - 3782 c[2] + 4895 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -2875 c[1] - 3750 c[2] + 4895 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -2155 c[1] - 3974 c[2] + 4911 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -2315 c[1] - 3942 c[2] + 4911 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -1595 c[1] - 4166 c[2] + 4927 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -1755 c[1] - 4134 c[2] + 4927 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -1979 c[1] - 4102 c[2] + 4927 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -4515 c[1] - 2862 c[2] + 4743 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -3955 c[1] - 3054 c[2] + 4759 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -4115 c[1] - 3022 c[2] + 4759 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -3555 c[1] - 3214 c[2] + 4775 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -3715 c[1] - 3182 c[2] + 4775 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -2995 c[1] - 3406 c[2] + 4791 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -5515 c[1] - 2262 c[2] + 4623 c[3] - 1900 c[4] + 347 c[5] - 30 c[6] + c[7],  

 -4955 c[1] - 2454 c[2] + 4639 c[3] - 1900 c[4] + 347 c[5] - 30 c[6] + c[7]}
```

```

Array[c, 7].g
19 585 c[1] - 163 118 c[2] + 150 995 c[3] - 56 044 c[4] + 10 063 c[5] - 870 c[6] + 29 c[7]

cert = Flatten[
  Array[c, 7] /. FindInstance[19 585 c[1] - 163 118 c[2] + 150 995 c[3] - 56 044 c[4] +
    10 063 c[5] - 870 c[6] + 29 c[7] < 0 &&
    845 c[1] - 5934 c[2] + 5303 c[3] - 1940 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    1501 c[1] - 6158 c[2] + 5319 c[3] - 1940 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -75 c[1] - 5270 c[2] + 5167 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -235 c[1] - 5238 c[2] + 5167 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -395 c[1] - 5206 c[2] + 5167 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    421 c[1] - 5462 c[2] + 5183 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    485 c[1] - 5462 c[2] + 5183 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    261 c[1] - 5430 c[2] + 5183 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    325 c[1] - 5430 c[2] + 5183 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    101 c[1] - 5398 c[2] + 5183 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    165 c[1] - 5398 c[2] + 5183 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    661 c[1] - 5590 c[2] + 5199 c[3] - 1932 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1875 c[1] - 4350 c[2] + 5015 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -2035 c[1] - 4318 c[2] + 5015 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1155 c[1] - 4574 c[2] + 5031 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1315 c[1] - 4542 c[2] + 5031 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1475 c[1] - 4510 c[2] + 5031 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1635 c[1] - 4478 c[2] + 5031 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -595 c[1] - 4766 c[2] + 5047 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -755 c[1] - 4734 c[2] + 5047 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -915 c[1] - 4702 c[2] + 5047 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1139 c[1] - 4670 c[2] + 5047 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1075 c[1] - 4670 c[2] + 5047 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -355 c[1] - 4894 c[2] + 5063 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -579 c[1] - 4862 c[2] + 5063 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -515 c[1] - 4862 c[2] + 5063 c[3] - 1924 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -3515 c[1] - 3462 c[2] + 4863 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -3115 c[1] - 3622 c[2] + 4879 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -3275 c[1] - 3590 c[2] + 4879 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -2555 c[1] - 3814 c[2] + 4895 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -2715 c[1] - 3782 c[2] + 4895 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -2875 c[1] - 3750 c[2] + 4895 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -2155 c[1] - 3974 c[2] + 4911 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -2315 c[1] - 3942 c[2] + 4911 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1595 c[1] - 4166 c[2] + 4927 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1755 c[1] - 4134 c[2] + 4927 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -1979 c[1] - 4102 c[2] + 4927 c[3] - 1916 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -4515 c[1] - 2862 c[2] + 4743 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -3955 c[1] - 3054 c[2] + 4759 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -4115 c[1] - 3022 c[2] + 4759 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
    -3555 c[1] - 3214 c[2] + 4775 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&

```

```

-3715 c[1] - 3182 c[2] + 4775 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
-2995 c[1] - 3406 c[2] + 4791 c[3] - 1908 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
-5515 c[1] - 2262 c[2] + 4623 c[3] - 1900 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0 &&
-4955 c[1] - 2454 c[2] + 4639 c[3] - 1900 c[4] + 347 c[5] - 30 c[6] + c[7] ≥ 0,
Array[c, 7], Integers]]

{425, 1747, 6111, 11531, 0, 0, 0}

GCD[425, 1747, 6111, 11531, 0, 0, 0]
1

Reverse[cert]
{0, 0, 0, 11531, 6111, 1747, 425}

cert.g
-156 440

cert.Transpose[A]
{28920, 14168, 59080, 46984, 34888, 32232, 59432, 20136,
47336, 8040, 35240, 8392, 64696, 52600, 77144, 65048, 52952, 40856,
77496, 65400, 53304, 14008, 41208, 53656, 14360, 41560, 82408,
70664, 58568, 71016, 58920, 46824, 59272, 47176, 59624, 47528,
8232, 64536, 64888, 52792, 53144, 41048, 53496, 46664, 47016}

```

$$\text{chi} = (-7 + x) (-5 + x)^8 (5 + x)^{15} \left(-3176 + 3557 x - 1500 x^2 + 298 x^3 - 28 x^4 + x^5 \right)$$

$$(-7 + x) (-5 + x)^8 (5 + x)^{15} \left(-3176 + 3557 x - 1500 x^2 + 298 x^3 - 28 x^4 + x^5 \right)$$

```

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{1295, 24371, -30241, 14683, -3659, 497, -35, 1},
 {2415, 23987, -30209, 14683, -3659, 497, -35, 1},
 {-385, 25507, -30481, 14699, -3659, 497, -35, 1},
 {735, 25123, -30449, 14699, -3659, 497, -35, 1},
 {-2065, 26643, -30721, 14715, -3659, 497, -35, 1},
 {9975, 18035, -28561, 14491, -3651, 497, -35, 1},
 {11095, 17651, -28529, 14491, -3651, 497, -35, 1},
 {7175, 19555, -28833, 14507, -3651, 497, -35, 1},
 {8295, 19171, -28801, 14507, -3651, 497, -35, 1},
 {9415, 18787, -28769, 14507, -3651, 497, -35, 1},
 {4375, 21075, -29105, 14523, -3651, 497, -35, 1},
 {5495, 20691, -29073, 14523, -3651, 497, -35, 1},
 {6615, 20307, -29041, 14523, -3651, 497, -35, 1},
 {2695, 22211, -29345, 14539, -3651, 497, -35, 1},
 {3815, 21827, -29313, 14539, -3651, 497, -35, 1},
 {16975, 12835, -27121, 14315, -3643, 497, -35, 1},
 {14175, 14355, -27393, 14331, -3643, 497, -35, 1},
 {15295, 13971, -27361, 14331, -3643, 497, -35, 1},
 {11375, 15875, -27665, 14347, -3643, 497, -35, 1},
 {12495, 15491, -27633, 14347, -3643, 497, -35, 1},
 {13615, 15107, -27601, 14347, -3643, 497, -35, 1},
 {8575, 17395, -27937, 14363, -3643, 497, -35, 1},
 {23975, 7635, -25681, 14139, -3635, 497, -35, 1},
 {21175, 9155, -25953, 14155, -3635, 497, -35, 1},
 {18375, 10675, -26225, 14171, -3635, 497, -35, 1},
 {14455, 12579, -26529, 14187, -3635, 497, -35, 1},
 {28175, 3955, -24513, 13979, -3627, 497, -35, 1}}

```

```
A = {{1295, 24 371, -30 241, 14 683, -3659, 497, -35, 1},
{2415, 23 987, -30 209, 14 683, -3659, 497, -35, 1},
{-385, 25 507, -30 481, 14 699, -3659, 497, -35, 1},
{735, 25 123, -30 449, 14 699, -3659, 497, -35, 1},
{-2065, 26 643, -30 721, 14 715, -3659, 497, -35, 1},
{9975, 18 035, -28 561, 14 491, -3651, 497, -35, 1},
{11 095, 17 651, -28 529, 14 491, -3651, 497, -35, 1},
{7175, 19 555, -28 833, 14 507, -3651, 497, -35, 1},
{8295, 19 171, -28 801, 14 507, -3651, 497, -35, 1},
{9415, 18 787, -28 769, 14 507, -3651, 497, -35, 1},
{4375, 21 075, -29 105, 14 523, -3651, 497, -35, 1},
{5495, 20 691, -29 073, 14 523, -3651, 497, -35, 1},
{6615, 20 307, -29 041, 14 523, -3651, 497, -35, 1},
{2695, 22 211, -29 345, 14 539, -3651, 497, -35, 1},
{3815, 21 827, -29 313, 14 539, -3651, 497, -35, 1},
{16 975, 12 835, -27 121, 14 315, -3643, 497, -35, 1},
{14 175, 14 355, -27 393, 14 331, -3643, 497, -35, 1},
{15 295, 13 971, -27 361, 14 331, -3643, 497, -35, 1},
{11 375, 15 875, -27 665, 14 347, -3643, 497, -35, 1},
{12 495, 15 491, -27 633, 14 347, -3643, 497, -35, 1},
{13 615, 15 107, -27 601, 14 347, -3643, 497, -35, 1},
{8575, 17 395, -27 937, 14 363, -3643, 497, -35, 1},
{23 975, 7635, -25 681, 14 139, -3635, 497, -35, 1},
{21 175, 9155, -25 953, 14 155, -3635, 497, -35, 1},
{18 375, 10 675, -26 225, 14 171, -3635, 497, -35, 1},
{14 455, 12 579, -26 529, 14 187, -3635, 497, -35, 1},
{28 175, 3955, -24 513, 13 979, -3627, 497, -35, 1}};
```

```
A // MatrixForm
```

$$\left(\begin{array}{cccccccccc} 1295 & 24\,371 & -30\,241 & 14\,683 & -3659 & 497 & -35 & 1 \\ 2415 & 23\,987 & -30\,209 & 14\,683 & -3659 & 497 & -35 & 1 \\ -385 & 25\,507 & -30\,481 & 14\,699 & -3659 & 497 & -35 & 1 \\ 735 & 25\,123 & -30\,449 & 14\,699 & -3659 & 497 & -35 & 1 \\ -2065 & 26\,643 & -30\,721 & 14\,715 & -3659 & 497 & -35 & 1 \\ 9975 & 18\,035 & -28\,561 & 14\,491 & -3651 & 497 & -35 & 1 \\ 11\,095 & 17\,651 & -28\,529 & 14\,491 & -3651 & 497 & -35 & 1 \\ 7175 & 19\,555 & -28\,833 & 14\,507 & -3651 & 497 & -35 & 1 \\ 8295 & 19\,171 & -28\,801 & 14\,507 & -3651 & 497 & -35 & 1 \\ 9415 & 18\,787 & -28\,769 & 14\,507 & -3651 & 497 & -35 & 1 \\ 4375 & 21\,075 & -29\,105 & 14\,523 & -3651 & 497 & -35 & 1 \\ 5495 & 20\,691 & -29\,073 & 14\,523 & -3651 & 497 & -35 & 1 \\ 6615 & 20\,307 & -29\,041 & 14\,523 & -3651 & 497 & -35 & 1 \\ 2695 & 22\,211 & -29\,345 & 14\,539 & -3651 & 497 & -35 & 1 \\ 3815 & 21\,827 & -29\,313 & 14\,539 & -3651 & 497 & -35 & 1 \\ 16\,975 & 12\,835 & -27\,121 & 14\,315 & -3643 & 497 & -35 & 1 \\ 14\,175 & 14\,355 & -27\,393 & 14\,331 & -3643 & 497 & -35 & 1 \\ 15\,295 & 13\,971 & -27\,361 & 14\,331 & -3643 & 497 & -35 & 1 \\ 11\,375 & 15\,875 & -27\,665 & 14\,347 & -3643 & 497 & -35 & 1 \\ 12\,495 & 15\,491 & -27\,633 & 14\,347 & -3643 & 497 & -35 & 1 \\ 13\,615 & 15\,107 & -27\,601 & 14\,347 & -3643 & 497 & -35 & 1 \\ 8575 & 17\,395 & -27\,937 & 14\,363 & -3643 & 497 & -35 & 1 \\ 23\,975 & 7635 & -25\,681 & 14\,139 & -3635 & 497 & -35 & 1 \\ 21\,175 & 9155 & -25\,953 & 14\,155 & -3635 & 497 & -35 & 1 \\ 18\,375 & 10\,675 & -26\,225 & 14\,171 & -3635 & 497 & -35 & 1 \\ 14\,455 & 12\,579 & -26\,529 & 14\,187 & -3635 & 497 & -35 & 1 \\ 28\,175 & 3955 & -24\,513 & 13\,979 & -3627 & 497 & -35 & 1 \end{array} \right)$$

```
g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
```

```
{-76\,245, 791\,111, -896\,845, 427\,535, -106\,151, 14\,413, -1015, 29}
```

Array[c, 8].Transpose[A]

```
{1295 c[1] + 24371 c[2] - 30241 c[3] + 14683 c[4] - 3659 c[5] + 497 c[6] - 35 c[7] + c[8],  

 2415 c[1] + 23987 c[2] - 30209 c[3] + 14683 c[4] - 3659 c[5] + 497 c[6] - 35 c[7] + c[8],  

 -385 c[1] + 25507 c[2] - 30481 c[3] + 14699 c[4] - 3659 c[5] + 497 c[6] - 35 c[7] + c[8],  

 735 c[1] + 25123 c[2] - 30449 c[3] + 14699 c[4] - 3659 c[5] + 497 c[6] - 35 c[7] + c[8],  

 -2065 c[1] + 26643 c[2] - 30721 c[3] + 14715 c[4] - 3659 c[5] + 497 c[6] - 35 c[7] + c[8],  

 9975 c[1] + 18035 c[2] - 28561 c[3] + 14491 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8],  

 11095 c[1] + 17651 c[2] - 28529 c[3] +  

 14491 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8],  

 7175 c[1] + 19555 c[2] - 28833 c[3] + 14507 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8],  

 8295 c[1] + 19171 c[2] - 28801 c[3] + 14507 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8],  

 9415 c[1] + 18787 c[2] - 28769 c[3] + 14507 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8],  

 4375 c[1] + 21075 c[2] - 29105 c[3] + 14523 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8],  

 5495 c[1] + 20691 c[2] - 29073 c[3] + 14523 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8],  

 6615 c[1] + 20307 c[2] - 29041 c[3] + 14523 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8],  

 2695 c[1] + 22211 c[2] - 29345 c[3] + 14539 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8],  

 3815 c[1] + 21827 c[2] - 29313 c[3] + 14539 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8],  

 16975 c[1] + 12835 c[2] - 27121 c[3] + 14315 c[4] - 3643 c[5] + 497 c[6] -  

 35 c[7] + c[8], 14175 c[1] + 14355 c[2] - 27393 c[3] + 14331 c[4] - 3643 c[5] +  

 497 c[6] - 35 c[7] + c[8], 15295 c[1] + 13971 c[2] - 27361 c[3] + 14331 c[4] -  

 3643 c[5] + 497 c[6] - 35 c[7] + c[8], 11375 c[1] + 15875 c[2] - 27665 c[3] +  

 14347 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8], 12495 c[1] + 15491 c[2] -  

 27633 c[3] + 14347 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8], 13615 c[1] +  

 15107 c[2] - 27601 c[3] + 14347 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8],  

 8575 c[1] + 17395 c[2] - 27937 c[3] + 14363 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8],  

 23975 c[1] + 7635 c[2] - 25681 c[3] + 14139 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] + c[8],  

 21175 c[1] + 9155 c[2] - 25953 c[3] + 14155 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] + c[8],  

 18375 c[1] + 10675 c[2] - 26225 c[3] + 14171 c[4] -  

 3635 c[5] + 497 c[6] - 35 c[7] + c[8], 14455 c[1] + 12579 c[2] -  

 26529 c[3] + 14187 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] + c[8],  

 28175 c[1] + 3955 c[2] - 24513 c[3] + 13979 c[4] - 3627 c[5] + 497 c[6] - 35 c[7] + c[8]}
```

Array[c, 8].g

```
-76245 c[1] + 791111 c[2] - 896845 c[3] +  

 427535 c[4] - 106151 c[5] + 14413 c[6] - 1015 c[7] + 29 c[8]
```

```

cert = Flatten[
  Array[c, 8] /. FindInstance[-76245 c[1] + 791111 c[2] - 896845 c[3] + 427535 c[4] -
    106151 c[5] + 14413 c[6] - 1015 c[7] + 29 c[8] < 0 &&
    1295 c[1] + 24371 c[2] - 30241 c[3] + 14683 c[4] - 3659 c[5] + 497 c[6] -
    35 c[7] + c[8] ≥ 0 && 2415 c[1] + 23987 c[2] - 30209 c[3] + 14683 c[4] -
    3659 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 && -385 c[1] + 25507 c[2] -
    30481 c[3] + 14699 c[4] - 3659 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
    735 c[1] + 25123 c[2] - 30449 c[3] + 14699 c[4] - 3659 c[5] + 497 c[6] -
    35 c[7] + c[8] ≥ 0 && -2065 c[1] + 26643 c[2] - 30721 c[3] +
    14715 c[4] - 3659 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
    9975 c[1] + 18035 c[2] - 28561 c[3] + 14491 c[4] - 3651 c[5] + 497 c[6] -
    35 c[7] + c[8] ≥ 0 && 11095 c[1] + 17651 c[2] - 28529 c[3] +
    14491 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
    7175 c[1] + 19555 c[2] - 28833 c[3] + 14507 c[4] - 3651 c[5] + 497 c[6] -
    35 c[7] + c[8] ≥ 0 && 8295 c[1] + 19171 c[2] - 28801 c[3] +
    14507 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
    9415 c[1] + 18787 c[2] - 28769 c[3] + 14507 c[4] - 3651 c[5] + 497 c[6] -
    35 c[7] + c[8] ≥ 0 && 4375 c[1] + 21075 c[2] - 29105 c[3] +
    14523 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
    5495 c[1] + 20691 c[2] - 29073 c[3] + 14523 c[4] - 3651 c[5] + 497 c[6] -
    35 c[7] + c[8] ≥ 0 && 6615 c[1] + 20307 c[2] - 29041 c[3] +
    14523 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
    2695 c[1] + 22211 c[2] - 29345 c[3] + 14539 c[4] - 3651 c[5] + 497 c[6] -
    35 c[7] + c[8] ≥ 0 && 3815 c[1] + 21827 c[2] - 29313 c[3] +
    14539 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
    16975 c[1] + 12835 c[2] - 27121 c[3] + 14315 c[4] - 3643 c[5] +
    497 c[6] - 35 c[7] + c[8] ≥ 0 && 14175 c[1] + 14355 c[2] -
    27393 c[3] + 14331 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
    15295 c[1] + 13971 c[2] - 27361 c[3] + 14331 c[4] - 3643 c[5] +
    497 c[6] - 35 c[7] + c[8] ≥ 0 && 11375 c[1] + 15875 c[2] -
    27665 c[3] + 14347 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
    12495 c[1] + 15491 c[2] - 27633 c[3] + 14347 c[4] - 3643 c[5] +
    497 c[6] - 35 c[7] + c[8] ≥ 0 && 13615 c[1] + 15107 c[2] -
    27601 c[3] + 14347 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
    8575 c[1] + 17395 c[2] - 27937 c[3] + 14363 c[4] - 3643 c[5] + 497 c[6] -
    35 c[7] + c[8] ≥ 0 && 23975 c[1] + 7635 c[2] - 25681 c[3] +
    14139 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
    21175 c[1] + 9155 c[2] - 25953 c[3] + 14155 c[4] - 3635 c[5] + 497 c[6] -
    35 c[7] + c[8] ≥ 0 && 18375 c[1] + 10675 c[2] - 26225 c[3] +
    14171 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
    14455 c[1] + 12579 c[2] - 26529 c[3] + 14187 c[4] - 3635 c[5] + 497 c[6] -
    35 c[7] + c[8] ≥ 0 && 28175 c[1] + 3955 c[2] - 24513 c[3] + 13979 c[4] -
    3627 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0, Array[c, 8], Integers]]

{8, -1000, -7250, -51880, -369160, 0, 0, -783400120}

```

```

GCD[8, -1000, -7250, -51880, -369160, 0, 0, -783400120]
2

cert = cert / 2
{4, -500, -3625, -25940, -184580, 0, 0, -391700060}

Reverse[cert]
{-391700060, 0, 0, -184580, -25940, -3625, -500, 4}

cert.g
-1005415

cert.Transpose[A]
{244445, 324925, 124685, 205165, 4925, 861005, 941485, 660765, 741245, 821725,
460525, 541005, 621485, 340765, 421245, 1357805, 1157565, 1238045, 957325,
1037805, 1118285, 757085, 1854605, 1654365, 1454125, 1173405, 2151165}

```

$$\text{chi} = (-7 + x) (-5 + x)^8 (5 + x)^{15} \left(-2616 + 3365 x - 1484 x^2 + 298 x^3 - 28 x^4 + x^5 \right) \\ (-7 + x) (-5 + x)^8 (5 + x)^{15} \left(-2616 + 3365 x - 1484 x^2 + 298 x^3 - 28 x^4 + x^5 \right)$$

```

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{37975, -2765, -22801, 13787, -3619, 497, -35, 1},
 {1015, 23347, -29585, 14555, -3651, 497, -35, 1},
 {-2905, 25251, -29889, 14571, -3651, 497, -35, 1},
 {9695, 17011, -27905, 14363, -3643, 497, -35, 1},
 {4655, 19299, -28241, 14379, -3643, 497, -35, 1},
 {5775, 18915, -28209, 14379, -3643, 497, -35, 1},
 {735, 21203, -28545, 14395, -3643, 497, -35, 1},
 {1855, 20819, -28513, 14395, -3643, 497, -35, 1},
 {-2065, 22723, -28817, 14411, -3643, 497, -35, 1},
 {22295, 8771, -25921, 14155, -3635, 497, -35, 1},
 {17255, 11059, -26257, 14171, -3635, 497, -35, 1},
 {18375, 10675, -26225, 14171, -3635, 497, -35, 1},
 {19495, 10291, -26193, 14171, -3635, 497, -35, 1},
 {14455, 12579, -26529, 14187, -3635, 497, -35, 1},
 {15575, 12195, -26497, 14187, -3635, 497, -35, 1},
 {10535, 14483, -26833, 14203, -3635, 497, -35, 1},
 {11655, 14099, -26801, 14203, -3635, 497, -35, 1},
 {30975, 2435, -24241, 13963, -3627, 497, -35, 1},
 {27055, 4339, -24545, 13979, -3627, 497, -35, 1},
 {28175, 3955, -24513, 13979, -3627, 497, -35, 1},
 {29295, 3571, -24481, 13979, -3627, 497, -35, 1},
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 {25375, 5475, -24785, 13995, -3627, 497, -35, 1},
 {20335, 7763, -25121, 14011, -3627, 497, -35, 1},
 {43575, -5805, -22257, 13755, -3619, 497, -35, 1},
 {40775, -4285, -22529, 13771, -3619, 497, -35, 1},
 {36855, -2381, -22833, 13787, -3619, 497, -35, 1},
 {34055, -861, -23105, 13803, -3619, 497, -35, 1},
 {47775, -9485, -21089, 13595, -3611, 497, -35, 1},
 {43855, -7581, -21393, 13611, -3611, 497, -35, 1}}

```

```
A = {{1015, 23 347, -29 585, 14 555, -3651, 497, -35, 1},
 {-2905, 25 251, -29 889, 14 571, -3651, 497, -35, 1},
 {9695, 17 011, -27 905, 14 363, -3643, 497, -35, 1},
 {4655, 19 299, -28 241, 14 379, -3643, 497, -35, 1},
 {5775, 18 915, -28 209, 14 379, -3643, 497, -35, 1},
 {735, 21 203, -28 545, 14 395, -3643, 497, -35, 1},
 {1855, 20 819, -28 513, 14 395, -3643, 497, -35, 1},
 {-2065, 22 723, -28 817, 14 411, -3643, 497, -35, 1},
 {22 295, 8771, -25 921, 14 155, -3635, 497, -35, 1},
 {17 255, 11 059, -26 257, 14 171, -3635, 497, -35, 1},
 {18 375, 10 675, -26 225, 14 171, -3635, 497, -35, 1},
 {19 495, 10 291, -26 193, 14 171, -3635, 497, -35, 1},
 {14 455, 12 579, -26 529, 14 187, -3635, 497, -35, 1},
 {15 575, 12 195, -26 497, 14 187, -3635, 497, -35, 1},
 {10 535, 14 483, -26 833, 14 203, -3635, 497, -35, 1},
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 {28 175, 3955, -24 513, 13 979, -3627, 497, -35, 1},
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 {24 255, 5859, -24 817, 13 995, -3627, 497, -35, 1},
 {25 375, 5475, -24 785, 13 995, -3627, 497, -35, 1},
 {20 335, 7763, -25 121, 14 011, -3627, 497, -35, 1},
 {43 575, -5805, -22 257, 13 755, -3619, 497, -35, 1},
 {40 775, -4285, -22 529, 13 771, -3619, 497, -35, 1},
 {36 855, -2381, -22 833, 13 787, -3619, 497, -35, 1},
 {37 975, -2765, -22 801, 13 787, -3619, 497, -35, 1},
 {34 055, -861, -23 105, 13 803, -3619, 497, -35, 1},
 {47 775, -9485, -21 089, 13 595, -3611, 497, -35, 1},
 {43 855, -7581, -21 393, 13 611, -3611, 497, -35, 1}};
```

```
A // MatrixForm
```

$$\left(\begin{array}{cccccccccc} 1015 & 23\,347 & -29\,585 & 14\,555 & -3651 & 497 & -35 & 1 \\ -2905 & 25\,251 & -29\,889 & 14\,571 & -3651 & 497 & -35 & 1 \\ 9695 & 17\,011 & -27\,905 & 14\,363 & -3643 & 497 & -35 & 1 \\ 4655 & 19\,299 & -28\,241 & 14\,379 & -3643 & 497 & -35 & 1 \\ 5775 & 18\,915 & -28\,209 & 14\,379 & -3643 & 497 & -35 & 1 \\ 735 & 21\,203 & -28\,545 & 14\,395 & -3643 & 497 & -35 & 1 \\ 1855 & 20\,819 & -28\,513 & 14\,395 & -3643 & 497 & -35 & 1 \\ -2065 & 22\,723 & -28\,817 & 14\,411 & -3643 & 497 & -35 & 1 \\ 22\,295 & 8771 & -25\,921 & 14\,155 & -3635 & 497 & -35 & 1 \\ 17\,255 & 11\,059 & -26\,257 & 14\,171 & -3635 & 497 & -35 & 1 \\ 18\,375 & 10\,675 & -26\,225 & 14\,171 & -3635 & 497 & -35 & 1 \\ 19\,495 & 10\,291 & -26\,193 & 14\,171 & -3635 & 497 & -35 & 1 \\ 14\,455 & 12\,579 & -26\,529 & 14\,187 & -3635 & 497 & -35 & 1 \\ 15\,575 & 12\,195 & -26\,497 & 14\,187 & -3635 & 497 & -35 & 1 \\ 10\,535 & 14\,483 & -26\,833 & 14\,203 & -3635 & 497 & -35 & 1 \\ 11\,655 & 14\,099 & -26\,801 & 14\,203 & -3635 & 497 & -35 & 1 \\ 30\,975 & 2435 & -24\,241 & 13\,963 & -3627 & 497 & -35 & 1 \\ 27\,055 & 4339 & -24\,545 & 13\,979 & -3627 & 497 & -35 & 1 \\ 28\,175 & 3955 & -24\,513 & 13\,979 & -3627 & 497 & -35 & 1 \\ 29\,295 & 3571 & -24\,481 & 13\,979 & -3627 & 497 & -35 & 1 \\ 24\,255 & 5859 & -24\,817 & 13\,995 & -3627 & 497 & -35 & 1 \\ 25\,375 & 5475 & -24\,785 & 13\,995 & -3627 & 497 & -35 & 1 \\ 20\,335 & 7763 & -25\,121 & 14\,011 & -3627 & 497 & -35 & 1 \\ 43\,575 & -5805 & -22\,257 & 13\,755 & -3619 & 497 & -35 & 1 \\ 40\,775 & -4285 & -22\,529 & 13\,771 & -3619 & 497 & -35 & 1 \\ 36\,855 & -2381 & -22\,833 & 13\,787 & -3619 & 497 & -35 & 1 \\ 37\,975 & -2765 & -22\,801 & 13\,787 & -3619 & 497 & -35 & 1 \\ 34\,055 & -861 & -23\,105 & 13\,803 & -3619 & 497 & -35 & 1 \\ 47\,775 & -9485 & -21\,089 & 13\,595 & -3611 & 497 & -35 & 1 \\ 43\,855 & -7581 & -21\,393 & 13\,611 & -3611 & 497 & -35 & 1 \end{array} \right)$$

```
g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
{13 355, 649 511, -841 709, 419 375, -105 735, 14 413, -1015, 29}
```

```
Array[c, 8].Transpose[A]
```

```
{1015 c[1] + 23 347 c[2] - 29 585 c[3] + 14 555 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8],  
- 2905 c[1] + 25 251 c[2] - 29 889 c[3] + 14 571 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8],  
9695 c[1] + 17 011 c[2] - 27 905 c[3] + 14 363 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8],  
4655 c[1] + 19 299 c[2] - 28 241 c[3] + 14 379 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8],  
5775 c[1] + 18 915 c[2] - 28 209 c[3] + 14 379 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8],  
735 c[1] + 21 203 c[2] - 28 545 c[3] + 14 395 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8],  
1855 c[1] + 20 819 c[2] - 28 513 c[3] + 14 395 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8],  
- 2065 c[1] + 22 723 c[2] - 28 817 c[3] + 14 411 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8],  
22 295 c[1] + 8771 c[2] - 25 921 c[3] + 14 155 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] + c[8],  
17 255 c[1] + 11 059 c[2] - 26 257 c[3] + 14 171 c[4] - 3635 c[5] + 497 c[6] -  
35 c[7] + c[8], 18 375 c[1] + 10 675 c[2] - 26 225 c[3] + 14 171 c[4] -  
3635 c[5] + 497 c[6] - 35 c[7] + c[8], 19 495 c[1] + 10 291 c[2] -  
26 193 c[3] + 14 171 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] + c[8], 14 455 c[1] +  
12 579 c[2] - 26 529 c[3] + 14 187 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] + c[8],  
15 575 c[1] + 12 195 c[2] - 26 497 c[3] + 14 187 c[4] - 3635 c[5] + 497 c[6] -  
35 c[7] + c[8], 10 535 c[1] + 14 483 c[2] - 26 833 c[3] + 14 203 c[4] -  
3635 c[5] + 497 c[6] - 35 c[7] + c[8], 11 655 c[1] + 14 099 c[2] -  
26 801 c[3] + 14 203 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] + c[8],  
30 975 c[1] + 24 35 c[2] - 24 241 c[3] + 13 963 c[4] - 3627 c[5] + 497 c[6] - 35 c[7] + c[8],  
27 055 c[1] + 43 39 c[2] - 24 545 c[3] + 13 979 c[4] - 3627 c[5] + 497 c[6] - 35 c[7] + c[8],  
28 175 c[1] + 39 55 c[2] - 24 513 c[3] + 13 979 c[4] - 3627 c[5] + 497 c[6] - 35 c[7] + c[8],  
29 295 c[1] + 35 71 c[2] - 24 481 c[3] + 13 979 c[4] - 3627 c[5] + 497 c[6] - 35 c[7] + c[8],  
24 255 c[1] + 58 59 c[2] - 24 817 c[3] + 13 995 c[4] - 3627 c[5] + 497 c[6] - 35 c[7] + c[8],  
25 375 c[1] + 54 75 c[2] - 24 785 c[3] + 13 995 c[4] - 3627 c[5] + 497 c[6] - 35 c[7] + c[8],  
20 335 c[1] + 77 63 c[2] - 25 121 c[3] + 14 011 c[4] - 3627 c[5] + 497 c[6] - 35 c[7] + c[8],  
43 575 c[1] - 58 05 c[2] - 22 257 c[3] + 13 755 c[4] - 3619 c[5] + 497 c[6] - 35 c[7] + c[8],  
40 775 c[1] - 42 85 c[2] - 22 529 c[3] + 13 771 c[4] - 3619 c[5] + 497 c[6] - 35 c[7] + c[8],  
36 855 c[1] - 23 81 c[2] - 22 833 c[3] + 13 787 c[4] - 3619 c[5] + 497 c[6] - 35 c[7] + c[8],  
37 975 c[1] - 27 65 c[2] - 22 801 c[3] + 13 787 c[4] - 3619 c[5] + 497 c[6] - 35 c[7] + c[8],  
34 055 c[1] - 86 1 c[2] - 23 105 c[3] + 13 803 c[4] - 3619 c[5] + 497 c[6] - 35 c[7] + c[8],  
47 775 c[1] - 94 85 c[2] - 21 089 c[3] + 13 595 c[4] - 3611 c[5] + 497 c[6] - 35 c[7] + c[8],  
43 855 c[1] - 75 81 c[2] - 21 393 c[3] + 13 611 c[4] - 3611 c[5] + 497 c[6] - 35 c[7] + c[8]}
```

```
Array[c, 8].g
```

```
13 355 c[1] + 649 511 c[2] - 841 709 c[3] +  
419 375 c[4] - 105 735 c[5] + 14 413 c[6] - 1015 c[7] + 29 c[8]
```

```
cert = Flatten[
```

```
Array[c, 8] /. FindInstance[13 355 c[1] + 649 511 c[2] - 841 709 c[3] + 419 375 c[4] -  
105 735 c[5] + 14 413 c[6] - 1015 c[7] + 29 c[8] < 0 &&  
1015 c[1] + 23 347 c[2] - 29 585 c[3] + 14 555 c[4] - 3651 c[5] + 497 c[6] -  
35 c[7] + c[8] ≥ 0 && -2905 c[1] + 25 251 c[2] - 29 889 c[3] + 14 571 c[4] -  
3651 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 && 9695 c[1] + 17 011 c[2] -  
27 905 c[3] + 14 363 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&  
4655 c[1] + 19 299 c[2] - 28 241 c[3] + 14 379 c[4] - 3643 c[5] + 497 c[6] -  
35 c[7] + c[8] ≥ 0 && 5775 c[1] + 18 915 c[2] - 28 209 c[3] +
```

```

14 379 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
735 c[1] + 21 203 c[2] - 28 545 c[3] + 14 395 c[4] - 3643 c[5] + 497 c[6] -
35 c[7] + c[8] ≥ 0 && 1855 c[1] + 20 819 c[2] - 28 513 c[3] +
14 395 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
-2065 c[1] + 22 723 c[2] - 28 817 c[3] + 14 411 c[4] - 3643 c[5] + 497 c[6] -
35 c[7] + c[8] ≥ 0 && 22 295 c[1] + 8771 c[2] - 25 921 c[3] +
14 155 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
17 255 c[1] + 11 059 c[2] - 26 257 c[3] + 14 171 c[4] - 3635 c[5] +
497 c[6] - 35 c[7] + c[8] ≥ 0 && 18 375 c[1] + 10 675 c[2] -
26 225 c[3] + 14 171 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
19 495 c[1] + 10 291 c[2] - 26 193 c[3] + 14 171 c[4] - 3635 c[5] +
497 c[6] - 35 c[7] + c[8] ≥ 0 && 14 455 c[1] + 12 579 c[2] -
26 529 c[3] + 14 187 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
15 575 c[1] + 12 195 c[2] - 26 497 c[3] + 14 187 c[4] - 3635 c[5] +
497 c[6] - 35 c[7] + c[8] ≥ 0 && 10 535 c[1] + 14 483 c[2] -
26 833 c[3] + 14 203 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
11 655 c[1] + 14 099 c[2] - 26 801 c[3] + 14 203 c[4] - 3635 c[5] +
497 c[6] - 35 c[7] + c[8] ≥ 0 && 30 975 c[1] + 2435 c[2] -
24 241 c[3] + 13 963 c[4] - 3627 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
27 055 c[1] + 4339 c[2] - 24 545 c[3] + 13 979 c[4] - 3627 c[5] + 497 c[6] -
35 c[7] + c[8] ≥ 0 && 28 175 c[1] + 3955 c[2] - 24 513 c[3] +
13 979 c[4] - 3627 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
29 295 c[1] + 3571 c[2] - 24 481 c[3] + 13 979 c[4] - 3627 c[5] + 497 c[6] -
35 c[7] + c[8] ≥ 0 && 24 255 c[1] + 5859 c[2] - 24 817 c[3] +
13 995 c[4] - 3627 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
25 375 c[1] + 5475 c[2] - 24 785 c[3] + 13 995 c[4] - 3627 c[5] + 497 c[6] -
35 c[7] + c[8] ≥ 0 && 20 335 c[1] + 7763 c[2] - 25 121 c[3] +
14 011 c[4] - 3627 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
43 575 c[1] - 5805 c[2] - 22 257 c[3] + 13 755 c[4] - 3619 c[5] + 497 c[6] -
35 c[7] + c[8] ≥ 0 && 40 775 c[1] - 4285 c[2] - 22 529 c[3] +
13 771 c[4] - 3619 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
36 855 c[1] - 2381 c[2] - 22 833 c[3] + 13 787 c[4] - 3619 c[5] + 497 c[6] -
35 c[7] + c[8] ≥ 0 && 37 975 c[1] - 2765 c[2] - 22 801 c[3] +
13 787 c[4] - 3619 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
34 055 c[1] - 861 c[2] - 23 105 c[3] + 13 803 c[4] - 3619 c[5] + 497 c[6] -
35 c[7] + c[8] ≥ 0 && 47 775 c[1] - 9485 c[2] - 21 089 c[3] +
13 595 c[4] - 3611 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
43 855 c[1] - 7581 c[2] - 21 393 c[3] + 13 611 c[4] - 3611 c[5] +
497 c[6] - 35 c[7] + c[8] ≥ 0, Array[c, 8], Integers]]}

{0, 2250, 25 343, 212 711, 1568 930, 0, 0, 3 329 450 510}

GCD[0, 2250, 25 343, 212 711, 1568 930, 0, 0, 3 329 450 510]

1

Reverse[cert]

{3 329 450 510, 0, 0, 1568 930, 212 711, 25 343, 2250, 0}

```

cert.g

- 1 104 572

certTranspose[A]

{53 780, 36 884, 84 948, 121 076, 68 052, 104 180, 51 156, 34 260, 133 012, 169 140, 116 116, 63 092, 99 220, 46 196, 82 324, 29 300, 164 180, 147 284, 94 260, 41 236, 77 364, 24 340, 60 468, 212 244, 142 324, 125 428, 72 404, 55 508, 50 548, 33 652}

$$\text{chi} = (-7 + x) (-5 + x)^8 (5 + x)^{15} (17 - 10x + x^2) (-176 + 101x - 18x^2 + x^3) \\ (-7 + x) (-5 + x)^8 (5 + x)^{15} (17 - 10x + x^2) (-176 + 101x - 18x^2 + x^3)$$

```

CoefficientList[feasibleinterlacingpolylist[chi], x]
{{-6097, 29235, -31233, 14747, -3659, 497, -35, 1},
 {-6545, 29299, -31233, 14747, -3659, 497, -35, 1},
 {3495, 21891, -29313, 14539, -3651, 497, -35, 1},
 {-425, 23795, -29617, 14555, -3651, 497, -35, 1},
 {1463, 23283, -29585, 14555, -3651, 497, -35, 1},
 {1015, 23347, -29585, 14555, -3651, 497, -35, 1},
 {2135, 22963, -29553, 14555, -3651, 497, -35, 1},
 {-1337, 24803, -29857, 14571, -3651, 497, -35, 1},
 {-1785, 24867, -29857, 14571, -3651, 497, -35, 1},
 {12175, 15555, -27633, 14347, -3643, 497, -35, 1},
 {13615, 15107, -27601, 14347, -3643, 497, -35, 1},
 {8575, 17395, -27937, 14363, -3643, 497, -35, 1},
 {8255, 17459, -27937, 14363, -3643, 497, -35, 1},
 {9695, 17011, -27905, 14363, -3643, 497, -35, 1},
 {10815, 16627, -27873, 14363, -3643, 497, -35, 1},
 {4655, 19299, -28241, 14379, -3643, 497, -35, 1},
 {5775, 18915, -28209, 14379, -3643, 497, -35, 1},
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 {8463, 18083, -28145, 14379, -3643, 497, -35, 1},
 {2975, 20435, -28481, 14395, -3643, 497, -35, 1},
 {21175, 9155, -25953, 14155, -3635, 497, -35, 1},
 {21975, 8835, -25921, 14155, -3635, 497, -35, 1},
 {17255, 11059, -26257, 14171, -3635, 497, -35, 1},
 {18375, 10675, -26225, 14171, -3635, 497, -35, 1},
 {19495, 10291, -26193, 14171, -3635, 497, -35, 1},
 {14455, 12579, -26529, 14187, -3635, 497, -35, 1},
 {15575, 12195, -26497, 14187, -3635, 497, -35, 1},
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 {11655, 14099, -26801, 14203, -3635, 497, -35, 1},
 {7735, 16003, -27105, 14219, -3635, 497, -35, 1},
 {27055, 4339, -24545, 13979, -3627, 497, -35, 1},
 {28175, 3955, -24513, 13979, -3627, 497, -35, 1},
 {24255, 5859, -24817, 13995, -3627, 497, -35, 1},
 {25375, 5475, -24785, 13995, -3627, 497, -35, 1},
 {34055, -861, -23105, 13803, -3619, 497, -35, 1}}

```

```
A = {{-6097, 29 235, -31 233, 14 747, -3659, 497, -35, 1},
{-6545, 29 299, -31 233, 14 747, -3659, 497, -35, 1},
{3495, 21 891, -29 313, 14 539, -3651, 497, -35, 1},
{-425, 23 795, -29 617, 14 555, -3651, 497, -35, 1},
{1463, 23 283, -29 585, 14 555, -3651, 497, -35, 1},
{1015, 23 347, -29 585, 14 555, -3651, 497, -35, 1},
{2135, 22 963, -29 553, 14 555, -3651, 497, -35, 1},
{-1337, 24 803, -29 857, 14 571, -3651, 497, -35, 1},
{-1785, 24 867, -29 857, 14 571, -3651, 497, -35, 1},
{12 175, 15 555, -27 633, 14 347, -3643, 497, -35, 1},
{13 615, 15 107, -27 601, 14 347, -3643, 497, -35, 1},
{8575, 17 395, -27 937, 14 363, -3643, 497, -35, 1},
{8255, 17 459, -27 937, 14 363, -3643, 497, -35, 1},
{9695, 17 011, -27 905, 14 363, -3643, 497, -35, 1},
{10 815, 16 627, -27 873, 14 363, -3643, 497, -35, 1},
{4655, 19 299, -28 241, 14 379, -3643, 497, -35, 1},
{5775, 18 915, -28 209, 14 379, -3643, 497, -35, 1},
{7343, 18 467, -28 177, 14 379, -3643, 497, -35, 1},
{6895, 18 531, -28 177, 14 379, -3643, 497, -35, 1},
{8463, 18 083, -28 145, 14 379, -3643, 497, -35, 1},
{2975, 20 435, -28 481, 14 395, -3643, 497, -35, 1},
{21 175, 9155, -25 953, 14 155, -3635, 497, -35, 1},
{21 975, 8835, -25 921, 14 155, -3635, 497, -35, 1},
{17 255, 11 059, -26 257, 14 171, -3635, 497, -35, 1},
{18 375, 10 675, -26 225, 14 171, -3635, 497, -35, 1},
{19 495, 10 291, -26 193, 14 171, -3635, 497, -35, 1},
{14 455, 12 579, -26 529, 14 187, -3635, 497, -35, 1},
{15 575, 12 195, -26 497, 14 187, -3635, 497, -35, 1},
{10 535, 14 483, -26 833, 14 203, -3635, 497, -35, 1},
{11 655, 14 099, -26 801, 14 203, -3635, 497, -35, 1},
{7735, 16 003, -27 105, 14 219, -3635, 497, -35, 1},
{27 055, 4339, -24 545, 13 979, -3627, 497, -35, 1},
{28 175, 3955, -24 513, 13 979, -3627, 497, -35, 1},
{24 255, 5859, -24 817, 13 995, -3627, 497, -35, 1},
{25 375, 5475, -24 785, 13 995, -3627, 497, -35, 1},
{34 055, -861, -23 105, 13 803, -3619, 497, -35, 1}};
```

```
A // MatrixForm
```

$$\left(\begin{array}{cccccccccc} -6097 & 29235 & -31233 & 14747 & -3659 & 497 & -35 & 1 \\ -6545 & 29299 & -31233 & 14747 & -3659 & 497 & -35 & 1 \\ 3495 & 21891 & -29313 & 14539 & -3651 & 497 & -35 & 1 \\ -425 & 23795 & -29617 & 14555 & -3651 & 497 & -35 & 1 \\ 1463 & 23283 & -29585 & 14555 & -3651 & 497 & -35 & 1 \\ 1015 & 23347 & -29585 & 14555 & -3651 & 497 & -35 & 1 \\ 2135 & 22963 & -29553 & 14555 & -3651 & 497 & -35 & 1 \\ -1337 & 24803 & -29857 & 14571 & -3651 & 497 & -35 & 1 \\ -1785 & 24867 & -29857 & 14571 & -3651 & 497 & -35 & 1 \\ 12175 & 15555 & -27633 & 14347 & -3643 & 497 & -35 & 1 \\ 13615 & 15107 & -27601 & 14347 & -3643 & 497 & -35 & 1 \\ 8575 & 17395 & -27937 & 14363 & -3643 & 497 & -35 & 1 \\ 8255 & 17459 & -27937 & 14363 & -3643 & 497 & -35 & 1 \\ 9695 & 17011 & -27905 & 14363 & -3643 & 497 & -35 & 1 \\ 10815 & 16627 & -27873 & 14363 & -3643 & 497 & -35 & 1 \\ 4655 & 19299 & -28241 & 14379 & -3643 & 497 & -35 & 1 \\ 5775 & 18915 & -28209 & 14379 & -3643 & 497 & -35 & 1 \\ 7343 & 18467 & -28177 & 14379 & -3643 & 497 & -35 & 1 \\ 6895 & 18531 & -28177 & 14379 & -3643 & 497 & -35 & 1 \\ 8463 & 18083 & -28145 & 14379 & -3643 & 497 & -35 & 1 \\ 2975 & 20435 & -28481 & 14395 & -3643 & 497 & -35 & 1 \\ 21175 & 9155 & -25953 & 14155 & -3635 & 497 & -35 & 1 \\ 21975 & 8835 & -25921 & 14155 & -3635 & 497 & -35 & 1 \\ 17255 & 11059 & -26257 & 14171 & -3635 & 497 & -35 & 1 \\ 18375 & 10675 & -26225 & 14171 & -3635 & 497 & -35 & 1 \\ 19495 & 10291 & -26193 & 14171 & -3635 & 497 & -35 & 1 \\ 14455 & 12579 & -26529 & 14187 & -3635 & 497 & -35 & 1 \\ 15575 & 12195 & -26497 & 14187 & -3635 & 497 & -35 & 1 \\ 10535 & 14483 & -26833 & 14203 & -3635 & 497 & -35 & 1 \\ 11655 & 14099 & -26801 & 14203 & -3635 & 497 & -35 & 1 \\ 7735 & 16003 & -27105 & 14219 & -3635 & 497 & -35 & 1 \\ 27055 & 4339 & -24545 & 13979 & -3627 & 497 & -35 & 1 \\ 28175 & 3955 & -24513 & 13979 & -3627 & 497 & -35 & 1 \\ 24255 & 5859 & -24817 & 13995 & -3627 & 497 & -35 & 1 \\ 25375 & 5475 & -24785 & 13995 & -3627 & 497 & -35 & 1 \\ 34055 & -861 & -23105 & 13803 & -3619 & 497 & -35 & 1 \end{array} \right)$$

```
g = CoefficientList[D[chi, x] / mu[chi] // Factor, x]
```

```
{-49765, 742247, -874829, 423855, -105943, 14413, -1015, 29}
```

```
Array[c, 8].Transpose[A]
```

```
{-6097 c[1] + 29235 c[2] - 31233 c[3] + 14747 c[4] - 3659 c[5] + 497 c[6] - 35 c[7] + c[8],  
-6545 c[1] + 29299 c[2] - 31233 c[3] + 14747 c[4] - 3659 c[5] + 497 c[6] - 35 c[7] + c[8],  
3495 c[1] + 21891 c[2] - 29313 c[3] + 14539 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8],  
-425 c[1] + 23795 c[2] - 29617 c[3] + 14555 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8],  
1463 c[1] + 23283 c[2] - 29585 c[3] + 14555 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8],  
1015 c[1] + 23347 c[2] - 29585 c[3] + 14555 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8],  
2135 c[1] + 22963 c[2] - 29553 c[3] + 14555 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8],  
-1337 c[1] + 24803 c[2] - 29857 c[3] + 14571 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8],  
-1785 c[1] + 24867 c[2] - 29857 c[3] + 14571 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8],  
12175 c[1] + 15555 c[2] - 27633 c[3] + 14347 c[4] -  
3643 c[5] + 497 c[6] - 35 c[7] + c[8], 13615 c[1] + 15107 c[2] -  
27601 c[3] + 14347 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8],  
8575 c[1] + 17395 c[2] - 27937 c[3] + 14363 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8],  
8255 c[1] + 17459 c[2] - 27937 c[3] + 14363 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8],  
9695 c[1] + 17011 c[2] - 27905 c[3] + 14363 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8],  
10815 c[1] + 16627 c[2] - 27873 c[3] +  
14363 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8],  
4655 c[1] + 19299 c[2] - 28241 c[3] + 14379 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8],  
5775 c[1] + 18915 c[2] - 28209 c[3] + 14379 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8],  
7343 c[1] + 18467 c[2] - 28177 c[3] + 14379 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8],  
6895 c[1] + 18531 c[2] - 28177 c[3] + 14379 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8],  
8463 c[1] + 18083 c[2] - 28145 c[3] + 14379 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8],  
2975 c[1] + 20435 c[2] - 28481 c[3] + 14395 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8],  
21175 c[1] + 9155 c[2] - 25953 c[3] + 14155 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] + c[8],  
21975 c[1] + 8835 c[2] - 25921 c[3] + 14155 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] + c[8],  
17255 c[1] + 11059 c[2] - 26257 c[3] + 14171 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] +  
c[8], 18375 c[1] + 10675 c[2] - 26225 c[3] + 14171 c[4] - 3635 c[5] + 497 c[6] -  
35 c[7] + c[8], 19495 c[1] + 10291 c[2] - 26193 c[3] + 14171 c[4] - 3635 c[5] +  
497 c[6] - 35 c[7] + c[8], 14455 c[1] + 12579 c[2] - 26529 c[3] + 14187 c[4] -  
3635 c[5] + 497 c[6] - 35 c[7] + c[8], 15575 c[1] + 12195 c[2] - 26497 c[3] +  
14187 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] + c[8], 10535 c[1] + 14483 c[2] -  
26833 c[3] + 14203 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] + c[8], 11655 c[1] +  
14099 c[2] - 26801 c[3] + 14203 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] + c[8],  
7735 c[1] + 16003 c[2] - 27105 c[3] + 14219 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] + c[8],  
27055 c[1] + 4339 c[2] - 24545 c[3] + 13979 c[4] - 3627 c[5] + 497 c[6] - 35 c[7] + c[8],  
28175 c[1] + 3955 c[2] - 24513 c[3] + 13979 c[4] - 3627 c[5] + 497 c[6] - 35 c[7] + c[8],  
24255 c[1] + 5859 c[2] - 24817 c[3] + 13995 c[4] - 3627 c[5] + 497 c[6] - 35 c[7] + c[8],  
25375 c[1] + 5475 c[2] - 24785 c[3] + 13995 c[4] - 3627 c[5] + 497 c[6] - 35 c[7] + c[8],  
34055 c[1] - 861 c[2] - 23105 c[3] + 13803 c[4] - 3619 c[5] + 497 c[6] - 35 c[7] + c[8]}
```

```
Array[c, 8].g
```

```
-49765 c[1] + 742247 c[2] - 874829 c[3] +  
423855 c[4] - 105943 c[5] + 14413 c[6] - 1015 c[7] + 29 c[8]
```

```
cert = Flatten[
```

```
Array[c, 8] /. FindInstance[-49765 c[1] + 742247 c[2] - 874829 c[3] + 423855 c[4] -
```

$$\begin{aligned}
& 105943 c[5] + 14413 c[6] - 1015 c[7] + 29 c[8] < 0 \&& \\
& -6097 c[1] + 29235 c[2] - 31233 c[3] + 14747 c[4] - 3659 c[5] + 497 c[6] - \\
& 35 c[7] + c[8] \geq 0 \&& -6545 c[1] + 29299 c[2] - 31233 c[3] + 14747 c[4] - \\
& 3659 c[5] + 497 c[6] - 35 c[7] + c[8] \geq 0 \&& 3495 c[1] + 21891 c[2] - \\
& 29313 c[3] + 14539 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8] \geq 0 \&& \\
& -425 c[1] + 23795 c[2] - 29617 c[3] + 14555 c[4] - 3651 c[5] + 497 c[6] - \\
& 35 c[7] + c[8] \geq 0 \&& 1463 c[1] + 23283 c[2] - 29585 c[3] + \\
& 14555 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8] \geq 0 \&& \\
& 1015 c[1] + 23347 c[2] - 29585 c[3] + 14555 c[4] - 3651 c[5] + 497 c[6] - \\
& 35 c[7] + c[8] \geq 0 \&& 2135 c[1] + 22963 c[2] - 29553 c[3] + \\
& 14555 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8] \geq 0 \&& \\
& -1337 c[1] + 24803 c[2] - 29857 c[3] + 14571 c[4] - 3651 c[5] + \\
& 497 c[6] - 35 c[7] + c[8] \geq 0 \&& -1785 c[1] + 24867 c[2] - \\
& 29857 c[3] + 14571 c[4] - 3651 c[5] + 497 c[6] - 35 c[7] + c[8] \geq 0 \&& \\
& 12175 c[1] + 15555 c[2] - 27633 c[3] + 14347 c[4] - 3643 c[5] + \\
& 497 c[6] - 35 c[7] + c[8] \geq 0 \&& 13615 c[1] + 15107 c[2] - \\
& 27601 c[3] + 14347 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8] \geq 0 \&& \\
& 8575 c[1] + 17395 c[2] - 27937 c[3] + 14363 c[4] - 3643 c[5] + 497 c[6] - \\
& 35 c[7] + c[8] \geq 0 \&& 8255 c[1] + 17459 c[2] - 27937 c[3] + \\
& 14363 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8] \geq 0 \&& \\
& 9695 c[1] + 17011 c[2] - 27905 c[3] + 14363 c[4] - 3643 c[5] + 497 c[6] - \\
& 35 c[7] + c[8] \geq 0 \&& 10815 c[1] + 16627 c[2] - 27873 c[3] + \\
& 14363 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8] \geq 0 \&& \\
& 4655 c[1] + 19299 c[2] - 28241 c[3] + 14379 c[4] - 3643 c[5] + 497 c[6] - \\
& 35 c[7] + c[8] \geq 0 \&& 5775 c[1] + 18915 c[2] - 28209 c[3] + \\
& 14379 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8] \geq 0 \&& \\
& 7343 c[1] + 18467 c[2] - 28177 c[3] + 14379 c[4] - 3643 c[5] + 497 c[6] - \\
& 35 c[7] + c[8] \geq 0 \&& 6895 c[1] + 18531 c[2] - 28177 c[3] + \\
& 14379 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8] \geq 0 \&& \\
& 8463 c[1] + 18083 c[2] - 28145 c[3] + 14379 c[4] - 3643 c[5] + 497 c[6] - \\
& 35 c[7] + c[8] \geq 0 \&& 2975 c[1] + 20435 c[2] - 28481 c[3] + \\
& 14395 c[4] - 3643 c[5] + 497 c[6] - 35 c[7] + c[8] \geq 0 \&& \\
& 21175 c[1] + 9155 c[2] - 25953 c[3] + 14155 c[4] - 3635 c[5] + 497 c[6] - \\
& 35 c[7] + c[8] \geq 0 \&& 21975 c[1] + 8835 c[2] - 25921 c[3] + \\
& 14155 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] + c[8] \geq 0 \&& \\
& 17255 c[1] + 11059 c[2] - 26257 c[3] + 14171 c[4] - 3635 c[5] + \\
& 497 c[6] - 35 c[7] + c[8] \geq 0 \&& 18375 c[1] + 10675 c[2] - \\
& 26225 c[3] + 14171 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] + c[8] \geq 0 \&& \\
& 19495 c[1] + 10291 c[2] - 26193 c[3] + 14171 c[4] - 3635 c[5] + \\
& 497 c[6] - 35 c[7] + c[8] \geq 0 \&& 14455 c[1] + 12579 c[2] - \\
& 26529 c[3] + 14187 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] + c[8] \geq 0 \&& \\
& 15575 c[1] + 12195 c[2] - 26497 c[3] + 14187 c[4] - 3635 c[5] + \\
& 497 c[6] - 35 c[7] + c[8] \geq 0 \&& 10535 c[1] + 14483 c[2] - \\
& 26833 c[3] + 14203 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] + c[8] \geq 0 \&& \\
& 11655 c[1] + 14099 c[2] - 26801 c[3] + 14203 c[4] - 3635 c[5] + \\
& 497 c[6] - 35 c[7] + c[8] \geq 0 \&& 7735 c[1] + 16003 c[2] - \\
& 27105 c[3] + 14219 c[4] - 3635 c[5] + 497 c[6] - 35 c[7] + c[8] \geq 0 \&&
\end{aligned}$$

```

27 055 c[1] + 4339 c[2] - 24 545 c[3] + 13 979 c[4] - 3627 c[5] + 497 c[6] -
35 c[7] + c[8] ≥ 0 && 28 175 c[1] + 3955 c[2] - 24 513 c[3] +
13 979 c[4] - 3627 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
24 255 c[1] + 5859 c[2] - 24 817 c[3] + 13 995 c[4] - 3627 c[5] + 497 c[6] -
35 c[7] + c[8] ≥ 0 && 25 375 c[1] + 5475 c[2] - 24 785 c[3] +
13 995 c[4] - 3627 c[5] + 497 c[6] - 35 c[7] + c[8] ≥ 0 &&
34 055 c[1] - 861 c[2] - 23 105 c[3] + 13 803 c[4] - 3619 c[5] +
497 c[6] - 35 c[7] + c[8] ≥ 0, Array[c, 8], Integers]]

{-2001, -7066, -19 411, -27 929, 0, 0, 0, 0}

GCD[-2001, -7066, -19 411, -27 929, 0, 0, 0, 0]

1

Reverse[cert]

{0, 0, 0, 0, -27 929, -19 411, -7066, -2001}

cert.g

-1 678 113

cert.Transpose[A]

{20 387, 464 611, 1 259 611, 1 103 947, 322 699, 766 923, 617 995, 18 107, 462 331,
1 412 995, 1 075 971, 1 069 235, 1 257 331, 920 307, 771 379, 913 571, 764 643, 171 491,
615 715, 22 563, 460 051, 1 378 283, 1 417 451, 1 222 619, 1 073 691, 924 763, 918 027,
769 099, 762 363, 613 435, 457 771, 1 227 075, 1 078 147, 922 483, 773 555, 926 939}

```