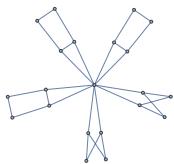


```

In[°]:= theonlyvalid21 = 

; adj21 = AdjacencyMatrix[theonlyvalid21];

In[°]:= Length[all2560]
Out[°]= 2560

In[°]:= Jacobi[x_, n_, matn_] := (-22 + x) (-2 + x)^42 (6 + x)^15 (8 + x)^2 * Det[

$$\frac{x+4}{(x+6)(x-2)} \text{IdentityMatrix}[n] + \frac{\text{matn}}{(x+6)(x-2)} + \frac{9 \text{ConstantArray}[1, \{n, n\}]}{(x+6)(x-2)(x-22)} +$$


$$\frac{(\text{residue} \text{mat} * (x-14)) \llbracket \text{Range}[n], \text{Range}[n] \rrbracket + \text{RA} \llbracket \text{Range}[n], \text{Range}[n] \rrbracket}{(x+8)(x+6)(x-2)(x-22)}]$$
;

```

In[°]:= Jacobi[53, 21, adj21]

Out[°]= 16 235 399 957 685 910 857 160 339 368 675 855 206 433 975 230 193 151 623 129 978 226 875

```

In[°]:= coclique22all = {};
For[j = 1, j ≤ 2560, j++,
  mat = ConstantArray[0, {22, 22}];
  mat[[Range[21], Range[21]]] = adj21;
  mat[[22, Range[20]]] = all2560[[j]];
  mat[[Range[20], 22]] = all2560[[j]];
  If[IntegerQ[Jacobi[53, 22, mat]], AppendTo[coclique22all, mat]]
] // AbsoluteTiming
coclique22all // Length

```

Out[°]= {3.10365, Null}

Out[°]= 454

```

In[°]:= coclique22graphs = Array[coclique22g, Length[coclique22all]];
For[i = 1, i ≤ Length[coclique22all], i++,
  coclique22graphs[[i]] = AdjacencyGraph[coclique22all[[i]]]
]
coclique22 = DeleteDuplicatesBy[coclique22graphs, CanonicalGraph];
Length[coclique22]

```

Out[°]= 7

In[•]:= Length[all454]

Out[•] = 454

```
In[®]:= co clique22all // Length
Out[®]= 454

In[®]:= co clique23allfrom22all = {};
For[i = 1, i ≤ 454, i++,
  n = 23;
  If[Mod[i, 10] == 0, Print[i]];
  For[j = 1, j ≤ 454, j++,
    mat = ConstantArray[0, {n, n}];
    mat[[Range[n - 1], Range[n - 1]]] = co clique22all[[i]];
    mat[[n, Range[20]]] = all454[[j]];
    mat[[Range[20], n]] = all454[[j]];
    If[IntegerQ[Jacobi[53, n, mat]], AppendTo[co clique23allfrom22all, mat]]
  ]
] // AbsoluteTiming
co clique23allfrom22all // Length
10
20
30
40
50
60
70
80
90
100
110
120
130
140
150
160
170
180
190
200
210
```

```

220
230
240
250
260
270
280
290
300
310
320
330
340
350
360
370
380
390
400
410
420
430
440
450

Out[®]= {300.39, Null}

Out[®]= 37 080

In[®]:= co clique23graphsfrom22all =
  Array[co clique23g22all, Length[co clique23allfrom22all]];
  For[i = 1, i ≤ Length[co clique23allfrom22all], i++,
    co clique23graphsfrom22all[[i]] = AdjacencyGraph[co clique23allfrom22all[[i]]];
  ]
  co clique23from22all =
    DeleteDuplicatesBy[co clique23graphsfrom22all, CanonicalGraph];
  Length[co clique23from22all]

Out[®]= 30

```

```
In[®]:= co clique23all = {};
For[i = 1, i ≤ 7, i++,
  n = 23;
  Print[i];
  For[j = 1, j ≤ 454, j++,
    mat = ConstantArray[0, {n, n}];
    mat[[Range[n - 1], Range[n - 1]]] = AdjacencyMatrix[co clique22[[i]]];
    mat[[n, Range[20]]] = all454[[j]];
    mat[[Range[20], n]] = all454[[j]];
    If[IntegerQ[Jacobi[53, n, mat]], AppendTo[co clique23all, mat]]
  ]
] // AbsoluteTiming
co clique23all // Length

1
2
3
4
5
6
7

Out[®]= {4.25689, Null}

Out[®]= 1556

In[®]:= co clique23graphs = Array[co clique23g, Length[co clique23all]];
For[i = 1, i ≤ Length[co clique23all], i++,
  co clique23graphs[[i]] = AdjacencyGraph[co clique23all[[i]]];
]
co clique23 = DeleteDuplicatesBy[co clique23graphs, CanonicalGraph];
Length[co clique23]

Out[®]= 30
```

```

In[®]:= co clique24all454 = {};
For[i = 1, i ≤ 30, i++,
  n = 24;
  If[Mod[i, 3] == 0, Print[i]];
  For[j = 1, j ≤ 454, j++,
    mat = ConstantArray[0, {n, n}];
    mat[[Range[n - 1], Range[n - 1]]] = AdjacencyMatrix[co clique23[[i]]];
    mat[[n, Range[20]]] = all454[[j]];
    mat[[Range[20], n]] = all454[[j]];
    If[IntegerQ[Jacobi[53, n, mat]], AppendTo[co clique24all454, mat]]
  ]
] // AbsoluteTiming
co clique24all454 // Length

3
6
9
12
15
18
21
24
27
30

Out[®]= {20.0645, Null}

Out[®]= 2924

In[®]:= co clique24all2560 = {};
For[i = 1, i ≤ 30, i++,
  n = 24;
  If[Mod[i, 3] == 0, Print[i]];
  For[j = 1, j ≤ 2560, j++,
    mat = ConstantArray[0, {n, n}];
    mat[[Range[n - 1], Range[n - 1]]] = AdjacencyMatrix[co clique23[[i]]];
    mat[[n, Range[20]]] = all2560[[j]];
    mat[[Range[20], n]] = all2560[[j]];
    If[IntegerQ[Jacobi[53, n, mat]], AppendTo[co clique24all2560, mat]]
  ]
] // AbsoluteTiming
co clique24all2560 // Length

```



```
In[6]:= Complement[coclique24all2560, coclique24all454] [[1]] // MatrixForm
```

Out[•]/MatrixForm=

0	1	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0		
1	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	
0	1	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	
1	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1
0	0	0	0	0	1	0	1	0	0	0	0	0	0	0	0	0	0	0	1	0	1
0	0	0	0	1	0	1	0	0	0	0	0	0	0	0	0	0	0	0	1	1	0
0	0	0	0	0	1	0	1	0	0	0	0	0	0	0	0	0	0	0	1	1	0
0	0	0	0	0	0	1	0	1	0	0	0	0	0	0	0	0	0	0	1	0	1
0	0	0	0	0	0	0	1	0	1	0	0	0	0	0	0	0	0	0	0	1	0
0	0	0	0	0	0	0	0	0	1	0	1	0	0	0	0	0	0	0	1	0	1
0	0	0	0	0	0	0	0	0	0	1	0	1	0	0	0	0	0	0	1	1	1
0	0	0	0	0	0	0	0	0	0	0	1	0	1	0	0	0	0	0	0	1	0
0	0	0	0	0	0	0	0	0	0	0	1	0	1	0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	0	0	0	0	0	1	0	1	0	0	0	0	1	1	0
0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	1	0	0	0	1	1	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	1	0	0	0	1	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	1	0	0	0	1
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	1	1	1	1
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	1	1	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	0
1	1	0	0	1	1	0	0	1	1	0	0	1	0	1	0	1	0	1	0	0	0
0	0	1	1	0	1	1	0	0	1	1	0	1	0	1	0	1	0	1	0	0	0
0	0	1	1	1	0	0	1	1	1	0	0	0	1	0	1	1	0	1	0	0	0
0	0	1	1	0	1	1	0	0	1	0	1	0	0	1	1	1	0	1	0	0	0

$\ln[\bullet] := \mathbf{A} =$

In[•]:= Range[24]

```
Out[6]= {1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24}
```

```

In[®]:= ran = {1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 24};

In[®]:= Jacobi[53, 21, A[[ran, ran]]]

Out[®]= 16 235 399 957 685 910 857 160 339 368 675 855 206 433 975 230 193 151 623 129 978 226 875

In[®]:= clique24graphs454 = Array[clique24g, Length[clique24all454]];
For[i = 1, i ≤ Length[clique24all454], i++,
  clique24graphs454[[i]] = AdjacencyGraph[clique24all454[[i]]]
]
clique24n454 = DeleteDuplicatesBy[clique24graphs454, CanonicalGraph];
Length[clique24n454]

Out[®]= 171

In[®]:= clique24graphs2560 = Array[clique24g, Length[clique24all2560]];
For[i = 1, i ≤ Length[clique24all2560], i++,
  clique24graphs2560[[i]] = AdjacencyGraph[clique24all2560[[i]]]
]
clique24n2560 = DeleteDuplicatesBy[clique24graphs2560, CanonicalGraph];
Length[clique24n2560]

Out[®]= 187

In[®]:= clique24refined = {};
For[i = 1, i ≤ Length[clique24], i++,
  If[Mod[i, 4] == 0, Print[i]];
  If[PolynomialQ[Jacobi[x, 24, AdjacencyMatrix[clique24[[i]]]] // Factor, x],
    AppendTo[clique24refined, clique24[[i]]]
  ] // AbsoluteTiming
]
clique24refined // Length

4
8
12
16
20
24
28
32
36
40
44
48
52
56
60
64

```

68
72
76
80
84
88
92
96
100
104
108
112
116
120
124
128
132
136
140
144
148
152
156
160
164
168
172
176
180
184
*Out[*⁶*] = {152.077, Null}*
*Out[*⁷*] = 171*

```
In[®]:= co clique25all = {};
For[i = 1, i ≤ 171, i++,
  n = 25;
  If[Mod[i, 5] == 0, Print[i]];
  For[j = 1, j ≤ 2560, j++,
    mat = ConstantArray[0, {n, n}];
    mat[[Range[n - 1], Range[n - 1]]] = AdjacencyMatrix[co clique24refined[[i]]];
    mat[[n, Range[20]]] = all2560[[j]];
    mat[[Range[20], n]] = all2560[[j]];
    If[IntegerQ[Jacobi[53, n, mat]], AppendTo[co clique25all, mat]]
  ]
] // AbsoluteTiming
co clique25all // Length
```

```
5
10
15
20
25
30
35
40
45
50
55
60
65
70
75
80
85
90
95
100
105
110
115
120
125
130
135
140
145
150
155
160
165
170
Out[®]= {890.125, Null}
Out[®]= 6608
```

```

In[®]:= co clique25graphs = Array[co clique25g, Length[co clique25all]];
For[i = 1, i ≤ Length[co clique25all], i++,
  co clique25graphs[[i]] = AdjacencyGraph[co clique25all[[i]]];
]
co clique25 = DeleteDuplicatesBy[co clique25graphs, CanonicalGraph];
Length[co clique25]

Out[®]= 467

In[®]:= co clique25refined = {};
For[i = 1, i ≤ Length[co clique25], i++,
  If[Mod[i, 10] == 0, Print[i]];
  If[PolynomialQ[Jacobi[x, 25, AdjacencyMatrix[co clique25[[i]]]] // Factor, x],
    AppendTo[co clique25refined, co clique25[[i]]];
  ] // AbsoluteTiming
co clique25refined // Length

10
20
30
40
50
60
70
80
90
100
110
120
130
140
150
160
170
180
190
200
210
220
230
240
250
260

```

```

270
280
290
300
310
320
330
340
350
360
370
380
390
400
410
420
430
440
450
460
Out[°]= {491.361, Null}

Out[°]= 467

```

```

In[°]:= coclique26all = {};
For[i = 1, i ≤ 467, i++,
  n = 26;
  If[Mod[i, 15] == 0, Print[i]];
  For[j = 1, j ≤ 454, j++,
    mat = ConstantArray[0, {n, n}];
    mat[[Range[n - 1], Range[n - 1]]] = AdjacencyMatrix[coclique25refined[[i]]];
    mat[[n, Range[20]]] = all454[[j]];
    mat[[Range[20], n]] = all454[[j]];
    If[IntegerQ[Jacobi[53, n, mat]], AppendTo[coclique26all, mat]]
  ]
] // AbsoluteTiming
coclique26all // Length

```

15
30
45
60
75
90
105
120
135
150
165
180
195
210
225
240
255
270
285
300
315
330
345
360
375
390
405
420
435
450
465

Out[]= {461.459, Null}

Out[]= 6706

```
In[®]:= coclique26graphs = Array[coclique26g, Length[coclique26all]];
For[i = 1, i ≤ Length[coclique26all], i++,
  coclique26graphs[[i]] = AdjacencyGraph[coclique26all[[i]]];
]
coclique26 = DeleteDuplicatesBy[coclique26graphs, CanonicalGraph];
Length[coclique26]

Out[®]= 1007

In[®]:= coclique26refined = {};
For[i = 1, i ≤ Length[coclique26], i++,
  If[Mod[i, 20] == 0, Print[i]];
  If[PolynomialQ[Jacobi[x, 26, AdjacencyMatrix[coclique26[[i]]]] // Factor, x],
    AppendTo[coclique26refined, coclique26[[i]]];
  ] // AbsoluteTiming
]
coclique26refined // Length

20
40
60
80
100
120
140
160
180
200
220
240
260
280
300
320
340
360
380
400
420
440
460
480
500
520
```

540
560
580
600
620
640
660
680
700
720
740
760
780
800
820
840
860
880
900
920
940
960
980
1000

Out[1]= {1312.64, Null}

Out[2]= 965

```
In[®]:= co clique27all = {};
For[i = 1, i ≤ 965, i++,
  n = 27;
  If[Mod[i, 20] == 0, Print[i]];
  For[j = 1, j ≤ 454, j++,
    mat = ConstantArray[0, {n, n}];
    mat[[Range[n - 1], Range[n - 1]]] = AdjacencyMatrix[co clique26refined[[i]]];
    mat[[n, Range[20]]] = all454[[j]];
    mat[[Range[20], n]] = all454[[j]];
    If[IntegerQ[Jacobi[53, n, mat]], AppendTo[co clique27all, mat]]
  ]
] // AbsoluteTiming
co clique27all // Length
20
40
60
80
100
120
140
160
180
200
220
240
260
280
300
320
340
360
380
400
420
440
460
480
500
520
540
560
```

```

580
600
620
640
660
680
700
720
740
760
780
800
820
840
860
880
900
920
940
960
Out[=] {985.47, Null}

Out[=] 7140

In[=]:= co clique27graphs = Array[co clique27g, Length[co clique27all]];
For[i = 1, i ≤ Length[co clique27all], i++,
  co clique27graphs[[i]] = AdjacencyGraph[co clique27all[[i]]];
]
co clique27 = DeleteDuplicatesBy[co clique27graphs, CanonicalGraph];
Length[co clique27]

Out[=] 1113

In[=]:= co clique27refined = {};
For[i = 1, i ≤ Length[co clique27], i++,
  If[Mod[i, 20] == 0, Print[i]];
  If[PolynomialQ[Jacobi[x, 27, AdjacencyMatrix[co clique27[[i]]]] // Factor, x],
    AppendTo[co clique27refined, co clique27[[i]]];
  ] // AbsoluteTiming
co clique27refined // Length

20
40
60
80

```

100
120
140
160
180
200
220
240
260
280
300
320
340
360
380
400
420
440
460
480
500
520
540
560
580
600
620
640
660
680
700
720
740
760
780
800
820
840
860

```

880
900
920
940
960
980
1000
1020
1040
1060
1080
1100
Out[=]= {1721.29, Null}
Out[=]= 879

```

```

In[=]:= co clique28all = {};
For[i = 1, i ≤ 879, i++,
  n = 28;
  If[Mod[i, 20] == 0, Print[i]];
  For[j = 1, j ≤ 454, j++,
    mat = ConstantArray[0, {n, n}];
    mat[[Range[n - 1], Range[n - 1]]] = AdjacencyMatrix[co clique27refined[[i]]];
    mat[[n, Range[20]]] = all454[[j]];
    mat[[Range[20], n]] = all454[[j]];
    If[IntegerQ[Jacobi[53, n, mat]], AppendTo[co clique28all, mat]]
  ]
] // AbsoluteTiming
co clique28all // Length
20
40
60
80
100
120
140
160
180
200

```

220
240
260
280
300
320
340
360
380
400
420
440
460
480
500
520
540
560
580
600
620
640
660
680
700
720
740
760
780
800
820
840
860

Out[]= {991.886, Null}

Out[]= 2030

```

In[®]:= co clique28graphs = Array[co clique28g, Length[co clique28all]];
For[i = 1, i ≤ Length[co clique28all], i++,
  co clique28graphs[[i]] = AdjacencyGraph[co clique28all[[i]]]
]
co clique28 = DeleteDuplicatesBy[co clique28graphs, CanonicalGraph];
Length[co clique28]

Out[®]= 665

In[®]:= co clique28refined = {};
For[i = 1, i ≤ Length[co clique28], i++,
  If[Mod[i, 15] == 0, Print[i]];
  If[PolynomialQ[Jacobi[x, 28, AdjacencyMatrix[co clique28[[i]]]] // Factor, x],
    AppendTo[co clique28refined, co clique28[[i]]]
  ] // AbsoluteTiming
co clique28refined // Length

15
30
45
60
75
90
105
120
135
150
165
180
195
210
225
240
255
270
285
300
315
330
345
360
375
390

```

```

405
420
435
450
465
480
495
510
525
540
555
570
585
600
615
630
645
660

Out[=] {1172.59, Null}

Out[=] 417

In[=]:= deg10n29 = {};
For[i = 1, i ≤ 417, i++,
  val = AdjacencyMatrix[co clique28refined[[i]]].ConstantArray[1, 28];
  For[j = 1, j ≤ 20, j++,
    If[val[[j]] == 10, AppendTo[deg10n29, i];
     Print[i, " ", val]; Break[]]
  ]
]
deg10n29 // Length

43 {4, 8, 4, 8, 6, 6, 6, 6, 6, 6, 6, 6, 4, 10, 4, 8, 4, 8, 4, 10, 10, 10, 10, 10, 10, 10, 10}
46 {6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 2, 10, 6, 8, 4, 8, 4, 10, 10, 10, 10, 10, 10, 10, 10, 10}
47 {4, 8, 4, 8, 6, 6, 6, 6, 6, 6, 6, 6, 4, 10, 4, 8, 4, 8, 4, 10, 10, 10, 10, 10, 10, 10, 10, 10}
49 {6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 4, 10, 4, 6, 4, 10, 4, 10, 10, 10, 10, 10, 10, 10, 10}
50 {4, 8, 4, 8, 6, 6, 6, 6, 6, 6, 6, 6, 6, 4, 10, 4, 8, 4, 8, 4, 10, 10, 10, 10, 10, 10, 10, 10}
53 {6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 4, 10, 4, 8, 2, 8, 6, 10, 10, 10, 10, 10, 10, 10, 10}
61 {6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 2, 10, 6, 8, 4, 8, 4, 10, 10, 10, 10, 10, 10, 10, 10}
62 {6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 4, 10, 4, 6, 4, 10, 4, 10, 10, 10, 10, 10, 10, 10}
63 {6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 8, 2, 8, 6, 6, 4, 10, 4, 10, 10, 10, 10, 10, 10, 10}
66 {6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 10, 2, 10, 2, 10, 10, 10, 10, 10, 10, 10, 10}
125 {4, 8, 4, 8, 6, 6, 6, 6, 4, 10, 4, 6, 6, 6, 6, 8, 4, 8, 4, 10, 10, 10, 10, 10, 10, 10}
```

```

139 {4, 8, 4, 8, 6, 6, 6, 6, 8, 6, 4, 6, 6, 6, 6, 4, 10, 4, 10, 10, 10, 10, 10, 10, 10, 10}
141 {4, 8, 4, 8, 6, 6, 6, 6, 8, 6, 4, 6, 6, 6, 6, 4, 10, 4, 10, 10, 10, 10, 10, 10, 10}
152 {6, 6, 6, 6, 6, 6, 6, 4, 10, 4, 6, 4, 6, 8, 6, 8, 4, 8, 4, 10, 10, 10, 10, 10, 10}
153
{6, 6, 6, 6, 6, 6, 6, 4, 10, 4, 6, 6, 6, 6, 4, 10, 4, 10, 10, 10, 10, 10, 10, 10}
154 {6, 6, 6, 6, 6, 6, 6, 8, 6, 4, 4, 6, 8, 6, 6, 4, 10, 4, 10, 10, 10, 10, 10, 10, 10}
155 {6, 6, 6, 6, 6, 6, 6, 4, 10, 4, 6, 4, 6, 8, 6, 8, 4, 8, 4, 10, 10, 10, 10, 10, 10, 10}
156 {6, 6, 6, 6, 6, 6, 6, 4, 10, 4, 6, 6, 6, 6, 8, 2, 8, 6, 10, 10, 10, 10, 10, 10}
158
{6, 6, 6, 6, 6, 6, 6, 4, 10, 4, 6, 6, 6, 6, 4, 10, 4, 10, 10, 10, 10, 10, 10, 10}
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160 {6, 6, 6, 6, 6, 6, 6, 8, 6, 4, 6, 6, 6, 6, 2, 10, 6, 10, 10, 10, 10, 10, 10, 10}
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177
{6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 10, 2, 10, 2, 10, 10, 10, 10, 10, 10, 10}
178 {6, 6, 6, 6, 6, 6, 6, 6, 10, 6, 2, 6, 6, 6, 6, 6, 6, 6, 10, 10, 10, 10, 10, 10, 10, 10}
183 {6, 6, 6, 6, 6, 6, 6, 6, 10, 6, 2, 6, 6, 6, 6, 6, 6, 6, 6, 10, 10, 10, 10, 10, 10, 10, 10}
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185 {6, 6, 6, 6, 6, 6, 6, 6, 10, 6, 2, 6, 6, 6, 6, 6, 6, 6, 10, 10, 10, 10, 10, 10, 10, 10}
193 {6, 6, 6, 6, 6, 6, 6, 6, 10, 6, 2, 6, 6, 6, 6, 6, 6, 6, 6, 10, 10, 10, 10, 10, 10, 10, 10}
194 {6, 6, 6, 6, 6, 6, 6, 6, 10, 6, 2, 6, 6, 6, 6, 6, 6, 6, 10, 10, 10, 10, 10, 10, 10, 10}
195 {6, 6, 6, 6, 6, 6, 6, 6, 10, 6, 2, 6, 6, 6, 6, 6, 6, 6, 10, 10, 10, 10, 10, 10, 10, 10}
199 {4, 8, 4, 8, 6, 6, 6, 6, 10, 2, 6, 6, 6, 6, 6, 6, 6, 6, 10, 10, 10, 10, 10, 10, 10, 10}
201 {4, 8, 4, 8, 6, 6, 6, 6, 10, 2, 6, 6, 6, 6, 6, 6, 6, 6, 10, 10, 10, 10, 10, 10, 10, 10}
213 {6, 6, 6, 6, 6, 6, 6, 6, 10, 2, 6, 4, 6, 8, 6, 6, 6, 6, 6, 10, 10, 10, 10, 10, 10, 10, 10}
215 {6, 6, 6, 6, 6, 6, 6, 6, 10, 2, 6, 4, 6, 8, 6, 6, 6, 6, 6, 10, 10, 10, 10, 10, 10, 10, 10}
221 {6, 6, 6, 6, 6, 6, 6, 6, 10, 6, 2, 6, 6, 6, 6, 6, 6, 6, 6, 10, 10, 10, 10, 10, 10, 10, 10}
240 {6, 6, 6, 6, 6, 6, 6, 6, 10, 6, 2, 6, 6, 6, 6, 6, 6, 6, 10, 10, 10, 10, 10, 10, 10, 10}
241 {6, 6, 6, 6, 6, 6, 6, 6, 10, 6, 2, 6, 6, 6, 6, 6, 6, 6, 10, 10, 10, 10, 10, 10, 10, 10}
242 {6, 6, 6, 6, 6, 6, 6, 6, 10, 6, 2, 6, 6, 6, 6, 6, 6, 6, 10, 10, 10, 10, 10, 10, 10, 10}
244 {4, 8, 4, 8, 6, 6, 6, 6, 6, 6, 6, 4, 10, 4, 8, 4, 8, 4, 10, 10, 10, 10, 10, 10, 10, 10}
253
{6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 4, 10, 4, 6, 4, 10, 4, 10, 10, 10, 10, 10, 10, 10}
256
{6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 4, 10, 4, 6, 4, 10, 4, 10, 10, 10, 10, 10, 10, 10}
259 {4, 8, 4, 8, 6, 6, 6, 6, 6, 6, 6, 4, 10, 4, 8, 4, 8, 4, 10, 10, 10, 10, 10, 10, 10, 10}
270 {6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 4, 10, 4, 8, 2, 8, 6, 10, 10, 10, 10, 10, 10, 10, 10}

```

```

273 {6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 4, 10, 4, 8, 2, 8, 6, 10, 10, 10, 10, 10, 10, 10}
291 {6, 6, 6, 6, 6, 6, 6, 6, 10, 6, 2, 6, 6, 6, 6, 6, 6, 10, 10, 10, 10, 10, 10, 10, 10}
292 {6, 6, 6, 6, 6, 6, 6, 6, 10, 6, 2, 6, 6, 6, 6, 6, 6, 10, 10, 10, 10, 10, 10, 10, 10}
293 {6, 6, 6, 6, 6, 6, 6, 6, 10, 6, 2, 6, 6, 6, 6, 6, 6, 10, 10, 10, 10, 10, 10, 10, 10}
299 {6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 2, 10, 6, 8, 4, 8, 4, 10, 10, 10, 10, 10, 10, 10}
300
{6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 4, 10, 4, 6, 4, 10, 4, 10, 10, 10, 10, 10, 10, 10}
301 {6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 8, 2, 8, 6, 6, 4, 10, 4, 10, 10, 10, 10, 10, 10}
364
{6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 10, 2, 10, 2, 10, 10, 10, 10, 10, 10, 10}
365 {6, 6, 6, 6, 6, 6, 6, 6, 6, 10, 6, 2, 6, 6, 6, 6, 6, 6, 6, 10, 10, 10, 10, 10, 10, 10, 10}
373 {6, 6, 6, 6, 4, 8, 4, 8, 6, 8, 6, 4, 6, 6, 6, 6, 6, 4, 10, 4, 10, 10, 10, 10, 10, 10, 10}
377 {6, 6, 6, 6, 6, 6, 6, 4, 10, 4, 6, 4, 6, 8, 6, 8, 4, 8, 4, 10, 10, 10, 10, 10, 10, 10}
378
{6, 6, 6, 6, 6, 6, 6, 4, 10, 4, 6, 6, 6, 6, 6, 4, 10, 4, 10, 10, 10, 10, 10, 10, 10}
379 {6, 6, 6, 6, 6, 6, 6, 6, 4, 10, 4, 6, 6, 6, 6, 6, 8, 2, 8, 6, 10, 10, 10, 10, 10, 10, 10}
382 {6, 6, 6, 6, 6, 6, 6, 6, 8, 6, 4, 4, 6, 8, 6, 6, 4, 10, 4, 10, 10, 10, 10, 10, 10, 10, 10}
383 {6, 6, 6, 6, 6, 6, 6, 6, 8, 6, 4, 4, 6, 8, 6, 6, 4, 10, 4, 10, 10, 10, 10, 10, 10, 10}
384 {6, 6, 6, 6, 6, 6, 6, 6, 8, 6, 4, 4, 6, 8, 6, 6, 4, 10, 4, 10, 10, 10, 10, 10, 10, 10}
388 {6, 6, 6, 6, 6, 6, 6, 6, 8, 6, 4, 6, 6, 6, 6, 6, 2, 10, 6, 10, 10, 10, 10, 10, 10, 10}
389 {6, 6, 6, 6, 6, 6, 6, 6, 8, 6, 4, 4, 6, 8, 6, 6, 4, 10, 4, 10, 10, 10, 10, 10, 10, 10}
395 {6, 6, 6, 6, 6, 6, 6, 6, 10, 6, 2, 6, 6, 6, 6, 6, 6, 6, 10, 10, 10, 10, 10, 10, 10, 10}
405 {6, 6, 6, 6, 6, 6, 6, 6, 10, 6, 2, 6, 6, 6, 6, 6, 6, 6, 10, 10, 10, 10, 10, 10, 10, 10}
406 {6, 6, 6, 6, 6, 6, 6, 6, 10, 6, 2, 6, 6, 6, 6, 6, 6, 6, 10, 10, 10, 10, 10, 10, 10, 10}
416 {6, 6, 6, 6, 6, 6, 6, 6, 10, 6, 2, 6, 6, 6, 6, 6, 6, 6, 10, 10, 10, 10, 10, 10, 10, 10}
417 {6, 6, 6, 6, 6, 6, 6, 6, 10, 6, 2, 6, 6, 6, 6, 6, 6, 6, 10, 10, 10, 10, 10, 10, 10, 10}

```

Out[6] = 69

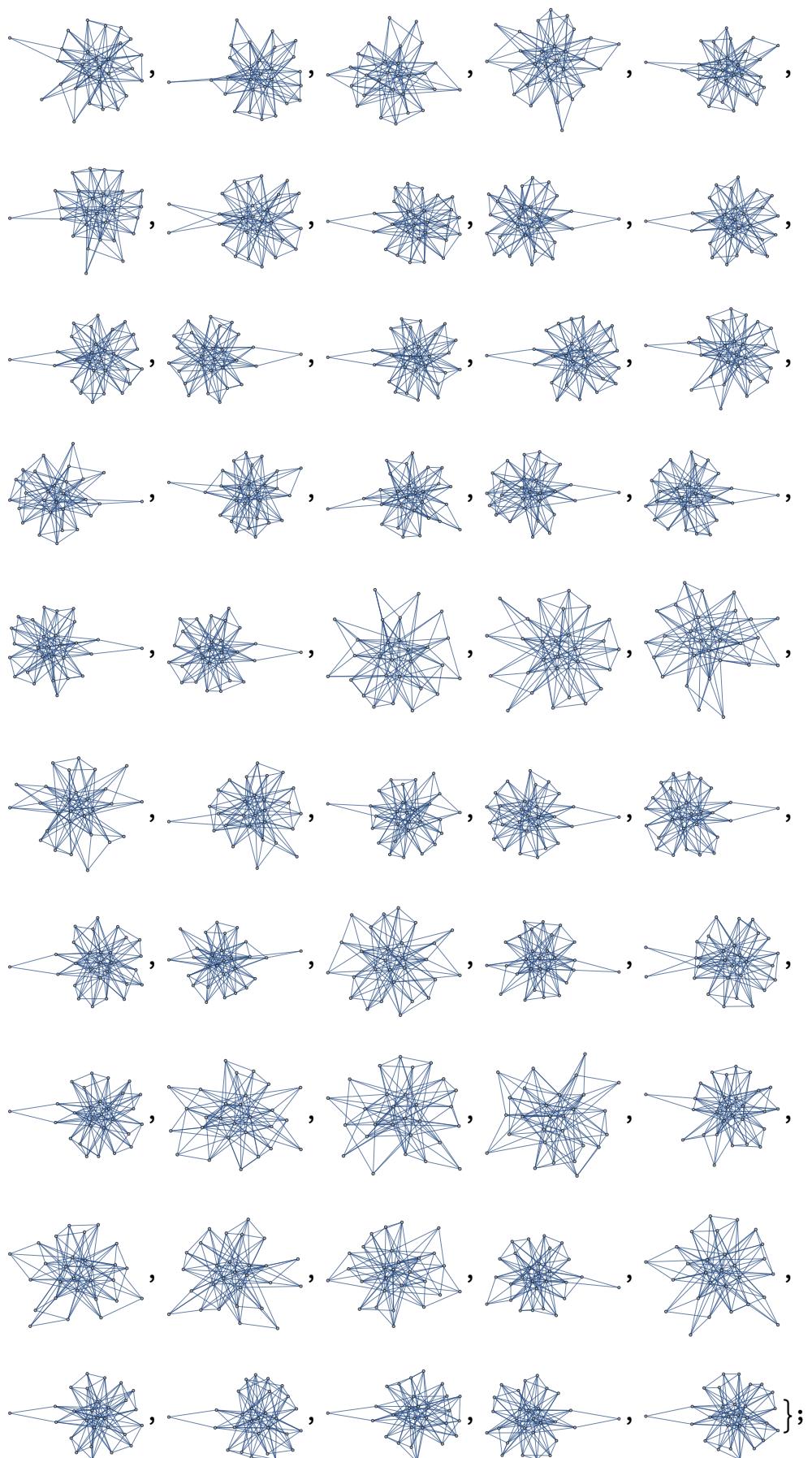
In[7]:= deg10n29

```

Out[7]= {43, 46, 47, 49, 50, 53, 61, 62, 63, 66, 125, 139, 141, 152, 153, 154, 155, 156, 158,
159, 160, 162, 165, 167, 171, 177, 178, 183, 184, 185, 193, 194, 195, 199, 201, 213,
215, 221, 240, 241, 242, 244, 253, 256, 259, 270, 273, 291, 292, 293, 299, 300, 301,
364, 365, 373, 377, 378, 379, 382, 383, 384, 388, 389, 395, 405, 406, 416, 417}

```

```
In[6]:= coclique28refined[[405]] // AdjacencyMatrix // MatrixForm
```



```
In[5]:= AdjacencyMatrix[  ] // MatrixForm
```

Out[•]//MatrixForm=

```
In[5]:= FindGraphIsomorphism[, , All]
```

```

Out[6] = {<| 1 → 1, 2 → 2, 3 → 3, 4 → 4, 5 → 5, 6 → 6, 7 → 7, 8 → 8, 9 → 9, 10 → 10, 11 → 11,
           12 → 12, 13 → 13, 14 → 14, 15 → 15, 16 → 16, 17 → 17, 18 → 18, 19 → 19, 20 → 20,
           21 → 21, 22 → 22, 23 → 23, 24 → 24, 25 → 25, 26 → 26, 27 → 27, 28 → 28 |>,
<| 1 → 5, 2 → 6, 3 → 7, 4 → 8, 5 → 1, 6 → 2, 7 → 3, 8 → 4, 9 → 9, 10 → 10, 11 → 11,
           12 → 12, 13 → 17, 14 → 18, 15 → 19, 16 → 20, 17 → 13, 18 → 14, 19 → 15, 20 → 16,
           21 → 21, 22 → 25, 23 → 23, 24 → 27, 25 → 22, 26 → 26, 27 → 24, 28 → 28 |>,
<| 1 → 16, 2 → 15, 3 → 14, 4 → 13, 5 → 20, 6 → 19, 7 → 18, 8 → 17, 9 → 11, 10 → 10,
           11 → 9, 12 → 12, 13 → 8, 14 → 7, 15 → 6, 16 → 5, 17 → 4, 18 → 3, 19 → 2, 20 → 1,
           21 → 23, 22 → 24, 23 → 21, 24 → 25, 25 → 27, 26 → 28, 27 → 22, 28 → 26 |>,
<| 1 → 20, 2 → 19, 3 → 18, 4 → 17, 5 → 16, 6 → 15, 7 → 14, 8 → 13, 9 → 11, 10 → 10,
           11 → 9, 12 → 12, 13 → 4, 14 → 3, 15 → 2, 16 → 1, 17 → 8, 18 → 7, 19 → 6, 20 → 5,
           21 → 23, 22 → 27, 23 → 21, 24 → 22, 25 → 24, 26 → 28, 27 → 25, 28 → 26 |> } 
```

```
In[®]:= GraphAutomorphismGroup[]
Out[®]= PermutationGroup[
{Cycles[{{1, 5}, {2, 6}, {3, 7}, {4, 8}, {13, 17}, {14, 18}, {15, 19}, {16, 20},
{22, 25}, {24, 27}}], Cycles[{{1, 16, 5, 20}, {2, 15, 6, 19}, {3, 14, 7, 18},
{4, 13, 8, 17}, {9, 11}, {21, 23}, {22, 24, 25, 27}, {26, 28}}]}]

In[®]:= GroupOrder[%6]
Out[®]= 4

In[®]:= co clique29all = {};
For[i = 1, i ≤ 417, i++,
n = 29;
If[Mod[i, 15] == 0, Print[i]];
For[j = 1, j ≤ 454, j++,
mat = ConstantArray[0, {n, n}];
mat[[Range[n - 1], Range[n - 1]]] = AdjacencyMatrix[co clique28refined[[i]]];
mat[[n, Range[20]]] = all454[[j]];
mat[[Range[20], n]] = all454[[j]];
If[IntegerQ[Jacobi[53, n, mat]], AppendTo[co clique29all, mat]]
]
] // AbsoluteTiming
co clique29all // Length
```

```

15
30
45
60
75
90
105
120
135
150
165
180
195
210
225
240
255
270
285
300
315
330
345
360
375
390
405

Out[6] = {516.183, Null}

Out[6] = 128

In[7] := co clique29graphs = Array[co clique29g, Length[co clique29all]];
For[i = 1, i ≤ Length[co clique29all], i++,
  co clique29graphs[[i]] = AdjacencyGraph[co clique29all[[i]]];
]
co clique29 = DeleteDuplicatesBy[co clique29graphs, CanonicalGraph];
Length[co clique29]

Out[7] = 56

In[8] := AdjacencyMatrix[co clique29[[56]]].ConstantArray[1, 29]
Out[8] = {4, 7, 5, 10, 7, 8, 5, 6, 8, 7, 6, 5, 8, 4,
  7, 7, 7, 5, 8, 6, 10, 10, 10, 10, 10, 10, 10, 10}

```

```

In[]:= Jacobi[53, 29, AdjacencyMatrix[co clique29[[56]]]]
Jacobi[x, 29, AdjacencyMatrix[co clique29[[56]]]] // Factor

Out[=] 270 260 461 526 483 871 266 743 056 343 762 377 305 573 244 790 078 125

Out[=] 
$$\frac{1}{(6+x)^2} (-2+x)^{14} (2+x)^3 (4+x) (2+4x+x^2)^2$$


$$(36\,096 + 139\,200 x + 72\,352 x^2 - 207\,392 x^3 - 336\,000 x^4 -$$


$$218\,340 x^5 - 74\,364 x^6 - 12\,986 x^7 - 686 x^8 + 128 x^9 + 22 x^{10} + x^{11})$$


In[]:= co clique29refined = {};
For[i = 1, i ≤ Length[co clique29], i++,
  If[Mod[i, 4] == 0, Print[i]];
  If[PolynomialQ[Jacobi[x, 29, AdjacencyMatrix[co clique29[[i]]]] // Factor, x],
    AppendTo[co clique29refined, co clique29[[i]]]]
] // AbsoluteTiming
co clique29refined // Length

4
8
12
16
20
24
28
32
36
40
44
48
52
56

Out[=] {113.802, Null}

Out[=] 0

In[]:= Length[co clique29all]

Out[=] 128

In[]:= co clique29nomodiso = {};
For[i = 1, i ≤ Length[co clique29all], i++,
  If[Mod[i, 4] == 0, Print[i];
  If[PolynomialQ[Jacobi[x, 29, co clique29all[[i]]] // Factor, x],
    AppendTo[co clique29nomodiso, co clique29all[[i]]]]
] // AbsoluteTiming
co clique29nomodiso // Length

```

4
8
12
16
20
24
28
32
36
40
44
48
52
56
60
64
68
72
76
80
84
88
92
96
100
104
108
112
116
120
124
128

Out[¹] = {260.534, Null}

Out[²] = 0