n, i, j, k Index variables for meta-lists

num Numeric literals

nat Internal literal numbers

hex Bit vector literal, specified by C-style hex number bin Bit vector literal, specified by C-style binary number

stringString literalsbacktick_stringString literals

regexp Regular expresions, as a string literal

x, y, z Variables ix Variables

```
l
                                                       Source locations
                        ::=
x^l, y^l, z^l, name
                                                       Location-annotated names
                              x l
                              (ix)l
                                                          Remove infix status
                              name_-t \to x^l
                                                  Μ
                                                          Extract x from a name_t
ix^l
                                                       Location-annotated infix names
                              ix l
                        ::=
                                                       Type variables
\alpha
                              \dot{x}
\alpha^l
                                                       Location-annotated type variables
                        ::=
                              \alpha l
N
                                                       numeric variables
                              ",x
N^l
                                                       Location-annotated numeric variables
                              N l
id
                                                       Long identifers
                              x_1^l \dots x_n^l . x^l l
tnv
                                                       Union of type variables and Nexp type variables, without lo
                              \alpha
                              N
tnvar^l
                        ::=
                                                       Union of type variables and Nexp type variables, with locati
                              \alpha^l
                                                       Type variable lists
tnvs
                              tnv_1 \dots tnv_n
tnvars^l
                                                       Type variable lists
                        ::=
                              tnvar_1^l ... tnvar_n^l
Nexp_aux
                                                       Numerical expressions for specifying vector lengths and inde
                        ::=
                              N
                              num
                              Nexp_1 * Nexp_2
                              Nexp_1 + Nexp_2
```

(Nexp)

```
Nexp
                                                                 Location-annotated vector lengths
                           ::=
                                 Nexp\_aux\ l
Nexp\_constraint\_aux
                                                                 Whether a vector is bounded or fixed size
                           ::=
                                 Nexp = Nexp'
                                 Nexp \ge Nexp'
Nexp\_constraint
                                                                 Location-annotated Nexp range
                           ::=
                                 Nexp\_constraint\_aux\ l
                           ::=
                                                                 Types
typ\_aux
                                                                    Unspecified type
                                                                    Type variables
                                                                    Function types
                                 typ_1 \rightarrow typ_2
                                 typ_1*....*typ_n
                                                                    Tuple types
                                                                    As a typ to permit applications over Nexps, o
                                 Nexp
                                 id\ typ_1 \dots typ_n
                                                                    Type applications
                                 backtick\_string\ typ_1\ ..\ typ_n
                                                                    Backend-Type applications
                                 (typ)
                                                                 Location-annotated types
typ
                                 typ_aux l
                                                                 Literal constants
lit\_aux
                           ::=
                                 true
                                 false
                                 string
                                                                   hex and bin are constant bit vectors, entered
                                 hex
                                 bin
                                 string
                                 string
                                 ()
                                 bitzero
                                                                   bitzero and bitone are constant bits, if commo
                                 bitone
lit
                           ::=
                                 lit\_aux\ l
                                                                    Location-annotated literal constants
;?
                           ::=
                                                                 Optional semi-colons
pat\_aux
                                                                 Patterns
                                                                    Wildcards
                                 (pat \mathbf{as} x^l)
                                                                   Named patterns
                                 (pat:typ)
                                                                    Typed patterns
                                                                    Single variable and constructor patterns
                                 id pat_1 ... pat_n
```

```
\langle |fpat_1; \dots; fpat_n; ?| \rangle
                                                                             Record patterns
                      [|pat_1; ...; pat_n;^?|]
                                                                             Vector patterns
                      [|pat_1 ... pat_n|]
                                                                             Concatenated vector patterns
                      (pat_1, \ldots, pat_n)
                                                                             Tuple patterns
                      [pat_1; ...; pat_n; ?]
                                                                             List patterns
                      (pat)
                      pat_1 :: pat_2
                                                                             Cons patterns
                      x^l + num
                                                                             constant addition patterns
                      lit
                                                                             Literal constant patterns
pat
                                                                          Location-annotated patterns
                      pat\_aux l
                                                                          Field patterns
fpat
                      id = pat l
               ::=
                                                                          Optional bars
                                                                          Expressions
exp_aux
                      id
                                                                             Identifiers
                      backtick_string
                                                                             identifier that should be literally used in out
                      N
                                                                             Nexp var, has type num
                      \mathbf{fun}\;psexp
                                                                             Curried functions
                     function ||^{?} pexp_{1}| \dots || pexp_{n}| end
                                                                             Functions with pattern matching
                      exp_1 \ exp_2
                                                                             Function applications
                      exp_1 ix^l exp_2
                                                                             Infix applications
                      \langle |fexps| \rangle
                                                                             Records
                      \langle |exp \mathbf{with} fexps| \rangle
                                                                             Functional update for records
                      exp.id
                                                                             Field projection for records
                      [|exp_1; ...; exp_n;^?|]
                                                                             Vector instantiation
                      exp.(Nexp)
                                                                             Vector access
                      exp.(Nexp_1..Nexp_2)
                                                                             Subvector extraction
                      match exp with |?| pexp_1| ... | pexp_n| l end
                                                                             Pattern matching expressions
                      (exp:typ)
                                                                             Type-annotated expressions
                      \mathbf{let}\ letbind\ \mathbf{in}\ exp
                                                                             Let expressions
                                                                             Tuples
                      (exp_1, \ldots, exp_n)
                      [exp_1; ...; exp_n; ?]
                                                                             Lists
                      (exp)
                      begin exp end
                                                                             Alternate syntax for (exp)
                      if exp_1 then exp_2 else exp_3
                                                                             Conditionals
                                                                             Cons expressions
                      exp_1 :: exp_2
                      lit
                                                                             Literal constants
                      \{exp_1|exp_2\}
                                                                             Set comprehensions
                      \{exp_1 | \mathbf{forall} \ qbind_1 .. \ qbind_n | exp_2\}
                                                                             Set comprehensions with explicit binding
                      \{exp_1; ...; exp_n;^?\}
                                                                             Sets
```

```
q \ qbind_1 \dots qbind_n.exp
                                                                                       Logical quantifications
                         [exp_1| forall qbind_1 ... qbind_n|exp_2]
                                                                                       List comprehensions (all binders mu
                         do id \ pat_1 \leftarrow exp_1; \ ... \ pat_n \leftarrow exp_n; \ \mathbf{in} \ exp \ \mathbf{end}
                                                                                       Do notation for monads
                                                                                    Location-annotated expressions
                   ::=
exp
                          exp\_aux l
                                                                                    Quantifiers
q
                   ::=
                         forall
                         exists
qbind
                                                                                    Bindings for quantifiers
                         x^{l}
                         (pat \, \mathbf{IN} \, exp)
                                                                                       Restricted quantifications over sets
                          (pat \mathbf{MEM} \ exp)
                                                                                       Restricted quantifications over lists
                                                                                    Field-expressions
fexp
                   ::=
                         id = exp l
                                                                                    Field-expression lists
fexps
                   ::=
                         fexp_1; \dots; fexp_n; ? l
                                                                                    Pattern matches
                   ::=
pexp
                         pat \rightarrow exp l
                                                                                    Multi-pattern matches
psexp
                         pat_1 \dots pat_n \to exp \ l
tannot?
                   ::=
                                                                                    Optional type annotations
                         : typ
funcl_aux
                                                                                    Function clauses
                         x^l pat_1 \dots pat_n tannot? = exp
letbind\_aux
                                                                                    Let bindings
                   ::=
                         pat\ tannot? = exp
                                                                                       Value bindings
                         funcl_{-}aux
                                                                                       Function bindings
letbind
                                                                                    Location-annotated let bindings
                          letbind\_aux\ l
funcl
                                                                                    Location-annotated function clauses
                         funcl_aux l
                                                                                    Name or name with type for inductive
name_{-}t
                         x^l
```

```
(x^l:typ)
                                                                                                            Names with optional type
name\_ts
                                    name\_t_0 ... name\_t_n
                                                                                                            Inductively defined relat
rule\_aux
                                   x^l: \mathbf{forall} \ name_-t_1 \dots name_-t_i.exp \Longrightarrow x_1^l \ exp_1 \dots exp_n
                                                                                                            Location-annotated indu
rule
                                    rule\_aux\ l
witness?
                                                                                                            Optional witness type na
                                    witness type x^l;
check?
                                                                                                            Option check name decla
                                    \mathbf{check}\,x^l;
functions?
                                                                                                            Optional names and typ
                                   x^{l}: typ
x^{l}: typ; functions^{?}
indreln\_name\_aux
                                                                                                            Name for inductively de-
                                    [x^l: typschm\ witness?\ check?\ functions?]
indreln\_name
                                                                                                            Location-annotated name
                            ::=
                                    indreln\_name\_aux\;l
                                                                                                            Type lists
typs
                                    typ_1 * ... * typ_n
ctor\_def
                                                                                                            Datatype definition clau
                                    x^l of typs
                                                                                                       S
                                                                                                               Constant constructors
texp
                                                                                                            Type definition bodies
                                                                                                               Type abbreviations
                                     \begin{array}{c} \langle |x_1^l:typ_1;\ldots;x_n^l:typ_n\,;^?|\rangle \\ |?\;ctor\_def_1|\ldots|ctor\_def_n \end{array} 
                                                                                                               Record types
                                                                                                               Variant types
name?
                                                                                                            Optional name specifica
                             ::=
                                    [name = regexp]
                                                                                                            Type definitions
td
                            ::=
```

```
\begin{array}{l} x^{l} \, tnvars^{l} \, name^{?} = texp \\ x^{l} \, tnvars^{l} \, name^{?} \end{array}
                                                                                                 Definitions of opaque types
                     ::=
                                                                                              Typeclass constraints
c
                           id\ tnvar^l
cs
                                                                                              Typeclass and length constraint
                                                                                                  Must have > 0 constraints
                           Nexp\_constraint_1, \dots, Nexp\_constraint_i \Rightarrow
                                                                                                  Must have > 0 constraints
                            c_1, \dots, c_i; Nexp\_constraint_1, \dots, Nexp\_constraint_n \Rightarrow
                                                                                                  Must have > 0 of both form of
                                                                                              Type and instance scheme prefix
c\_pre
                     ::=
                           \mathbf{forall}\,tnvar_1^l\dots tnvar_n^l.cs
                                                                                                 Must have > 0 type variables
typschm
                                                                                              Type schemes
                            c\_pre\ typ
instschm
                                                                                              Instance schemes
                    ::=
                            c\_pre(id\ typ)
                                                                                              Backend target names
target
                     ::=
                           hol
                           isabelle
                           ocaml
                           coq
                            tex
                           html
                           lem
open\_import
                                                                                              Open or import statements
                           open
                           import
                           open import
                           include
                           include import
                                                                                              Backend target name lists
                           \{target_1; ..; target_n\}
\{target_1; ..; target_n\}
                                                                                                  all targets except the listed or
                            non_exec
                                                                                                  all non-executable targets, use
\tau?
                                                                                              Optional targets
```

$lemma_typ$::= 	assert lemma theorem	Types of Lemmata
$lemma_decl$::=	$lemma_typ \ au^? \ x^l : exp$	Lemmata and Tests
dexp	::= 	$egin{aligned} \mathbf{name_s} &= string \ l \ \mathbf{format} &= string \ l \ \mathbf{arguments} &= exp_1 \dots exp_n \ l \ \mathbf{targuments} &= texp_1 \dots texp_n \ l \end{aligned}$	declaration field-expressions
$declare_arg$::= 	string $\langle dexp_1;; dexp_n; ^? l \rangle$	arguments to a declaration
component	::=	module function type field	components
$termination_setting$::= 	automatic manual	termination settings
$exhaustivity_setting$::= 	exhaustive inexhaustive	exhaustivity settings
$elim_opt$::= 	id	optional terms used as eliminators for patter
$fixity_decl$::= 	$egin{aligned} \mathbf{right_assoc} \ nat \\ \mathbf{left_assoc} \ nat \\ \mathbf{non_assoc} \ nat \end{aligned}$	fixity declarations for infix identifiers
$target_rep_rhs$::= 	infix fixity_decl backtick_string exp typ special $string exp_1 \dots exp_n$	right hand side of a target representation de

```
target\_rep\_lhs
                              ::=
                                       \begin{array}{l} \mathbf{target\_rep} \ component \ id \ x_1^l \ldots x_n^l \\ \mathbf{target\_rep} \ component \ id \ tnvars^l \end{array}
sort
                              ::=
                                        backtick\_string
sorts\_rhs
                              ::=
                                        sort_1 ... sort_n
declare\_def
                              ::=
                                        declare \tau? compile\_message id = string
                                       \operatorname{declare} \tau^{?}\operatorname{rename\,module}^{-}=x^{l}
                                       \operatorname{declare} \tau^{?} rename component\ id = x^{l}
                                        \mathbf{declare} \, \tau^{?} \, \mathbf{ascii\_rep} \, component \, id = backtick\_string
                                        \mathbf{declare}\ target \mathbf{\_rep}\ target \mathbf{\_rep}\ target \mathbf{\_rep}\ lhs = \ target \mathbf{\_rep}\ rhs
                                        declare target target\_sorts id = sorts\_rhs
                                       \begin{array}{l} \mathbf{declare} \ \mathbf{set\_flag} \ x_1^l = x_2^l \\ \mathbf{declare} \ \tau^? \ \mathbf{termination\_argument} \ id = termination\_setting \end{array}
                                        declare \tau? pattern_match exhaustivity_setting id tnvars^l = [id_1; ...; id_n; ?]elim\_opt
val\_def
                                       let \tau? letbind
                                       let \operatorname{\mathbf{rec}} \tau^? \operatorname{\mathit{funcl}}_1 and ... and \operatorname{\mathit{funcl}}_n
                                       let inline \tau? letbind
                                        let lem_transform \tau? letbind
ascii\_opt
                              ::=
                                        [backtick\_string]
instance\_decl
                              ::=
                                       instance
                                        default_instance
class\_decl
                              ::=
                                        class
                                        class inline
val\_spec
                              ::=
                                        \mathbf{val} \ x^l \ ascii\_opt : typschm
def_aux
                              ::=
                                       type td_1 and ... and td_n
```

```
val\_def
                                                                                                                                                          Valu
                     lemma\_decl
                                                                                                                                                          Lem
                     declare\_def
                                                                                                                                                          a de
                     module x^{l} = struct defs end
                                                                                                                                                          Mod
                     module x^l = id
                                                                                                                                                          Mod
                     open\_import\ id_1\ ...\ id_n
                                                                                                                                                          impo
                     open\_import \ 	au^? \ backtick\_string_1 \dots backtick\_string_n
                                                                                                                                                          impo
                     indreln 	au^{?} indreln\_name_1 and ... and indreln\_name_i rule_1 and ... and rule_n
                                                                                                                                                          Indu
                                                                                                                                                          Top-
                     class\_decl(x^l\ tnvar^l)\ \mathbf{val}\ 	au_1^?\ x_1^l\ ascii\_opt_1: typ_1\ l_1 \dots \mathbf{val}\ 	au_n^?\ x_n^l\ ascii\_opt_n: typ_n\ l_n\ \mathbf{end} instance\_decl\ instschm\ val\_def_1\ l_1 \dots val\_def_n\ l_n\ \mathbf{end}
                                                                                                                                                          Type
                                                                                                                                                          Type
def
                                                                                                                                                      Locatio
             ::=
                     def\_aux\ l
;;?
             ::=
                                                                                                                                                      Option
                     ;;
defs
                                                                                                                                                      Definit
                     def_1; ?_1? ... def_n; ?_n?
                                                                                                                                                      Unique
p
                     x_1 \dots x_n \cdot x
                     _{-}list
                     \_bool
                     __num
                     \_set
                     \_string
                     _{-}unit
                     _{-}bit
                     \_vector
                                                                                                                                                      Type v
                     \{tnv_1 \mapsto t_1 ... tnv_n \mapsto t_n\}
                                                                                                                                                      Interna
t, u
                     t_1 \rightarrow t_2
                     t_1 * \dots * t_n
                     p t\_args
                     ne
                                                                                                                                                Μ
                     \sigma(t)
                                                                                                                                                          Mult
                     \sigma(tnv)
                                                                                                                                                Μ
                                                                                                                                                          Sing
                     \mathbf{curry}(t\_multi, t)
                                                                                                                                                          Curr
                                                                                                                                                Μ
```

ne

::=

interna

```
N
                       nat
                       ne_1 * ne_2
                       ne_1 + ne_2
                       (-ne)
                       normalize(ne)
                                                                              Μ
                                                                              Μ
                       ne_1 + \dots + ne_n
                       bitlength(bin)
                                                                              Μ
                       bitlength (hex)
                                                                              Μ
                       length (pat_1 \dots pat_n)
                                                                              Μ
                       length (exp_1 \dots exp_n)
                                                                              Μ
                                                                                   Lists of types
t\_args
                ::=
                       t_1 \dots t_n
                       \sigma(t\_args)
                                                                              Μ
                                                                                       Multiple substitutions
t_{-}multi
                                                                                   Lists of types
                       (t_1 * .. * t_n)
                       \sigma(t_{-}multi)
                                                                              Μ
                                                                                       Multiple substitutions
                ::=
                                                                                   Numeric expression constraints
nec
                       ne\langle nec
                       ne = nec
                       ne <= nec
                                                                                    Sets of names
names
                       \{x_1,\ldots,x_n\}
                 \mathcal{C}
                                                                                    Typeclass constraint lists
                       (p_1 tnv_1) \dots (p_n tnv_n)
env\_tag
                                                                                    Tags for the (non-constructor) value description
                                                                                       Bound to a method
                       method
                                                                                       Specified with val
                       val
                       let
                                                                                       Defined with let or indreln
v\_desc
                                                                                    Value descriptions
                ::=
                        \langle \mathbf{forall} \ tnvs.t\_multi \rightarrow p, (x \mathbf{of} \ names) \rangle
                                                                                       Constructors
                        \langle \mathbf{forall} \ tnvs.\mathcal{C} \Rightarrow t, env\_tag \rangle
                                                                                       Values
f\_desc
                ::=
                 \langle \mathbf{forall} \ tnvs.p \rightarrow t, (x \mathbf{of} \ names) \rangle
                                                                                       Fields
xs
                ::=
                       x_1 \dots x_n
```

```
\Sigma^{\mathcal{C}}
                                                                                                                                                 Typeclass constraints
                                               \{(p_1 t_1), \dots, (p_n t_n)\}
\Sigma^{\mathcal{C}}_1 \cup \dots \cup \Sigma^{\mathcal{C}}_n
                                                                                                                                      Μ
\Sigma^{\mathcal{N}}
                                                                                                                                                 Nexp constraint lists
                                                \{nec_1, \dots, nec_n\} 
\Sigma^{\mathcal{N}}_1 \cup \dots \cup \Sigma^{\mathcal{N}}_n 
                                                                                                                                      Μ
E
                                                                                                                                                 Environments
                                     \begin{vmatrix} \langle E^{\mathrm{M}}, E^{\mathrm{P}}, E^{\mathrm{F}}, E^{\mathrm{X}} \rangle \\ | E_1 \uplus E_2 \end{vmatrix} 
                                                                                                                                      Μ
                                                                                                                                      Μ
E^{\mathbf{X}}
                                                                                                                                                 Value environments
                                                \left\{ \begin{aligned} & \{x_1 \mapsto v\_desc_1, \, \dots, x_n \mapsto v\_desc_n \} \\ & E_1^{\mathsf{X}} \uplus \, \dots \, \uplus \, E_n^{\mathsf{X}} \end{aligned} \right. 
                                                                                                                                      Μ
E^{\mathrm{F}}
                                                                                                                                                 Field environments
                                               \{x_1 \mapsto f \_desc_1, \dots, x_n \mapsto f \_desc_n\} 
E_1^{\mathsf{F}} \uplus \dots \uplus E_n^{\mathsf{F}} 
                                                                                                                                      Μ
E^{\mathrm{M}}
                                                                                                                                                 Module environments
                                               \{x_1 \mapsto E_1, \dots, x_n \mapsto E_n\}
E^{\mathrm{P}}
                                                                                                                                                 Path environments
                                     | \{x_1 \mapsto p_1, \dots, x_n \mapsto p_n\} 
| E_1^P \uplus \dots \uplus E_n^P 
                                                                                                                                      Μ
E^{\mathrm{L}}
                                                                                                                                                 Lexical bindings
                                    \begin{vmatrix} \{x_1 \mapsto t_1, \dots, x_n \mapsto t_n\} \\ \{x_1^l \mapsto t_1, \dots, x_n^l \mapsto t_n\} \\ E_1^L \uplus \dots \uplus E_n^L \end{vmatrix} 
                                                                                                                                      Μ
tc\_abbrev
                                                                                                                                                 Type abbreviations
tc\_def
                                                                                                                                                 Type and class constructor definitions
                                                tnvs\ tc\_abbrev
                                                                                                                                                       Type constructors
\Delta
                                                                                                                                                 Type constructor definitions
                                                \begin{cases} p_1 \mapsto tc\_def_1, \, \dots, p_n \mapsto tc\_def_n \\ \Delta_1 \uplus \Delta_2 \end{cases} 
                                                                                                                                      Μ
                                                                                                                                                 Typeclass definitions
                                           \{p_1 \mapsto xs_1, \dots, p_n \mapsto xs_n\}\delta_1 \uplus \delta_2
```

Μ

```
A typeclass instance, t must not contain nested types
inst
                   ::=
                          \mathcal{C} \Rightarrow (p \ t)
                    Ι
                                                                    Global instances
                           \{inst_1, ..., inst_n\}
                           I_1 \cup I_2
                                                              Μ
D
                                                                    Global type definition store
                           \langle \Delta, \delta, I \rangle
                           D_1 \uplus D_2
                                                              Μ
                                                              Μ
terminals
                                                                        >=
                                                                        ->
                                                                        <-
                                                                        ==>
                                                                        <|
                                                                        |>
                           \forall
                           \not\in
                           \subset
                           \neq
                           Ø
formula
                           judgement
                           formula_1 .. formula_n
                           E^{\mathrm{M}}(x) \triangleright E
                                                                        Module lookup
```

Path lookup

Field lookup

Value lookup

Lexical binding lookup

Type constructor lookup

Type constructor lookup

 $E^{\mathrm{P}}(x) \triangleright p$

 $E^{\mathrm{L}}(x) \triangleright t$

 $\delta(p) \triangleright xs$

 $E^{\mathrm{F}}(x) \triangleright f_{-}desc$

 $E^{\mathbf{X}}(x) \triangleright v_{-}desc$

 $\Delta(p) \triangleright tc_def$

```
\mathbf{dom}\left(E_{1}^{\mathrm{M}}\right)\,\cap\,\mathbf{dom}\left(E_{2}^{\mathrm{M}}\right)=\,\emptyset
                                                   \mathbf{dom}\left(E_{1}^{\mathbf{X}}\right) \cap \mathbf{dom}\left(E_{2}^{\mathbf{X}}\right) = \emptyset
                                                  \mathbf{dom}\,(E_1^{\mathrm{F}})\cap\,\mathbf{dom}\,(E_2^{\mathrm{F}})=\emptyset
                                                  \mathbf{dom}\,(\overline{E_1^{\mathrm{P}}}) \,\cap\, \mathbf{dom}\,(\overline{E_2^{\mathrm{P}}}) = \emptyset
                                                  disjoint doms (E_1^{\scriptscriptstyle \rm L},\,\ldots,\,E_n^{\scriptscriptstyle \rm L})
                                                                                                                                                         Pairwise disjoint domains
                                                   disjoint doms (E_1^{\mathbf{X}}, \dots, E_n^{\mathbf{X}})
                                                                                                                                                         Pairwise disjoint domains
                                                   compatible overlap (x_1 \mapsto t_1, ..., x_n \mapsto t_n)
                                                                                                                                                         (x_i = x_j) \Longrightarrow (t_i = t_j)
                                                   \mathbf{duplicates}\left(tnvs\right) = \emptyset
                                                   duplicates (x_1, ..., x_n) = \emptyset
                                                   x \not\in \mathbf{dom}(E^{\mathrm{L}})
                                                   x \not\in \mathbf{dom}(E^{X})
                                                   x \not\in \mathbf{dom}(E^{\mathrm{F}})
                                                   p \not\in \mathbf{dom}(\delta)
                                                  p \not\in \mathbf{dom}(\Delta)
                                                   \mathbf{FV}(t) \subset tnvs
                                                                                                                                                         Free type variables
                                                   \mathbf{FV}(t_{-}multi) \subset tnvs
                                                                                                                                                         Free type variables
                                                  \mathbf{FV}\left(\mathcal{C}\right) \subset \mathit{tnvs}
                                                                                                                                                         Free type variables
                                                   inst \ \mathbf{IN} \ I
                                                   (p t) \not\in I
                                                   E_1^{\scriptscriptstyle \rm L}=E_2^{\scriptscriptstyle \rm L}
                                                  E_1^{^{\mathrm{I}}} = E_2^{^{\mathrm{X}}}

E_1^{^{\mathrm{F}}} = E_2^{^{\mathrm{F}}}
                                                   E_1 = E_2
                                                   \Delta_1 = \Delta_2
                                                  \delta_1 = \delta_2
                                                   I_1 = I_2
                                                   names_1 = names_2
                                                   t_1 = t_2
                                                  \sigma_1 = \sigma_2
                                                   p_1 = p_2
                                                  xs_1 = xs_2
                                                   tnvs_1 = tnvs_2
convert\_tnvars
                                                  tnvars^l \leadsto tnvs
                                                  tnvar^l \leadsto tnv
look\_m
                                        ::=
                                                  E_1(x_1^l \dots x_n^l) \triangleright E_2
                                                                                                                                                         Name path lookup
look\_m\_id
                                        ::=
                                                   E_1(id) \triangleright E_2
                                                                                                                                                         Module identifier lookup
look\_tc
                                                   E(id) \triangleright p
                                                                                                                                                         Path identifier lookup
check\_t
                                        ::=
```

```
\Delta \vdash t \mathbf{ok}
                                                                                                                                                                 Well-formed types
                                               \Delta, tnv \vdash t ok
                                                                                                                                                                 Well-formed type/Nexps m
teq
                                    ::=
                                               \Delta \vdash t_1 = t_2
                                                                                                                                                                 Type equality
convert\_typ
                                               \Delta, E \vdash typ \leadsto t
                                                                                                                                                                 Convert source types to int
                                               \vdash Nexp \leadsto ne
                                                                                                                                                                 Convert and normalize num
convert\_typs
                                    ::=
                                               \Delta, E \vdash typs \leadsto t\_multi
check\_lit
                                    ::=
                                              \vdash lit:t
                                                                                                                                                                Typing literal constants
inst\_field
                                    ::=
                                               \Delta, E \vdash field id : p \ t\_args \rightarrow t \triangleright (x \ \textbf{of} \ names)
                                                                                                                                                                 Field typing (also returns c
inst\_ctor
                                    ::=
                                               \Delta, E \vdash \mathbf{ctor} \ id : t\_multi \rightarrow p \ t\_args \triangleright (x \ \mathbf{of} \ names)
                                                                                                                                                                 Data constructor typing (al
inst\_val
                                    ::=
                                               \Delta, E \vdash \mathbf{val} \ id : t \triangleright \Sigma^{\mathcal{C}}
                                                                                                                                                                 Typing top-level bindings, of
not\_ctor
                                    ::=
                                               E, E^{\text{L}} \vdash x \text{ not ctor}
                                                                                                                                                                 v is not bound to a data co
not\_shadowed
                                    ::=
                                               E^{\mathrm{L}} \vdash id \text{ not shadowed}
                                                                                                                                                                 id is not lexically shadowed
check\_pat
                                    ::=
                                              \begin{array}{l} \Delta, E, E_1^{\text{\tiny L}} \vdash pat: t \vartriangleright E_2^{\text{\tiny L}} \\ \Delta, E, E_1^{\text{\tiny L}} \vdash pat\_aux: t \vartriangleright E_2^{\text{\tiny L}} \end{array}
                                                                                                                                                                 Typing patterns, building t
                                                                                                                                                                 Typing patterns, building t
id_{-}field
                                    ::=
                                               E \vdash id \mathbf{field}
                                                                                                                                                                 Check that the identifier is
id\_value
                                    ::=
                                               E \vdash id value
                                                                                                                                                                 Check that the identifier is
check\_exp
                                    ::=
                                               \Delta, E, E^{\mathrm{L}} \vdash exp : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}
                                                                                                                                                                Typing expressions, collecti
                                              \Delta, E, E^{\mathrm{L}} \vdash exp\_aux : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}
                                                                                                                                                                 Typing expressions, collecti
                                              \Delta, E, E_1^{\text{L}} \vdash qbind_1 ... qbind_n \triangleright E_2^{\text{L}}, \Sigma^{\mathcal{C}}
\Delta, E, E_1^{\text{L}} \vdash \textbf{list} qbind_1 ... qbind_n \triangleright E_2^{\text{L}}, \Sigma^{\mathcal{C}}
\Delta, E, E^{\text{L}} \vdash funcl \triangleright \{x \mapsto t\}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}
```

Build the environment for o Build the environment for o Build the environment for a

		$\Delta, E, E_1^{\text{L}} \vdash letbind \triangleright E_2^{\text{L}}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}$	Build the environment for a let bin
$check_rule$::=	$\Delta, E, E^{L} \vdash rule \triangleright \{x \mapsto t\}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}$	Build the environment for an induc
$check_texp_tc$::=	$xs, \Delta_1, E \vdash \mathbf{tc} \ td \triangleright \Delta_2, E^{\mathrm{P}}$	Extract the type constructor inform
$check_texps_tc$::= 	$xs, \Delta_1, E \vdash \mathbf{tc} \ td_1 td_i \rhd \Delta_2, E^{\mathrm{P}}$	Extract the type constructor inform
$check_texp$::=	$\Delta, E \vdash tnvs \ p = texp \triangleright \langle E^{\scriptscriptstyle F}, E^{\scriptscriptstyle X} \rangle$	Check a type definition, with its pa
$check_texps$::=	$xs, \Delta, E \vdash td_1 td_n \rhd \langle E^{\scriptscriptstyle F}, E^{\scriptscriptstyle X} \rangle$	
$convert_class$::=	$\delta, E \vdash id \leadsto p$	Lookup a type class
$solve_class_constraint$::=	$I \vdash (p\ t) \mathbf{IN} \mathcal{C}$	Solve class constraint
$solve_class_constraints$::=	$I \vdash \Sigma^{\mathcal{C}} \triangleright \mathcal{C}$	Solve class constraints
$check_val_def$::=	$\Delta, I, E \vdash val_def \rhd E^{\mathbf{X}}$	Check a value definition
$check_t_instance$::=	$\Delta, (\alpha_1,, \alpha_n) \vdash t$ instance	Check that t be a typeclass instance
$check_defs$::= 	$\overline{z_j}^j, D_1, E_1 \vdash def \rhd D_2, E_2$ $\overline{z_j}^j, D_1, E_1 \vdash defs \rhd D_2, E_2$	Check a definition Check definitions, given module pa
judgement	::=	$convert_tnvars$ $look_m$ $look_m_id$ $look_tc$ $check_t$	

teq

 $convert_typ$

 $convert_typs$ $check_lit$

 $inst_field$

```
inst\_ctor
      inst\_val
      not\_ctor
      not\_shadowed
      check\_pat
      id\_field
      id\_value
      check\_exp
      check\_rule
      check\_texp\_tc
      check\_texps\_tc
      check\_texp
      check\_texps
      convert\_class
      solve\_class\_constraint
      solve\_class\_constraints
      check\_val\_def
      check\_t\_instance
      check\_defs
::=
      n
      num
      nat
      hex
      bin
      string
```

 $user_syntax$

 $backtick_string$ regexp \boldsymbol{x} ix ix^l α α^l N N^l idtnv $tnvar^l$ tnvs $tnvars^l$ $Nexp_aux$ Nexp

 $Nexp_constraint_aux$

```
Nexp\_constraint
typ\_aux
typ
lit\_aux
lit
;?
pat\_aux
pat
fpat
exp\_aux
exp
q
qbind
fexp
fexps
pexp
psexp
tannot?
funcl\_aux
letbind\_aux
letbind
funcl
name\_t
name\_ts
rule\_aux
rule
witness? check?
functions?
indreln\_name\_aux
indreln\_name
typs
ctor\_def
texp
name?
td
c
cs
c\_pre
typschm
instschm
target
open\_import
	au^?
```

```
lemma\_typ
lemma\_decl
dexp
declare\_arg
component
termination\_setting
exhaustivity\_setting
elim\_opt
fixity\_decl
target\_rep\_rhs
target\_rep\_lhs
sort
sorts\_rhs
declare\_def
val\_def
ascii\_opt
instance\_decl
class\_decl
val\_spec
def\_aux
_{;;?}^{\mathit{def}}
defs
p
\sigma
t
ne
t\_args
t\_multi
nec
names
env\_tag
v\_desc
f\_desc
xs
\Sigma^{\mathcal{C}}
\Sigma^{\mathcal{N}}
E
E^{\mathbf{X}}
E^{\scriptscriptstyle \mathrm{F}}
E^{\mathrm{M}}
E^{\mathrm{P}}
E^{\scriptscriptstyle 
m L}
tc\_abbrev
tc\_def
```

$$\begin{array}{c|c} & \Delta \\ & \delta \\ & inst \\ & I \\ & D \\ & terminals \\ & formula \end{array}$$

 $tnvars^l \leadsto tnvs$

$$\frac{tnvar_1^l \leadsto tnv_1 \quad .. \quad tnvar_n^l \leadsto tnv_n}{tnvar_1^l .. tnvar_n^l \leadsto tnv_1 .. tnv_n} \quad \text{CONVERT_TNVARS_NONE}$$

 $tnvar^l \leadsto tnv$

$$\frac{\overline{\alpha \ l \leadsto \alpha}}{N \ l \leadsto N} \quad \begin{array}{ll} \text{Convert_tnvar_a} \\ \\ \hline \end{array}$$

 $E_1(x_1^l ... x_n^l) \triangleright E_2$ Name path lookup

$$\frac{E(\) \rhd E \quad \text{LOOK_M_NONE}}{E^{\text{M}}(x) \rhd E_{1}}$$

$$\frac{E_{1}(\ \overline{y_{i}^{l}}^{i}\) \rhd E_{2}}{\langle E^{\text{M}}, E^{\text{P}}, E^{\text{F}}, E^{\text{X}} \rangle (x \ l \ \overline{y_{i}^{l}}^{i}\) \rhd E_{2}} \quad \text{LOOK_M_SOME}$$

 $E_1(id) \triangleright E_2$ Module identifier lookup

$$\frac{E_1(\overline{y_i^l}^i x l_1) \triangleright E_2}{E_1(\overline{y_i^l}^i x l_1 l_2) \triangleright E_2} \quad \text{LOOK_M_ID_ALL}$$

 $|E(id) \triangleright p|$ Path identifier lookup

$$\frac{E(\overline{y_{i}^{l}}^{i}) \triangleright \langle E^{\mathrm{M}}, E^{\mathrm{P}}, E^{\mathrm{F}}, E^{\mathrm{X}} \rangle}{E(\overline{y_{i}^{l}}^{i} x \ l_{1} \ l_{2}) \triangleright p} \quad \text{LOOK_TC_ALL}$$

 $\Delta \vdash t \text{ ok}$ Well-formed types

$$\begin{array}{c|c} \overline{\Delta \vdash \alpha \, \mathbf{ok}} & \text{CHECK_T_VAR} \\ \hline \Delta \vdash t_1 \, \mathbf{ok} \\ \hline \Delta \vdash t_2 \, \mathbf{ok} \\ \hline \Delta \vdash t_1 \to t_2 \, \mathbf{ok} \end{array} \quad \text{CHECK_T_FN} \\ \hline \\ \frac{\Delta \vdash t_1 \, \mathbf{ok} \quad \quad \Delta \vdash t_n \, \mathbf{ok}}{\Delta \vdash t_1 * * t_n \, \mathbf{ok}} \quad \text{CHECK_T_TUP} \\ \hline \\ \frac{\Delta(p) \rhd tnv_1 ...tnv_n \, tc_abbrev}{\Delta, tnv_1 \vdash t_1 \, \mathbf{ok} \quad ... \quad \Delta, tnv_n \vdash t_n \, \mathbf{ok}} \\ \hline \Delta \vdash p \, t_1 ... t_n \, \mathbf{ok} \end{array} \quad \text{CHECK_T_APP}$$

 $\Delta, tnv \vdash t$ ok Well-formed type/Nexps matching the application type variable

$$\frac{\Delta \vdash t \, \mathbf{ok}}{\Delta, \alpha \vdash t \, \mathbf{ok}} \quad \text{CHECK_TLEN_T}$$

$$\overline{\Delta, N \vdash ne \, \mathbf{ok}} \quad \text{CHECK_TLEN_LEN}$$

 $\Delta \vdash t_1 = t_2$ Type equality

$$\frac{\Delta \vdash t \text{ ok}}{\Delta \vdash t = t} \quad \text{TEQ_REFL}$$

$$\frac{\Delta \vdash t_2 = t_1}{\Delta \vdash t_1 = t_2} \quad \text{TEQ_SYM}$$

$$\frac{\Delta \vdash t_1 = t_2}{\Delta \vdash t_2 = t_3} \quad \text{TEQ_TRANS}$$

$$\frac{\Delta \vdash t_1 = t_3}{\Delta \vdash t_1 = t_3} \quad \text{TEQ_ARROW}$$

$$\frac{\Delta \vdash t_1 = t_3}{\Delta \vdash t_1 \to t_2 = t_3 \to t_4} \quad \text{TEQ_ARROW}$$

$$\frac{\Delta \vdash t_1 = u_1 \quad \dots \quad \Delta \vdash t_n = u_n}{\Delta \vdash t_1 * \dots * t_n = u_1 * \dots * u_n} \quad \text{TEQ_TUP}$$

$$\frac{\Delta(p) \rhd \alpha_1 \dots \alpha_n}{\Delta \vdash t_1 = u_1 \quad \dots \quad \Delta \vdash t_n = u_n} \quad \text{TEQ_APP}$$

$$\frac{\Delta(p) \rhd \alpha_1 \dots \alpha_n \dots \alpha_n}{\Delta \vdash p t_1 \dots t_n = p u_1 \dots u_n} \quad \text{TEQ_APP}$$

$$\frac{\Delta(p) \rhd \alpha_1 \dots \alpha_n \dots u}{\Delta \vdash p t_1 \dots t_n = \{\alpha_1 \mapsto t_1 \dots \alpha_n \mapsto t_n\}(u)} \quad \text{TEQ_EXPAND}$$

$$\frac{ne = \text{normalize}(ne')}{\Delta \vdash ne = ne'} \quad \text{TEQ_NEXP}$$

 $\Delta, E \vdash typ \leadsto t$ Convert source types to internal types

$$\begin{array}{c} \Delta, E \vdash typ \leadsto t_1 \\ \Delta \vdash t_1 = t_2 \\ \Delta, E \vdash typ \leadsto t_2 \end{array} \\ \hline \Delta, E \vdash typ \leadsto t_2 \\ \hline - Nexp \leadsto ne \\ \hline - Nexp \leadsto ne_2 \\ \hline + Nexp_1 \leadsto ne_1 \\ \hline - Nexp_1 \leadsto ne_2 \\ \hline - Nexp_1 \leadsto ne_1 \\ \hline - Nexp_2 \leadsto ne_2 \\ \hline - 1 Nexp_1 \leadsto ne_1 \\ \hline - Nexp_2 \leadsto ne_2 \\ \hline - 1 Nexp_1 \leadsto ne_1 \\ \hline - Nexp_2 \leadsto ne_2 \\ \hline - 1 Nexp_1 \leadsto ne_1 \\ \hline - Nexp_2 \leadsto ne_2 \\ \hline - 1 Nexp_1 \leadsto ne_1 \\ \hline - Nexp_2 \leadsto ne_2 \\ \hline - 1 Nexp_1 \leadsto ne_1 \\ \hline - 1 Nexp_1 \leadsto ne_$$

 $\Delta, E \vdash \mathbf{ctor}\ id : t_multi \rightarrow p\ t_args \triangleright (x\ \mathbf{of}\ names)$

Data constructor typing (also returns canonical constru

```
\begin{array}{l} E(\,\overline{x_i^l}^{\,i}\,) \,\rhd\, \langle E^{\scriptscriptstyle{\mathrm{M}}}, E^{\scriptscriptstyle{\mathrm{P}}}, E^{\scriptscriptstyle{\mathrm{F}}}, E^{\scriptscriptstyle{\mathrm{X}}} \rangle \\ E^{\scriptscriptstyle{\mathrm{X}}}(y) \,\rhd\, \langle\, \mathbf{forall}\, tnv_1 \mathinner{\ldotp\ldotp} tnv_n.t\_multi \,\to\, p, (z\,\mathbf{of}\,\, names) \rangle \end{array}
                                         \Delta \vdash t_1 \mathbf{ok} \quad ... \quad \Delta \vdash t_n \mathbf{ok}
                                                                                                                                                                                                                                    — INST_CTOR_ALL
\overline{\Delta, E \vdash \mathbf{ctor} \, \overline{x_i^l}^i} \, y \, l_1 \, l_2 : \{tnv_1 \mapsto t_1 \dots tnv_n \mapsto t_n\}(t\_multi) \to p \, t_1 \dots t_n \rhd (z \, \mathbf{of} \, names)
     \Delta, E \vdash \mathbf{val} \ id : t \triangleright \Sigma^{\mathcal{C}} Typing top-level bindings, collecting typeclass constraints
                              E(\overline{x_i^l}^i) \rhd \langle E^{\mathrm{M}}, E^{\mathrm{P}}, E^{\mathrm{F}}, E^{\mathrm{X}} \rangle 
E^{\mathrm{X}}(y) \rhd \langle \mathbf{forall} \ tnv_1 \dots tnv_n. (p_1 \ tnv_1') \dots (p_i \ tnv_i') \Rightarrow t, \ env\_tag \rangle
                               \Delta \vdash t_1 \mathbf{ok} \quad \dots \quad \Delta \vdash t_n \mathbf{ok}
                             \sigma = \{ \underbrace{t_n v_1 \mapsto t_1 \dots t_n \mapsto t_n} \}
                               \frac{\sigma = \{tnv_1 \mapsto t_1 .. tnv_n \mapsto t_n\}}{\Delta, E \vdash \mathbf{val} \, \overline{x_i^l}^{\ i} \, y \, l_1 \, l_2 : \sigma(t) \triangleright \{(p_1 \, \sigma(tnv_1')), ..., (p_i \, \sigma(tnv_1'))\}}  INST_VAL_ALL
     E, E^{\mathsf{L}} \vdash x \, \mathbf{not} \, \mathbf{ctor} \, | \, v \, \text{is not bound to a data constructor}
                                                                                        \frac{E^{\text{L}}(x) \vartriangleright t}{E.\,E^{\text{L}} \vdash x \, \mathbf{not} \, \mathbf{ctor}} \quad \text{Not\_ctor\_val}
                                                          \frac{x \not\in \mathbf{dom}\left(E^{\mathbf{X}}\right)}{\langle E^{\mathbf{M}}, E^{\mathbf{P}}, E^{\mathbf{F}}, E^{\mathbf{X}}\rangle, E^{\mathbf{L}} \vdash x \, \mathbf{not} \, \mathbf{ctor}} \quad \text{NOT\_CTOR\_UNBOUND}
                       \frac{E^{\mathbf{X}}(x) \triangleright \langle \mathbf{forall} \ tnv_{1} ... \ tnv_{n}.(p_{1} \ tnv_{1}') ... (p_{i} \ tnv_{i}') \Rightarrow t, env\_tag \rangle}{\langle E^{\mathbf{M}}, E^{\mathbf{P}}, E^{\mathbf{F}}, E^{\mathbf{X}} \rangle, E^{\mathbf{L}} \vdash x \ \mathbf{not} \ \mathbf{ctor}}  NOT_CTOR_BOUND
     E^{\text{L}} \vdash id \text{ not shadowed}
                                                                              id is not lexically shadowed
                                                                  \frac{x \not\in \mathbf{dom}(E^{L})}{E^{L} \vdash x \ l_{1} \ l_{2} \ \mathbf{not \ shadowed}} \quad \text{NOT\_SHADOWED\_SING}
                                                    \overline{E^{\text{L}} \vdash x_1^l \dots x_n^l. y^l. z^l \ l \ \textbf{not shadowed}} \quad \text{NOT\_SHADOWED\_MULTI}
     \Delta, E, E_1^{\text{L}} \vdash pat : t \triangleright E_2^{\text{L}} Typing patterns, building their binding environment
                                                                       \frac{\Delta, E, E_1^{\text{L}} \vdash pat\_aux : t \triangleright E_2^{\text{L}}}{\Delta, E, E_1^{\text{L}} \vdash pat\_aux \ l : t \triangleright E_2^{\text{L}}} \quad \text{CHECK\_PAT\_ALL}
   \Delta, E, E_1^{\mathrm{L}} \vdash pat\_aux : t \triangleright E_2^{\mathrm{L}}
                                                                                             Typing patterns, building their binding environment
                                                                           \frac{\Delta \vdash t \text{ ok}}{\Delta, E, E^{\text{L}} \vdash \_: t \vartriangleright \{\,\}} \quad \text{CHECK\_PAT\_AUX\_WILD}
                                                \begin{array}{c} \Delta, E, E_1^{\text{\tiny L}} \vdash pat : t \vartriangleright E_2^{\text{\tiny L}} \\ x \not\in \mathbf{dom}\,(E_2^{\text{\tiny L}}) \\ \overline{\Delta, E, E_1^{\text{\tiny L}} \vdash (pat \ \mathbf{as} \ x \ l) : t \vartriangleright E_2^{\text{\tiny L}} \uplus \{x \mapsto t\}} \end{array} \quad \text{CHECK\_PAT\_AUX\_AS}
                                                              \begin{split} & \Delta, E, E_1^{\text{L}} \vdash pat: t \vartriangleright E_2^{\text{L}} \\ & \frac{\Delta, E \vdash typ \leadsto t}{\Delta, E, E_1^{\text{L}} \vdash (pat: typ): t \vartriangleright E_2^{\text{L}}} & \text{CHECK\_PAT\_AUX\_TYP} \end{split}
          \Delta, E \vdash \mathbf{ctor}\ id : (t_1 * ... * t_n) \rightarrow p\ t\_args \triangleright (x\ \mathbf{of}\ names)
           E^{\text{L}} \vdash id \text{ not shadowed}
          \Delta, E, E^{\scriptscriptstyle L} \vdash pat_1: t_1 \, \rhd \, E_1^{\scriptscriptstyle L} \quad .. \quad \Delta, E, E^{\scriptscriptstyle L} \vdash pat_n: t_n \, \rhd \, E_n^{\scriptscriptstyle L}
          disjoint doms (E_1^{\text{L}}, ..., E_n^{\text{L}})
                    \Delta, E, E^{\text{L}} \vdash id \ pat_1 ... pat_n : p \ t\_args \triangleright E_1^{\text{L}} \uplus ... \uplus E_n^{\text{L}}  CHECK_PAT_AUX_IDENT_CONSTR
```

```
\Delta \vdash t \mathbf{ok}
                                                             \frac{E, E^{\text{L}} \vdash x \text{ not ctor}}{\Delta, E, E^{\text{L}} \vdash x \ l_1 \ l_2 \ : t \rhd \{x \mapsto t\}} \quad \text{CHECK\_PAT\_AUX\_VAR}
                              \overline{\Delta, E \vdash \mathbf{field}\ id_i : p\ t\_args \rightarrow t_i \triangleright (x_i \ \mathbf{of}\ names)}^i
                              \Delta, E, E^{\mathrm{L}} \vdash pat_i : t_i \triangleright E_i^{\mathrm{L}}^i
                             \begin{array}{l} \operatorname{disjoint \, doms} \left( \, \overline{E_i^{\scriptscriptstyle \mathrm{L}}}^{\, i} \, \right) \\ \operatorname{duplicates} \left( \, \overline{x_i}^{\, i} \, \right) = \, \emptyset \end{array}
                              \frac{1}{\Delta,E,E^{\text{\tiny L}} \vdash \langle | \ \overline{id_i = pat_i \ l_i}^i \ ;^?| \rangle : p \ t\_args \ \rhd \ \uplus \ \overline{E_i^{\text{\tiny L}}}^i} \quad \text{CHECK\_PAT\_AUX\_RECORD}
                    \Delta, E, E^{\mathrm{L}} \vdash \mathit{pat}_1 : t \, \rhd \, E_1^{\mathrm{L}} \quad \dots \quad \Delta, E, E^{\mathrm{L}} \vdash \mathit{pat}_n : t \, \rhd \, E_n^{\mathrm{L}}
                    disjoint doms (E_1^L, \ldots, E_n^L)
                    \mathbf{length}\left(pat_1 \dots pat_n\right) = nat
          \overline{\Delta, E, E^{\text{L}} \vdash [|pat_1; \dots; pat_n;^?|]} : \_\text{vector } nat \ t \vartriangleright E_1^{\text{L}} \uplus \dots \uplus E_n^{\text{L}} \quad \text{CHECK\_PAT\_AUX\_VECTOR}
\Delta, E, E^{\text{\tiny L}} \vdash \textit{pat}_1: \_\textbf{vector} \; \textit{ne}_1 \; t \, \rhd \, E^{\text{\tiny L}}_1 \quad \dots \quad \Delta, E, E^{\text{\tiny L}} \vdash \textit{pat}_n: \_\textbf{vector} \; \textit{ne}_n \; t \, \rhd \, E^{\text{\tiny L}}_n
\mathbf{disjoint}\,\mathbf{doms}\,(E_1^{\scriptscriptstyle{\mathrm{L}}},\,\dots,E_n^{\scriptscriptstyle{\mathrm{L}}})
ne' = ne_1 + \dots + ne_n
                                                                                                                                                                                                                                                               CHECK_PAT_AUX_VECTOR
                                   \Delta, E, E^{\text{L}} \vdash [|pat_1 \dots pat_n|] : \_\text{vector } ne' \ t \triangleright E_1^{\text{L}} \uplus \dots \uplus E_n^{\text{L}}
                      \Delta, E, E^{\mathrm{L}} \vdash \mathit{pat}_1 : t_1 \mathrel{\vartriangleright} E_1^{\mathrm{L}} \quad .... \quad \Delta, E, E^{\mathrm{L}} \vdash \mathit{pat}_n : t_n \mathrel{\vartriangleright} E_n^{\mathrm{L}}
                      \mathbf{disjoint}\,\mathbf{doms}\,(E_1^{\scriptscriptstyle{\mathrm{L}}},\,\ldots,E_n^{\scriptscriptstyle{\mathrm{L}}})
                      \frac{\Delta, E, E^{\text{L}} \vdash (pat_1, \dots, pat_n)}{\Delta, E, E^{\text{L}} \vdash (pat_1, \dots, pat_n) : t_1 * \dots * t_n \triangleright E_1^{\text{L}} \uplus \dots \uplus E_n^{\text{L}}} \quad \text{CHECK\_PAT\_AUX\_TUP}
                           \Delta, E, E^{\mathsf{L}} \vdash \mathit{pat}_1 : t \, \rhd \, E_1^{\mathsf{L}} \quad \dots \quad \Delta, E, E^{\mathsf{L}} \vdash \mathit{pat}_n : t \, \rhd \, E_n^{\mathsf{L}}
                           disjoint doms (E_1^{\scriptscriptstyle \rm L},\,..\,,E_n^{\scriptscriptstyle \rm L})
                               \Delta, \overline{E, E^{\text{\tiny L}} \vdash [pat_1; \ ..; pat_n \ ;^?] : \_\textbf{list} \ t \vartriangleright E_1^{\text{\tiny L}} \uplus \ .. \uplus E_n^{\text{\tiny L}}} \quad \text{CHECK\_PAT\_AUX\_LIST}
                                                                  \frac{\Delta, E, E_1^{\text{L}} \vdash pat : t \triangleright E_2^{\text{L}}}{\Delta, E, E_1^{\text{L}} \vdash (pat) : t \triangleright E_2^{\text{L}}} \quad \text{CHECK\_PAT\_AUX\_PAREN}
                                                             \begin{array}{l} \Delta, E, E_1^{\text{L}} \vdash pat_1 : t \vartriangleright E_2^{\text{L}} \\ \Delta, E, E_1^{\text{L}} \vdash pat_2 : \_\_\textbf{list} \ t \vartriangleright E_3^{\text{L}} \end{array}
                                            \frac{\mathbf{disjoint\,doms}\,(E_2^{\mathrm{L}},E_3^{\mathrm{L}})}{\Delta,E,E_1^{\mathrm{L}}\vdash\mathit{pat}_1::\mathit{pat}_2:\_\mathbf{list}\;t\,\vartriangleright\,E_2^{\mathrm{L}}\uplus E_3^{\mathrm{L}}}
                                                                                                                                                                            CHECK_PAT_AUX_CONS
                                                                            \frac{\vdash lit:t}{\Delta,E,E^{\text{L}}\vdash lit:t\,\vartriangleright\,\{\,\}} \quad \text{CHECK\_PAT\_AUX\_LIT}
                                                                       E, E^{\text{\tiny L}} \vdash x \text{ not ctor}
                                                                                                                                                                                     CHECK\_PAT\_AUX\_NUM\_ADD
                           \overline{\Delta, E, E^{\text{L}} \vdash x \ l + num : \_\text{num} \ \triangleright \{x \mapsto \_\text{num} \ \}}
  E \vdash id \mathbf{field}
                                                  Check that the identifier is a permissible field identifier
                                                                     \frac{E^{\mathrm{F}}(x) \triangleright f\_desc}{\langle E^{\mathrm{M}}, E^{\mathrm{P}}, E^{\mathrm{F}}, E^{\mathrm{X}} \rangle \vdash x \ l_1 \ l_2 \ \mathbf{field}} \quad \text{ID\_FIELD\_EMPTY}
                                                                                            E^{\mathrm{M}}(x) \triangleright E
                                                                                           x \not\in \mathbf{dom}(E^{\mathrm{F}})
                                                              \frac{E \vdash \overline{y_{i}^{l}}.^{i} z^{l} \ l_{2} \, \mathbf{field}}{\langle E^{\text{\tiny{M}}}, E^{\text{\tiny{P}}}, E^{\text{\tiny{F}}}, E^{\text{\tiny{X}}} \rangle \vdash x \ l_{1}. \, \overline{y_{i}^{l}}.^{i} z^{l} \ l_{2} \, \mathbf{field}} \quad \text{id_{FIELD\_CONS}}
```

 $E \vdash id$ value Check that the identifier is a permissible value identifier

```
\frac{E^{\mathbf{X}}(x) \vartriangleright v\_desc}{\langle E^{\mathbf{M}}, E^{\mathbf{P}}, E^{\mathbf{F}}, E^{\mathbf{X}} \rangle \vdash x \ l_1 \ l_2 \ \mathbf{value}} \quad \text{ID\_VALUE\_EMPTY}
                                                                                                 E^{\mathrm{M}}(x) \triangleright E
                                                                                                x \not\in \mathbf{dom}(E^{X})
                                                                  \frac{E \vdash \overline{y_i^l}.^i \ z^l \ l_2 \, \mathbf{value}}{\langle E^{\text{\tiny M}}, E^{\text{\tiny P}}, E^{\text{\tiny F}}, E^{\text{\tiny X}} \rangle \vdash x \ l_1. \ \overline{y_i^l}.^i \ z^l \ l_2 \, \mathbf{value}} \quad \text{id\_value\_cons}
       \Delta, E, E^{\mathrm{L}} \vdash exp : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}
                                                                                                          Typing expressions, collecting typeclass and index constraints
                                                                       \frac{\Delta, E, E^{\mathsf{L}} \vdash exp\_aux : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}}{\Delta, E, E^{\mathsf{L}} \vdash exp\_aux \ l : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}} \quad \text{CHECK\_EXP\_ALL}
   \Delta, E, E^{\mathsf{L}} \vdash exp\_aux : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}
                                                                                                                 Typing expressions, collecting typeclass and index constraints
                                                                      \frac{E^{\text{L}}(x) \triangleright t}{\Delta, E, E^{\text{L}} \vdash x \ l_1 \ l_2 : t \triangleright \{\}, \{\}} \quad \text{CHECK\_EXP\_AUX\_VAR}
                                                                \overline{\Delta, E, E^{\perp} \vdash N : \_\mathbf{num} \triangleright \{\}, \{\}}
                                                                                                                                                                         CHECK_EXP_AUX_NVAR
                                  E^{\mathrm{L}} \vdash id \text{ not shadowed}
                                  E \vdash id \text{ value}
                                  \Delta, E \vdash \mathbf{ctor} id : t\_multi \to p \ t\_args \rhd (x \ \mathbf{of} \ names)
                                                                                                                                                                                                               CHECK_EXP_AUX_CTOR
                                     \Delta, E, E^{\text{\tiny L}} \vdash id : \mathbf{curry} (t\_multi, p \ t\_args) \rhd \{\}, \{\}
                                                                                 E^{\mathsf{L}} \vdash id \text{ not shadowed}
                                                                                 E \vdash id value
                                                                            \frac{\Delta, E \vdash \mathbf{val} \, id : t \triangleright \Sigma^{\mathcal{C}}}{\Delta, E, E^{\mathsf{L}} \vdash id : t \triangleright \Sigma^{\mathcal{C}}, \{\}} \quad \text{CHECK\_EXP\_AUX\_VAL}
                              \begin{array}{lll} \Delta, E, E^{\mathrm{L}} \vdash pat_{1} : t_{1} \rhd E_{1}^{\mathrm{L}} & \dots & \Delta, E, E^{\mathrm{L}} \vdash pat_{n} : t_{n} \rhd E_{n}^{\mathrm{L}} \\ \Delta, E, E^{\mathrm{L}} \uplus E_{1}^{\mathrm{L}} \uplus & \dots & \uplus E_{n}^{\mathrm{L}} \vdash exp : u \rhd \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}} \end{array}
                              \mathbf{disjoint}\,\mathbf{doms}\,(E_1^{\scriptscriptstyle{\mathrm{L}}},\,\dots,E_n^{\scriptscriptstyle{\mathrm{L}}})
                                                                                                                                                                                                                                              CHECK_EXP_AUX_FN
        \overline{\Delta, E, E^{\text{L}} \vdash \mathbf{fun} \ pat_{1} \dots pat_{n} \rightarrow exp \ l : \mathbf{curry} \left( (t_{1} * \dots * t_{n}), u \right) \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}}
                                               \frac{\overline{\Delta}, E, E^{\text{\tiny L}} \vdash \textit{pat}_i : t \vartriangleright E_i^{\text{\tiny L}}{}^i}{\overline{\Delta}, E, E^{\text{\tiny L}} \uplus E_i^{\text{\tiny L}} \vdash \textit{exp}_i : u \vartriangleright \Sigma^{\mathcal{C}}{}_i, \Sigma^{\mathcal{N}}{}_i{}^i}
      \Delta, E, E^{\text{\tiny L}} \vdash \mathbf{function} \mid^{?} \overline{pat_{i} \rightarrow exp_{i} \, l_{i}}^{i} \, \mathbf{end} : t \rightarrow u \, \triangleright \, \overline{\Sigma^{\mathcal{C}_{i}}}^{i} \, . \, \overline{\Sigma^{\mathcal{N}_{i}}}^{i}
                                                          \begin{array}{l} \Delta, E, E^{\text{\tiny L}} \vdash exp_1 : t_1 \rightarrow t_2 \rhd \Sigma^{\mathcal{C}}_{1}, \Sigma^{\mathcal{N}}_{1} \\ \Delta, E, E^{\text{\tiny L}} \vdash exp_2 : t_1 \rhd \Sigma^{\mathcal{C}}_{2}, \Sigma^{\mathcal{N}}_{2} \end{array}
                                    \frac{1}{\Delta,E,E^{\text{L}} \vdash exp_1 \; exp_2 : t_2 \, \triangleright \, \Sigma^{\mathcal{C}}_1 \, \cup \, \Sigma^{\mathcal{C}}_2, \Sigma^{\mathcal{N}}_1 \, \cup \, \Sigma^{\mathcal{N}}_2} \quad \text{Check_exp_aux_app}
                                          \begin{array}{l} \Delta, E, E^{\mathrm{L}} \vdash (\mathit{ix}) \, : t_1 \to t_2 \to t_3 \rhd \Sigma^{\mathcal{C}}_1, \Sigma^{\mathcal{N}}_1 \\ \Delta, E, E^{\mathrm{L}} \vdash \mathit{exp}_1 : t_1 \rhd \Sigma^{\mathcal{C}}_2, \Sigma^{\mathcal{N}}_2 \end{array}
                                           \Delta, E, E^{\mathsf{L}} \vdash exp_2 : t_2 \rhd \Sigma^{\mathcal{C}}_3, \Sigma^{\mathcal{N}}_3
\frac{1}{\Delta,E,E^{\text{L}} \vdash exp_1 \ ix \ l \ exp_2 : t_3 \rhd \Sigma^{\mathcal{C}}_1 \ \cup \ \Sigma^{\mathcal{C}}_2 \ \cup \ \Sigma^{\mathcal{C}}_3, \Sigma^{\mathcal{N}}_1 \ \cup \ \Sigma^{\mathcal{N}}_2 \ \cup \ \Sigma^{\mathcal{N}}_3} \quad \text{Check_exp_aux_infix_app1}
                                                                                                                                                                       \begin{array}{lll} \Delta, E, E^{\text{\tiny L}} \vdash & x & : t_1 \rightarrow t_2 \rightarrow t_3 \rhd \Sigma^{\mathcal{C}}_1, \Sigma^{\mathcal{N}}_1 \\ \Delta, E, E^{\text{\tiny L}} \vdash & exp_1 : t_1 \rhd \Sigma^{\mathcal{C}}_2, \Sigma^{\mathcal{N}}_2 \end{array}
                                                                                                                                                                       \Delta, E, E^{\mathsf{L}} \vdash exp_2 : t_2 \triangleright \Sigma^{\mathcal{C}}_3, \Sigma^{\mathcal{N}}_3
 <<no parses (char 18): TD,E,E_l |- exp1 '***x' l exp2 : t3 gives S_c1 union S_c2 union S_c3,</pre>
```

```
\overline{\Delta}, E \vdash \mathbf{field}\ id_i : p\ t\_args \rightarrow t_i \triangleright (x_i \ \mathbf{of}\ names)^i
                                  \overline{\Delta, E, E^{\text{L}} \vdash exp_i : t_i \triangleright \Sigma^{\mathcal{C}}_i, \Sigma^{\mathcal{N}}_i}
                                  \operatorname{duplicates}(\overline{x_i}^i) = \emptyset
                                  names = \{ \overline{x_i}^i \}
                                                                                                                                                                                                   CHECK_EXP_AUX_RECORD
                        \Delta, E, E^{\text{\tiny L}} \vdash \langle | \overline{id_i = exp_i} \, \overline{l_i}^{\; i} \, ; ^? \, l | \rangle : p \; t\_args \, \triangleright \, \overline{\Sigma^{\mathcal{C}}_i}^{\; i} , \overline{\Sigma^{\mathcal{N}_i}}^{\; i}
                                              \overline{\Delta, E \vdash \mathbf{field}\ id_i : p\ t\_args \rightarrow t_i \triangleright (x_i \ \mathbf{of}\ names)}^i
                                              \overline{\Delta, E, E^{\text{L}} \vdash exp_i : t_i \triangleright \Sigma^{\mathcal{C}}_i, \Sigma^{\mathcal{N}}_i}
                                              \mathbf{duplicates} \, (\, \overline{x_i}^{\, i} \, ) = \, \emptyset
                                              \Delta, E, E^{L} \vdash exp : p \ t\_args \triangleright \Sigma^{C'}, \Sigma^{N'}
\Delta, E, E^{\text{L}} \vdash \langle | exp \ \overline{\textbf{with}} \ \overline{id_i = exp_i \ l_i}^i ; ^? \ l | \rangle : p \ t\_args \rhd \Sigma^{\mathcal{C}'} \cup \ \overline{\Sigma^{\mathcal{C}}_i}^i , \Sigma^{\mathcal{N}'} \cup \ \overline{\Sigma^{\mathcal{N}}_i}^i  CHECK_EXP_AUX_RECUP
                       \Delta, E, E^{\mathsf{L}} \vdash exp_1 : t \triangleright \Sigma^{\mathcal{C}}_1, \Sigma^{\mathcal{N}}_1 \quad \dots \quad \Delta, E, E^{\mathsf{L}} \vdash exp_n : t \triangleright \Sigma^{\mathcal{C}}_n, \Sigma^{\mathcal{N}}_n
                       length(exp_1 ... exp_n) = nat
\frac{\Delta, E, E^{\text{L}} \vdash [|exp_1; \dots; exp_n;^?|] : \_\textbf{vector} \ nat \ t \vartriangleright \Sigma^{\mathcal{C}}_1 \cup \dots \cup \Sigma^{\mathcal{C}}_n, \Sigma^{\mathcal{N}}_1 \cup \dots \cup \Sigma^{\mathcal{N}}_n} \quad \text{CHECK\_EXP\_AUX\_VECTOR}}{}
                                       \Delta, E, E^{L} \vdash exp : \_vector ne' t \triangleright \Sigma^{C}, \Sigma^{N}
                                      \vdash Nexp \leadsto ne
                                                                                                                                                                                      CHECK_EXP_AUX_VECTORGET
                            \overline{\Delta, E, E^{\mathsf{L}} \vdash exp.(Nexp) : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}} \cup \{ne\langle ne'\}\}}
                                                  \Delta, E, E^{L} \vdash exp : \_vector ne' t \triangleright \Sigma^{C}, \Sigma^{N}
                                                  \vdash Nexp_1 \leadsto ne_1
                                                  \vdash Nexp_2 \leadsto ne_2
                                                  ne = ne_2 + (-ne_1)
                                                                                                                                                                                                                                        CHECK_EXP_AUX_VECTORSUB
\overline{\Delta, E, E^{\text{\tiny{L}}} \vdash exp.(Nexp_1..Nexp_2) : \_\text{\textbf{vector}} \ ne \ t \vartriangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}} \ \cup \ \{ne_1 \langle ne_2 \langle ne' \} \}
                                          E \vdash id \mathbf{field}
                                          \Delta, E \vdash \mathbf{field}\ id : p\ t\_args \rightarrow t \triangleright (x\ \mathbf{of}\ names)
                                          \Delta, E, E^{\text{L}} \vdash exp : p \ t\_args \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}
                                                                                                                                                                                                CHECK_EXP_AUX_FIELD
                                                                 \Delta, E, E^{\text{L}} \vdash exp.id : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}
                                                                     \overline{\Delta,E,E^{\scriptscriptstyle L} \vdash \mathit{pat}_i : t \, \rhd \, E_i^{\scriptscriptstyle L}}^{\,\,i}
                                                                    \frac{-1}{\Delta, E, E^{L} \uplus E_{i}^{L} \vdash exp_{i} : u \rhd \Sigma^{C}_{i}, \Sigma^{N}_{i}}^{i}}{\Delta, E, E^{L} \vdash exp : t \rhd \Sigma^{C'}, \Sigma^{N'}}^{i}
\Delta, E, E^{\text{L}} \vdash \mathbf{match} \ \overline{exp} \ \overline{\mathbf{with}} \ |^{?} \ \overline{pat_{i} \rightarrow exp_{i} \ l_{i}}^{i} \ l \ \mathbf{end} : u \vartriangleright \Sigma^{\mathcal{C}'} \cup \ \overline{\Sigma^{\mathcal{C}}_{i}}^{i}, \Sigma^{\mathcal{N}'} \cup \ \overline{\Sigma^{\mathcal{N}_{i}}}^{i}  CHECK_EXP_AUX_CASE
                                                                   \Delta, E, E^{L} \vdash exp : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}
                                                                   \Delta, E \vdash typ \leadsto t
                                                        \frac{1}{\Delta, E, E^{\text{L}} \vdash (exp: typ): t \triangleright \Sigma^{\mathcal{C}}. \Sigma^{\mathcal{N}}} \quad \text{CHECK\_EXP\_AUX\_TYPED}
                                                            \begin{array}{l} \Delta, E, E_1^{\text{\tiny L}} \vdash letbind \, \rhd \, E_2^{\text{\tiny L}}, \Sigma^{\mathcal{C}}{}_1, \Sigma^{\mathcal{N}}{}_1 \\ \Delta, E, E_1^{\text{\tiny L}} \uplus \, E_2^{\text{\tiny L}} \vdash exp : t \, \rhd \, \Sigma^{\mathcal{C}}{}_2, \Sigma^{\mathcal{N}}{}_2 \end{array}
                         \frac{1}{\Delta,E,E_1^{\tt L} \vdash \mathbf{let} \ letbind \ \mathbf{in} \ exp: t \vartriangleright \Sigma^{\mathcal{C}}_1 \ \cup \ \Sigma^{\mathcal{C}}_2,\Sigma^{\mathcal{N}}_1 \ \cup \ \Sigma^{\mathcal{N}}_2} \quad \text{CHECK\_EXP\_AUX\_LET}
\frac{\Delta, E, E^{\text{\tiny L}} \vdash exp_1 : t_1 \rhd \Sigma^{\mathcal{C}}_1, \Sigma^{\mathcal{N}}_1 \quad \dots \quad \Delta, E, E^{\text{\tiny L}} \vdash exp_n : t_n \rhd \Sigma^{\mathcal{C}}_n, \Sigma^{\mathcal{N}}_n}{\Delta, E, E^{\text{\tiny L}} \vdash (exp_1, \, \dots, \, exp_n) : t_1 \ast \dots \ast t_n \rhd \Sigma^{\mathcal{C}}_1 \cup \dots \cup \Sigma^{\mathcal{C}}_n, \Sigma^{\mathcal{N}}_1 \cup \dots \cup \Sigma^{\mathcal{N}}_n}
                                                                                                                                                                                                                                                             CHECK_EXP_AUX_TUP
         \Delta \vdash t \mathbf{ok}
 \frac{\Delta, E, E^{\mathsf{L}} \vdash exp_1 : t \vartriangleright \Sigma^{\mathcal{C}}_1, \Sigma^{\mathcal{N}}_1 \quad .. \quad \Delta, E, E^{\mathsf{L}} \vdash exp_n : t \vartriangleright \Sigma^{\mathcal{C}}_n, \Sigma^{\mathcal{N}}_n}{\Delta, E, E^{\mathsf{L}} \vdash [exp_1; \, ..; exp_n \, ;^?] : \_\mathbf{list} \; t \vartriangleright \Sigma^{\mathcal{C}}_1 \cup ... \cup \Sigma^{\mathcal{C}}_n, \Sigma^{\mathcal{N}}_1 \cup ... \cup \Sigma^{\mathcal{N}}_n} \quad \text{CHECK\_EXP\_AUX\_LIST}
                                                                \frac{\Delta, E, E^{\mathsf{L}} \vdash exp : t \rhd \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}}{\Delta, E, E^{\mathsf{L}} \vdash (exp) : t \rhd \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}} \quad \text{CHECK\_EXP\_AUX\_PAREN}
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\frac{\Delta, E, E^{\mathsf{L}} \vdash \mathit{exp} : t \vartriangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}}{\Delta, E, E^{\mathsf{L}} \vdash \mathbf{begin} \, \mathit{exp} \, \mathbf{end} : t \vartriangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}}
                                                                                                                                                                                                                               CHECK_EXP_AUX_BEGIN
                                                                                          \begin{array}{l} \Delta, E, E^{\mathrm{L}} \vdash exp_{1} : \_\mathbf{bool} \rhd \Sigma^{\mathcal{C}}_{1}, \Sigma^{\mathcal{N}}_{1} \\ \Delta, E, E^{\mathrm{L}} \vdash exp_{2} : t \rhd \Sigma^{\mathcal{C}}_{2}, \Sigma^{\mathcal{N}}_{2} \end{array}
                                                                                          \Delta, E, E^{\mathrm{L}} \vdash exp_3 : t \triangleright \Sigma^{\mathcal{C}_3}, \Sigma^{\mathcal{N}_3}
\overline{\Delta, E, E^{\scriptscriptstyle L} \vdash \mathbf{if} \ exp_1 \, \mathbf{then} \ exp_2 \, \mathbf{else} \ exp_3 : t \, \triangleright \, \Sigma^{\mathcal{C}}_1 \, \cup \, \Sigma^{\mathcal{C}}_2 \, \cup \, \Sigma^{\mathcal{C}}_3, \Sigma^{\mathcal{N}}_1 \, \cup \, \Sigma^{\mathcal{N}}_2 \, \cup \, \Sigma^{\mathcal{N}}_3}
                                                                                                                                                                                                                                                                                                                                                CHECK_EXP_AUX_IF
                                                                         \Delta, E, E^{\mathrm{L}} \vdash exp_1 : t \triangleright \Sigma^{\mathcal{C}}_1, \Sigma^{\mathcal{N}}_1
                                                                        \Delta, E, E^{\text{\tiny L}} \vdash exp_2 : \_\textbf{list} \ t \ \triangleright \ \Sigma^{\mathcal{C}_2}, \Sigma^{\mathcal{N}_2}
                              \frac{1}{\Delta, E, E^{\text{\tiny L}} \vdash exp_1 :: exp_2 : \_\textbf{list} \ t \vartriangleright \Sigma^{\mathcal{C}}_1 \cup \Sigma^{\mathcal{C}}_2, \Sigma^{\mathcal{N}}_1 \cup \Sigma^{\mathcal{N}}_2}
                                                                                                \frac{\vdash lit:t}{\Delta,E,E^{\text{\tiny L}}\vdash lit:t\,\vartriangleright\,\{\,\},\{\,\}}\quad\text{CHECK\_EXP\_AUX\_LIT}
                                 \Delta \vdash t_i \mathbf{ok}^i
                                 \Delta, E, E^{\mathrm{L}} \uplus \{ \overline{x_i \mapsto t_i}^i \} \vdash exp_1 : t \rhd \Sigma^{\mathcal{C}}_1, \Sigma^{\mathcal{N}}_1
                                  \Delta, E, E^{L} \uplus \{ \overline{x_i \mapsto t_i}^i \} \vdash exp_2 : \_bool \triangleright \Sigma^{\mathcal{C}}_2, \Sigma^{\mathcal{N}}_2
                                 \mathbf{disjoint}\,\mathbf{doms}\,(E^{\scriptscriptstyle{\mathrm{L}}},\{\,\overline{x_i\mapsto t_i}^{\,i}\,\})
                                  E = \langle E^{\mathrm{M}}, E^{\mathrm{P}}, E^{\mathrm{F}}, E^{\mathrm{X}} \rangle
                                  x_i \not\in \mathbf{dom}(E^{\mathrm{X}})
                    \overline{\Delta, E, E^{\text{L}} \vdash \{exp_1 | exp_2\}} : \_\mathbf{set} \ t \rhd \Sigma^{\mathcal{C}}_1 \cup \Sigma^{\mathcal{C}}_2, \Sigma^{\mathcal{N}}_1 \cup \Sigma^{\mathcal{N}}_2}
                                                                                                                                                                                                                                                               CHECK_EXP_AUX_SET_COMP
\begin{array}{c} \Delta, E, E_{1}^{\text{L}} \vdash \overline{qbind_{i}}^{i} \triangleright E_{2}^{\text{L}}, \Sigma^{\mathcal{C}}_{1} \\ \Delta, E, E_{1}^{\text{L}} \uplus E_{2}^{\text{L}} \vdash exp_{1} : t \triangleright \Sigma^{\mathcal{C}}_{2}, \Sigma^{\mathcal{N}}_{2} \\ \Delta, E, E_{1}^{\text{L}} \uplus E_{2}^{\text{L}} \vdash exp_{2} : \_\textbf{bool} \ \triangleright \Sigma^{\mathcal{C}}_{3}, \Sigma^{\mathcal{N}}_{3} \\ \hline \Delta, E, E_{1}^{\text{L}} \vdash \{exp_{1} | \textbf{forall} \ \overline{qbind_{i}}^{i} | exp_{2}\} : \_\textbf{set} \ t \triangleright \Sigma^{\mathcal{C}}_{1} \cup \Sigma^{\mathcal{C}}_{2} \cup \Sigma^{\mathcal{C}}_{3}, \Sigma^{\mathcal{N}}_{2} \cup \Sigma^{\mathcal{N}}_{3} \end{array}
             \Delta \vdash t \mathbf{ok}
 \frac{\Delta, E, E^{\text{L}} \vdash exp_1 : t \vartriangleright \Sigma^{\mathcal{C}}_1, \Sigma^{\mathcal{N}}_1 \quad .. \quad \Delta, E, E^{\text{L}} \vdash exp_n : t \vartriangleright \Sigma^{\mathcal{C}}_n, \Sigma^{\mathcal{N}}_n}{\Delta, E, E^{\text{L}} \vdash \{exp_1; ...; exp_n; ?\} : \_\mathbf{set} \; t \vartriangleright \Sigma^{\mathcal{C}}_1 \cup ... \cup \Sigma^{\mathcal{C}}_n, \Sigma^{\mathcal{N}}_1 \cup ... \cup \Sigma^{\mathcal{N}}_n} \quad \text{CHECK\_EXP\_AUX\_SET}
                                  \frac{\Delta, E, E_{1}^{\text{L}} \vdash \overline{qbind_{i}}^{i} \triangleright E_{2}^{\text{L}}, \Sigma^{\mathcal{C}}_{1}}{\Delta, E, E_{1}^{\text{L}} \uplus E_{2}^{\text{L}} \vdash exp: \_bool \triangleright \Sigma^{\mathcal{C}}_{2}, \Sigma^{\mathcal{N}}_{2}} \xrightarrow{\text{CHECK\_EXP\_AUX\_QUANT}} \Delta, E, E_{1}^{\text{L}} \vdash q \overline{qbind_{i}}^{i} \cdot exp: \_bool \triangleright \Sigma^{\mathcal{C}}_{1} \cup \Sigma^{\mathcal{C}}_{2}, \Sigma^{\mathcal{N}}_{2}}
                                                                        \begin{array}{l} \Delta, E, E_1^{\text{\tiny L}} \vdash \textbf{list} \ \overline{qbind_i}^{\ i} \rhd E_2^{\text{\tiny L}}, \Sigma^{\mathcal{C}}_1 \\ \Delta, E, E_1^{\text{\tiny L}} \uplus E_2^{\text{\tiny L}} \vdash exp_1 : t \rhd \Sigma^{\mathcal{C}}_2, \Sigma^{\mathcal{N}}_2 \\ \Delta, E, E_1^{\text{\tiny L}} \uplus E_2^{\text{\tiny L}} \vdash exp_2 : \_\textbf{bool} \ \rhd \Sigma^{\mathcal{C}}_3, \Sigma^{\mathcal{N}}_3 \end{array}
                                                                                                                                                                                                                                                                                                                              CHECK_EXP_AUX_LIST_COMP_
\overline{\Delta, E, E_1^{\text{L}} \vdash [exp_1| \mathbf{forall} \overline{qbind_i}^i | exp_2] : \_\mathbf{list} \ t \rhd \Sigma^{\mathcal{C}}_1 \cup \Sigma^{\mathcal{C}}_2 \cup \Sigma^{\mathcal{C}}_3, \Sigma^{\mathcal{N}}_2 \cup \Sigma^{\mathcal{N}}_3}
    \Delta, E, E_1^{\text{L}} \vdash qbind_1 ... qbind_n \triangleright E_2^{\text{L}}, \Sigma^{\mathcal{C}} Build the environment for quantifier bindings, collecting typeclass cons
                                                                                                                                                                      CHECK\_LISTQUANT\_BINDING\_EMPTY
                                                                               \overline{\Delta, E, E^{\mathrm{L}} \vdash \triangleright \{\}, \{\}}
                                             \Delta \vdash t \mathbf{ok}
                                             \Delta, E, E_1^{\mathrm{L}} \uplus \{x \mapsto t\} \vdash \overline{qbind_i}^i \rhd E_2^{\mathrm{L}}, \Sigma^{\mathcal{C}}_1
                                            \mathbf{disjoint} \mathbf{doms} (\{x \mapsto \overline{t}\}, E_2^{\mathrm{L}})
                                       \frac{\text{disjoint doins}\left( \left\{ x \mapsto t \right\}, E_{2}^{\text{L}} \right)}{\Delta, E, E_{1}^{\text{L}} \vdash x \ l \ \overline{qbind_{i}}^{\ i} \ \rhd \left\{ x \mapsto t \right\} \uplus E_{2}^{\text{L}}, \Sigma^{\mathcal{C}}_{1}}
```

 $CHECK_LISTQUANT_BINDING_VAR$

```
\begin{array}{l} \Delta, E, E_1^{\text{L}} \vdash pat : t \vartriangleright E_3^{\text{L}} \\ \Delta, E, E_1^{\text{L}} \vdash exp : \_\mathbf{set} \ t \vartriangleright \Sigma^{\mathcal{C}}_1, \Sigma^{\mathcal{N}}_1 \end{array}
                                       \Delta, E, E_1^{\mathrm{L}} \uplus E_3^{\mathrm{L}} \vdash \overline{qbind_i}^i \rhd E_2^{\mathrm{L}}, \Sigma^{\mathcal{C}}_2
        \frac{\mathbf{disjoint} \, \mathbf{doms} \, (E_{3}^{\mathtt{L}}, E_{2}^{\mathtt{L}})}{\Delta, E, E_{1}^{\mathtt{L}} \vdash (\mathit{pat} \, \mathbf{IN} \, \mathit{exp}) \, \overline{\mathit{qbind}_{i}}^{i} \rhd E_{2}^{\mathtt{L}} \uplus E_{3}^{\mathtt{L}}, \Sigma^{\mathcal{C}}_{1} \, \cup \, \Sigma^{\mathcal{C}}_{2}}
                                                                                                                                                                                            CHECK\_LISTQUANT\_BINDING\_RESTR
                                   \begin{array}{l} \Delta, E, E_1^{\text{\tiny L}} \vdash pat : t \vartriangleright E_3^{\text{\tiny L}} \\ \Delta, E, E_1^{\text{\tiny L}} \vdash exp : \_\textbf{list} \ t \vartriangleright \Sigma^{\mathcal{C}}_1, \Sigma^{\mathcal{N}}_1 \end{array}
                                   \Delta, E, E_1^{\mathsf{L}} \uplus E_3^{\mathsf{L}} \vdash \overline{\mathit{qbind}_i}^i \rhd E_2^{\mathsf{L}}, \Sigma^{\mathcal{C}}_2
                                  disjoint doms (E_3^{\scriptscriptstyle 
m L},E_2^{\scriptscriptstyle 
m L})
\frac{\Delta E_3, E_2, E_3}{\Delta, E, E_1^{\text{L}} \vdash (pat \, \mathbf{MEM} \, exp) \, \overline{qbind_i}^i \, \triangleright \, E_2^{\text{L}} \uplus E_3^{\text{L}}, \Sigma^{\mathcal{C}}_1 \, \cup \, \Sigma^{\mathcal{C}}_2} \quad \text{Check_listquant_binding_list_restr}
   \Delta, E, E_1^{\text{L}} \vdash \text{list } qbind_1 ... qbind_n \triangleright E_2^{\text{L}}, \Sigma^{\mathcal{C}} Build the environment for quantifier bindings, collecting typeclass
                                                                                                                                                   CHECK\_QUANT\_BINDING\_EMPTY
                                                             \overline{\Delta, E, E^{\text{L}} \vdash \text{list} \triangleright \{\}, \{\}}
                                            \begin{array}{l} \Delta, E, E_{1}^{\text{\tiny L}} \vdash pat : t \vartriangleright E_{3}^{\text{\tiny L}} \\ \Delta, E, E_{1}^{\text{\tiny L}} \vdash exp : \_\textbf{list} \ t \vartriangleright \Sigma^{\mathcal{C}}_{1}, \Sigma^{\mathcal{N}}_{1} \end{array}
                                             \Delta, E, E_1^{\rm L} \uplus E_3^{\rm L} \vdash \overline{qbind_i}^i \rhd E_2^{\rm L}, \Sigma^{\mathcal{C}}_2
                                            disjoint doms (E_3^{\scriptscriptstyle 
m L},E_2^{\scriptscriptstyle 
m L})
  \frac{\Box}{\Delta, E, E_1^{\text{L}} \vdash \ \textbf{list} \ (pat \ \textbf{MEM} \ exp) \ \overline{qbind_i}^{\ i} \ \rhd \ E_2^{\text{L}} \uplus E_3^{\text{L}}, \Sigma^{\mathcal{C}}_1 \ \cup \ \Sigma^{\mathcal{C}}_2} \\ } \quad \text{CHECK\_QUANT\_BINDING\_RESTR}
   \Delta, E, E^{\text{L}} \vdash funcl \rhd \{x \mapsto t\}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}
                                                                                                                             Build the environment for a function definition clause, collecting typec
                                        \begin{array}{lll} \Delta, E, E^{\mathrm{L}} \vdash pat_{1} : t_{1} \rhd E_{1}^{\mathrm{L}} & \dots & \Delta, E, E^{\mathrm{L}} \vdash pat_{n} : t_{n} \rhd E_{n}^{\mathrm{L}} \\ \Delta, E, E^{\mathrm{L}} \uplus E_{1}^{\mathrm{L}} \uplus & \dots & \uplus E_{n}^{\mathrm{L}} \vdash exp : u \rhd \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}} \end{array}
                                       disjoint doms (E_1^{\text{L}}, \dots, E_n^{\text{L}})
                                        \Delta, E \vdash typ \leadsto u
\frac{-}{\Delta, E, E^{\mathsf{L}} \vdash x \ l_1 \ pat_1 \dots pat_n : typ = exp \ l_2 \triangleright \{x \mapsto \mathbf{curry} \ ((t_1 * \dots * t_n), u)\}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}}{} CHECK_FUNCL_ANNOT
                               \begin{array}{l} \Delta, E, E^{\mathsf{L}} \vdash \mathit{pat}_1 : t_1 \rhd E_1^{\mathsf{L}} \quad \dots \quad \Delta, E, E^{\mathsf{L}} \vdash \mathit{pat}_n : t_n \rhd E_n^{\mathsf{L}} \\ \Delta, E, E^{\mathsf{L}} \uplus E_1^{\mathsf{L}} \uplus \ \dots \ \uplus E_n^{\mathsf{L}} \vdash \mathit{exp} : u \rhd \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}} \end{array}
                               disjoint doms (E_1^{\text{L}}, \dots, E_n^{\text{L}})
\overline{\Delta, E, E^{\text{L}} \vdash x \ l_1 \ pat_1 \dots pat_n = exp \ l_2 \triangleright \{x \mapsto \mathbf{curry} \ ((t_1 * \dots * t_n), u)\}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}} \quad \text{CHECK\_FUNCL\_NOANNOT}
   \Delta, E, E_1^{\text{L}} \vdash letbind \triangleright E_2^{\text{L}}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}} Build the environment for a let binding, collecting typeclass and index con
                                                            \begin{array}{l} \Delta, E, E_1^{\text{L}} \vdash pat : t \vartriangleright E_2^{\text{L}} \\ \Delta, E, E_1^{\text{L}} \vdash exp : t \vartriangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}} \end{array}
                                                             \Delta, E \vdash typ \leadsto t
                                       \frac{\Delta, E + egp + v}{\Delta, E, E_1^{\mathsf{L}} \vdash pat : typ = exp \ l \rhd E_2^{\mathsf{L}}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}}
                                                                                                                                                                                 CHECK_LETBIND_VAL_ANNOT
                                          \begin{array}{c} \Delta, E, E_{1}^{\text{L}} \vdash pat : t \vartriangleright E_{2}^{\text{L}} \\ \Delta, E, E_{1}^{\text{L}} \vdash exp : t \vartriangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}} \\ \hline \Delta, E, E_{1}^{\text{L}} \vdash pat = exp \ l \vartriangleright E_{2}^{\text{L}}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}} \end{array}
                                                                                                                                                                   CHECK_LETBIND_VAL_NOANNOT
                                                   \frac{\Delta, E, E_1^{\text{L}} \vdash funcl\_aux \ l \rhd \{x \mapsto t\}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}}{\Delta, E, E_1^{\text{L}} \vdash funcl\_aux \ l \rhd \{x \mapsto t\}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}} \quad \text{CHECK\_LETBIND\_FN}
     \Delta, E, E^{\mathrm{L}} \vdash rule \triangleright \{x \mapsto t\}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}
                                                                                                                            Build the environment for an inductive relation clause, collecting typed
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\overline{\Delta \vdash t_i \, \mathbf{ok}}^i
                                                                                    E_2^{\mathrm{L}} = \{ \overline{name_- t_i \to x \mapsto t_i}^i \}
\begin{array}{c} \Delta, E, E_{1}^{\text{L}} \uplus E_{2}^{\text{L}} \vdash exp' : \_\textbf{bool} \quad \triangleright \Sigma^{\mathcal{C}'}, \Sigma^{\mathcal{N}'} \\ \Delta, E, E_{1}^{\text{L}} \uplus E_{2}^{\text{L}} \vdash exp_{1} : u_{1} \triangleright \Sigma^{\mathcal{C}}_{1}, \Sigma^{\mathcal{N}}_{1} \quad ... \quad \Delta, E, E_{1}^{\text{L}} \uplus E_{2}^{\text{L}} \vdash exp_{n} : u_{n} \triangleright \Sigma^{\mathcal{C}}_{n}, \Sigma^{\mathcal{N}}_{n} \\ \overline{\Delta, E, E_{1}^{\text{L}} \vdash x_{1}^{l} : \textbf{ forall } \overline{name\_t_{i}}^{i} . exp' \Longrightarrow x \ l \ exp_{1} ... \ exp_{n} \ l' \triangleright \{x \mapsto \textbf{curry} \left( (u_{1} * ... * u_{n}), \_\textbf{-bool} \right) \}, \Sigma^{\mathcal{C}'} \cup \Sigma^{\mathcal{C}}_{1} \cup \mathbb{C}^{\mathcal{C}}_{n} \\ \end{array}
     xs, \Delta_1, E \vdash \mathbf{tc} \ td \triangleright \Delta_2, E^{\mathrm{P}}
                                                                                     Extract the type constructor information
                                                              tnvars^l \leadsto tnvs
                                                              \Delta, E \vdash typ \leadsto t
                                                              \mathbf{duplicates}\left(tnvs\right) = \emptyset
                                                              \mathbf{FV}(t) \subset tnvs
                                                              \overline{y_i}. i \ x \not\in \mathbf{dom}(\Delta)
                                                                                                                                                                                    CHECK_TEXP_TC_ABBREV
     \overline{\overline{y_i}^i, \Delta, E \vdash \mathbf{tc} \ x \ l \ tnvars^l = typ \triangleright \{\overline{y_i.}^i \ x \mapsto tnvs \ .t\}, \{x \mapsto \overline{y_i.}^i \ x\}}
                                                           tnvars^l \leadsto tnvs
                                                           \mathbf{duplicates}\left(tnvs\right) = \emptyset
                                                           \overline{y_i} x \notin \mathbf{dom}(\Delta)
            \overline{\overline{y_i}^i, \Delta, E_1 \vdash \mathbf{tc} \ x \ l \ tnvars^l \triangleright \{\overline{y_i}^i \ x \mapsto tnvs \}, \{x \mapsto \overline{y_i}^i \ x\}}
                                                                                                                                                                        CHECK_TEXP_TC_ABSTRACT
                                                                                     tnvars^l \leadsto tnvs
                                                                                     \mathbf{duplicates}(tnvs) = \emptyset
                                                                                     \overline{y_i} x \notin \mathbf{dom}(\Delta)
\frac{\overline{y_i \cdot x_j - x_j}}{\overline{y_i \cdot x_j}} = \langle |x_1^l : typ_1; \dots; x_j^l : typ_j; ?| \rangle \triangleright \{\overline{y_i \cdot x_j} + tnvs\}, \{x \mapsto \overline{y_i \cdot x_j}\}
                                                                                                                                                                                                                                         CHECK_TEXP_TC_REC
                                                                                  tnvars^l \leadsto tnvs
                                                                                   \mathbf{duplicates}(tnvs) = \emptyset
                                                                                   \overline{y_i} x \notin \mathbf{dom}(\Delta)
\overline{\overline{y_i}^i, \Delta_1, E \vdash \mathbf{tc} \ x \ l \ tnvars^l \ = |? \ ctor\_def_1| \dots | ctor\_def_j \ \rhd \ \{\overline{y_i.}^i \ x \mapsto tnvs \ \}, \{x \mapsto \overline{y_i.}^i \ x\}
     xs, \Delta_1, E \vdash \mathbf{tc} td_1 ... td_i \triangleright \Delta_2, E^{P} Extract the type constructor information
                                                             \overline{xs, \Delta, E \vdash \mathbf{tc} \triangleright \{\}, \{\}} \quad \text{CHECK\_TEXPS\_TC\_EMPTY}
                      xs, \Delta_1, E \vdash \mathbf{tc} \ td \triangleright \Delta_2, E_2^{\mathrm{P}}
                     \begin{array}{l} xs, \Delta_1 \uplus \Delta_2, E \uplus \langle \{\,\}, E_2^{\scriptscriptstyle \mathrm{P}}, \{\,\}, \{\,\} \rangle \vdash \mathbf{tc} \, \overline{td_i}^{\,i} \rhd \Delta_3, E_3^{\scriptscriptstyle \mathrm{P}} \\ \mathbf{dom} \, (E_2^{\scriptscriptstyle \mathrm{P}}) \, \cap \, \mathbf{dom} \, (\underline{E}_3^{\scriptscriptstyle \mathrm{P}}) = \emptyset \end{array}
                                   xs, \Delta_1, E \vdash \mathbf{tc} \ td \ \overline{td_i}^i \rhd \Delta_2 \uplus \Delta_3, E_2^{\mathrm{P}} \uplus E_3^{\mathrm{P}}
                                                                                                                                                                        CHECK_TEXPS_TC_ABBREV
      \Delta, E \vdash tnvs \ p = texp \triangleright \langle E^{F}, E^{X} \rangle Check a type definition, with its path already resolved
                                                                                                                                            CHECK_TEXP_ABBREV
                                                        \overline{\Delta, E \vdash tnvs \ p = typ \, \triangleright \, \langle \{\,\}, \{\,\} \rangle}
                                     \Delta, E \vdash typ_i \leadsto t_i
                                     names = \{ \overline{x_i}^i \}
                                     \mathbf{duplicates}\left(\overline{x_{i}}^{i}\right) = \emptyset
                                     \overline{\mathbf{FV}(t_i) \subset tnvs}
                                    E^{\mathrm{F}} = \{ \overline{x_i \mapsto \langle \mathbf{forall} \ tnvs.p \rightarrow t_i, (x_i \mathbf{of} \ names) \rangle^i} \}  CHECK_TEXP_REC
                                              \Delta, E \vdash tnvs \ p = \langle | \ \overline{x_i^l : typ_i}^i ; ? | \rangle \rhd \langle E^F, \{ \} \rangle
```

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\overline{\Delta, E \vdash typs_i \leadsto t\_multi_i}^i
                              names = \{ \overline{x_i}^i \}
                              \mathbf{duplicates}\left(\,\overline{x_i}^{\,i}\,\right) = \emptyset
                             \overline{\mathbf{FV}(t_{-}multi_{i})} \subset tnvs^{i}
                              E^{X} = \{ \overline{x_i \mapsto \langle \mathbf{forall} \ tnvs.t_{-}multi_i \rightarrow p, (x_i \mathbf{of} \ names) \rangle}^i \}
                                                                                                                                                                                                               CHECK_TEXP_VAR
                                                   \Delta, E \vdash tnvs \ p = |? \overline{x_i^l \text{ of } typs_i}^i \rhd \langle \{ \}, E^{\mathbf{X}} \rangle
   xs, \Delta, E \vdash td_1 ... td_n \triangleright \langle E^{\scriptscriptstyle F}, E^{\scriptscriptstyle X} \rangle
                                                                                                                                              CHECK_TEXPS_EMPTY
                                                                          \overline{y_i}^i, \Delta, E \vdash \triangleright \langle \{ \}, \{ \} \rangle
                                     tnvars^l \leadsto tnvs
                                     \Delta, E_1 \vdash tnvs \overline{y_i}.^i x = texp \triangleright \langle E_1^F, E_1^X \rangle
                                    \begin{array}{l} \overline{y_i}^{\,i}, \Delta, E \vdash \overline{td_j}^{\,j} \, \rhd \, \langle E_2^{\scriptscriptstyle \mathrm{F}}, E_2^{\scriptscriptstyle \mathrm{X}} \rangle \\ \mathbf{dom} \, (E_1^{\scriptscriptstyle \mathrm{X}}) \, \cap \, \mathbf{dom} \, (E_2^{\scriptscriptstyle \mathrm{X}}) = \emptyset \\ \mathbf{dom} \, (E_1^{\scriptscriptstyle \mathrm{F}}) \, \cap \, \mathbf{dom} \, (E_2^{\scriptscriptstyle \mathrm{F}}) = \emptyset \end{array}
                                                                                                                                                                                  CHECK_TEXPS_CONS_CONCRETE
       \overline{y_i}^{\;i}, \Delta, \overline{E \vdash x \; l \; tnvars^l \; = \; texp \; \overline{td_j}^{\;j} \; \rhd \; \langle E_1^{\scriptscriptstyle \mathrm{F}} \uplus E_2^{\scriptscriptstyle \mathrm{F}}, E_1^{\scriptscriptstyle \mathrm{X}} \uplus E_2^{\scriptscriptstyle \mathrm{X}} \rangle}
                                   \frac{\overline{y_i}^i, \Delta, E \vdash \overline{td_j}^j \, \triangleright \, \langle E^{\scriptscriptstyle F}, E^{\scriptscriptstyle X} \rangle}{\overline{y_i}^i, \Delta, E \vdash x \, l \, tnvars^l \, \, \overline{td_j}^j \, \triangleright \, \langle E^{\scriptscriptstyle F}, E^{\scriptscriptstyle X} \rangle} \quad \text{CHECK\_TEXPS\_CONS\_ABSTRACT}
   \delta, E \vdash id \leadsto p Lookup a type class
                                                                                              E(id) \triangleright p
                                                                                        \frac{\delta(p) \triangleright xs}{\delta, E \vdash id \leadsto p} \quad \text{CONVERT\_CLASS\_ALL}
   I \vdash (p \ t) \mathbf{IN} \, \mathcal{C}
                                                       Solve class constraint
                                                                                                                                                                           SOLVE_CLASS_CONSTRAINT_IMMEDIATE
\overline{I \vdash (p \alpha) \mathbf{IN} (p_1 tnv_1) ... (p_i tnv_i) (p \alpha) (p'_1 tnv'_1) ... (p'_i tnv'_j)}
                  (p_1 tnv_1) ... (p_n tnv_n) \Rightarrow (p t) \mathbf{IN} I
                 \frac{I \vdash (p_1 \sigma(tnv_1)) \mathbf{IN} \mathcal{C} \quad .. \quad I \vdash (p_n \sigma(tnv_n)) \mathbf{IN} \mathcal{C}}{I \vdash (p \sigma(t)) \mathbf{IN} \mathcal{C}}
                                                                                                                                                                      SOLVE_CLASS_CONSTRAINT_CHAIN
   I \vdash \Sigma^{\mathcal{C}} \triangleright \mathcal{C}
                                               Solve class constraints
                                 \frac{I \vdash (p_1 \ t_1) \ \mathbf{IN} \ \mathcal{C} \quad .. \quad I \vdash (p_n \ t_n) \ \mathbf{IN} \ \mathcal{C}}{I \vdash \{(p_1 \ t_1), \dots, (p_n \ t_n)\} \triangleright \mathcal{C}} \quad \text{SOLVE\_CLASS\_CONSTRAINTS\_ALL}
    \Delta, I, E \vdash val\_def \triangleright E^{x} Check a value definition
                                               \Delta, E, \{\} \vdash letbind \triangleright \{\overline{x_i \mapsto t_i}^i\}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}

I \vdash \Sigma^{\mathcal{C}} \triangleright \mathcal{C}
                                               \overline{\mathbf{FV}\left(t_{i}\right)} \subset \mathit{tnvs}^{i}
                                                \mathbf{FV}\left(\mathcal{C}\right) \subset \mathit{tnvs}
                                                                                                                                                                                                            CHECK_VAL_DEF_VAL
                   \overline{\Delta, I, E_1 \vdash \mathbf{let} \, \tau^? \, letbind} \, \triangleright \, \{ \, \overline{x_i \mapsto \langle \, \mathbf{forall} \, tnvs. \mathcal{C} \Rightarrow t_i, \mathbf{let} \rangle}^{\, i} \, \}
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\overline{\Delta, E, E^{\text{L}} \vdash funcl_i \triangleright \{x_i \mapsto t_i\}, \Sigma^{\mathcal{C}}_i, \Sigma^{\mathcal{N}}_i}^i
                                               I \vdash \Sigma^{\mathcal{C}} \triangleright \mathcal{C}
                                              \overline{\mathbf{FV}\left(t_{i}\right)} \subset \mathit{tnvs}^{i}
                                              \mathbf{FV}\left(\mathcal{C}\right) \subset \mathit{tnvs}
                                              \mathbf{compatible}\,\mathbf{overlap}\,(\,\overline{x_i\mapsto t_i}^{\,i}\,)
                                              E^{L} = \{ \overline{x_i \mapsto t_i}^i \}
            \frac{\mathcal{L} - \{\omega_{i} + r \cdot v_{i}\}}{\Delta, I, E \vdash \mathbf{let} \operatorname{rec} \tau^{?} \overline{funcl_{i}}^{i} \rhd \{\overline{x_{i} \mapsto \langle \operatorname{\mathbf{forall}} tnvs. \mathcal{C} \Rightarrow t_{i}, \operatorname{\mathbf{let}} \rangle}^{i}\}}
                                                                                                                                                                                                                      CHECK_VAL_DEF_RECFUN
       \Delta, (\alpha_1, ..., \alpha_n) \vdash t  instance
                                                                                                       Check that t be a typeclass instance
                                                                                                                                                   CHECK\_T\_INSTANCE\_VAR
                                                                               \overline{\Delta}. (\alpha) \vdash \alpha instance
                                                                                                                                                                                    CHECK\_T\_INSTANCE\_TUP
                                               \overline{\Delta,(\alpha_1,\ldots,\alpha_n)\vdash\alpha_1*\ldots*\alpha_n} instance
                                                                                                                                                                    CHECK_T_INSTANCE_FN
                                                              \overline{\Delta,(\alpha_1,\alpha_2)\vdash\alpha_1\to\alpha_n\ \mathbf{instance}}
                                                         \frac{\Delta(p) \vartriangleright \alpha_1' \mathinner{\ldotp\ldotp} \alpha_n'}{\Delta, (\alpha_1, \mathinner{\ldotp\ldotp\ldotp}, \alpha_n) \vdash p \alpha_1 \mathinner{\ldotp\ldotp} \alpha_n \, \mathbf{instance}} \quad \text{Check\_tlinstance\_tc}
      \overline{z_j}^j, D_1, E_1 \vdash def \triangleright D_2, E_2 Check a definition
                                        \overline{z_i}^j, \Delta_1, E \vdash \mathbf{tc} \overline{td_i}^i \triangleright \Delta_2, E^{\mathrm{P}}
                       \frac{\overline{z_{j}}^{j}, \Delta_{1} \uplus \Delta_{2}, E \uplus \langle \{\}, E^{\mathrm{P}}, \{\}, \{\} \rangle \vdash \overline{td_{i}}^{i} \rhd \langle E^{\mathrm{F}}, E^{\mathrm{X}} \rangle}{\overline{z_{j}}^{j}, \langle \Delta_{1}, \delta, I \rangle, E \vdash \mathbf{type} \, \overline{td_{i}}^{i} \, l \rhd \langle \Delta_{2}, \{\}, \{\} \rangle, \langle \{\}, E^{\mathrm{P}}, E^{\mathrm{F}}, E^{\mathrm{X}} \rangle} \quad \text{CHECK_DEF_TYPE}
                                                                                \Delta, I, E \vdash val\_def \, \rhd \, E^{\scriptscriptstyle \mathrm{X}}
                                         \frac{-1}{z_i^{j}}, \langle \Delta, \delta, I \rangle, E \vdash val\_def \ l \triangleright \epsilon, \langle \{ \}, \{ \}, \{ \}, E^{\mathbf{x}} \rangle CHECK_DEF_VAL_DEF
                                                                                                                                           \overline{\Delta, E_1, E^{\scriptscriptstyle L} \vdash rule_i \, \triangleright \, \{x_i \mapsto t_i\}, \Sigma^{\mathcal{C}}{}_i, \Sigma^{\mathcal{N}}{}_i}^i
                                                                                                                                           \frac{I \vdash \overline{\Sigma^{C}_{i}}^{i} \triangleright C}{\mathbf{FV}(t_{i}) \subset tnvs}^{i}
                                                                                                                                            \mathbf{FV}\left(\mathcal{C}\right) \subset \mathit{tnvs}
                                                                                                                                           \mathbf{compatible}\,\mathbf{overlap}\,(\,\overline{x_i\mapsto t_i}^{\,i}\,)
                                                                                                                                            E^{L} = \{ \overline{x_i \mapsto t_i}^i \}
E_2 = \langle \{ \}, \{ \}, \{ \}, \{ \overline{x_i \mapsto \langle \mathbf{forall} \ tnvs. \mathcal{C} \Rightarrow t_i, \mathbf{let} \rangle}^i \} \rangle <<no parses (char 59): </zj//j/>,<TD,TC,I>,E1 |- indreln targets_opt indreln_names*** </rule
\frac{\overline{z_j}^{\,j}\,x,D_1,E_1\vdash defs \, \triangleright \, D_2,E_2}{\overline{z_j}^{\,j}\,,D_1,E_1\vdash \mathbf{module}\,x\,l_1 = \, \mathbf{struct}\, defs\, \mathbf{end}\, l_2 \, \triangleright \, D_2, \langle \{x\mapsto E_2\},\{\,\},\{\,\},\{\,\}\rangle}
                                                                                                                                                                                                                                                   CHECK_DEF_MODULE
        \frac{E_1(id) \triangleright E_2}{\overline{z_j}^j, D, E_1 \vdash \mathbf{module} \ x \ l_1 = id \ l_2 \triangleright \epsilon, \langle \{x \mapsto E_2\}, \{\}, \{\}, \{\}, \} \rangle}
                                                                                                                                                                                                        CHECK\_DEF\_MODULE\_RENAME
                                    \Delta, E \vdash typ \leadsto t
                                  \mathbf{FV}(t) \subset \overline{\alpha_i}^i
\mathbf{FV}(\overline{\alpha_k'}^k) \subset \overline{\alpha_i}^i
\delta, E \vdash id_k \leadsto p_k^k
                 \frac{E' = \langle \{\}, \{\}, \{\}, \{x \mapsto \langle \operatorname{\mathbf{forall}} \overline{\alpha_i}^i. \overline{(p_k \alpha_k')}^k \Rightarrow t, \operatorname{\mathbf{val}} \rangle \} \rangle}{\overline{z_j}^j, \langle \Delta, \delta, I \rangle, E \vdash \operatorname{\mathbf{val}} x \ l_1 : \operatorname{\mathbf{forall}} \overline{\alpha_i} \overline{l_i''}^i. \overline{id_k \alpha_k' l_k'}^k \Rightarrow typ \ l_2 \rhd \epsilon, E'} \quad \text{CHECK_DEF_SPEC}
```

$$\begin{array}{c} \overline{\Delta,E_1 \vdash typ_i \leadsto t_i}^i \\ \hline \mathbf{FV}(t_i) \subset \alpha^i \\ p = \overline{z_j}^{-j} x \\ E_2 = \langle \{\}, \{x \mapsto p\}, \{\}, \{\overline{y_i \mapsto \langle \mathbf{forall} \alpha.(p \, \alpha) \Rightarrow t_i, \mathbf{method} \rangle}^i \} \rangle \\ \delta_2 = \{p \mapsto \overline{y_i}^i\} \\ p \not \in \mathbf{dom}(\delta_1) \\ \hline \\ \overline{z_j}^j, \langle \Delta, \delta_1, I \rangle, E_1 \vdash \mathbf{class}(x \, l \, \alpha \, l'') \, \overline{\mathbf{val} \, y_i \, l_i} : typ_i \, \overline{l_i}^i \, \mathbf{end} \, l' \, \triangleright \, \langle \{\}, \delta_2, \{\} \rangle, E_2 \\ \hline \\ E = \langle E^{\mathsf{M}}, E^{\mathsf{P}}, E^{\mathsf{F}}, E^{\mathsf{N}} \rangle \\ \Delta, E \vdash typ' \leadsto t' \\ \Delta, (\overline{\alpha_i}^i) \vdash t' \, \mathbf{instance} \\ twus = \overline{\alpha_i}^i \\ \mathbf{duplicates}(tnvs) = \emptyset \\ \overline{\delta, E \vdash id_k \leadsto p_k}^k \\ \hline \\ \mathbf{FV}(\overline{\alpha_k'}^k) \subset tnvs \\ E(id) \triangleright p \\ \delta(p) \triangleright \overline{z_j}^j \\ \underline{I_2} = \{ \overline{\Rightarrow (p_k \, \alpha_k')^k} \} \\ \overline{\Delta, I \cup I_2, E \vdash val.def_n \triangleright E_n^{\mathsf{N}}^n} \\ \mathbf{disjoint} \, \mathbf{doms}(\overline{E_n^{\mathsf{N}}}^n) \\ \hline \\ E^{\mathsf{X}}(x_k) \triangleright \langle \mathbf{forall} \, tnvs. \Rightarrow \{\alpha'' \mapsto t'\}(t_k), \mathbf{let} \rangle^k \} = \overline{E_n}^n \\ \overline{x_k} \models \overline{z_j}^j \\ \underline{I_3} = \{ (\overline{p_k} \, \alpha_k') \Rightarrow (p \, t')^k \} \\ (p \, \{\alpha_i \mapsto \alpha_i''^i\}(t')) \not \in I \\ \hline \overline{z_j}^j, \langle \Delta, \delta, I \rangle, E \vdash \mathbf{instance} \, \mathbf{forall} \, \overline{\alpha_i'}^i \, i.d_k \, \alpha_k' \, \overline{y_i''}^k \Rightarrow (id \, typ') \, \overline{val_def_n \, l_n}^n \, \mathbf{end} \, t' \triangleright \langle \{\}, \{\}, I_3 \rangle, \epsilon \\ \end{array} \right.$$

 $\overline{z_j}^j$, D_1 , $E_1 \vdash defs \triangleright D_2$, E_2 Check definitions, given module path, definitions and environment

Definition rules: 141 good 4 bad Definition rule clauses: 435 good 4 bad